# Applying Dynamical Systems Modeling to Time-Intensive Data

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## Ecological Momentary Assessment (EMA)

#### **Ecological**

- Real-world environments & experience
- Provides ecological validity

#### **Momentary**

- Real-time assessment & focus
- Avoids recall bias

#### **Assessment**

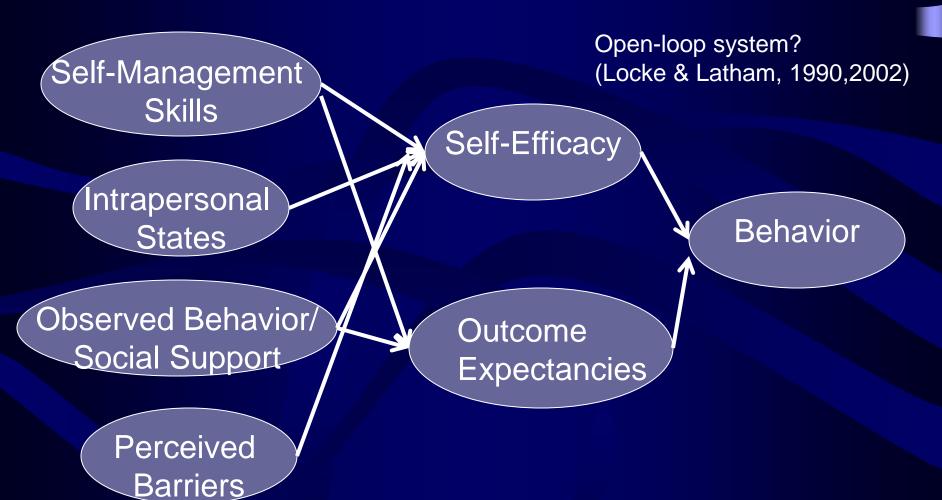
- Self-report
- Repeated
- Intensive Longitudinal Data (ILD)
- Allows analysis of physiological/ psychological/behavioral processes over time





(Stone & Shiffman, 1994)

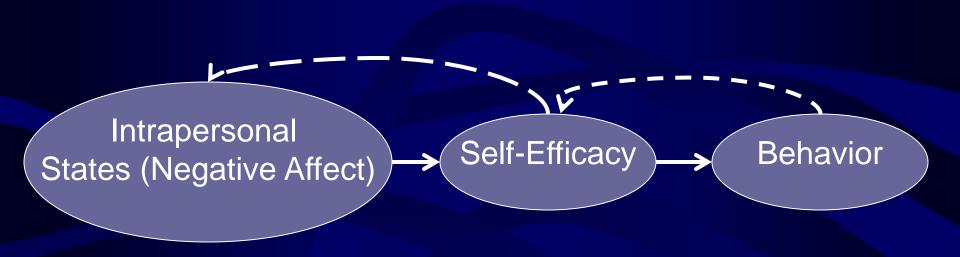
## Social Cognitive Theory (SCT)



## Social Cognitive Theory (SCT)

Closed-loop system? (Carver & Scheier, 1998, 2002) Self-Management Skills Self-Efficacy Intrapersonal **Behavior** States Observed Behavior/ Outcome Social Support Expectancies Perceived Barriers

Intensive Longitudinal Data (ILD) and Ecological Momentary Assessment (EMA) can yield insights into "closed loop" behavior.



# Traditional EMA Data Analytic Techniques

### Multilevel regression modeling

- -Adjusts SE's based on clustering of observations within people
- -Allows effects to vary across people
- -Difficulty with feedback loops, nonlinear effects, and effects that vary dynamically over time
- SAS (PROC Mixed/PROC NL Mixed)
- HLM (Bryk & Raudenbush)
- SPSS (Mixed Models)
- SUDAAN (SEMETHOD=zeger)

# Advantages of Dynamical Systems Modeling of EMA Data

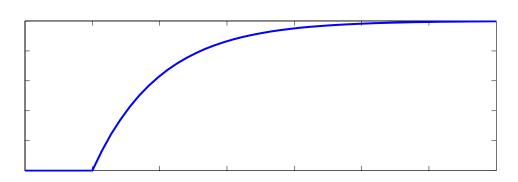
- Better understand the concepts of effect and change in behavioral systems; this includes characterizing speed, shape, and magnitude of response, both within and between participants.
- Allows the more efficient use of intensive longitudinal data.
- Ultimately enables the use of control systems engineering principles for achieving just-in-time adaptive interventions.

### First-Order System

$$\tau \frac{dy}{dt} + y(t) = K \ u(t)$$

#### Output y(t)

(e.g., Craving, Cigarettes Smoked)



#### Input *u(t)*

(e.g., Quitting, Dosage Change, Stress)

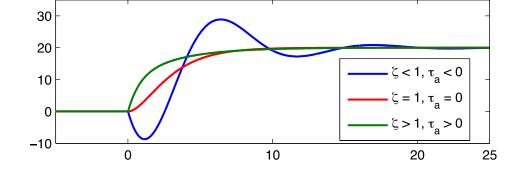
The gain K and time constant tau reflect magnitude and speed-of-response, respectively.

### Second-Order System

$$\tau^2 \frac{d^2 y}{dt^2} + 2\zeta \tau \frac{dy}{dt} + y(t) = K_p \left( u(t) + \tau_a \frac{du}{dt} \right)$$

### Output y(t)

(e.g., Craving, Cigarettes Smoked)



#### Input *u(t)*

(e.g., Quitting, Dosage Change, Stress)

Second-order systems can display underdamped (oscillatory) behavior and "inverse" response.



- Longitudinal EMA study of the psychological, social, and contextual influences on physical activity
- Low- and middle-income adults living in Southern California
- 3 waves of EMA separated by 6 months each

### **EMA Procedures**

- Loaned mobile phone
- Monitoring occurred across 4 days (Sat.-Tues) for each wave
- Signal-interval contingent hybrid sampling

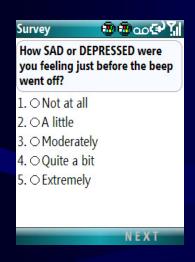
**Ecological Momentary Assessment Prompting Schedule** 

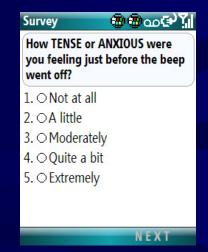
| Day      | 6:30-  | 8-10am | 10am- | 12-2pm | 2-4pm | 4-6pm | 6-8pm | 8-10pm |
|----------|--------|--------|-------|--------|-------|-------|-------|--------|
| _        | 6:45am |        | 12pm  | -      | -     | -     | -     | -      |
| Saturday | X      | Х      | X     | Х      | Х     | Х     | Х     | Х      |
| Sunday   | X      | X      | X     | X      | X     | X     | X     | X      |
| Monday   | X      | X      | X     | X      | X     | X     | X     | X      |
| Tuesday  | X      | Х      | Х     | X      | Х     | X     | X     | X      |

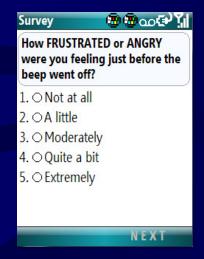
Note: Question sequences are prompted at a random time within each interval.

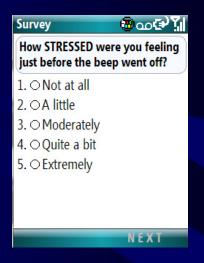
### **EMA Items**

#### Negative Affect (4 items, $\alpha = .87$ )

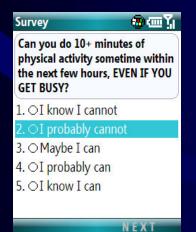


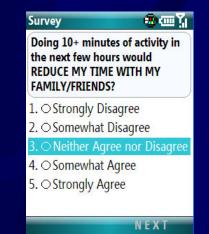






#### Self-Efficacy (2 items, $\alpha = .92$ )





### Accelerometer



- Actigraph GT2M
- Time-stamped and linked with EMA data
- Moderate-to-vigorous physical activity (MVPA) >2200 ct/min (≥ 3 METs)
- Outcome variable: MVPA min in the +60 min after that EMA prompt

## **PARTICIPANTS**

| Table 1: Descriptive Characteristics (wave 2) |   |  |  |  |  |
|---|---|--|--|--|--|
| N   | 97                                      |  |  |  |  |
| Age   | 28-74 years ( $M = 40.6$ , $SD = 9.6$ ) |  |  |  |  |
| Sex   | 72% Female                              |  |  |  |  |
| Ethnicity                                     | 34% Hispanic                            |  |  |  |  |
| Income  | 24% < \$40,000/year                     |  |  |  |  |
| Marital Status                                | 66% Married                             |  |  |  |  |
| Weight Status                                 | 64% Overweight/Obese                    |  |  |  |  |

# Dynamical Systems Modeling Approach

- Average responses at each time "bucket" over all participants to obtain a time series per construct
- Visualize the data
- Consult experts to determine the proper set of inputs and outputs to examine
- Apply AutoRegressive with eXternal (ARX) estimation
- Validate through multiple measures (goodness of fit, simulation/cross-validation, and step response)

goodness-of-fit (%) = 100 
$$\left(1 - \frac{||y(t) - \tilde{y}(t)||_2}{||y(t) - \bar{y}||_2}\right)$$

## Model Structure

 $ARX-[n_a n_b n_k]$  model structure

$$y(t) + \dots + a_{n_a}y(t - n_a) = b_{11}u_1(t - n_k) + \dots + b_{n_b1}u_1(t - n_k - n_b + 1)$$

$$\vdots$$

$$+ b_{1i}u_i(t - n_k) + \dots + b_{n_bi}u_i(t - n_k - n_b + 1)$$

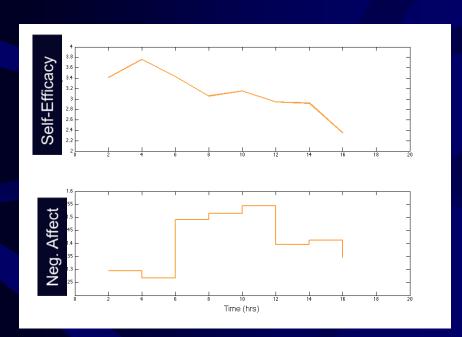
$$\vdots$$

$$+ b_{1n_u}u_{n_u}(t - n_k) + \dots + b_{n_bn_u}u_{n_u}(t - n_k - n_b + 1) + e(t)$$

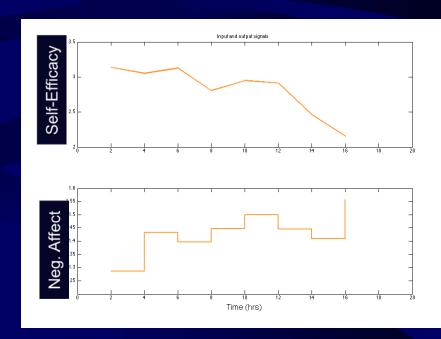
- Lagged set of inputs  $u_1(t)...u_{n_u}(t)$  and output y(t)
- Parameters readily estimated using linear regression
- Subsequent estimation step can lead to a system of continuous differential equations

## Raw Descriptive Data for Input (Neg. Affect) and Output (Self-Efficacy)

Wave 2, Day 1: Saturday



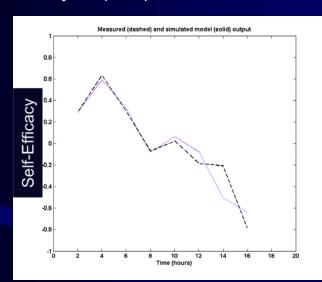
Wave 2, Day 4: Tuesday



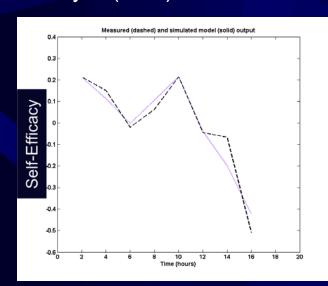
## Self-Efficacy as a Function of Neg. Affect

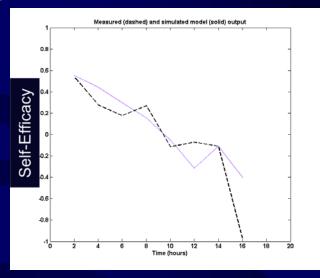
Day 1 (Sat): Fit 68.65%

ARX-[4 4 1] Day 2 (Sun): Fit 44.72%

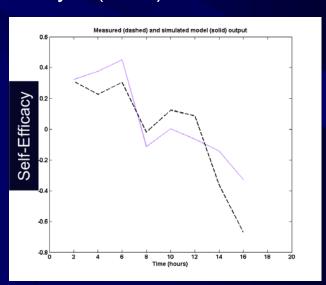


Day 3 (Mon): Fit 72.68%





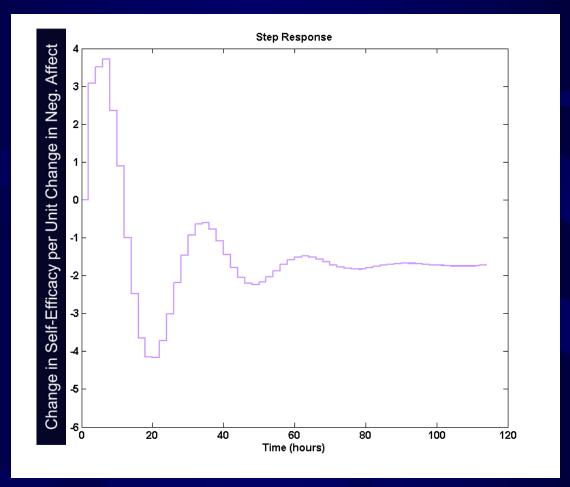
Day 4 (Tues): Fit 45.18%



## Step Response for the Relationship Between Neg. Affect and Self-Efficacy

Estimation using days 1-4

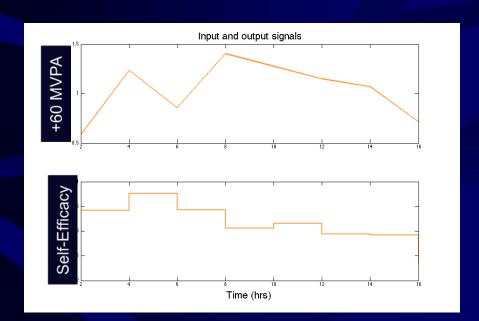
ARX-[4 4 1]



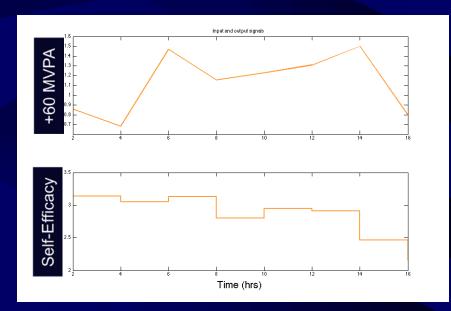
Response is underdamped and shows inverse response. System gain has sign in the expected direction.

## Raw Descriptive Data for Input (Self-Efficacy) and Output (+60 MVPA)

Wave 2, Day 1: Saturday

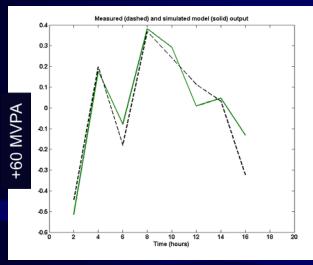


Wave 2, Day 4: Tuesday

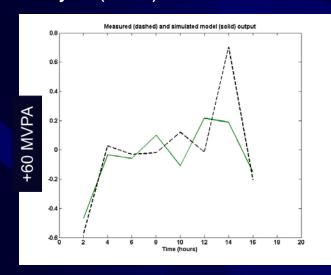


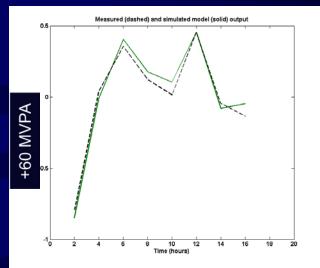
## +60 MVPA as a Function of Neg. Affect

Day 1 (Sat): Fit 66.73% ARX-[4 4 1] Day 2 (Sun): Fit 83.52%

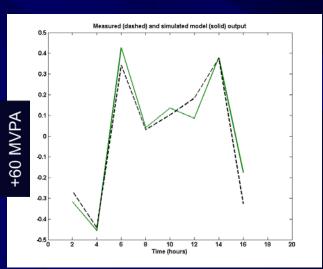


Day 3 (Mon): Fit 32.52%





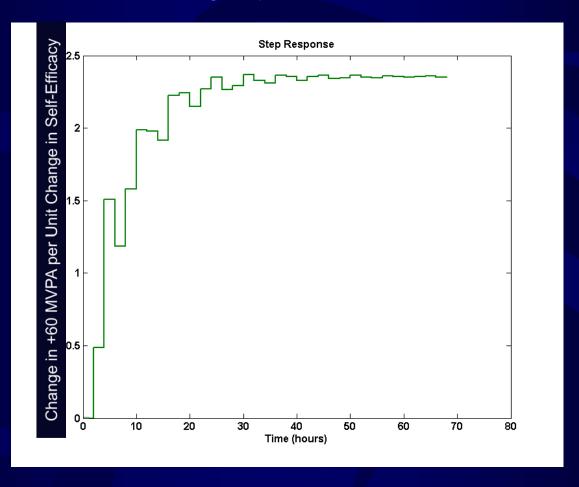
Day 4 (Tues): Fit 74.63%



## Step Response for the Relationship Between Neg. Affect and Self-Efficacy

Estimation using Days 1-4

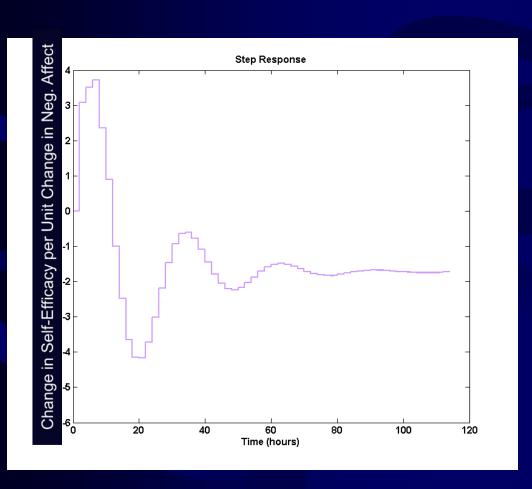
ARX-[4 4 1]



### Some Observations

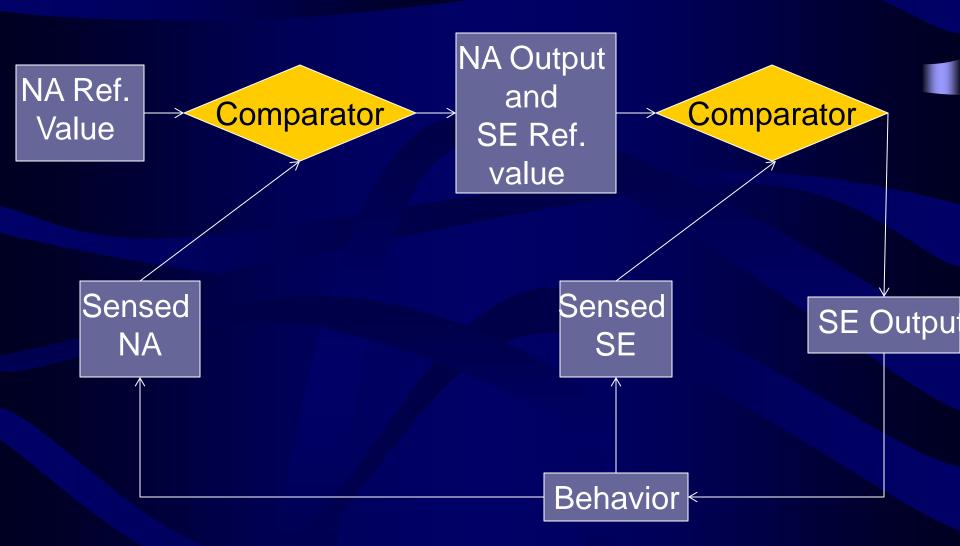
- Many possibilities exist for examining the data exhaustively, based on per day, weekend vs. weekday, discrete-time vs. continuous-time models, etc.
- Each day has its own interesting dynamics; eight data points, however, limited what could be estimated at a single day level.
- Including additional days facilitated the use of higherorder models and gave greater flexibility to the estimator, at the expense of better knowledge of differences between days, weekend vs. weekday, etc.
- Many possibilities for cross-validation that need to be further investigated.
- As a observational study, limited excitation impacts the results (particularly in the self-efficacy modeling).

# Negative Affect → Self-efficacy: Underdamped Response



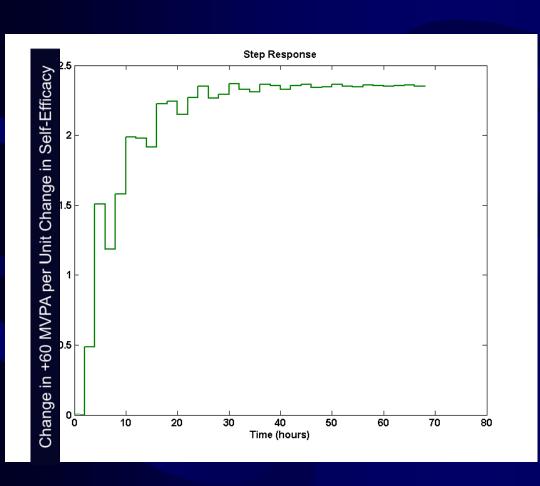
- Oscillating pattern with initial "inverse response"
- Highly transient/shortterm effects
- Within-person changes in direction of association
- Denotes "aggressive" or "over-compensatory" control "at the threshold of stability"

## Systems Theory of Self-Regulation



Carver & Scheier, 1990, 1998

# Self-Efficacy → MVPA: Overdamped Response



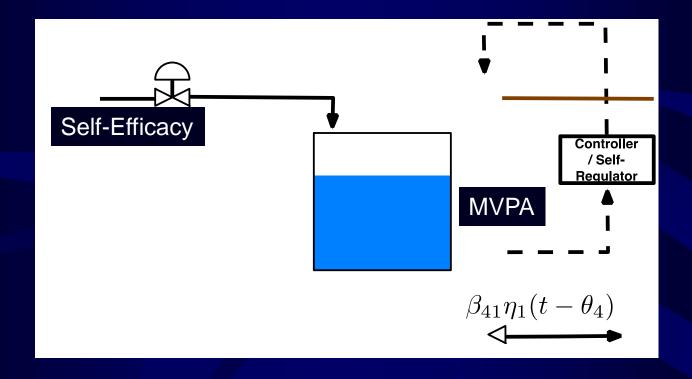
#### Possibility #1

- Closed-loop system with a well-tuned controller
- Negative Feedback

#### Possibility #2

 Open-loop system reflecting a basic accumulation-depletion process (i.e., fluid analogy)

# Fluid Analogy Depicting Self-Regulation



The fluid analogy depicts accumulation-depletion of the output (*MVPA*) as a result of changes in the input (*self-efficacy*). A controller / self-regulator relying on a sensed value of the output attempts to compensate for the input change, resulting in potentially significant variability.

# Comparable Systems Theories in Psychology/Biology

#### Underdamped response (over-compensatory self-regulation)

- Stress-induced shift from goal-directed to habit behavior (Schwabe & Wolf, 2009, 2010)
- General Adaptation Syndrome (Selye)

### Overdamped response (well-tuned self-regulation)

- Goal-directed behavior (Carver & Scheier)
- Ideal/ought selves, approach/avoidance (Higgins)

## Ongoing Issues/Challenges to Consider

- Consider revisiting the experimental
  - Generate a more time-intensive data set
  - Facilitate cross-validation
  - Measure and/or revise constructs to enable more persistent excitation in the data, reduce correlations between signals and allow for "reverse-engineering" the self-regulator
- Examine model structures that include nonlinearity or time-varying parameters
- Apply methods for estimating differential equations that are more in line with statistical methodological approaches (e.g., Trail et al., Psych Methods, in press).

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## Thank You



