Supplementary Material cblearn: Comparison-based Machine Learning in Python

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22 September 2023

Empirical evaluation

We generated embeddings of comparison-based datasets to measure runtime and triplet error as a small empirical evaluation of our ordinal embedding implementations. We compared various CPU and GPU implementations in cblearn with third-party implementations in R (loe Terada and Luxburg 2014), and MATLAB (Maaten and Weinberger 2012). In contrast to synthetic benchmarks (e.g., Vankadara et al. 2021), we used the real-world datasets that can be accessed through cblearn, converted to triplets. The embeddings were arbitrarily chosen to be 2D. Every algorithm runs once per dataset on a compute node (8 cores of a Intel®Xeon ®Gold 6240; 96GB RAM; NVIDIA RTX 2080ti) with a run-time limit of 24 hours. Some runs did fail by exceeding those constraints: our FORTE implementation failed by an out of memory error on the imagenet-v2 dataset. The MATLAB implementation of tSTE timed out on things and imagenet-v2 datasets. The R implementation of SOE on the imagenet-v2 dataset by an "unsupported long vector" error, caused by the large size of the requested embedding.

The benchmarking scripts and results are publicly available in a separate repository¹.

Is there a "best" estimator?

Comparing all ordinal embedding estimators in cblearn, SOE, CKL, GNMDS, and tSTE were performing about equally well in both runtime and accuracy (Figure 1). The GPU implementations are slower on the tested datasets and for SOE and GNMDS noticeably less accurate.

¹https://github.com/cblearn/cblearn-benchmark

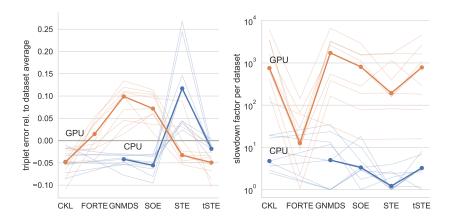


Figure 1: The triplet error and runtime per estimator and dataset, relative to the mean error or the fastest run. Thin lines show runs on the different datasets; the thick lines indicate the respective median. With the exception of *STE*, all CPU algorithms are able to embed the triplets similarly well. There are just minor differences in the runtime of the CPU implementations. The GPU implementations are usually significantly slower on the data sets used.

When should GPU implementations be preferred?

In terms of accuracy and runtime, our GPU (or pytorch) implementations could not outperform the CPU (or scipy) pendants on the tested datasets. However, Figure 1 shows the GPU runtime grows slower with the number of triplets, such that they potentially outperform CPU implementations with large datasets of 10^7 triplets and more. In some cases, the GPU implementations show the overall best accuracy. An additional advantage of GPU implementations is that they require no explicit gradient definition, which simplifies the implementation of new algorithms.

There are various explanations for the speed disadvantage of our pytorch implementations. On the one hand, it may be due to the overhead of converting between numpy and pytorch and calculating the gradient (AutoGrad). On the other hand, it can also be due to the optimizer or the selected hyperparameters. To get a first impression of these factors, we have built minimal examples of the CKL algorithm (Tamuz et al. 2011) and estimated 2D embeddings of the Vogue Cover dataset (Heikinheimo and Ukkonen 2013). Figure 3 shows the runtimes and triplet accuracies on a standard laptop. The small markers show runs with different initialization and the bold markers the respective means. The CKL implementation of cblearn is approximately three times slower than the minimal version, probably due to data validation and conversion overheads. If the gradient is not provided directly but calculated automatically with PyTorch's AutoGrad functions, the minimal example runs ~11 times slower. The most

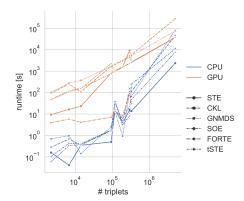


Figure 2: The runtime increases almost linearly with the number of triplets. However, GPU implementations have a flatter slope and thus can compensate for the initial time overhead on large datasets.

severe impact has changing the optimization algorithm to stochastic optimization (Adam, lr=10). However, it can be assumed in accordance with the results in previous sections, that this overhead is compensated with increasing dataset size.

An additional challenge of stochastic optimizers like Adam (Kingma and Ba 2014) is their sensitivity to hyperparameter choices. This sensitivity is demonstrated in Figure , where the learning rate of Adam is varied for the toy example. Especially runtime largely depends on the learning rate, while the error is less sensitive to it. Likewise, the performance of pytorch ordinal embedding implementations could be improved by using more sophisticated tuning of optimizer parameters.

[The runtime and error for different learning rates of the Adam optimizer in a minimal example with CKL estimating a 2D embedding of 60 objects.] images/adam_lr_triplets.pdf){width=50%}

How does cblearn compare to other implementations?

In a small comparison, our implementations run multiple times faster with approximately the same accuracy as reference implementations (Figure 4). We compared our CPU implementations of SOE the corresponding reference implementations in R , loe (Terada and Luxburg 2014), and our implementation of CKL, GNMDS, STE, tSTE with the MATLAB of Maaten and Weinberger (2012). This comparison is not exhaustive, but it shows that our implementations are competitive with the reference implementations in terms of accuracy and runtime. Of course, we cannot separate the factors of algorithm implementation and runtime environment.

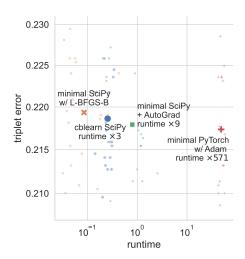


Figure 3: The runtime and error for different optimization methods in minimal CKL implementations. cblearn's CKL implementation is shown for reference.

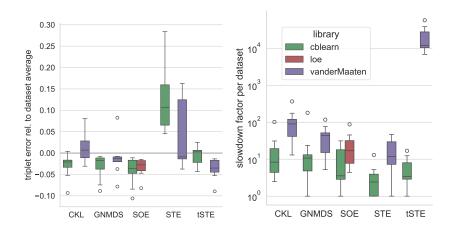


Figure 4: The triplet error and runtime per estimator and dataset, relative to the mean error and the fastest run. Thin lines show runs on the different datasets; the thick lines indicate the respective median. The triplet error is broadly similar for all implementations, but *cblearn* is many times faster for all algorithms.

Code example

from cblearn import datasets, preprocessing, embedding
from sklearn.model_selection import cross_val_score
import seaborn as sns; sns.set_theme("poster", "whitegrid")

References

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