

Question 1:

1. $BH \rightarrow E$ holds.

We prove it by computing the transitive closure of BH :

With $H \rightarrow AC$, we derive $BH \rightarrow BHAC$

With $AB \rightarrow DE$, we derive $BH \rightarrow BHACDE$,

Hence, $BH \rightarrow E$ holds.

2. $T = \emptyset$

Find a super key X .

Let $X := \{B, E, G, H, I\}$

$X^+ = \{A, B, C, D, E, G, H, I, J\}$

Try to remove B , $\{E, G, H, I\}^+ = \{A, C, E, G, H, I\}$

Thus, B cannot be removed.

Try to remove E , $\{B, G, H, I\}^+ = \{A, B, C, D, E, G, H, I, J\}$

Thus, $X := \{B, G, H, I\}$

Try to remove G , $\{B, H, I\}^+ = \{A, B, C, D, E, G, H, I, J\}$

Thus, $X := \{B, H, I\}$

Try to remove H , $\{B, I\}^+ = \{B, I\}$

Thus, H cannot be removed.

Try to remove I , $\{B, H\}^+ = \{A, B, C, D, E, G, H, J\}$

Thus, I cannot be removed.

So $\{B, H, I\}$ is a candidate key and add to T .

Find another super key X .

Let $X := \{B, C, G, I, J\}$

$X^+ = \{A, B, C, D, E, G, H, I, J\}$

Try to remove B , $\{C, G, I, J\}^+ = \{A, C, E, G, H, I, J\}$

Thus, B cannot be removed.

Try to remove C , $\{B, G, I, J\}^+ = \{B, G, I, J\}$

Thus, C cannot be removed.

Try to remove G , $\{B, C, I, J\}^+ = \{A, B, C, D, E, G, H, I, J\}$

Thus, $X := \{B, C, I, J\}$

Try to remove I , $\{B, C, J\}^+ = \{B, C, G, J\}$

Thus, I cannot be removed.

Try to remove J , $\{B, C, I\}^+ = \{A, B, C, D, E, G, H, J\}$

Thus, $X := \{B, C, I\}$

So $\{B, C, I\}$ is a candidate key and add to T .

Cannot find other super keys that do not contain any candidate key in T .

So candidate keys are $\{B, H, I\}$, $\{B, C, I\}$.

3. 1NF since it only contains atomic attribute values.
Not in 2NF since $CI \rightarrow A$ violates 2NF, the non-prime attribute A is partially dependent on key {B,C,I}.

4. Step 1. Reduce right, F is converted to
 $F1 = \{AB \rightarrow D, AB \rightarrow E, BC \rightarrow G, CDE \rightarrow H, CDE \rightarrow J, H \rightarrow A, H \rightarrow C, CI \rightarrow E, CI \rightarrow G, CI \rightarrow H, DHI \rightarrow E, DHI \rightarrow J\}$
 Step 2. Reduce Left. F1 is converted to ($DHI \rightarrow E$ is reduced to $HI \rightarrow E$)
 $F2 = \{AB \rightarrow D, AB \rightarrow E, BC \rightarrow G, CDE \rightarrow H, CDE \rightarrow J, H \rightarrow A, H \rightarrow C, CI \rightarrow E, CI \rightarrow G, CI \rightarrow H, HI \rightarrow E, DHI \rightarrow J\}$
 Step3. Remove redundancy, F2 is converted to (remove redundancy: $CI \rightarrow E, DHI \rightarrow J$)

Thus, $F_{min} = \{AB \rightarrow D, AB \rightarrow E, BC \rightarrow G, CDE \rightarrow H, CDE \rightarrow J, H \rightarrow A, H \rightarrow C, CI \rightarrow G, CI \rightarrow H, HI \rightarrow E\}$

Or $F_{min} = \{AB \rightarrow DE, BC \rightarrow G, CDE \rightarrow HJ, H \rightarrow AC, CI \rightarrow GH, HI \rightarrow E\}$

5. Not lossless since there's no row contains "a" entirely.

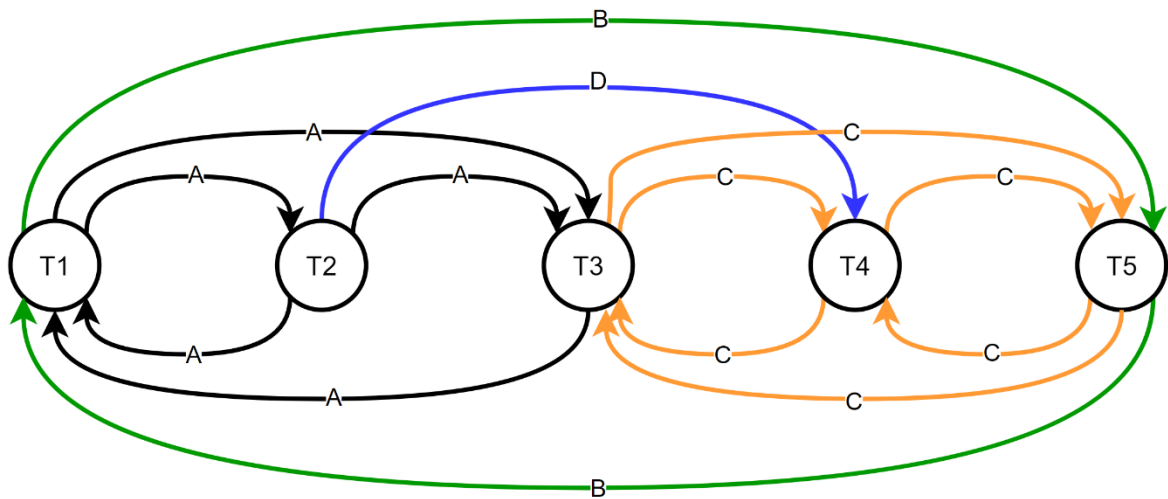
	A	B	C	D	E	G	H	I	J
R1	a	a	b	b	a	b	a	b	b
R2	b	b	a	a	b	b	a	a	a
R3	b	a	b	b	b	a	a	b	a
	A	B	C	D	E	G	H	I	J
R1	a	a	a	b	a	a	a	b	b
R2	a	b	a	a	b	b	a	a	a
R3	a	a	a	b	a	a	a	b	a

6. R violates BCNF because of $AB \rightarrow DE$, decompose R into $R1(A,B,D,E)$, $R2(A,B,C,G,H,I,J)$.
 $R2$ violates BCNF because of $BC \rightarrow G$, decompose $R2$ into $R21(B,C,G)$, $R22(A,B,C,H,I,J)$.
 $R22$ violates BCNF because of $H \rightarrow AC$, decompose $R22$ into $R221(H,A,C)$, $R222(B,H,I,J)$.
 $R222$ violates BCNF because of $BH \rightarrow J$, since $BH \rightarrow BAC \rightarrow DEC \rightarrow J$, decompose $R222$ into $R2221(B,H,J)$, $R2222(B,H,I)$.

R can be decomposed into $R1(A,B,D,E)$, $R21(B,C,G)$, $R221(H,A,C)$, $R2221(B,H,J)$ and $R2222(B,H,I)$.

Question 2:

1. T1, T5: Redo
T3, T4: Undo
T2: Do Nothing
2. The transaction schedule is not conflict serializable because its precedence graphs is not acyclic



3. T1 waits T5 for B, T5 waits for T3 for C, T3 waits T1 for A.

T1	WL(A)	R(A)	...				WL(B)	R(B)	W(B)	W(A)	...			UL(A)	UL(B)				
T2	...																		
T3			WL(C)	R(C)	...				WL(A)	R(A)	W(C)	W(A)	...			UL(C)	UL(A)		
T4	...																		
T5					WL(B)	W(B)	...				WL(C)	R(C)	W(C)	...				UL(B)	UL(C)

Question 3:

1.

LRU													
QUERY	Initial	1	3	3	2	3	4	5	2	1	5	2	6
Buffer 1	N	1	1	1	1	1	4	4	4	1	1	1	6
Buffer 2	N	N	3	3	3	3	3	3	2	2	2	2	2
Buffer 3	N	N	N	N	2	2	2	5	5	5	5	5	5
Page Fault:		F	F		F		F	F	F	F			F
Hit:				H		H					H	H	
Number of Page Fault:		8											

2.

MRU													
QUERY	Initial	1	3	3	2	3	4	5	2	1	5	2	6
Buffer 1	N	1	1	1	1	1	1	1	1	1	1	1	1
Buffer 2	N	N	3	3	3	3	4	5	5	5	5	5	5
Buffer 3	N	N	N	N	2	2	2	2	2	2	2	2	6
Page Fault:		F	F		F		F	F					F
Hit:				H		H			H	H	H	H	
Number of Page Fault:		6											

3.

FIFO													
QUERY	Initial	1	3	3	2	3	4	5	2	1	5	2	6
Buffer 1	N	1	1	1	1	1	4	4	4	4	4	2	2
Buffer 2	N	N	3	3	3	3	3	5	5	5	5	5	6
Buffer 3	N	N	N	N	2	2	2	2	2	1	1	1	1
Page Fault:		F	F		F		F	F		F		F	F
Hit:				H		H			H		H		
Number of Page Fault:		8											

4. MRU performs the best in the given query because it has the least number of page faults.