

Chapter I. Introduction

[TODO] Add cycle diagram: input (lua code) > lua2prolog > prolua > output (result and environment)

I.a. Why Lua?

[TODO] Why Lua? Simple, powerful yet expressive, well documented, hasn't been done, etc.

I.b. Why Prolog?

[TODO] Why Prolog? Power of expression, ease of use, etc.

I.c. Constraints

The interpreter will work for Lua 5.1 and below. This is because I'm not familiar with some of the changes made in later versions of Lua, most notably the change in how the environment is managed. I'll have to do a bit more research to be able to update Prolua.

Of the eight basic types of values in Lua, only only **numbers**, **strings**, **booleans**, **tables**, **functions** and **nil** will be implemented. The **userdata** and **thread** types will be excluded, as well as the features that depend on these types, such as coroutines.

I.d. Notation

[TODO] Explain notation and how to read it.

Chapter II. Syntax

Our first order of business is to define an abstract syntax specific to Prolua, from Lua's concrete syntax given below in EBNF

```
chunk ::= {stat [`;']} [laststat [`;']]
block ::= chunk
stat ::=
      varlist `=' explist |
      functioncall
      do block end |
      while exp do block end |
      repeat block until exp
      if exp then block {elseif exp then block} [else block] end |
for Name `=' exp `,' exp [`,' exp] do block end |
for namelist in explist do block end |
      function funcname funcbody |
      local function Name funcbody |
local namelist [`=' explist]
laststat ::= return [explist] | break
funcname ::= Name { '.' Name} [ ':' Name]
varlist ::= var {',' var}
var ::= Name | prefixexp '[' exp ']' | prefixexp '.' Name
namelist ::= Name {',' Name}
explist ::= exp {',' exp}
exp ::=
      nil | false | true | Number | String | '...' | function |
      prefixexp | tableconstructor | exp binop exp | unop exp
prefixexp ::= var | functioncall | '(' exp ')'
functioncall ::= prefixexp args | prefixexp ':' Name args
args ::= '(' [explist] ')' | tableconstructor | String
function ::= function funcbody
funcbody ::= '(' [parlist] ')' block end
parlist ::= namelist [',' '...'] | '...'
tableconstructor ::= '{' [fieldlist] '}'
fieldlist ::= field {fieldsep field} [fieldsep]
field ::= '[' exp ']' '=' exp | Name '=' exp | exp
fieldsep ::= ',' | ';'
binop ::=
       ..

'+' | '-' | '*' | '/' |

'^' | '%' | '..' | '<' | '<=' | '>' | '>=' | '==' | '~=' | and | or
unop ::= '-' | not | '#'
```

a. Sets

Let Expression be	the set of all	possible expre	essions in Lua,	and <i>Expressio</i>	<i>nList</i> a list of
expressions such t	hat				

expressionlist:
$$expressionList$$
 expressionlist: $expressionList$ $expressionList$ expressionList

Let Name be the set of all possible identifer names in Lua, and NameList a list of names such that

$$namelist: \frac{n \in Name, \ ns \in NameList}{n::ns \in NameList}$$

Let **ParameterName** be an extension of **Name** to include the name "vararg", then let **ParameterNameList** be a list of parameter names such that

$$\begin{array}{ll} parameter: & \hline parameterName = Name \ \cup \ \{vararg\} & parlist: \hline \\ parlist: & \hline p::ps \ \in \ ParameterNameList \\ \hline \end{array}$$

Let *Variable*, a subset of *Expression*, be the set of all possible variables in Lua, and *VariableList* a list of variables such that

$$\text{variablelist:} \frac{}{[] \in \text{VariableList}} \quad \text{variablelist:} \frac{\text{v} \in \text{Variable}, \quad \text{vs} \in \text{VariableList}}{\text{v::vs} \in \text{VariableList}}$$

Let *Value*, a subset of *Expression*, be the set of all possible values in Lua, and *ValueList* a list of values such that

$$\mbox{valuelist:} \frac{\mbox{valuelist:} \frac{\mbox{v} \in \mbox{Value, } \mbox{v} \in \mbox{ValueList}}{\mbox{v::vs} \in \mbox{ValueList}}$$

Let **Statement** be the set of all possible statements (instructions) in Lua, and **StatementList** a list of statements such that

```
 statementlist: \frac{s \in Statement, ss \in StatementList}{s::ss \in StatementList}
```

b. Values and Types

Nil is a type of value whose main property is to be different from any other value; it usually represents the absence of a useful value

value:
$$\frac{v \in \{nil\}}{niltype(v) \in Value}$$

Boolean values are defined as false and true.

value:
$$\frac{v \in \{false, true\}}{booleantype(v) \in Value}$$

Number represents real numbers.

$$value: \frac{v \in \mathbb{R}}{numbertype(v) \in Value}$$

A **string** represents arrays of 8-bit characters. There's no **character** type in Lua but to be able to define the syntax of a string, we need to define what a character is. Unfortunately, the character set is too large to enumerate so we'll simplify by supposing that it's the set of all 8-bit ASCII characters. A string is then considered to be a concatenation of characters

$$string: \frac{c \in Character, s \in String}{[] \in String}$$

$$value: \frac{s \in String}{stringtype(s) \in Value}$$

The type **table** implements associative arrays, i.e. arrays that can be indexed with any value except nil. Tables can contain values of all types including 'nil', in which case the table field is deleted

$$table: \frac{k \in Value \setminus \{niltype(nil)\}, \ v \in Value, \ t \in Table}{\langle k, v \rangle :: t \in Table}$$

$$value: \frac{t \in Table}{tabletype(t) \in Value}$$

In Lua, tables are not passed by value but by **reference**. A reference is nothing more than a positive non-zero integer that indexes a table's position in the environment

$$\text{value:} \frac{n \in \mathbb{N}_{+}^{*}}{\text{referencetype(n)} \in \text{Value}}$$

Function bodies are considered values in Lua and are defined syntactically as

$$value: \frac{ps \in ParameterNameList}{functionbody(ps, \, ss) \, \in \, Value}$$

Variables store values. To be able to retrieve a value of a variable, we need the variable's name

expression:
$$\frac{n \in Name}{variable(n) \in Expression}$$

Lua defines a **variadic expression** represented by three dots "..." which is a placeholder for a list of values

```
expression: \frac{}{\text{vararg} \in \text{Expression}}
```

b. Operators

Calling a unary operator requires the operator's name and the expression to be evaluated

expression:
$$\frac{n \in \{\text{negative, not, length}\}, e \in \text{Expression}}{\text{unop}(n,e) \in \text{Expression}}$$

Almost like a unary operator, calling **binary operators** requires the name of the operator and two expressions to be evaluated

$$\begin{split} \text{expression:} \frac{n \in \{\text{add, subtract, multiply, divide, modulo, exponent}\}, & \ e_{lhs}, e_{rhs} \in \text{Expression} \\ & binop(n, e_{lhs}, e_{rhs}) \in \text{Expression} \\ \\ \text{expression:} \frac{n \in \{\text{equal, lt, le, gt, ge, and, or, concatenate}\}, & \ e_{lhs}, e_{rhs} \in \text{Expression}}{binop(n, e_{lhs}, e_{rhs}) \in \text{Expression}} \end{split}$$

We define the table access operator which retrieves the value for a given key in a given table

expression:
$$\frac{t, k \in Expression}{access(t, k) \in Expression}$$

c. Statements.

The unit of execution in Lua is called a **chunk** which is simply a sequence of statements that are executed sequentially

statement:
$$\frac{ss \in StatementList}{chunk(ss) \in Statement}$$

Lua allows multiple **assignments**. Therefore, the syntax for assignment defines a list of variables on the left side and a list of expressions on the right. Syntactically, the assignment operator takes two lists of expressions which it will evaluate into appropriate values

statement:
$$\frac{\text{es}_{\text{lhs}}, \text{es}_{\text{rhs}} \in \text{ExpressionList}}{\text{assign}(\text{es}_{\text{lhs}}, \text{es}_{\text{rhs}}) \in \text{Statement}}$$

Function calls are expressions but can be executed as statements, in which case all return values are thrown away

```
statement: \frac{e \in Expression, \quad es \in ExpressionList}{functioncall(e,es) \in Statement}
```

The do statement allows us to explicitly delimit a block of statements to produce a single statement

statement:
$$\frac{ss \in StatementList}{do(ss) \in Statement}$$

A while loop is defined as

statement:
$$\frac{e \in Expression, ss \in StatementList}{while(e, ss) \in Statement}$$

A repeat-until loop is similar to a while loop

$$statement: \frac{e \in Expression, \quad ss \in StatementList}{repeat(e, \, ss) \, \in \, Statement}$$

An **if-else** condition takes an expression that it evaluates into a boolean value, a statement that will be executed if the aforementioned value is true, and another if it is false

$$statement: \frac{e \in Expression, s_{true}, s_{false} \in Statement}{if(e, s_{true}, s_{false}) \in Statement}$$

We can then define an **if** condition (without the **else**) as "if(e, s_{true} , do([]))", an **if-elseif** condition recursively as "if(e, s_{true} , if_i(e_i, s_{truei} , do([]))", and finally an **if-elseif-else** condition as "if(e, s_{true} , if_i(e_i, s_{truei} , s_{false}))".

The numeric for loop is defined syntactically as

$$statement: \frac{n \in Name, \quad e_{initial}, e_{end}, e_{increment} \in Expression, \quad ss \in StatementList}{for(n, e_{initial}, e_{end}, e_{increment}, ss) \in Statement}$$

while the generic for loop is defined as

$$statement: \frac{ns \in NameList, \ es \in ExpressionList, \ ss \in StatementList}{for(ns, \, es, \, ss) \in Statement}$$

Declaring local variables requires the name of the variable as well as a value that will be assigned to the variable. If no value is specified, then **nil** is implied.

statement:
$$\frac{n \in Name}{localvariable(n) \in Statement}$$
 statement: $\frac{n \in Name, v \in Value}{localvariable(n, v) \in Statement}$

The **return** statement returns one or more values from a function or a chunk

statement:
$$es \in ExpressionList$$

return(es) \in Statement

With the abstract syntax defined, we now know the **form** that a Prolua program will take. For example, consider the following Lua program¹

```
function toCelsius(fahrenheit)
    return (fahrenheit - 32)*(5 / 9);
end;

t = {min = 0, 0, 0, max = 0}

t.min = toCelsius(5);

local i = 1;

while (i < 4) do
    t[i] = toCelsius(5^(i + 1));
    i = i + 1;
end;

t.max = toCelsius(5^5);

return t.min, t[1], t[2], t[3], t.max;</pre>
```

and its generated Prolua program (formatted for readability)

```
chunk([
assign([variable('toCelsius')], [functionbody(['fahrenheit'],
[return([binop(multiply, binop(subtract, variable('fahrenheit')
numbertype(32)), binop(divide, numbertype(5), numbertype(9)))])]))
assign([variable('t')], [tabletype([[stringtype('min'), numbertype(0)],
[numbertype(1), numbertype(0)], [numbertype(2), numbertype(0)], [numbertype(3),
numbertype(0)], [stringtype('max'), numbertype(0)]])]),
assign([access(variable('t'), stringtype('min'))],
[functioncall(variable('toCelsius'), [numbertype(5)])]),
localvariable('i', numbertype(1)),
while(binop(lt, variable('i'), numbertype(4)), [assign([access(variable('t'),
variable('i'))], [functioncall(variable('toCelsius'), [binop(exponent,
numbertype(5), binop(add, variable('i'), numbertype(1)))]),
assign([variable('i')], [binop(add, variable('i'), numbertype(1))])]),
assign([access(variable('t'), stringtype('max'))],
[functioncall(variable('toCelsius'), [binop(exponent, numbertype(5),
numbertype(5))])]),
return([access(variable('t'), stringtype('min')), access(variable('t'),
numbertype(1)), access(variable('t'), numbertype(2)), access(variable('t'),
numbertype(3)), access(variable('t'), stringtype('max'))])
]).
```

We can see that the output is essentially a Prolog program with predicates that resemble the previously defined abstract syntax.

¹ This is the **temperature.lua** program provided in the samples.

Chapter III. Semantics

As I mentioned before, the syntax describes the form of a Prolua program, but says nothing about its behavior...

[TODO] Describe Prolua semantics.