

$$dz = \frac{\partial z}{\partial x} dx + \frac{\partial z}{\partial y} dy$$

$$f_x = 3x^2 - 2y \quad f_y = 3y^2 - 2x \quad dx = 0.04 \quad dy = -0.05$$

$$dz = [3(x)^2 - 2(y)] 0.04 + [3(y)^2 - 2(x)] (-0.05)$$

$$= 6(0.04) + 23(-0.05) = 0.24 - 1.15 = -0.91$$

$$\boxed{dz = -0.91}$$

$$5: \quad dx/dy \quad x^2 + y^2 = 4xy \quad x^2 + y^2 - 4xy = 0$$

$$\frac{dx}{dy} = - \frac{f_x}{f_y}$$

$$f_x = 2x - 4y$$

$$f_y = 2y - 4x$$

$$\frac{dx}{dy} = - \frac{2x - 4y}{2y - 4x} = - \frac{x - 2y}{y - 2x}$$

$$\boxed{\frac{dy}{dx} = - \frac{x - 2y}{y - 2x}}$$

$$6: \quad f(x, y, z) = x \sin(y) \cos(z) \quad P(1, 0, 0)$$

$$f_x = \sin(y) \cos(z)$$

$$f_y = x \cos(y) \cos(z)$$

$$f_z = -x \sin(y) \sin(z)$$

$$\nabla f = \begin{bmatrix} \sin(y) \cos(z) \\ x \cos(y) \cos(z) \\ -x \sin(y) \sin(z) \end{bmatrix}$$

$$V = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$$

$$|V| = \sqrt{1^2 + 2^2 + (-1)^2} = \sqrt{1 + 4 + 1} = \sqrt{6}$$

$$\hat{V} = \begin{bmatrix} 1/\sqrt{6} \\ 2/\sqrt{6} \\ -1/\sqrt{6} \end{bmatrix}$$

$$\nabla f(1, 0, 0) = \begin{bmatrix} \sin(0) \cos(0) \\ (1) \cos(0) \cos(0) \\ -(1) \sin(0) \sin(0) \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

$$D_{\hat{V}}(1, 0, 0) = \nabla f(1, 0, 0) \cdot \hat{V} = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1/\sqrt{6} \\ 2/\sqrt{6} \\ -1/\sqrt{6} \end{bmatrix} = 2/\sqrt{6}$$

$$\boxed{D_{\hat{V}}(1, 0, 0) = 2/\sqrt{6}}$$