# Columbia Business School

## BA Excel Add-In User's Manual (Version 0.0.36)

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### 1. The BA Add-In Functions

### 1.1. Linear Regression Functions

### 1.1.1. LinearRegTrain

The example illustrated below is available on the add-in webpage by downloading the Linear and Logistic Regression file and going to the linear Reg sheet.

**LinearRegTrain** is an array function that allows you to estimate the coefficients  $(\beta_0, \beta_1, ..., \beta_K)$  of a regression equation of the form

$$Y = \beta_0 + \beta_1 Var1 + \beta_2 Var2 + ... + \beta_K VarK + \epsilon$$

using observed data on the independent variables (Var1, Var2, ..., VarK) and on the dependent variable Y. This function outputs the estimated coefficients, the standard errors, the associated p-values, and the R-squared of the regression.

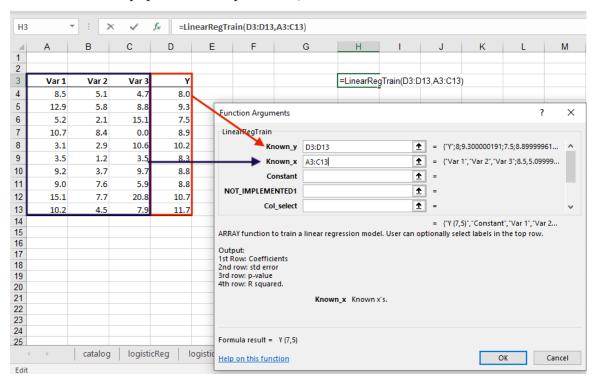
We illustrate how this function works with a dataset that contains 10 observations of 3 independent variables (Var1, Var2, Var3) and the dependent variable Y.

To use the function:

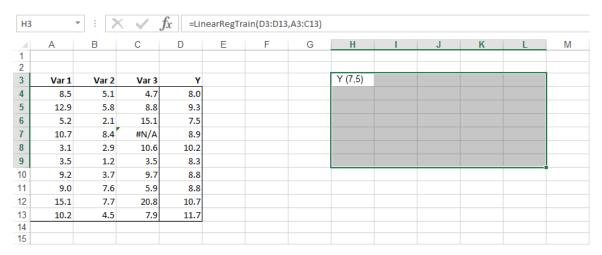
1. Select the cell where you want to display the output (H3 in the example) and call the function by typing =LinearRegTrain( and then clicking on the  $f_x$  symbol next to the formula bar. (Alternatively, you can call the function by clicking on the  $f_x$  symbol first, which will display a menu of all available functions, and then clicking on LinearRegTrain.)

НЗ		- : ×	~	f <sub>∞</sub> =Lin	earRegTr	ain(					
4	Α	В	С	D	Е	F	G	Н	1	J	K
1											
2											
3	Var 1	Var 2	Var 3	Y				=LinearRe	gTrain(		
4	8.5	5.1	4.7	8.0							
5	12.9	5.8	8.8	9.3							
6	5.2	2.1	15.1	7.5							
7	10.7	8.4	0.0	8.9							
8	3.1	2.9	10.6	10.2							
9	3.5	1.2	3.5	8.3							
10	9.2	3.7	9.7	8.8							
11	9.0	7.6	5.9	8.8							
12	15.1	7.7	20.8	10.7							
13	10.2	4.5	7.9	11.7							
14											
15 16 17											
16											
17											

2. When you call the function, the window Function Arguments will appear. Follow the instructions to populate the input fields, then click OK.



3. The string Y(7,5) will appear in cell H3, where Y is the name of the variable in cell D3. This indicates that you should select an output array of 7 rows and 5 columns. Select the output array starting from cell H3 as the next figure shows.



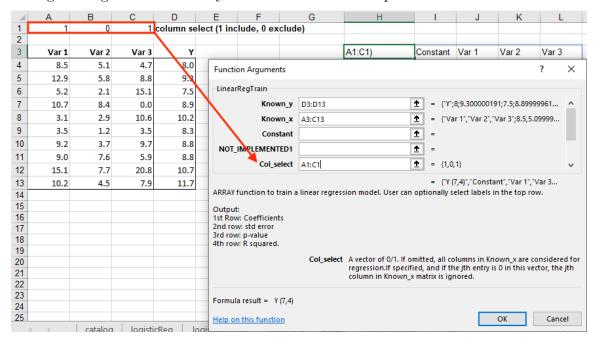
4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the output. Remark: for recent versions of Excel, this step is not necessary.

4	Α	В	С	D	Е	F	G	Н	1	J	K	L
1												
2												
3	Var 1	Var 2	Var 3	Υ				Y (7,5)	Constant	Var 1	Var 2	Var 3
4	8.5	5.1	4.7	8.0				Coefficients	7.837367	0.120385	-0.00744	0.042174
5	12.9	5.8	8.8	9.3				Std error	1.292461	0.229497	0.348021	0.091981
6	5.2	2.1	15.1	7.5				p-value	0.09%	61.87%	98.36%	66.27%
7	10.7	8.4	0.0	8.9				R-sqr	0.197115			
8	3.1	2.9	10.6	10.2				Number valid obs	10			
9	3.5	1.2	3.5	8.3				Total obs	10			
10	9.2	3.7	9.7	8.8								
11	9.0	7.6	5.9	8.8								
12	15.1	7.7	20.8	10.7								
13	10.2	4.5	7.9	11.7								
14												
15												

The second row of the output contains the estimates of the coefficients: the column (Constant) refers to the coefficient  $\beta_0$ , while the columns (Var1,Var2,Var3) refer to the coefficients  $(\beta_1, \beta_2, \beta_3)$  respectively. In the following rows we have standard errors and p-values of the estimates as well as the  $R^2$  of the regression. The last two rows contain the number of valid observations and the total number of observations respectively.

You can also format the output to display only three decimals and to display percentages.

**Optional Input: Col\_select.** The optional input Col\_select allows you to specify which variables you want to include in your regression. For example, the configuration below runs a logistic regression with only Var1 and Var3 as independent variables.



### 1.1.2. LinearRegPredict

The example illustrated below is available on the add-in webpage by downloading the Linear and Logistic Regression file and going to the linear Reg sheet.

**LinearRegPredict** uses the coefficients  $(\beta_0^e, \beta_1^e, ..., \beta_K^e)$  that we estimate with **LinearReg-Train** and the data on the independent variables (Var1, Var2, ..., VarK) to compute a prediction for the dependent variable using the formula

$$\mathbf{Y}^{\mathbf{p}} = \beta_0^e + \beta_1^e \mathbf{Var1} + \beta_2^e \mathbf{Var2} + \ldots + \beta_K^e \mathbf{VarK}.$$

For example, using the coefficients that we estimated in the **LinearRegTrain** example we would predict Y using the following formula

$$Y^p = 7.854 + 0.114Var1 + 0.023Var2 + 0.034Var3$$

which, for the first observation, yields a prediction of

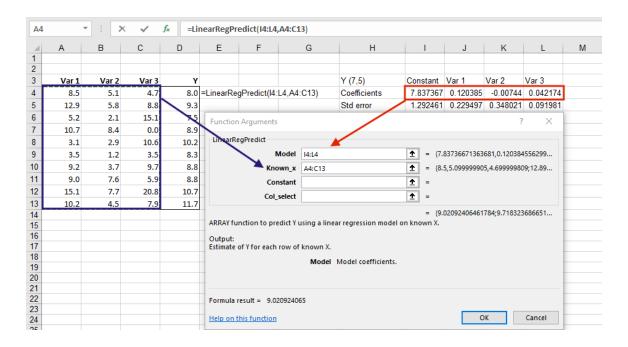
$$9.1001 = 7.854 + 0.114 * 8.5 + 0.023 * 5.1 + 0.034 * 4.7.$$

To use the function:

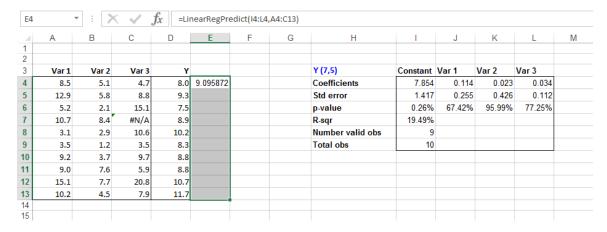
1. Select the first cell in which you want the output to be displayed; call the function by typing =LinearRegPredict( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.

SUN	1	- : ×	~	f <sub>x</sub> =Lin	nearRegPre	dict(							
4	Α	В	С	D	Е	F	G	Н	1	J	K	L	M
1													
2				.,				V (7.5)	0	V 4	\/ 0	V 2	
3	Var 1	Var 2	Var 3	Υ				Y (7,5)		Var 1	Var 2	Var 3	
4	8.5	5.1	4.7	8.0	=LinearReg	Predict(		Coefficients	7.837367	0.120385	-0.00744	0.042174	
5	12.9	5.8	8.8	9.3				Std error	1.292461	0.229497	0.348021	0.091981	
6	5.2	2.1	15.1	7.5				p-value	0.09%	61.87%	98.36%	66.27%	
7	10.7	8.4	0.0	8.9				R-sqr	0.197115				
8	3.1	2.9	10.6	10.2				Number valid obs	10				
9	3.5	1.2	3.5	8.3				Total obs	10				
10	9.2	3.7	9.7	8.8									
11	9.0	7.6	5.9	8.8									
12	15.1	7.7	20.8	10.7									
13	10.2	4.5	7.9	11.7									
14													
15 16													
16													

2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click OK.



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of observations that will contain the predictions associated to each observation. In the figure below, we have 10 observations and we select cells E4:E13.



4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title (for example "LinearRegPredict") to the output-column and format the output-cells to display only the first 3 decimals, as in the figure below. Remark: for recent versions of Excel, this step is not necessary.

E4		▼] : [×	· ·	f <sub>x</sub> =Lin	nearRegPre	dict(I4:L4,	A4:C13)						
4	Α	В	С	D	Е	F	G	Н	1	J	K	L	М
1													
2													
3	Var 1	Var 2	Var 3	Y				Y (7,5)	Constant	Var 1	Var 2	Var 3	
4	8.5	5.1	4.7	8.0	9.020924			Coefficients	7.837367	0.120385	-0.00744	0.042174	
5	12.9	5.8	8.8	9.3	9.718324			Std error	1.292461	0.229497	0.348021	0.091981	
6	5.2	2.1	15.1	7.5	9.084577			p-value	0.09%	61.87%	98.36%	66.27%	
7	10.7	8.4	0.0	8.9	9.063009			R-sqr	0.197115				
8	3.1	2.9	10.6	10.2	8.636036			Number valid obs	10				
9	3.5	1.2	3.5	8.3	8.397397			Total obs	10				
10	9.2	3.7	9.7	8.8	9.326475								
11	9.0	7.6	5.9	8.8	9.113132								
12	15.1	7.7	20.8	10.7	10.47513								
13	10.2	4.5	7.9	11.7	9.364997								
14													
15 16													
16													

**Optional Input: Col\_select.** See explanation at the end of Section 1.1.1.

### 1.2. Logistic Regression Functions

### 1.2.1. LogisticRegTrain

The example illustrated below is available on the add-in webpage by downloading the Linear and Logistic Regression file and going to the logistic Reg sheet.

**LogisticRegTrain** is an array function that allows you to estimate the coefficients  $(\beta_0, \beta_1, ..., \beta_K)$  of a logistic regression model using observed data on the independent variables (Var1, Var2, ..., VarK) and on the dependent variable Y. Note that the dependent variable in a logistic regression must be binary, i.e. it must take values 0 or 1. This function outputs the estimated coefficients, the standard errors, and the associated p-values. This function allows you to estimate the probability that the dependent variable is equal to 1 as

$$Pr(\text{dependent variable equals one}) = \frac{\exp(w)}{1 + \exp(w)},$$

with

$$w = \beta_0 + \beta_1 \text{Var1} + \beta_2 \text{Var2} + ... + \beta_K \text{VarK}.$$

We illustrate how this function works with a dataset that contains 18 observations of 3 independent variables (Var1, Var2, Var3) and the dependent variable Y.

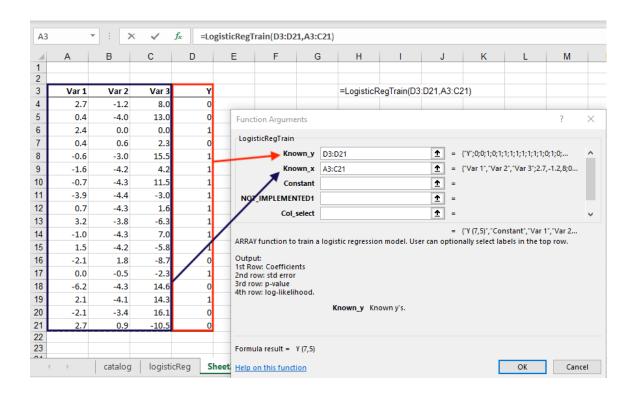
To use the function:

1. Select the cell where you want to display the output (H3 in the example) and call the function by typing =LogisticRegTrain( and then clicking on the  $f_x$  symbol next to the formula bar. (Alternatively, you can call the function by clicking on the  $f_x$ 

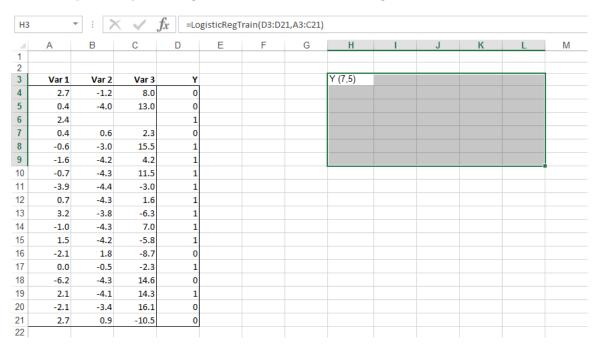
symbol first, which will display a menu of all available functions, and then clicking on LogisticRegTrain.)

SUN	1	- : ×	· .	f <sub>x</sub> =Log	gisticReg	Train(				
4	Α	В	С	D	Е	F	G	Н	1	J
1										
2	Var 1	Var 2	Var 3	Υ				=LogisticF	RegTrain(	
4	2.7	-1.2	8.0	0						
5	0.4	-4.0	13.0	0						
6	2.4	0.0	0.0	1						
7	0.4	0.6	2.3	0						
8	-0.6	-3.0	15.5	1						
9	-1.6	-4.2	4.2	1						
10	-0.7	-4.3	11.5	1						
11	-3.9	-4.4	-3.0	1						
12	0.7	-4.3	1.6	1						
13	3.2	-3.8	-6.3	1						
14	-1.0	-4.3	7.0	1						
15	1.5	-4.2	-5.8	1						
16	-2.1	1.8	-8.7	0						
17	0.0	-0.5	-2.3	1						
18	-6.2	-4.3	14.6	0						
19	2.1	-4.1	14.3	1						
20	-2.1	-3.4	16.1	0						
21	2.7	0.9	-10.5	0						

2. When you call the function, the window Function Arguments will appear. Follow the instructions to populate the input fields, then click  $\tt OK$ .



3. The string Y(7,5) will appear in cell H3, where Y is the name of the variable in cell D3. This indicates that you should select an output array of 7 rows and 5 columns. Select the output array starting from cell H3 as the next figure shows.



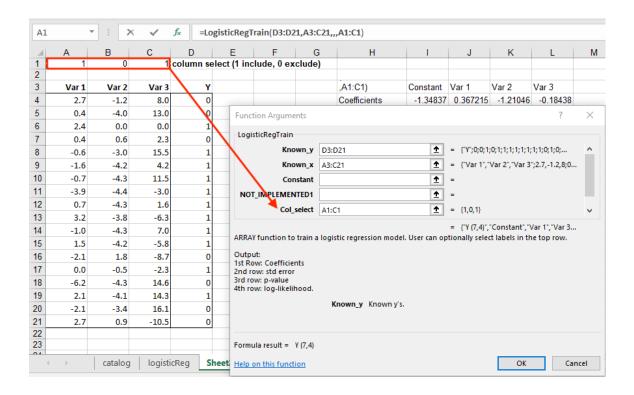
4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the output. Remark: for recent versions of Excel, this step is not necessary.

N11	•	· i ×	~	f <sub>x</sub>									
4	Α	В	С	D	Е	F	G	Н	1	J	K	L	М
1													
2													
3	Var 1	Var 2	Var 3	Y				Y (7,5)	Constant		Var 2	Var 3	
4	2.7	-1.2	8.0	0				Coefficients	-1.34837	0.367215	-1.21046	-0.18438	
5	0.4	-4.0	13.0	0				Std error	1.054453	0.314121	0.588221	0.124832	
6	2.4	0.0	0.0	1				p-value	20.10%	24.24%	3.96%	13.97%	
7	0.4	0.6	2.3	0				Log-likelihood	-7.36825				
8	-0.6	-3.0	15.5	1				Number valid obs	18				
9	-1.6	-4.2	4.2	1				Total obs	18				
10	-0.7	-4.3	11.5	1									
11	-3.9	-4.4	-3.0	1									
12	0.7	-4.3	1.6	1									
13	3.2	-3.8	-6.3	1									
14	-1.0	-4.3	7.0	1									
15	1.5	-4.2	-5.8	1									
16	-2.1	1.8	-8.7	0									
17	0.0	-0.5	-2.3	1									
18	-6.2	-4.3	14.6	0									
19	2.1	-4.1	14.3	1									
20	-2.1	-3.4	16.1	0									
21	2.7	0.9	-10.5	0									
22				_									

The second row of the output contains the estimates of the coefficients: the column (Constant) refers to the coefficient  $\beta_0$ , while the columns (Var1,Var2,Var3) refer to the coefficients  $(\beta_1, \beta_2, \beta_3)$  respectively. In the following rows we have standard errors and p-values of the estimates. The last two rows contain the number of valid observations and the total number of observations respectively.

You can also format the output to display only three decimals and to display percentages.

**Optional Input: Col\_select.** The optional input Col\_select allows you to specify which variables you want to include in your regression. For example, the configuration below runs a logistic regression with only Var1 and Var3 as independent variables.



### 1.2.2. LogisticRegPredict

The example illustrated below is available on the add-in webpage by downloading the Linear and Logistic Regression file and going to the logistic Reg sheet.

**LogisticRegPredict** uses the coefficients  $(\beta_0^e, \beta_1^e, ..., \beta_K^e)$  that we estimate with **LogisticRegTrain** and the data on the independent variables (Var1, Var2, ..., VarK) to compute a prediction p for the probability that the dependent variable is equal to 1. The prediction is calculated in two steps:

(i) Obtain the exponent w of the logistic function as

$$w = \beta_0^e + \beta_1^e \mathtt{Var1} + \beta_2^e \mathtt{Var2} + \ldots + \beta_K^e \mathtt{VarK}.$$

(ii) Calculate the probability that Y=1 as follows

$$p = \frac{\exp(w)}{1 + \exp(w)}.$$

For example, using the coefficients that we estimated in the **LogisticRegTrain** example we would predict p for the first observation in the example as follows

$$w = -2.047 + 0.301 * 2.7 - 1.432 * (-1.2) - 0.207 * 8 = -1.172$$

and

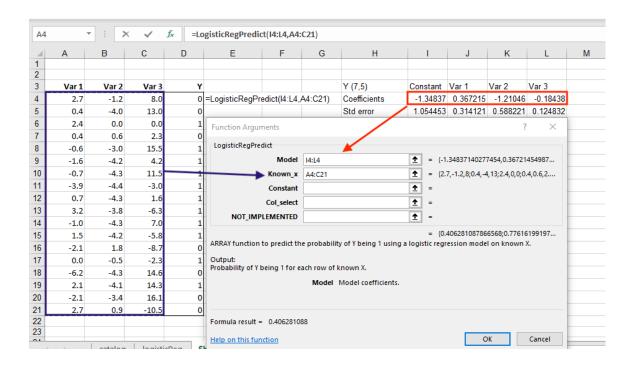
$$p = \frac{\exp(-1.172)}{1 + \exp(-1.172)} = 23.61\%$$

To use the function:

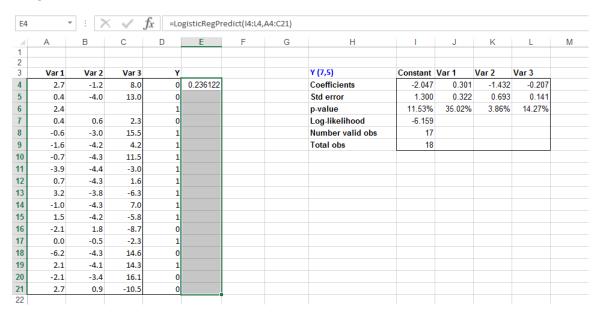
1. Select the first cell in which you want the output to be displayed; call the function by typing =LogisticRegPredict( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.

							_						
SU	М	T : >	× •/	f <sub>x</sub> =Lo	gisticRegPred	lict(							
4	Α	В	С	D	Е	F	G	Н	1	J	K	L	М
1													
2				.,				V (7.5)	01	V 4	V 0	V 2	
	Var 1	Var 2	Var 3					Y (7,5)		Var 1	Var 2	Var 3	
4	2.7	-1.2	8.0	0	=LogisticRegF	Predict(		Coefficients	-1.34837	0.367215	-1.21046	-0.18438	
5	0.4	-4.0	13.0	0				Std error	1.054453	0.314121	0.588221	0.124832	
6	2.4	0.0	0.0	1				p-value	20.10%	24.24%	3.96%	13.97%	
7	0.4	0.6	2.3	0				Log-likelihood	-7.36825				
8	-0.6	-3.0	15.5	1				Number valid obs	18				
9	-1.6	-4.2	4.2	1				Total obs	18				
10	-0.7	-4.3	11.5	1									
11	-3.9	-4.4	-3.0	1									
12	0.7	-4.3	1.6	1									
13	3.2	-3.8	-6.3	1									
14	-1.0	-4.3	7.0	1									
15	1.5	-4.2	-5.8	1									
16	-2.1	1.8	-8.7	0									
17	0.0	-0.5	-2.3	1									
18	-6.2	-4.3	14.6	0									
19	2.1	-4.1	14.3	1									
20	-2.1	-3.4	16.1	0									
21	2.7	0.9	-10.5	0									
22													

2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click  $\tt OK$ .



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of observations that will contain the predictions associated to each observation. In the figure below, we have 18 observations and we select cells E4:E21.



4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title (for example "LogisticRegPredict") to the output-column and format the output-cells to display percentages, as in the figure below. Remark: for recent versions of Excel, this step is not necessary.

A2		:   ×	~	f <sub>x</sub>									
4	Α	В	С	D	E	F	G	Н	1	J	K	L	M
1													
2	Var 1	Var 2	Var 3	Y				Y (7,5)	Constant	Var 1	Var 2	Var 3	
4	2.7	-1.2	8.0	0	0.406281088			Coefficients	-1.34837	0.367215	-1.21046	-0.18438	
5	0.4	-4.0	13.0	0	0.776161992			Std error	1.054453	0.314121	0.588221	0.124832	
6	2.4	0.0	0.0	1	0.385313171			p-value	20.10%	24.24%	3.96%	13.97%	
7	0.4	0.6	2.3	0	0.086920689			Log-likelihood	-7.36825				
8	-0.6	-3.0	15.5	1	0.311058582			Number valid obs	18				
9	-1.6	-4.2	4.2	1	0.91479336			Total obs	18				
10	-0.7	-4.3	11.5	1	0.814452492								
11	-3.9	-4.4	-3.0	1	0.956836256								
12	0.7	-4.3	1.6	1	0.9785141								
13	3.2	-3.8	-6.3	1	0.996271542								
14	-1.0	-4.3	7.0	1	0.900136079								
15	1.5	-4.2	-5.8	1	0.995301276								
16	-2.1	1.8	-8.7	0	0.063312717								
17	0.0	-0.5	-2.3	1	0.420900958								
18	-6.2	-4.3	14.6	0	0.247490071								
19	2.1	-4.1	14.3	1	0.851834057								
20	-2.1	-3.4	16.1	0	0.274394336								
21 22	2.7	0.9	-10.5	0	0.620025405								

**Optional Input: Col\_select.** See explanation at the end of Section 1.2.1.

### 1.3. K-Nearest Neighbor Functions (Content-based)

*Tip:* The functions in this section do content-based prediction, which means that they predict a score (or rating) based on other known attributes of content. The dependent variable (score or rating) and the independent variables (other attributes) are distinct, and in general you need information on both to be able to use these functions.

### 1.3.1. knn\_in

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn sheet.

knn\_in applies the k-nearest neighbor algorithm to make predictions within a specified sample. The inputs of the function are: the parameter k of nearest neighbor to match; the known variables (Var1, Var2, ..., VarM), on the basis of which the observations are matched; the known outcomes Y. The nearest neighbor to a given observation are the observations which have minimum Euclidean distance

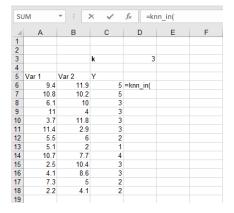
$$d(i,j) = \sqrt{(\mathtt{Var1}_i - \mathtt{Var1}_j)^2 + (\mathtt{Var2}_i - \mathtt{Var2}_j)^2 + ... + (\mathtt{VarM}_i - \mathtt{VarM}_j)^2}$$

and the prediction p is computed as a simple average of the k-nearest neighbor outcomes

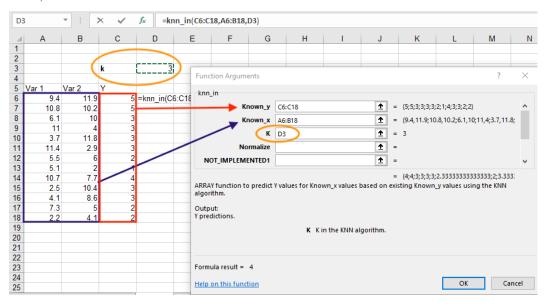
$$p = \frac{\mathbf{Y}_1 + \mathbf{Y}_2 + \dots + \mathbf{Y}_k}{k}.$$

To use the function:

1. Write the parameter k in an empty cell, k=3 in the example below; select the first cell in which you want the output to be displayed; call the function by typing  $=knn_i$  (in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click  $\tt OK$ .



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of observations. In the figure below, we selected cells D6:D18.

D6		· : ×	<b>/</b>	$f_{\mathcal{X}}$ =kn	n_in(C6:C	L8,A6:B18,	03)
4	Α	В	С	D	Е	F	G
1							
2							
3			k	3			
4							
5	Var 1	Var 2	Y				
6	9.4	11.9	5	4.00			
7	10.8	10.2	5				
8	6.1	10.0	3				
9	11.0	4.0	3				
10	3.7	11.8	3				
11	11.4	2.9	3				
12	5.5	6.0	2				
13	5.1	2.0	1				
14	10.7	7.7	4				
15	2.5	10.4	3				
16	4.1	8.6	3				
17	7.3	5.0	2				
18	2.2	4.1	2				
19							
20							

4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title (for example "knn\_in predict") to the output-column and format the output-cells to display only the first two decimals. Remark: for recent versions of Excel, this step is not necessary.

G	5	<b>-</b> : :	×	<b>~</b>	f <sub>x</sub>		
4	Α	В		С	D	Е	F
1							
2							
3			k		3		
4							
5	Var 1	Var 2	Υ				
6	9.4	11.9		5	4.00		
7	10.8	10.2		5	4.00		
8	6.1	10		3	3.00		
9	11	4		3	3.00		
10	3.7	11.8		3	3.00		
11	11.4	2.9		3	3.00		
12	5.5	6		2	2.33		
13	5.1	2		1	2.00		
14	10.7	7.7		4	3.33		
15	2.5	10.4		3	3.00		
16	4.1	8.6		3	2.67		
17	7.3	5		2	2.00		
18	2.2	4.1		2	2.00		
19							

### 1.3.2. knn\_in\_rmse

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn\_full sheet.

knn\_in\_rmse is a function that computes the Root Mean Squared Error (RMSE) for k-nearest neighbor predictions (as the ones you can obtain with knn\_in).

The inputs of the function are: the known variables (Var1, Var2, ..., VarM) on the basis of which the observations are matched; the known outcomes Y; the parameter k for which we want to compute the RMSE of predictions.

For a given k, the error is computed as follows

$$RMSE = \sqrt{\frac{(Y_1 - p_1)^2 + (Y_2 - p_2)^2 + \dots + (Y_N - p_N)^2}{N}},$$

where N is the total number of observations.

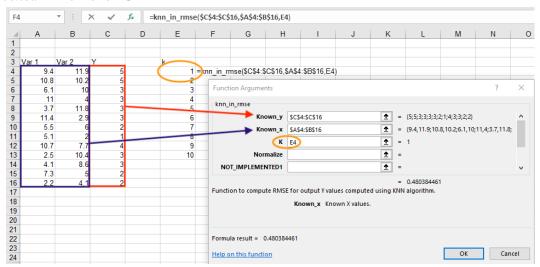
*Note:* this is not an array function and can be evaluated in a single stand-alone cell, in which case it outputs the RMSE for a specified k. However, it is particularly useful when you want to compare RMSEs for different k. We will illustrate how to do this in the example below.

#### To use the function:

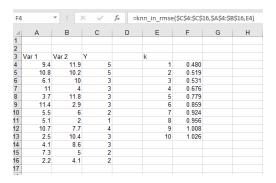
1. Write a list of parameters k for which you want to compute the RMSE, k = 1, 2, ..., 10 in the example below; select the cell next to the first value for k; call the function by typing  $=knn_in_rmse($  in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.

SU	SUM * : X									
4	Α	В	С	D	E	F	G	Н		
1										
2										
3	Var 1	Var 2	Υ		k					
4	9.4	11.9	5		1		nse(			
5	10.8	10.2	5		2					
6	6.1	10	3		3					
7	11	4	3		4					
8	3.7	11.8	3		5					
9	11.4	2.9	3		6					
10	5.5	6	2		7					
11	5.1	2	1		8					
12	10.7	7.7	4		9					
13	2.5	10.4	3		10					
14	4.1	8.6	3							
15	7.3	5	2							
16	2.2	4.1	2							
17										
18										
19										

2. Input the references to the cells that contain the independent and dependent variable data, as in the figure below, then *lock* the cell references with \$ signs. Input the reference of the cell that contains the first value for k, and make sure that this is *not locked*. Then click OK.



3. The function will display the output in the selected cell (F4). Copy the content of the cell down until cell F13, the formula will automatically update the calculation for every k. You can also format the output to display only three decimals.



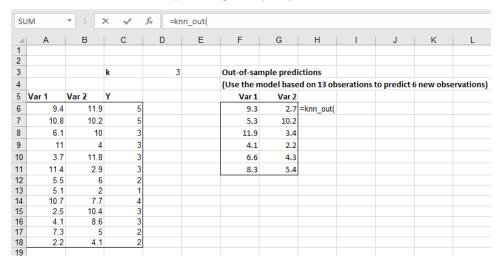
### 1.3.3. knn\_out

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn\_full sheet.

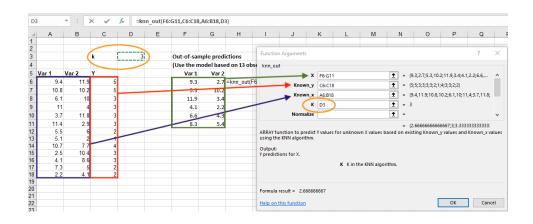
knn\_out applies the-k nearest neighbor algorithm to make predictions on the outcome variable Y of a new set of observations using a known sample.

To use the function:

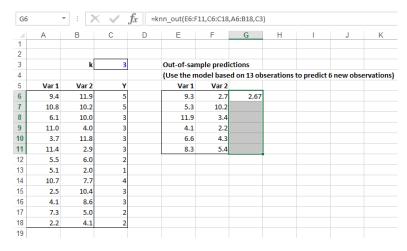
1. Write the parameter k in an empty cell, k=3 in the example below. Select the first cell in which you want the output to be displayed; call the function by typing  $=knn_out($  in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



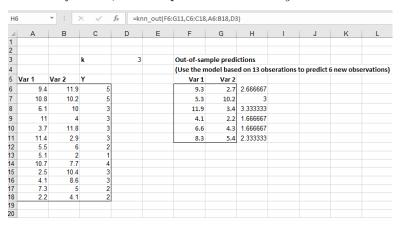
2. The function takes as inputs the new observations X, the old observations and the known outcomes, as well as the parameter k. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click OK.



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of new observations.



4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also format the output to display only two decimals. Remark: for recent versions of Excel, this step is not necessary.



### 1.4. K-Nearest Neighbor Functions (User-based)

Tip: The functions in this section do user-based prediction, which means that they predict a score (or rating) based on the scores of other users. These function do not use any other content-attribute (as movie characteristics). You should use these functions when you want to predict ratings (for example, movie ratings) based only on the ratings of other users.

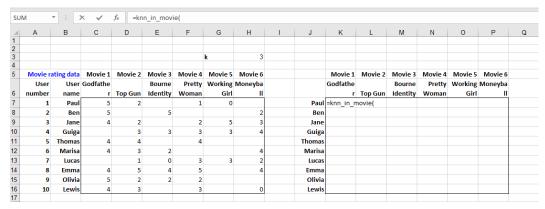
### 1.4.1. knn\_in\_movie

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn\_in\_movie sheet.

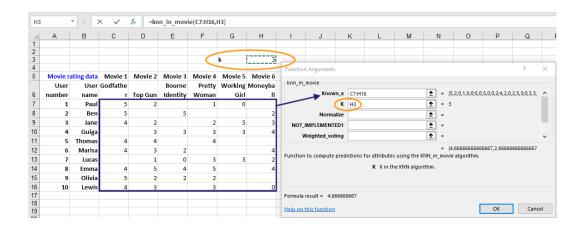
knn\_in\_movie uses the k-nearest neighbor algorithm to make predictions within a specified sample of users' ratings.

To use the function:

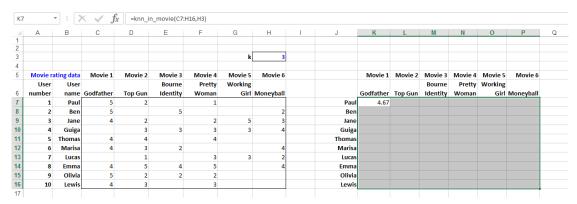
1. Write the parameter k in an empty cell, k=3 in the example below; select the first cell in which you want the output to be displayed; call the function by typing  $=knn_in_movie$  in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



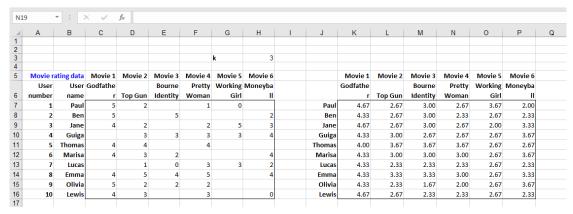
2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click  $\tt OK$ .



3. Remember that this is an array function. Select the area in which you want the output to be displayed: this should have the same number of rows and columns as the area that contains the users' ratings. In the figure below, we selected cells K7:P16.



4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title to the output-column and format the output-cells to display only the first two decimals. Remark: for recent versions of Excel, this step is not necessary.



### 1.4.2. knn\_in\_movie\_rmse

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn\_in\_movie sheet.

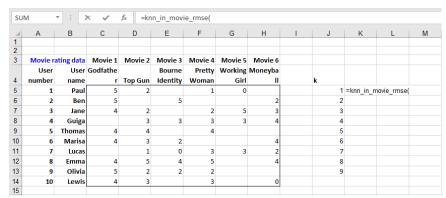
knn\_in\_movie\_rmse is a function that computes the Root Mean Squared Error (RMSE) for k-nearest neighbor predictions (as the ones you can obtain with knn in movie).

The inputs of the function are the users' ratings for a set of movies and the parameter k for which we want to compute the RMSE of predictions.

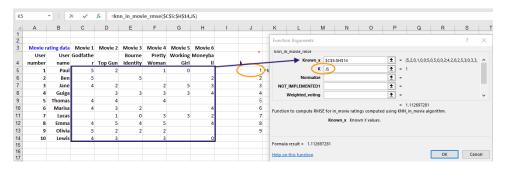
*Note:* this is not an array function and can be evaluated in a single stand-alone cell, in which case it outputs the RMSE for a specified k. However, it is particularly useful when you want to compare RMSEs for different k. We will illustrate how to do this in the example below.

To use the function:

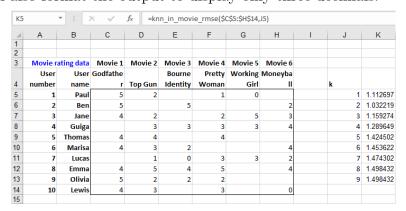
1. Write a list of parameters k for which you want to compute the RMSE, k = 1, 2, ..., 9 in the example below; select the cell next to the first value for k; call the function by typing  $=knn_in_rmse($  in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



2. Input the references to the cells that contain the users' ratings, as in the figure below, then lock the cell references with \$ signs. Input the reference of the cell that contains the first value for k, and make sure that this is  $not\ locked$ . Then click OK.



3. The function will display the output in the selected cell (K5). Copy the content of the cell down until cell K13, the formula will automatically update the calculation for every k. You can also format the output to display only three decimals.



#### 1.5. Other KNN Functions

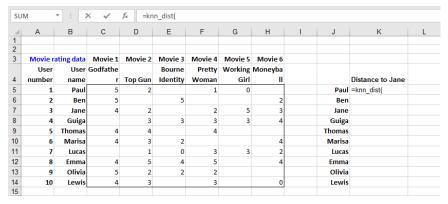
The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the knn\_full sheet.

### 1.5.1. knn\_dist

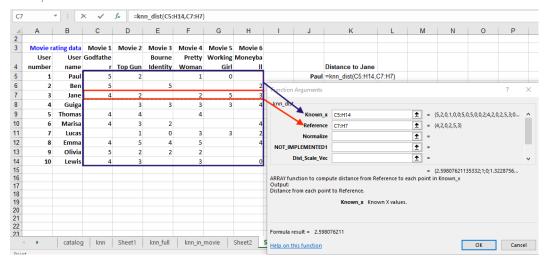
**knn\_dist** is an array function that uses users' ratings to compute the distance of each user from a given user that you specify.

To use the function:

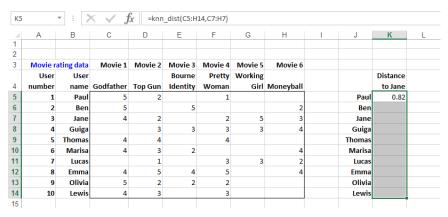
- 0. Decide the baseline user from which you want to compute the distances (we use **Jane** in the example below).
- 1. Select the first cell in which you want the output to be displayed; call the function by typing =knn\_dist( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



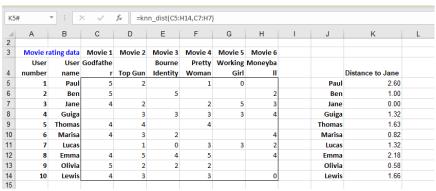
2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click OK.



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of users. In the figure below, we selected cells K5:K14.



4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title to the output-column and format the output-cells to display only the first two decimals. Remark: for recent versions of Excel, this step is not necessary.

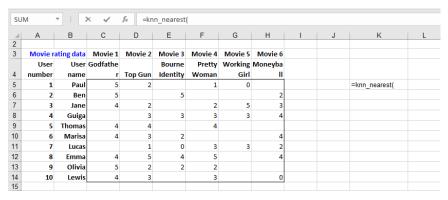


### 1.5.2. knn\_nearest

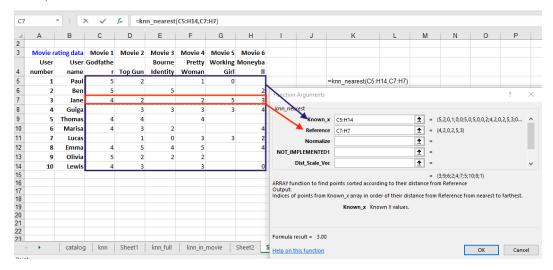
knn\_nearest is an array function that uses users' ratings to rank users in order of proximity (smallest distance) to a given user that you specify. The numbers returned are indices of the rows in the input table in order of distance. (Note, in particular, that they are not "ranks".)

To use the function:

- 0. Decide the baseline user from which you want to compute the distance rankings (we use **Jane** in the example below).
- 1. Select the first cell in which you want the output to be displayed; call the function by typing =knn\_nearest( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



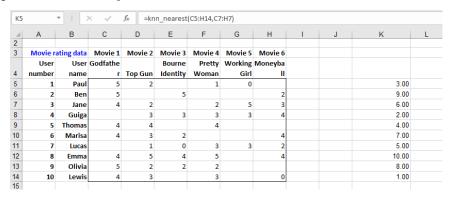
2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click  $\tt OK$ .



3. Remember that this is an array function. Select the column in which you want the output to be displayed: this should be a column of the same length as the number of users. In the figure below, we selected cells K5:K14.

	K5	•	(-	<i>f</i> <sub>x</sub> =knn	_nearest(0	C5:H14,C7:H	17)					
A	Α	В	С	D	Е	F	G	Н	- 1	J	K	L
1												
2												
3	Movie r	ating data	Movie 1	Movie 2	Movie 3	Movie 4	Movie 5	Movie 6				
	User	User	Godfathe		Bourne	Pretty	Working	Moneyba				
4	number	name	r	Top Gun	Identity	Woman	Girl	ll ll				
5	1	Paul	5	2		1					3	
6	2	Ben	5		5			2				
7	3	Jane	4	2		2	5	3				
8	4	Guiga		3	3	3	3	4				
9	5	Thomas	4	4		4						
10	6	Marisa	4	3	2			4				
11	7	Lucas		1		3	3	2				
12	8	Emma	4	5	4	5		4				
13	9	Olivia	5	2	2	2						
14	10	Lewis	4	3		3						
15											,	

4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the predictions. You can also add a title to the output-column and format the output-cells to display the ranking without any decimals. Remark: for recent versions of Excel, this step is not necessary.



To understand the output, consider the first number returned, 3. This means that the closest person to Jane is the 3rd row (i.e., Jane herself). The second number is 9. This means the second closest person is the 9th row (i.e., Olivia).

### 1.6. BA\_RMSE

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the ROC\_no\_cost sheet.

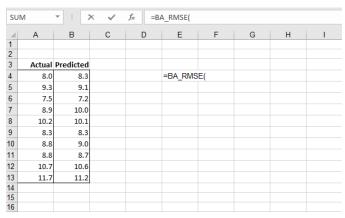
Suppose that you have access to 10 experiments for which you observed **actual outcome** and the **predicted outcome** generated by some predictive model.

Actual	Predicted
8.0	8.3
9.3	9.1
7.5	7.2
8.9	10.0
10.2	10.1
8.3	8.3
8.8	9.0
8.8	8.7
10.7	10.6
11.7	11.2

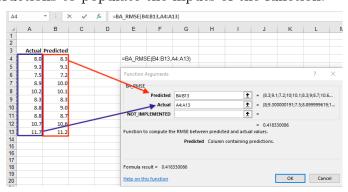
We illustrate in this section a function that computes the Root Mean Square Error.

To use the function:

1. Select the cell in which you want the output to be displayed; call the function by typing =BA\_RMSE( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.



2. Follow the instructions to populate the inputs of the function.



3. Click OK to display the result, in the example we have RMSE=0.42.

### 1.7. Classification Functions

In this section we will illustrate a set of functions that you can use to solve classification problems. All the examples will be built upon the following dataset. Suppose that you have access to 17 experiments (e.g. clinical tests, spam/non-spam email classification, etc.) for which you observe the **actual outcome** of the experiment (1 if successful and 0 if not successful) and the **probability of success** generated by some predictive model.

	Predicted
Actual	probability
outcome	(score)
0	0.04
0	0.11
0	0.62
0	0.40
1	0.62
1	0.76
1	0.38
1	0.61
0	0.22
1	0.36
0	0.29
1	0.20
0	0.18
1	0.11
1	0.30
1	0.31
0	0.18

#### 1.7.1. confusionMatrix

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the ROC\_no\_cost sheet.

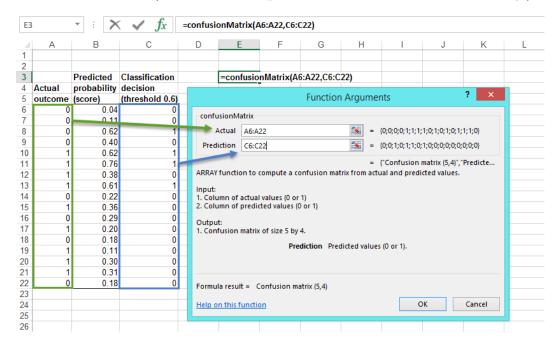
Before illustrating the function, we build a classifier on the above dataset with a classification threshold of 0.6: we predict as successful (1) the experiments that have a probability of success of at least 0.6 and not successful (0) the others.

	Predicted	Classification
Actual	probability	decision
outcome	(score)	(threshold 0.6)
0	0.04	0
0	0.11	0
0	0.62	1
0	0.40	0
1	0.62	1
1	0.76	1
1	0.38	0
1	0.61	1
0	0.22	0
1	0.36	0
0	0.29	0
1	0.20	0
0	0.18	0
1	0.11	0 0 1 0 1 1 0 0 0 0 0 0
1	0.30	0
1	0.31	0
0	0.18	0

We will use **confusionMatrix** to compute the Confusion Matrix associated to the above classifier.

To use the function:

- 1. Select the first cell in which you want the output to be displayed; call the function by typing =confusionMatrix( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.
- 2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click OK. (The actual and predicted values must both be binary.)



3. Remember that this is an array function. Select the set of cells in which you want the output to be displayed. In the figure below, we selected cells E3:H7. Remark: for recent versions of Excel, this step is not necessary.

E3	}	- : ×	$\checkmark f_x$	=confusi	onMatrix(A	A6:A22,C6:C	22)		
4	Α	В	С	D	E	F	G	Н	1
1									
2									
3		Predicted	Classification		Confusion	matrix (5,	4)		
4	Actual	probability							
5	outcome		(threshold 0.6)						
6	0	0.04	0						
7	0	0.11	0						
8	0	0.62	1						
9	0	0.40	0						
10	1	0.62	1						
11	1	0.76	1						
12	1	0.38	0						
13	1	0.61	1						
14	0	0.22	0						
15	1	0.36	0						
16	0	0.29	0						
17	1	0.20	0						
18	0	0.18	0						
19	1	0.11	0						
20	1	0.30	0						
21	1	0.31	0						
22	0	0.18	0						
23									

4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the output. You can also format the output-cells to display the labels of the matrix in boldface.

Confusion matrix (5,4)	Predicted		
Actual	1	0	Total
1	3	6	9
0	1	7	8
Total	4	13	17

#### 1.7.2. ROC

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the ROC no cost sheet.

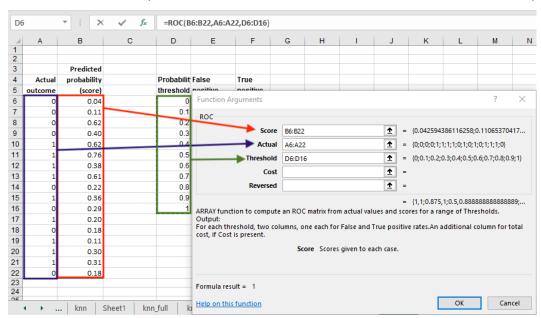
An important measure for evaluating the performance of a given classification model is the error rate. For example, consider the confusion matrix calculated in the previous section: the classifier built using a threshold of 0.6 has a false positive rate of 1/8 = 12.5% and a true positive rate of 3/9 = 33.3%. The ROC curve is simply a plot of the true positive versus the false positive rate for different thresholds. Note that, in principle, one can use any score for classification purposes. In the example, the score used was the predicted probability, but any other score can be used as well. By varying the classification threshold, different (FPR, TPR) pairs result, and the ROC curve captures all possible achievable pairs using that particular score/classifier. The ROC curve is a useful tool when you are trying to decide which classification threshold you should select.

To use the function:

0. Insert in a column the list of threshold values you want to test.

Probability	False	True	
threshold	positive	positive	
0.0			
0.1			
0.2			
0.3			
0.4			
0.5			
0.6			
0.7			
0.8			
0.9			
1.0			

- 1. Select the cell immediately to the right of the first threshold value, and call the function by typing =ROC( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.
- 2. Follow the instructions to populate the input fields, as demonstrated in the figure below, then click OK. (For the ROC curve with "Cost" see section 1.7.4 below.)



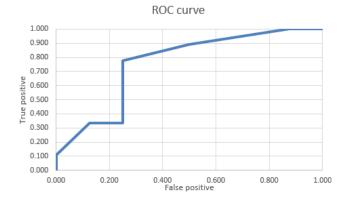
3. Remember that this is an array function. Select the set of cells in which you want the output to be displayed.

False True	bability
sitive positiv	nreshold_p
1.000	0.0
	0.1
	0.2
	0.3
	0.4
	0.5
	0.6
	0.7
	0.8
	0.9
	1.0

4. Position the cursor in the formula bar, and press Ctrl+Shift+Enter to display the output. You can also format the output-cells to display only three decimals. Remark: for recent versions of Excel, this step is not necessary.

Probability	False	True	
threshold	positive	positive	
0.0	1.000	1.000	
0.1	0.875	1.000	
0.2	0.500	0.889	
0.3	0.250	0.778	
0.4	0.250	0.333	
0.5	0.125	0.333	
0.6	0.125	0.333	
0.7	0.000	0.111	
0.8	0.000	0.000	
0.9	0.000	0.000	
1.0	0.000	0.000	

5. You can easily plot the false positive and true positive rates to display the ROC curve. To generate the graph below: select the set of cells that display the output of the ROC function; then select INSERT - Charts - Scatter - Scatter with straight lines.



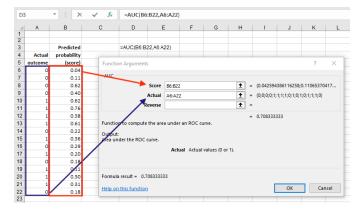
### 1.7.3. AUC

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the ROC\_no\_cost sheet.

This function computes the area under the ROC curve.

To use the function:

- 1. Select the cell in which you want the output to be displayed; call the function by typing =AUC( in the formula bar and then pressing the  $f_x$  symbol next to the formula bar.
- 2. Follow the instructions to populate the inputs of the function.



3. Click OK to display the result, in the example we have AUC=0.71.

### 1.7.4. ROC (with cost information)

The example illustrated below is available on the add-in webpage by downloading the Classification, KNN, Misc file and going to the ROC\_with\_cost sheet.

This is a variation on the basic **ROC** function, when you have a cost associated to each type of classification error. The costs must be expressed in terms of a cost matrix.

1	Α	В	C D	E	F	G	Н	1	J	K
1										
2										
3		Predicted								
4	Actual	probability	Probability	False	True	Total		Cost matrix	Predicted	
5	outcome	(score)	threshold	positive	positive	Cost		Actual	1	0
6	0	0.04	0.0					1	6	10
7	0	0.11	0.1					0	3	0
8	0	0.62	0.2							
9	0	0.40	0.3							
10	1	0.62	0.4							
11	1	0.76	0.5							
12	1	0.38	0.6							
13	1	0.61	0.7							
14	0	0.22	0.8							
15	1	0.36	0.9							
16	0	0.29	1.0							
17	1	0.20								
18	0	0.18								
19	1	0.11								
20	1	0.30								
21	1	0.31								
22	0	0.18								

To use the function follow the same steps as the basic **ROC** function, with the following variations:

- At Step 2. insert also the cost matrix information: type J6:K7 in the Cost input field.
- At Step 3. select three columns, as the function now outputs also the total cost. Remark: for recent versions of Excel, this step is not necessary.

Probability	False	True	Total	
threshold	positive	positive	Cost	
0.0	1.000			
0.1				
0.2				
0.3				
0.4				
0.5				
0.6				
0.7				
0.8				
0.9				
1.0				

#### 1.8. Monte Carlo Simulation

In this section we will illustrate how to run a Monte Carlo Simulation in a spreadsheet.

The example illustrated below is available on the add-in webpage by downloading the Monte Carlo Simulation file and going to the MCSim sheet.

**Example: simple revenue simulation.** Suppose that you have 100 customers coming into your shop on each day and that each customer purchases something with probability 40%. The accrued revenue per purchase is normally distributed with a mean of \$20 and a

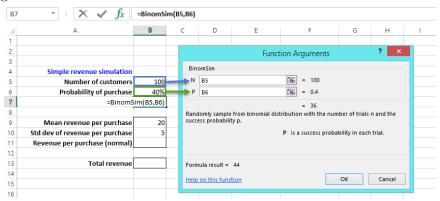
standard deviation of \$5. Simulate the **number of purchases**, the **revenue per purchase**, and the **total revenues**. Run the simulation for 500 trials.

To set up the simulation:

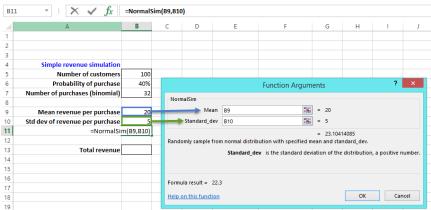
S0. Populate the spreadsheet with the given data.

	A	В	С	D	E	F
1						
2						
3						
4	Simple revenue simulation					
5	Number of customers	100				
6	Probability of purchase	40%	Simula	ation trials	500	
7	Number of purchases (binomial)					
8						
9	Mean revenue per purchase	20				
10	Std dev of revenue per purchase	5				
11	Revenue per purchase (normal)					
12						
13	Total revenue					
14						

- S1. Insert the formulas for the quantities you want to simulate.
  - (S1.i) Number of purchases: this is a random sample from a Binomial distribution with 100 trials and probability equal to 0.4. You can use the add-in function BinomSim to generate this number.



(S1.ii) Revenue per purchase: this is a random sample from a Normal distribution with mean 20 and standard deviation 5. You can use the add-in function NormalSim to generate this number.



- (S1.ii) Total Revenues: this is simply the product of number of purchases times revenue per purchase. Select cell B13 and insert the formula =B7\*B11.
- S2. Create the formula row, which will be your input for the simulation. Simply copy and paste the formulas from (1.i), (1.ii) and (1.iii) to an empty row. We did this in the figure below, in particular we inserted =B7 in cell E5, =B11 in cell F5, and =B13 in cell G5.

<b>E</b> 5	· : × / fx	=B7						
4	А	В	С	D	E	F	G	Н
1								
2								
3								
4	Simple revenue simulation				Num purchase	Rev per purchase	Total rev	
5	Number of customers	100		Formula	32	21.8	698.9	
6	Probability of purchase	40%	Simul	ation trials	500			
7	Number of purchases (binomial)	32						
8								
9	Mean revenue per purchase	20						
10	Std dev of revenue per purchase	5						
11	Revenue per purchase (normal)	21.8						
12								
13	Total revenue	698.9						
14								

S3. You can also add an (optional) row of labels which indicates the variable for which you would like an histogram to be automatically generated, along with the simulation results. In our example we insert a row of labels with 0s for the first two variables and 1 for **total revenues**. As a result an histogram for this last variable will be generated, along with the simulation results.

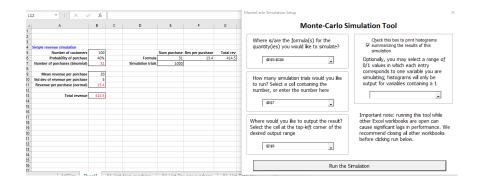
	Num purchase	Rev per purchase	Total rev
Formula	32	21.8	698.9
Simulation trials	500		

To run the simulation:

RO. Go to the CBS BA ADD-IN tab and then select the Monte Carlo Simulation to pop up the MonteCarlo Simulation Dialog. (Alternatively, the dialog can be popped up by clicking Ctrl+Shift+M.)



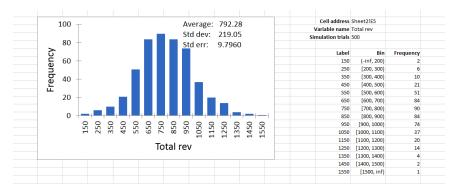
R1. Populate the inputs of the function in the Dialog Box and then click OK. Also, by selecting the Print Histogram check box you can automatically generate histograms of the selected variables. Note that the simulation can track any number of variables in a single row, not just the three used in this example.



You can format the output of the simulation to display nicely as in the figure below.

Name to a second and the second and						
Simple revenue simulation						_
Number of customers	100			Rev per purchase	Total rev	
Probability of purchase	40%	Formula		24.4	950.4	
Number of purchases (binomial)	39	Simulation trials	1000			
Mean revenue per purchase	20	CPU seconds	1.349609375			
Std dev of revenue per purchase	5		Num purchase	Rev per purchase	Total rev	
Revenue per purchase (normal)	24.4	Average	40.036	19.961	798.388	
		Standard deviation	4.881	5.088	224.135	
Total revenue	950.4	Standard error	0.154	0.161	7.088	
		Minimum	25	3.769	135.699	
		Maximum	57	35.190	1609.583	
		Percentiles				
		0.01	28	8.238	291.362	
		0.05	32	11.658	458.831	
		0.1	34	13.363	525.463	
		0.5	40	19.868	791.722	
		0.9	46	26.385	1084.082	
		0.95	48	28.281	1191.772	
		0.99	52	32.369	1391.070	

In separate sheets the macro outputs the histograms. As an example, we present the histogram of **total revenues**.



You can use CBS BA Add-In | Clear histogram sheets to clear previously created histogram sheets.