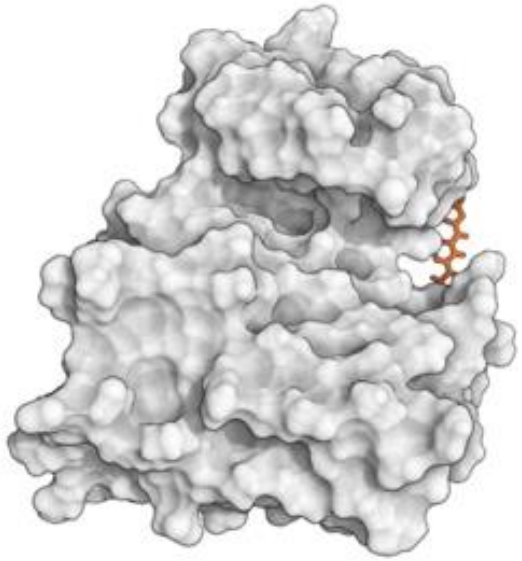
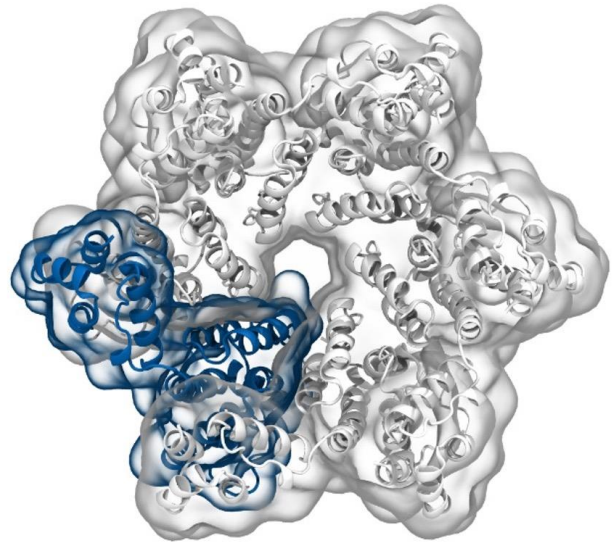
Simulation of Biomolecules



Markov State Modelling



2023 CCP5 Summer School

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Markov State Modelling (MSM)

Can we predict the equilibrium structure of a peptide?

Run 5 μs molecular dynamics simulation

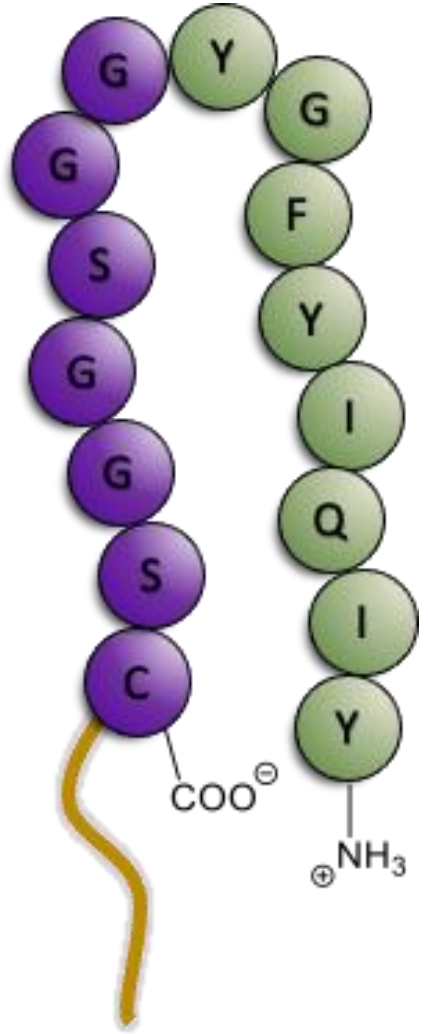
↓

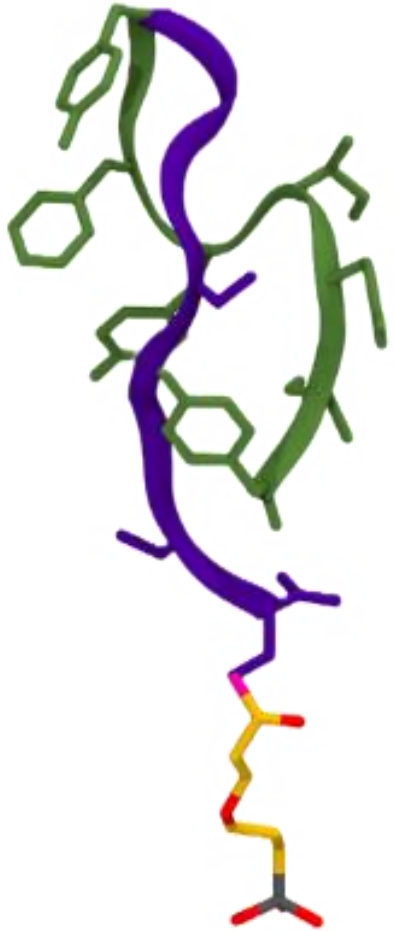
Use a Markov Model to identify dominant conformations in solution

↓

Report most stable structure

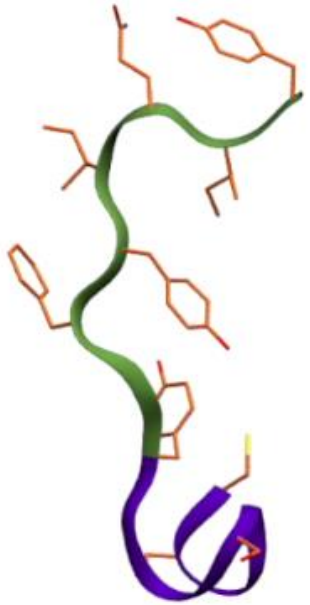
AlphaFold suggestion





MSMs allow for quantitive data from molecular simulations

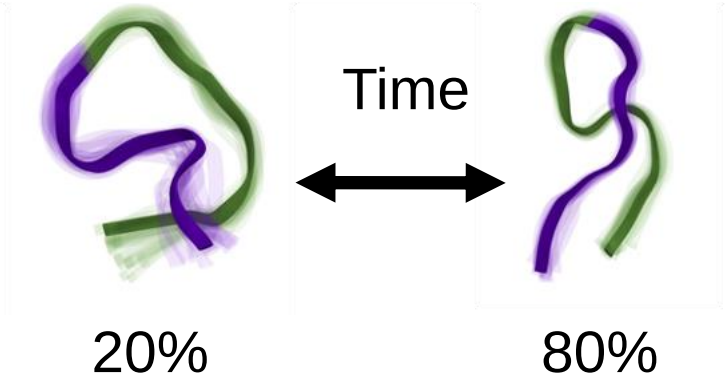
YITIY TAYAG SGGSC



Protein dynamics

Clustering is the first step towards a model providing quantitive equilibrium and kinetic information from the simulation

Simulation movie

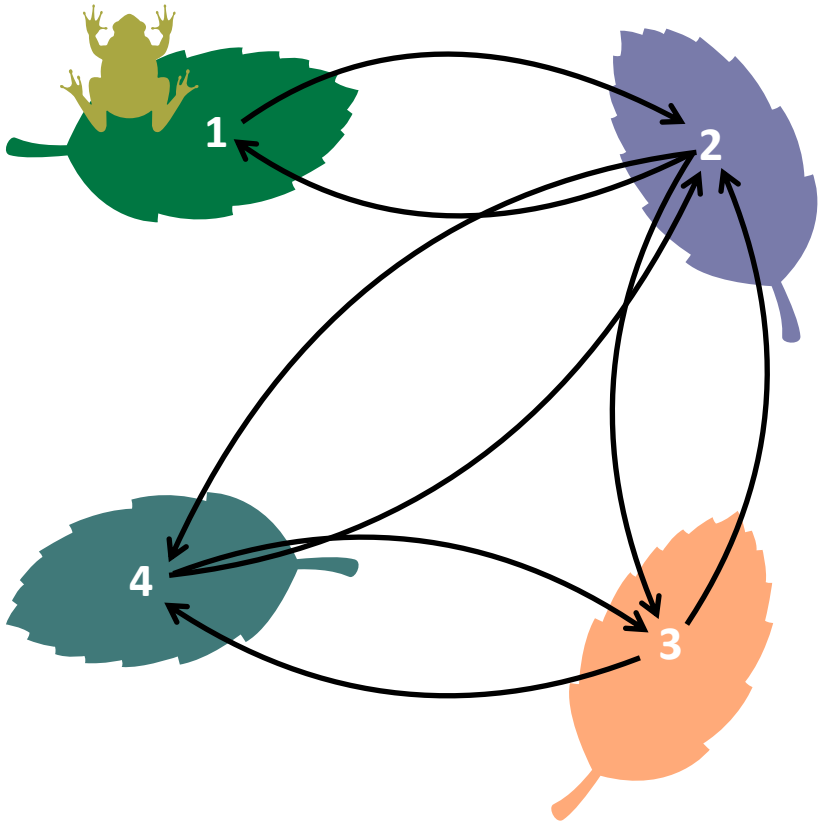


Probabilistic understanding of the trajectory

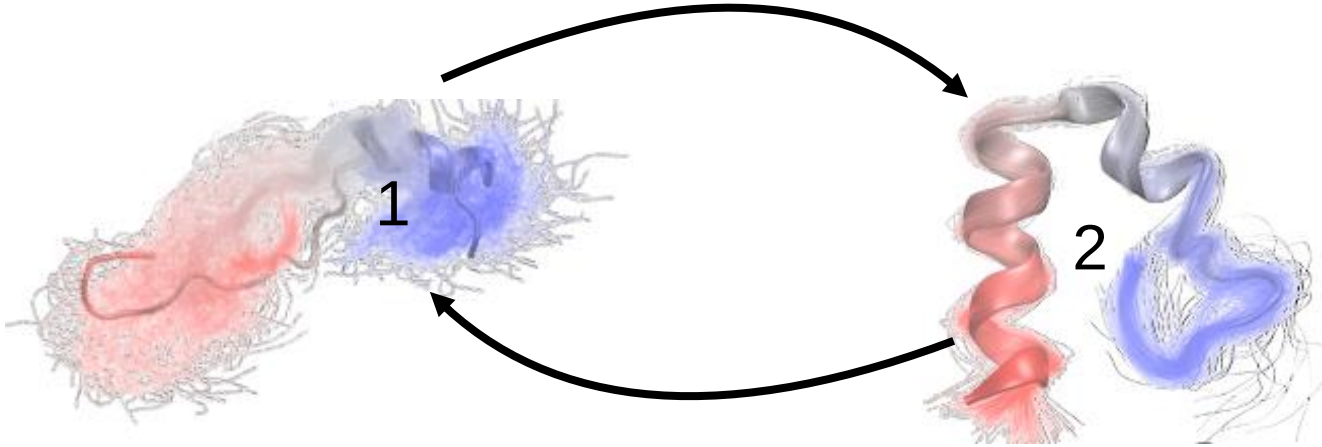
[…] Ryan Zhu, A. Mey […], ***Viruses***, 2023

Frogs jumping and proteins moving

Over the period of a day:

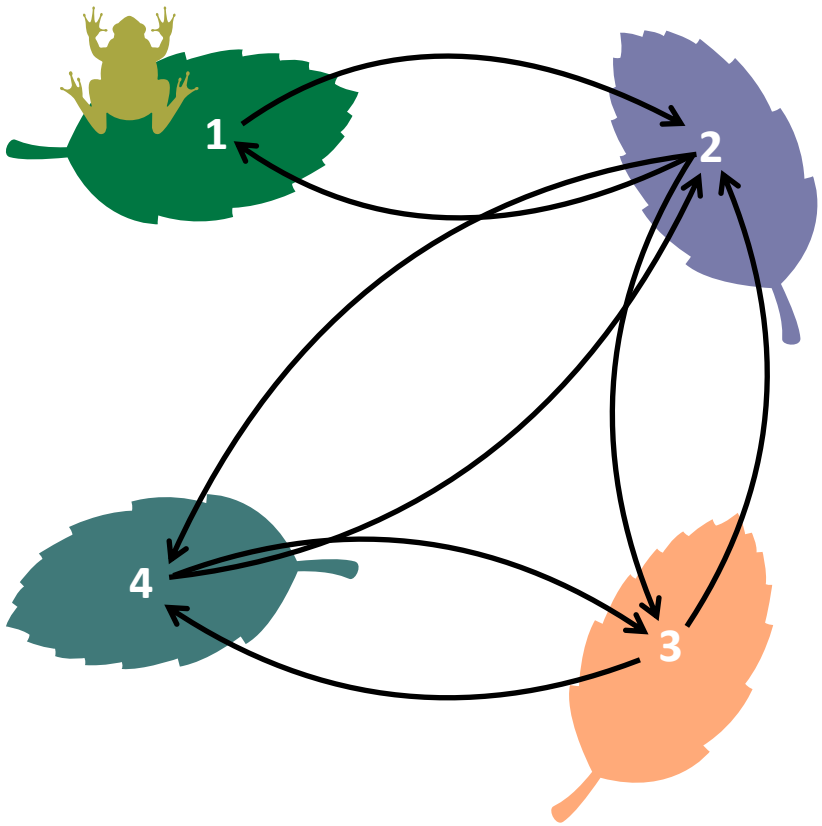


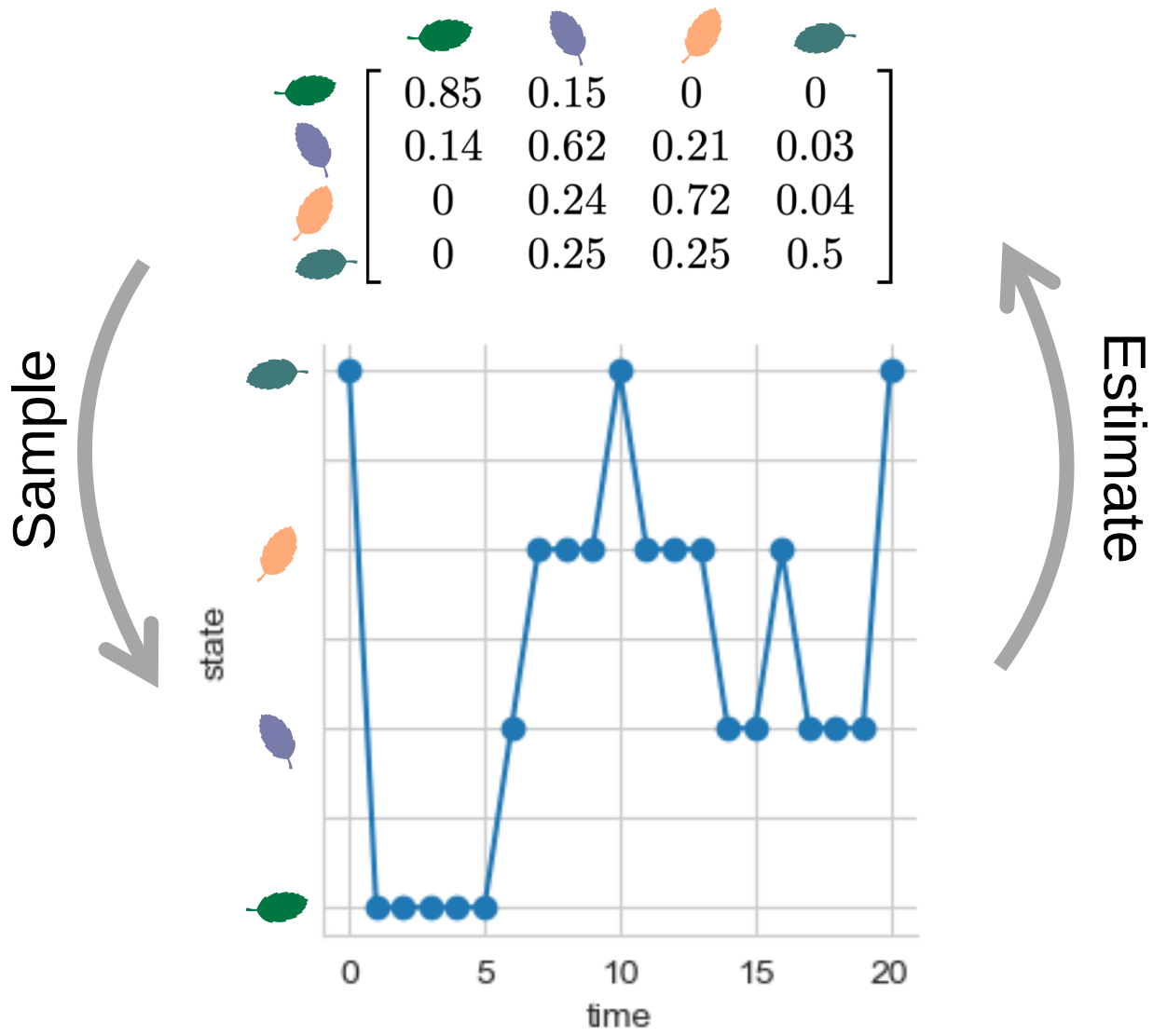
What do a protein and a frog jumping have in common?



What is a Markov chain?

Over the period of a day:





What is a Markov chain?

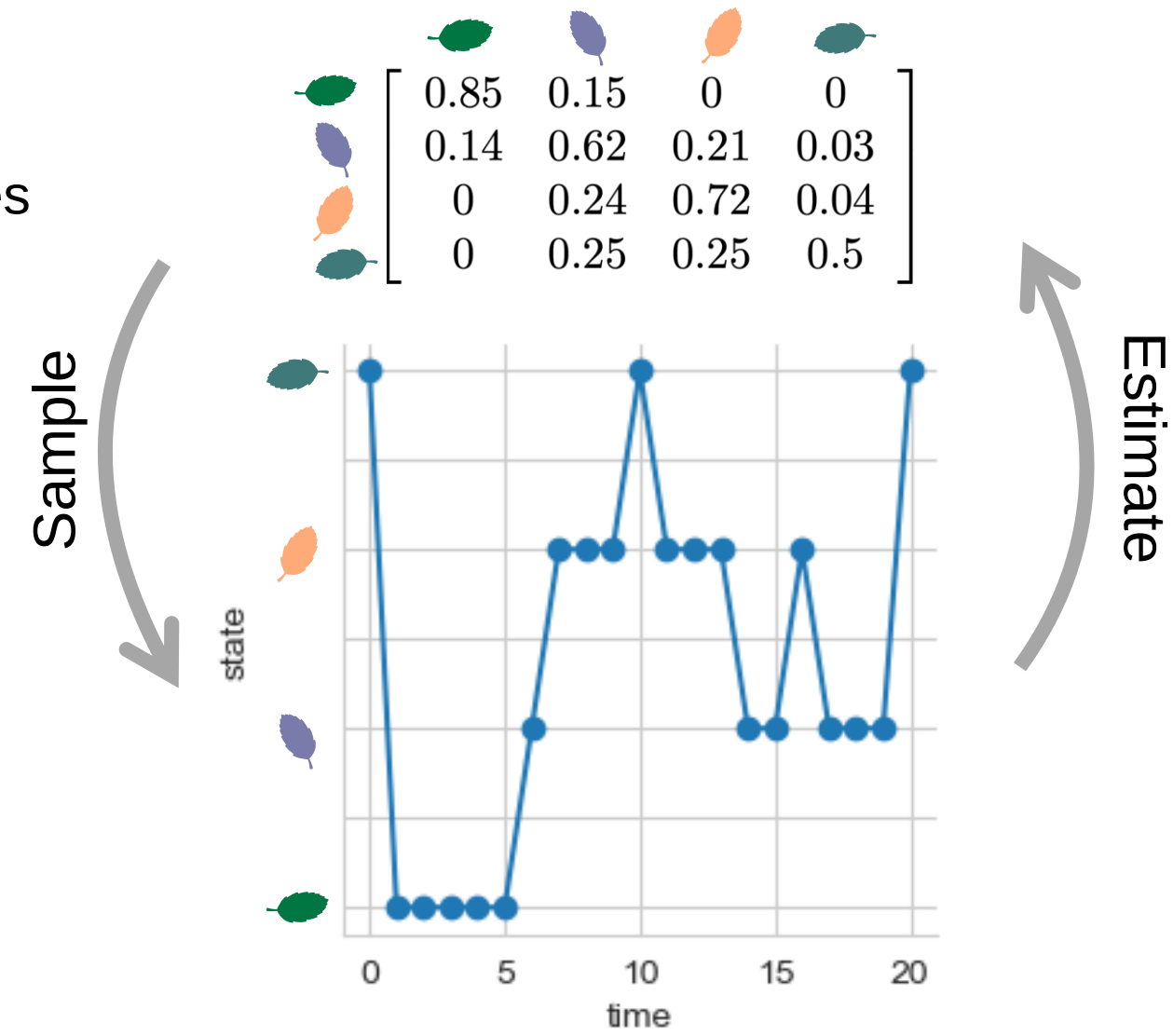
Transition matrices are:
- Stochastic matrices
- Containing conditional jump probabilities

If they are **irreducible** and **ergodic**:
- They have a stationary probability
- Has a stationary probability **π.**
- The stationary probability is the eigenvector of the eigenvalue λ_1

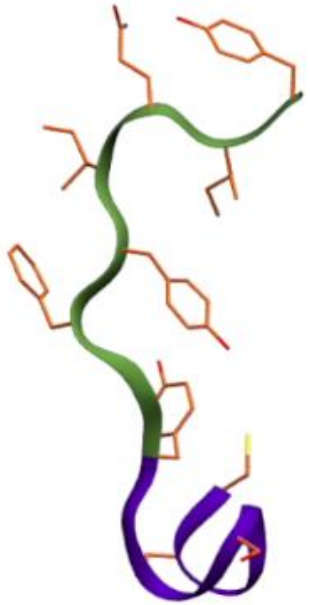
$$\lambda_1 = 1 > \lambda_2 > \lambda_3, \ldots, > \lambda_n$$

If they are reversible

$$\pi_i P_{ij} = \pi_j P_{ji}$$



How to model protein dynamics using a Markov approach?

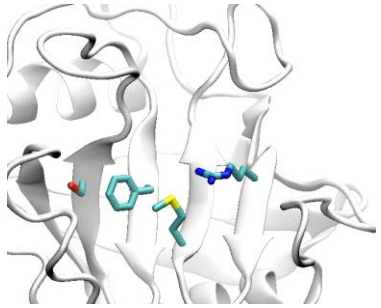


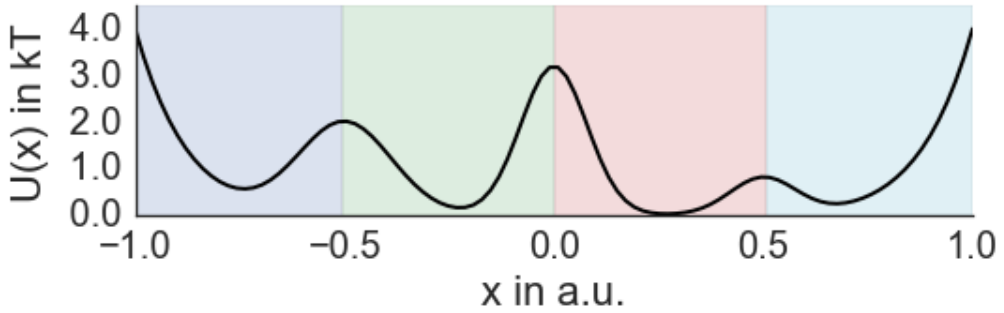
?

Approximate with a transition matrix from the trajectory:

$$P = \begin{bmatrix} P_{1,1} & P_{1,2} & \dots & P_{1,j} & \dots & P_{1,S} \\ P_{2,1} & P_{2,2} & \dots & P_{2,j} & \dots & P_{2,S} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ P_{i,1} & P_{i,2} & \dots & P_{i,j} & \dots & P_{i,S} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ P_{S,1} & P_{S,2} & \dots & P_{S,j} & \dots & P_{S,S} \end{bmatrix}.$$

Building a Markov Model requires several steps





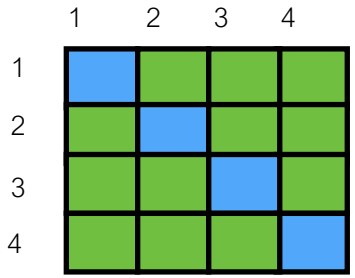
MD data

Featurization (select features)

Dimensionality Reduction (tICA)

Discretization (k-means)

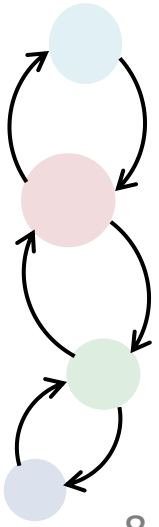
Discrete Trajectories



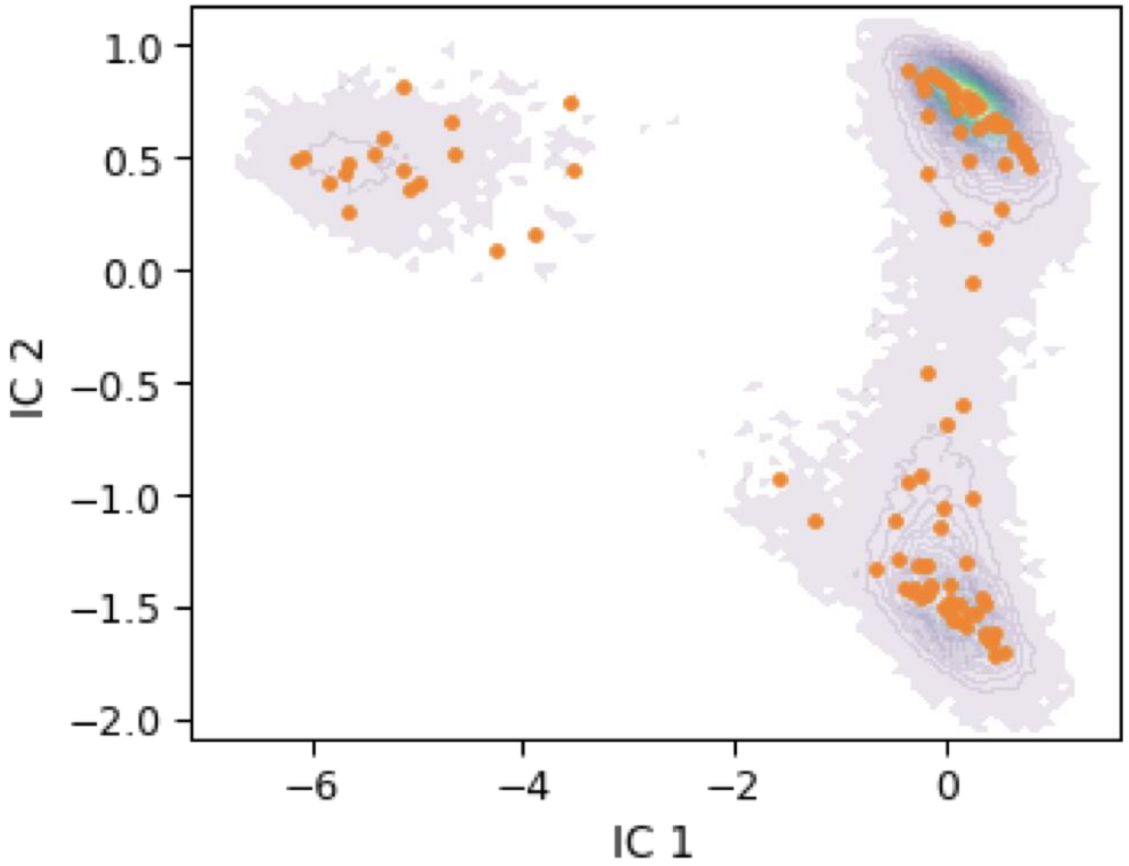
MSM estimation (MLE)

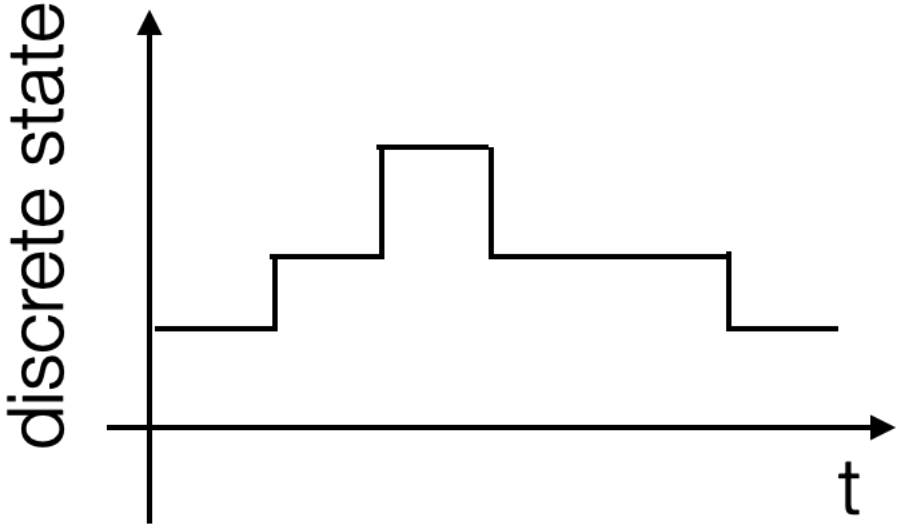
MSM validation (ITS convergence & CK test)

MSM



Clustering on reduced dimensional space





k-means

regular
spatial

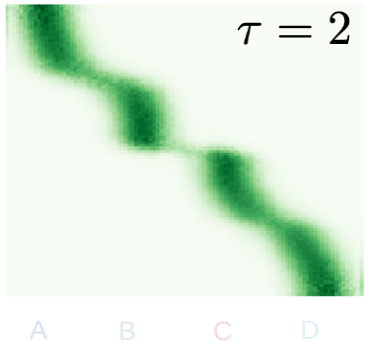
etc.

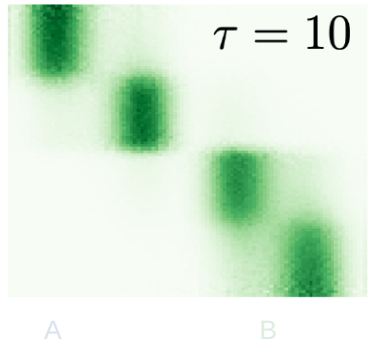
Dimensionality reduction and discretisation require a lot of parameter optimisation. It is necessary to spend a good amount of time on hyper parameter optimisation.

The transition matrix contains all quantative properties

Approximate with a transition matrix from the trajectory:

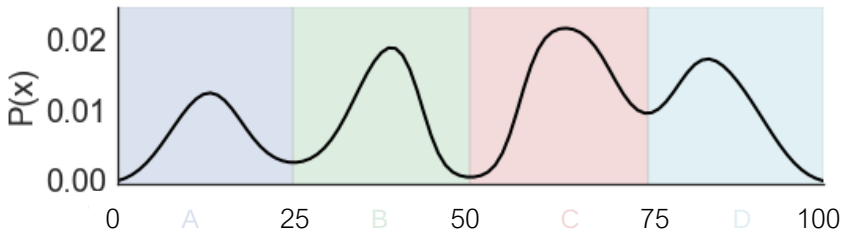
$$P = \begin{bmatrix} P_{1,1} & P_{1,2} & \dots & P_{1,j} & \dots & P_{1,S} \\ P_{2,1} & P_{2,2} & \dots & P_{2,j} & \dots & P_{2,S} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ P_{i,1} & P_{i,2} & \dots & P_{i,j} & \dots & P_{i,S} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ P_{S,1} & P_{S,2} & \dots & P_{S,j} & \dots & P_{S,S} \end{bmatrix}.$$

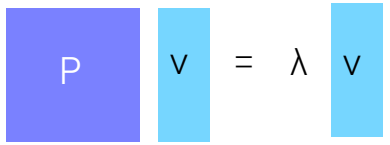




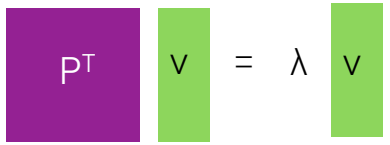
varying the lag time

$$\lambda_1 = 1 > \lambda_2 > \lambda_3, \dots, > \lambda_n$$





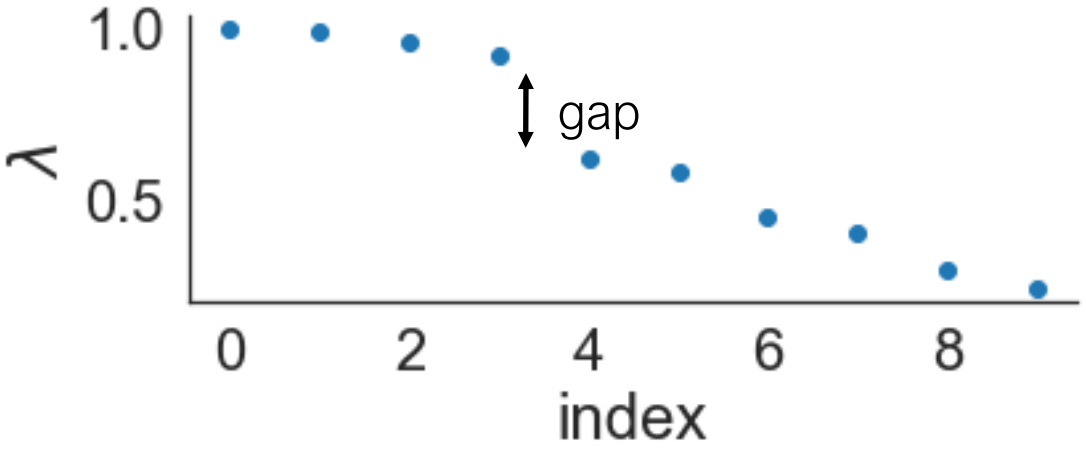
right eigenvector



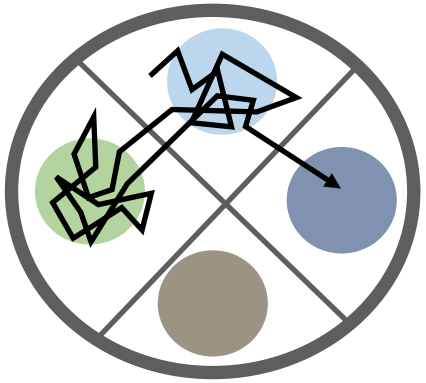
left eigenvector

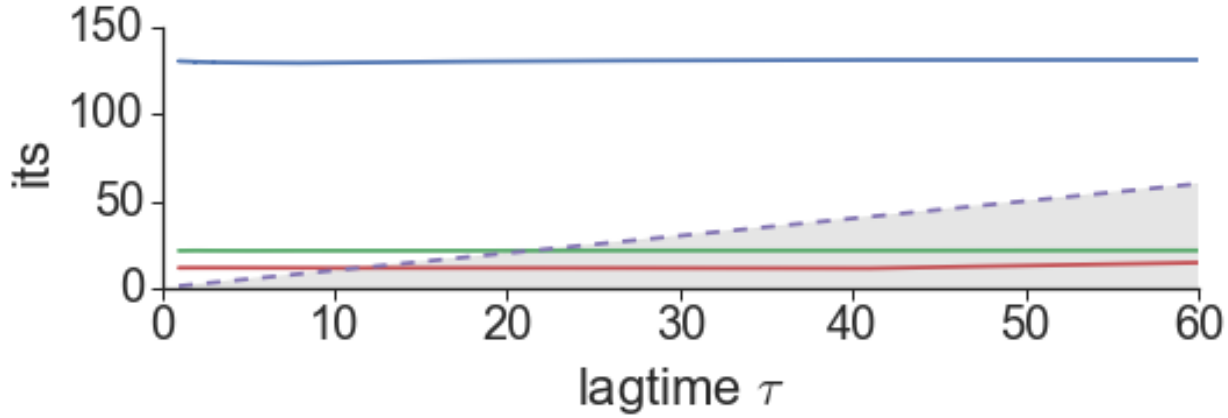
We can find the most likely structure/coordinates!

Eigenvalues tell us about timescales



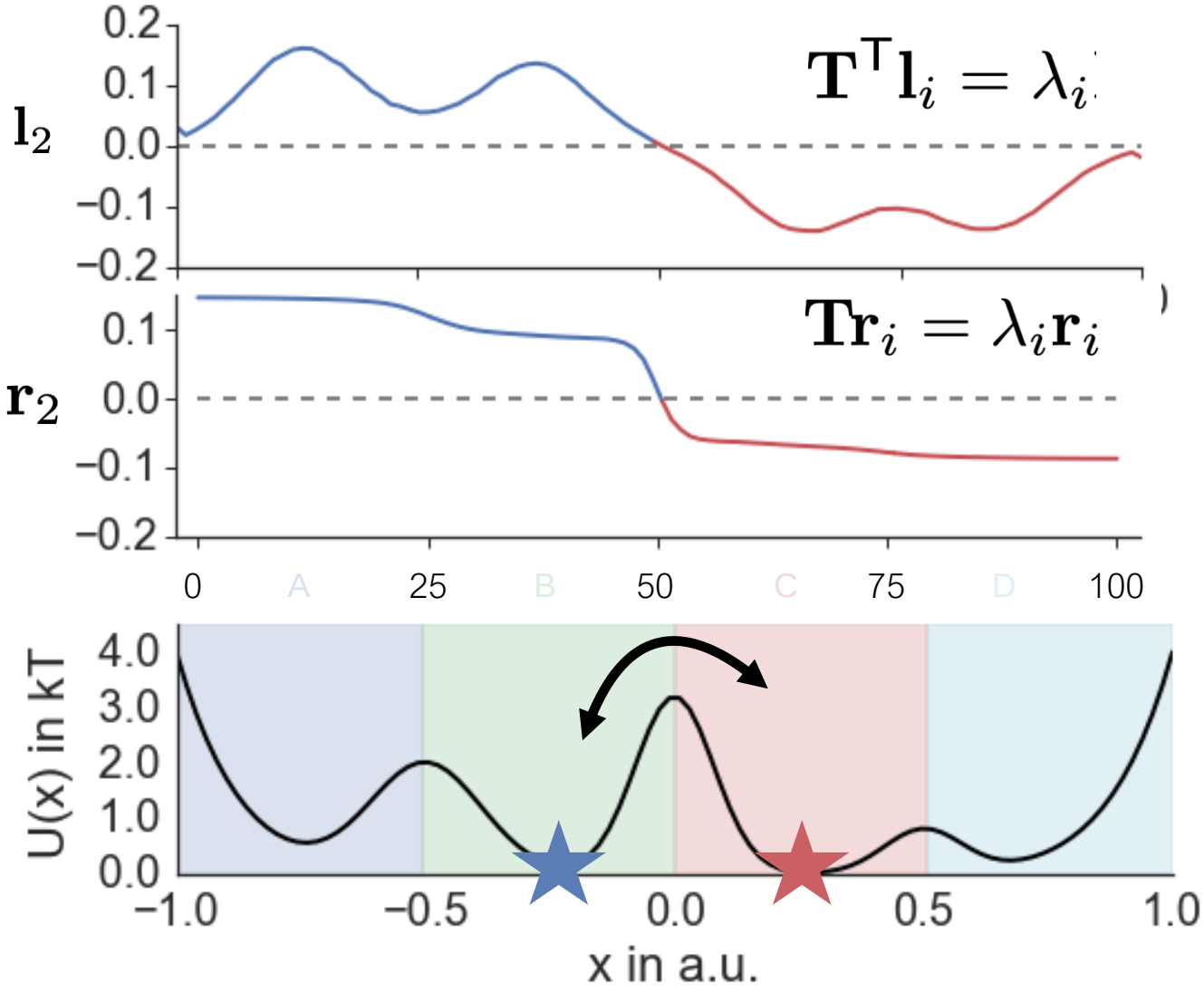
$$\lambda_1 = 1 > \lambda_2 > \lambda_3, \ldots, > \lambda_n$$





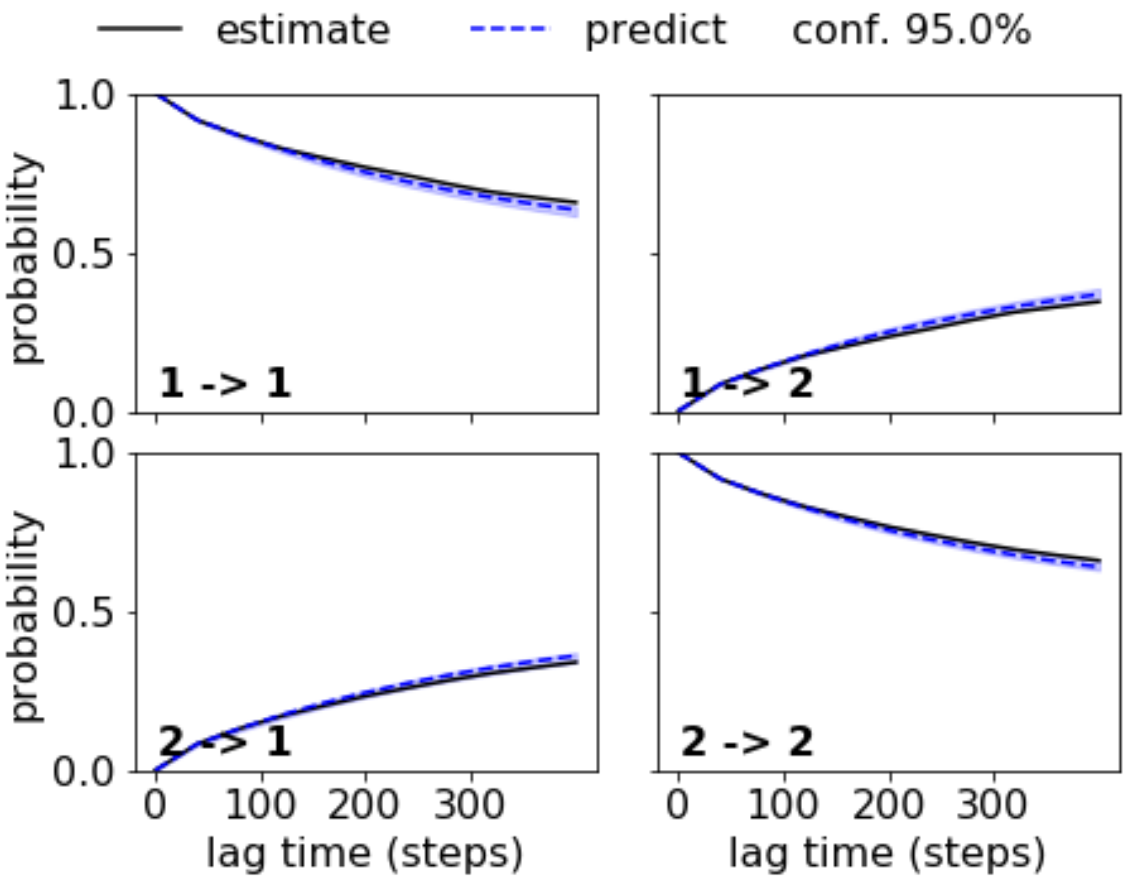
$$t_i = -\frac{\tau}{\ln|\lambda_i|}$$

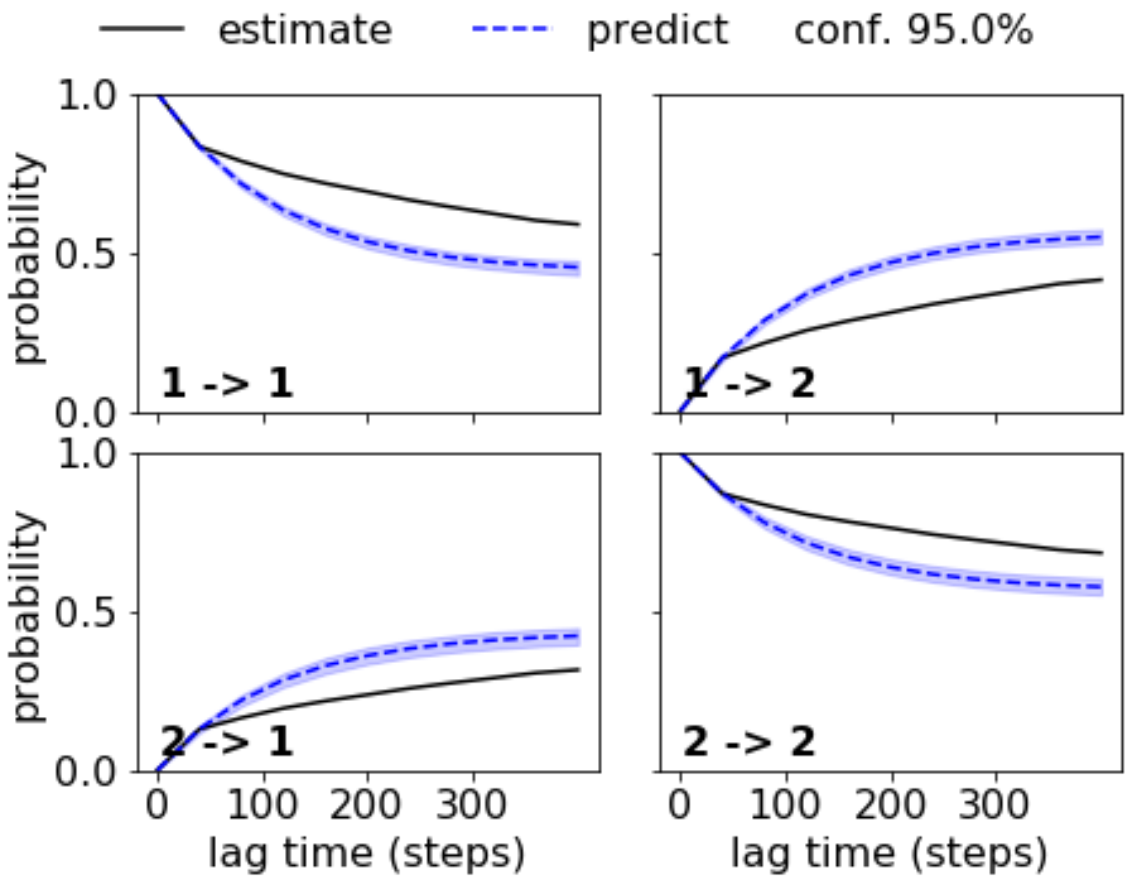
The eigenvectors tell us about the slowest processes



Validation with the Chapman-Kolmogorov (CK) test

$$T(k\tau) = T(\tau)^k$$





Conformational dynamics of a peptide

Can we predict the equilibrium structure of a peptide?

Run 5 μs molecular dynamics simulation

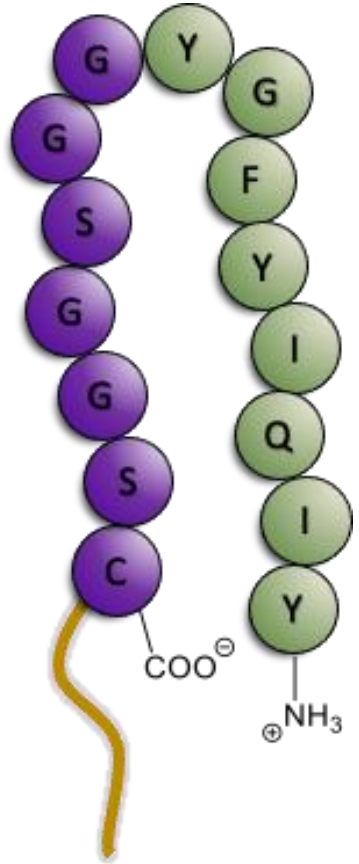
↓

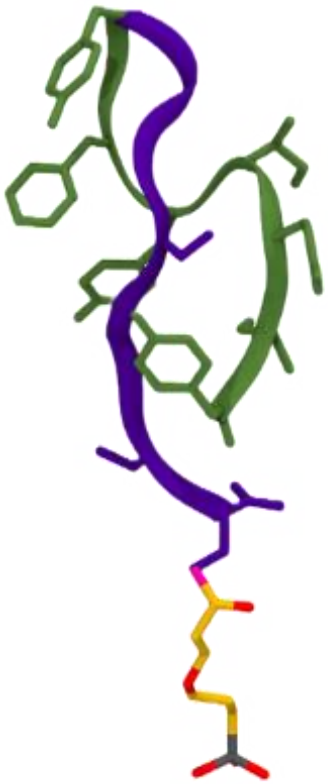
Use a Markov Model to identify dominant conformations in solution

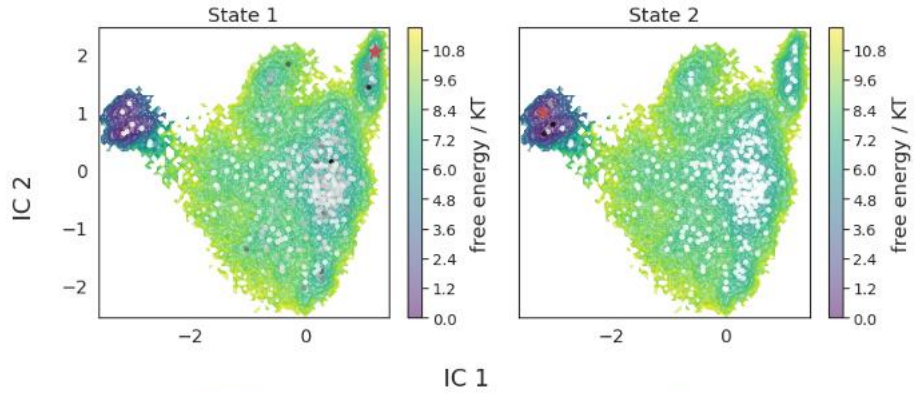
↓

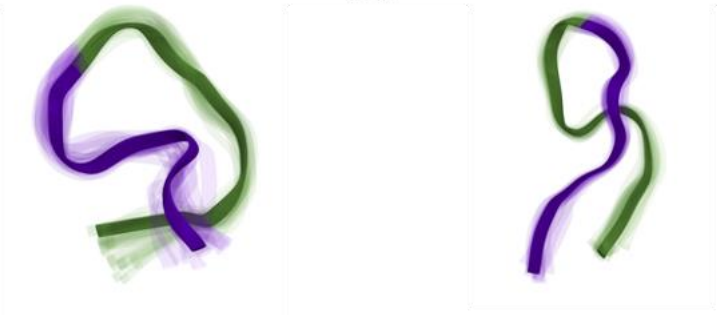
Report most stable structure

AlphaFold suggestion







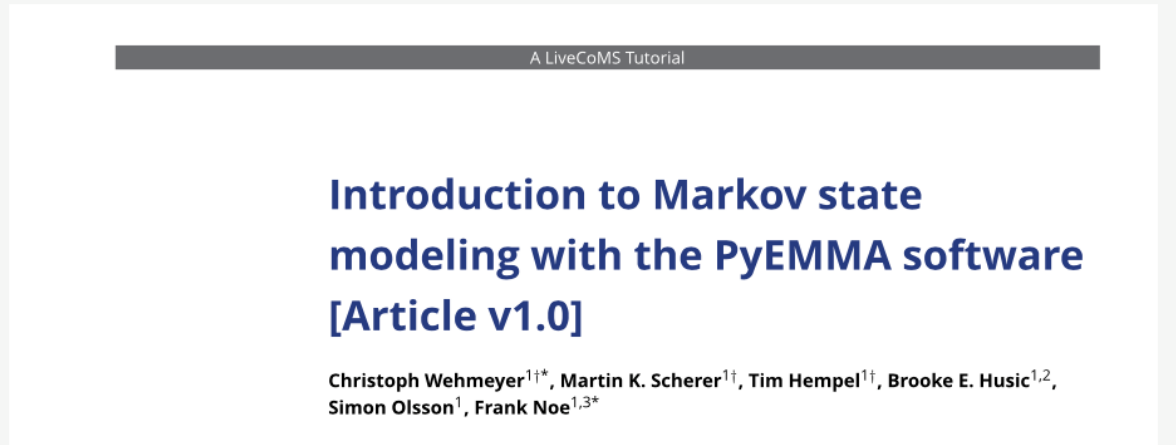


20%

80%

Python tools are available for building MSMs

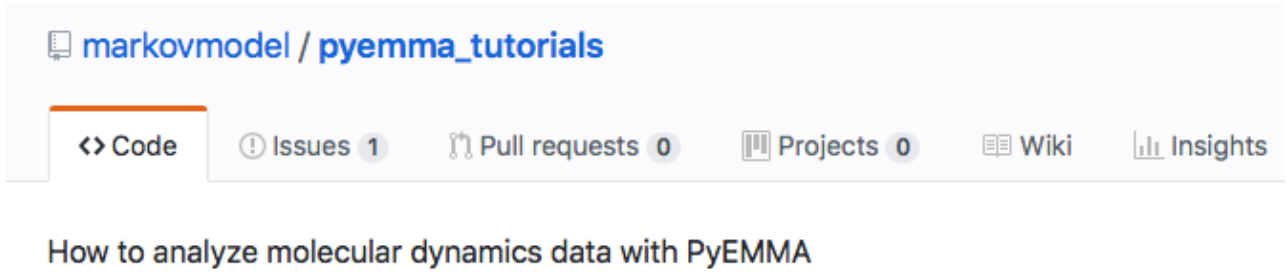
https://www.livecomsjournal.org


A LiveCoMS Tutorial

Introduction to Markov state modeling with the PyEMMA software [Article v1.0]

Christoph Wehmeyer[1†*], Martin K. Scherer[1†], Tim Hempel[1†], Brooke E. Husic[1,2], Simon Olsson[1], Frank Noe[1,3*]

https://github.com/markovmodel/pyemma_tutorials



https://github.com/deeptime-ml/deeptime