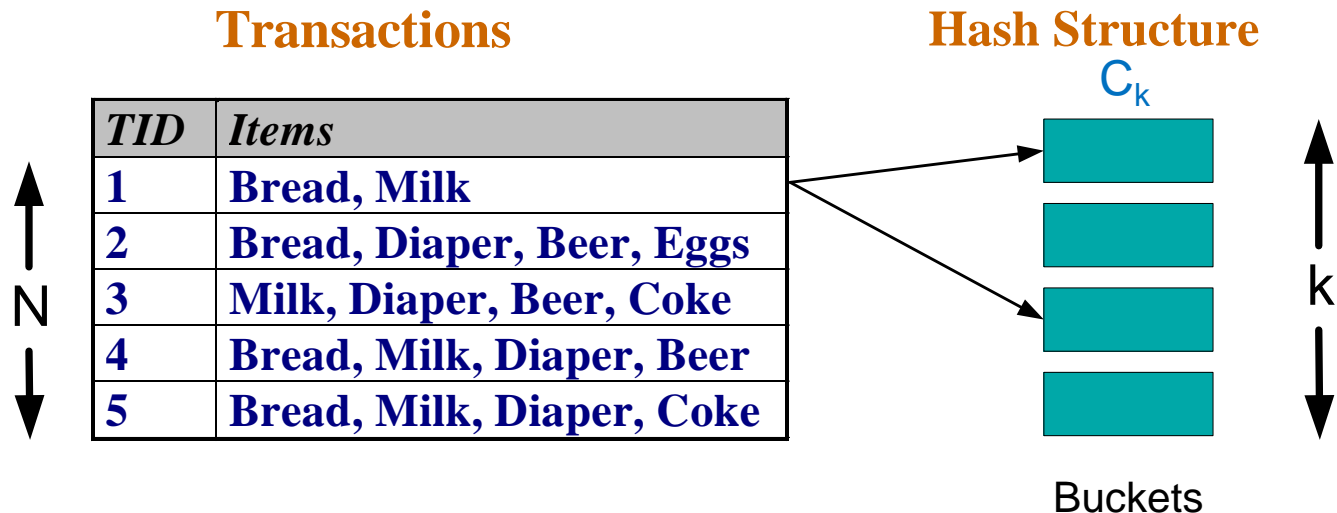


# Computing Frequent Itemsets

- Given the set of **candidate** itemsets  $C_k$ , we need to compute the support and find the **frequent** itemsets  $L_k$ .
- Scan the data, and use a **hash structure** to keep a counter for each candidate itemset that appears in the data



# A simple hash structure

- Create a dictionary (hash table) that stores the candidate itemsets as keys, and the number of appearances as the value.
- Increment the counter for each itemset that you see in the

# Example

Suppose you have 15 candidate itemsets of length 3:

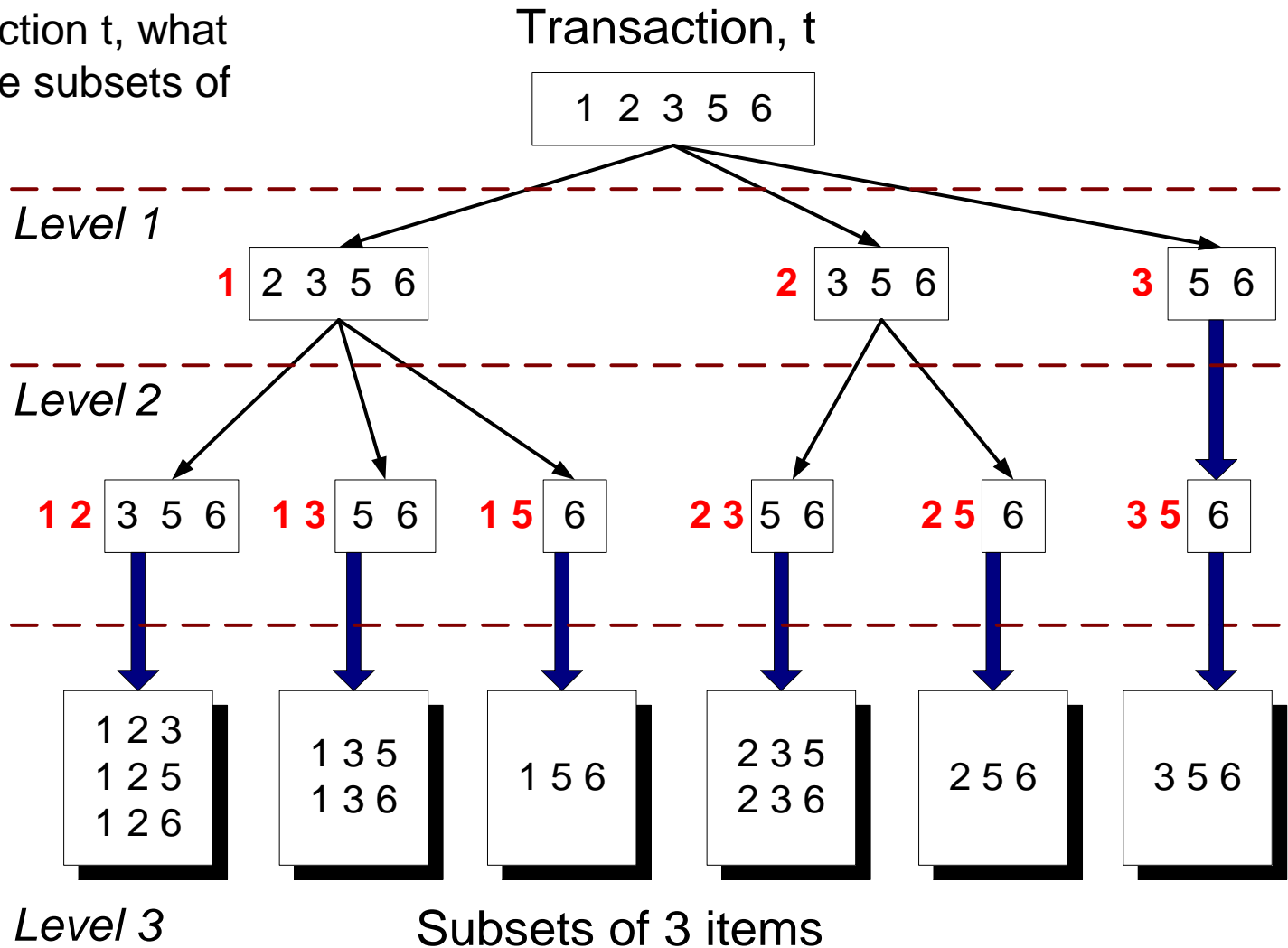
{1 4 5}, {1 2 4}, {4 5 7}, {1 2 5}, {4 5 8},  
{1 5 9}, {1 3 6}, {2 3 4}, {5 6 7}, {3 4 5},  
{3 5 6}, {3 5 7}, {6 8 9}, {3 6 7}, {3 6 8}

Hash table stores the counts of the candidate itemsets as they have been computed so far

| Key     | Value |
|---------|-------|
| {3 6 7} | 0     |
| {3 4 5} | 1     |
| {1 3 6} | 3     |
| {1 4 5} | 5     |
| {2 3 4} | 2     |
| {1 5 9} | 1     |
| {3 6 8} | 0     |
| {4 5 7} | 2     |
| {6 8 9} | 0     |
| {5 6 7} | 3     |
| {1 2 4} | 8     |
| {3 5 7} | 1     |
| {1 2 5} | 0     |
| {3 5 6} | 1     |
| {4 5 8} | 0     |

# Subset Generation

Given a transaction  $t$ , what are the possible subsets of size 3?



Recursion!

# Example

Tuple {1,2,3,5,6} generates the following itemsets of length 3:

{1 2 3}, {1 2 5}, {1 2 6}, {1 3 5}, {1 3 6},  
{1 5 6}, {2 3 5}, {2 3 6}, {3 5 6},

Increment the counters for the itemsets in the dictionary

| Key     | Value |
|---------|-------|
| {3 6 7} | 0     |
| {3 4 5} | 1     |
| {1 3 6} | 3     |
| {1 4 5} | 5     |
| {2 3 4} | 2     |
| {1 5 9} | 1     |
| {3 6 8} | 0     |
| {4 5 7} | 2     |
| {6 8 9} | 0     |
| {5 6 7} | 3     |
| {1 2 4} | 8     |
| {3 5 7} | 1     |
| {1 2 5} | 0     |
| {3 5 6} | 1     |
| {4 5 8} | 0     |

# Example

Tuple {1,2,3,5,6} generates the following itemsets of length 3:

{1 2 3}, {1 2 5}, {1 2 6}, {1 3 5}, {1 3 6},  
{1 5 6}, {2 3 5}, {2 3 6}, {3 5 6},

Increment the counters for the itemsets in the dictionary

| Key     | Value |
|---------|-------|
| {3 6 7} | 0     |
| {3 4 5} | 1     |
| {1 3 6} | 4     |
| {1 4 5} | 5     |
| {2 3 4} | 2     |
| {1 5 9} | 1     |
| {3 6 8} | 0     |
| {4 5 7} | 2     |
| {6 8 9} | 0     |
| {5 6 7} | 3     |
| {1 2 4} | 8     |
| {3 5 7} | 1     |
| {1 2 5} | 1     |
| {3 5 6} | 2     |
| {4 5 8} | 0     |

# The Hash Tree Structure

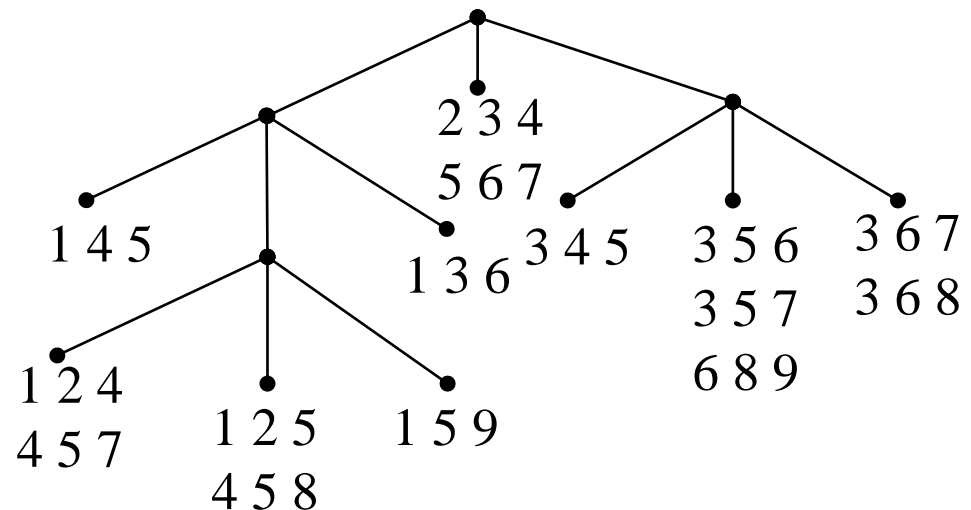
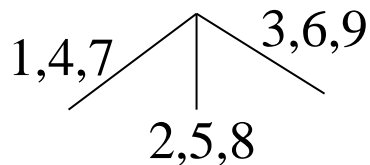
Suppose you have the same 15 candidate itemsets of length 3:

{1 4 5}, {1 2 4}, {4 5 7}, {1 2 5}, {4 5 8}, {1 5 9}, {1 3 6}, {2 3 4},  
{5 6 7}, {3 4 5}, {3 5 6}, {3 5 7}, {6 8 9}, {3 6 7}, {3 6 8}

You need:

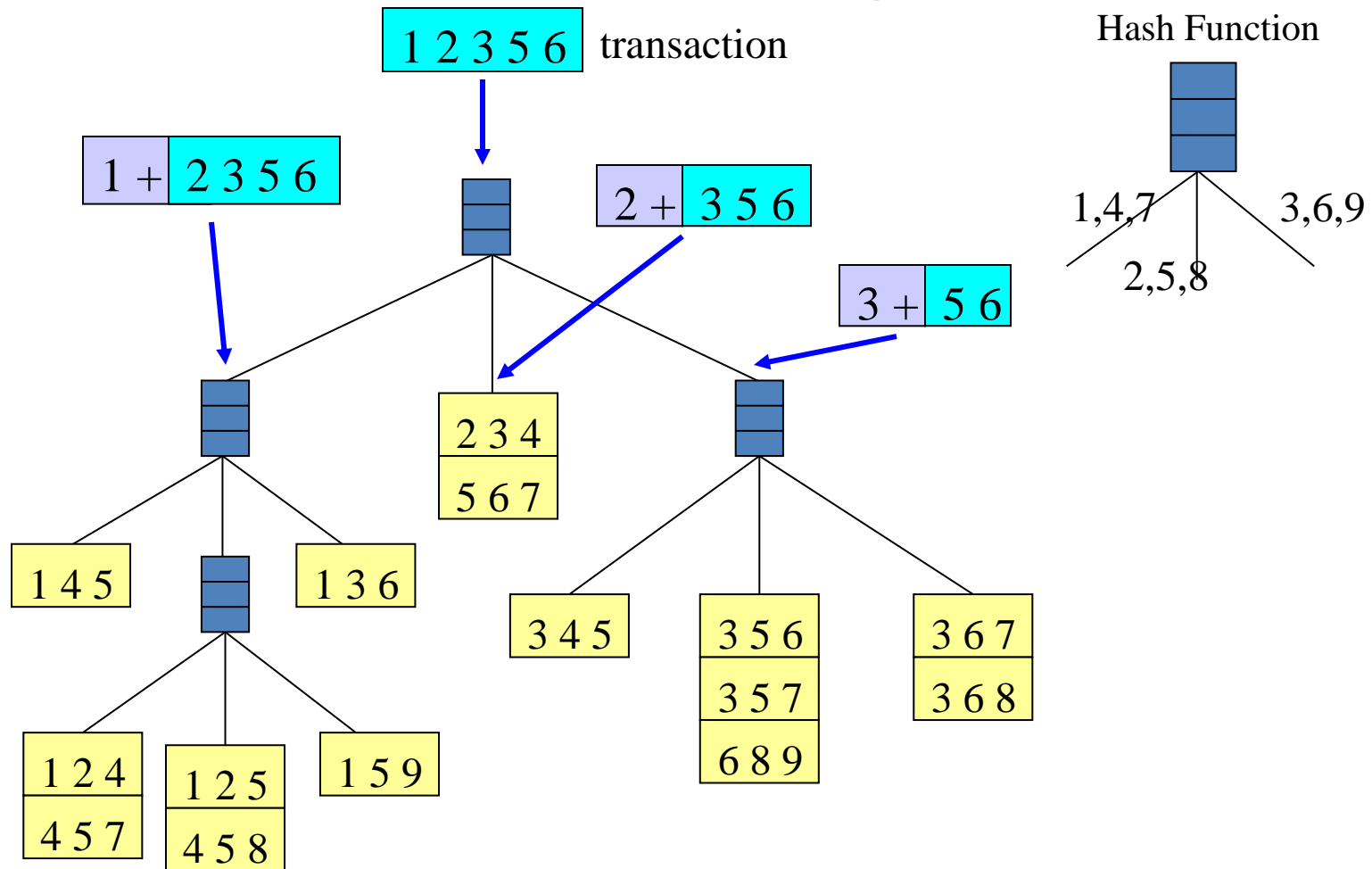
- Hash function
- Leafs: Store the itemsets

Hash function =  $x \bmod 3$



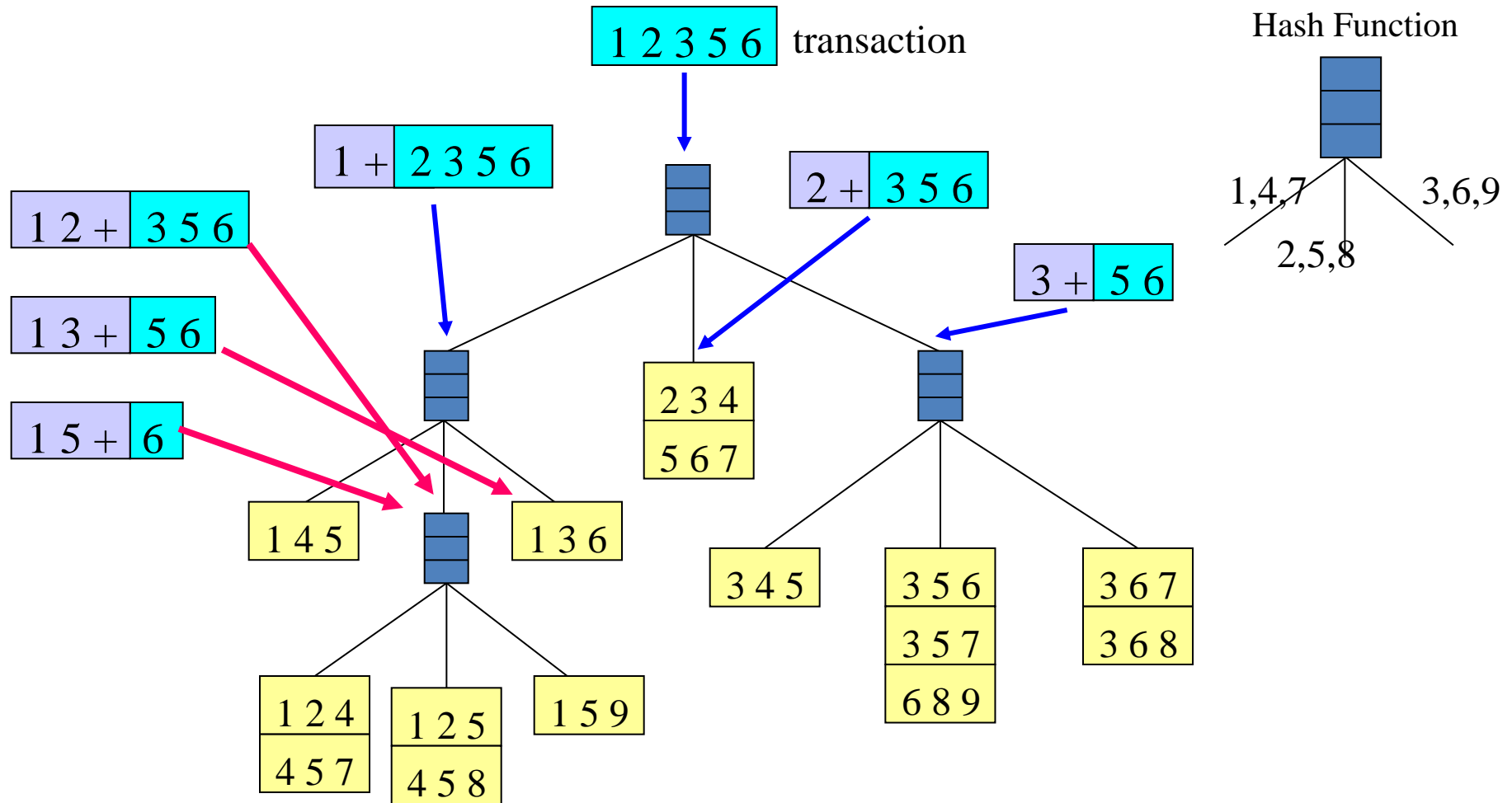
At the  $i$ -th level we hash on the  $i$ -th item

# Subset Operation Using Hash Tree

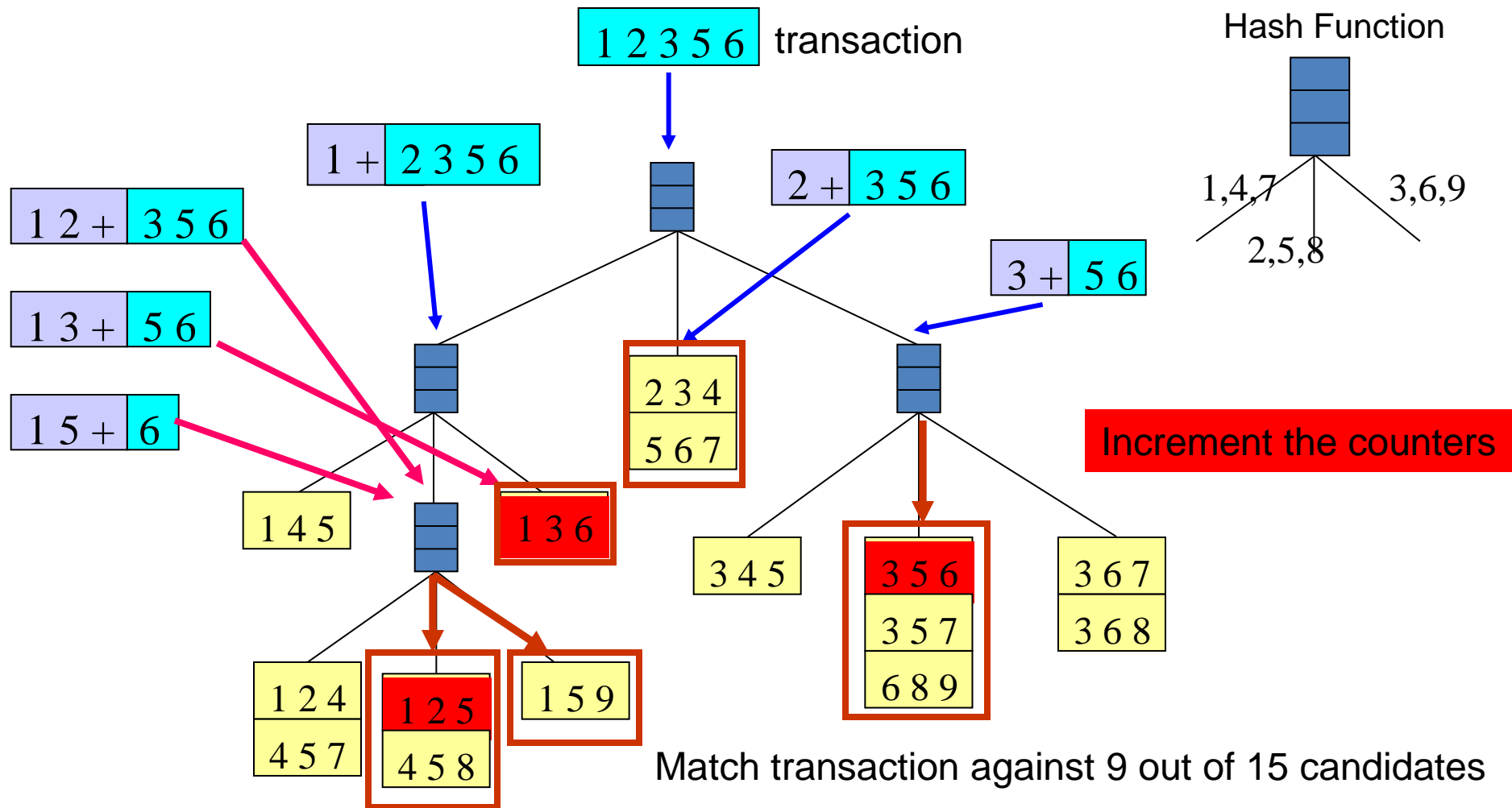




# Subset Operation Using Hash Tree



# Subset Operation Using Hash Tree



Hash-tree enables to enumerate itemsets in transaction and match them against candidates