

# Alchemical Free Energy Methods with BioSimSpace

Julien Michel, Anna Herz, Finlay Clark, Lester Hedges, Christopher Woods

CCPBioSim Training Week – Leeds - 20/09/2022



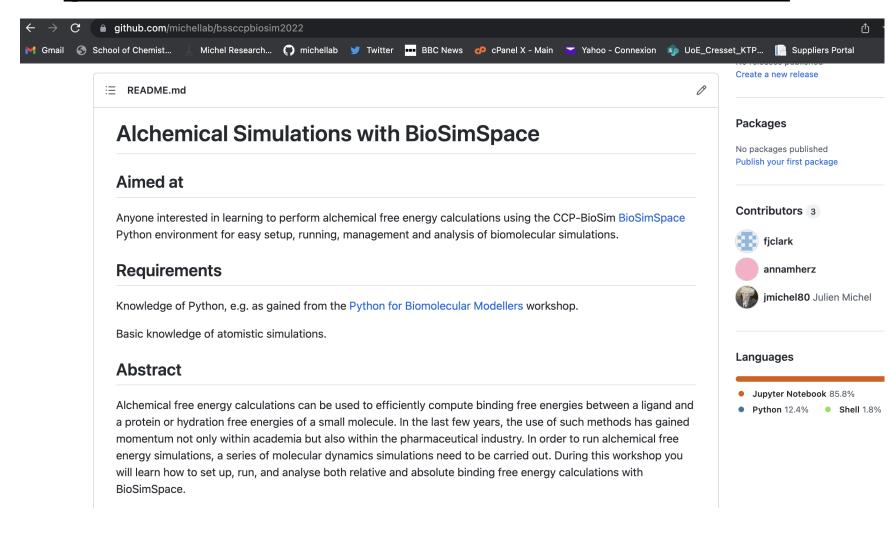
#### Schedule

- 9.00 9.30 Set up & Lecture
- 9.30 10.15 Introduction to Alchemistry with BioSimSpace
- 10.15 10.30 Coffee Break
- 10.30 11.15 Relative Binding Free Energies with BioSimSpace
- 11.15 12.00 Absolute Binding Free Energies with BioSimSpace



#### Workshop materials

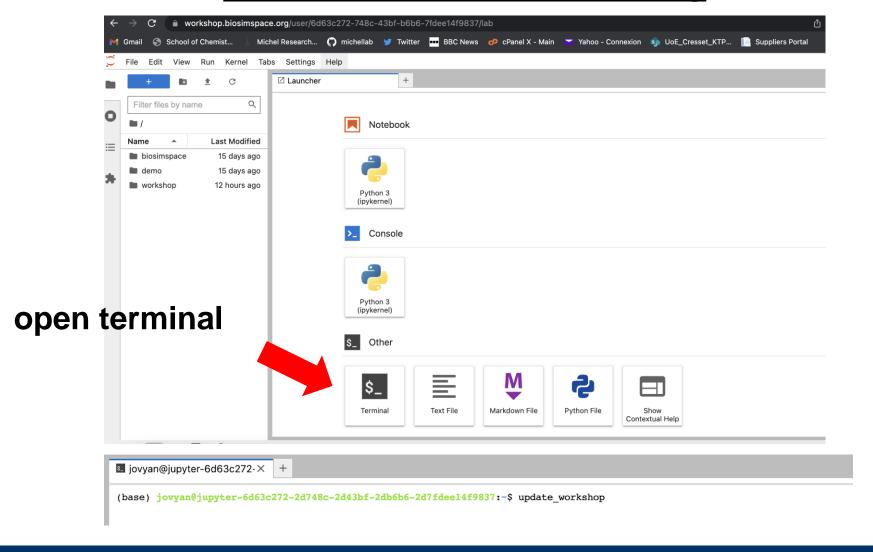
#### github.com/michellab/bssccpbiosim2022





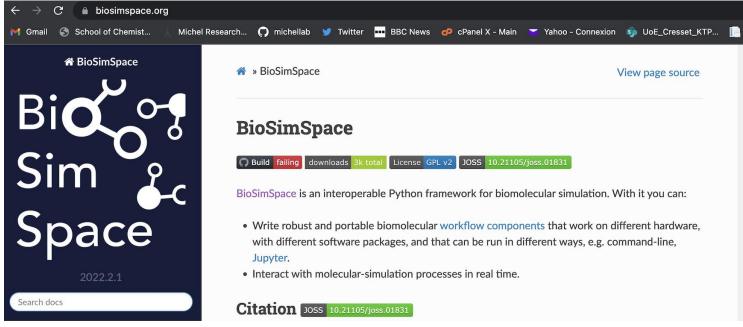
#### Accessing the workshop server

#### workshop.biosimspace.org





#### What is BioSimSpace?



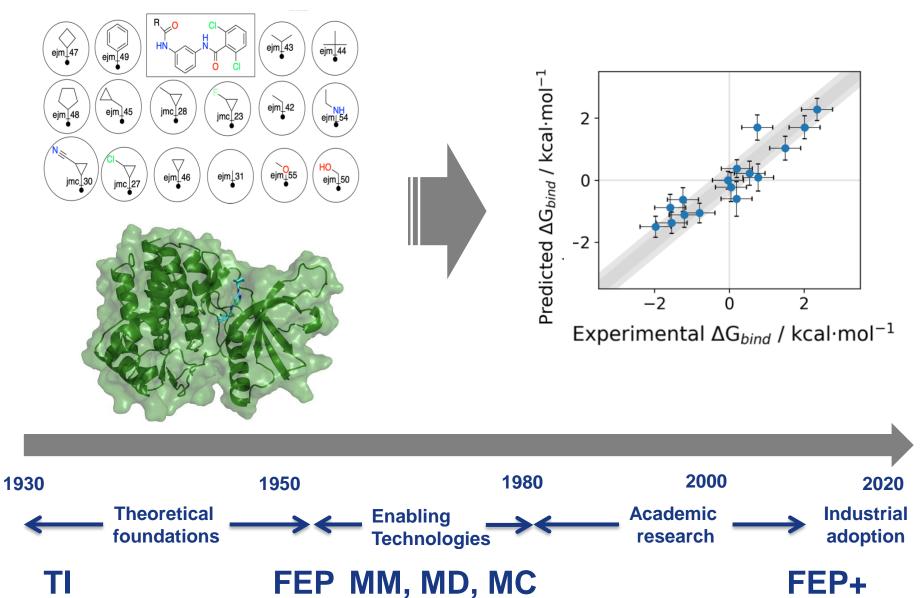


BioSimSpace: An interoperable Python framework for biomolecular simulation

Lester O. Hedges<sup>1</sup>, Antonia S.J.S. Mey<sup>2</sup>, Charles A. Laughton<sup>3</sup>, Francesco L. Gervasio<sup>4</sup>, Adrian J. Mulholland<sup>5</sup>, Christopher J. Woods<sup>1</sup>, and Julien Michel<sup>2</sup>

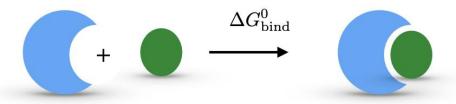


## Alchemical free energy methods in drug design

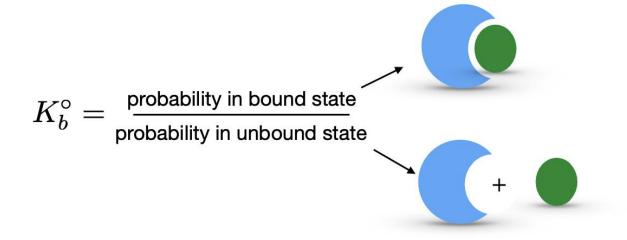




## Free energy of binding



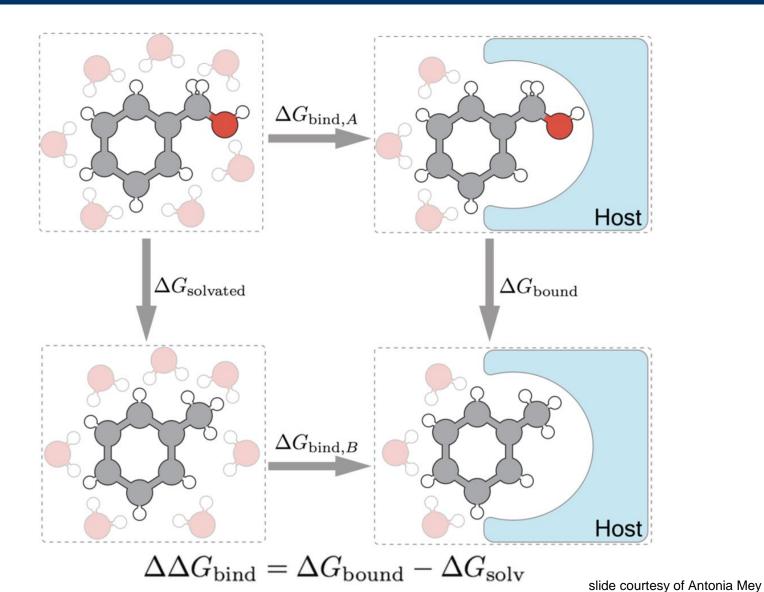
$$\Delta G_{\mathrm{bind}}^{\circ} = -k_B T \ln K_b^{\circ}$$



Sample this using Molecular dynamics?

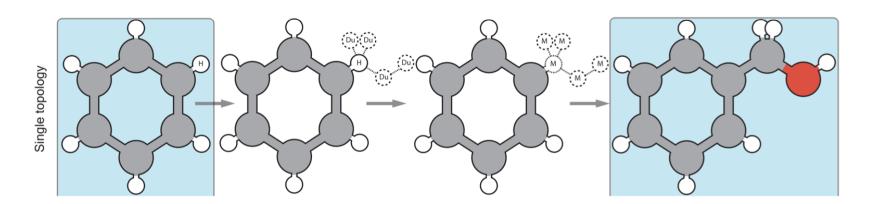


# The alchemical pathway





#### The lambda coordinate



**Endpoint 1** 

 $\lambda = 0$ 

 $\lambda = 0.5$ 

Endpoint 2

$$U(\lambda, \mathbf{x}) = (1 - \lambda)U_0(\mathbf{x}) + \lambda U_1(\mathbf{x}) + U_{\text{unaffected}}$$



#### Potential energy functions

$$\begin{split} U &= \sum_{\text{bonds}} \frac{1}{2} k_b (r - r_0)^2 + \sum_{\text{angles}} \frac{1}{2} k_a (\theta - \theta_0)^2 + \sum_{\text{torsions}} \frac{V_n}{2} [1 + \cos(n\phi - \delta)] \\ &+ \sum_{\text{improper}} V_{imp} + \sum_{\text{LJ}} 4\epsilon_{ij} \left( \frac{\sigma_{ij}^{12}}{r_{ij}^{12}} - \frac{\sigma_{ij}^6}{r_{ij}^6} \right) + \sum_{\text{elec}} \frac{q_i q_j}{r_{ij}}, \end{split}$$

- The functional form and parameter set define a force field.
- Commonly used force fields include:
   CHARMM (Chemistry at Harvard Molecular Mechanics)
   AMBER (Assisted Model Building with Energy Refinement)
   OPLS (Optimised Potentials for Liquid Simulations)

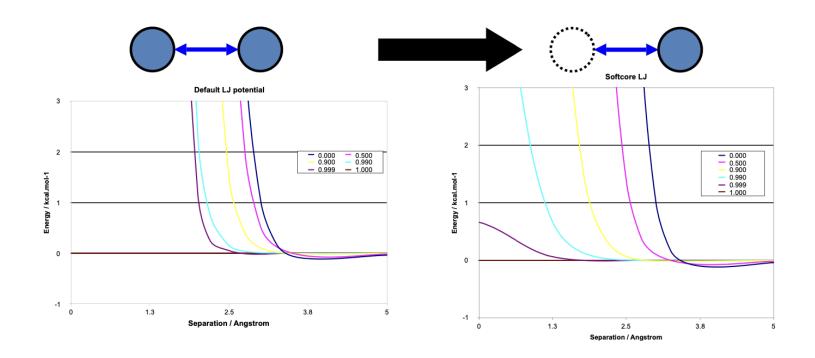


#### Softcore potentials

Zacharias et al. *J. Chem. Phys.* 100, 9025-, **1994** 

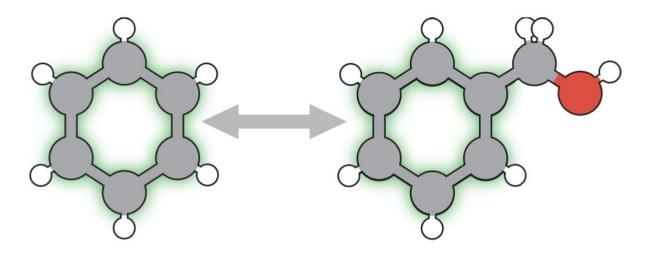
$$V_{\rm LJ} = (1 - \lambda) \left[ \frac{A}{(r^2 + \delta \lambda)^6} - \frac{B}{(r^2 + \delta \lambda)^3} \right]$$

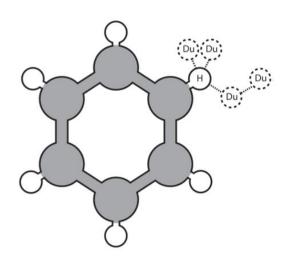
#### Dummy atoms!





# BioSimSpace merged molecules

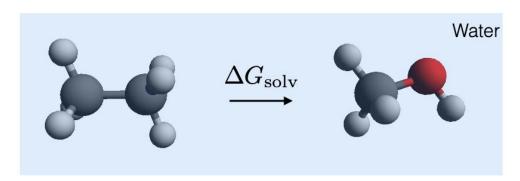


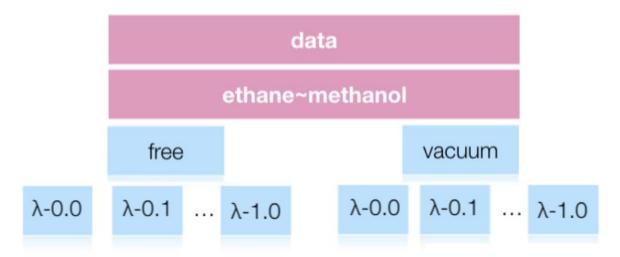


BioSimSpace holds a merged molecule and can write intermediates



# BioSimSpace setups inputs for different simulation engines





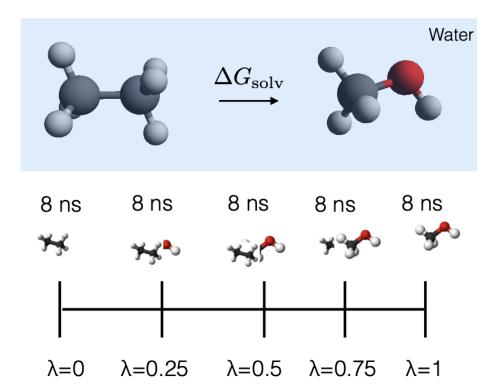


**AMBER** MD





#### BioSimSpace analyses simulation outputs

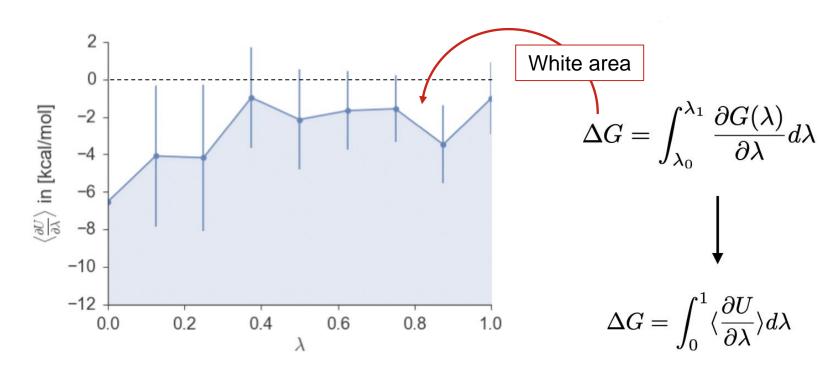


#### **Zwanzig equation**

$$\Delta G_{AB} = G(A) - G(B) = -k_B T \ln \langle \exp(-\frac{U_B - U_A}{k_B T}) \rangle_A$$



#### Thermodynamic integration



The integral represents the area under the curve.

There are different ways in which one can numerically integrate.

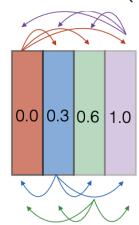


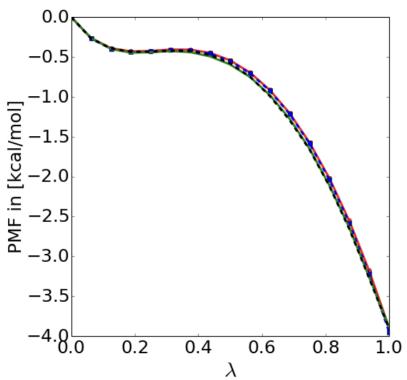
#### Multistate Bennett Acceptance Ratio (MBAR)

$$e^{-f_i} = \sum_{n=1}^{N} \frac{e^{-u_i(\vec{x}_n)}}{\sum_k N_k e^{f_k - u_k(\vec{x}_n)}}$$

The free energy is correct up to an additive constant, which will cancel out when evaluating free energy differences.

$$\Delta G_{AB} = G(\lambda_1) - G(\lambda_0)$$

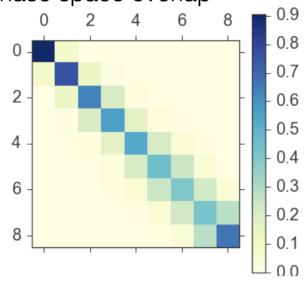






#### Overlap matrix

Overlap matrix estimates the phase space overlap



Define a weight matrix W containing the weight of each sample x<sub>n</sub>.

$$W_{n,i}(x_n) = rac{e^{eta G_i - eta U_i(x_n)}}{\sum_{k=1}^K N_k e^{eta G_k - eta U_k(x_n)}}$$
Probability of  $p_i(x_n)$  of  $x_n$  occurring

at lambda window i.

$$O = W^TWN$$

**N** is a diagonal matrix with the number of samples collected at each lambda window.



#### Let's get started

