

# Provably Secure Authentication of Digital Media Through Invertible Watermarks\*

Jana Dittmann<sup>1</sup>, Stefan Katzenbeisser<sup>2</sup>, Christian Schallhart<sup>2</sup>, Helmut Veith<sup>2</sup>

<sup>1</sup> Otto-von-Guericke Universität Magdeburg, Germany,  
jana.dittmann@iti.cs.uni-magdeburg.de

<sup>2</sup> Technische Universität München, Germany  
katzenbe,schallha,veith@in.tum.de

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## Abstract

The recent advances in multimedia technology have made the manipulation of digital images, videos or audio files easy. On the one hand the broad availability of these new capabilities enabled numerous new applications. On the other hand, for the same reasons, digital media can easily be forged by almost anyone. To counteract this risk, fragile watermarks were proposed to protect the integrity and authenticity of digital multimedia objects. Traditional watermarking schemes employ non-cryptographic and signal processing oriented techniques, which fail to provide any provable security guarantee against malicious modification attempts. In this paper, we give for the first time a provably secure authentication mechanism for digital multimedia files that is based on both cryptographic signatures and invertible watermarks. While traditional watermarking schemes introduce some small irreversible distortion in the digital content, invertible watermarks can be completely removed from a watermarked work.

## 1 Introduction

The recent advances in multimedia technology brought powerful tools for manipulating digital images, videos or audio files to everybody's desktop. While this enables numerous new applications, the authenticity and integrity of digital artefacts cannot be readily asserted—the origin and integrity of almost every digital object must be doubted. For example, a picture displaying a car accident cannot be readily trusted as evidence, since it is possible to modify the location of the cars on the picture only using a common personal computer

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running digital image processing tools. Similar problems apply to digital sound clips or video files, where sets of samples can be removed or replaced.

This problem was first noted by Friedman [5], who proposed to sign digital images using a cryptographic signature in order to assert their authenticity and integrity. The apparent drawback of this proposal was that the signature and the image had to be stored separately. The direct encoding of signatures into digital images was made possible by the availability of sophisticated fragile watermarking schemes. A fragile watermark is a digital watermark [9] that is *not* robust against common signal processing tools—if a watermarked object is modified, the watermark cannot be detected any more. Fragile watermarks were proposed as tools to assure the integrity of image files [11, 13]. In these approaches, non-cryptographic signatures are encoded as fragile watermarks in digital images. An image is deemed authentic if and only if it is possible to recover and verify its embedded signature. If a file with such a watermark is modified, then either the watermark cannot be detected any more or the recovered non-cryptographic signature does not match the image. In both cases, the image is considered to be tampered. Unfortunately, this approach has the apparent drawback that it is not possible to formally prove its security in a cryptographically precise way.

In high security applications, like medical imaging, there is another concern, namely that the watermark embedding process induces some distortion that interferes with the contents of the digital media files. For example, X-ray images are extremely sensitive to blurring operations, which limits the use of watermarking schemes in medical applications. To address these concerns, invertible (or reversible) watermarking schemes were proposed [8, 3, 4, 12, 10, 1]. Invertible watermarking schemes allow to insert a watermark into an object as usual, but facilitate the lossless removal of the watermark from an untampered watermarked object. More precisely, if a watermark is successfully detected, the information contained in the recovered watermark, together with the watermark key, suffices to remove the watermark completely from the object. Most invertible watermarks are also fragile and therefore suitable to implement authentication schemes.

In this paper we provide the first construction for a provably secure authentication scheme for digital media files that relies on watermarking technology. Technically, we use invertible fragile watermarks to embed a digital signature of the media. After reviewing the necessary watermarking technology in Section 2, we introduce media authentication schemes in Section 3. Finally, we give two provably secure constructions for media authentication schemes in Sections 4 and 5; the second construction can be used for large media files or in streaming applications.

## 2 Invertible Watermarks

While virtually all previous watermarking schemes introduced some small amount of irreversible distortion in the data during the embedding process, *invertible watermarking* schemes were first introduced by Honsinger et.al. [8]. They were able to construct a watermarking scheme where a watermark can be completely removed from an untampered watermarked object, thereby recovering the original object. However, their construction is

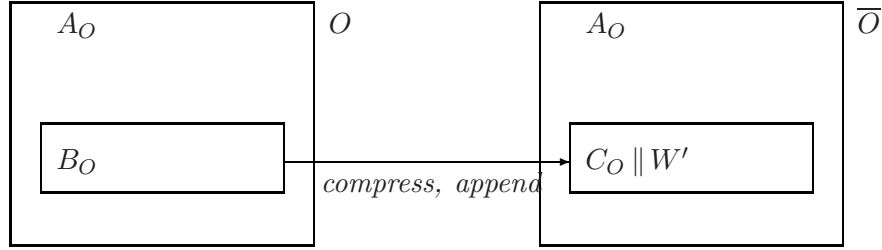


Figure 1: Invertible watermarking. An object  $O$  is divided into two parts  $A_O$  and  $B_O$ . The watermark consists of the compressed part  $B_O$ , denoted by  $C_O$ , and the watermark payload  $W'$ .

not practical, as it introduces (small, but visible) distortions in the watermarked objects.

Fridrich et. al. [3] introduced a general framework that allows to construct an invertible (fragile) watermarking scheme out of a fragile one. The general idea is to divide the object  $O$ , dependent on a public key  $K_W$ , into two parts  $A_O$  and  $B_O$ . The latter part contains perceptually insignificant portions of the object that can be overwritten by a watermark without lowering the object quality, whereas  $A_O$  contains perceptually visible parts that must be preserved. To provide invertibility, the original part  $B_O$  is compressed and stored in the watermark; denote the compressed part  $B_O$  with  $C_O$ . The watermark  $W$  consists of the watermark payload  $W'$  and  $C_O$ , thus  $W = C_O \parallel W'$ .  $W$  replaces the part  $B_O$  in the watermarked object  $\bar{O}$ . This general framework is depicted in Figure 1.

The distortion of the watermark can easily be removed by separating the marked object  $\bar{O}$  into the two parts  $A_{\bar{O}}$  and  $B_{\bar{O}}$ . During the watermark insertion process, only  $B_{\bar{O}}$  was modified, so  $A_{\bar{O}} = A_O$ . Now,  $B_{\bar{O}}$  has the form  $W = C_O \parallel W'$ ; decompressing  $C_O$  yields to the part  $B_O$  of the original object  $O$ . By overwriting  $B_{\bar{O}}$  with  $B_O$  in the object  $\bar{O}$ ,  $O$  can be completely recovered. This procedure works only if  $\bar{O}$  was not altered; it is therefore a fragile watermarking scheme.

In the rest of the paper, we denote an invertible watermarking scheme as a tuple of two probabilistic polynomial algorithms  $\langle \text{SEPARATE}, \text{JOIN} \rangle$ . On input  $O$  and  $K_W$ ,  $\text{SEPARATE}$  produces the tuple  $\langle A_O, B_O \rangle$ .  $\text{JOIN}$  inverts the algorithm  $\text{SEPARATE}$ , i.e., on input  $\langle A_{\bar{O}}, B_{\bar{O}} \rangle$  and  $K_W$  it outputs  $\bar{O}$ . Except with negligible probability, we require that

$$\text{JOIN}(K_W, \text{SEPARATE}(K_W, O)) = O,$$

for all objects  $O$  and keys  $K_W$  with  $\text{SEPARATE}(K_W, O) \neq \text{FAIL}$ .

From the previous description it is obvious that it is not possible to embed an invertible watermark in every object. In case the part  $B_O$  cannot be sufficiently compressed, there is not enough room to store both the watermark payload and the compressed part  $C_O$ . However, typical multimedia files (such as images or audio files) contain enough redundant, compressible information so that the watermarking operation works for virtually all relevant objects. In this paper, we do not detail the insertion and recovery operations of invertible watermarking schemes and rather use them as black-box primitives. For specific

implementation details of invertible watermarking schemes, we refer to [3, 4, 2].

### 3 Media Authentication Schemes

Similar to cryptographic signatures, media authentication schemes based on invertible watermarks can be described in terms of four probabilistic polynomial time algorithms  $\langle \text{GENKEY}, \text{PROTECT}, \text{VERIFY}, \text{RECONSTRUCT} \rangle$ . The algorithm GENKEY denotes the key-generation process; by using a private key, PROTECT authenticates an object  $O$  and outputs its signed version  $\overline{O}$ . Signed objects can be verified by the algorithm VERIFY and a public key; VERIFY either outputs TRUE or FALSE. In the first case, the object is deemed authentic; in the latter case, the object is considered modified. Finally, RECONSTRUCT reverses the protection mechanism and losslessly reconstructs  $O$  out of  $\overline{O}$ .

#### 3.1 Definition

More formally, an *invertible media authentication scheme* is defined as follows:

- Algorithm GENKEY generates the necessary keys for the application. On input  $1^n$ , GENKEY produces a triple of strings  $\langle K_P, K_V, K_R \rangle$  with  $|K_P \parallel K_V \parallel K_R| = n$ ; the operation  $\parallel$  denotes string concatenation. The key  $K_P$  will be used in the protection step, whereas  $K_V$  and  $K_R$  are used for verification and recovery. The verification key  $K_V$  is a public key, whereas  $K_P$  and  $K_R$  are private keys.
- Algorithm PROTECT takes  $K_P$ ,  $K_R$  and an object  $O$ . The output of the algorithm consists of an authenticated object  $\overline{O}$ .
- Algorithm VERIFY takes the verification key  $K_V$  and an object  $\overline{O}$  and outputs a boolean variable.
- Algorithm RECONSTRUCT takes the keys  $K_R$  and  $K_V$  and an object  $\overline{O}$  and restores the original object  $O$ .

Note that we have defined all algorithms as probabilistic, which implies that they can fail on certain instances (for example it may not be possible to embed a watermark in an invertible manner); in this case, the algorithms output a special symbol FAIL. We require that the media authentication scheme “works” for almost all objects that can be authenticated. In particular,

$$\text{VERIFY}(\text{PROTECT}(O, K_P, K_R), K_V) = \text{TRUE}$$

and

$$\text{RECONSTRUCT}(\text{PROTECT}(O, K_P, K_R), K_R, K_V) = O$$

must hold except for a negligible fraction of all objects  $O$  with  $\text{PROTECT}(O, K_P, K_R) \neq \text{FAIL}$ .

As usual, we will denote a cryptographic *signature scheme* as triple of probabilistic polynomial time algorithms  $\mathbb{S} = \langle \text{GENSIGN}, \text{SIGN}, \text{SIGVERIFY} \rangle$ , where GENSIGN denotes

the key generation, SIGN the signing and SIGVERIFY the signature verification algorithm. A signature scheme is said to be secure, if it is secure against existential forgery of signatures under a chosen-message attack [7]; that is, if the attacker is unable (even with access to a signing oracle) to forge a valid pair of a message and a corresponding signature.

### 3.2 Attacker Model

Sticking to Kerckhoffs' principle, we assume that an attacker possesses complete knowledge of the system; furthermore, the attacker has access to the public verification key  $K_V$ . Similar to attacks against cryptographic signature schemes, we can distinguish several types of attacks against media authentication schemes according to the possibilities for an attacker to interfere with the system. It seems natural to assume that an attacker will know several protected media files under one verification key  $K_V$ , as such objects might be freely available on the Internet. A more powerful attacker may even launch a *chosen message attack*. In this setup, an attacker is able to obtain protected objects of his own choice. That is, he can obtain a signed object  $\overline{O}$  corresponding to an object  $O$  chosen during the attack. In imaging applications, such an attack is particularly realistic, as long as the attacker has physical access to the imaging device and can take pictures of his own choice.

For this reason, we adopt the notion of existential forgery under chosen message attacks for the present scenario. In particular, an attacker can query an oracle for authenticated objects of his own choice and perform any polynomially bounded computation. We say that an attack is successful, if the attacker manages to output an object  $\overline{O}$  together with an alleged original  $O$  such that  $\text{VERIFY}(\overline{O}, K_V) = \text{TRUE}$  and the original object  $O$  was *not* presented to the oracle previously.

**Definition 1** Let  $\langle \text{GENKEY}, \text{PROTECT}, \text{VERIFY}, \text{RECONSTRUCT} \rangle$  a media authentication scheme and  $\text{QUERY}_{K_P}$  be an oracle that computes  $\overline{O} \leftarrow \text{PROTECT}(O, K_P)$  on input  $O$ . Furthermore, let  $\langle K_P, K_V, K_R \rangle \in [\text{GENKEY}(1^{n_K})]$ .

An attack is a probabilistic algorithm  $\text{ATTACK}$  with oracle access to  $\text{QUERY}_{K_P}$  and success probability  $\varepsilon_{\text{ATTACK}}$  such that

$$\text{ATTACK}(1^n, K_V) = \begin{cases} \langle O, \overline{O} \rangle & \text{such that } \text{VERIFY}(\overline{O}, K_V) = \text{TRUE}, |O| = n, \\ & \overline{O} \in [\text{PROTECT}(O, K_P)] \text{ and } O \neq O_i \text{ for all } 1 \leq i \leq l, \\ & \text{with probability } \varepsilon_{\text{ATTACK}} \\ \text{FAIL} & \text{with probability } 1 - \varepsilon_{\text{ATTACK}}, \end{cases}$$

where  $O_i$  denotes the input to the  $i$ -th oracle query  $\text{QUERY}_{K_P}$ . The probability is taken over all coin tosses of  $\text{ATTACK}$  and all keys  $\langle K_P, K_V, K_R \rangle$ .

We say that a media authentication scheme is secure, if the success probability of *every* probabilistic polynomial time attack is negligible:

**Definition 2** A media authentication scheme is secure against existential forgery of authenticated objects, if every probabilistic polynomial time attack  $\text{ATTACK}$  has negligible success probability.

## 4 Offline Media Authentication

In this section, we describe an offline media authentication scheme. We call a scheme offline, if the protection algorithm needs access to the whole media file at once.

Let  $\mathbb{S} = \langle \text{GENSIGN}, \text{SIGN}, \text{SIGVERIFY} \rangle$  be a cryptographic signature scheme producing signatures of length  $k$ ,  $\text{ENCRYPT}$  and  $\text{DECRYPT}$  be the encryption and decryption operation of a symmetric cipher and  $\text{COMPRESS}$  be the compression algorithm of a lossless compression scheme. Furthermore, we fix an invertible watermarking scheme  $\langle \text{SEPARATE}, \text{JOIN} \rangle$  that can embed watermark strings of length  $k$ .

Loosely speaking, the media authentication scheme stores a cryptographic signature of the unmodified portion of the object (the part  $A_O$ ) and the encrypted, compressed part  $B_O$  as an invertible watermark. The construction is as follows:

- **GENKEY** runs  $\text{GENSIGN}$  to obtain a key pair  $\langle K_{SS}, K_{VS} \rangle$ ; furthermore, it computes a key  $K_E$  for the symmetric cipher and a random string  $K_W$ . Let  $K_P = K_{SS} \parallel K_W$ ,  $K_V = K_{VS} \parallel K_W$  and  $K_R = K_E \parallel K_W$ .
- **PROTECT**, on input  $O$ ,  $K_P = K_{SS} \parallel K_W$  and  $K_R = K_E \parallel K_W$ , separates  $O$ , using algorithm  $\text{SEPARATE}$  and key  $K_W$ , into two parts  $A_O$  and  $B_O$ . The latter part is compressed to obtain  $C_O$ . Denote with  $W'$  the string  $W' = X \parallel s$ , where

$$X \leftarrow \text{ENCRYPT}(K_E, C_O \parallel H(O))$$

and

$$s \leftarrow \text{SIGN}(K_{SS}, A_O \parallel X).$$

**PROTECT** runs  $\text{JOIN}$  on  $K_W$  and  $\langle A_O, W' \rangle$  to obtain the authenticated object  $\overline{O}$  or **FAIL**. If  $\text{JOIN}$  fails, **PROTECT** outputs **FAIL**, otherwise  $\overline{O}$ .

- **VERIFY**, on input  $\overline{O}$  and  $K_V = K_{VS} \parallel K_W$ , runs  $\text{SEPARATE}$  on  $K_W$  and  $\overline{O}$  to obtain the two parts  $A_{\overline{O}}$  and  $B_{\overline{O}}$  of  $\overline{O}$ . The latter part has the form  $B_{\overline{O}} = X \parallel s$ , where  $X$  is an arbitrary string and  $s$  is a cryptographic signature. **VERIFY** outputs the Boolean value

$$\text{SIGVERIFY}(K_{VS}, A_{\overline{O}} \parallel X, s).$$

- **RECONSTRUCT**, on input  $\overline{O}$ ,  $K_R = K_E \parallel K_W$  and  $K_V = K_{VS} \parallel K_W$ , first runs **VERIFY** to assure the integrity of  $\overline{O}$ ; in case **VERIFY** outputs **FALSE**, **RECONSTRUCT** exits with **FAIL**. Otherwise, it separates  $\overline{O}$  (using  $\text{SEPARATE}$  and key  $K_W$ ) into the two parts  $A_{\overline{O}}$  and  $B_{\overline{O}}$ . The latter part has the form  $B_{\overline{O}} = X \parallel s$ . By using  $K_E$ , **RECONSTRUCT** decrypts  $X$  to obtain  $C_O \parallel h$ , where  $h$  denotes a hash; the part  $C_O$  is decompressed to obtain  $B_O$ . Finally, the part  $B_{\overline{O}}$  of  $\overline{O}$  is overwritten with  $B_O$  to obtain an object  $O$ . If  $H(O) = h$ , **RECONSTRUCT** outputs  $O$ , otherwise **FAIL**.

Intuitively, the scheme is secure because of the following argument: in case an attacker modified the part  $A_{\overline{O}}$  of  $\overline{O}$ , the embedded cryptographic signature  $s$  is matched against a modified string. On the other hand, if any bit in  $B_{\overline{O}}$  is modified, then the embedded fragile

watermark (containing either the signature  $s$  or the compressed part  $B_O$ ) is destroyed. In all cases, the tampering will be detected during the verification step. Formally, we can state this result as a theorem:

**Theorem 1** *If  $\mathbb{S}$  is a cryptographic signature scheme secure against existential forgery of messages under a chosen message attack, then the above scheme is a secure media authentication scheme.*

*Proof.* Suppose, for the sake of contradiction, that there exists an attack ATTACK (with access to the media authentication oracle  $\text{QUERY}_{K_P}$ ) against the scheme, which succeeds with non-negligible probability. We show that in this case there exists also an attack FORGE (with access to a signing oracle  $\text{SIGNQUERY}_{K_{SS}}$ ) against  $\mathbb{S}$ , which contradicts the assumption.

We construct the signature forging algorithm FORGE (for the public signature key  $K_{VS}$ ) in the following manner. On input  $K_{VS}$ , FORGE first chooses random keys  $K_E$  and  $K_W$ . Finally, FORGE simulates ATTACK. Whenever ATTACK makes an oracle query  $\text{QUERY}_{K_P}(O_i)$ , this query is replaced by the following probabilistic algorithm, which utilizes the signing oracle  $\text{SIGNQUERY}_{K_{SS}}$ ; here,  $K_{SS}$  denotes the corresponding secret signature key:

$\langle A_{O_i}, B_{O_i} \rangle \leftarrow \text{SEPARATE}(K_W, O_i)$   
 compress  $B_{O_i}$  to obtain  $C_{O_i}$   
 $X_i \leftarrow \text{ENCRYPT}(K_E, C_{O_i} \parallel H(O_i))$   
 query  $\text{SIGNQUERY}_{K_{SS}}(A_{O_i} \parallel X_i)$  for signature  $s$   
 $W'_i = X_i \parallel s$   
 output  $\text{JOIN}(K_W, \langle A_{O_i}, W'_i \rangle)$

Note that JOIN either outputs FAIL or the watermarked version  $\overline{O}_i$  of  $O_i$ .

When the simulation of ATTACK is finished, ATTACK either outputs FAIL or obtains a tuple  $\langle O, \overline{O} \rangle$ . In the first case, FORGE exits with FAIL. Otherwise, FORGE runs SEPARATE on  $\overline{O}$  and  $K_W$ , resulting in the tuple  $\langle A_{\overline{O}}, B_{\overline{O}} \rangle$ ;  $B_{\overline{O}}$  has the form  $B_{\overline{O}} = X \parallel s$ . Finally, FORGE outputs the pair  $\langle A_{\overline{O}} \parallel X, s \rangle$ . It is easy to see that FORGE perfectly simulates ATTACK so that a valid pair of a message and a signature is produced if and only if ATTACK succeeded.

It remains to show that the message  $A_{\overline{O}} \parallel X$  was not presented to the signature oracle previously. For this, assume the contrary, i.e., that there exists an index  $i$  such that  $A_{\overline{O}} \parallel X = A_{O_i} \parallel X_i$ . This can only be the case if  $A_{\overline{O}} = A_{O_i}$  and  $X = X_i$ , i.e.,  $\text{ENCRYPT}(K_E, C_{\overline{O}} \parallel H(\overline{O})) = \text{ENCRYPT}(K_E, C_{O_i} \parallel H(O_i))$ . This requires that both  $O$  and  $O_i$  agree on part  $A$ ; furthermore, by ENCRYPT being uniquely decipherable, we have  $C_{\overline{O}} \parallel H(\overline{O}) = C_{O_i} \parallel H(O_i)$ . This can only be the case if both  $O$  and  $O_i$  agree on part  $C$  and thus also on part  $B$ . We conclude that  $O = O_i$ , but this contradicts the definition of a successful attack against the media authentication scheme. This completes the proof.  $\square$

## 5 Online Media Authentication

The authentication method of the previous section assumes that the full media  $O$  is present when the media file is authenticated. However, for many multimedia applications such



a solution is unacceptable, e.g., in audio or video streaming. In this section we present an online authentication scheme that operates only on fixed-length chunks of media at a time, but nevertheless allows the full media object to be authenticated. For this purpose, an object  $O$  is considered to consist of  $n$  chunks of equal length  $O_1, \dots, O_n$ ; in abuse of notation, we write  $O = O_1 \parallel \dots \parallel O_n$ .

The online media authentication scheme presented in this paper is targeted towards applications where it must be possible to produce authenticated *excerpts*, i.e., small consecutive portions of the media stream. It is crucial that these excerpts can be produced without access to the secret protection key  $K_P$ . For example, consider the evidence produced by eavesdropping a telephone, which might be automatically authenticated by future devices; in a court hearing only a small and relevant part of the overall evidence is presented to the public. In order to prevent tampering, this excerpt should be produced *without* access to the secrets of the eavesdropping system. Nevertheless the integrity and authenticity of the excerpt should be publically verifiable.

Given an object  $O$ , we call an object  $O'$  an *excerpt* of  $O$ , if  $O'$  may be obtained from  $O$  by removing some chunks from the beginning and the end of  $O$ . Formally,  $O' = O'_1 \parallel \dots \parallel O'_m$  is an excerpt of  $O = O_1 \parallel \dots \parallel O_n$ , written as  $O' \preceq O$ , if  $m \leq n$  and there exists an index  $1 \leq i \leq n - m$  so that  $O'_1 = O_i, \dots, O'_m = O_{i+m}$ .

Given an original object  $O$ , it is possible with the proposed system to generate a signed object  $\bar{O}$  such that *each* excerpt of the signed object  $\bar{O}' \preceq \bar{O}$  can be checked for its integrity and authenticity. More precisely, the algorithm VERIFY will detect any modifications in an excerpt and will report the presence of non-consecutive chunks.

Formally, the attacker model we use for online authentication schemes is similar to the one presented in Section 3.2, with the exception that the production of excerpts is not considered an attack. Again, an attacker is forced to perform a selective forgery under a chosen message attack. However, the media object obtained at the end of the attack must not be an excerpt of an object submitted to the signing oracle previously.

**Definition 3** Let  $\langle \text{GENKEY}, \text{PROTECT}, \text{VERIFY}, \text{RECONSTRUCT} \rangle$  an online authentication scheme and  $\text{QUERY}_{K_P}$  be an oracle that, on input  $O$ , computes  $\bar{O} \leftarrow \text{PROTECT}'(O, K_P)$ . Furthermore, let  $\langle K_P, K_V, K_R \rangle \in [\text{GENKEY}'(1^{n_K})]$ . An attack is a probabilistic algorithm  $\text{SATTACK}$  with oracle access to  $\text{QUERY}_{K_P}$  and success probability  $\varepsilon_{\text{SATTACK}}$  such that

$$\text{SATTACK}(1^n, K_V) = \begin{cases} \langle O, \bar{O} \rangle & \begin{array}{l} \text{such that } \text{VERIFY}'(\bar{O}, K_V) = \text{TRUE}, |O| = n, \\ \bar{O} \in [\text{PROTECT}'(O, K_P)] \text{ and} \\ O \not\preceq O^{(i)} \text{ for all } 1 \leq i \leq l, \\ \text{with probability } \varepsilon_{\text{SATTACK}} \end{array} \\ \text{FAIL} & \text{with probability } 1 - \varepsilon_{\text{SATTACK}}, \end{cases}$$

where  $O^{(i)}$  denotes the input to the  $i$ -th oracle query  $\text{QUERY}_{K_P}$ . The probability is taken over all coin tosses of  $\text{SATTACK}$  and all keys  $\langle K_P, K_V, K_R \rangle$ .

Again, we say that an online media authentication scheme is secure, if *every* probabilistic attack has only negligible success probability.



## 5.1 Construction

In this section, we provide the construction of an online media authentication scheme that operates blockwise on the media content. Essentially, we apply the authentication scheme described in the previous section on each chunk  $O_i$ , with the exception that there is some linkage (computed by a hash function) between the chunks. Technically, we rely on the concept of hash chains [6].

Fix any collection of hash functions  $\mathbb{H} = \langle H_h : \{0,1\}^* \rightarrow \{0,1\}^{\ell(|h|)} \mid h \in \{0,1\}^* \rangle$  for any super-logarithmically growing function  $\ell : \mathbb{N} \mapsto \mathbb{N}$ . Denote with  $k_h$  an index to  $\mathbb{H}$ ; furthermore, let  $k$  be the length of the cryptographic signatures. We assume that both  $k_h$  and  $k$  are polynomial in the security parameter. For the construction we use an invertible watermarking scheme that is capable of storing  $k + \ell(k_h)$  bits. The construction is as follows:

- **GENKEY** runs **GENSIGN** to obtain a tuple of keys  $\langle K_{SS}, K_{VS} \rangle$ ; furthermore it computes a key  $K_E$  for a symmetric cipher and a random string  $K_W$ . **GENKEY'** outputs the keys  $K_P = K_{SS} \parallel K_W$ ,  $K_V = K_{VS} \parallel K_W$  and  $K_R = K_E \parallel K_W$ .
- **PROTECT**, on input  $O = O_1 \parallel \dots \parallel O_n$ ,  $K_P$  and  $K_R$ , performs the following steps:

```

 $h_0 \leftarrow \text{RANDOM}(\ell(k_h))$ 
for  $i = 1, \dots, n$  do
   $\langle A_{O_i}, B_{O_i} \rangle \leftarrow \text{SEPARATE}(K_W, O_i)$ 
  compress  $B_{O_i}$  to obtain  $C_{O_i}$ 
   $X_i \leftarrow \text{ENCRYPT}(K_E, C_{O_i} \parallel H_h(O_i))$ 
   $s_i \leftarrow \text{SIGN}(K_{SS}, A_{O_i} \parallel X_i \parallel h_{i-1})$ 
   $h_i \leftarrow H(A_{O_i} \parallel X_i \parallel h_{i-1})$ 
  let  $W_i = X_i \parallel h_{i-1} \parallel s_i$ 
   $\overline{O}_i \leftarrow \text{JOIN}(K_W, \langle A_{O_i}, W_i \rangle)$ 
  if  $\overline{O}_i = \text{FAIL}$ , exit with FAIL
end for
output  $\overline{O} = \overline{O}_1 \parallel \dots \parallel \overline{O}_n$ 

```

- **VERIFY**, on input  $\overline{O} = \overline{O}_1 \parallel \dots \parallel \overline{O}_n$  and  $K_V$ , performs the following steps:

```

for  $i = 1, \dots, n$  do
   $\langle A_{\overline{O}_i}, B_{\overline{O}_i} \rangle \leftarrow \text{SEPARATE}(K_W, \overline{O}_i)$ 
   $B_{\overline{O}_i}$  has the form  $X_i \parallel h_{i-1} \parallel s_i$ 
  if  $i > 1$  and  $h_{i-1} \neq \tilde{h}$  exit with FAIL
  let  $\tilde{h} = H_h(A_{\overline{O}_i} \parallel X_i \parallel h_{i-1})$ 
   $b_i \leftarrow \text{SIGVERIFY}(K_{VS}, A_{\overline{O}_i} \parallel X_i \parallel h_{i-1}, s_i)$ 
  if  $b_i = \text{FALSE}$ , exit with FALSE
end for
exit with TRUE

```

- **RECONSTRUCT** applies the reconstruction algorithm of Section 4 on the chunks of  $\overline{O}$ .

## 5.2 Security Against Forgeries

In a similar way as in Theorem 1, the security of the above scheme can be established:

**Theorem 2** *If  $\mathbb{S}$  is a cryptographic signature scheme secure against existential forgery of messages under a chosen message attack and if  $\mathbb{H}$  is a collection of preimage- and collision-resistant hash functions, then the above scheme is a secure online media authentication scheme.*

*Proof.* Suppose, for the sake of contradiction, that there exists an attack SATTACK against the above scheme, which succeeds with a non-negligible probability. We show that in this case there exists also an attack FORGE against  $\mathbb{S}$ , which contradicts the assumption.

We construct the signature forging algorithm FORGE (for the public signature verification key  $K_{VS}$ ) in the following manner. On input  $K_{VS}$ , FORGE first chooses random keys  $K_E$  and  $K_W$ . Finally, FORGE invokes SATTACK. In the rest of the proof, denote with  $O^{(i)}$  the input to the  $i$ -th query to the oracle  $\text{QUERY}_{K_P}$ , whereas  $O_j^{(i)}$  denotes the  $j$ -th chunk of  $O^{(i)}$ ; the number of chunks in  $O^{(i)}$  is given by  $n_i$ .

Whenever SATTACK makes an oracle query  $\text{QUERY}_{K_P}(O^{(i)})$  in order to obtain a signed stream  $\overline{O}^{(i)}$ , given  $O^{(i)} = O_1^{(i)} \parallel \dots \parallel O_{n_i}^{(i)}$ , this query is simulated by the following probabilistic computation that uses a signature oracle  $\text{SIGNQUERY}_{K_{SS}}$  (essentially, this code is equivalent to that of PROTECT):

```

 $s_{i,0} \leftarrow \text{RANDOM}(\ell(h_k))$ 
for  $j = 1, \dots, n_i$  do
     $\langle A_{O_j^{(i)}}, B_{O_j^{(i)}} \rangle \leftarrow \text{SEPARATE}(K_W, O_j^{(i)})$ 
    compress  $B_{O_j^{(i)}}$  to obtain  $C_{O_j^{(i)}}$ 
     $X_j^{(i)} \leftarrow \text{ENCRYPT}(K_E, C_{O_j^{(i)}} \parallel H_h(O_j^{(i)}))$ 
     $s_j^{(i)} \leftarrow \text{SIGNQUERY}_{K_{SS}}(A_{O_j^{(i)}} \parallel X_j^{(i)} \parallel h_{j-1}^{(i)})$ 
     $h_j^{(i)} \leftarrow H_h(A_{O_j^{(i)}} \parallel X_j^{(i)} \parallel h_{j-1}^{(i)})$ 
    let  $W_j^{(i)} = X_j^{(i)} \parallel h_{j-1}^{(i)} \parallel s_j^{(i)}$ 
     $\overline{O}_j^{(i)} \leftarrow \text{JOIN} \left( K_W, \langle A_{O_j^{(i)}}, W_j^{(i)} \rangle \right)$ 
    if  $\overline{O}_j^{(i)} = \text{FAIL}$ , exit with FAIL
end for
output  $\overline{O}^{(i)} = \overline{O}_1^{(i)} \parallel \dots \parallel \overline{O}_{n_i}^{(i)}$ 

```

Up to here, ATTACK perfectly simulates SATTACK. When the simulation of SATTACK is finished it obtains (with non-negligible probability) a tuple  $\langle O, \overline{O} \rangle$ , where  $\overline{O}$  is a signed media stream with  $n$  chunks and  $O \not\leq O^{(i)}$  for all  $1 \leq i \leq l$ . If SATTACK fails, ATTACK fails as well.

Denote with

$$\mathbf{Q} = \{A_{O_j^{(i)}} \parallel X_j^{(i)} \parallel h_{j-1}^{(i)} \mid 1 \leq i \leq l, 1 \leq j \leq n_i\}$$

the set of oracle queries. For all  $1 \leq k \leq n$ , ATTACK runs SEPARATE on  $\overline{O}_k$  and  $K_W$  to obtain  $A_{\overline{O}_k} = A_{O_k}$  and  $B_{\overline{O}_k}$ ; the latter string has the form  $B_{\overline{O}_k} = X_k \parallel h_{k-1} \parallel s_k$ . Consider two cases:

- Case 1: there exists an index  $1 \leq k \leq n$  such that  $A_{O_k} \parallel X_k \parallel h_{k-1} \notin \mathbf{Q}$ . Then, ATTACK outputs the tuple

$$\langle A_{\overline{O}_k} \parallel X_k \parallel h_{k-1}, s_k \rangle$$

as signature forgery. By assumption, this tuple is a valid forgery.

- Case 2: for all indices  $1 \leq k \leq n$  we have  $A_{\overline{O}_k} \parallel X_k \parallel h_{k-1} \in \mathbf{Q}$ . In this case, ATTACK fails. We argue later that this case can happen only with negligible probability.

ATTACK can distinguish the two cases in polynomial time; furthermore, the success probability of ATTACK equals the success probability of SATACK, up to a negligible quantity (resulting out of case 2). This contradicts the assumption.

It remains to show that case 2 happens only with negligible probability. Note that, by assumption,  $O$  (and thus also  $\overline{O}$ ) contains at least two chunks, as otherwise trivially  $O \preceq O^{(i)}$  for some index  $1 \leq i \leq l$ . Consider the last chunk  $\overline{O}_n$ ; its decomposition according to SEPARATE is given by  $\langle A_{\overline{O}_n}, X_n \parallel h_{n-1} \parallel s_n \rangle$ . By assumption, there exist indices  $1 \leq i \leq l$  and  $1 \leq j \leq n_i$  such that

$$A_{O_j^{(i)}} \parallel X_j^{(i)} \parallel h_{j-1}^{(i)} = A_{O_n} \parallel X_n \parallel h_{n-1}.$$

In particular, also  $h_{j-1}^{(i)} = h_{n-1}$ . Distinguish two cases:

- Case (a): We have  $j = 1$ . Now, as both  $\overline{O}$  and  $\overline{O}^{(i)}$  are valid,

$$h_{n-1} = H_h(A_{O_{n-1}} \parallel X_{n-1} \parallel h_{n-2}).$$

By assumption,  $h_{n-1} = h_0^{(i)}$ , which shows that  $A_{O_{n-1}} \parallel X_{n-1} \parallel h_{n-2}$  is a pre-image of the random string  $h_0^{(i)}$ .

- Case (b): We have  $j > 1$ . Again, as both  $\overline{O}$  and  $\overline{O}^{(i)}$  are valid,

$$h_{n-1} = H_h(A_{O_{n-1}} \parallel X_{n-1} \parallel h_{n-2})$$

and

$$h_{j-1}^{(i)} = H_h(A_{O_{j-1}^{(i)}} \parallel X_{j-1}^{(i)} \parallel h_{j-2}^{(i)}).$$

By assumption,  $h_{n-1} = h_{j-1}^{(i)}$ . If  $A_{O_{n-1}} \parallel X_{n-1} \parallel h_{n-2} \neq A_{O_{j-1}^{(i)}} \parallel X_{j-1}^{(i)} \parallel h_{j-2}^{(i)}$ , we have found a collision of  $H_h$ . Otherwise,  $A_{O_{n-1}} = A_{O_{j-1}^{(i)}}$ ,  $h_{n-2} = h_{j-2}^{(i)}$  and  $X_{n-1} = X_{j-1}^{(i)}$ .

The latter equation implies

$$\underbrace{\text{ENCRYPT}(K_E, C_{O_{n-1}} \parallel H(O_{n-1}))}_{X_{n-1}} = \underbrace{\text{ENCRYPT}(K_E, C_{O_{j-1}^{(i)}} \parallel H(O_{j-1}^{(i)}))}_{X_{j-1}^{(i)}}.$$

Since ENCRYPT is uniquely decipherable,  $C_{O_{n-1}} = C_{O_{j-1}^{(i)}}$ , implying that  $B_{O_{n-1}} = B_{O_{j-1}^{(i)}}$ . This shows that now  $O$  and  $O^{(i)}$  also agree on their second-last chunk. By assumption,  $O$  must therefore have at least one more chunk (as otherwise trivially  $O \preceq O^{(i)}$ ). Applying this argument inductively, we either find a collision or have  $n > j$ . In the latter case, as in case (a),  $A_{O_{n-j-1}} \parallel X_{n-j-1} \parallel h_{n-j-2}$  is a pre-image of  $h_0^{(i)}$ .

In summary, if case 2 happens, then we can either find a pre-image of a random string with respect to  $H_h$  or a collision of  $H_h$  (a formal proof of this claim uses again a reducibility argument). By the assumptions on  $\mathbb{H}$ , this can happen only with negligible probability. This completes the proof.  $\square$

## 6 Conclusions

Digital watermarking used to be dominated by signal processing approaches which typically did not provide any formal security guarantees. Currently, there is a trend to substantiate watermarking technology with a cryptographic foundation. In addition, the issue of data authenticity and data integrity for multimedia applications has become an active research topic in the watermarking community.

In this paper, we provide an approach which solves the data integrity problem for multimedia applications by combining methods from cryptography and watermarking. In particular, we present an offline media authentication scheme, an appropriate attacker model, and a security proof with respect to this attacker model. Furthermore, we provide an authentication scheme for online media streaming applications which has the following two properties: First, it is possible to verify the integrity and authenticity of an arbitrary excerpt of the signed object. Second, the generation of an excerpt is possible without access to the secret signing keys.

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