Advanced Gatistics - Interial 20/01/2022

Chapities on variances of named distributions

Section 1: One set of i.i.d. variables

det $n \in \mathbb{N}$ and let $X_1,..., X_n$ be independent, $W(\mu, \sigma^2)$ - distributed under P_{μ_1,σ^2} , where $\mu \in \mathbb{R}$, $\sigma^2 > 0$.

Soal: Find fest night ingripicance level a / conjedence level 1-d for the following hyprophyses:

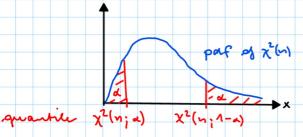
Ideo: lampare empirical variance to o.

lase 1: Brown mean p, i.e. p= po - rather theoretical case

· Empirical variance is
$$V = \frac{1}{n} \cdot \sum_{i=1}^{n} (X_i - \mu_0)^2$$

· Just statistic in
$$\frac{V}{G_{*}^{2}}$$

·
$$\frac{N}{G^2}$$
 V has $\chi^2(N)$ distribution under P_{μ_0,G^2}



· Regions of rejection for hypothesis Acts:

lase 2: Unknown mean pr, i.e. p. ER > Agrical case in applications

· Compinied mean is
$$M = \frac{1}{n} \sum_{i=1}^{n} X_{i}$$

· Empirical variance is
$$V^* = \frac{1}{n-1} \sum_{i=1}^{n} (X_i - M_i)^2$$

· Just Manistic is
$$\frac{V^{\times}}{6^2}$$

- · \frac{n-1}{62} V* has \chi^2 (n-1) distribution under P_{\mu,62}
- · Regions of rejection for hypothesis kerts:

Section 2: Two sets of i.i.d. variables

Let m, n E N, let X1,1, ..., X1, m; X2,1, ..., X2, be independent, and let

X 1,1,..., X1,m be N (m, 52) - distributed

X2,1,..., X2, be W(p2,02) - distributed

under Pra, 52; p2, 62, where p, 1 p2 ER, 62, 62 > 0.

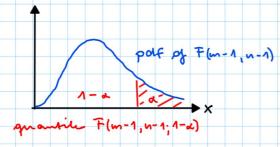
Soal: Find a tex for the following hypothesis:

3) Ho: o1 = o1; H1: o1 > o2

Idec: lonpare empirical variances of both ramples

Norme means pro, pre to be muleroun.

- · det V1 , V2 empirical variances of X1,1,..., X1, m, X2,1,..., X2,1
- · Jut Maristic is Vit .
- · $\frac{G_{2}^{2}}{G_{1}^{2}} \cdot \frac{V_{1}^{2}}{V_{2}^{2}}$ has $\mp (m-1, n-1)$ distribution under $P_{m_{1}G_{1}^{2}; p_{2}, G_{2}^{2}}$



· Region of rejection for hypothesis her :