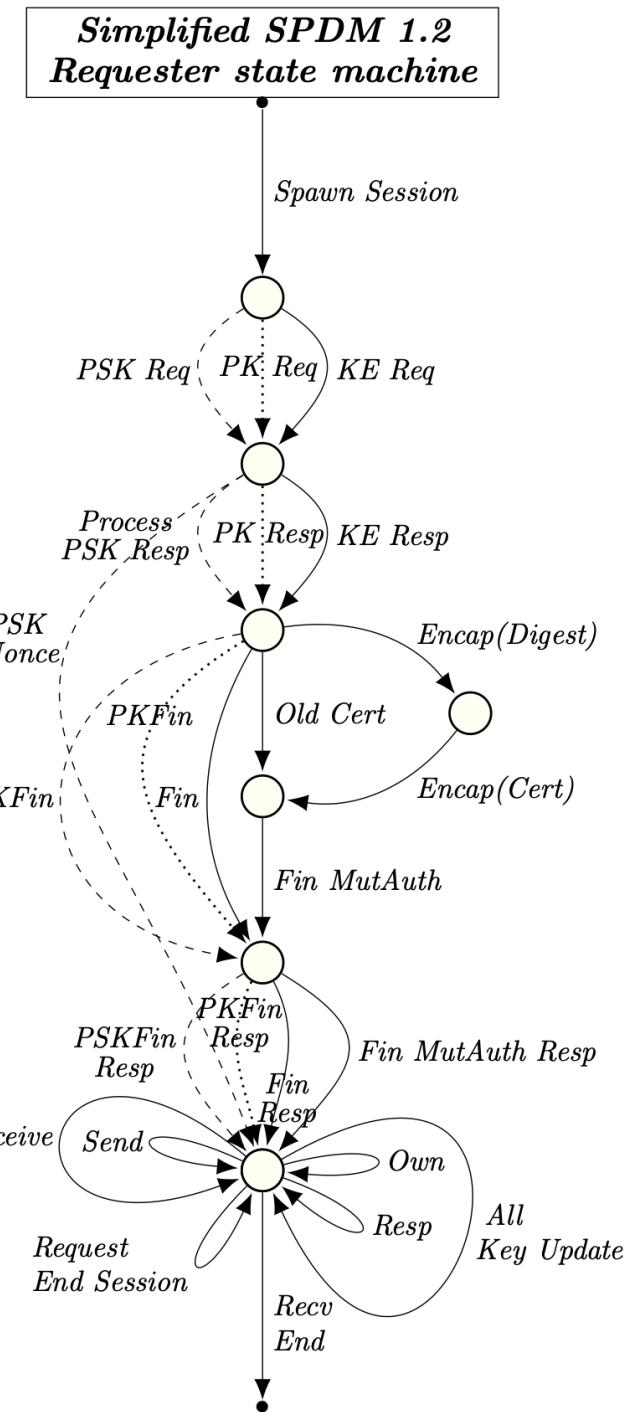




# Protocol analysis using Tam

Cas Cremers

May 4, CAPS workshop, Eurocrypt 2025





# Tamarin prover





# Tamarin prover



**Constraint solver**



# Tamarin prover





# Tamarin prover

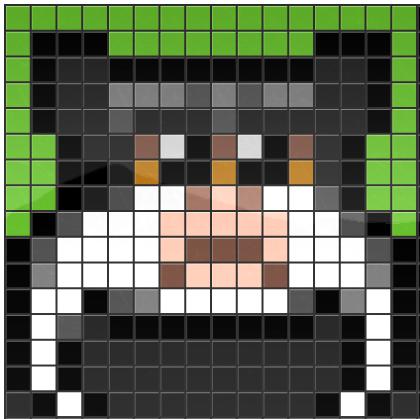


Emperor Tamarin



# Tamarin prover

Development started around 2010 at ETH



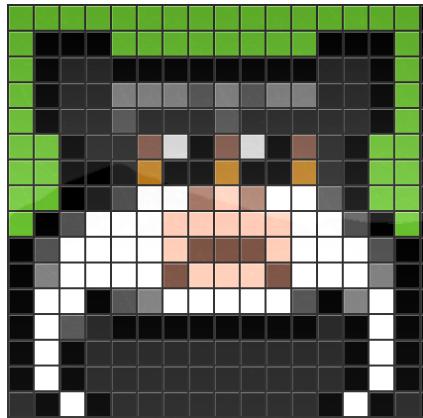
[tamarin-prover.com](http://tamarin-prover.com)

Current development core:

- CISPA (Cas Cremers)
- ETH Zurich (David Basin, Ralf Sasse)
- INRIA (Jannik Dreier)



# Tamarin prover



[tamarin-prover.com](http://tamarin-prover.com)

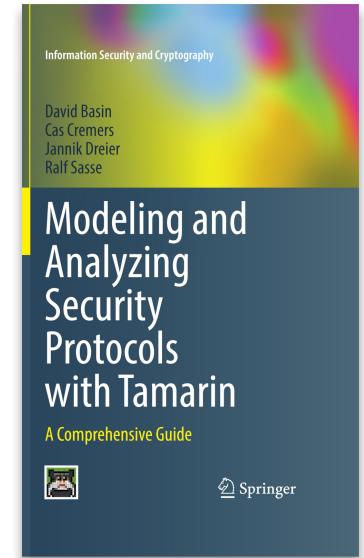
Development started around 2010 at ETH

Current development core:

- CISPA (Cas Cremers)
- ETH Zurich (David Basin, Ralf Sasse)
- INRIA (Jannik Dreier)

Open-source development, with

- Manual
- Online tutorials
- Active mailing list
- Syntax highlighting (vim, VSC, ...)
- Upcoming **book!** *Free for download*  
“Modeling and Analyzing Security Protocols with Tamarin: A Comprehensive Guide”





# Attacks Tamarin can find or prove absent

- Large attack scenarios (TLS 1.3 Rev 10: 18 messages)
- Cross-protocol attacks
- Unintended state machine transitions
- Downgrade attacks
- Nonce-reuse attacks (eg WiFi with AES-GCM)
- Invalid Curve Points
- Small order points
- DSKS attacks (Duplicate Signature Key Selection)
- Length extension attacks
- Maliciously generated keys
- Hybrid schemes



# Attacks Tamarin can find or prove absent

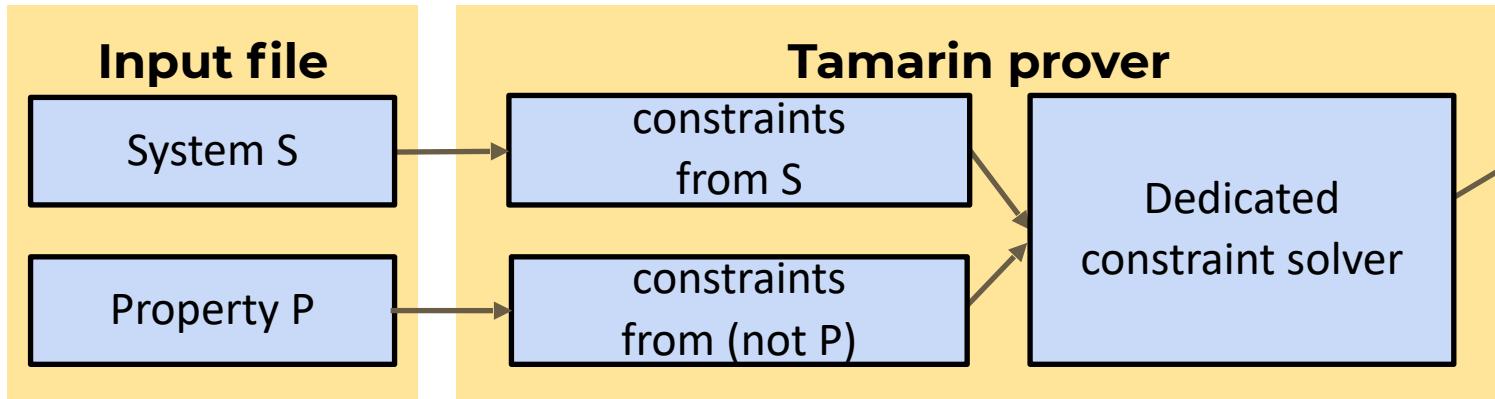
- Large attack scenarios (TLS 1.3 Rev 10: 18 messages)
- Cross-protocol attacks
- Unintended state machine transitions
- Downgrade attacks
- Nonce-reuse attacks (eg WiFi with AES-GCM)
- Invalid Curve Points
- Small order points
- DSKS attacks (Duplicate Signature)
- Length extension attacks
- Maliciously generated keys
- Hybrid schemes

**These attack types are NOT hard-coded!**

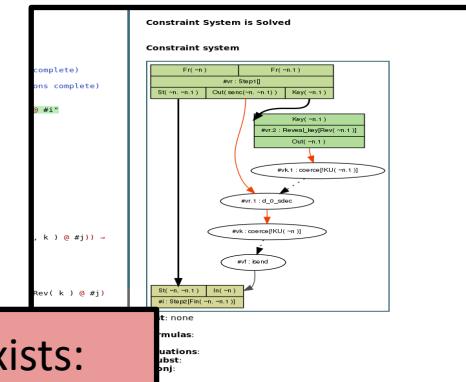
**Tamarin finds these through systematic, accurate modeling of cryptography and protocols.**



# Tamarin prover: workflow

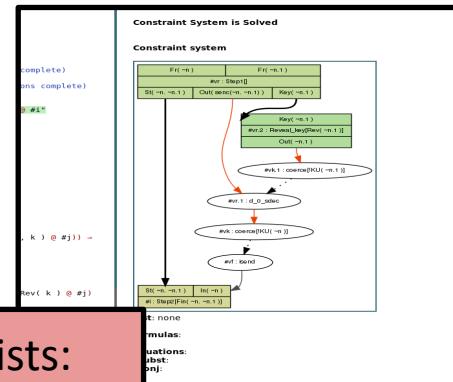
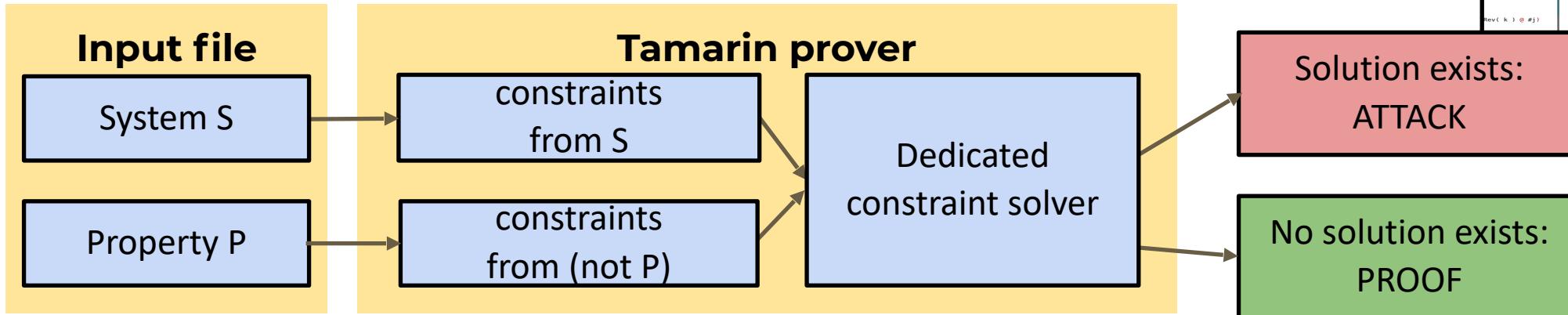


Solution exists:  
ATTACK



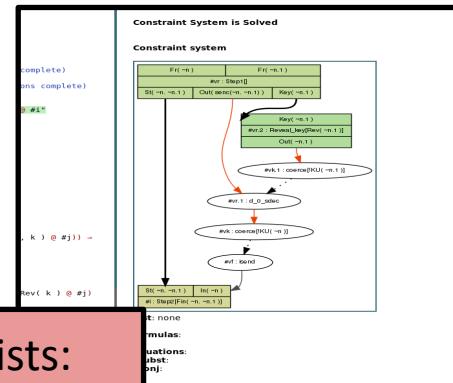
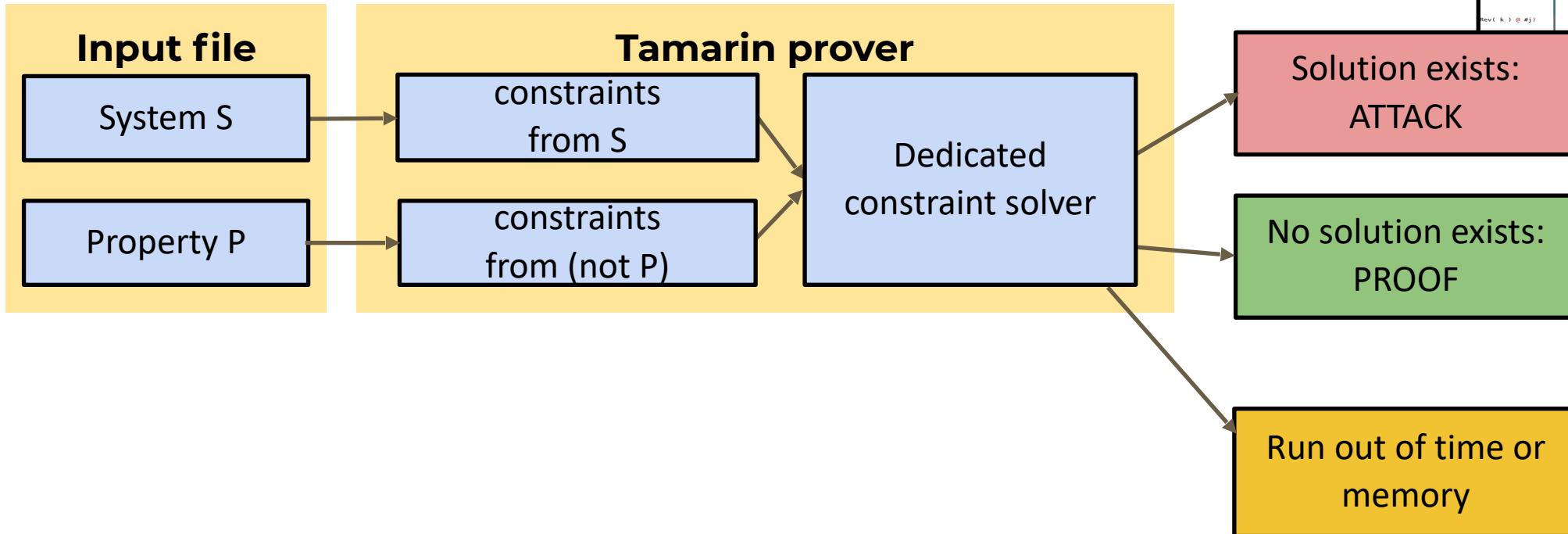


# Tamarin prover: workflow



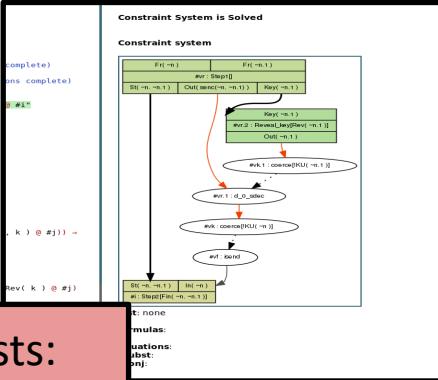
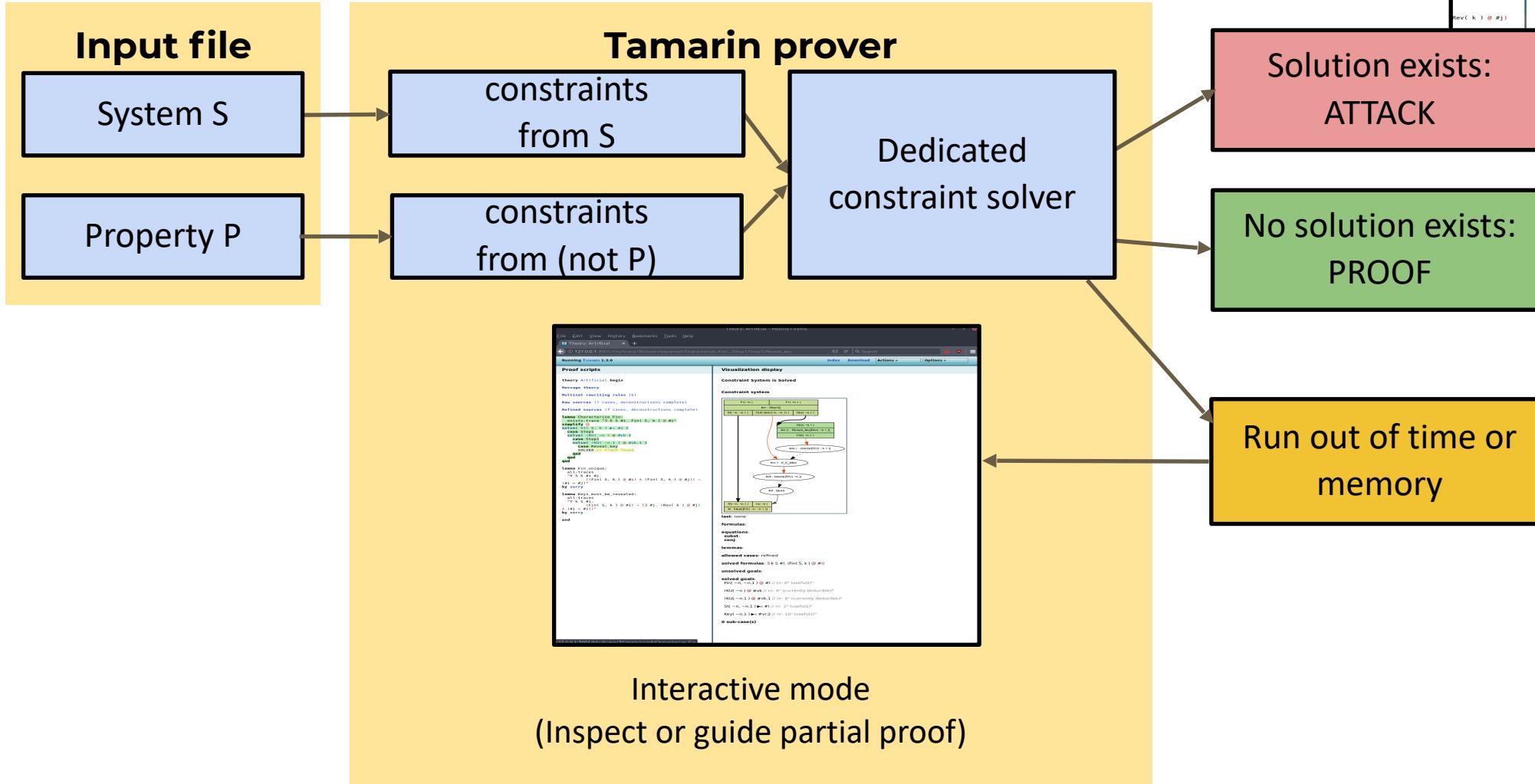


# Tamarin prover: workflow





# Tamarin prover: workflow





# Tamarin prover: workflow

Input file

System S

Property P

Tamarin prover

constraints  
from S

constraints  
from ( $\neg$  P)

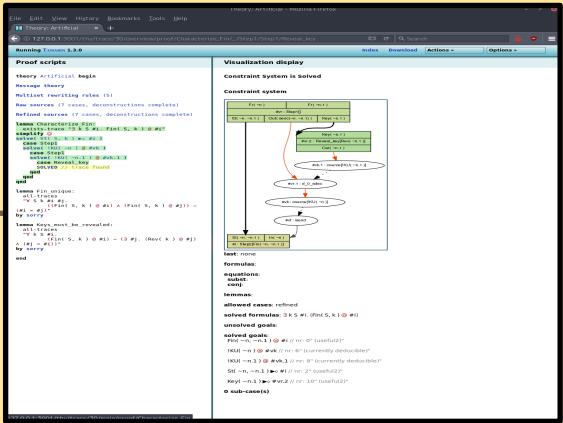
Dedicated  
constraint solver

Solution exists:  
ATTACK

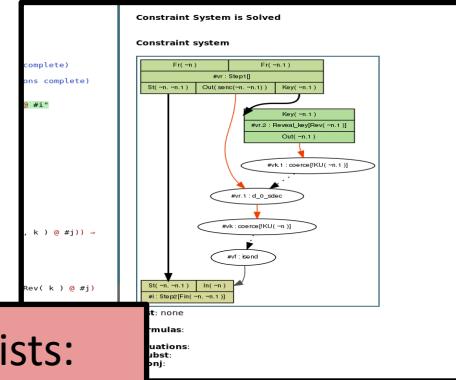
No solution exists:  
PROOF

Run out of time or  
memory

Provide **hints** for  
the prover  
(e.g. invariants)

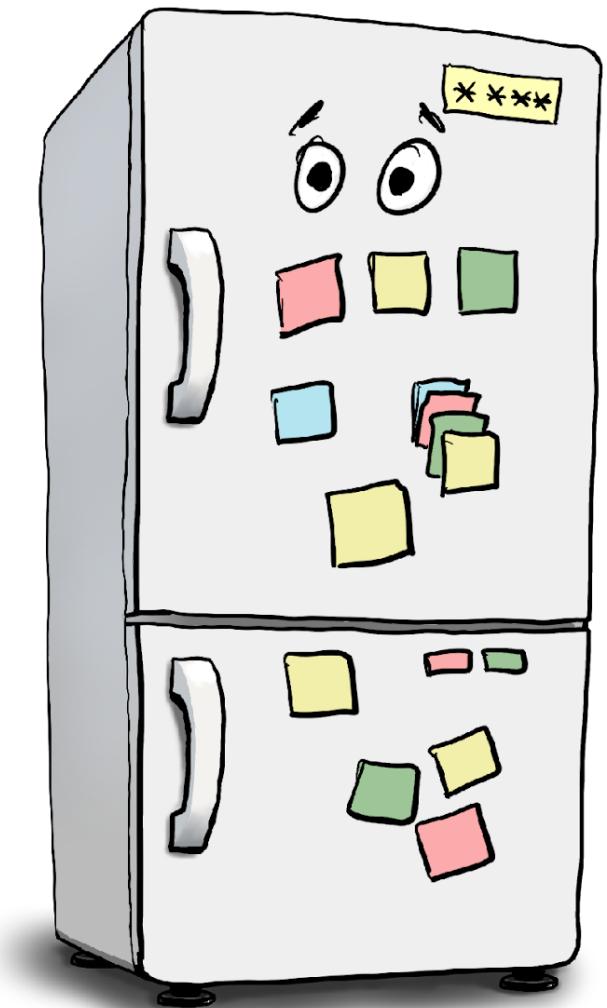


Interactive mode  
(Inspect or guide partial proof)





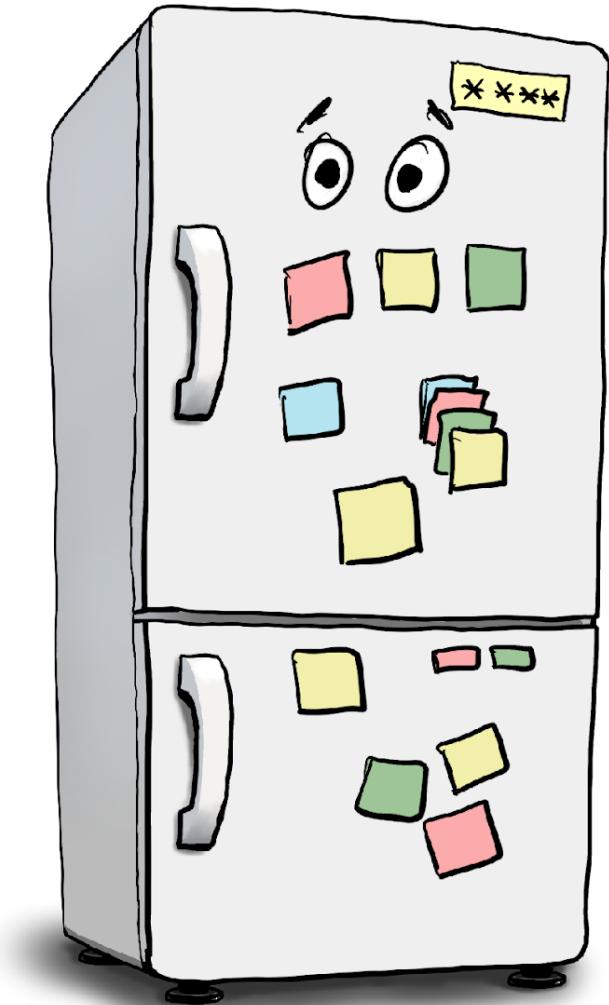
# Modeling in Tamarin: transition system





# Modeling in Tamarin: transition system

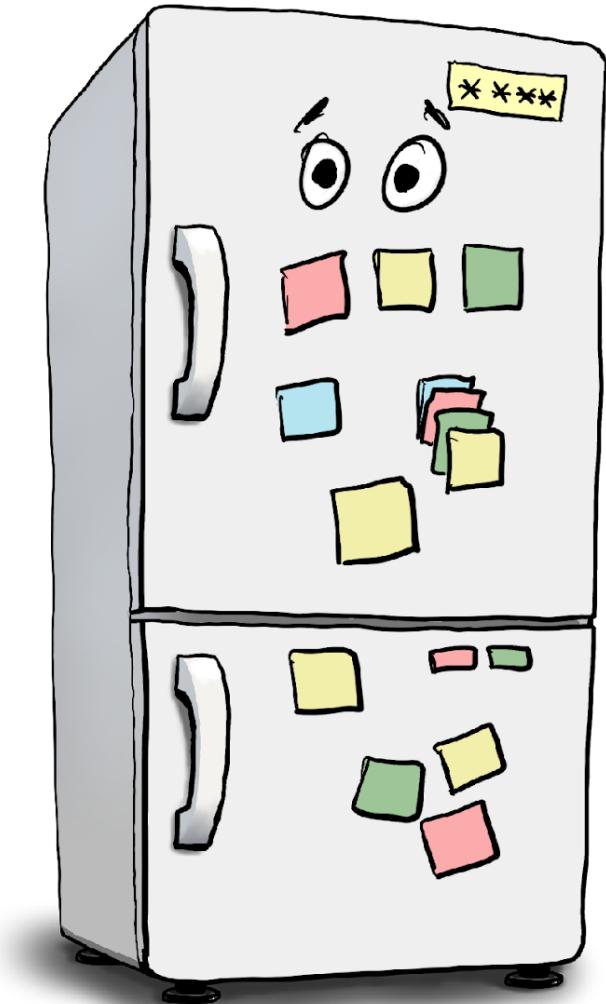
- Basic ingredients:
  - **Terms** (think “messages”)
  - **Facts** (think “sticky notes on the fridge”)
  - Special facts: **Fr(t)**, **In(t)**, **Out(t)**, **K(t)**





# Modeling in Tamarin: transition system

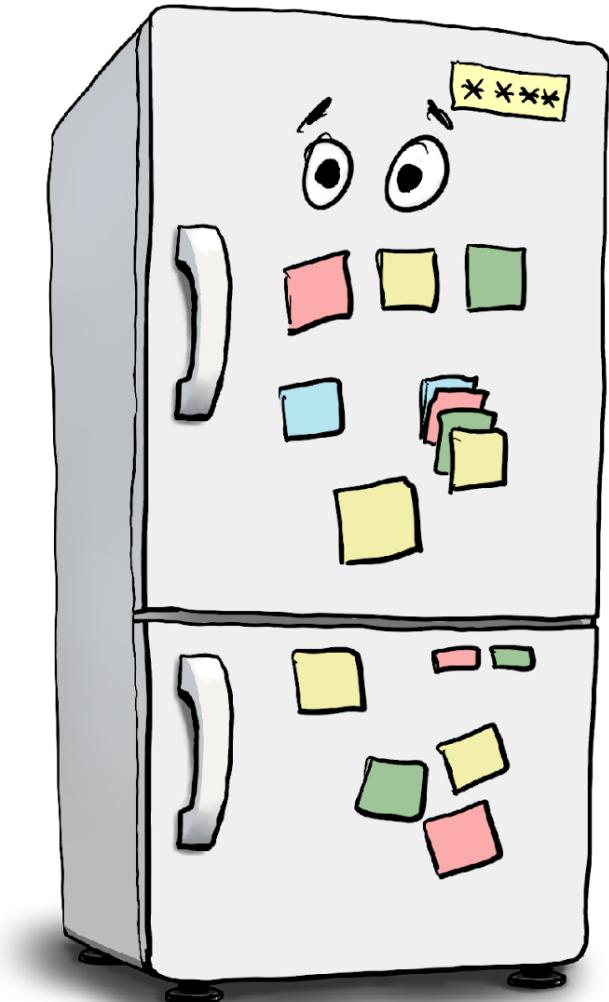
- Basic ingredients:
  - **Terms** (think “messages”)
  - **Facts** (think “sticky notes on the fridge”)
  - Special facts: **Fr(t)**, **In(t)**, **Out(t)**, **K(t)**
- State of system is a multiset of facts
  - **Initial state** is the empty multiset
  - **Rules** specify the transition rules (“moves”)





# Modeling in Tamarin: transition system

- Basic ingredients:
  - **Terms** (think “messages”)
  - **Facts** (think “sticky notes on the fridge”)
  - Special facts: **Fr(t)**, **In(t)**, **Out(t)**, **K(t)**
- State of system is a multiset of facts
  - **Initial state** is the empty multiset
  - **Rules** specify the transition rules (“moves”)
- Rules are of the form:
  - |  $\rightarrow r$
  - |  $\text{--[ } a \text{ ]} \rightarrow r$





# The model



# The model

- **Term algebra**
  - $\text{enc}(\_, \_), \text{dec}(\_, \_), \text{h}(\_, \_)$ ,  
 $\underline{\wedge} \underline{\phantom{x}}$ ,  $\underline{\phantom{x}}^{-1}$ ,  $\underline{\phantom{x}}^*$ ,  $\underline{1}$ , ...



# The model

- **Term algebra**

- $\text{enc}(\_, \_), \text{dec}(\_, \_), h(\_, \_)$ ,
  - $\underline{\wedge}$ ,  $\underline{-1}$ ,  $\underline{*}$ ,  $\underline{1}$ , ...

- **Equational theory**

- $\text{dec}(\text{enc}(m, k), k) =_E m$ ,
  - $(x^\wedge y)^\wedge z =_E x^\wedge (y^* z)$ ,
  - $(x^{-1})^{-1} =_E x$ , ...



# The model

- **Term algebra**

- $\text{enc}(\_,\_), \text{dec}(\_,\_), h(\_,\_),$   
 $\underline{\wedge}, \underline{-1}, \underline{*}, \underline{1}, \dots$

- **Equational theory**

- $\text{dec}(\text{enc}(m,k),k) =_E m,$
  - $(x \wedge y) \wedge z =_E x \wedge (y * z),$
  - $(x^{-1})^{-1} =_E x, \dots$

- **Facts**

- $F(t_1, \dots, t_n)$



# The model

- **Term algebra**

- $\text{enc}(\_,\_), \text{dec}(\_,\_), h(\_,\_),$   
 $\underline{\wedge}, \underline{-1}, \underline{*}, 1, \dots$

- **Equational theory**

- $\text{dec}(\text{enc}(m,k),k) =_E m,$
- $(x^y)^z =_E x^{(y^z)},$
- $(x^{-1})^{-1} =_E x, \dots$

- **Facts**

- $F(t_1, \dots, t_n)$

- **Transition system**

- State: multiset of facts
- Rules:  $I -[ a ] \rightarrow r$

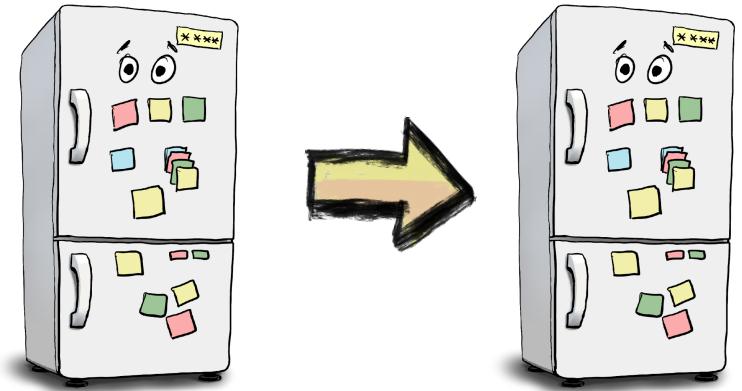


# The model

- **Term algebra**
  - $\text{enc}(\_, \_), \text{dec}(\_, \_), \text{h}(\_, \_)$ ,
  - $\underline{\wedge}$ ,  $\underline{-1}$ ,  $\underline{*}$ ,  $\underline{1}$ , ...
- **Equational theory**
  - $\text{dec}(\text{enc}(m, k), k) =_E m$ ,
  - $(x \wedge y) \wedge z =_E x \wedge (y * z)$ ,
  - $(x^{-1})^{-1} =_E x$ , ...
- **Facts**
  - $F(t_1, \dots, t_n)$
- **Transition system**
  - State: multiset of facts
  - Rules:  $I -[ a ] \rightarrow r$
- **Tamarin-specific**
  - Built-in Dolev-Yao attacker rules:  
 $\text{In}(\ )$ ,  
 $\text{Out}(\ )$ ,  
 $K(\ )$
  - Special **Fresh** rule:
    - $[] --[] \rightarrow [ Fr(x) ]$
    - Constraint on system such that **x** is unique



# Semantics



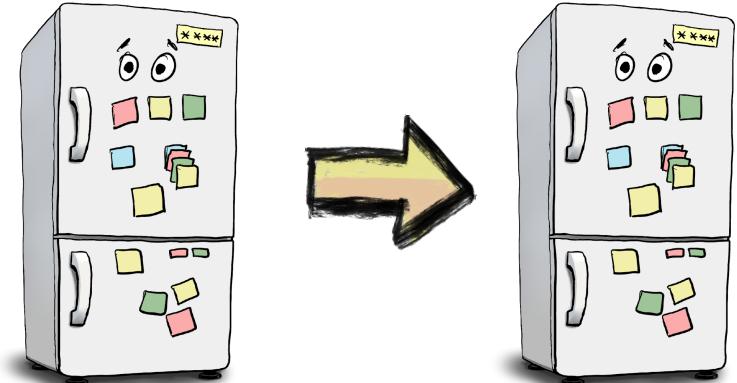


# Semantics

- **Transition relation**

$S -[a] \rightarrow_R ((S \setminus^{\#} I) \cup^{\#} r)$  , where

- $I -[a] \rightarrow r$  is a ground instance of a rule in  $R$ , and
- $I \subseteq^{\#} S$  w.r.t. the equational theory





# Semantics

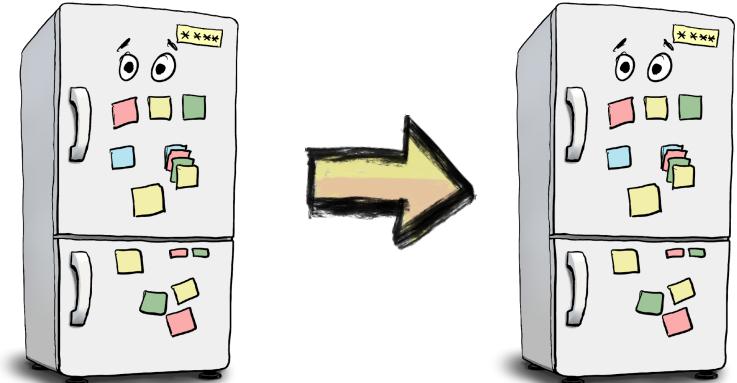
- **Transition relation**

$S -[a] \rightarrow_R ((S \setminus^{\#} I) \cup^{\#} r)$ , where

- $I -[a] \rightarrow r$  is a ground instance of a rule in  $R$ , and
- $I \subseteq^{\#} S$  w.r.t. the equational theory

- **Executions**

$$\begin{aligned} \text{-Exec}(R) = & \{ [ ] -[a_1] \rightarrow \dots -[a_n] \rightarrow S_n \\ & | \forall n . Fr(n) \text{ appears only once on right-hand side of rule} \} \end{aligned}$$



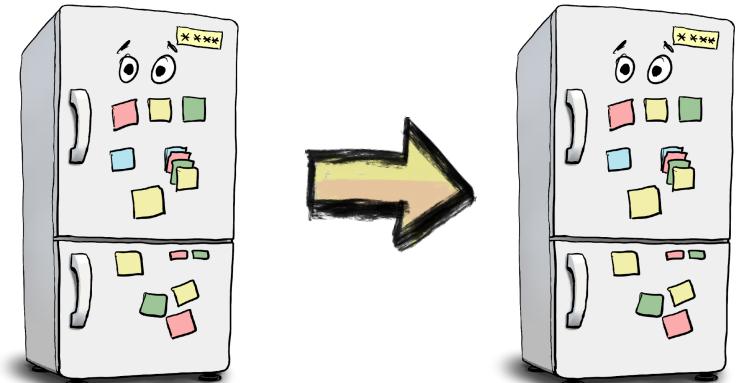


# Semantics

- **Transition relation**

$S -[a] \rightarrow_R ((S \setminus^{\#} I) \cup^{\#} r)$ , where

- $I -[a] \rightarrow r$  is a ground instance of a rule in  $R$ , and
- $I \subseteq^{\#} S$  w.r.t. the equational theory



- **Executions**

- $\text{Exec}(R) = \{ [ ] -[a_1] \rightarrow \dots -[a_n] \rightarrow S_n \mid \forall n . Fr(n) \text{ appears only once on right-hand side of rule} \}$

- **Traces**

- $\text{Traces}(R) = \{ [a_1, \dots, a_n] \mid [ ] -[a_1] \rightarrow \dots -[a_n] \rightarrow S_n \in \text{Exec}(R) \}$

-Property specification using first-order logic over traces



# Semantics: example 1

'c'

constant



# Semantics: example 1

'c' constant

- Rules

- rule 1: [ ] –[ Init() ] $\rightarrow$  [ A('5') ]
  - rule 2: [ A(x) ] –[ Step(x) ] $\rightarrow$  [ B(x) ]



# Semantics: example 1

'c'

constant

- Rules

- rule 1: [ ]       $\neg[\text{Init}()] \rightarrow [\text{A('5')}]$
- rule 2: [ A(x) ]  $\neg[\text{Step}(x)] \rightarrow [\text{B}(x)]$

- Execution example

- [ ]
- $\neg[\text{Init}()] \rightarrow [\text{A('5')}]$
- $\neg[\text{Init}()] \rightarrow [\text{A('5')}, \text{A('5')}]$
- $\neg[\text{Step('5')}] \rightarrow [\text{A('5')}, \text{B('5')}]$



# Semantics: example 1

'c' constant

- Rules

- rule 1: [ ]  $\neg [ \text{Init}() ] \rightarrow [ A('5') ]$
- rule 2: [ A(x) ]  $\neg [ \text{Step}(x) ] \rightarrow [ B(x) ]$

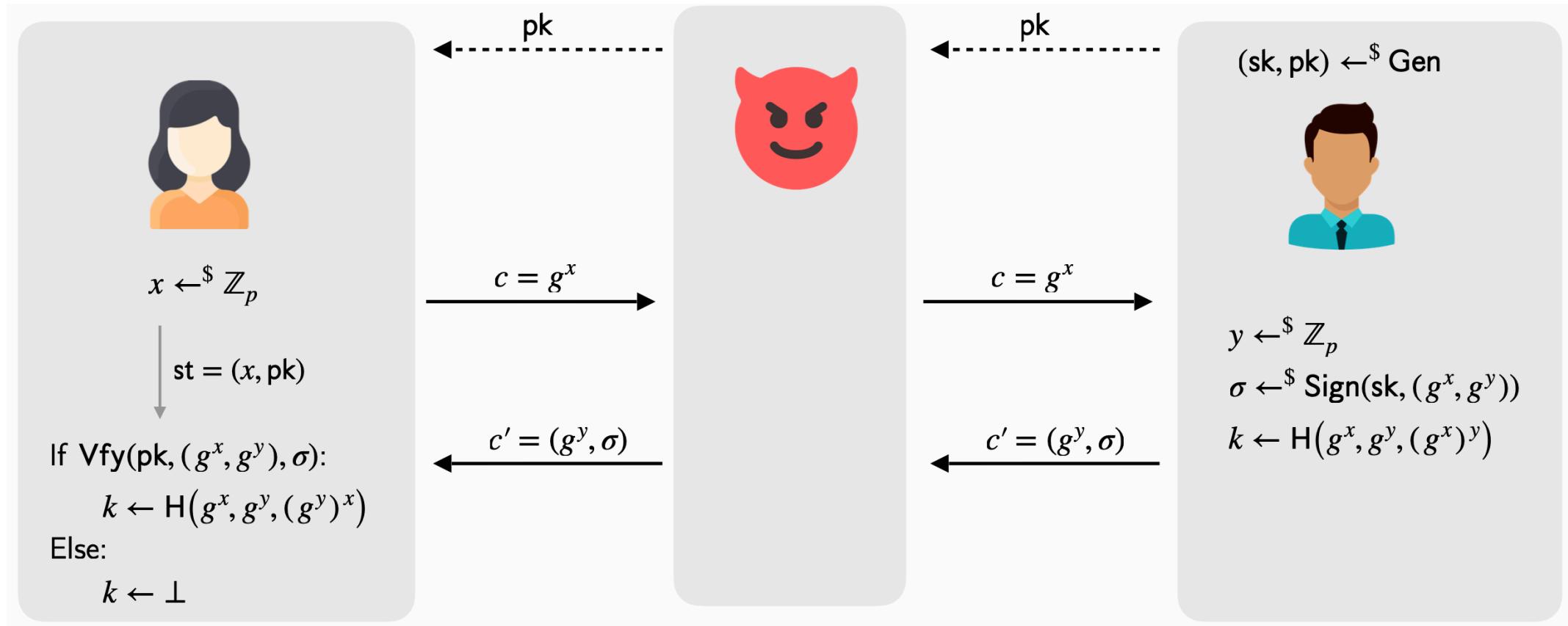
- Execution example

- [ ]
- $\neg [ \text{Init}() ] \rightarrow [ A('5') ]$
- $\neg [ \text{Init}() ] \rightarrow [ A('5'), A('5') ]$
- $\neg [ \text{Step}('5') ] \rightarrow [ A('5'), B('5') ]$

- Corresponding trace: [ Init(), Init(), Step('5') ]



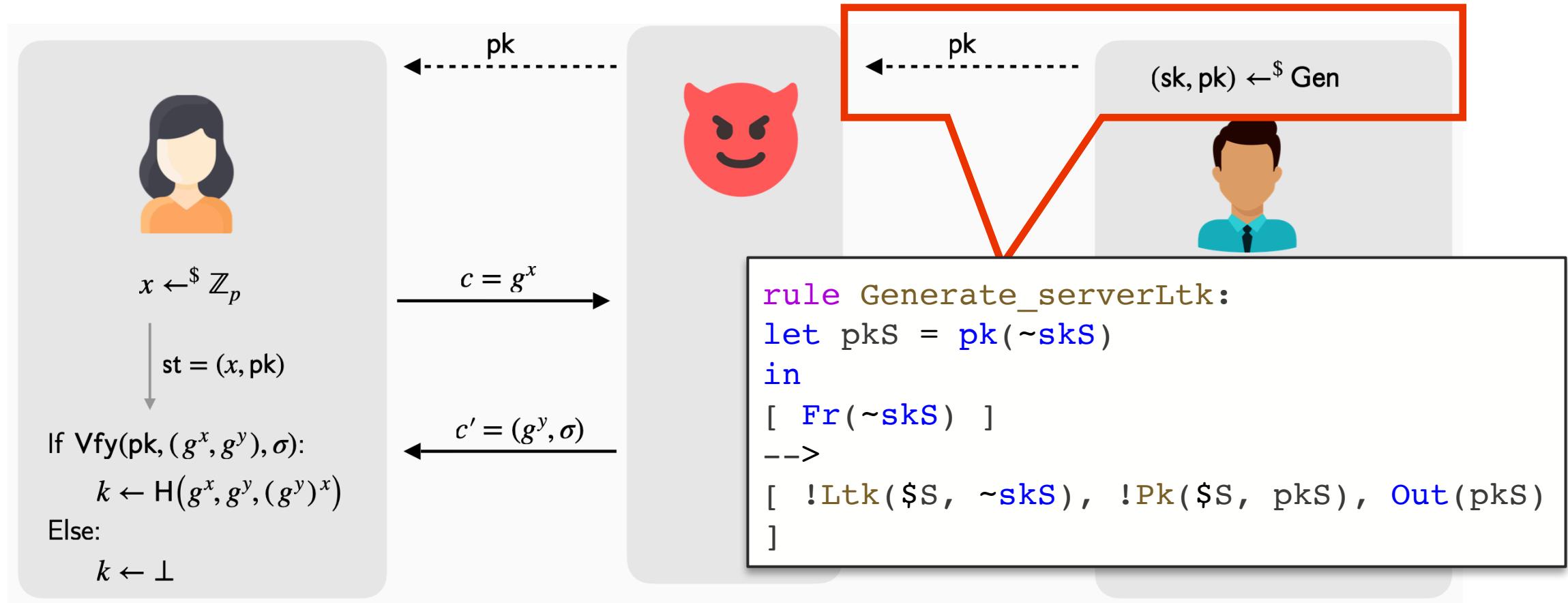
# Unilateral signed Diffie-Hellman





# Key setup

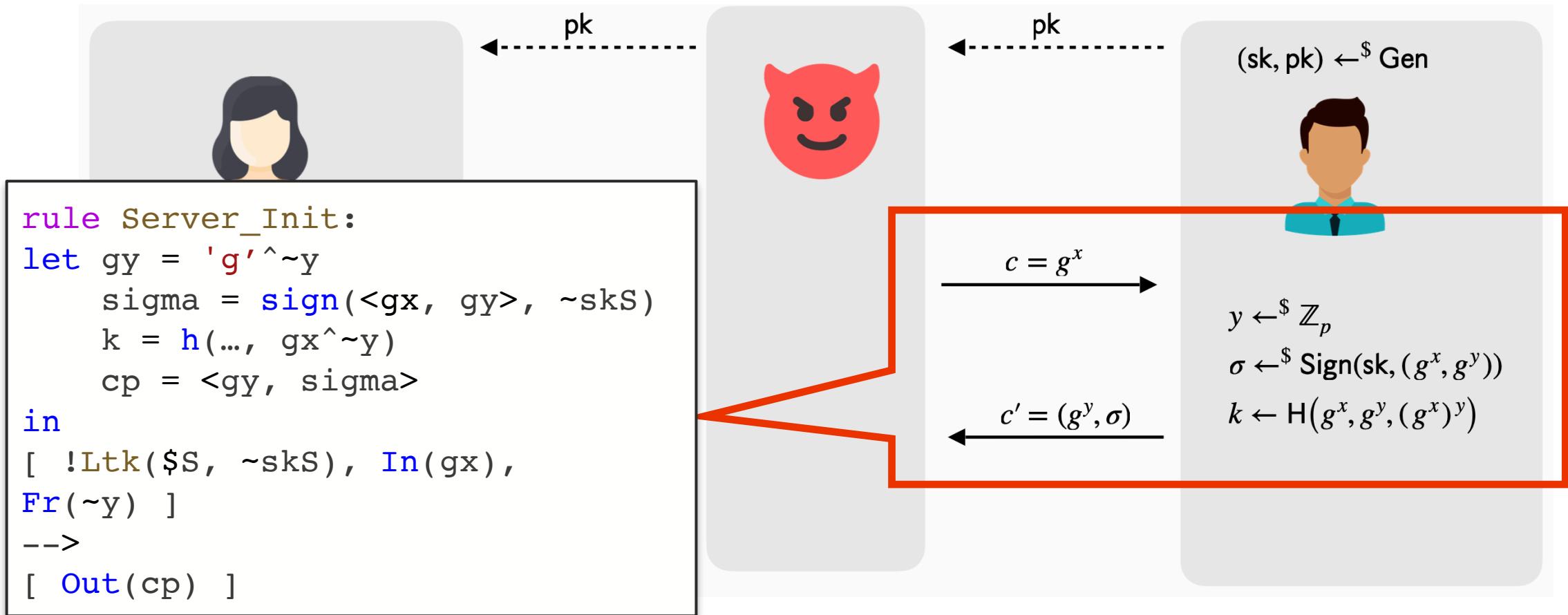
'c'	constant
$\sim x$	fresh type
$\$x$	public type





# Server

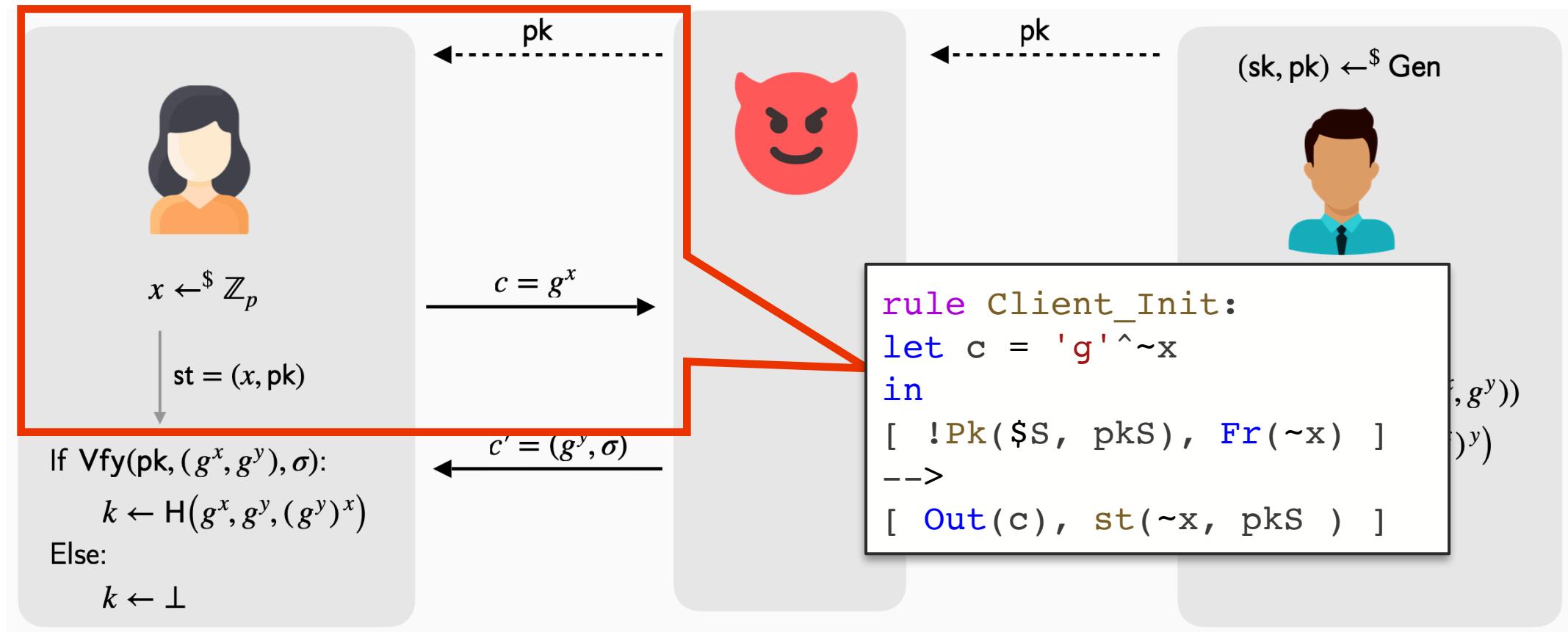
'c'	constant
$\sim x$	fresh type
$\$x$	public type





# Client (1/2)

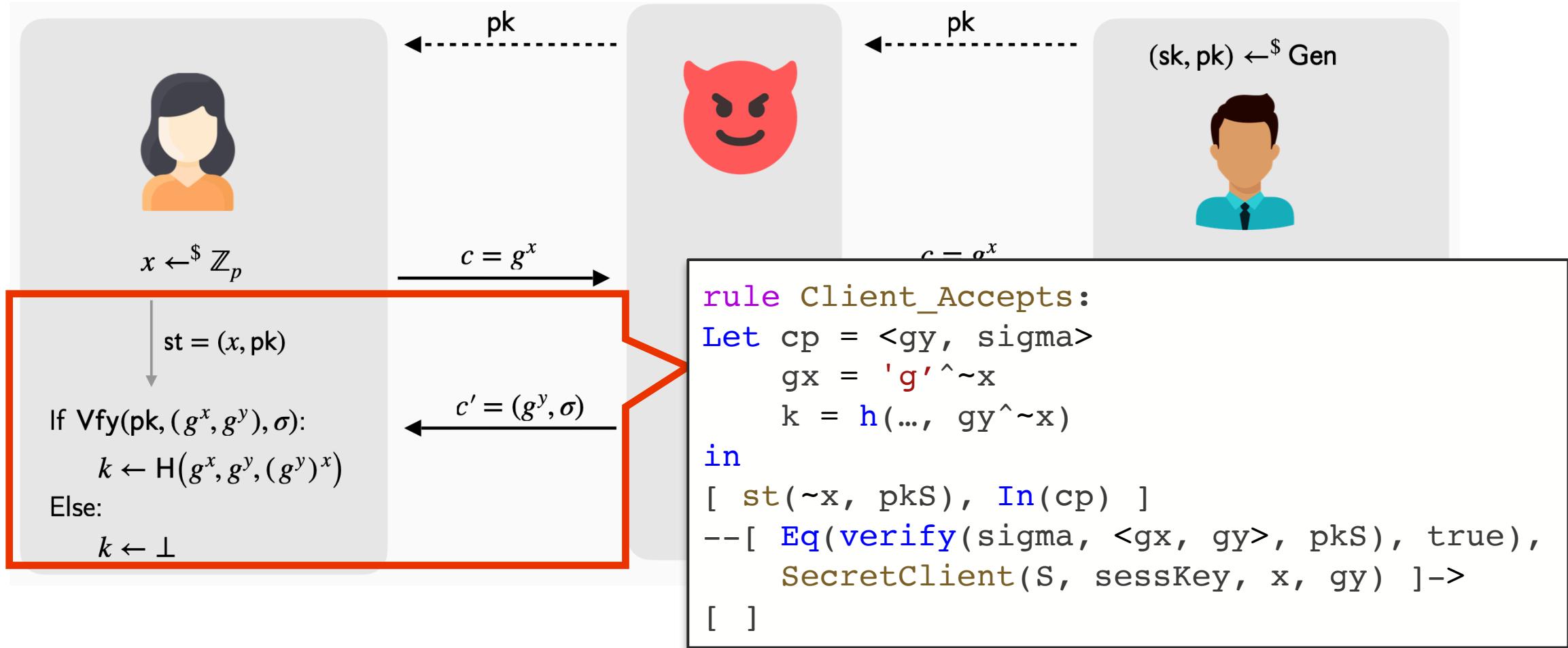
'c'	constant
$\sim x$	fresh type
$\$x$	public type





# Client (2/2)

'c'	constant
$\sim x$	fresh type
$\$x$	public type





# Security properties

'c'	constant
$\sim x$	fresh type
$\$x$	public type

```

lemma SessionKey_Secrecy:
"All pkS sessKey x gy #i. SecretClient(pkS, sessKey, x, gy)
@ #i
==>
not(Ex #j . K(sessKey) @ #j)
| (Ex skS #j . CompromiseLtk(pkS, skS)@ #j)
| (Ex gx #j . CompromiseEphemeralKey(x, gx)@ #j)
| (Ex y #j . CompromiseEphemeralKey(y, gy)@ #j)"

```

st =  $(x, \text{pk})$

If  $\text{Vfy}(\text{pk}, (g^x, g^y), \sigma)$ :

$$k \leftarrow H(g^x, g^y, (g^y)^x)$$

Else:

$$k \leftarrow \perp$$

$$c' = (g^y, \sigma)$$

Let  $cp = \langle gy, \sigma \rangle$   
 $gx = 'g'^{\sim x}$   
 $k = h(..., gy^{\sim x})$   
in  
[  $st(\sim x, pkS)$ ,  $\text{In}(cp)$  ]  
-- [  $\text{Eq}(\text{verify}(\sigma, \langle gx, gy \rangle, pkS), \text{true})$ ,  
 $\text{SecretClient}(S, sessKey, x, gy)$  ] ->  
[ ]



# **DEMO (command line)**



signedDH.spthy 1

signedDH &gt; signedDH.spthy



```
52
53 // Generate Server's long-term (s_sk, s_pk).
54 rule Generate_serverLtk:
55   let pkS = pk(~sk)
56   in
57   [ Fr(~sk) ]
58   -->
59   [ !Ltk($S, ~sk),
60   | !Pk($S, pkS),
61   | Out(pkS) ]
62
63 // Client generates DH pair (x_sk, x_pk), and sends the public key Out(x_pk).
64 rule Client_Init:
65   let x_pk = 'g'^~x_sk
66   in
```

PROBLEMS 25

OUTPUT

SPELL CHECKER 24

PORTS

TERMINAL



reup@Re-D7s-max signedDH %

tamarin-prover s...

zsh signedDH



1

The screenshot shows a code editor interface with a sidebar containing icons for file operations, search, and help. The main area displays a file named `signedDH.spthy` with the following content:

```
signedDH > signedDH.spthy
52
53 // Generate Server's long-term (s_sk, s_pk).
54 rule Generate_serverLtk:
55   let pkS = pk(~sk)
56   in
57   [ Fr(~sk) ]
58   -->
59   [ !Ltk($S, ~sk),
60   | !Pk($S, pkS),
61   | Out(pkS) ]
62
63 // Client generates DH pair (x_sk, x_pk), and sends the public key Out(x_pk).
64 rule Client_Init:
65   let x_pk = 'g'^~x_sk
66   in
```

Below the code editor, there is a navigation bar with tabs: PROBLEMS (25), OUTPUT, SPELL CHECKER (24), PORTS, and TERMINAL. The TERMINAL tab is active, showing the command-line output of the Tamarin Prover:

```
reup@Re-D7s-max signedDH % tamarin-prover signedDH.spthy
=====
summary of summaries:
analyzed: signedDH.spthy
processing time: 0.25s

ExecutabilityClient (exists-trace): analysis incomplete (1 steps)
ExecutabilityServer (exists-trace): analysis incomplete (1 steps)
ExecutabilityClientEnd (exists-trace): analysis incomplete (1 steps)
BothPartiesCanReachEnd (exists-trace): analysis incomplete (1 steps)
ServerKeySecrecy (all-traces): analysis incomplete (1 steps)
SessionKey_Secrecy (all-traces): analysis incomplete (1 steps)
ForwardSecrecy (all-traces): analysis incomplete (1 steps)
ClientSide_Injective_Authentication (all-traces): analysis incomplete (1 steps)
Unique_Commits (all-traces): analysis incomplete (1 steps)
ClientSide_Injective_Authentication_simplified (all-traces): analysis incomplete (1 steps)
=====
```

A context menu is open over the terminal output, showing options: "Navigate to Command", "Scroll to Previous Command (⌘↑)", and "Scroll to Next Command (⌘↓)". To the right of the terminal, there is a sidebar with two entries: "tamarin-prover s..." and "zsh signedDH".

At the bottom of the screen, there is a status bar with the following information: "reup@Re-D7s-max signedDH %", "main\* 24 protocol-ladder", "Aurora Naska (2 months ago)", "Ln 90, Col 1", and "Run".

signedDH.spthy 1

signedDH > signedDH.spthy

```
52
53 // Generate Server's long-term (s_sk, s_pk).
54 rule Generate_serverLtk:
55   let pkS = pk(~sk)
56   in
57   [ Fr(~sk) ]
58   -->
59   [ !Ltk($S, ~sk),
60   | !Pk($S, pkS),
61   | Out(pkS) ]
62
63 // Client generates DH pair (x_sk, x_pk), and sends the public key Out(x_pk).
64 rule Client_Init:
65   let x_pk = 'g'^~x_sk
66   in
```

PROBLEMS 25 OUTPUT SPELL CHECKER 24 PORTS TERMINAL

```
reup@Re-D7s-max signedDH % tamarin-prover signedDH.spthy --prove
=====
summary of summaries:
analyzed: signedDH.spthy
processing time: 0.38s

ExecutabilityClient (exists-trace): verified (2 steps)
ExecutabilityServer (exists-trace): verified (4 steps)
ExecutabilityClientEnd (exists-trace): verified (7 steps)
BothPartiesCanReachEnd (exists-trace): verified (8 steps)
ServerKeySecrecy (all-traces): falsified - found trace (6 steps)
SessionKey_Secrecy (all-traces): verified (14 steps)
ForwardSecrecy (all-traces): verified (14 steps)
ClientSide_Injective_Authentication (all-traces): verified (11 steps)
Unique_Commits (all-traces): verified (10 steps)
ClientSide_Injective_Authentication_simplified (all-traces): verified (7 steps)
=====
```

reup@Re-D7s-max signedDH %

Aurora Naska (2 months ago)



# **DEMO (GUI)**



## Proof scripts

```
Lemma SessionKey_Secrecy:
  all-traces
  "¬ S sessKey x_sk y_pk #i.
   (SecretClient( S, sessKey, x_sk, y_pk ) @ #i) =  

   (CCC-(∃ #j. K( sessKey ) @ #j)) ∨  

   (∃ s_sk #j. CompromiseLtk( S, s_sk ) @ #j) ∨  

   (∃ x_pk #j. CompromiseEphemeralKey( x_sk, x_pk )  

   ∨ ∃ y_sk #j. CompromiseEphemeralKey( y_sk, y_pk ))  

edit lemma or delete lemma  

by sorry /* removed */
```

[add lemma](#)

```
Lemma ForwardSecrecy:
  all-traces
  "¬ S sessKey x_sk y_pk #i #k.
   ((SecretClient( S, sessKey, x_sk, y_pk ) @ #i) ∧  

   (K( sessKey ) @ #k)) ⇒  

   (((∃ s_sk #j. (CompromiseLtk( S, s_sk ) @ #j) ∧  

   (∃ x_pk #j. CompromiseEphemeralKey( x_sk, x_pk )  

   ∨ ∃ y_sk #j. CompromiseEphemeralKey( y_sk, y_pk )))  

edit lemma or delete lemma  

by sorry
```

[add lemma](#)

```
Lemma ClientSide_Injective_Authentication:
  all-traces
  "¬ S x_pk y_pk s_pk serverSign sessKey #i.
   (ClientAccepts( S, x_pk, y_pk, s_pk, serverSign,  

   (∃ #j.  

   ((#j < #i) ∧  

   (ServerAccepts( S, x_pk, y_pk, s_pk, serverSi  

   t))) ∨  

   (ClientAccepts( S, x_pk, y_pk, s_pk, serve  

   t)))  

   ∨  

   (∃ s_sk #j. CompromiseLtk( S, s_sk ) @ #j))"  

2 edit lemma or delete lemma
```

## Lemma: SessionKey\_Secrecy

Applicable Proof Methods: Goals sorted according to the 'smart' heuristic (loop breakers delayed)

1. simplify

2. induction

a. autoprove (A. for all solutions)

b. autoprove (B. for all solutions) with proof-depth bound 5

s. autoprove (S. for all solutions) for all lemmas

## Constraint system

last: none

## formulas:

$$\exists S \text{ sessKey } x_{\text{sk}} y_{\text{pk}} \#i.$$

$$(\text{SecretClient}(S, \text{sessKey}, x_{\text{sk}}, y_{\text{pk}}) @ \#i) \wedge$$

$$(\exists \#j. (\text{K}(\text{sessKey}) @ \#j)) \wedge$$

$$(\forall s_{\text{sk}} \#j. (\text{CompromiseLtk}(S, s_{\text{sk}}) @ \#j) \Rightarrow \perp) \wedge$$

$$(\forall x_{\text{pk}} \#j. (\text{CompromiseEphemeralKey}(x_{\text{sk}}, x_{\text{pk}}) @ \#j) \Rightarrow \perp) \wedge$$

$$(\forall y_{\text{sk}} \#j. (\text{CompromiseEphemeralKey}(y_{\text{sk}}, y_{\text{pk}}) @ \#j) \Rightarrow \perp)$$

## subterms:

## equations:

subst:

conj:

lemmas:  $\forall x y \#i. (\text{Eq}(x, y) @ \#i) \Rightarrow x = y$ 

allowed cases: refined

## solved formulas:



## Proof scripts

```

Lemma SessionKey_Secrecy:
all-traces
"∀ S sessKey x_sk y_pk #i.
(SecretClient( S, sessKey, x_sk, y_pk ) @ #i) =>
(¬(∃ #j. K( sessKey ) @ #j)) ∨
(∃ s_sk #j. CompromiseLtk( S, s_sk ) @ #j) ∨
(∃ x_pk #j. CompromiseEphemeralKey( x_sk, x_pk ) @ #j) ∨
(∃ y_sk #j. CompromiseEphemeralKey( y_sk, y_pk ) @ #j)

edit lemma or delete lemma
simplify
solve( StateCC( $C, ~x_sk ) ▷o #i )
case Client_Init
solve( !Pk( $S, pk(x) ) ▷1 #i )
case Generate_serverLtk
solve( !KUC sign(<'g'^~x_sk, y_pk), ~sk ) @ #vk.2 )
case Server_Init
solve( !KUC h('g'^(~x_sk*~y_sk)) ) @ #vk.3 )
case c_h
solve( !KUC 'g'^(~x_sk*~y_sk) ) @ #vk.5 )
case Client_Init
solve( !KUC ~y_sk ) @ #vk.6 )
case Compromise_EphemeralKey
by contradiction /* from formulas */
qed
next
case Server_Init
solve( !KUC ~x_sk ) @ #vk.6 )
case Compromise_EphemeralKey
by contradiction /* from formulas */
qed
next
case c_exp
solve( !KUC ~x_sk ) @ #vk.8 )
case Compromise_EphemeralKey
by contradiction /* from formulas */
qed
qed
qed
next

```

## Visualization display

Applicable Proof Methods: Goals sorted according to the 'smart' heuristic (loop breakers delayed)

1. simplify

2. induction

a. autoprove (A. for all solutions)

b. autoprove (B. for all solutions) with proof-depth bound 5

s. autoprove (S. for all solutions) for all lemmas

Constraint system

last: none

formulas:

$$\exists S \text{ sessKey } x_{\text{sk}} y_{\text{pk}} \#i \#k. \\ (\text{SecretClient}(S, \text{sessKey}, x_{\text{sk}}, y_{\text{pk}}) @ \#i) \wedge (K(\text{sessKey}) @ \#k) \\ \wedge \\ (\forall s_{\text{sk}} \#j. (\text{CompromiseLtk}(S, s_{\text{sk}}) @ \#j) \Rightarrow \neg(\#j < \#i)) \wedge \\ (\forall x_{\text{pk}} \#j. (\text{CompromiseEphemeralKey}(x_{\text{sk}}, x_{\text{pk}}) @ \#j) \Rightarrow \perp) \wedge \\ (\forall y_{\text{sk}} \#j. (\text{CompromiseEphemeralKey}(y_{\text{sk}}, y_{\text{pk}}) @ \#j) \Rightarrow \perp)$$

subterms:

equations:

subst:

conj:

lemmas:  $\forall x y \#i. (\text{Eq}(x, y) @ \#i) \Rightarrow x = y$

allowed cases: refined

solved formulas:



## Proof scripts

```
lemma ServerKeySecrecy:
  all-traces
  "¬ S sessKey #i.
   (SecretServer( S, sessKey ) @ #i) =>
   (¬( ∃ #j. KC( sessKey ) @ #j)) ∨
   ( ∃ s_sk #j. CompromiseLtk( S, s_sk ) @ #j) ∨
   ( ∃ eKey ePubKey #j.
     CompromiseEphemeralKey( eKey, ePubKey ) @ #j)
```

[edit lemma](#) or [delete lemma](#)[simplify](#)[solveC !Ltk\( \\$S, ~s\\_sk \) ▷o #i \)](#)

case Generate\_serverLtk

[solveC splitEqs\(0\) \)](#)

case split\_case\_1

[solveC !KUC h\(x\\_pk^~y\\_sk \) @ #vk.1 \)](#)

case c\_h

[solveC !KUC x\\_pk^~y\\_sk \) @ #vk.2 \)](#)

case Server\_Init

[SOLVED // trace found](#)

qed

qed

qed

qed

[add lemma](#)

lemma SessionKey\_Secrecy:

all-traces

"¬ S sessKey x\_sk y\_pk #i.

```
(SecretClient( S, sessKey, x_sk, y_pk ) @ #i) =>
(¬( ∃ #j. KC( sessKey ) @ #j)) ∨
( ∃ s_sk #j. CompromiseLtk( S, s_sk ) @ #j) ∨
( ∃ x_pk #j. CompromiseEphemeralKey( x_sk, x_pk
( ∃ y_sk #j. CompromiseEphemeralKey( y_sk, y_pk )
```

[edit lemma](#) or [delete lemma](#)

by sorry /\* removed \*/

[add lemma](#)

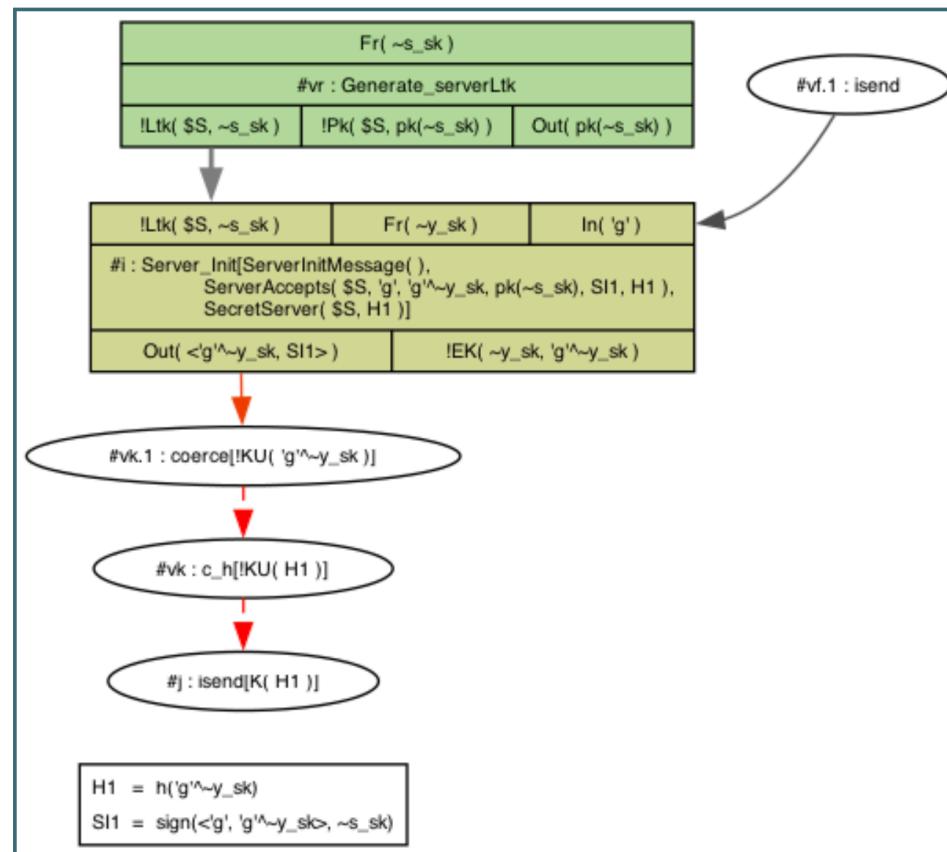
## Visualization display

Applicable Proof Methods: Goals sorted according to the 'smart' heuristic (loop breakers delayed)

1. SOLVED // trace found

a. [autoprove \(A. for all solutions\)](#)b. [autoprove \(B. for all solutions\)](#) with proof-depth bound 5s. [autoprove \(S. for all solutions\)](#) for all lemmas

## Constraint system





## Proof scripts

```
Lemma ForwardSecrecy:
  all-traces
```

```
  "V S sessKey x_sk y_pk #i #k.
    ((SecretClient( S, sessKey, x_sk, y_pk ) @ #i) ∧
     (KC sessKey ) @ #k)) ⇒
    (((Ǝ s_sk #j. (CompromiseLtk( S, s_sk ) @ #j) ∧ (
      (Ǝ x_pk #j. CompromiseEphemeralKey( x_sk, x_pk
      (Ǝ y_sk #j. CompromiseEphemeralKey( y_sk, y_pk
```

[edit lemma](#) or [delete lemma](#)

[simplify](#)

[solve](#)( StateC( \$C, ~x\_sk ) ▷<sub>0</sub> #i )

case Client\_Init

[solve](#)( !Pk( \$S, pk(x) ) ▷<sub>1</sub> #i )

case Generate\_serverLtk

[solve](#)( !KUC( sign(<'g'^~x\_sk, y\_pk), ~sk ) @ #vk.2 )

case Server\_Init

[solve](#)( !KUC( h('g'^~(x\_sk\*y\_sk)) ) @ #vk.3 )

case c\_h

[solve](#)( !KUC( 'g'^~(x\_sk\*y\_sk) ) @ #vk.5 )

case Client\_Init

[solve](#)( !KUC( ~y\_sk ) @ #vk.6 )

case Compromise\_EphemeralKey

by contradiction /\* from formulas \*/

qed

next

case Server\_Init

[solve](#)( !KUC( ~x\_sk ) @ #vk.6 )

case Compromise\_EphemeralKey

by contradiction /\* from formulas \*/

qed

next

case c\_exp

[solve](#)( !KUC( ~x\_sk ) @ #vk.8 )

case Compromise\_EphemeralKey

by contradiction /\* from formulas \*/

qed

qed

next

## Visualization display

Applicable Proof Methods: Goals sorted according to the 'smart' heuristic (loop breakers delayed)

1. simplify

2. induction

a. [autoprove](#) (A. for all solutions)

b. [autoprove](#) (B. for all solutions) with proof-depth bound 5

s. [autoprove](#) (S. for all solutions) for all lemmas

## Constraint system

last: none

## formulas:

Ǝ S x\_pk y\_pk s\_pk serverSign sessKey #i.

(ClientAccepts( S, x\_pk, y\_pk, s\_pk, serverSign, sessKey ) @ #i)

^

(∀ #j.

(ServerAccepts( S, x\_pk, y\_pk, s\_pk, serverSign, sessKey ) @ #j)

⇒

((¬(#j < #i)) ∨

(∃ #t.

(ClientAccepts( S, x\_pk, y\_pk, s\_pk, serverSign, sessKey ) @ #t)

^

¬(#t = #i)))) ∧

(∀ s\_sk #j. (CompromiseLtk( S, s\_sk ) @ #j) ⇒ ⊥)

## subterms:

## equations:

subst:

conj:



## But Tamarin can do much more...

- Modern models high double-digits number of rules, covering all modes of complex protocols in one go

Some examples:

- IETF TLS 1.3
- SPDM 1.2
- 5G-AKA
- EMV (Chip and pin)
- Noise protocol suite
- Apple iMessage PQ3



## But Tamarin can do much more...

- Modern models high double-digits number of rules, covering all modes of complex protocols in one go

Some examples:

- IETF TLS 1.3
- SPDM 1.2
- 5G-AKA
- EMV (Chip and pin)
- Noise protocol suite
- Apple iMessage PQ3

Tamarin found 18-messageattack on draft 10+ that breaks post-handshake authentication



## But Tamarin can do much more...

- Modern models high double-digits number of rules, covering all modes of complex protocols in one go

Some examples:

- IETF TLS 1.3
- SPDM 1.2
- 5G-AKA
- EMV (Chip and pin)
- Noise protocol suite
- Apple iMessage PQ3

Tamarin found 18-messageattack on draft 10+ that breaks post-handshake authentication

Tamarin found cross-protocol attack that breaks psk authenticaton



## But Tamarin can do much more...

- Modern models high double-digits number of rules, covering all modes of complex protocols in one go

Some examples:

- IETF TLS 1.3
- SPDM 1.2
- 5G-AKA
- EMV (Chip and pin)
- Noise protocol suite
- Apple iMessage PQ3

Tamarin found 18-messageattack on draft 10+ that breaks post-handshake authentication

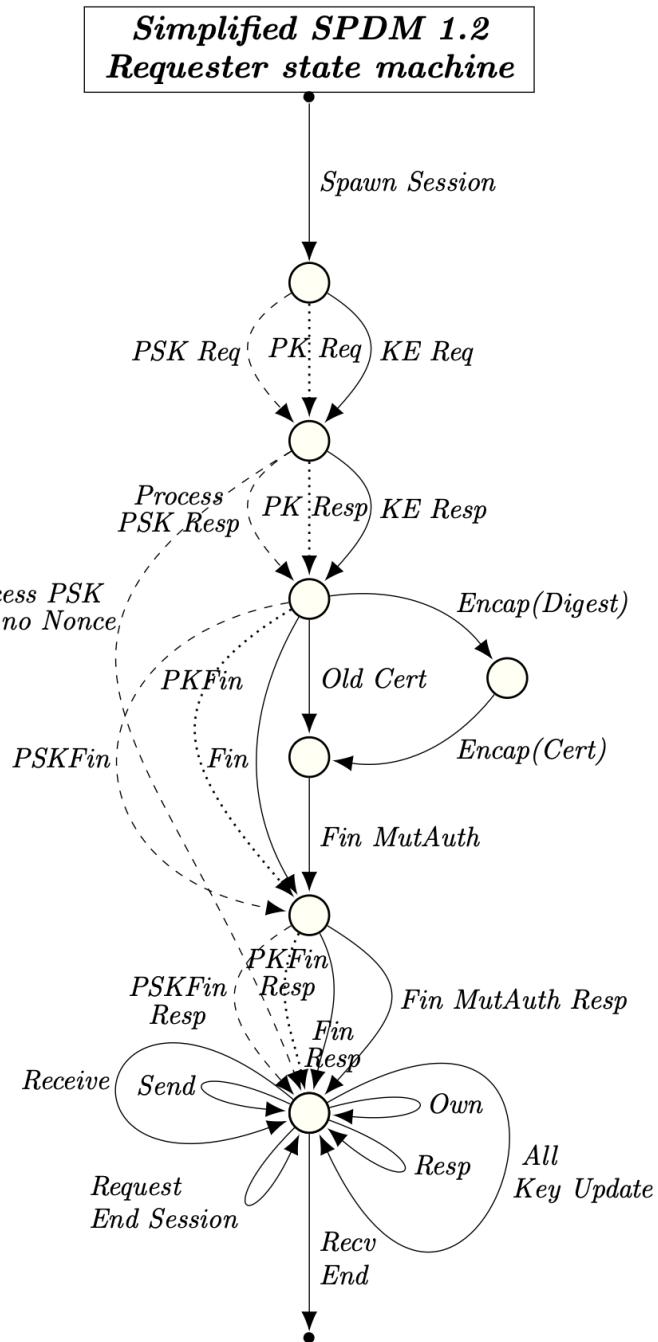
Tamarin found cross-protocol attack that breaks psk authenticaton

We can automate “the strongest property” that holds for each noise pattern



# Complexity example: SPDM 1.2

- Simplified picture:
- Actual model nearly 70 rules
- Tamarin finds a cross-protocol attack that breaks PSK authentication
  - Works on reference implementation and Intel's rust implementation
  - CVE with score 9.0 (critical)
- Prove fixed version





# Recent developments: Blurring the lines

- We are moving beyond traditional symbolic/Dolev-Yao features

A good starting point is:  
<https://ia.cr/2019/779>



# Recent developments: Blurring the lines

- We are moving beyond traditional symbolic/Dolev-Yao features

• “*Perfect cryptography*”  
and  
“*one symbolic model for each  
cryptographic primitive*”

• “*Symbolic models explicitly specify  
the possible adversary operations*”

A good starting point is:  
<https://ia.cr/2019/779>



# Recent developments: Blurring the lines

- We are moving beyond traditional symbolic/Dolev-Yao features

• “*Perfect cryptography*”  
and  
“*one symbolic model for each cryptographic primitive*”

• “*Symbolic models explicitly specify the possible adversary operations*”

- New: a range of symbolic models for
  - Signatures
  - AEADs
  - Hash functions
  - DH/EC
  - KEMs

A good starting point is:  
<https://ia.cr/2019/779>



# Recent developments: Blurring the lines

- We are moving beyond traditional symbolic/Dolev-Yao features

- “*Perfect cryptography*” and  
“*one symbolic model for each cryptographic primitive*”

- New: a range of symbolic models for
  - Signatures
  - AEADs
  - Hash functions
  - DH/EC
  - KEMs

- “*Symbolic models explicitly specify the possible adversary operations*”

- We can avoid this by trace restrictions:  
Instead of explicitly specifying allowed transitions, generalize and restrict

A good starting point is:  
<https://ia.cr/2019/779>



# Reality, models, and gaps



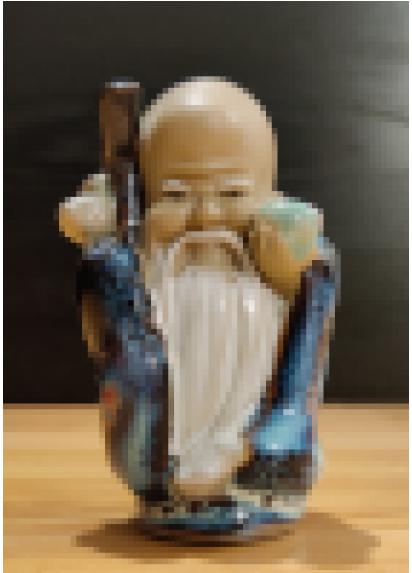
Reality



# Reality, models, and gaps



Reality



Computational



# Reality, models, and gaps



Reality



Computational



Symbolic



# Reality, models, and gaps



Reality



Computational



Symbolic



# The need to create breathing room

**Multiple approaches for provable security**

**In practice, the results are incomparable**





# The need to create breathing room

**Multiple approaches for provable security**

**In practice, the results are incomparable**



- *We should not fight this but embrace it*
  - Study multiple approaches, don't discard
  - Need space and time for new ideas to come to fruition



# The need to create breathing room

**Multiple approaches for provable security**

**In practice, the results are incomparable**



- *We should not fight this but embrace it*
  - Study multiple approaches, don't discard
  - Need space and time for new ideas to come to fruition
    - **Reviewing**
      - “you didn't do everything”
      - “use other method instead”



# The need to create breathing room

**Multiple approaches for provable security**

**In practice, the results are incomparable**



- *We should not fight this but embrace it*
  - Study multiple approaches, don't discard
  - Need space and time for new ideas to come to fruition
    - **Reviewing**
      - “you didn't do everything”
      - “use other method instead”
    - **Writing:**
      - Framing of results:
      - “formally verified” “provably secure” unhelpful



# Conclusions

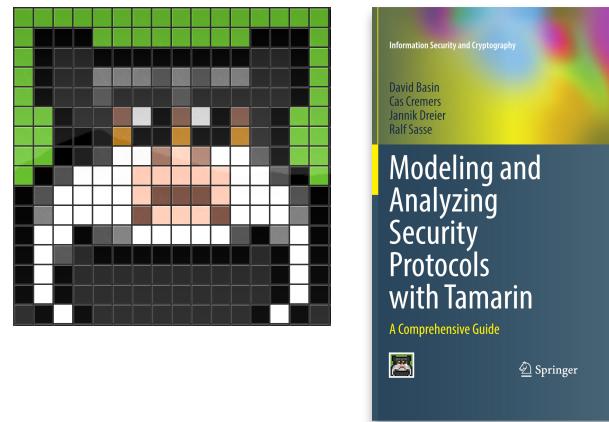


# Conclusions: Tamarin

- Tamarin is a mature tool
- capable of dealing with highly complex models
- Offers state-of-the art features
- Proofs or attack-finding
- GUI enables guiding/inspecting partial proofs
- Active development, user community, tutorials, book (soon: lecture slides based on book)

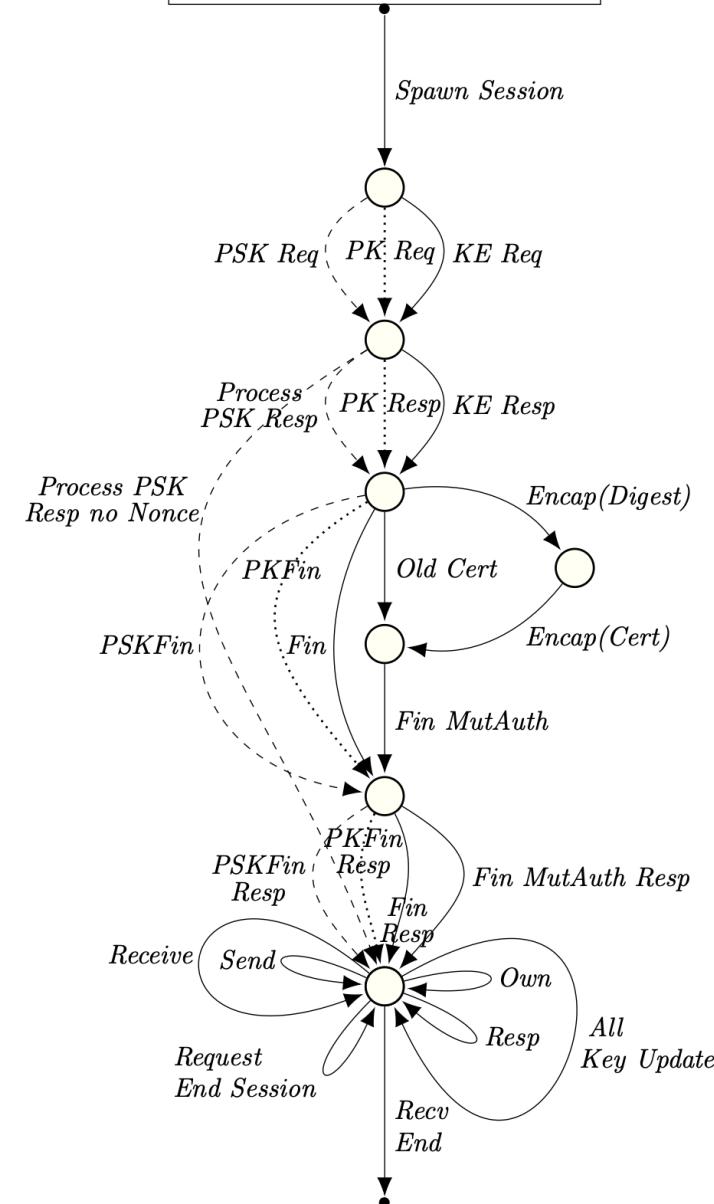
Cas Cremers – [cremers@cispa.de](mailto:cremers@cispa.de)

[tamarin-prover.com](http://tamarin-prover.com)



- IETF TLS 1.3
- SPDM 1.2
- 5G-AKA
- EMV (Chip and pin)
- Noise protocol suite
- Apple iMessage PQ3

*Simplified SPDM 1.2 Requester state machine*



# Backup slides

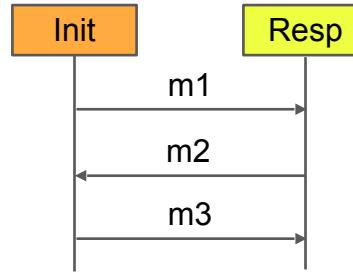


# Tamarin use in industry



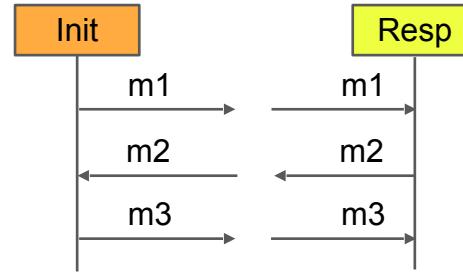


# Protocols and threat models



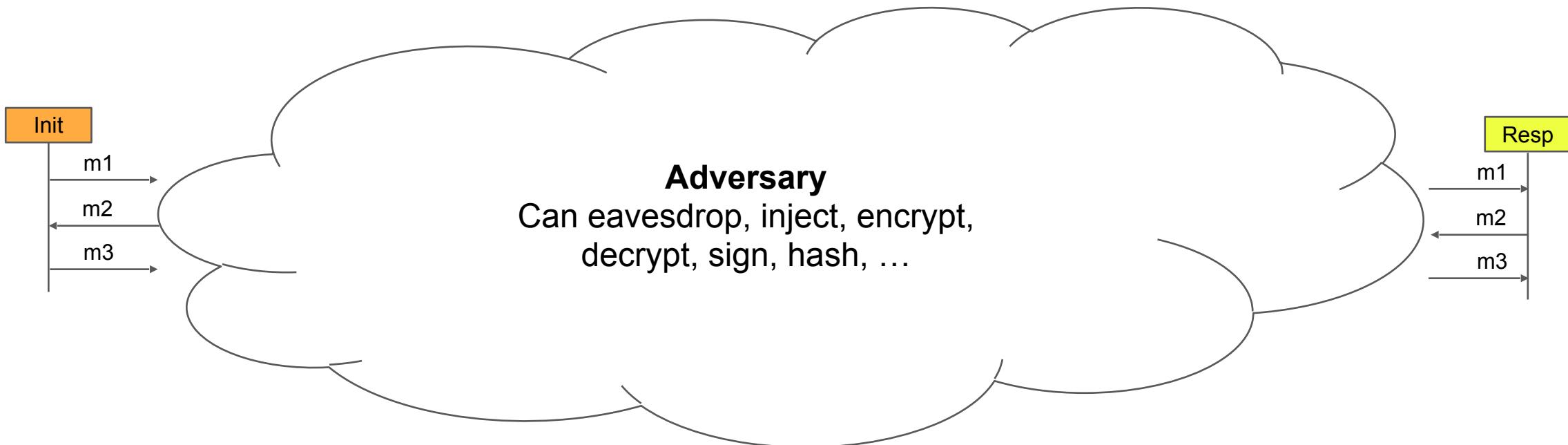


# Protocols and threat models



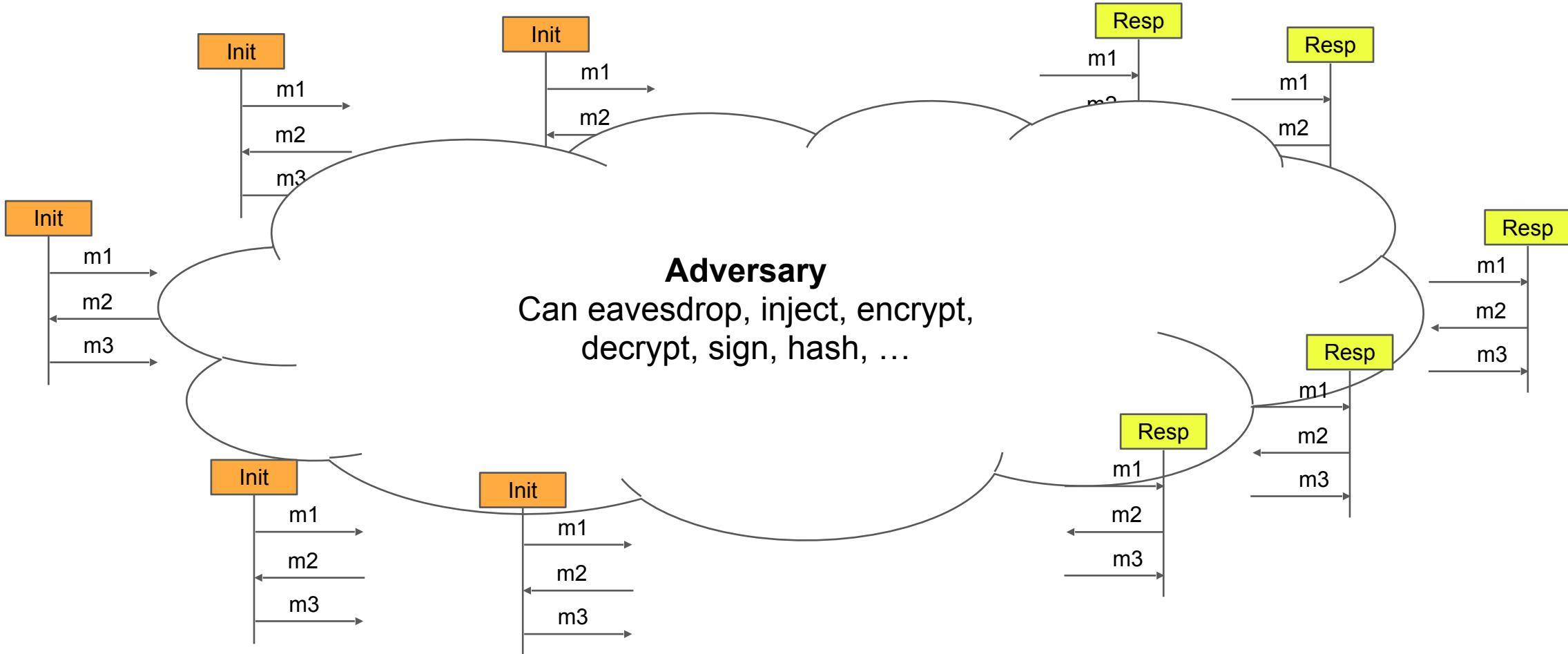


# Protocols and threat models



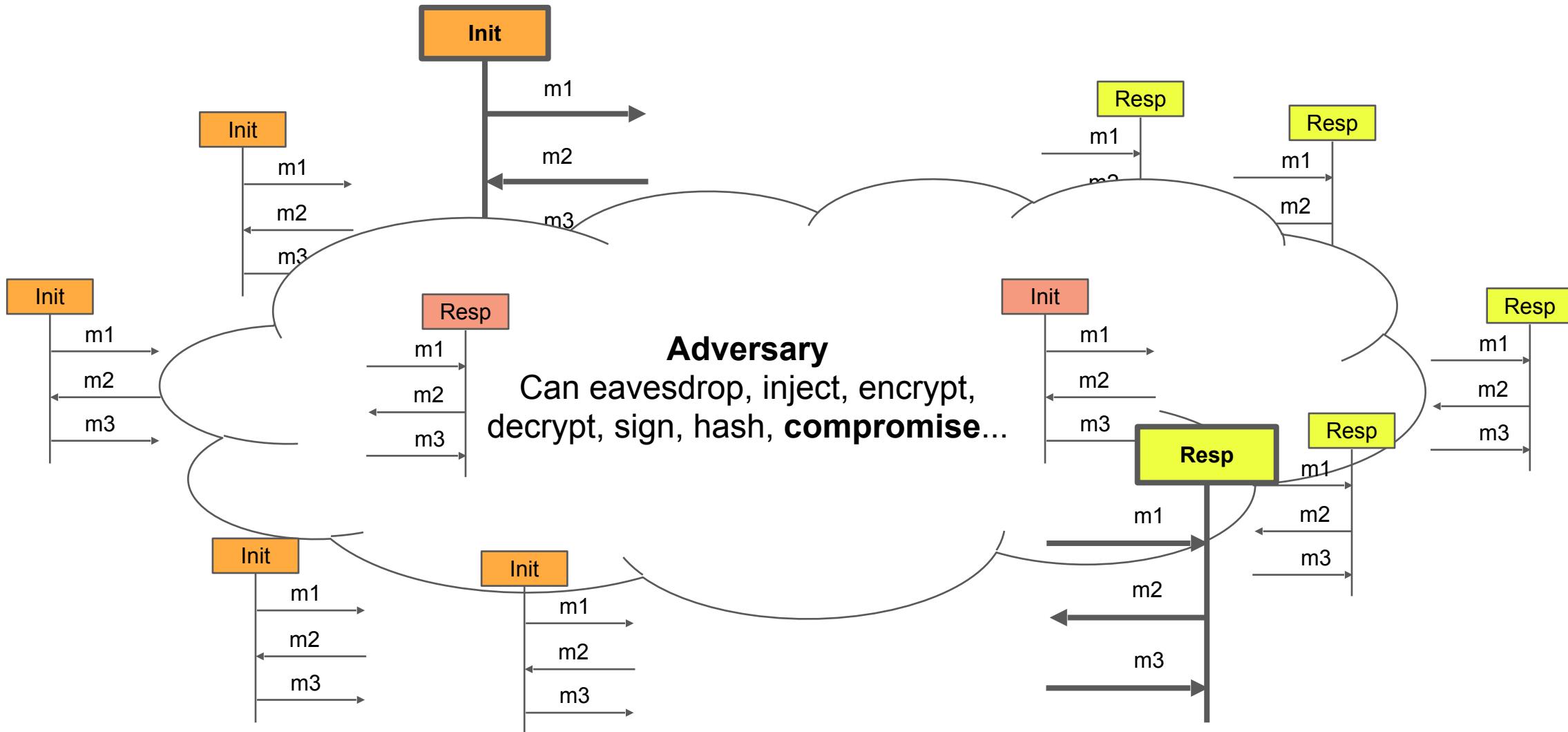


# Protocols and threat models





# Protocols and threat models





# SPDM: Security Protocol and Data Model

- Industry support behind this protocol:
  - DMTF- Distributed Management Task Force
  - Supported by other standards groups





# SPDM: Security Protocol and Data Model

- Industry support behind this protocol:
  - DMTF- Distributed Management Task Force
  - Supported by other standards groups
- Two party protocol for secure communication over the wire:
  - authentication of hardware identities
  - measurement for firmware identities
  - session key exchange protocols to enable confidentiality & integrity





- Secure Protocol and Data Model



Option/version  
negotiation

A wooden sign with horizontal planks, centered on a blue background. The text "Option/version negotiation" is written in white, sans-serif font on the sign.

- Secure Protocol and Data Model



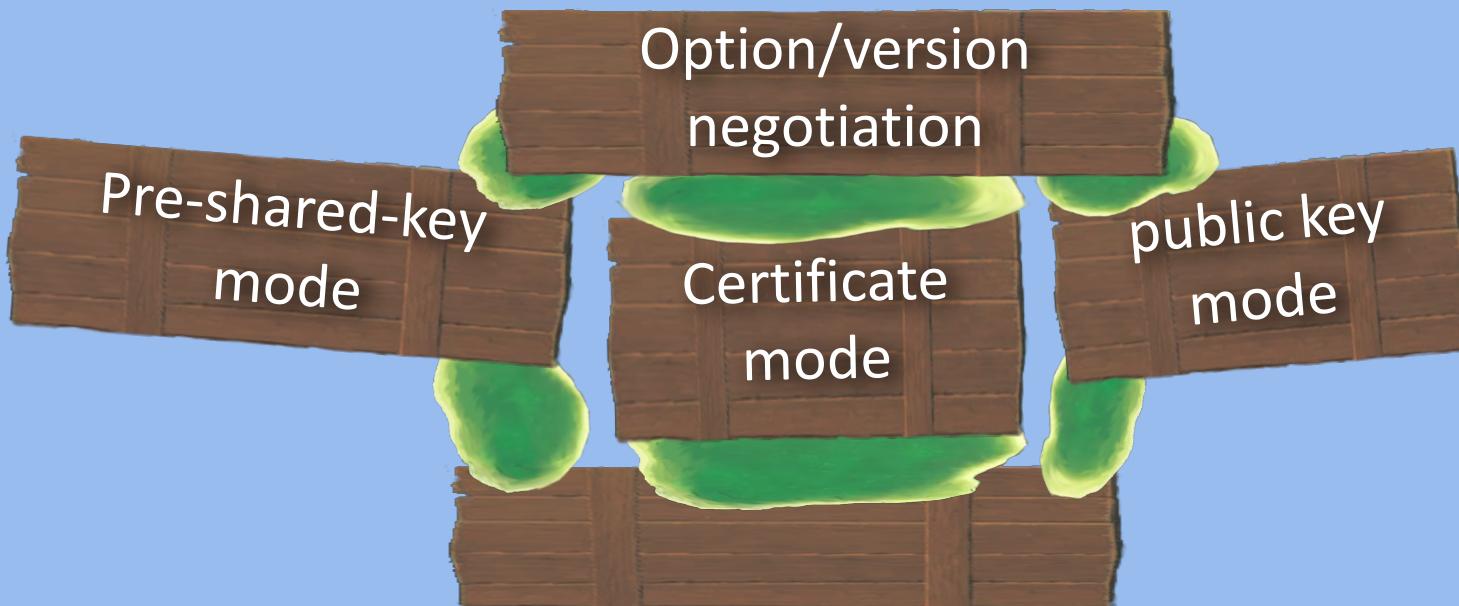
- Secure Protocol and Data Model



- Secure Protocol and Data Model



- Secure Protocol and Data Model



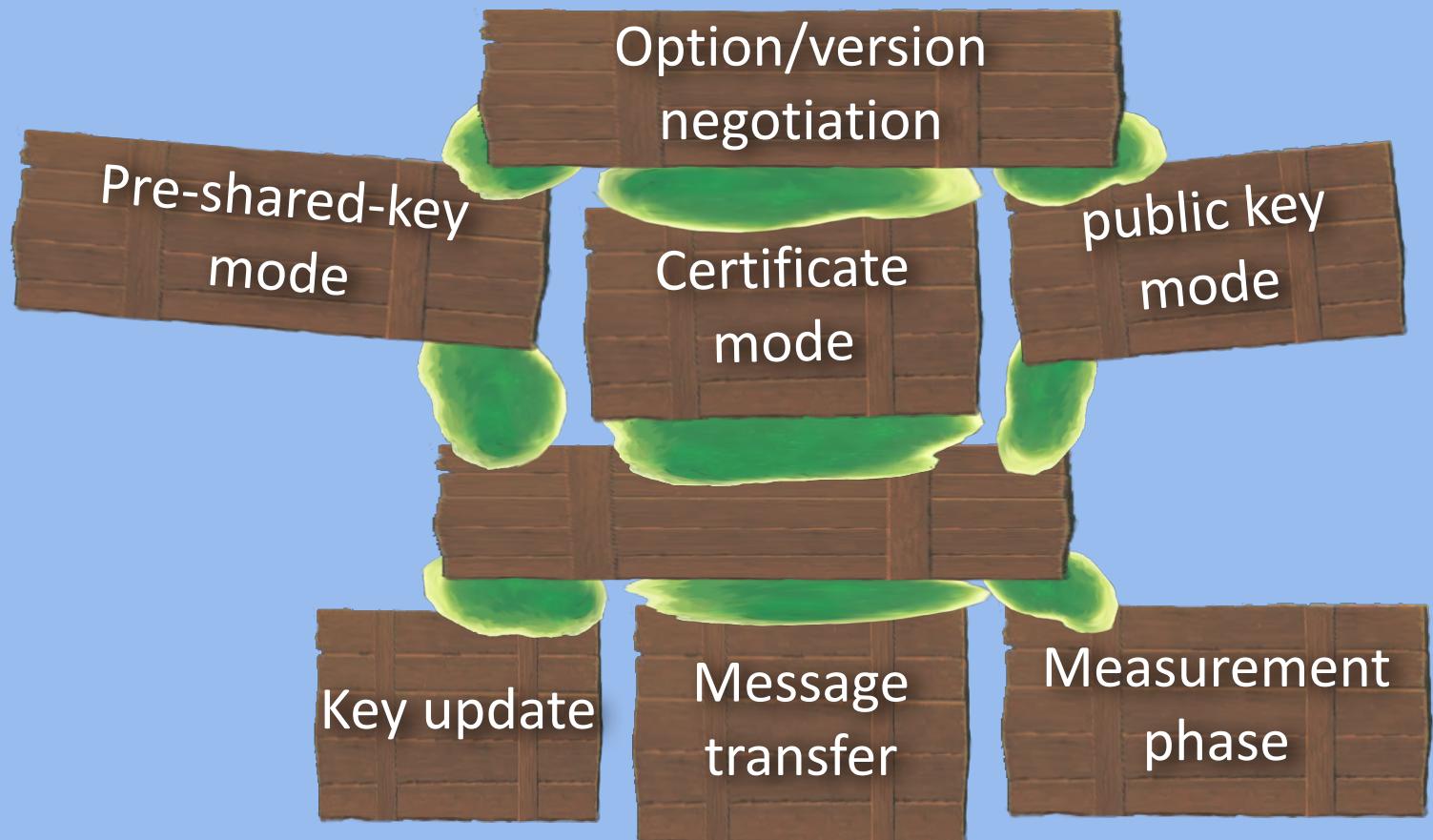
- Secure Protocol and Data Model



- Secure Protocol and Data Model

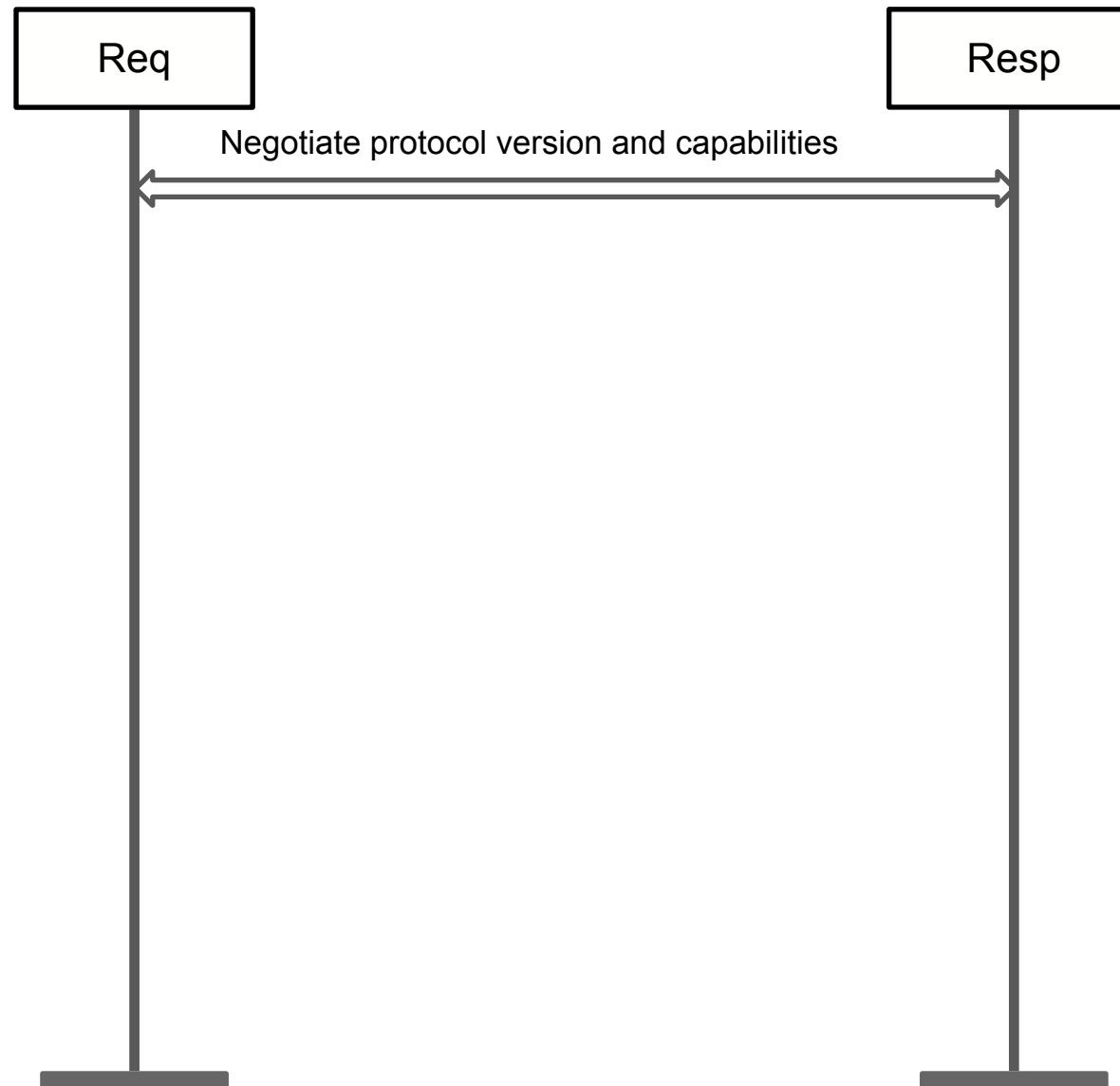


- Secure Protocol and Data Model



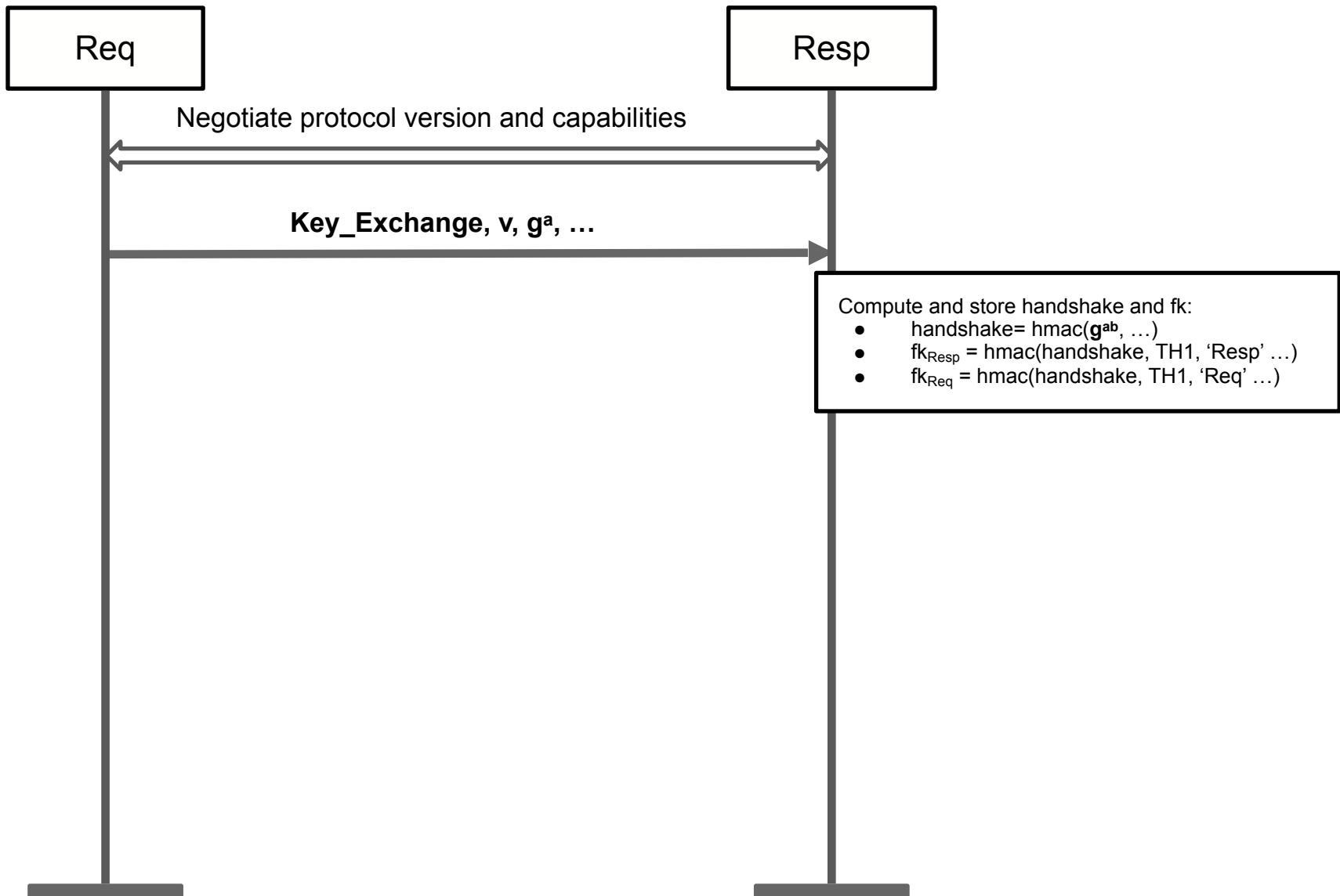


# Key Exchange with Certificates



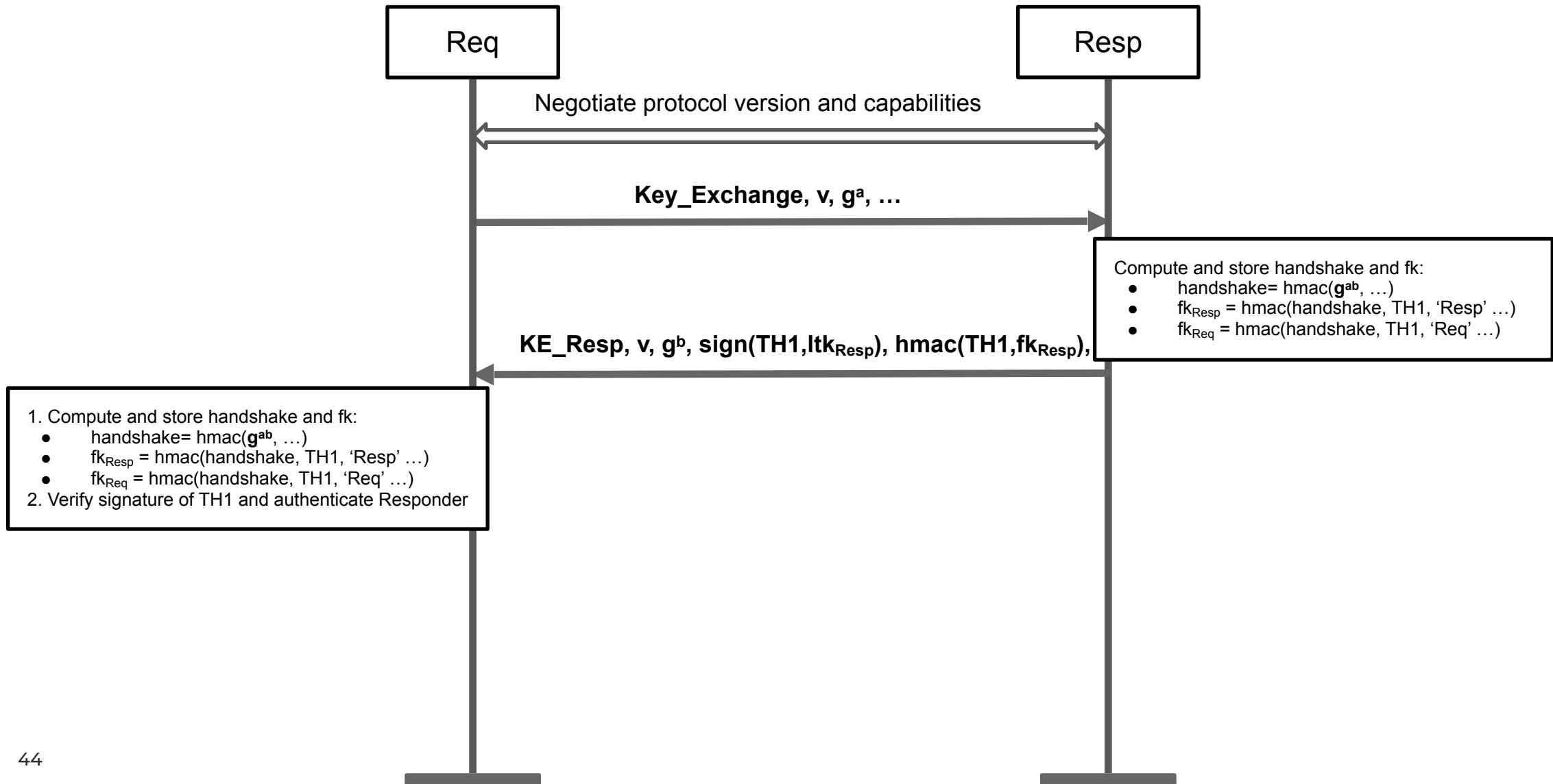


# Key Exchange with Certificates



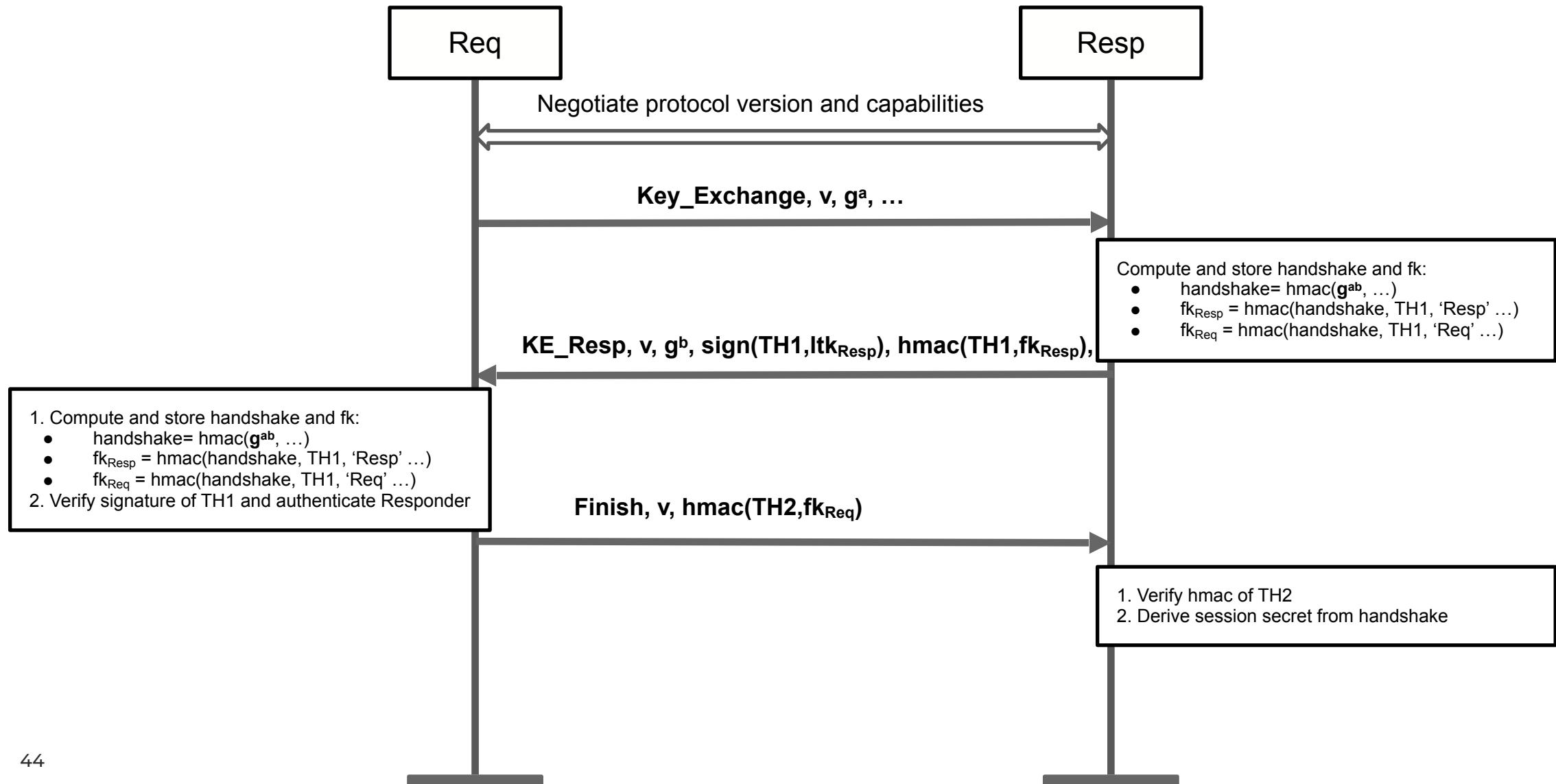


# Key Exchange with Certificates



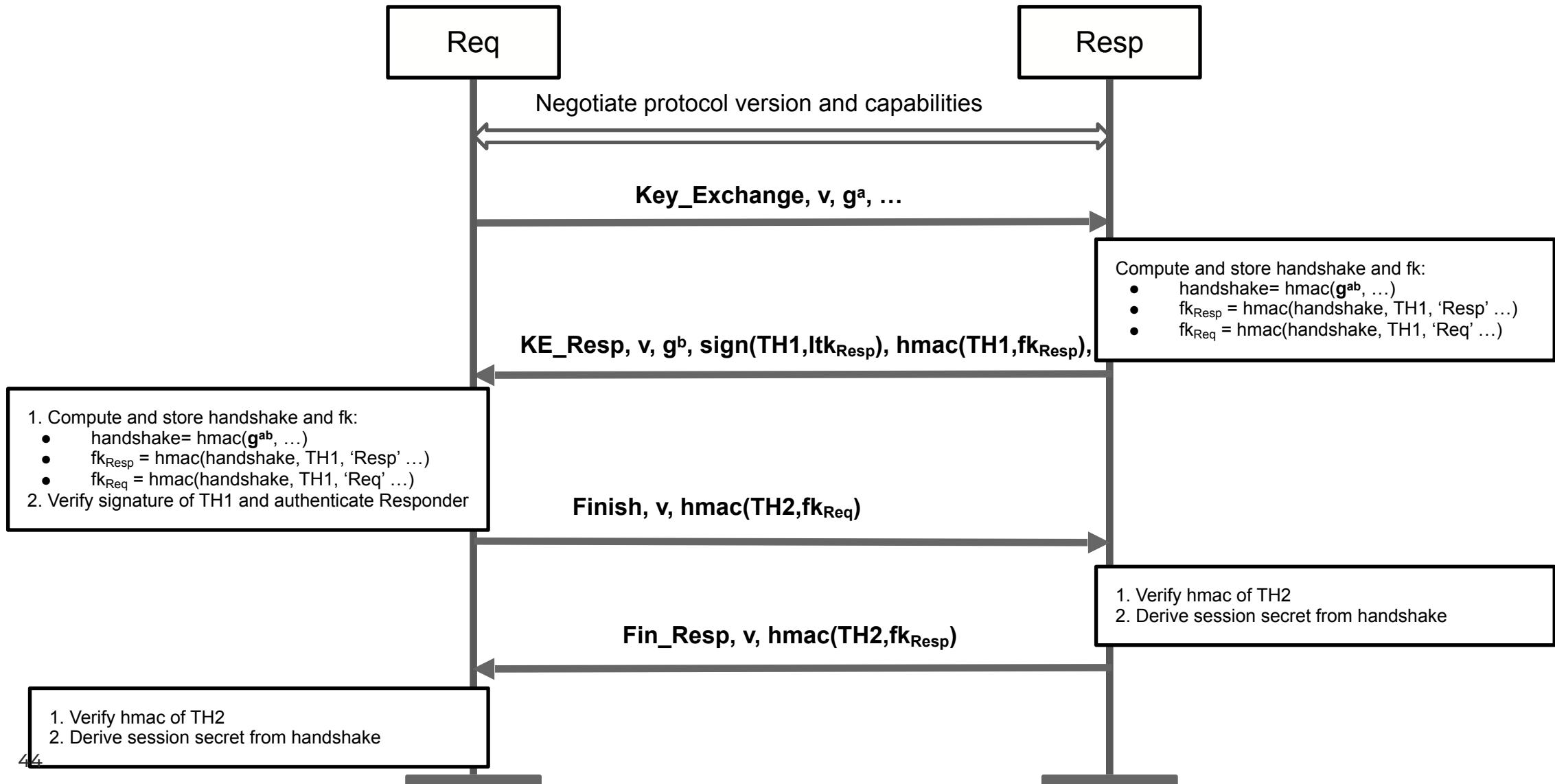


# Key Exchange with Certificates



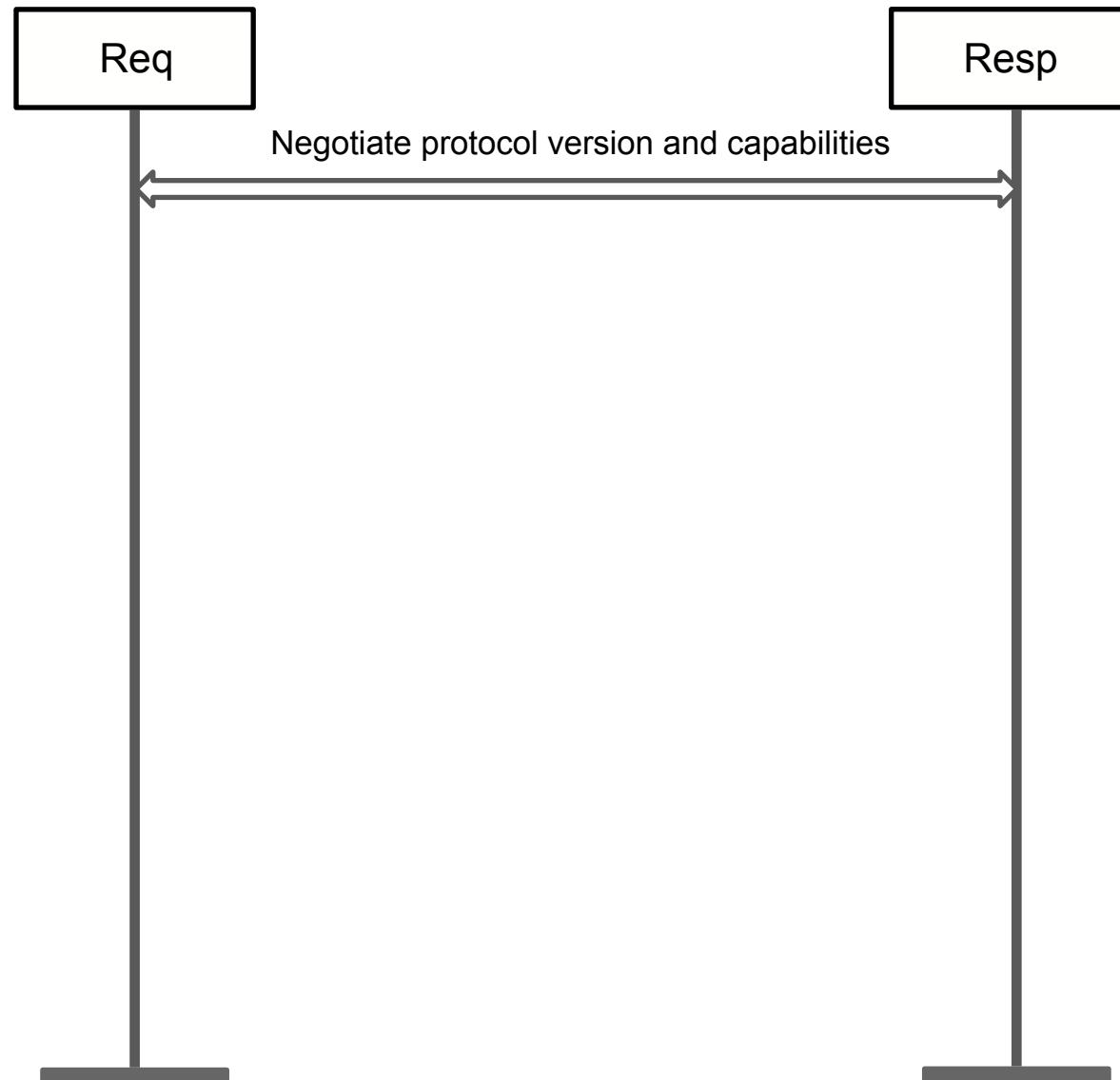


# Key Exchange with Certificates



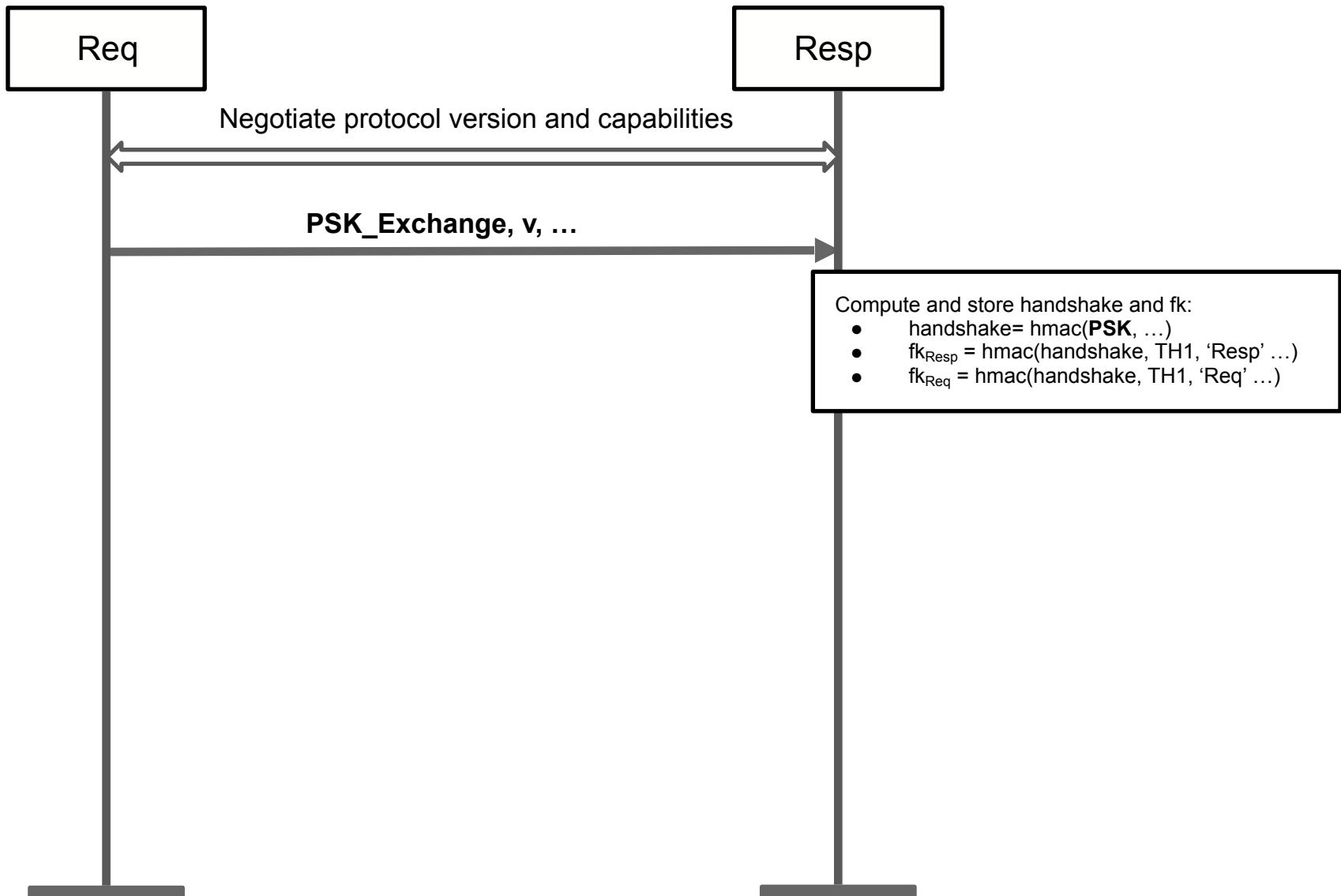


# Key Exchange with Preshared Key PSK



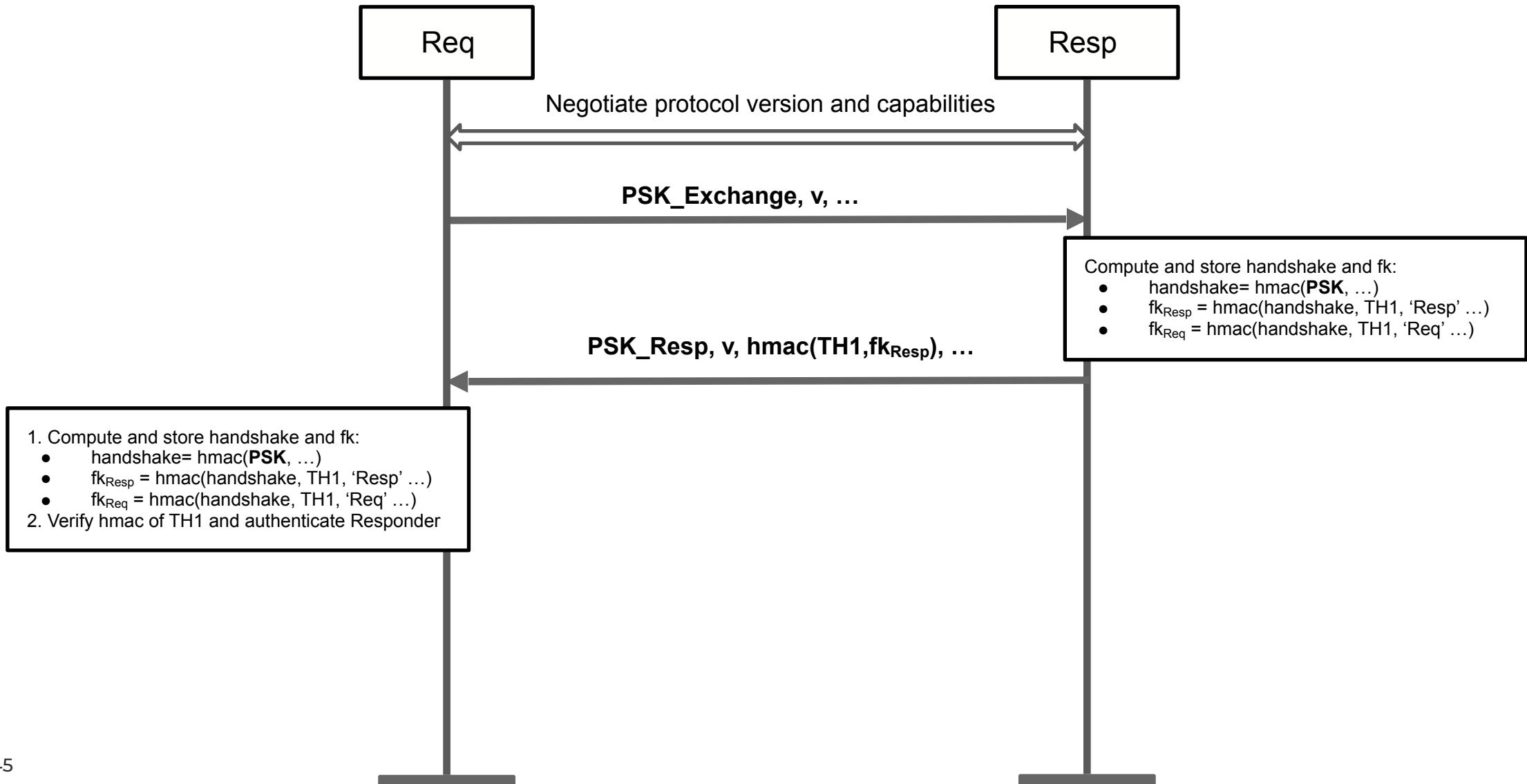


# Key Exchange with Preshared Key PSK



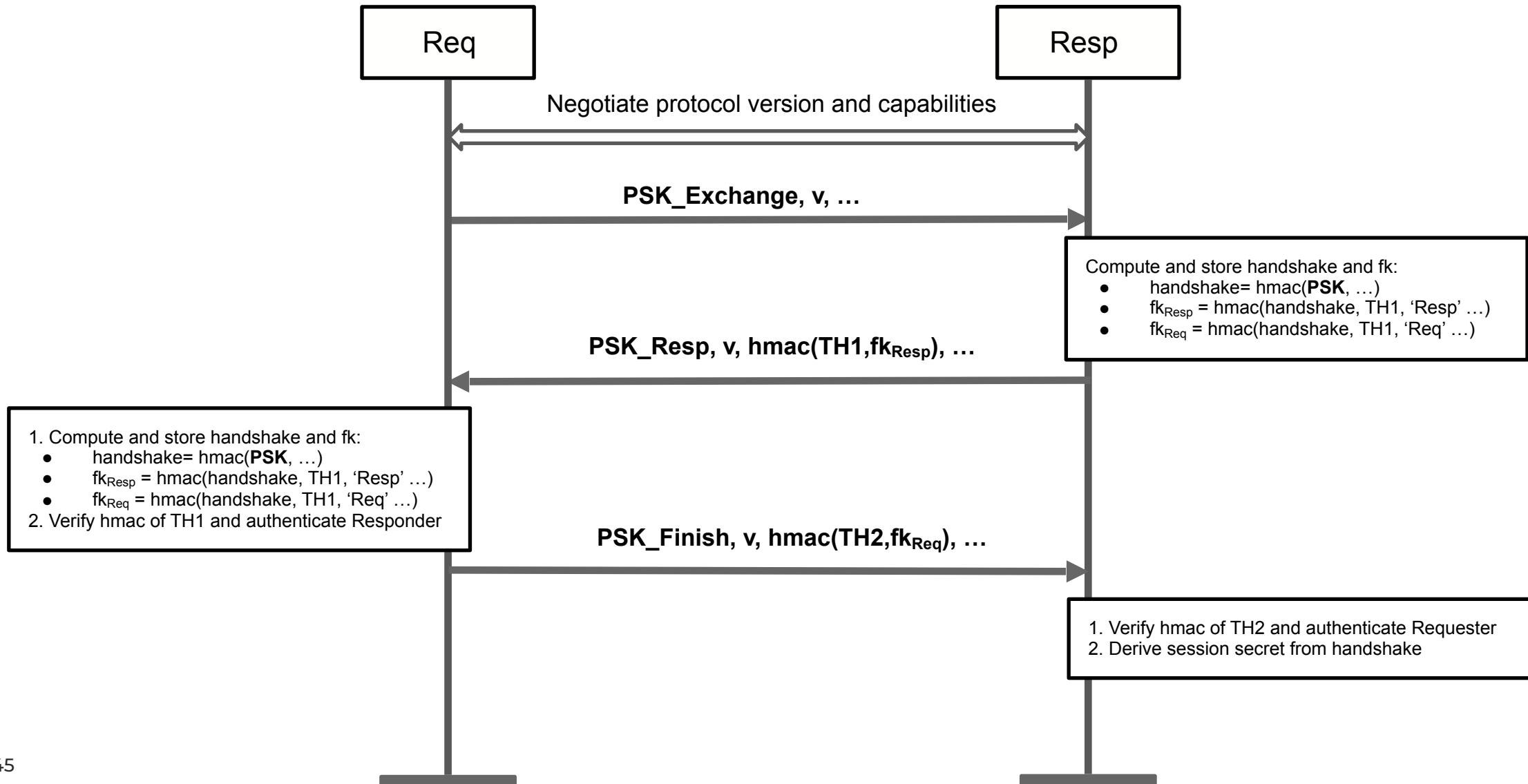


# Key Exchange with Preshared Key PSK



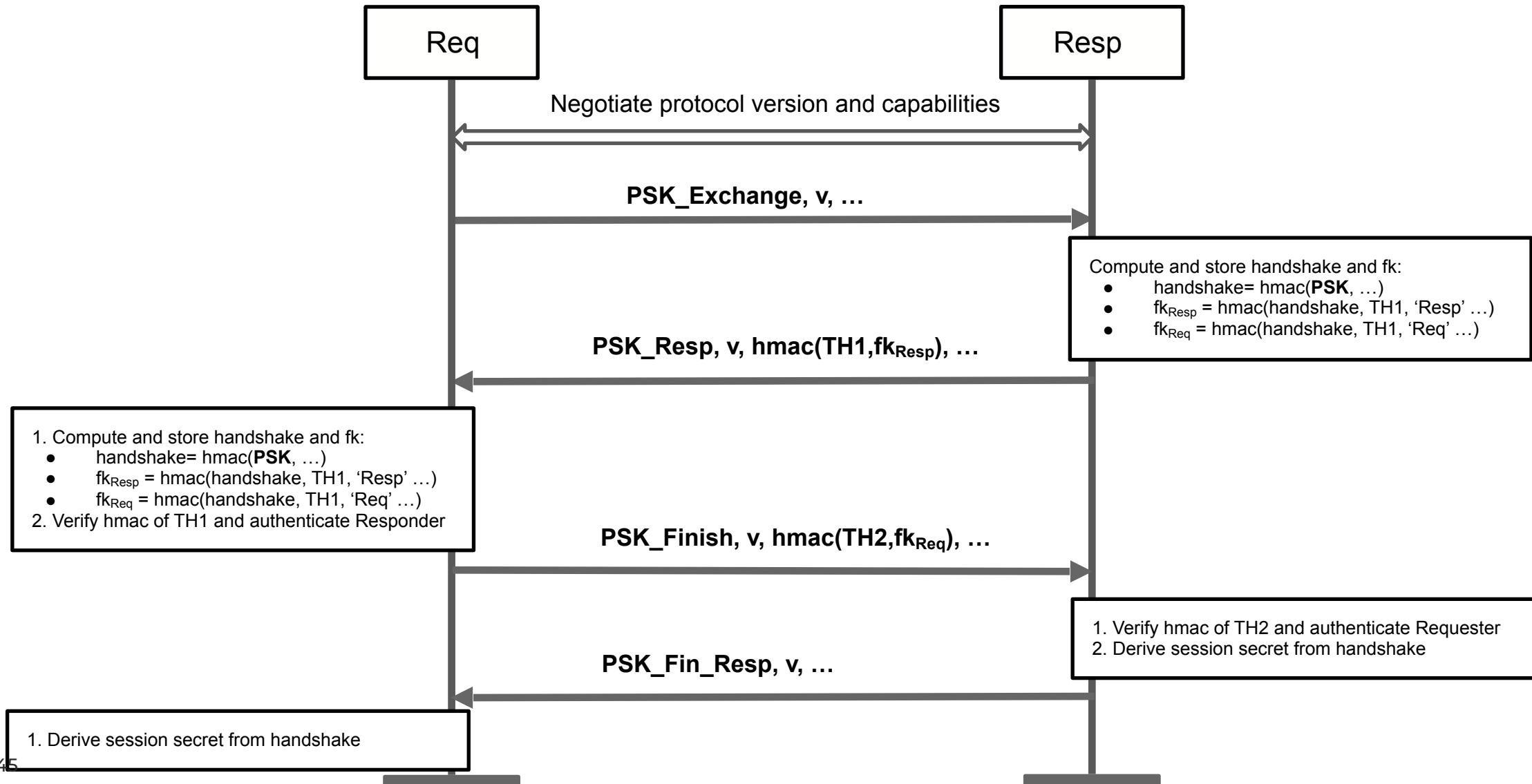


# Key Exchange with Preshared Key PSK



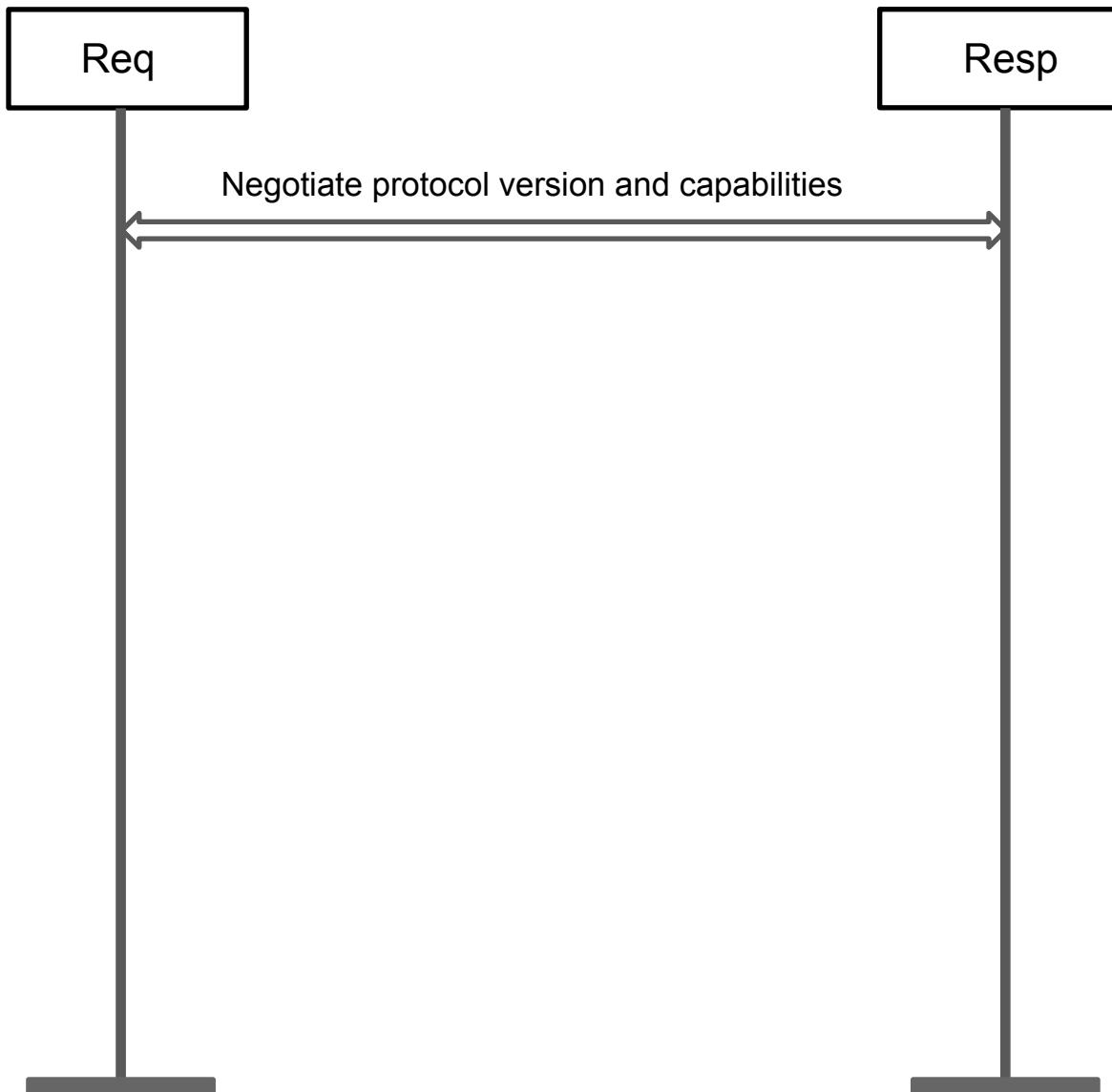


# Key Exchange with Preshared Key PSK



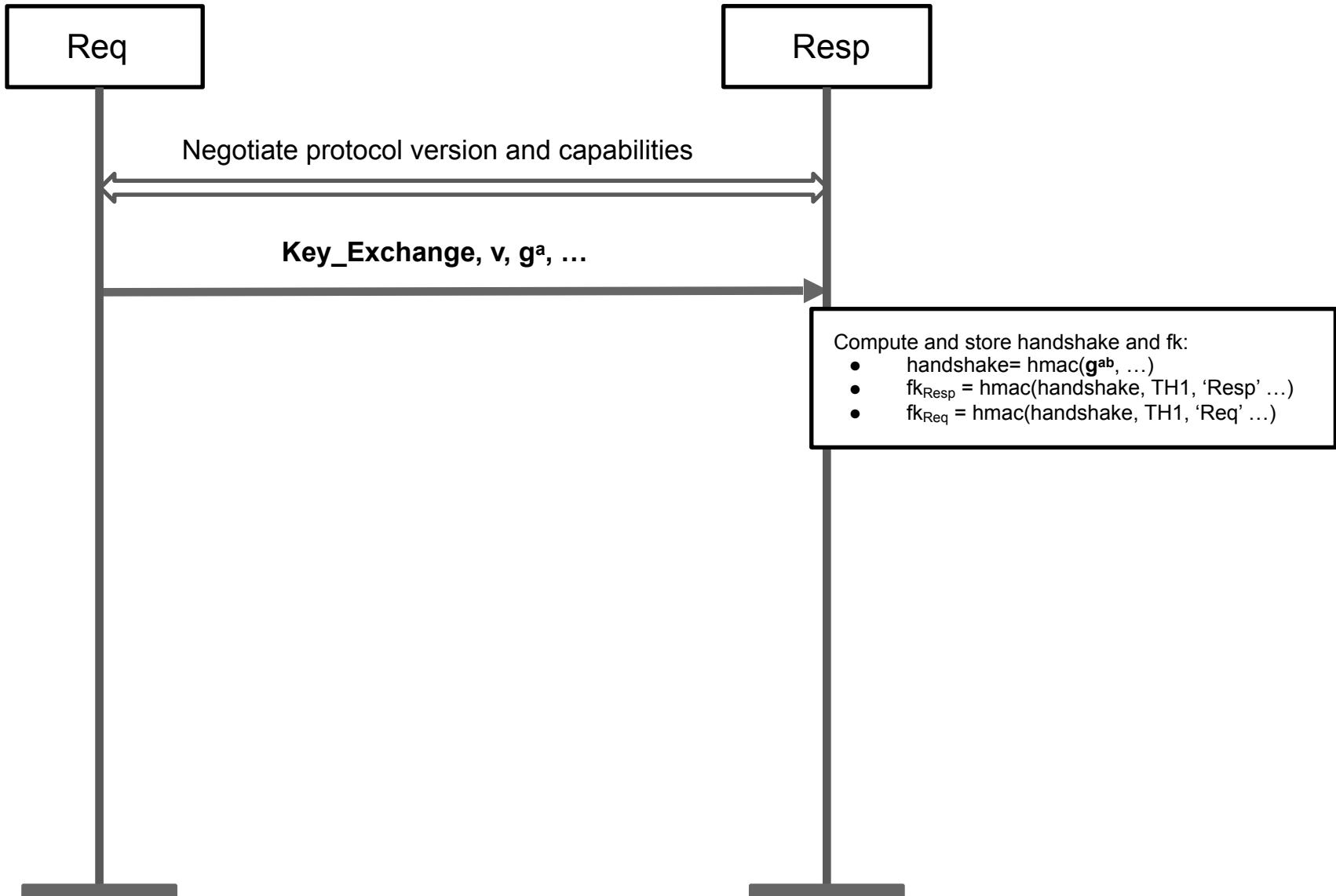


# Mode Switch Attack (found by Tamarin )



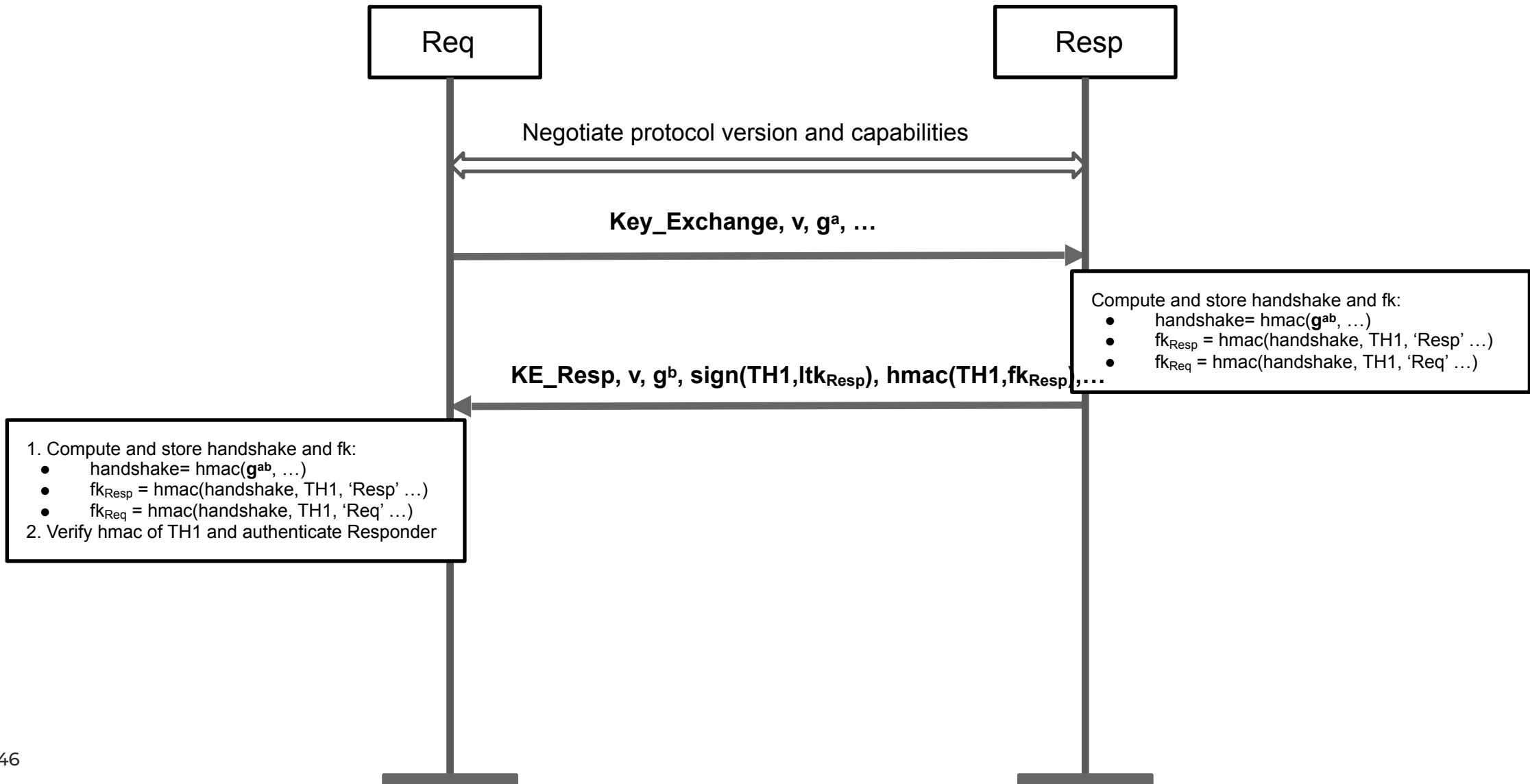


# Mode Switch Attack (found by Tamarin )



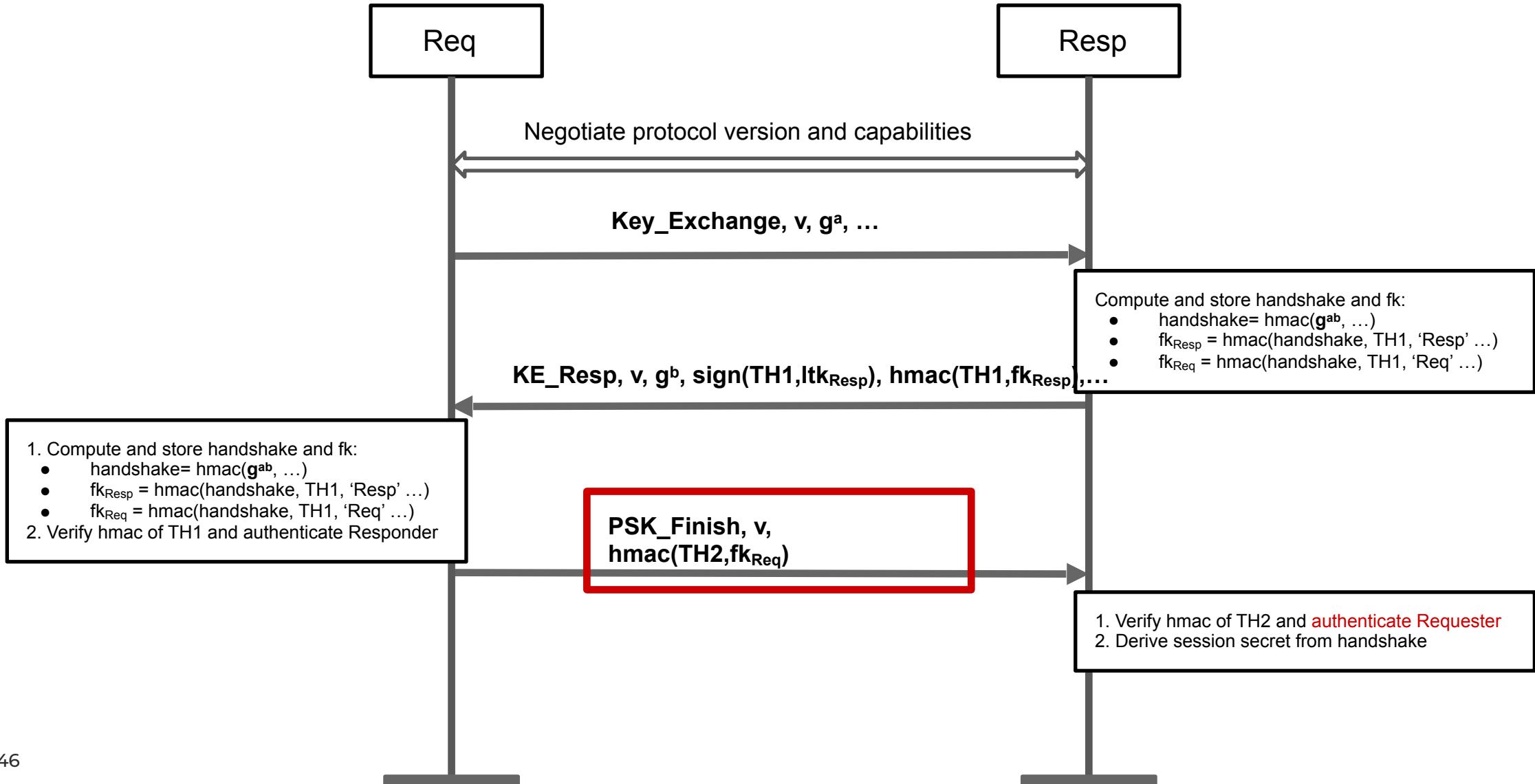


# Mode Switch Attack (found by Tamarin )



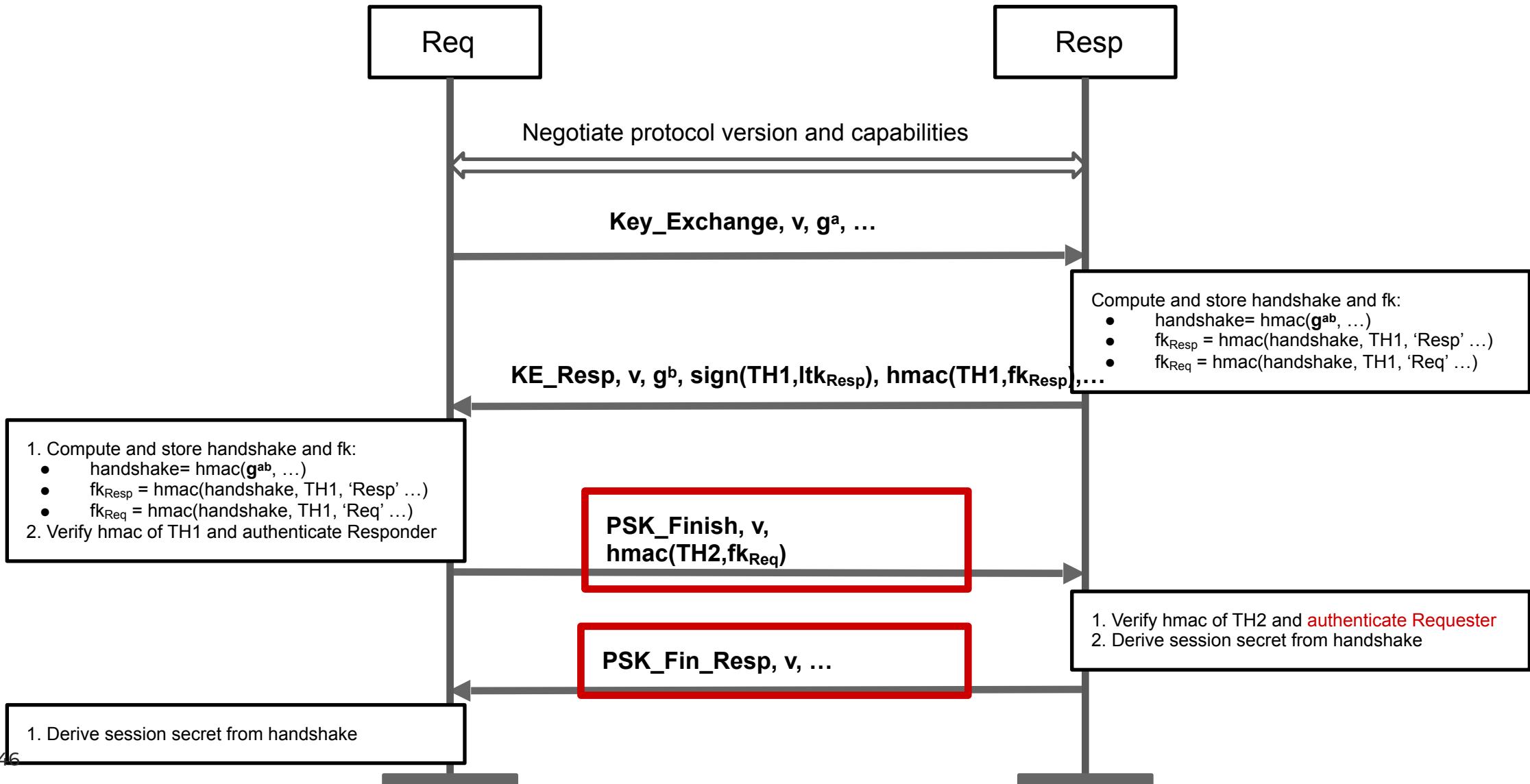


# Mode Switch Attack (found by Tamarin )





# Mode Switch Attack (found by Tamarin )





## SPDM attack on PSK mode

- Attack allows network attacker, without any knowledge, to get responder to accept in PSK mode
  - Breaks mutual authentication
  - Attacker learns key
- Automatically found by the Tamarin prover
- CVE for reference implementation
- Our fixes now in reference C implementation, Intel's Rust implementation, and the new standard



# SPDM attack : outcome

≡

Sign in Register

## CVE-2023-31127

OpenCVE > Vulnerabilities (CVE) > CVE-2023-31127

**libspdm** is a sample implementation that follows the DMTF SPDM specifications. A vulnerability has been identified in SPDM session establishment in libspdm prior to version 2.3.1. If a device supports both DHE session and PSK session with mutual authentication, the attacker may be able to establish the session with `KEY\_EXCHANGE` and `PSK\_FINISH` to bypass the mutual authentication. This is most likely to happen when the Requester begins a session using one method (DHE, for example) and then uses the other method's finish (PSK\_FINISH in this example) to establish the session. The session hashes would be expected to fail in this case, but the condition was not detected. This issue only impacts the SPDM responder, which supports `KEY\_EX\_CAP=1` and `PSK\_CAP=10b` at same time with mutual authentication requirement. The SPDM requester is not impacted. The SPDM responder is not impacted if `KEY\_EX\_CAP=0` or `PSK\_CAP=0` or `PSK\_CAP=01b`. The SPDM responder is not impacted if mutual authentication is not required. libspdm 1.0, 2.0, 2.1, 2.2, 2.3 are all impacted. Older branches are not maintained, but users of the 2.3 branch may receive a patch in version 2.3.2. The SPDM specification (DSP0274) does not contain this vulnerability.

CVSS v3 **8.8 HIGH**

**8.8 /10**

CVSS v3 : HIGH

V3 Legend ⓘ

**Vector :**

**Exploitability : 2.8 / Impact : 5.9**

Attack Vector	NETWORK
Attack Complexity	LOW
Privileges Required	LOW



# Conclusions: the Tamarin Prover



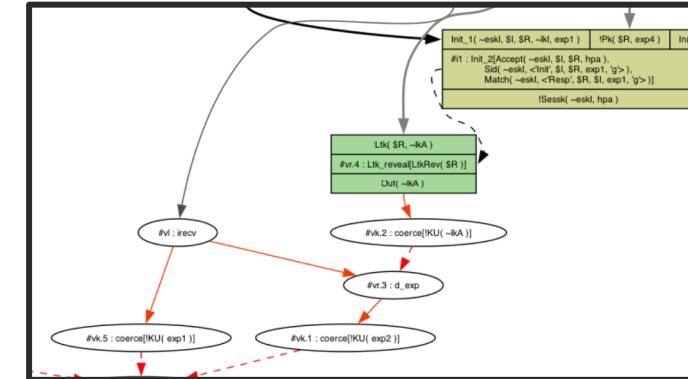
CVE-2023-31127 SPDM

OpenCVE > Vulnerabilities (CVE) > CVE-2023-31127

libspdm is a sample implementation that follows the DMTF SPDM specification in libspdm prior to version 2.3.1. If a device supports both DHE session and

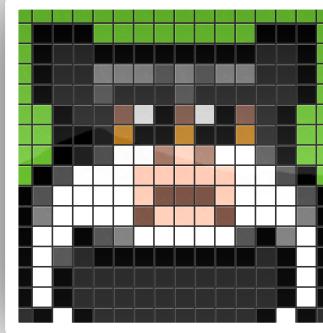
CVSS v3 8.8 HIGH

8.8 / 10



Fine-grained models of  
cryptography

E.g. post-quantum KEMs



[tamarin-prover.com](http://tamarin-prover.com)

[cremers@cispa.de](mailto:cremers@cispa.de)

Open source on github  
Mailing list  
Manual & tutorials  
Upcoming book



## Examples

- Tamarin has been applied to a wide range of protocol problems
  - Library of small examples
  - Several larger case studies
- 
- IETF TLS 1.3
  - SPDM 1.2
  - 5G-AKA
  - Noise protocol suite
  - Apple iMessage with PQ3  
<https://security.apple.com/blog/imessage-pq3/>

*The Real  
End*