

Assignment - I - Entropy
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| Instance | a <sub>1</sub> | a <sub>2</sub> | a <sub>3</sub> | classification |
|----------|----------------|----------------|----------------|----------------|
| 1        | T              | Hot            | High           | No             |
| 2        | T              | Hot            | High           | No             |
| 3        | F              | Hot            | High           | Yes            |
| 4        | F              | Cool           | Normal         | Yes            |
| 5        | F              | Cool           | Normal         | Yes            |
| 6        | T              | Cool           | High           | No             |
| 7        | T              | Hot            | High           | No             |
| 8        | T              | Hot            | Normal         | Yes            |
| 9        | F              | Cool           | Normal         | Yes            |

|     |   |      |      |      |
|-----|---|------|------|------|
| 10. | F | cool | High | Yes. |
|-----|---|------|------|------|

For calculating Entropy:-

- Step 1:- overall Entropy for the Data set
- Step 2: Find Individual Entropy for each attribute
- Step 3: For that attribute calculate the Information gain formula.
- Step 4: Repeat 3 & 4 for all attributes.
- Step 5: Sum the Entropy found from all each attribute.

Calculation:-

1) Overall Entropy:-

Given

No. of DS = 10

Positive =  $\frac{6}{10}$

Negative =  $\frac{4}{10}$

$$= -1.322$$

$$\frac{4}{10} = 0.4$$

$$\frac{6}{10} = 0.6$$

$$= -1.322$$

$$= -0.737$$

Entropy formula:-

$$E(S) = -P_s \log_2 P_s - N_s \log_2 N_s$$

$$E(S) = -\frac{6}{10} \log_2 \frac{6}{10} - \frac{4}{10} \log_2 \frac{4}{10}$$

$$= 0.5288 + 0.4222$$

$$E(S) = 0.971$$

## 2) Entropy & IGF ( $a_1$ )

values - True, False (2)

| <u>True</u> | <u>False</u> |
|-------------|--------------|
| Total - 5   | Total - 5    |
| $T_s = 4/5$ | $F_s = 5/5$  |
| $T_n = 1/5$ | $F_n = 0$    |
|             | are Yes      |

$$E(T) = - \frac{4}{5} \log_2 \frac{4}{5} - \frac{1}{5} \log_2 \frac{1}{5}$$

$$= 0.25752 + 0.4644$$

$$E(F) = 0$$

$$E(T) = 0.72192$$

INFORMATION GAIN FORMULA FOR  $a_1$  :-

$$G(a_1) = \text{Entropy} - \frac{\text{True}}{a_1} * E(T) - \frac{\text{False}}{a_1} * E(F)$$

$$G(a_1) = 0.971 - \frac{5}{10} * 0.72192 - \frac{5}{10} * 0$$

$$= 0.971 - 0.36096 - 0$$

$$G(a_1) = 0.61$$



3) Entropy & ICF (a2) :-

values - Hot, cool

Hot  
Total - 5  
Hs - 3/5  
Hn - 2/5

3/5 = 0.6  
L = 0.73  
2/5 = 0.4  
L = -1.92

$$E(H) = -3/5 \log_2 3/5 - 2/5 \log_2 2/5$$

$$= 0.44225 + 0.5288$$

$$= 0.971$$

cool  
Total - 5  
Cs - 4/5  
Cn - 1/5

$$E(C) = -4/5 \log_2 4/5 - 1/5 \log_2 1/5$$

$$= 0.72192$$

IFG FA a2 :-

$$G(a2) = 0.971 - 5/10 * 0.971 - 5/10 * 0.72192$$

$$= 0.971 - (0.5 * 0.971) - (0.5 * 0.72192)$$

$$= 0.971 - 0.4855 - 0.36096$$

$$= 0.971 - 0.84646$$

$$G(a2) = 0.124$$

3)  $a_3$ :-

value = 2

H

$$T = 6$$

$$H_S = 2/6$$

$$H_N = 4/6$$

$$2/6 = 0.33$$

$$L = -1.385$$

$$4/6 = 0.67$$

$$L = -0.585$$

$$= -2/6 \log_2 2/6 - 4/6 \log_2 4/6$$

$$= 0.52305 + 0.39195$$

$$= 0.915$$

N

$$T = 5$$

$$N_S = 4/5$$

$$N_N = 0$$

$$= 0$$

$$= 0$$

IBF:-

$$= 0.917 - 6/10 * 0.915 = 0$$

$$= 0.917 - 0.549 = 0.368$$

$$a(a_3) = 0.368$$

$$a_1 = 0.61$$

$$a_2 = 0.124$$

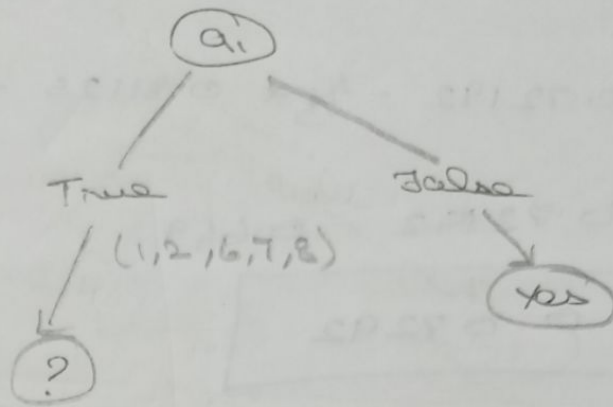
$$a_3 = 0.368$$



Even the calculated I<sub>n</sub> we can also to find the root node

Decision tree

Root node



From False we get a conclusion, But in true we have to again learn the dataset belongs to true.

|   | a <sub>1</sub> | a <sub>2</sub> | a <sub>3</sub> | classification |
|---|----------------|----------------|----------------|----------------|
| 1 | T              | Hot            | High           | No             |
| 2 | T              | Hot            | High           | No             |
| 6 | T              | cool           | High           | No             |
| 7 | T              | Hot            | High           | No             |
| 8 | T              | Hot            | Normal         | Yes            |

By using this dataset again we have to calculate next 1st attribute

$$\begin{aligned}
 \frac{1}{5} &= 0.2, L = -2.322, \frac{4}{5} = 0.8, L = 0.322 \\
 E(S) &= -\frac{1}{5} \log_2 \frac{1}{5} - \frac{4}{5} \log_2 \frac{4}{5} \\
 &= 0.4644 + 0.25752 \\
 E(S) &= 0.72192
 \end{aligned}$$

a<sub>2</sub> :- Entropy

Hot, cool

T - 4 Hot

H<sub>S</sub> = 3/4

H<sub>N</sub> = 1/4

$$\begin{aligned}
 E(H) &= -\frac{3}{4} \log_2 \frac{3}{4} - \frac{1}{4} \log_2 \frac{1}{4} \\
 &= 0.31125 + 0.5 \\
 &= 0.81125
 \end{aligned}$$

cool

T = 1

C<sub>S</sub> = 0

C<sub>N</sub> = 1/1

E(C) = 0

3/4 = 0.75

L = 0.415

1/4 = 0.25

L = 2

IGF  $a_2$

$$= 0.72192 - \frac{4}{5} * 0.81125 - 0$$

$$= 0.72192 - 0.649$$

$$G(a_2) = 0.07292$$

$a_3$  :-

Entropy :-

values - High, normal

$$\text{High} - 4$$

$$H_S - 0$$

$$H_D - 4/4$$

$$E(H) = 0$$

normal - 1

$$H_S - \frac{1}{1}$$

$$H_D - 0$$

$$E(D) = 0$$

yes

IGF :-

$$= 0.72192 - 0 - 0$$

$$G(a_3) = 0.72192$$

$$a_2 = 0.07292$$

$$a_3 = 0.72192$$



# Decision Tree

