



Using block ciphers

Security for many-time key

Example applications:

1. File systems: Same AES key used to encrypt many files.
2. IPsec: Same AES key used to encrypt many packets.

Semantic Security for many-time key

Key used more than once \Rightarrow adv. sees many CTs with same key

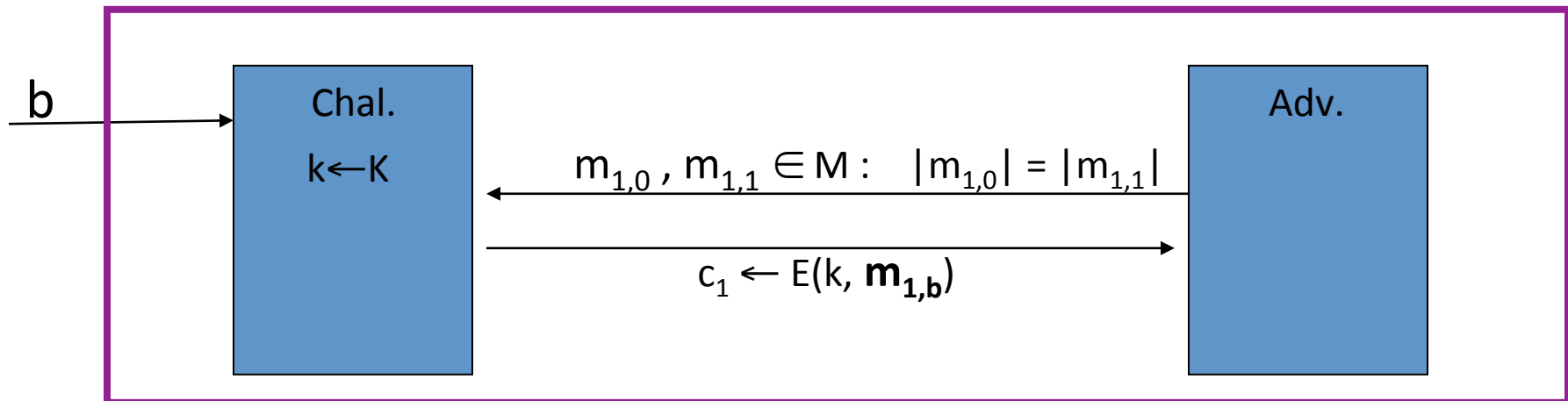
Adversary's power: chosen-plaintext attack (CPA)

- Can obtain the encryption of arbitrary messages of his choice
(conservative modeling of real life)

Adversary's goal: Break semantic security

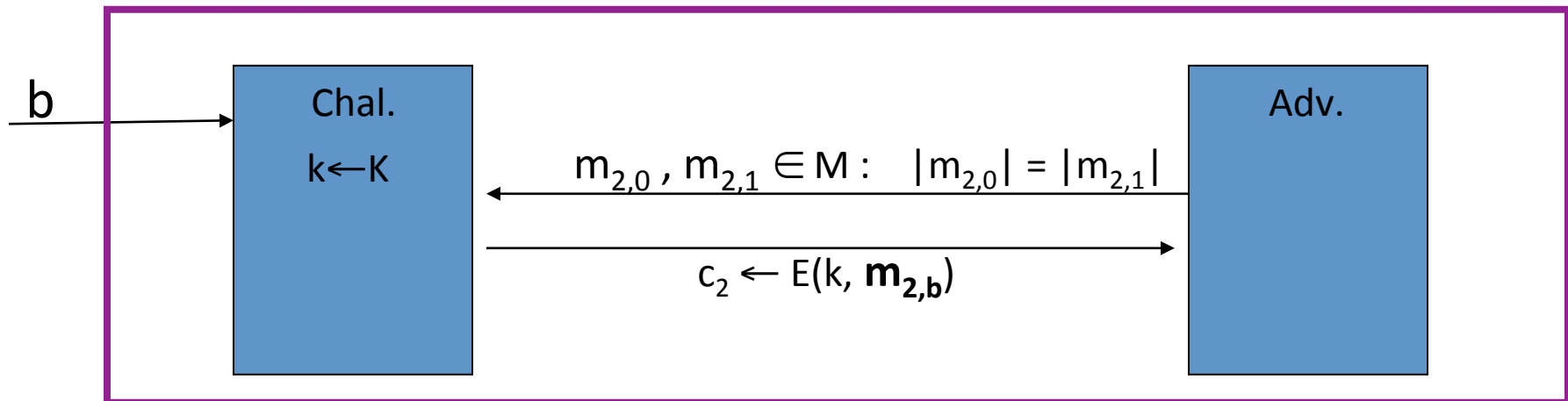
Semantic Security for many-time key

$E = (E, D)$ a cipher defined over (K, M, C) . For $b=0,1$ define $\text{EXP}(b)$ as:



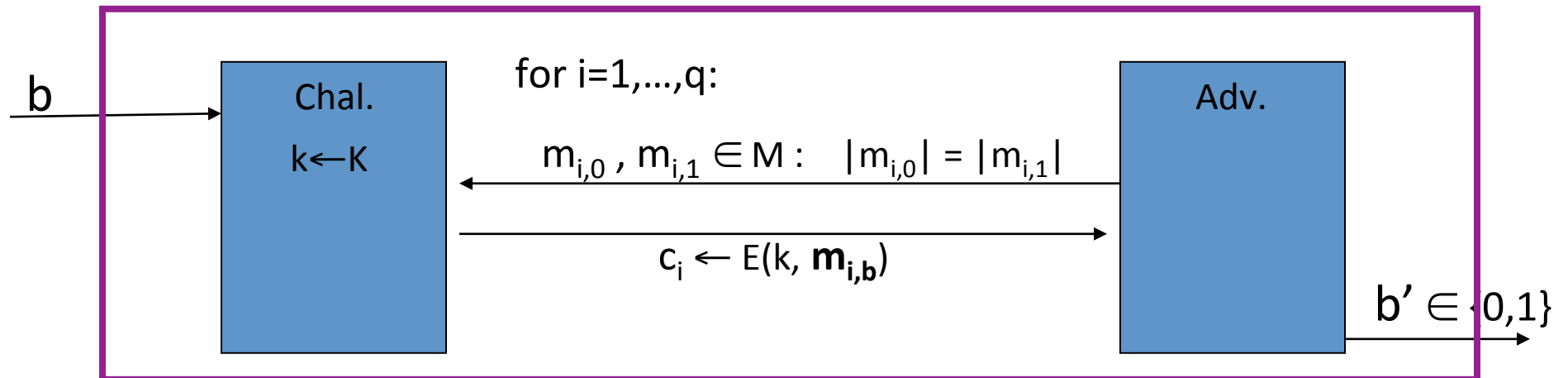
Semantic Security for many-time key

$E = (E, D)$ a cipher defined over (K, M, C) . For $b=0,1$ define $\text{EXP}(b)$ as:



Semantic Security for many-time key (CPA security)

$E = (E, D)$ a cipher defined over (K, M, C) . For $b=0,1$ define $\text{EXP}(b)$ as:



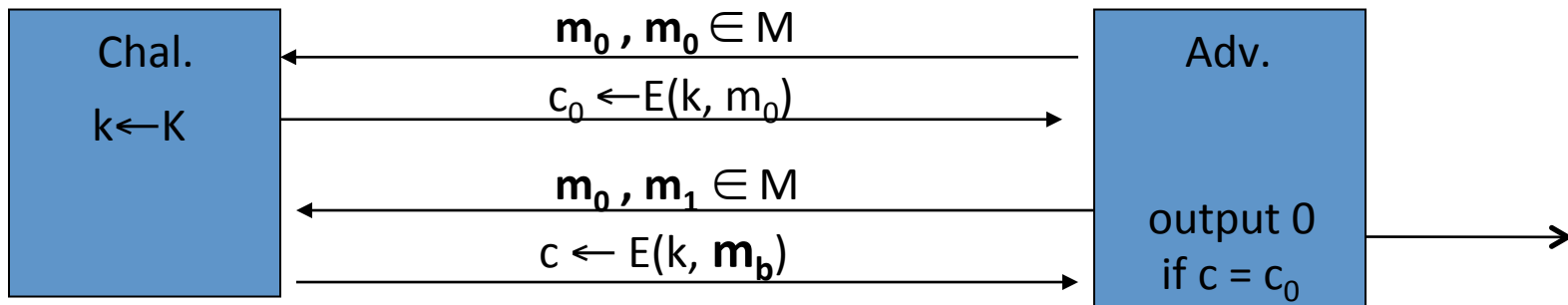
if adv. wants $c = E(k, m)$ it queries with $m_{j,0} = m_{j,1} = m$

Def: E is sem. sec. under CPA if for all “efficient” A :

$$\text{Adv}_{\text{CPA}}[A, E] = \left| \Pr[\text{EXP}(0)=1] - \Pr[\text{EXP}(1)=1] \right| \text{ is “negligible.”}$$

Ciphers insecure under CPA

Suppose $E(k,m)$ always outputs same ciphertext for msg m . Then:

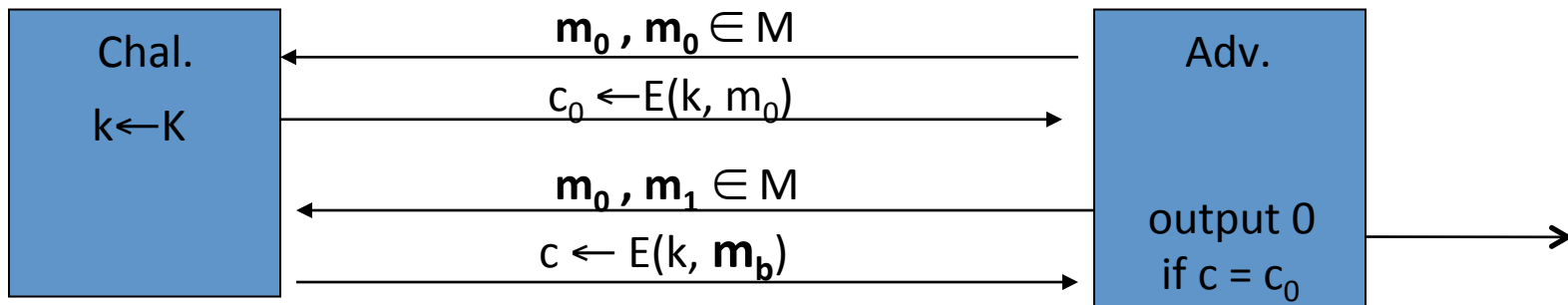


So what? an attacker can learn that two encrypted files are the same, two encrypted packets are the same, etc.

- Leads to significant attacks when message space M is small

Ciphers insecure under CPA

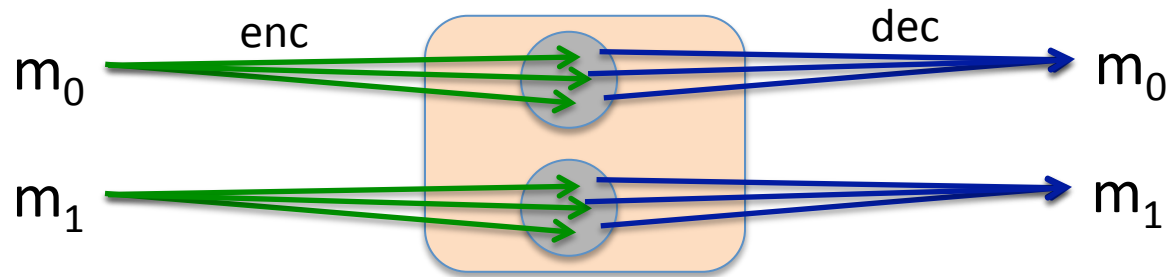
Suppose $E(k,m)$ always outputs same ciphertext for msg m . Then:



If secret key is to be used multiple times \Rightarrow
given the same plaintext message twice,
encryption must produce different outputs.

Solution 1: randomized encryption

- $E(k,m)$ is a randomized algorithm:



⇒ encrypting same msg twice gives different ciphertexts (w.h.p)

⇒ ciphertext must be longer than plaintext

Roughly speaking: CT-size = PT-size + “# random bits”

Let $F: K \times R \rightarrow M$ be a secure PRF.

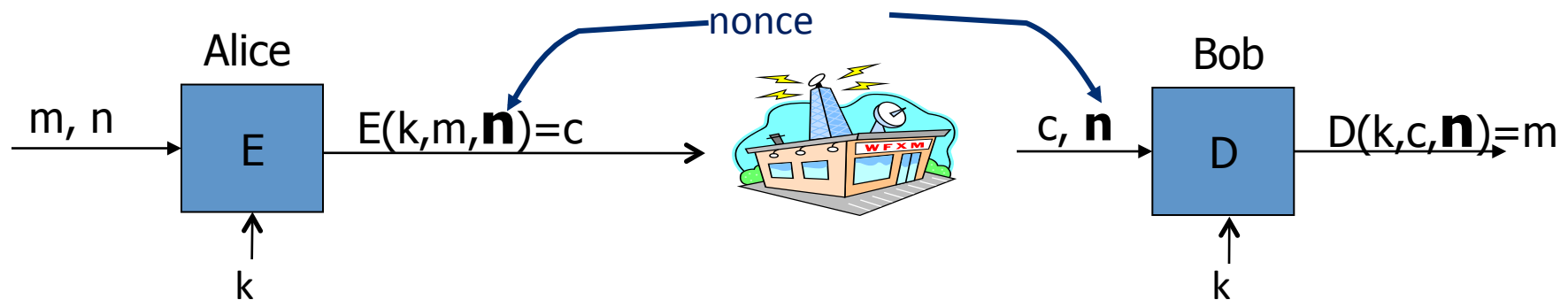
$$\approx_p (r, F(k,r) \oplus m)$$

For $m \in M$ define $E(k,m) = [r \xleftarrow{R} R, \text{ output } (r, F(k,r) \oplus m)]$

Is E semantically secure under CPA?

- ☐ Yes, whenever F is a secure PRF
- ☐ No, there is always a CPA attack on this system
- ☒ Yes, but only if R is large enough so r never repeats (w.h.p)
- ☐ It depends on what F is used

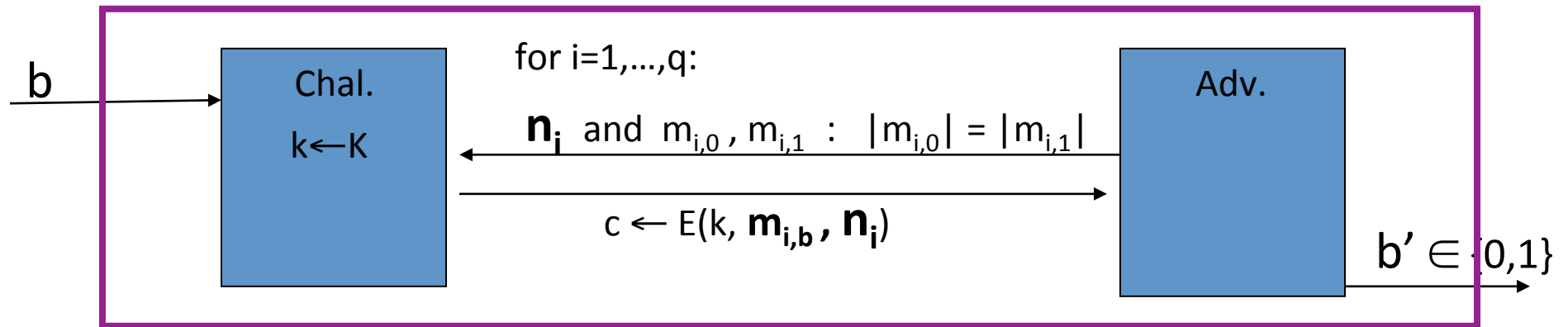
Solution 2: nonce-based Encryption



- nonce n : a value that changes from msg to msg.
(k, n) pair never used more than once
- method 1: nonce is a **counter** (e.g. packet counter)
 - used when encryptor keeps state from msg to msg
 - if decryptor has same state, need not send nonce with CT
- method 2: encryptor chooses a **random nonce**, $n \leftarrow \mathcal{N}$

CPA security for nonce-based encryption

System should be secure when nonces are chosen adversarially.



All nonces $\{n_1, \dots, n_q\}$ must be distinct.

Def: nonce-based E is sem. sec. under CPA if for all “efficient” A :

$$\text{Adv}_{\text{nCPA}}[A, E] = \left| \Pr[\text{EXP}(0)=1] - \Pr[\text{EXP}(1)=1] \right| \text{ is “negligible.”}$$

Let $F: K \times R \rightarrow M$ be a secure PRF. Let $r = 0$ initially.

For $m \in M$ define $E(k, m) = [r++, \text{ output } (r, F(k, r) \oplus m)]$

Is E CPA secure nonce-based encryption?

$\approx_p (r, F(r) \oplus m)$

- ☐ Yes, whenever F is a secure PRF
- ☐ No, there is always a nonce-based CPA attack on this system
- ☐ Yes, but only if R is large enough so r never repeats
- ☐ It depends on what F is used

End of Segment