## Review

# Isothermal titration calorimetry and differential scanning calorimetry as complementary tools to investigate the energetics of biomolecular recognition

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The principles of isothermal titration calorimetry (ITC) and differential scanning calorimetry (DSC) are reviewed together with the basic thermodynamic formalism on which the two techniques are based. Although ITC is particularly suitable to follow the energetics of an association reaction between biomolecules, the combination of ITC and DSC provides a more comprehensive description of the thermodynamics of an associating system. The reason is that the parameters  $\Delta G$ ,  $\Delta H$ ,  $\Delta S$ , and  $\Delta C_p$  obtained from ITC are global properties of the system under study. They may be composed to varying degrees of contributions from the binding reaction proper, from conformational changes of the component molecules during association, and from changes in molecule/solvent interactions and in the state of protonation. Copyright © 1999 John Wiley & Sons, Ltd.

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#### Introduction

Specific binding is fundamental to the molecular organization of living matter. Virtually all biological phenomena depend in one way or another on molecular recognition, which either is intermolecular as in ligand binding to a macromolecule and in the formation of macromolecular complexes, or intramolecular as in protein folding. Here we deal with intermolecular recognition, that is, with binding reactions. The specificity and precision of binding reactions has fascinated biologists and chemists from the very beginning of modern biochemistry, and one of the most rapidly advancing fields today is the study of molecular recognition between macromolecules. The quantitative description of the forces that govern the formation of biomolecular complexes is part of this endeavor. It has great practical significance to the knowledge-based development of new drugs, vaccines and other medicinal compounds.

The number of high resolution crystal structures of biomolecular complexes is growing fast and there is a large data base describing the complementarity of interacting surfaces and the precise orientation of interacting groups. From the many detailed, yet static, pictures of biomolecular complexes we have learned *how* molecules interact, but we less well know *why* they do so. This means we have to find

**Abbreviations used:** DSC, differential scanning calorimetry; 11C, isotherma titration calorimetry.

ways to rationalize structure in terms of energetics, a task that still is enormously difficult inspite of some very promising theoretical developments and of the steady accumulation of experimental results. Theoretical concepts have developed in the tradition of physical-organic chemistry. It is difficult to adapt these concepts in a straightforward way to complex biomacromolecules. Proteins and nucleic acids are so large that in solution they may be regarded as individual macroscopic systems surrounded by solvent (Privalov and Potekhin, 1986). They behave cooperatively and often undergo structural rearrangements during binding reactions. The changes range from the subtle adjustments of dihedral angles to the prominent rearrangement and even refolding of entire molecular domains (Padlan, 1996). For example, in a DNA binding protein the domain that binds to the DNA target site can be unstructured in the free protein and becomes folded only when it is bound to DNA (Patikoglou and Burley, 1997). The energetic consequence of such binding-induced refolding is far from being understood, but the energetic cost is thought to be large. From this perspective, binding specificity has to be redefined. It is no longer a simple function of spatial complementarity and of accumulation of favorable interactions between molecules that can be treated as rigid bodies. Binding between large and flexible biomolecules has a complicated energy profile involving different energetic expenditures in going from the free components to the final complex. The free energy of complex formation turns out to be a very small number resulting from a delicate balance between large favorable and large unfavorable contributions. Moreover, binding takes place only if the total free

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energy change decreases, regardless of the actual amount of favorable free energy change accumulated by direct molecular contact between the associating biomolecules. This is to say, solvent effects are as important to the energy balance as are direct noncovalent interactions (Collins, 1997; Jelesarov *et al.*, 1998).

# **Basic Thermodynamic Relationship Describing Binding Phenomena**

The Gibbs free energy change,  $\Delta G$ , of an association reaction is temperature dependent and is described by

$$\begin{split} \Delta G(T) &= \Delta H(T_{\rm R}) + \int_{T_{\rm R}}^T \Delta C_{\rm p} \mathrm{d}T - T \Delta S(T_{\rm R}) \\ &- T \int_{T_{\rm P}}^T \Delta C_{\rm p} \mathrm{d}\ln T \end{split} \tag{1}$$

 $\Delta H$  and  $\Delta S$  are the change in enthalpy and entropy, respectively,  $\Delta C_{\rm p}$  is the heat capacity change, and  $T_{\rm R}$  is an appropriate reference temperature. If  $\Delta C_{\rm p}$  is temperature-independent in the temperature interval of interest, Eq. (1) simplifies to

$$\Delta G(T) = \Delta H(T_{\rm R}) - T \Delta S(T_{\rm R}) + \Delta C_{\rm p} [T - T_{\rm R} - T \ln(T/T_{\rm R})]$$
(2)

Equations (1) and (2) show that the free energy of association has an enthalpy and an entropy component. The changes of enthalpy and entropy depend on temperature according to

$$\Delta C_{\rm p} = \frac{\mathrm{d}(\Delta H)}{\mathrm{d}T} = T \frac{\mathrm{d}(\Delta S)}{\mathrm{d}T} \tag{3}$$

To characterize the thermodynamics of a binding reaction means to determine  $\Delta G$ ,  $\Delta H$  and  $\Delta S$  at a given reference temperature and to obtain  $\Delta C_{\rm p}$  to predict the change of the above three parameters with temperature.

#### Non-calorimetric determination of binding energetics

 $\Delta G$  is accessible through many types of binding experiments because  $\Delta G$  is related to the association constant  $K_A$  by  $\Delta G$  = -RT ln  $K_A$  where R is the gas constant (8.314 J K<sup>-1</sup>mol<sup>-1</sup>) and T is the absolute temperature in degrees Kelvin. In the simplest case a molecule L reacts with another molecule M to the complex ML. The association constant is  $K_A = [ML]/[M][L]$  where the brackets indicate concentration expressed in units of mol  $I^{-1}$  and  $K_A$  has units of I mol<sup>-1</sup>. To take the logarithm,  $K_A$  must be a dimensionless ratio. This is achieved by normalizing the molar concentrations to the standard state concentration of I mol  $I^{-1}$ . Alternatively,  $K_A$ 

can be expressed as (mol fraction)<sup>-1</sup>, where 1 mol 1<sup>-1</sup> equals  $1.8 \times 10^{-2}$  mol fraction (corresponding to 1/55.56 mol H<sub>2</sub>O per 1). The choice of the standard state is a matter of convention yet is important when comparing values of  $\Delta G$  and  $\Delta S$ .

There are many ways to measure  $K_A$ . Let us begin with the simple equilibrium between L, M and ML:

$$L+M \stackrel{K_{A}}{\longrightarrow} ML$$

Techniques like equilibrium dialysis, ultracentrifugation, or radio-ligand binding assay directly yield values for [ML], [M], or [L] to calculate  $K_A$ . More indirect and mostly spectroscopic methods yield an observable p the change of which is proportional to the degree of saturation, Y, according to:

$$Y = \frac{\Delta p_i}{\Delta p_{\text{max}}} = \frac{[ML]}{[M] + [ML]} = \frac{K_A[L]}{1 + K_A[L]}$$
(4)

 $\Delta p_i$  is a signal change (e.g. a change of fluorescence accompanying the formation of the complex, ML), and  $\Delta p_{\rm max}$  is the maximum signal change at full saturation (Y=1). From Y measured at different temperatures,  $K_A(T)$  and  $\Delta G(T)$  are obtained.  $\Delta H(T)$  and  $\Delta S(T)$  can be derived using the integrated form of the van't Hoff equation:

$$\int_{T_1}^{T_2} \mathrm{d} \ln K_{\rm A} = \int_{T_1}^{T_2} \frac{\Delta H}{RT^2} \mathrm{d}T \tag{5a}$$

and

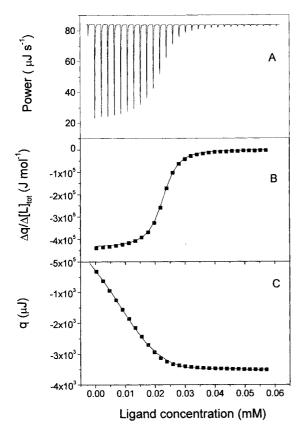
$$\int_{T_1}^{T_2} \Delta G = -\int_{T_1}^{T_2} \Delta S dT \tag{5b}$$

Further, taking the second derivative of  $\Delta G(T)$  with respect to temperature, one obtains  $\Delta C_{\rm p}$ . The non-calorimetric approach to the thermodynamics of an association reaction, commonly called a van't Hoff analysis, has severe drawbacks. First, for technical reasons, experiments can be performed only in a limited temperature range, and experimental errors propagate into large errors of  $\Delta H$ ,  $\Delta S$ , and of  $\Delta C_{\rm p}$  in particular. Second,  $K_{\rm A}$  very often appears temperature-independent in the experimentally accessible T-range because of enthalpy/entropy compensation between large and strongly temperature-dependent  $\Delta H$  and  $\Delta S$ . Therefore, the van't Hoff analysis of a binding reaction is often flawed.

## **Isothermal Titration Calorimetry**

ITC and DSC are the only methods for the direct determination of  $\Delta H$ . The principle of ITC is now reviewed first. It is the most direct method to measure the heat change on formation of a complex at constant temperature. Since a titration experiment is performed in which L is titrated into a solution of M (or M into a solution of L),  $K_A$  and the stoichiometry, n, of the complex are also obtained by ITC. Moreover, ITC experiments performed at different temperatures yield  $\Delta C_p$  defined by Eq. (3).

 $<sup>^1</sup>$ In this article the components of a complex are designated L and M, irrespective of their size and chemical nature. Thus, L and M can be proteins, nucleic acids, low molecular weight metabolites, salt ions, and so on. L often is named the ligand and M the receptor. However, this assignment is arbitrary.



**Figure 1.** ITC titration data describing the formation of a 16 bp DNA duplex by mixing the complementary strands at 30 °C. *Panel A* shows the differential power signal recorded in the experiment. After integration with respect to time and normalization per mol of added ligand (which in this case is single-stranded DNA),  $\Delta H_{\rm app}$ ,  $K_{\rm A}$  and n can be calculated from Eq. (6) by nonlinear least squares analysis, as detailed in the text. The integrated data can be plotted in two ways: as a sigmoidal plot (*panel B*) or as a hyperbolic saturation curve (*panel C*). The  $\Delta H_{\rm app}$  obtained from this analysis is a global property of the system corrected for nonspecific effects. The solid lines in panels B and C correspond to  $\Delta H_{\rm app} = 436$  kJ mol $^{-1}$ ,  $K_{\rm A} = 3.1 \times 10^6 {\rm M}^{-1}$ , and n = 1.

#### The ITC experiment

The basic principle is simple.<sup>2</sup> The experiment is performed at a constant temperature by titrating one binding partner (called the 'titrant', e.g. L) into a solution containing the other binding partner (called the 'titrand', e.g. M) in the sample cell of the calorimeter. After each addition of a small aliquot of L, the heat released or absorbed in the sample cell is measured with respect to a reference cell filled with buffer. The heat change is expressed as the electrical power (J s<sup>-1</sup>) required to maintain a constant small temperature difference between the sample cell and the reference cell, which are both placed in an adiabatic jacket. Addition of L is automated and occurs from a precision syringe driven by a

computer-controlled stepper motor. The contents of the sample cell are stirred to effect rapid mixing of the reactants. In commercially available instruments volumes of sample cells are in the range 0.2–1.4 ml. The amount of titrand required per experiment depends on the magnitude of the heat change; 10–100 nmol of protein are typical.

Figure 1A shows the raw data of an ITC experiment. Each peak corresponds to the heat released on addition of an aliquot of ligand to the receptor. Integration of the differential power signal with respect to time yields the apparent heat change,  $\Delta q_{i,\mathrm{app}}$ , between additions i-1 and i:

$$\Delta q_{i,app} = q_i - q_{i-1}$$

 $\Delta q_{i,\mathrm{app}}$  corresponds to the area of the ith peak in Fig. 1A. If  $K_{\mathrm{A}}$  is large and the molar ratio of L to M at the beginning of the titration is low, then virtually all the ligand is bound to the receptor and the peak areas are similar. As the fractional saturation increases,  $\Delta q_{i,\mathrm{app}}$  gradually decreases. Eventually all receptor sites are saturated. Small heat changes registered after full saturation are caused by the heat of ligand dilution,  $q_{i,\mathrm{dil}}$ , and by other nonspecific effects,  $q_{i,\mathrm{ns}}$ .  $\Delta q_{i,\mathrm{app}}$  is proportional to the volume of the calorimetric cell,  $V_{\mathrm{cell}}$ , to the change in concentration of the bound ligand,  $\Delta [L_i]_{\mathrm{bound}} = [L_i]_{\mathrm{bound}}$ ,  $-[L_{i-1}]_{\mathrm{bound}}$ , and to the apparent molar enthalpy of association,  $\Delta H_{\mathrm{app}}$ . We write:

$$\Delta q_{i,\text{app}} = \Delta q_i + \Delta q_{i,\text{dil}} + \Delta q_{i,\text{ns}}$$

$$= \Delta [L_i]_{\text{bound}} \times V_{\text{cell}} \times \Delta H_{\text{app}}$$
(6a)

 $\Delta q_{i,\mathrm{dil}} + \Delta q_{i,\mathrm{ns}}$  is obtained from a blank titration of ligand into buffer.  $V_{\mathrm{cell}}$  is known, and  $\Delta H_{\mathrm{app}}$  is constant at fixed pressure, temperature and solvent conditions.  $\Delta H_{\mathrm{app}}$  and  $K_{\mathrm{A}}$  are calculated from:

$$\Delta q_i = \Delta q_{i,\mathrm{app}} - \Delta q_{i,\mathrm{dil}} - \Delta q_{i,\mathrm{ns}} = n[M]_{\mathrm{tot}} V_{\mathrm{cell}} \Delta H_{\mathrm{app}} \times \mathbb{R}$$
(6b)

 $[M]_{\text{tot}}$  is the total concentration of M in the sample cell of the calorimeter.  $\Delta q_i$  is the effective heat change caused by the formation of complex ML at the ith step of the titration, and  $\mathbb{R}$  is the root of the quadratic equation:

$$Y_i^2 - Y_i \times \left(1 + \frac{1}{nK_A[M]_{tot}} + \frac{[L_i]_{tot}}{n[M]_{tot}}\right) + n[L_i]_{tot}[M]_{tot} = 0$$
(7)

 $Y_i$  is the degree of saturation defined by  $Y_i = \Delta[L_i]_{\text{bound}}/[M]_{\text{tot}}$ .  $[L_i]_{\text{tot}}$  is the total concentration of L added until injection i, and n is the number of identical and independent binding sites for the ligand L on the receptor M. A nonlinear regression procedure based on Eq (6b) yields n,  $K_A$  and  $\Delta H_{\text{app}}$  from a single titration experiment.

The experimental data can be plotted in two ways. In the differential mode the total heat accumulated up to injection i is normalized to the total ligand concentration at step i and is plotted against the total ligand concentration at step i (or against the ratio of the total ligand concentration at step i to the total receptor concentration,  $[L_i]_{tot}/[M]_{tot}$ ). This yields the familiar sigmoidal titration curve shown in Fig. 1B from which the total calorimetric heat change per mol of complex,  $\Delta H_{app}$ , can be calculated. In the integral mode, the total cumulative heat is plotted against the total ligand concentration to yield a hyperbolic saturation curve (Fig.

<sup>&</sup>lt;sup>2</sup>Technical details on the construction of modern mixing calorimeters, their performance and sensitivity, and on the theory of data analysis have been described elsewhere (McKinnon *et al.*, 1984; Wiseman *et al.*, 1989; Freire *et al.*, 1990; Breslauer *et al.*, 1992).

1C). The same parameters are obtained from either plot. Comparative statistical analysis of the two plots can give information about the accumulation of systematic errors (Bundle and Sigurskjold, 1994). The number of binding sites, n, and  $\Delta H_{\rm app}$  are strongly correlated, and the successful deconvolution of the binding isotherm often depends on additional independent information about the number of binding sites of M.

The case discussed applies only to the binding of L to a receptor M with n identical and independent binding sites. In the case of a receptor with multiple binding sites of different affinity, statistical thermodynamic treatment of the data is required. The partition function Q gives a general description of a binding reaction (Wyman and Gill, 1990). Q relates the sum of concentrations of all species to the concentration of an arbitrarily chosen reference species, conveniently the unligated form of a receptor:

$$Q = \frac{[M] + \sum_{j=1}^{n} [ML_j]}{[M]} = 1 + \frac{\sum_{j=1}^{n} [ML_j]}{[M]} = 1 + \sum_{j=1}^{n} \beta_j \cdot [L]^j$$
(8)

In this equation, [L] and  $[ML_j]$  are the concentrations of free ligand and ligated receptor, respectively, n is the number of binding sites on the receptor, and  $\beta_j$  is the overall binding constant relative to the unligated receptor. It can be written in terms of the overall step-wise (macroscopic) binding constants, K, as

$$\beta_j = \prod_{i=1}^n K_j$$

or in terms of the intrinsic (microscopic) site binding constants,  $\kappa$ , as

$$\beta_j = \frac{n!}{j!(n-j)!} \prod_{i=1}^n \kappa_j$$

Different binding models can be discriminated depending on the definition of  $\beta_j$ . In the case of a single binding site, Eq. (8) reduces to:

$$Q = 1 + K_{\mathcal{A}}[L] \tag{8a}$$

where  $K_A$  is the intrinsic (microscopic) site binding constant. If the receptor has one set of j identical and independent binding sites:

$$Q = (1 + K_{\mathcal{A}} \cdot [L])^j \tag{8b}$$

For m sets, each containing j identical and independent binding sites:

$$Q = \prod_{1}^{m} (1 + K_{A,m} \cdot [L])^{j_m}$$
 (8c)

In the case of cooperativity between a priori identical binding sites, the first ligand binds with  $K_{A,1} = K_A$ , the second with  $K_{A,2} = a \times K_A$ , the third with  $K_{A,3} = a \times b \times K_A$ , and so on. The cooperativity factors a, b, ... account for the change of intrinsic binding affinity of the unoccupied sites when the degree of saturation increases.

Equation (7) shows that the deconvolution of the binding isotherm from an ITC experiment requires calculation of the change in the degree of saturation,  $Y_i$ , with ligand concentration. In terms of the binding partition function,  $Y_i$  is expressed by

$$Y_{i} = \frac{\partial \ln Q}{\partial \ln[L]} = \frac{\sum_{j=1}^{n} j \beta_{j} [L_{i}]^{j}}{Q}$$

$$\tag{9}$$

Since  $[L_i]_B = [M]_{tot} \times Y_i$ , the total heat change after completion of injection *i* is

$$\Delta q_i = M_T \times V_{\text{cell}} \frac{\sum\limits_{j=1}^n \Delta H_{\text{app},i} j \beta_j [L_i]^j}{O}$$
 (10)

With the help of this statistical thermodynamic treatment it is possible to deconvolute a heat binding isotherm of a complex system involving non-equivalent and/or interacting binding sites. There are instructive examples demonstrating the strength of this approach (Eisenstein et al., 1994; Ferrari and Lohman, 1994; Hyre and Spicer, 1995; Bruzzese and Connelly, 1997; Gopal et al., 1997). The deconvolution has a firm thermodynamic foundation and avoids additional assumptions as is necessary in the analysis of spectroscopic binding data. In practice, however, the success much depends on the quality of the experimental data and on the number of coupled fitting parameters.

#### Informational content of ITC data

Free energy changes. As in other binding experiments, to obtain reliable binding constants the concentrations of the interacting species have to be in a proper range so that both the free ligands and the complex are populated. If the concentration of binding sites is very much higher than  $1/K_A$ , all the ligand added will be bound until saturation, and the binding isotherm as displayed in Fig. 1B has a rectangular shape with a slope approaching infinity. In the opposite case in which the binding site concentration is much below  $1/K_A$ , the binding isotherm is very shallow and full saturation is difficult to approach. For accurate values of  $K_A$ , the concentration of receptor binding sites should not be very much higher than  $1/K_A$ . The dimensionless number obtained by multiplying  $K_A$  with the total binding site concentration is called the c-value (Wiseman et al., 1989). As a rule of thumb, c-values between 10 and 100 give good  $K_A$ -values. Often, however, optimal concentrations are not accessible. For very tight binding reactions, optimal concentrations are too small to yield measurable heat changes. It is for this reason that even with the most sensitive instruments presently available,  $K_{\rm A}$  higher than about  $10^9~{\rm M}^{-1}~(\Delta G \sim -50~{\rm kJ~mol}^{-1}$  at room temperature) can not be very accurately measured. Very tight binding can be analyzed by DSC to be discussed in the section Differential Scanning Calorimetry. At the other extreme when  $K_A$  is very low, the concentrations required for cvalues between 10 and 100 may be so high that aggregation of macromolecules can obscure the binding reaction.

If  $\Delta G$  of binding is temperature dependent, it is sometimes possible to chose a temperature at which  $K_A$  can be measured by ITC. Unfortunately, often  $K_A$  is practically independent of temperature because of strong enthalpy/ entropy compensation. In this case, the thermodynamic linkage theory provides a general framework for calculating high binding constants from an appropriate thermodynamic cycle. For example,  $K_A$  can change with pH and one may chose a pH where  $K_A$  can be obtained by ITC. If the p $K_a$ values of the ligated and the ligand-free form of the receptor is known,  $\Delta G$  at the tight binding pH conditions can be calculated (Doyle et al., 1995; Baker and Murphy, 1996; Kavanoor and Eftink, 1997). Alternatively, ITC titrations can be conducted by titrating a strongly binding ligand into a solution containing the receptor already saturated with a weaker ligand. Free binding energies are obtained from such a displacement experiment if the strong and weak ligands exhibit suitable differences in binding enthalpy (Khalifah et al., 1993; Hu and Eftink, 1994; Sigurskjold et al., 1994).

Enthalpy changes. The molar binding enthalpy  $\Delta H_{\rm app}$  is a fitting parameter according to Eqs (6b) and (10) and is obtained together with  $K_{\rm A}$  from data collected in the optimal concentration range. A better practice is to measure  $\Delta H_{\rm app}$  at concentrations where the binding partners are fully associated when the degree of saturation is still low. In such experiments the accuracy of  $\Delta H_{\rm app}$  is better, yet the c-value is too high for accurate determination of  $K_{\rm A}$ . Thus, in practice  $K_{\rm A}$  and  $\Delta H_{\rm app}$  are best obtained from experiments performed at different concentration ratios.

The enthalpy change measured by ITC is a global property of the whole system. It is the total heat released or absorbed in the calorimetric cell on each addition of the ligand. The total heat contains contributions arising from nonspecific effects. These are the heat of dilution of the ligand into buffer, heat caused by the incomplete match of the temperatures of the solutions in the cell and at the injection syringe tip, or heat effects from mixing of buffers of slightly different chemical composition. The nonspecific heat effects are accounted for by  $\Delta q_{i,dil}$  and  $\Delta q_{i,ns}$  in Eqs (6a) and (6b). But even the corrected heat change  $\Delta q_i$  of Eq. (6b) is itself composed of different contributions. This is the reason why the molar enthalpy change is an apparent quantity ( $\Delta H_{\rm app}$ ). It only depends on the initial and final state of the binding reaction, the solvated free molecules and the final solvated complex.

Contribution of reorganization of solvent to  $\Delta H_{\rm app}$  and  $\Delta G$ . From the comparison of the calorimetric enthalpy change in H<sub>2</sub>O and D<sub>2</sub>O it was concluded that solvent reorganization accounts for a large portion of  $\Delta H_{\rm app}$ (Connelly et al., 1993; Chervenak and Toone, 1994). Indeed, in high-resolution crystal structures, water molecules can be seen at the complex interface where they may improve the complementarity of the interacting surfaces, and bound water is sometimes visible at the empty contact surface of the free molecules (Ladbury, 1996). Extended Hbond networks at the complex interface can make the enthalpy change more favorable, often counterbalanced by an entropic penalty (Bhat et al., 1994; Holdgate et al., 1997). That addition or removal of interfacial water contributes to the free energy of binding was directly shown by lowering the water activity through addition of glycerol

or another osmolyte (Kornblatt *et al.*, 1993; Robinson and Sligar, 1993; Jelesarov and Bosshard, 1994; Goldbaum *et al.*, 1996; Xavier *et al.*, 1997). Complexes with a low degree of surface complementarity and with no net change of hydration are tolerant to osmotic pressure (Lundbäck *et al.*, 1998).

Contribution of direct noncovalent bonds to  $\Delta H_{\rm app}$ . Apart from the bulk hydration effects, direct noncovalent bonds at the interface contribute to  $\Delta H_{\rm app}$ . These contributions may be considered to represent the binding enthalpy in a strict sense. Yet it is very difficult to sort out the enthalpy of formation of each specific noncovalent interaction. The net enthalpy effect of a particular noncovalent bond X-Y at the interface can result from the balance between the interaction enthalpy of the bond X-Y in the complex and the enthalpies from bonds between the solvent or solutes and X and Y in the isolated molecules. Further, subtle rearrangements of the packing interactions at the binding site compared to the free molecule may add to  $\Delta H_{\rm app}$ .

Mutational approaches have been tried to analyze the contributions of individual bonds to the enthalpy change. Examples are alanine scanning mutagenesis (Pearce et al., 1996), removal of a particular H-bond at the binding site (Connelly et al., 1994), or the construction of double mutant cycles (Frisch et al., 1997). Calorimetric analysis of mutants suffers from a major problem: Can one attribute a change of  $\Delta H_{\rm app}$  to the removal of a specific contact? Or is the enthalpic effect of an indirect nature and decomposition of  $\Delta H_{\rm app}$  in terms of individual residue-residue contacts or even atom-atom interactions is not possible? It has been argued on theoretical grounds that such decomposition of  $\Delta H_{\rm app}$  (as well as of  $\Delta G$  and  $\Delta S$ ) is not possible (Mark and van Gunsteren, 1994). But others have argued in favor of decomposition of  $\Delta H_{app}$  (Boresch and Karplus, 1995; Brady and Sharp, 1995).

In general, changes of  $\Delta H_{\rm app}$  are not, or only weakly correlated to changes in  $\Delta G$ . Recent careful analysis of three protein systems indeed suggests the correlation can not be made (Ito *et al.*, 1993; Pearce *et al.*, 1996; Frisch *et al.*, 1997). One reason for this unfortunate situation is enthalpy/entropy compensation. The overall change in binding enthalpy due to a particular mutation can be partly compensated by an entropy change. As a result, there only is a small change in the free energy of binding. This common thermodynamic behavior is thought to reflect a major role of compensating enthalpy and entropy contributions of water to the binding process (Lumry and Rajender, 1970; Dunitz, 1995; van Oss, 1997).

Calorimteric and van't Hoff enthalpy changes. The van't Hoff enthalpy change ( $\Delta H_{\rm vH}$ ) is calculated from the temperature dependence of  $K_{\rm A}$  obtained either by ITC or calculated from spectroscopic or other data [Eq. (5)]. Hence,  $\Delta H_{\rm vH}$  reflects the enthalpy intimately associated with the binding event that causes the signal change, for example the quenching of the fluorescence of a tryptophan residue in the complex ML. Therefore,  $\Delta H_{\rm vH}$  equals  $\Delta H_{\rm cal}$  only if the binding reaction follows a two-state transition between free and bound molecules and if the signal change used to calculate  $K_{\rm A}$  reflects the entire population of free and bound molecules. Otherwise,  $\Delta H_{\rm cal}$  and  $\Delta H_{\rm vH}$  are different. Indeed, systematic discrepancies between  $\Delta H_{\rm cal}$  and  $\Delta H_{\rm vH}$ 

have been reported (Gilli *et al.*, 1994; Naghibi *et al.*, 1995) and there have been attempts to rationalize the differences (Dunitz, 1995; Chaires, 1997; van Oss, 1997). On the other hand, a ratio of  $\Delta H_{\rm cal}/\Delta H_{\rm vH}=1$  can be taken to indicate that a binding event conforms to a two-state transition from free molecules to the complex with no detectable intermediates and with at most very minor contributions from water reorganization, conformational rearrangements, or changes in the state of protonation.<sup>3</sup>

**Protonation effects.** Among the many possible contributions to  $\Delta H_{\rm app}$ , the effect of changes in the protonation state is worth considering in more detail because the number of protons,  $n_{\rm H+}$ , taken up or released during the binding process can be measured by titration calorimetry (Murphy *et al.*, 1993; Jelesarov and Bosshard, 1994; Gomez and Freire, 1995; Kresheck *et al.*, 1995). If binding involves a change in the protonation state of L and/or M, protons are exchanged with the buffered medium. Therefore, the calorimetrically observed enthalpy change,  $\Delta H_{\rm app}$ , depends on the enthalpy of ionization of the buffer,  $\Delta H_{\rm buffer}$ . Repeating the experiment at the same pH in buffers of different  $\Delta H_{\rm buffer}$  allows one to calculate the binding enthalpy,  $\Delta H_{\rm bind}$ , from:

$$\Delta H_{\rm app} = \Delta H_{\rm bind} + n_{\rm H+} \times \Delta H_{\rm buffer}$$
 (11)

Values of  $\Delta H_{\rm buffer}$  have been tabulated (Christensen *et al.*, 1976) or can be measured by ITC (Jelesarov and Bosshard, 1994).  $\Delta H_{\rm bind}$  can be partitioned further into a term that is independent of the protonation change,  $\Delta H'_{\rm bind}$ , and a term describing the enthalpic contribution of the protonation reaction,  $\Delta H_{\rm H+}$ :

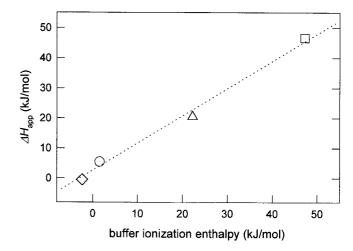
$$\Delta H_{\rm bind} = \Delta H'_{\rm bind} + n_{\rm H+} \Delta H_{\rm H+} \tag{11a}$$

Combining Eqs (11) and (11a):

$$\Delta H_{\rm app} = \Delta H'_{\rm bind} + n_{\rm H+} (\Delta H_{\rm H+} + \Delta H_{\rm buffer})$$
 (11b)

If a pH can be found where binding is pH-independent  $(n_{\rm H+}=0)$ ,  $\Delta H_{\rm app}=\Delta H'_{\rm bind}$  follows from Eq. (11b). Figure 2 shows an example in which binding of two proteins is accompanied by the uptake of a single proton. This system was particularly revealing since  $\Delta H'_{\text{bind}}$  was 26kJ mol<sup>-1</sup>, very much higher than  $\Delta H_{\rm app}$  because  $\Delta H'_{\rm bind}$  and  $\Delta H_{\rm buffer}$ almost canceled at pH 7. In practice, it is recommended to always repeat the ITC experiment at the same pH in a buffer that has a different heat of ionization. If the same  $\Delta H_{\rm app}$  is found in both buffers, there is no change in protonation of L and/or M when the complex forms. Conversely, variation of  $\Delta H_{\rm app}$  with buffer is a clear sign of a protonation event during the association reaction. Occasionally, one may obtain a hint from  $\Delta H_{\rm H+}$  (deduced with the help of Eq. 11) about the nature of the group(s) undergoing protonation/ deprotonation (Jelesarov and Bosshard, 1994; Gomez and Freire, 1995; Baker and Murphy, 1997).

Heat capacity changes. Modern ITC instruments allow to



**Figure 2.** Apparent enthalpy change,  $\Delta H_{\rm app}$ , for the binding of ferredoxin to ferredoxin:NADP+ oxidoreductase at 27 °C as a function of the ionization enthalpy of the buffer. ITC experiments were performed at pH 7.5 in Tris (square), Mops (triangle), phosphate (circle), and cacodylate buffer (diamond). Dashed line: linear least squares fit to Eq. (11). Slope = 0.96  $\pm$  0.03; intercept at zero buffer ionization enthalpy = 1.03  $\pm$  1.46 kJ mol<sup>-1</sup>. (Adapted from Jelesarov and Bosshard, 1994.)

precisely measure  $\Delta H_{\rm app}$  between about 5 and 70°C, and  $\Delta C_{\rm p}$  can be calculated from a plot of  $\Delta H_{\rm app}$  versus T (Eq. 3). In many cases such plots are linear within the experimental error in a narrow temperature range, suggesting that  $\Delta C_{
m p}$ itself does not depend on temperature. What is the origin of the change in heat capacity when a complex is formed?  $\Delta C_{\rm p}$ is almost always negative if the complex is taken as the reference state. This means that the complex has a smaller heat capacity than the sum of its free components. This and other observations as well as theoretical considerations indicate that  $\Delta C_p$  originates from changes in the degree of surface hydration in the free and the complexed molecules, and to a lesser extent also from changes in molecular vibrations (Sturtevant, 1977; Murphy and Freire, 1992; Spolar et al., 1992; Gomez et al., 1995; Makhatadze and Privalov, 1995). The often seen temperature-independence of  $\Delta C_{\rm p}$  infers that neither the area of contact surface nor the difference of the vibrational content between the complex and its components change within the observed temperature

Calculated and measured  $\Delta C_p$ . The association of two proteins to a complex can be compared to the folding of a single protein. In both reactions a substantial fraction of polar and nonpolar surface is buried and the degree of surface hydration is likely to change. There are semiempirical methods to calculate  $\Delta C_p$  from the change of the water-accessible polar and nonpolar surface area in protein folding and in protein association (Murphy and Freire, 1992; Spolar et al., 1992; Makhatadze and Privalov, 1995). Several communications report good agreement between the experimentally determined  $\Delta C_p$  and that calculated from the molecular surface buried in the complex (Connelly and Thomson, 1992; Murphy et al., 1993; Baker and Murphy, 1997; McNemar et al., 1997). However, a good correlation seems to hold only for those interactions that conform to a lock-and-key or rigid-body binding model. Very often this

 $<sup>^3</sup>$  For  $\Delta H_{\rm cal}/\Delta H_{\rm vH}=1$  in a system in which there is considerable water reorganization, conformational rearrangement or change in protonation states, the observable  $p_i$  of Eq. (4) has to mirror all the above phenomena. This seems not very likely in case the observable is, for example, a fluorescence change of a single chromophore.

model is inadequate. Significant discrepancies between calculated and measured  $\Delta C_{\rm p}$  were reported for small ligand binding (Faergeman et al., 1996; Holdgate et al., 1997), for protein-protein complexes (Bhat et al., 1994; Pearce et al., 1996), and most notably for protein-DNA complexes (Jin et al., 1993; Ladbury et al., 1994; Ayala et al., 1995; Merabet and Ackers, 1995; Berger et al., 1996; Oda et al., 1998). It is accepted that a lack of correlation between measured and calculated values of  $\Delta C_{\rm p}$  is a consequence of folding transitions coupled to the association event (Spolar and Record, 1994), and also to significant dynamic restriction of vibrational modes at the complex interface (Botuyan et al., 1993; Ladbury et al., 1994; Berglund et al., 1997). Interestingly, weaker complexes tend to show larger  $\Delta C_{\rm p}$ values per unit of surface area of contact. The likely reason is enhanced enthalpic and entropic fluctuation at a less tight complex interface (Tidor and Karplus, 1994). Large conformational rearrangements during binding and the preexistence of temperature-dependent conformational equilibria can cause deviations from linearity in the plots of  $\Delta H_{\rm app}$  against T, that is, temperature-dependent  $\Delta C_{\rm p}$ (Ferrari and Lohman, 1994; Bruzzese and Connelly, 1997). No doubt, the methods to calculate  $\Delta C_p$  from the parametrization of structural data need much improvement before becoming reliable predictors of heat capacity changes. In the meantime one has to rely on experiments. Here, a very careful examination of the conformational states of the molecules in isolation and of the complex they form is required to account for the observed energetic values in structural terms (Pearce et al., 1996; Wintrode and Privalov, 1997; Oda et al., 1998). This information can be obtained by DSC.

Entropy changes. The entropy of association can be calculated from measured values of  $\Delta G$ ,  $\Delta H$  and  $\Delta C_{\rm p}$ according to the laws of thermodynamics. The change in entropy of a complex relative to the unligated molecules is largely caused by hydration effects because the entropy of hydration of polar and apolar groups is large and there is significant reduction of water accessible surface on binding. Therefore, when a complex is formed the overall entropy change is often large and often positive. Occasionally, however, ordering of water at the complex interface occurs, which contributes unfavorably to  $\Delta S$  and favorably to  $\Delta H$ (Holdgate et al., 1997). Another important, unfavorable contribution to the entropy change originates from the reduction of side chain mobility at the binding site. Furthermore, a statistical term has to be added to the entropy change to account for the reduction in the number of particles and their degrees of freedom in the complex. Different estimates of the mixing entropy have been discussed, yet it appears that the 'cratic' correction accounts adequately for the loss of translation and rotation (Kauzmann, 1959; Murphy et al., 1994; Tamura and Privalov, 1997). Obviously, a negative entropy change can have different reasons and, most importantly, does not necessarily indicate that hydration of the interface remains unchanged or increases with respect to the free complex partners. On the other hand, a positive  $\Delta S$  is a strong undication that water molecules have been expelled from the complex interface.

#### Concluding remarks on ITC

The beauty of titration calorimetry is in its simplicity, which allows to obtain the entire set of thermodynamic parameters from performing only a few experiments at a series of different temperatures. The difficulty, however, lies in the fact that the observed heat change, which is the immediate outcome of ITC, is a global property. Only in those cases where the binding reaction follows a lock-and-key or rigidbody mechanism that can be described by a two-state transition between free and complexed molecules, and in which there is no change in the protonation state of L and/or M nor in the hydration state of the interface,  $\Delta H_{\rm app}$  is equal to the 'true' binding enthalpy attributable to noncovalent bonds in the complex. A good indicator - though no proof for this simple mechanism is the equality  $\Delta H_{\rm cal} = \Delta H_{\rm vH}$ . In the majority of cases  $\Delta H_{\mathrm{app}}$  has different origins, which often are difficult to distinguish. The contributions to  $\Delta H_{\mathrm{app}}$ sometimes can be separated. For example, a positive entropy change is a good indication for the extrusion of water from the complex interface. A change of  $\Delta H_{\rm app}$  with the chemical nature of the buffer points to a protonation/ deprotonation event concurrent with the binding reaction, and careful analysis of  $\Delta H_{\rm app}$  with buffer and pH can reveal the number and sometime even the nature of the group(s) whose ionization state changes. Finally, calculation of  $\Delta C_{\rm p}$ from the area of the surface buried in the complex (possible only if the necessary three-dimensional structures are available) and comparison with  $\Delta C_{\rm p}$  obtained by ITC can give a clue as to changes in conformational states and vibrational contents between the complex and its free components. These latter changes can be analyzed in more detail with the help of DSC to be discussed now.

# **Differential Scanning Calorimetry**

DSC is the most direct experimental technique to resolve the energetics of conformational transitions of biological macromolecules. By measuring the temperature dependence of the partial heat capacity, a basic thermodynamic property, DSC gives immediate access to the thermodynamic mechanism that governs a conformational equilibrium, for example between the folded and the unfolded forms of a protein, or between single and double stranded DNA. The theory of DSC and the thermodynamic interpretation of the experimental data have been the subject of excellent reviews (Privalov and Potekhin, 1986; Sturtevant, 1987; Freire, 1995). The combination of DSC with ITC to characterize the energy profile of an interacting system in a broad temperature interval and at varying solvent conditions has been brought up before (Connelly, 1994; Plum and Breslauer, 1995). Here we wish to give a basic description of the informational content of DSC measurements with special emphasis on the potential of DSC to analyze the energetics of macromolecular association reactions.

#### The DSC experiment

DSC measures the heat capacity of a solution of the

molecule under study as a function of temperature. Modern scanning calorimeters are equipped with twin cells and operate in a differential mode. The solution containing the solute – in the present context a biological macromolecule – is placed in the sample cell and an equal volume of solvent (buffer) in the reference cell. The system is heated (or cooled) quasi-adiabatically at a constant rate, typically 0.5–1.5 K min<sup>-1</sup>. Since the heat capacities of the solution in the sample cell and the solvent in the reference cell differ, a certain amount of electrical power is required to zero the temperature difference between the two cells. The power difference (J s<sup>-1</sup>), after normalization by the scanning rate (K s<sup>-1</sup>), is a direct measure of the heat capacity difference between the solution and the solvent:  $\Delta C_p^{\text{sol}\text{-solv}} = C_p^{\text{sol}\text{-}} - C_p^{\text{solv}}$  (in units of J K<sup>-1</sup>).

Obviously, one is interested in  $C_p(T)$ , the partial specific heat capacity (J K $^{-1}$  g $^{-1}$ ) of the solute M To obtain  $C_p(T)$ , the partial specific heat capacity of the solvent,  $C_{p,solv}(T)$ , has to be subtracted. This correction requires precise knowledge of the masses of the macromolecule and the solvent, of the mass of the solvent displaced by the macromolecule, and of the partial specific volumes of the macromolecule and the solvent. These quantities are temperature dependent and the coefficients of thermal expansion of the chemical species as well as of the calorimetric cell must be known. It can be shown that the partial specific heat capacity of the solute M (in units of J K $^{-1}$  g $^{-1}$ ) is given by:

$$C_{\rm p}(T) = C_{\rm p}^{\rm solv} \frac{\overline{v}_M}{\overline{v}_{\rm S}} + \frac{\Delta C_{\rm p}^{\rm sol-solv}}{m_M}$$
 (12)

 $m_M$  and  $\overline{\nu}_M$  are, respectively, the mass and the partial specific volume of M, and  $\overline{\nu}_s$  is the partial specific volume of the solvent.

Because the measured power difference,  $\Delta C_{\rm p}^{\rm sol-solv}$ , is small and the volumes of the calorimetric cells are 0.3–1.5 ml, milligram amounts of biomacromolecules are necessary for DSC measurements. In some cases, the macromolecule concentrations may be so high that the solutions are far from the ideal condition to which the thermodynamic models apply. This difficulty has to be kept in mind when performing DSC measurements and one has to check for nonspecific aggregation of macromolecules in the calorimeter cell, often revealed by a faint turbidity when the solution is removed from the cell after the experiment.

#### Informational content of DSC data

The first result obtained from a DSC experiment is the partial specific heat capacity,  $C_p(T)$ . This quantity contains important information about the conformational state of a protein in the temperature interval of the experiment. For small globular proteins, the absolute value of  $C_p$  at 25 °C varies in the range 1.2–2.3 J K<sup>-1</sup> g<sup>-1</sup> and increases linearly with temperature with a slope of  $(6-8) \times 10^{-3}$  J K<sup>-2</sup> g<sup>-1</sup>. Deviations from these values may indicate loose packing of the protein or structural fluctuations (Privalov and Potekhin,

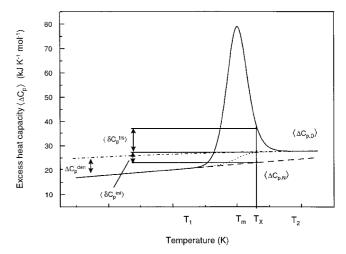


Figure 3. Partial molar heat capacity of a protein undergoing reversible thermal denaturation in the temperature interval  $T_1$ and with a transition midpoint at  $T_{\rm m}$ . The heat capacity of the native state,  $\langle C_{p,N} \rangle$ , shows a linear temperature dependence (dashed line). The heat capacity of the denatured state,  $\langle \mathcal{C}_{\mathsf{p},\mathsf{D}} \rangle$ , is approximated by a quadratic function (dashed-dotted line). The functions  $\langle \textit{C}_{p,N}(\textit{T}) \rangle$  and  $\langle \textit{C}_{p,D}(\textit{T}) \rangle$  can be extrapolated into the transition zone between  $T_1$  and  $T_2$  in proportion to the progress of transition zone between  $r_1$  and  $r_2$  in population (dotted line). The difference between  $\langle C_{p,D} \rangle$  and  $\langle C_{p,N} \rangle$ is the heat capacity increment of protein denaturation,  $\Delta C_p$ is positive because the denatured protein has a larger heat capacity than the native protein. The excess partial heat capacity,  $\langle \Delta \mathcal{C}_p \rangle$ , is defined as  $\langle \Delta \mathcal{C}_p \rangle = \langle \mathcal{C}_p \rangle - \langle \mathcal{C}_{p,N} \rangle \cdot \langle \Delta \mathcal{C}_p \rangle$  is composed of the intrinsic excess heat capacity,  $\langle \delta \mathcal{C}_p^{\text{int}} \rangle$ , which accounts for all the molecular species that become populated in the progress of the transition from the native to the denatured state, and from the transition excess heat capacity,  $\langle \delta \mathcal{C}_p^{\, trs} \rangle$ , originating from the increased fluctuation of the system when the protein changes between different enthalpic states in the course of thermal denaturation. The relative magnitudes of  $\langle \delta \mathcal{C}_{\mathbf{p}}^{\;\; \mathrm{int}} \rangle$  and  $\langle \delta \mathcal{C}_{\mathbf{p}}^{\;\; \mathrm{trs}} \rangle$  at temperature  $T_x$  are indicated.

1986; Gomez et al., 1995). The partial specific heat capacity of the native protein is significantly lower than that of the denatured protein.  $C_{\rm p}$  of a fully unfolded protein can be approximated from the amino acid sequence by summing up the heat capacities of the amino acid residues and the contributions of the peptide bonds (Privalov and Makhatadze, 1990; Makhatadze and Privalov, 1995). If the experimentally measured  $C_{\rm p}$  after completion of unfolding is lower than  $C_{\rm p}$  calculated from the amino acid sequence, this may indicate that the denatured protein has some residual structure and is not a fully solvated polypeptide chain.<sup>5</sup>

When a protein solution is heated up,  $C_{\rm p}({\rm T})$  follows a peak-shaped curve if protein denaturation is cooperative and reversible. Figure 3 shows a typical DSC trace, also called a thermogram or a thermal transition curve. The protein denatures in the temperature interval  $T_1$  to  $T_2$  with a transition midpoint  $T_{\rm m}$ .

 $<sup>^4</sup>$  A constant pressure is applied to the two cells. Depending on this pressure, the upper temperature limit can be as high as 150 °C for aqueous solutions.

 $<sup>^5</sup>$ The term 'denatured' refers to the ensemble of conformational states when thermal transition is complete. In practice, this is at a temperature well above the transition temperature  $T_{\rm m}$ . The denatured protein is not necessarily equivalent to the completely unfolded protein, which is an idealized state referring to the polypeptide chain in its fully solvated conformation. Here we prefer the term 'denatured' to indicate this difference.

For a meaningful comparison of the thermal transition curves of different substances the specific heat capacity is inadequate because it is normalized to the mass of substance. The appropriate quantity is the partial *molar* heat capacity,  $\langle C_p \rangle$ , which has units of J K<sup>-1</sup> mol<sup>-1</sup>. It is obtained by multiplying  $C_p$  (J K<sup>-1</sup> g<sup>-1</sup>) by the molecular weight (g mol<sup>-1</sup>). The angular brackets,  $\langle \ \rangle$ , designate the ensemble-averaged population of all molecular states that become populated during the transition from the native to the denatured form. It is very important to recognize that during the transition the partial heat capacity function can no longer be ascribed to a single structural state.

Excess heat capacity, excess enthalpy and excess entropy. If the native state is taken as a reference, an excess partial molar heat capacity can be defined as

$$\langle \Delta C_{\rm p} \rangle = \langle C_{\rm p} \rangle - \langle C_{\rm p,N} \rangle$$

The excess heat capacity can be divided in two components. The first component accounts for the sum of the molecular species that become populated in the progress of the transition from the native to the denatured state. This component is often referred to as the *intrinsic* excess heat capacity,  $\langle \delta C_{\rm p}^{\rm int} \rangle$ . The second contribution to  $\langle \Delta C_{\rm p} \rangle$  originates from the increased fluctuation of the system when the protein changes between different enthalpic states in the course of thermal denaturation. This component is called *transition* excess heat capacity,  $\langle \delta C_{\rm p}^{\rm trs} \rangle$ , and is usually much larger than  $\langle \delta C_{\rm p}^{\rm int} \rangle$  as indicated in Fig. 3. The excess molar heat capacity can now be written as:

$$\langle \Delta C_{\rm p} \rangle = \langle \delta C_{\rm p}^{\rm int} \rangle + \langle \delta C_{\rm p}^{\rm trs} \rangle \tag{13}$$

To calculate  $\langle \delta C_{\rm p}^{\rm int} \rangle$ , the functions  $\langle C_{\rm p,N}(T) \rangle$  and  $\langle C_{\rm p,D}(T) \rangle$  have to be extrapolated into the transition zone between  $T_1$  and  $T_2$  in proportion to the progress of transition (Sturtevant, 1987). This extrapolation is indicated by the dotted line in Fig. 3. The excess enthalpy of the thermal denaturation,  $\Delta H_{\rm den}$ , is defined by:

$$\Delta H_{\rm den} = \int_{T_1}^{T_2} \langle \delta C_{\rm p}^{\rm trs} \rangle dT \tag{14}$$

 $\Delta H_{\rm den}$  corresponds to the area of the peak above the dotted line in Fig. 3. The excess entropy of denaturation is defined by:

$$\Delta S_{\text{den}} = \int_{T_1}^{T_2} \frac{\langle \delta C_{\text{p}}^{\text{trs}} \rangle}{T} dT$$
 (15)

 $\Delta H_{\rm den}$  represents the 'true' calorimetric estimate of the denaturation enthalpy and is a model-independent value, i.e. it does not depend on the shape of the transition curve between  $T_1$  and  $T_2$ .

The integral of  $\delta C_{\rm p}^{\rm trs}$  [Eq. (14)] can also be analyzed according to the van't Hoff equation to obtain  $\Delta H_{\rm den}^{\rm vH}$ , sometimes called the 'effective' enthalpy of transition.  $\Delta H_{\rm den}{}^{\rm vH}$  is model-dependent. The reason is that determination of  $\Delta H_{\rm den}^{\rm vH}$  assumes an equilibrium between only two forms, native and denatured protein, to calculate an equilibrium constant K(T) from which  $\Delta H_{\rm den}^{\rm vH}$  follows according to Eq. (5a).  $\Delta H_{\rm den}^{\rm vH}$  now can be compared with the calorimetric, model-independent enthalpy change,  $\Delta H_{\rm den}^{\rm cal}$ , described by Eq. (14) (the superscript<sup>cal</sup> is added only to distinguish the calorimetrically measured quantity from the calculated van't Hoff enthalpy change). If  $\Delta H_{\rm den}^{\rm vH}$  $/\Delta H_{\rm den}^{\rm cal} = 1$ , denaturation is thought to obey a two-state, cooperative unfolding reaction. A ratio >1 may indicate significantly populated intermediate states. Values above unity also result if the definition of the cooperatively folding unit is not the same in the calorimetric and in the van't Hoff analysis. This is the case if the excess heat capacity function does not display a symmetric curve and hides transitions between more than two states.<sup>8</sup> A ratio <1 points to an irreversible process. The approach to compare  $\Delta H_{\rm den}^{\rm vH}$  with  $\Delta H_{\rm den}^{\rm cal}$ , both calculated from DSC data as outlined above, may be in error when  $\langle \delta C_{\rm p}^{\rm int} \rangle$  is not much smaller than  $\langle \delta C_{\rm p}^{\rm trs} \rangle$  and, more generally, if the system deviates from the two-state behavior (Privalov and Potekhir, 1986).

Statistical thermodynamic treatment of the heat capacity function. At this point it is important to discuss the high informative potential of a statistical-mechanical treatment of DSC data. The strength of the DSC method is that it provides direct access to the system partition function without invoking *ad hoc* assumptions about the thermodynamic mechanism of conformational transition

 $<sup>^6</sup>$  The vibrational content of the polypeptide chain increases upon unfolding, which also contributes to the positive value of  $\Delta C_{\rm p}^{\rm \, den}$ . The magnitude of this effect is small in comparison to the hydration effect. Parametrisation of  $\Delta C_{\rm p}^{\rm \, den}$  in terms of the change in solvent-accessible surface area has been based on thermodynamic data for the dissolution of model compounds. The parametrisation partly accounts for vibrational contributions.

<sup>&</sup>lt;sup>1</sup>/<sub>7</sub> In the case of a simple two-state transition it is only the native and the denatured state.

 $<sup>^8</sup>$   $\langle \delta C_{\rm p}^{\rm trs}(T) \rangle$  is a symmetric bell-shaped curve only for monomolecular transitions. In the case dissociation of a complex and unfolding of its components are coupled reactions, the heat capacity trace is skewed at the high-temperature shoulder. The maximum of the heat absorption peak,  $T_{\rm m}$ , is higher than the temperature at which the transition is half-complete ( $F_{\rm i}$ =0.5, see the section 'Statistical thermodynamic treatment of the heat capacity function'.

(Freire and Biltonen, 1978a,b; Freire, 1994). For an arbitrary system containing N different states (N = 2 for a two-state transition), the system partition function is defined as:

$$Q = \sum_{i=1}^{N} K_i = \sum_{i=1}^{N} \exp\left(-\frac{\Delta G_i}{RT}\right)$$
 (16)

The expression under the summation sign represents the statistical factors of each state.  $\Delta G_i$  is defined by Eq. (1). The excess enthalpy of the system with respect to the native state is:

$$\langle \Delta H \rangle = \sum_{i=1}^{N} \Delta H_i F_i \tag{17}$$

where  $\Delta H_i$  is the enthalpy of state *i* relative to the native reference state, and  $F_i$  is the population of state *i* in terms of the system partition function Q:

$$F_i = \frac{\exp\left(-\frac{\Delta G_i}{RT}\right)}{Q} \tag{18}$$

Since the excess heat capacity is the first derivative of the excess enthalpy with respect to the temperature,  $\langle \Delta C_{\rm p} \rangle$  can be expressed as:

$$\langle \Delta C_p \rangle = \frac{\langle \Delta H \rangle}{\mathrm{d}T} = \frac{\sum_{i=1}^{N} (\Delta H_i F_i)}{\mathrm{d}T}$$

$$= \sum_{i=1}^{N} \Delta C_p^{\mathrm{den}} F_i + \sum_{i=1}^{N} \Delta H_i \frac{\mathrm{d}F_i}{\mathrm{d}T}$$
(19a)

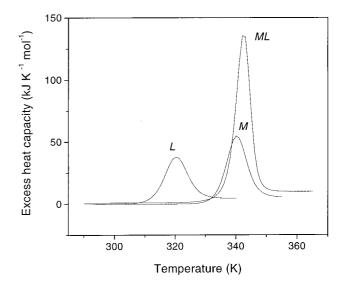
and after differentiation of  $dF_i/dT$ :

$$\langle \Delta C_p \rangle = \frac{\langle \Delta H \rangle}{\mathrm{d}T} = \sum_{i=1}^{N} \Delta C_p^{\mathrm{den}} F_i + \frac{\langle \Delta H^2 \rangle - \langle \Delta H \rangle^2}{RT^2}$$
$$= \sum_{i=1}^{N} \langle \delta C_{\mathrm{p},i}^{\mathrm{int}} \rangle + \sum_{i=1}^{N} \langle \delta C_{\mathrm{p},i}^{\mathrm{trs}} \rangle$$
(19b)

The statistical-mechanical treatment does not include arbitrary assumptions about the number of states populated in the transition process and about the mutual interaction of these states. The data can be rigorously tested against different thermodynamic models by variation of the definition of the partition function. Well-established statistical optimization procedures are used to find a model that best describes the experimental data. This approach has been successfully exploited to study complex unfolding processes (Montgomery *et al.*, 1993; Griko *et al.*, 1994a; Haynie and Freire, 1994; Johnson *et al.*, 1995).

#### Application of DSC to association reactions

How can we derive the energetic parameters of biological association reactions with the help of DSC data? If a ligand L binds to the native state of a protein M with high affinity, the heat capacity of the resulting complex LM will differ from that of M and L alone. As a consequence, the DSC



**Figure 4.** Simulated excess heat capacity profiles of ligand L, protein M and complex ML. In this idealized example, thermal transitions of L ( $T_{\rm m} = 320$  K) and M ( $T_{\rm m} = 340$  K) are well separated and lower than the thermal transition of the complex LM. Strong association leads to mutual stabilization of the complex partners in LM. The dissociation of the complex is tightly coupled to the denaturation of its components and a single peak appears in the heat capacity trace with  $T_{\rm m} = 343$  K, above the denaturation temperatures of L and M in isolation. The curves were calculated with the help of Eq. (22) for the conditions given in Fig. 5 with  $\Delta H_c$ (298 K) = -20 kJ mol $^{-1}$  and  $K_c$ (298 K) =  $10^{10}$  M $^{-1}$ .

profiles of L, M and ML will have distinct shapes. Dramatic deformations of the thermograms of proteins in the ligated state have been reported (Takahashi and Fukada, 1985; Shrake and Ross, 1990; Lin et al., 1994; Conejero-Lara and Mateo, 1996). The influence of ligand binding on the stability of a whole protein, or a protein domain, can be large even if the ligand is a small organic compound. The situation is even more complicated when the ligand itself is a macromolecule undergoing conformational transition(s) with temperature. Furthermore, because the binding affinity and the stability of the complex partners and the complex itself are sensitive to pH, to ionic strength and to the nature of cosolutes, the excess heat capacity function,  $\langle \Delta C_{\rm p}(T) \rangle$ , can be distorted when the solvent conditions vary (Ramsay and Freire, 1990; Carra and Privalov, 1997). A careful deconvolution of the observed thermograms gives insight in the thermodynamic forces that drive the association reaction and can provide structural and mechanistic information about the interacting molecular species (Davis et al., 1995; Litvinovich and Ingham, 1995; Filimonov and Rogov, 1996).

When the mutual stabilization of the complex partners in ML is high, the dissociation of the complex is tightly coupled to the denaturation of its components. The result is a single peak in the heat capacity trace at a temperature above the denaturation temperatures of L and M in isolation. Figure 4 shows an idealized example. In such a case, a simplified procedure can be applied to extract the enthalpy of complex formation. It involves extrapolation of the enthalpies of denaturation of the components to the melting temperature of the complex (Fukada  $et\ al.$ , 1985; Makarov

et al., 1994; Yakovlev et al., 1995). The energetics of complex formation can be studied also by investigating the dependence of  $\Delta H_{\rm m}$  and  $T_{\rm m}$  on the saturation level of the system (Bhushan and McNamee, 1990; Shrake and Ross, 1990; Anteneodo et al., 1994; Horvath et al., 1994). However, in the majority of systems studied so far, the DSC trace has a complicated shape and exhibits several overlapping transitions. Moreover, even if the dissociation and the denaturation take place in a narrow temperature range, there is no a priori information about a possible redistribution of sub-states in the melting zone.

Deconvolution of DSC traces. The thermodynamic theory of deconvolution of coupled equilibria in macromolecular systems has been developed already with the first appearance of sensitive microcalorimeters. An extensive thermodynamic framework for extracting the free energy and enthalpy of binding from DSC data was first developed by Robert et al. (1989) and by Brandts and Lin (1990). More recently, the statistical-mechanical aspects of the deconvolution technique have been formulated by other investigators in the light of a global linkage analysis of twodimensional heat capacity surfaces (by variation of temperature and ligand concentration; Ramsay and Freire, 1990; Straume and Freire, 1992; Straume, 1994; Barone et al., 1995). The idea is to redefine the partition function of the system to account for the interaction between the molecules and then to use the standard expression of statistical thermodynamics, which is analogous to Eq. (5a), to calculate the excess enthalpy:

$$\frac{\delta \ln Q}{\delta T} = \frac{\langle \Delta H \rangle}{RT^2} \tag{20}$$

The relevant equations can be explicitly solved for only a few simple models, but numerical methods of non-linear optimization can help to adapt a particular model to the experimental data. To illustrate a strategy of how to deal with heat capacity traces, we again consider the simple case of interaction between L and M to the 1:1 complex ML, which we call C. The total concentrations are kept equal,  $[L]_{\text{tot}} = [M]_{\text{tot}}$ . The overall process is described by the following scheme:

$$egin{array}{cccc} L_{
m N} & + & M_{
m N} \stackrel{\kappa_{
m C}}{\Longleftrightarrow} & C \ & & & \uparrow \downarrow K_M \ & & & & L_{
m D} & & M_{
m D} \end{array}$$

L and M exist in the native and the denatured form (subscripts  $_{\rm N}$  and  $_{\rm D}$ , respectively). The free components are described by the following set of parameters (X denotes L or M): free energies of denaturation,  $\Delta G_X$ ; equilibrium denaturation constants,  $K_X$ ; melting temperatures,  $T_{\rm mX}$ ; denaturation enthalpies,  $\Delta H_{\rm mX}$ ; and heat capacity increments of denaturation,  $\Delta C_{\rm p,X}^{\rm den}$ . The parameters for the complex C are: free energy of binding,  $\Delta G_{\rm C}$ ; binding constant,  $K_{\rm C}$ ; arbitrarily chosen reference temperature,  $T_{\rm R,C}$ ; enthalpy of complex formation,  $\Delta H_{\rm C}$ ; and heat capacity change of binding,  $\Delta C_{\rm p,C}$ . In what follows, two assumptions are made. Only  $L_{\rm N}$  and  $M_{\rm N}$  interact to form the complex C, and  $T_{\rm mC}$  is always higher than  $T_{\rm mX}$  as shown in the idealized example of Fig. 4. If this second condition is not fulfilled,

the denaturation of L and/or M are/is not coupled to the binding equilibrium.

The partition function of the system describes the relative population of the native and denatured states of L, M and the population of C. Formally, we can write separate functions for L and M:

$$Q_L = 1 + K_L + K_C[M_N]$$
  
 $Q_M = 1 + K_M + K_C[L_N]$ 

The two functions are coupled and the concentrations of  $L_N$ ,  $M_N$  and C are:

$$[L_{\mathrm{N}}] = \frac{[L]_{\mathrm{tot}}}{Q_L}$$
  $[M_{\mathrm{N}}] = \frac{[M]_{\mathrm{tot}}}{Q_M}$   $[C] = K_C[L_{\mathrm{N}}][M_{\mathrm{N}}]$ 

The concentrations of the free components,  $[L_N]$  and  $[M_N]$ , can be solved simultaneously in terms of the known total concentrations and the equilibrium constants  $K_L$ ,  $K_M$  and  $K_C$ , which are temperature dependent parameters according to (subscript  $_X$  denotes L, M or C and subscript  $_R$  a reference temperature):

$$K_X(T) = K_X(T_{R,X}) \exp\left[-\frac{\Delta H_{R,X}}{R} \left(\frac{1}{T} - \frac{1}{T_{R,X}}\right) + \frac{\Delta C_{p,X}}{R} \left(\ln \frac{T}{T_{R,X}} + \frac{T_{R,X}}{T} - 1\right)\right]$$
(21)

The excess enthalpy of the system, relative to the complex C as the reference state, for the given total concentrations  $[L]_{\text{tot}}$  and  $[M]_{\text{tot}}$ , can be written in analogy to Eq. (17) as:

$$\langle \Delta H \rangle = \sum_{X=L,M} \left[ \frac{K_X}{Q_X} \Delta H_X + \frac{K_X}{Q_X} \Delta C_{p,X} \right] - \frac{[C]}{[L]_{tot}} \Delta H_C - \frac{[C]}{[L]_{tot}} \Delta C_{p,C}$$
(22)

The last two terms in the above equation are correct only if  $[L]_{\text{tot}} = [M]_{\text{tot}}$ . The combination of Eqs (21) and (22) describes the excess enthalpy function,  $\langle \Delta H(T) \rangle$ , of an associating system. From the combined equations, the excess heat capacity function,  $\langle \Delta C_p(T) \rangle$ , is calculated by either explicit or by numerical differentiation.

A set of simulations according to this general procedure is shown in Fig. 5. Panel A shows how the DSC trace is influenced by the stability of the complex (variation of  $K_C$  at fixed  $K_M$  and  $K_L$ ). If the complex is weak, the thermogram shows the denaturation of free L and free M as two well separated thermal transitions. When the complex dominates, a single sharp peak at high temperature is seen because the dissociation of C and the denaturation of L and M are strongly coupled. For cases in between, the trace envelopes the dissociation of the complex and the denaturation of the free components. Panel B shows how the DSC trace changes

<sup>&</sup>lt;sup>9</sup> If  $[L]_{\text{tot}} \neq [M]_{\text{tot}}$ , the binding polynomial has to be used to calculate the fraction of complex at each temperature.

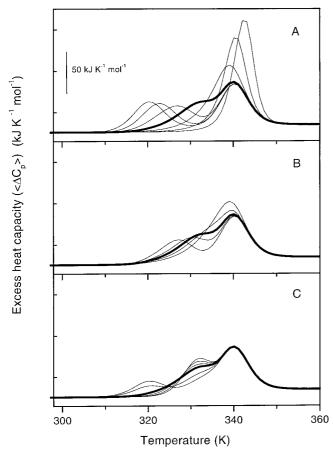


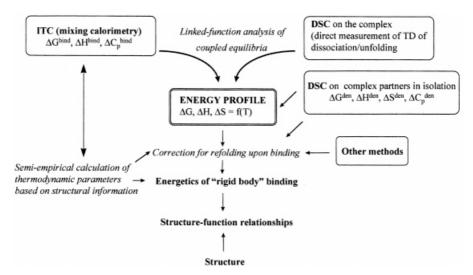
Figure 5. Simulated excess heat capacity profiles for the interacting system  $L + M \rightarrow C$ . The curves were simulated with the help of Eq. (22). The following parameters were fixed for all simulations:  $T_{\rm m,L} = 320 \, \text{K}$ ,  $T_{\rm m,M} = 340 \, \text{K}$ ,  $\Delta H_{\rm L}(T_{\rm m}) = 350 \, \text{kJ mol}^{-1}$ ,  $\Delta H_{\rm M}(T_{\rm m}) = 450 \, \text{kJ mol}^{-1}$ ,  $\Delta C_{\rm p,L} = 5.5 \, \text{kJ K}^{-1} \, \text{mol}^{-1}$ ,  $\Delta C_{\rm p,M} = 4.5 \, \text{kJ} \, \text{K}^{-1} \, \text{mol}^{-1}$ , and  $\Delta C_{\rm p,C} = -1 \, \text{kJ K}^{-1} \, \text{mol}^{-1}$ . The traces drawn in thick line are for identical conditions in all three panels. Panel A: variation of the DSC trace with variation of  $K_c$ . The curves from left to right were calculated for  $K_c = 1$ ,  $10^5$ ,  $10^6$ ,  $10^7$ ,  $10^8$ ,  $10^9$ , and  $10^{10}$  M $^{-1}$  at 298 K. The leftmost curve has two well-separated peaks centered at 320 and 340 K, respectively. The peaks correspond to the denaturation of free L and free M, respectively. The rightmost curve has a single peak centered at 343 K. It corresponds to the coupled dissociation and denaturation of the complex and its components, undisturbed by the presence of free L and M. The curves in between are composed to variable degrees of the transitions of the free and the complexed species.  $\Delta H_{\rm R,C}$  was fixed at  $-20~{\rm kJ~mol^{-1}}$  and 298 K. *Panel B*: variation of the DSC trace with variation of the excess enthalpy of the complex at the reference temperature 298 K. The curves from left to right were calculated for  $\Delta H_{B,C} = 20$ , 0, -20, -40, and -80 kJ at 298 K. It is seen how the temperature influences  $K_{\mathbb{C}}$ according to eqn (21). Hence, the overall trace of a DSC experiment changes with  $\Delta H_{R,C}$ . The leftmost trace calculated for  $\Delta H_{R,C}=+20$  kJ mol $^{-1}$  clearly has two peaks. The reason is that  $K_{\rm C}$  decreases with increasing temperature if  $\Delta H_{\rm R,C}$  is positive, as follows from Eq. (21). Conversely, K<sub>C</sub> increases with temperature if  $\Delta \textit{H}_{\textrm{R,C}} < 0$  and, therefore, the rightmost curve essentially has only a single peak, albeit with a broad shoulder.  $K_C$  was fixed at  $10^7~M^{-1}$  at 298 K. Panel C: Variation of the DSC trace with variation of the ratio [L]<sub>tot</sub>/[M]<sub>tot</sub>. The curves from left to right were calculated for [L]<sub>tot</sub>/[M]<sub>tot</sub> = 0.5, 0.67, 1, 1.5, 2, and 4.  $\Delta H_{\rm C}$ (298 K) was fixed at -20 kJ mol $^{-1}$  and  $K_{\rm C}$ (298 K) at  $10^7$  M $^{-1}$ .

with the magnitude of the enthalpy of complex formation,  $\Delta H_{\rm C}$ . From Eq. (21), it follows that  $K_{\rm C}$  has a maximum at the temperature where  $\Delta H_{\rm C}=0$ , that is, where  $\Delta H_{\rm C}$  changes sign. Panel C demonstrates how the DSC trace changes with the molar ratio of  $[L]_{\rm tot}/[M]_{\rm tot}$ .

In practice, models can be tested against the experimental data by statistical methods. The statistical analysis is simpler if the unfolding enthalpies, unfolding heat capacity increments and unfolding free energies of each complex partner in isolation are known from separate DSC scans. Here, the statistical analysis of the DSC traces as shown in Fig. 5 can be limited to the parameters of the association reaction, keeping the parameters pertaining to the free components fixed. In principle, it is also possible to perform a global statistical analysis without a priori knowledge of some of the thermodynamic parameters. However, such rigorous statistical analysis by non-linear fitting procedures can be flawed because of the multi-minima problem when the number of parameters is large and some parameters are strongly interdependent.

Applications of the deconvolution analysis. Deconvolution analysis of DSC traces was successfully applied to study the energetics of small ligand binding like ferric ion binding to transferrins (Lin et al., 1994), sulfate binding to yeast phosphoglycerate kinase (Hu and Sturtevant, 1989), and biotin binding to streptavidin (Gonzalez et al., 1997). Other examples are inhibitor binding to barnase (Martinez et al., 1994), to ribonuclease (Barone et al., 1995), and to thymidylate synthase (Chen et al., 1996), or monosaccharide binding to proteins (Schwarz et al., 1993). In most cases good agreement was observed between the binding free energies determined by DSC and other equilibrium methods, and the superiority of DSC to measure binding affinities not accessible by other techniques was documented. Indeed, DSC allows to measure very tight binding, and this is a major asset of the technique compared to ITC and to non-calorimetric equilibrium techniques. The high resolution potential of the deconvolution of complex heat capacity traces was documented in studies of protein systems like the S-protein-S-peptide complex (Graziano et al., 1996), the barnase-barstar complex (Martinez et al., 1995), and the heparin/antithrombin complex (DeLauder et al., 1992). Conformational transitions were found to accompany the dimerization of a thermolysin fragment (Conejero-Lara and Mateo, 1996), and the association of an unfolding intermediate of the Cro repressor from bacteriophage  $\bar{\lambda}$ was identified (Filimonov and Rogov, 1996).

The statistical mechanical approach to DSC data was successfully applied to study the domain structure and domain-domain interactions in some very complicated molecular systems like the *Escherchia coli* DNA gyrase (Blandamer et al., 1994), the multimeric molecular chaperon DnaK (Montgomery *et al.*, 1993), and the heparin-binding fragment of fibronectin (Novokhatny *et al.*, 1992). Recent work on protein binding to single-stranded DNA and to DNA-duplexes illustrated the power of the combined ITC and DSC approach. Protein–DNA association is characterized by low discrimination between specific and nonspecific binding and by large structural rearrangements accompanying the binding reaction. The thermodynamic analysis of these complex systems could



**Figure 6.** Scheme depicting the combined experimental and theoretical approach to the analysis of complex binding energetics. ITC provides the global thermodynamic parameters of the binding reaction (top left). Semi-empirical, structure-based calculations complement ITC data (lower left). DSC on the complex and on its free components (right hand side) can help to decompose the global parameters from ITC into contributions from conformational changes, folding of molecular domains, etc. Data from non-calorimetric methods complement the picture (bottom and lower right hand side). The energy profile of the binding reaction is the final result of the combined ITC-DSC approach (center) and a corner stone in the elucidation of structure–function relationships (bottom).

profit from the synergism of the ITC-DSC combination (Cooper *et al.*, 1994; Davis *et al.*, 1995; Merabet and Ackers, 1995; Carra and Privalov, 1997; Oda *et al.*, 1998).

#### **Conclusions**

We have tried to give an overview of the calorimetric techniques and to summarize some recent representative applications aimed at dissecting the energetics of macromolecular recognition. In view of the high sensitivity of commercially available instruments and of the capacity of molecular biology techniques and solid phase synthesis to produce large amounts of pure proteins and nucleic acids, the comprehensive thermodynamic description of a growing number of associating systems will become possible in the near future. Figure 6 illustrates how the power of ITC and DSC can be combined and linked with structural data. The central aim is to obtain an energy profile of the complex and to formulate a plausible mechanism of the association reaction. To know the energy profile means to know the heat capacity change of the association reaction and to predict the free energy, enthalpy, and entropy change of association over as broad a temperature range as possible and for varying conditions of solvent, pH, cosolutes, etc. To know the mechanism of the association reaction means to describe the transition from the free components to the final complex in terms of all intermediate states populated under equilibrium conditions, and to reveal their mutual interdependence.

ITC is clearly the method of choice to measure the free energy, enthalpy, heat capacity and stoichiometry of a binding reaction of modest affinity. Very weak and very tight binding constants are not directly accessible by ITC. Data collected by non-calorimetric methods are used to get van't Hoff enthalpies, which when compared with calorimetric enthalpies can help to clarify a binding mechanism. The quality of  $\Delta H$  and  $\Delta C_p$  from ITC is high when the association can be approximated by a rigid-body interaction. However, the lock-and-key concept is an oversimplification for many protein-protein complexes and is almost always inappropriate when applied to protein–DNA interactions. The resolution of ITC data can be improved substantially when the structure of the complex and of its free components is known (or a reasonable model can be proposed). In this case, semi-empirical, structure-based calculations can complement the experimental data. Still, these computational methods cannot (yet) replace experimental data. Here, the DSC technique comes to help. By deconvolution of the excess heat capacities of the interacting molecules one is in a position to ascribe at least part of the enthalpy and heat capacity measured by ITC to folding event(s) induced by the binding reaction. DSC data are invaluable in the estimation of entropic factors of a binding equilibrium and in measuring extremely high binding affinities. Statistical-mechanical analysis of two-dimensional excess heat capacity surfaces can provide further information on the nature of a complex and on the energetic factors driving its formation. DSC is the only method to access the system partition function to calculate the population of free and bound molecular species as a function of temperature and concentration.

Even the best and the most comprehensive set of thermodynamic data can be flawed, and we have tried to lay bare possible difficulties and inconsistencies of data analysis. Indeed, thermodynamic studies always need company of additional studies based on other biochemical, structural and biophysical methods. As stated in the Introduction, we know much about *how* biomacromolecules

associate and wish to better understand why they do so, but the how and why are strongly interdependent.

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