## Supporting Information for: MolSym: A Python Package for Handling Symmetry in Molecular Quantum Chemistry

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## Irreducible Representation Matrices

Define  $\varepsilon$  accordingly.

$$\varepsilon_n = e^{\frac{2\pi i}{n}} \tag{1}$$

$$\begin{array}{c|c} \mathbf{C1} & \hat{E} \\ \hline A & 1 \end{array}$$

$$\begin{array}{c|c|c} \mathbf{Cs} & \hat{E} & \hat{\sigma}_h \\ \hline A' & 1 & 1 \\ A'' & 1 & -1 \end{array}$$

$$\begin{array}{c|cc} \mathbf{Ci} & \hat{E} & \hat{i} \\ \hline Ag & 1 & 1 \\ Au & 1 & -1 \\ \end{array}$$

$$\begin{array}{c|c|c} \mathbf{C2} & \hat{E} & \hat{C}_2 \\ \hline A & 1 & 1 \\ B & 1 & -1 \\ \end{array}$$

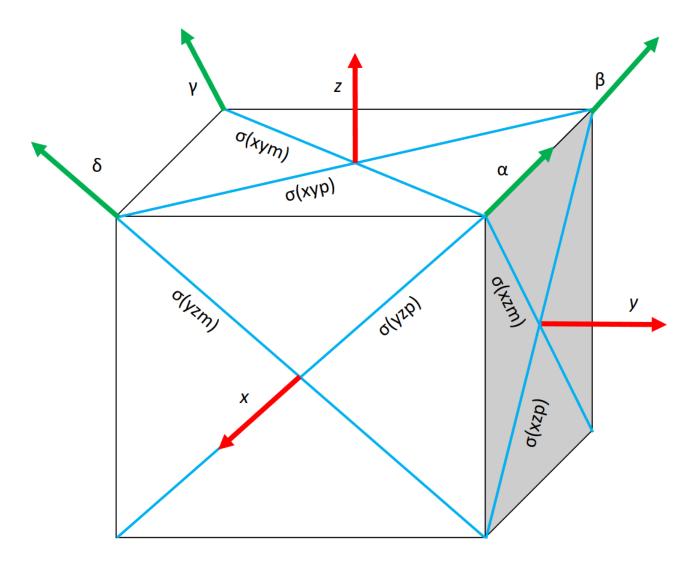


Figure 1: Definitions of vectors  $x,y,z,\ \alpha,\beta,\gamma,\delta$  (typically  $\hat{C}_3$  axes), and reflection planes  $\sigma xyp,\sigma xym,\sigma xzp,\sigma xzm,\sigma yzp,\sigma yzm$ .  $\hat{C}_2$  opertaions with xyp,xym,xzp,xzm,yzp,yzm are defined as rotations about the bisector, for example  $xyp=|1\vec{x}+1\vec{y}|$  and  $yzm=|1\vec{y}-1\vec{z}|$ .

C4	$\hat{E}$	$\hat{C}_4$	$\hat{C}_2$	$\hat{C}_4^3$
A	1	1	1	1
B	1	-1	1	-1
$E_1$	1	i	-1	-i
$E_2$	1	-i	-1	$i$

C5	$\hat{E}$	$\hat{C}_5$	$\hat{C}_5^2$	$\hat{C}_5^3$	$\hat{C}_5^4$
$\overline{A}$	1	1	1	1	1
$E1_1$	1	$arepsilon_5$	$\varepsilon_5^2$	$arepsilon_5^{2*}$	$arepsilon_5^*$
$E1_2$	1	$arepsilon_5^*$	$\varepsilon_5^{2*}$	$arepsilon_5^2$	$arepsilon_5$
$E2_1$	1	$arepsilon_5^2$	$arepsilon_5^*$	$arepsilon_5$	$\varepsilon_5^{2*}$
$E2_2$	1	$\varepsilon_5^{2*}$	$arepsilon_5$	$arepsilon_5^*$	$\varepsilon_5^2$

C6	$\hat{E}$	$\hat{C}_6$	$\hat{C}_3$	$\hat{C}_2$	$\hat{C}_3^2$	$\hat{C}_6^5$
$\overline{A}$	1	1	1	1	1	1
B	1	-1	1	-1	1	-1
$E1_1$	1	$arepsilon_6$	$arepsilon_3$	-1	$arepsilon_3^*$	$arepsilon_6^*$
$E1_2$	1	$arepsilon_6^*$	$\varepsilon_3^*$	-1	$arepsilon_3$	$\varepsilon_6$
$E2_1$	1	$arepsilon_3$	$\varepsilon_3^*$	1	$arepsilon_3$	$arepsilon_3^*$
$E2_2$	1	$arepsilon_3^*$	$\varepsilon_3$	1	$arepsilon_3^*$	$arepsilon_3$

C7	$\hat{E}$	$\hat{C}_7$	$\hat{C}_7^2$	$\hat{C}_7^3$	$\hat{C}_7^4$	$\hat{C}_7^5$	$\hat{C}_7^6$
$\overline{A}$	1	1	1	1	1	1	1
$E1_1$	1	$arepsilon_7$	$\varepsilon_7^2$	$\varepsilon_7^3$	$\varepsilon_7^{3*}$	$\varepsilon_7^{2*}$	$arepsilon_7^*$
$E1_2$	1	$\varepsilon_7^*$	$\varepsilon_7^{2*}$	$\varepsilon_7^{3*}$	$\varepsilon_7^3$	$\varepsilon_7^2$	$arepsilon_7$
$E2_1$	1	$\varepsilon_7^2$	$\varepsilon_7^{3*}$	$arepsilon_7^*$	$\varepsilon_7$	$\varepsilon_7^3$	$arepsilon_7^{2*}$
$E2_2$	1	$\varepsilon_7^{2*}$	$\varepsilon_7^3$	$arepsilon_7$	$arepsilon_7^*$	$\varepsilon_7^{3*}$	$arepsilon_7^2$
$E3_1$	1	$\varepsilon_7^3$	$\varepsilon_7^*$	$arepsilon_7^2$	$\varepsilon_7^{2*}$	$\varepsilon_7$	$\varepsilon_7^{3*}$
$E3_2$	1	$arepsilon_7^{3*}$	$\varepsilon_7$	$arepsilon_7^{2*}$	$\varepsilon_7^2$	$arepsilon_7^*$	$\varepsilon_7^3$

C8	$\hat{E}$	$\hat{C}_8$	$\hat{C}_4$	$\hat{C}^3_8$	$\hat{C}_2$	$\hat{C}_8^5$	$\hat{C}_4^3$	$\hat{C}_8^7$
$\overline{A}$	1	1	1	1	1	1	1	1
B	1	-1	1	-1	1	-1	1	-1
$E1_1$	1	$arepsilon_8$	i	$arepsilon_8^3$	-1	$arepsilon_8^{3*}$	-i	$arepsilon_8^*$
$E1_2$	1	$arepsilon_8^*$	-i	$\varepsilon_8^{3*}$	-1	$arepsilon_8^3$	i	$\varepsilon_8$
$E2_1$	1	i	-1	-i	1	i	-1	-i
$E2_2$	1	-i	-1	i	1	-i	-1	i
$E3_1$	1	$\varepsilon_8^{3*}$	i	$arepsilon_8^*$	-1	$arepsilon_8$	-i	$arepsilon_8^3$
$E3_2$	1	$arepsilon_8^3$	-i	$arepsilon_8$	-1	$arepsilon_8^*$	i	$arepsilon_8^{3*}$

C2h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_2$
$\overline{Ag}$	1	1	1	1
Bg	1	-1	1	-1
Au	1	-1	-1	1
Bu	1	1	-1	-1

C3h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{C}_3$	$\hat{C}_3^2$	$\hat{S}_3$	$\hat{S}_3^5$
A'	1	1	1	1	1	1
$E_1'$	1	1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$
$E_2'$	1	1	$arepsilon_3^*$	$\varepsilon_3$	$arepsilon_3^*$	$arepsilon_3$
A''	1	-1	1	1	-1	-1
$E_1''$	1	-1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_6^*$	$arepsilon_6$
$E_2''$	1	-1	$arepsilon_3^*$	$arepsilon_3$	$\varepsilon_6$	$arepsilon_6^*$

C4h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_4$	$\hat{C}_2$	$\hat{C}_4^3$	$\hat{S}_4$	$\hat{S}_4^3$
$\overline{Ag}$	1	1	1	1	1	1	1	1
Bg	1	1	1	-1	1	-1	-1	-1
$E_1g$	1	-1	1	i	-1	-i	-i	i
$E_2g$	1	-1	1	-i	-1	i	i	-i
Au	1	-1	-1	1	1	1	-1	-1
Bu	1	-1	-1	-1	1	-1	1	1
$E_1u$	1	1	-1	$i$	-1	-i	i	-i
$E_2u$	1	1	-1	-i	-1	i	-i	i

C5h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{C}_5$	$\hat{C}_5^2$	$\hat{C}_5^3$	$\hat{C}_5^4$	$\hat{S}_5$	$\hat{S}_5^7$	$\hat{S}_5^3$	$\hat{S}_{5}^{9}$
A'	1	1	1	1	1	1	1	1	1	1
$E1'_1$	1	1	$arepsilon_5$	$\varepsilon_5^2$	$\varepsilon_5^{2*}$	$arepsilon_5^*$	$arepsilon_5$	$arepsilon_5^2$	$arepsilon_5^{2*}$	$arepsilon_5^*$
$E1_2'$	1	1	$arepsilon_5^*$	$\varepsilon_5^{2*}$	$\varepsilon_5^2$	$arepsilon_5$	$arepsilon_5^*$	$arepsilon_5^{2*}$	$arepsilon_5^2$	$arepsilon_5$
$E2'_1$	1	1	$\varepsilon_5^2$	$arepsilon_5^*$	$arepsilon_5$	$\varepsilon_5^{2*}$	$\varepsilon_5^2$	$arepsilon_5^*$	$arepsilon_5$	$arepsilon_5^{2*}$
$E2_2'$	1	1	$\varepsilon_5^{2*}$	$arepsilon_5$	$arepsilon_5^*$	$\varepsilon_5^2$	$arepsilon_5^{2*}$	$arepsilon_5$	$arepsilon_5^*$	$arepsilon_5^2$
A''	1	-1	1	1	1	1	-1	-1	-1	-1
$E1_1''$	1	-1	$arepsilon_5$	$\varepsilon_5^2$	$\varepsilon_5^{2*}$	$arepsilon_5^*$	$-\varepsilon_5$	$-\varepsilon_5^2$	$-\varepsilon_5^{2*}$	$-\varepsilon_5^*$
$E1_2''$	1	-1	$arepsilon_5^*$	$\varepsilon_5^{2*}$	$arepsilon_5^2$	$arepsilon_5$	$-\varepsilon_5^*$	$-\varepsilon_5^{2*}$	$-\varepsilon_5^2$	$-\varepsilon_5$
$E2_1''$	1	-1	$\varepsilon_5^2$	$arepsilon_5^*$	$arepsilon_5$	$\varepsilon_5^{2*}$	$-\varepsilon_5^2$	$-\varepsilon_5^*$	$-\varepsilon_5$	$-\varepsilon_5^{2*}$
$E2_2''$	1	-1	$\varepsilon_5^{2*}$	$arepsilon_5$	$arepsilon_5^*$	$\varepsilon_5^2$	$-\varepsilon_5^{2*}$	$-\varepsilon_5$	$-\varepsilon_5^*$	$-\varepsilon_5^2$

C6h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_6$	$\hat{C}_3$	$\hat{C}_2$	$\hat{C}_3^2$	$\hat{C}_6^5$	$\hat{S}_6$	$\hat{S}_3$	$\hat{S}_3^5$	$\hat{S}_6^5$
$\overline{Ag}$	1	1	1	1	1	1	1	1	1	1	1	1
Bg	1	-1	1	-1	1	-1	1	-1	1	-1	-1	1
$E1_1g$	1	-1	1	$\varepsilon_6$	$\varepsilon_3$	-1	$arepsilon_3^*$	$\varepsilon_6^*$	$arepsilon_3^*$	$\varepsilon_6^*$	$\varepsilon_6$	$arepsilon_3$
$E1_2g$	1	-1	1	$\varepsilon_6^*$	$arepsilon_3^*$	-1	$arepsilon_3$	$\varepsilon_6$	$arepsilon_3$	$\varepsilon_6$	$arepsilon_6^*$	$arepsilon_3^*$
$E2_1g$	1	1	1	$arepsilon_3$	$arepsilon_3^*$	1	$arepsilon_3$	$\varepsilon_3^*$	$arepsilon_3$	$\varepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$
$E2_2g$	1	1	1	$\varepsilon_3^*$	$arepsilon_3$	1	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$
Au	1	-1	-1	1	1	1	1	1	-1	-1	-1	-1
Bu	1	1	-1	-1	1	-1	1	-1	-1	1	1	-1
$E1_1u$	1	1	-1	$\varepsilon_6$	$\varepsilon_3$	-1	$arepsilon_3^*$	$\varepsilon_6^*$	$arepsilon_6$	$\varepsilon_3$	$arepsilon_3^*$	$arepsilon_6^*$
$E1_2u$	1	1	-1	$\varepsilon_6^*$	$arepsilon_3^*$	-1	$arepsilon_3$	$\varepsilon_6$	$\varepsilon_6^*$	$\varepsilon_3^*$	$arepsilon_3$	$arepsilon_6$
$E2_1u$	1	-1	-1	$arepsilon_3$	$arepsilon_3^*$	1	$arepsilon_3$	$\varepsilon_3^*$	$\varepsilon_6^*$	$\varepsilon_6$	$arepsilon_6^*$	$arepsilon_6$
$E2_2u$	1	-1	-1	$\varepsilon_3^*$	$\varepsilon_3$	1	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_6$	$\varepsilon_6^*$	$arepsilon_6$	$arepsilon_6^*$

C4v	$\hat{E}$	$\hat{C}_4$	$\hat{C}_2$	$\hat{C}_4^3$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$

C4v	$\hat{\sigma}_v(1)$	$\hat{\sigma}_v(2)$	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$
A1	1	1	1	1
A2	-1	-1	-1	-1
B1	1	1	-1	-1
B2	-1	-1	1	1
E	$\left  \begin{array}{cc} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right $	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\left  \begin{array}{cc} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{array} \right $	$\left  \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} \right $

$$\begin{array}{c|c|c|c}
\hline
C5v & \hat{\sigma}_v(4) & \hat{\sigma}_v(5) \\
\hline
A1 & 1 & 1 \\
A2 & -1 & -1 \\
E1 & \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} & \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} \\
E2 & \begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} & \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix}
\end{array}$$

C6v	$\hat{E}$	$\hat{C}_6$	$\hat{C}_3$	$\hat{C}_2$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \left  \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \right  $
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

C6v	$\hat{C}_3^2$	$\hat{C}_6^5$	$\hat{\sigma}_v(1)$	$\hat{\sigma}_v(2)$
$\overline{A1}$	1	1	1	1
A2	1	1	-1	-1
B1	1	-1	1	1
B2	1	-1	-1	-1
E1	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} $	$\left  \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \right $
E2	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\left  \begin{array}{cc} 1 & 0 \\ 0 & -1 \end{array} \right $	$\left  \begin{array}{cc} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{array} \right  $

$$\begin{array}{|c|c|c|c|c|c|} \hline \textbf{C6v} & \hat{\sigma}_v(3) & \hat{\sigma}_d(1) & \hat{\sigma}_d(2) & \hat{\sigma}_d(3) \\ \hline A1 & 1 & 1 & 1 & 1 \\ A2 & -1 & -1 & -1 & -1 \\ B1 & 1 & -1 & -1 & -1 \\ B2 & -1 & 1 & 1 & 1 \\ \hline E1 & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ E2 & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \hline \end{array}$$

$\mathbf{D4}$	$\hat{E}$	$\hat{C}_4$	$\hat{C}_2$	$\hat{C}_4^3$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E	$\left  \begin{array}{cc} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \right $	$\left  \begin{array}{cc} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{array} \right $	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} $

D6	$\hat{E}$	$\hat{C}_{6}$	$\hat{C}_3$	$\hat{C}_2$
A1	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

$$\begin{array}{|c|c|c|c|c|c|} \hline \mathbf{D6} & \hat{C}_3^2 & \hat{C}_6^5 & \hat{C}_2'(1) & \hat{C}_2'(2) \\ \hline A1 & 1 & 1 & 1 & 1 & 1 \\ A2 & 1 & 1 & 1 & -1 & -1 \\ B1 & 1 & -1 & 1 & 1 \\ B2 & 1 & -1 & -1 & -1 \\ \hline E1 & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ E2 & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \end{array}$$

$$\begin{array}{|c|c|c|c|c|c|} \hline \mathbf{D6} & \hat{C}_{2}''(3) & \hat{C}_{2}''(1) & \hat{C}_{2}''(2) & \hat{C}_{2}''(3) \\ \hline A1 & 1 & 1 & 1 & 1 \\ A2 & -1 & -1 & -1 & -1 \\ B1 & 1 & -1 & -1 & -1 \\ B2 & -1 & 1 & 1 & 1 \\ \hline E1 & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ E2 & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \end{array}$$

D8	$\hat{E}$	$\hat{C}_8$ $ $	$\hat{C}_4$	$\hat{C}^3_8$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E3	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \mid$

D8	$\hat{C}_2$	$\hat{C}_8^5$ $ $	$\hat{C}_4^3$	$\hat{C}_8^7$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	-1	1	-1
B2	1	-1	1	-1
E1	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \ -rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E3	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix} \mid$

D8	$\hat{C}_2'(1)$	$\hat{C}_2'(2)$	$\hat{C}_2'(3)$	$\hat{C}_2'(4)$
A1	1	1	1	1
A2	-1	-1	-1	-1
B1	1	1	1	1
B2	-1	-1	-1	-1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\left  \begin{array}{cc} 0 & -1 \\ -1 & 0 \end{array} \right $	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

D8	$\hat{C}_2''(1)$	$\hat{C}_2''(2)$	$\hat{C}_{2}''(3)$	$\hat{C}_2''(4)$
$\overline{A1}$	1	1	1	1
A2	-1	-1	-1	-1
B1	-1	-1	-1	-1
B2	1	1	1	1
E1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E3	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$

$$\begin{array}{|c|c|c|c|c|c|} \hline \textbf{D3d} & \hat{E} & \hat{i} & \hat{C}_3 & \hat{C}_3^2 \\ \hline A1g & 1 & 1 & 1 & 1 & 1 \\ A2g & 1 & 1 & 1 & 1 & 1 \\ \hline Eg & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ \hline A1u & 1 & -1 & 1 & 1 \\ A2u & 1 & -1 & 1 & 1 \\ Eu & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \end{array}$$

D3d	$\hat{S}_{6}$	$\hat{S}_6^5$	$\hat{C}_2'(1)$	$\hat{C}_2'(2)$
A1g	1	1	1	1
A2g	1	1	-1	-1
Eg	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} $	$ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} $
A1u	-1	- <u>1</u>	1	1
A2u	-1	-1	-1	-1
Eu	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left  \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \right $

D3d	$\hat{C}_2'(3)$	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$	$\hat{\sigma}_d(3)$
A1g	1	1	1	1
A2g	-1	-1	-1	-1
Eg	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} $	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
A1u	1	-1	-1	$\begin{vmatrix} & & & & & \\ & & & & -1 \end{vmatrix}$
A2u	-1	1	1	1
Eu	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} $	$\left  \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \right $

D4d	$\hat{E}$	$\hat{C}_4$	$\hat{C}_2$	$\hat{C}_4^3$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	1	1	1
B2	1	1	1	1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
E3	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$

D4d	$\hat{S}_8$	$\hat{S}^3_8$	$\hat{S}_8^5$	$\hat{S}^7_8$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	-1	-1	-1	-1
B2	-1	-1	-1	-1
E1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E3	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix} \mid$

D4d	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$	$\hat{\sigma}_d(3)$	$\hat{\sigma}_d(4)$
A1	1	1	1	1
A2	-1	-1	-1	-1
B1	-1	-1	-1	-1
B2	1	1	1	1
E1	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E3	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $

D5d	$\hat{C}_2'(3)$	$\hat{C}_2'(4)$	$\hat{C}_2'(5)$	$\hat{\sigma}_d(1$
$\overline{A1g}$	1	1	1	
A2g	-1	-1	-1	_
E1g	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \\ \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $
E2g	$\begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $
A1u	1	1	1	_
A2u	-1	-1	-1	
E1u	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $	$\begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix} $
E2u	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} \\ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $	$ \begin{pmatrix} \cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \\ -\cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix} $
D5d	$\hat{\sigma}_d(2)$	$\hat{\sigma}_d(3)$	$\hat{\sigma}_d(4)$	$\hat{\sigma}_d(5)$
$\overline{A1g}$	1	1	1	1
A2g	-1	-1	-1	-1
E1g	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $ $ \begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix} $	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \qquad \begin{pmatrix} \cos \frac{2i}{5} \\ \sin \frac{2i}{5} \end{pmatrix}$	$ \begin{array}{ccc} \frac{\pi}{5} & \sin\frac{2\pi}{5} \\ \frac{\pi}{5} & -\cos\frac{2\pi}{5} \end{array} $ $ \begin{array}{ccc} \cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \cos\frac{\pi}{5} & \cos\frac{\pi}{5} \end{array} $ $ \begin{array}{ccc} \cos\frac{\pi}{5} & \cos\frac{\pi}{5} \end{array} $	$ \begin{array}{c c} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{array} $ $ \begin{array}{c c} \frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{array} $
E2g	$\begin{pmatrix} -\cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \qquad \begin{pmatrix} -c \\ \sin \theta \end{pmatrix}$	$ \begin{vmatrix} \cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \cos\frac{\pi}{5} & \cos\frac{\pi}{5} \end{vmatrix} \begin{vmatrix} \cos \pi \\ -\sin^2 \pi \end{vmatrix} $	$ \begin{pmatrix} \frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $
A1u	-1	-1	-1	-1
A2u	1	1	1	1
E1u	$\begin{pmatrix} -\cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} -\cos\frac{2}{5} \\ -\sin\frac{2}{5} \end{pmatrix} $ $ \begin{pmatrix} -\cos\frac{2}{5} \\ -\sin\frac{2}{5} \end{pmatrix} $ $ \begin{pmatrix} \cos\frac{2}{5} \\ -\sin\frac{2}{5} \end{pmatrix} $	$ \frac{\pi}{5} - \sin\frac{2\pi}{5} \\ \cos\frac{2\pi}{5} $ $ \cos\frac{2\pi}{5} $	$ \begin{vmatrix} \cos\frac{\pi}{5} & -\sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{vmatrix} $ $ \begin{vmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{vmatrix} $
E2u	$ \begin{pmatrix} \cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix} $	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \mid \begin{pmatrix} \cos \frac{7}{5} \\ -\sin \end{pmatrix}$	$\left(\frac{\pi}{5} - \sin\frac{\pi}{5}\right)$ $\left(\frac{\pi}{5} - \cos\frac{\pi}{5}\right)$	$ \cos \frac{3\pi}{5}  \sin \frac{2\pi}{5} $ $ \sin \frac{2\pi}{5}  \cos \frac{2\pi}{5} $

D6d	$\hat{E}$	$\hat{C}_{6}$	$\hat{C}_3$	$\hat{C}_2$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	1	1	1
B2	1	1	1	1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
E3	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
E4	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
E5	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$

D6d	$\hat{C}_3^2$	$\hat{C}_6^5$	$\hat{S}_12$	$\hat{S}_4$ $\Big $
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	1	1	-1	-1
B2	1	1	-1	-1
E1	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E2	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
E3	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E4	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
E5	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$

D6d	$\hat{S}_1 2^5$	$\hat{S}_1 2^7$	$\hat{S}_4^3$	$\hat{S}_121$
$\overline{A1}$	1	1	1	1
A2	1	1	1	1
B1	-1	-1	-1	-1
B2	-1	-1	-1	-1
E1	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix} \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left(-\frac{\sqrt{3}}{2} - \frac{1}{2}\right)$
E3	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E4	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
E5	$\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$
D6d	$\hat{C}_2'(1)$	$\hat{C}_2'(2)$	$\hat{C}_2'(3)$	$\hat{C}_2''(1)$
$\overline{A1}$	1	1	1	1
A2	-1	-1	-1	-1
B1	1	1	1	1
B2	-1	-1	-1	-1
E1	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$egin{pmatrix} rac{1}{2} & rac{\sqrt{3}}{2} \ rac{\sqrt{3}}{2} & -rac{1}{2} \end{pmatrix} \ egin{pmatrix} rac{1}{2} \ -rac{1}{2} \ \end{pmatrix}$	$\begin{bmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{bmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$
<i>E</i> 0	$\begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 1 \end{pmatrix}$	$\frac{1}{2}$ $-\frac{\sqrt{3}}{2}$	$\left(\begin{array}{cc} \frac{1}{2} & \frac{\sqrt{3}}{2} \end{array}\right)$	$\left\langle \begin{array}{cc} \frac{1}{2} & \frac{\sqrt{3}}{2} \end{array} \right\rangle$

$\mathbf{D6d}$	$\hat{C}_2''(2)$	$\hat{C}_2''(3)$	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$
$\overline{A1}$	1	1	1	1
A2	-1	-1	-1	-1
B1	1	1	-1	-1
B2	-1	-1	1	1
E1	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
E2	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} $
E4	$ \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} $	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E5	$\left  \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right $	$ \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} $	$\begin{pmatrix} \frac{\sqrt{3}}{2} & -\frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

D6d	$\hat{\sigma}_d(3)$	$\hat{\sigma}_d(4)$	$\hat{\sigma}_d(5)$	$\hat{\sigma}_d(6)$
A1	1	1	1	1
A2	-1	-1	-1	-1
B1	-1	-1	-1	-1
B2	1	1	1	1
E1	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$
E2	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \bigg $
E3	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E4	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
E5	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} \mid$

D2h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_2$	$\hat{C}'_2(1)$	$\hat{C}_2''(1)$	$\hat{\sigma}_v(1)$	$\hat{\sigma}_d(1)$
$\overline{Ag}$	1	1	1	1	1	1	1	1
B1g	1	1	1	1	-1	-1	-1	-1
B2g	1	-1	1	-1	-1	1	1	-1
B3g	1	-1	1	-1	1	-1	-1	1
Au	1	-1	-1	1	1	1	-1	-1
B1u	1	-1	-1	1	-1	-1	1	1
B2u	1	1	-1	-1	-1	1	-1	1
B3u	1	1	-1	-1	1	-1	1	-1

$$\begin{array}{|c|c|c|c|c|c|} \hline \mathbf{D3h} & \hat{C}_{2}'(1) & \hat{C}_{2}'(2) & \hat{C}_{2}'(3) & \hat{S}_{3} \\ \hline A1' & 1 & 1 & 1 & 1 \\ A2' & -1 & -1 & -1 & -1 & 1 \\ \hline E' & \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \hline A1'' & 1 & 1 & 1 & -1 \\ A2'' & -1 & -1 & -1 & -1 \\ \hline E'' & \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \end{array}$$

$$\begin{array}{|c|c|c|c|c|c|} \hline \textbf{D3h} & \hat{S}_3^5 & \hat{\sigma}_v(1) & \hat{\sigma}_v(2) & \hat{\sigma}_v(3) \\ \hline A1' & 1 & 1 & 1 & 1 & 1 \\ A2' & 1 & -1 & -1 & -1 & -1 \\ E' & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ A1'' & -1 & -1 & -1 & -1 \\ A2'' & -1 & 1 & 1 & 1 \\ E'' & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} & \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \end{array}$$

D4h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_4$
A1g	1	1	1	1
A2g	1	1	1	1
B1g	1	1	1	-1
B2g	1	1	1	-1
Eg	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\left  \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \right $
A1u	1	-1	-1	1
A2u	1	-1	-1	1
B1u	1	-1	-1	-1
B2u	1	-1	-1	-1
Eu	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left  \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \right $

D4h	$\hat{C}_2$	$\hat{C}_4^3$	$\hat{C}'_{2}(1)$	$\hat{C}_2'(2)$
$\overline{A1g}$	1	1	1	1
A2g	1	1	-1	-1
B1g	1	-1	1	1
B2g	1	-1	-1	-1
Eg	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left  \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \right $
A1u	1	1	1	1
A2u	1	1	-1	-1
B1u	1	-1	1	1
B2u	1	-1	-1	-1
Eu	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left  \begin{array}{cc} 0 & 1 \\ -1 & 0 \end{array} \right $	$\left  \begin{array}{cc} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right $	$\left  \begin{array}{cc} -1 & 0 \\ 0 & 1 \end{array} \right $

D4h	$\hat{C}_{2}''(1)$	$\hat{C}_2''(2)$	$\hat{S}_4$	$\hat{S}_4^3$
$\overline{A1g}$	1	1	1	1
A2g	-1	-1	1	$\mid \qquad 1 \mid$
B1g	-1	-1	-1	-1
B2g	1	1	-1	-1
Eg	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\left  \begin{array}{cc} \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{array} \right $
A1u	1	1	$\begin{vmatrix} & & & & & \\ & & & & -1 \end{vmatrix}$	$\begin{vmatrix} & & & -1 \end{vmatrix}$
A2u	-1	-1	-1	-1
B1u	-1	-1	1	1
B2u	1	1	1	1
Eu	$\left  \begin{array}{cc} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{array} \right $	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\left  \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \right $

D4h	$\hat{\sigma}_v(1)$	$\hat{\sigma}_v(2)$	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$
A1g	1	1	1	1
A2g	-1	-1	-1	-1
B1g	1	1	-1	-1
B2g	-1	-1	1	1
Eg	$\left  \begin{array}{cc} -1 & 0 \\ 0 & 1 \end{array} \right $	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
A1u	-1	-1	-1	-1
A2u	1	1	1	1
B1u	-1	-1	1	1
B2u	1	1	-1	-1
Eu	$\left  \begin{array}{cc} \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right $	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} $

$$\begin{array}{|c|c|c|c|c|c|} \hline \mathbf{D5h} & \hat{E} & \hat{\sigma}_h & \hat{C}_5 & \hat{C}_5^2 \\ \hline A1' & 1 & 1 & 1 & 1 & 1 \\ A2' & 1 & 1 & 1 & 1 & 1 \\ \hline E1' & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} \cos \frac{2\pi}{5} & -\sin \frac{2\pi}{5} \\ \sin \frac{2\pi}{5} & \cos \frac{2\pi}{5} \end{pmatrix} & \begin{pmatrix} -\cos \frac{\pi}{5} & -\sin \frac{\pi}{5} \\ \sin \frac{\pi}{5} & -\cos \frac{\pi}{5} \end{pmatrix} \\ E2' & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -\cos \frac{\pi}{5} & -\sin \frac{\pi}{5} \\ \sin \frac{\pi}{5} & -\cos \frac{\pi}{5} \end{pmatrix} & \begin{pmatrix} \cos \frac{2\pi}{5} & \sin \frac{2\pi}{5} \\ -\sin \frac{2\pi}{5} & \cos \frac{2\pi}{5} \end{pmatrix} \\ A1'' & 1 & -1 & 1 & 1 \\ A2'' & 1 & -1 & 1 & 1 \\ E1'' & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} \cos \frac{2\pi}{5} & -\sin \frac{2\pi}{5} \\ \sin \frac{2\pi}{5} & -\cos \frac{\pi}{5} \end{pmatrix} & \begin{pmatrix} -\cos \frac{\pi}{5} & -\sin \frac{\pi}{5} \\ \sin \frac{\pi}{5} & -\cos \frac{\pi}{5} \end{pmatrix} \\ E2'' & \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} & \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} & \begin{pmatrix} -\cos \frac{\pi}{5} & -\sin \frac{\pi}{5} \\ \sin \frac{\pi}{5} & -\cos \frac{\pi}{5} \end{pmatrix} & \begin{pmatrix} \cos \frac{2\pi}{5} & \sin \frac{2\pi}{5} \\ -\sin \frac{2\pi}{5} & \cos \frac{2\pi}{5} \end{pmatrix} \\ -\sin \frac{2\pi}{5} & \cos \frac{2\pi}{5} & -\sin \frac{\pi}{5} \end{pmatrix} & \begin{pmatrix} \cos \frac{2\pi}{5} & \sin \frac{2\pi}{5} \\ -\sin \frac{2\pi}{5} & \cos \frac{2\pi}{5} \end{pmatrix} \end{array}$$

D5h	$\hat{C}_5^3$	$\hat{C}_5^4$	$\hat{C}_2'(1)$	$\hat{C}_2'(2)$
$\overline{A1'}$	1	1	1	1
A2'	1	1	-1	-1
E1'	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix} $	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$
E2'	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix} $	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $
A1''	1	1	1	1
A2''	1	1	-1	-1
E1"	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{2\pi}{5} & \sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix} $	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ \sin\frac{\pi}{5} & \cos\frac{\pi}{5} \end{pmatrix}$
E2"	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ \sin\frac{2\pi}{5} & \cos\frac{2\pi}{5} \end{pmatrix} $	$\begin{pmatrix} -\cos\frac{\pi}{5} & \sin\frac{\pi}{5} \\ -\sin\frac{\pi}{5} & -\cos\frac{\pi}{5} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} \cos\frac{2\pi}{5} & -\sin\frac{2\pi}{5} \\ -\sin\frac{2\pi}{5} & -\cos\frac{2\pi}{5} \end{pmatrix} $

D6h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i}$	$\hat{C}_6$
A1g	1	1	1	1
A2g	1	1	1	1
B1g	1	-1	1	-1
B2g	1	-1	1	-1
E1g	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
A1u	1	-1	-1	1
A2u	1	-1	-1	1
B1u	1	1	-1	-1
B2u	1	1	-1	-1
E1u	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$

D6h	$\hat{C}_3$	$\hat{C}_2$	$\hat{C}_3^2$	$\hat{C}_6^5$ $\Big $
$\overline{A1g}$	1	1	1	1
A2g	1	1	1	1
B1g	1	-1	1	-1
B2g	1	-1	1	-1
E1g	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\left  \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \right  \left( \frac{1}{2} \right)$	$\begin{bmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{bmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \mid \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \mid \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
A1u	1	1	1	1
A2u	1	1	1	1
B1u	1	-1	1	-1
B2u	1	-1	1	-1
E1u	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\left  \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \right  \left($	$ \begin{vmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{vmatrix} $ $ \begin{vmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{vmatrix} $	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \mid \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} \mid \begin{pmatrix} 1 $	$\begin{bmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{bmatrix} \mid$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \mid$

D6h	$\hat{C}'_{2}(1)$	$\hat{C}_2'(2)$	$\hat{C}_2'(3)$	$\hat{C}_2''(1)$
$\overline{A1g}$	1	1	1	1
$A2g \\ B1g$	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$	$-1 \\ 1$	-1 1	$ \begin{array}{c c} -1 \\ -1 \end{array} $
B1g	-1	-1	-1	$\begin{array}{c c} & -1 \\ & 1 \end{array}$
E1g	$ \left  \begin{array}{cc} 1 & 0 \\ 0 & -1 \end{array} \right  $	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $
E2g	$\left  \begin{array}{cc} -1 & 0 \\ 0 & 1 \end{array} \right $	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $
A1u	1	1	1	1
A2u $B1u$	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$	-1 1	$-1 \\ 1$	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$
B1u $B2u$	$\begin{bmatrix} & & 1 \\ & & -1 \end{bmatrix}$	-1	-1	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$
E1u	$ \left  \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right  $	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & \sqrt{3} \end{pmatrix}$	
E2u	$ \left  \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \right  $	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{1}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $
D6h	$\hat{C}_2''(2)$	$\hat{C}_2''(3)$	$\hat{S}_6$	$\hat{S}_3$ $\Big $
$\overline{A1g}$	$\hat{C}_{2}''(2)$	$\hat{C}_{2}''(3)$	1	$\begin{array}{c c} \hat{S}_3 \\ \hline 1 \\ 1 \end{array}$
$\begin{array}{c} A1g \\ A2g \end{array}$	$\begin{bmatrix} 1 \\ -1 \end{bmatrix}$	1 -1	1 1	1   1
$\overline{A1g}$	$1$	1	1	1
$ \begin{array}{c} A1g \\ A2g \\ B1g \end{array} $	$\begin{vmatrix} & 1 \\ -1 \\ -1 \end{vmatrix}$	$ \begin{array}{ccc}  & & 1 \\  & -1 \\  & & -1 \\  & & 1 \\  & \left(-\frac{1}{2} & -\frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{array}\right) $	$ \begin{array}{ccc}  & 1 \\  & 1 \\  & 1 \\  & 1 \\  & \left(\frac{\frac{1}{2}}{2} & \frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{array}\right) $	$ \begin{array}{c c}  & 1 \\  & 1 \\  & -1 \\  & -1 \\  & -\frac{1}{2} & \frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{array} $
A1g $A2g$ $B1g$ $B2g$	$ \begin{array}{c cccc}  & 1 & \\  & -1 & \\  & -1 & \\  & 1 & \\  & (-1 & 0) & \\ \end{array} $	$ \begin{array}{ccc}  & & & 1 \\  & & -1 \\  & & & 1 \end{array} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} $	$ \begin{array}{ccc}  & 1 \\  & 1 \\  & 1 \\  & 1 \\  & \left(\frac{\frac{1}{2}}{2} & \frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{array}\right) $	$ \begin{array}{c cccc}  & 1 \\  & 1 \\  & -1 \\  & -1 \\  & -\frac{1}{2} & \frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\  & 1 & \sqrt{3} \end{array} $
A1g $A2g$ $B1g$ $B2g$ $E1g$ $E2g$ $A1u$	$ \begin{array}{ccc}  & 1 & \\  & -1 & \\  & -1 & \\  & 1 & \\  & & 1 \end{array} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ 1$	$ \begin{array}{ccc}  & & & 1 \\  & & -1 \\  & & & 1 \end{array} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix} $ $ 1$	$ \begin{array}{ccc} 1 \\ 1 \\ 1 \\ 1 \\ \left(\begin{array}{ccc} \frac{1}{2} & \frac{\sqrt{3}}{2} \end{array}\right) $	$ \begin{array}{c c} 1 \\ 1 \\ -1 \\ -1 \\ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ -1 $
A1g $A2g$ $B1g$ $B2g$ $E1g$ $E2g$ $A1u$ $A2u$	$ \begin{array}{ccc}  & 1 & \\  & -1 & \\  & -1 & \\  & 1 & \\  & & 1 \end{array} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{array}{cccc}  & 1 & \\  & & 1 & \\  & & & -1 \end{array} $	$ \begin{array}{ccc}  & & & 1 \\  & & -1 \\  & & & 1 \end{array} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ 1 $	$ \begin{array}{ccc}  & 1 \\  & 1 \\  & 1 \\  & 1 \\  & \frac{1}{2} & \frac{\sqrt{3}}{2} \\  & \frac{\sqrt{3}}{2} & \frac{1}{2} \\  & \frac{1}{2} & \frac{\sqrt{3}}{2} \\  & -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{array} $	$ \begin{array}{c c} 1 \\ 1 \\ -1 \\ -1 \\ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ -1 \\ -1 $
A1g A2g B1g B2g E1g E2g A1u A2u B1u	$ \begin{array}{ccc}  & 1 & \\  & -1 & \\  & -1 & \\  & 1 & \\  & & 1 \end{array} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{array}{cccc}  & 1 & \\  & -1 & $	$ \begin{array}{ccc}  & & & 1 \\  & & -1 \\  & & & 1 \end{array} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{array}{ccc}  & & 1 \\  & & -1 \\  & & -1 \\  & & -1 \end{array} $	$ \begin{array}{cccc}  & & & & & & & & & \\  & & & & & & & & \\  & & & &$	$ \begin{array}{c c} 1 \\ 1 \\ -1 \\ -1 \\ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ -1 \\ -1 \\ 1 $
A1g $A2g$ $B1g$ $B2g$ $E1g$ $E2g$ $A1u$ $A2u$	$ \begin{array}{ccc}  & 1 & \\  & -1 & \\  & -1 & \\  & 1 & \\  & & 1 \end{array} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{pmatrix}  -1 & 0 \\  0 & 1 \end{pmatrix} $ $ \begin{array}{cccc}  & 1 & \\  & & 1 & \\  & & & -1 \end{array} $	$ \begin{array}{ccc}  & & & 1 \\  & & -1 \\  & & & 1 \end{array} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ 1 $	$ \begin{array}{ccc}  & 1 \\  & 1 \\  & 1 \\  & 1 \end{array} $ $ \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ -1$	$ \begin{array}{c c} 1 \\ 1 \\ -1 \\ -1 \\ \begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix} \\ \begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} \\ -1 \\ -1 $

D6h	$\hat{S}_3^5$	$\hat{S}_6^5$	$\hat{\sigma}_v(1)$	$\hat{\sigma}_v(2)$
$\overline{A1g}$	1	1	1	1
A2g	1	1	-1	-1
B1g	-1	1	-1	-1
B2g	-1	1	1	1
E1g	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
A1u	-1	-1	-1	-1
A2u	-1	-1	1	1
B1u	1	-1	1	1
B2u	1	-1	-1	-1
E1u	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$

D6h	$\hat{\sigma}_v(3)$	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$	$\hat{\sigma}_d(3)$
A1g	1	1	1	1
A2g	-1	-1	-1	-1
B1g	-1	1	1	1
B2g	1	-1	-1	-1
E1g	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
A1u	-1	-1	-1	-1
A2u	1	1	1	1
B1u	1	-1	-1	-1
B2u	-1	1	1	1
E1u	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$

D8h	$\hat{E}$	$\hat{\sigma}_h$	$\hat{i} \mid$	$\hat{C}_8$ ]
A1g	1	1	1	1
A2g	1	1	1	1
B1g	1	1	1	-1
B2g	1	1	1	-1
E1g	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\left(egin{matrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{array} ight)$
E2g	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E3g	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
A1u	1	-1	-1	1
A2u	1	-1	-1	1
B1u	1	-1	-1	-1
B2u	1	-1	-1	-1
E1u	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\left(egin{matrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{matrix} ight)$
E2u	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E3u	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$

D8h	$\hat{C}_4$	$\hat{C}^3_8$	$\hat{C}_2$	$\hat{C}_8^5$
A1g	1	1	1	1
A2g	1	1	1	1
B1g	1	-1	1	-1
B2g	1	-1	1	-1
E1g	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E3g	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \ -rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$
A1u	1	1	1	1
A2u	1	1	1	1
B1u	1	-1	1	-1
B2u	1	-1	1	-1
E1u	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E3u	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$

D8h	$\hat{C}_4^3$	$\hat{C}^7_8$	$\hat{C}_2'(1)$	$\hat{C}_2'(2)$
$\overline{A1g}$	1	1	1	1
A2g	1	1	-1	-1
B1g	1	-1	1	1
B2g	1	-1	-1	-1
E1g	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$egin{pmatrix} rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \ -rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
E2g	$\left  \begin{array}{cc} -1 & 0 \\ 0 & -1 \end{array} \right $	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3g	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
A1u	1	1	1	1
A2u	1	1	-1	-1
B1u	1	-1	1	1
B2u	1	-1	-1	-1
E1u	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
E2u	$\left  \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \right $	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3u	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$

D8h	$\hat{C}_2'(3)$	$\hat{C}_2'(4)$	$\hat{C}_2''(1)$	$\hat{C}_2''(2)$
A1g	1	1	1	1
A2g	-1 1	-1 1	-1	-1
B1g $B2g$	-1	-1	-1	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$
E1g	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$ \begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} $
E2g	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E3g	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $
A1u	1	1	1	1
A2u	-1	-1	-1	-1
B1u	1	1	-1	-1
B2u	-1	-1	1	$\begin{bmatrix} 1 \\ \sqrt{2} \\ \sqrt{2} \end{bmatrix}$
E1u	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \mid$
E2u	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E3u	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix} \mid$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $

D8h	$\hat{C}_2''(3)$	$\hat{C}_2''(4)$	$\hat{S}_8$	$\hat{S}_4$ $\Big $
A1g	1	1	1	1
A2g	-1	-1	1	1
B1g	-1	-1	-1	1
B2g	1	1	-1	1
E1g	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E2g	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3g $A1u$	$\begin{pmatrix} 1 & 0 \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ $-1$	$ \begin{pmatrix} 0 & -1 \\ 0 & 1 \\ -1 & 0 \end{pmatrix} $
A2u	-1	-1	-1	-1
B1u	-1	-1	1	-1
B2u	1	1	1	-1
E1u	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E2u	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
E3u	$\begin{pmatrix} 1 & 0 \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 0 & -1 \\ 1 & 0 \end{pmatrix}$

D8h	$\hat{S}^3_8$	$\hat{S}_8^5$ $ $	$\hat{S}^3_4$ $ $	$\hat{S}_8^7$
A1g	1	1	1	1
A2g	1	1	1	1
B1g	-1	-1	1	-1
B2g	-1	-1	1	-1
E1g	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\left(egin{matrix} rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \ rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \end{matrix} ight)$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$
E2g	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$
E3g	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -rac{\sqrt{2}}{2} & rac{\sqrt{2}}{2} \ -rac{\sqrt{2}}{2} & -rac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $
A1u	-1	-1	-1	-1
A2u	-1	-1	-1	-1
B1u	1	1	-1	1
B2u	1	1	-1	1
E1u	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$
E2u	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$
E3u	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} \bigg $	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix} \mid$

D8h	$\hat{\sigma}_v(1)$	$\hat{\sigma}_v(2)$	$\hat{\sigma}_v(3)$	$\hat{\sigma}_v(4)$
A1g	1	1	1	1
A2g	-1	-1	-1	-1
B1g	1	1	1	1
B2g	-1	-1	-1	-1
E1g	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
E2g	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
E3g	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
A1u	-1	-1	-1	-1
A2u	1	1	1	1
B1u	-1	-1	-1	-1
B2u	1	1	1	1
E1u	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$
E2u	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
E3u	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

D8h	$\hat{\sigma}_d(1)$	$\hat{\sigma}_d(2)$	$\hat{\sigma}_d(3)$	$\hat{\sigma}_d(4)$	
A1g	1	1	1	1	
A2g $B1g$	$\begin{vmatrix} -1 \\ -1 \end{vmatrix}$	-1 $-1$	-1	$ \begin{array}{c c} -1 \\ -1 \end{array} $	
B2g	1	1	1	1	
E1g	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$ $\begin{pmatrix} 0 & -1 \end{pmatrix}$	
E2g	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$	
E3g	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	
$\begin{array}{c} A1u \\ A2u \end{array}$	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$	-1	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$	$\begin{bmatrix} -1 \\ 1 \end{bmatrix}$	
B1u	1	1	1	1	
B2u	1	-1	-1	-1	
E1u	$\begin{pmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$ \begin{bmatrix} -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{bmatrix} $	$ \begin{pmatrix} \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix} $	
E2u	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	
E3u	$\begin{pmatrix} -1 & 0 \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 \\ -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{pmatrix} $	$ \begin{vmatrix}     \begin{pmatrix}       \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \\       -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} \end{vmatrix} $	
$\mathbf{T}$	$\hat{E} \mid$	$\hat{C}_3(\alpha)$   $\hat{C}_3(\alpha)$	$\frac{2}{3}(\alpha)$   $\hat{C}$	$\hat{C}_3(\beta)$ $\hat{C}$	$\hat{Y}_3^2(\beta)$
$ \begin{array}{c c} A \\ E_1 \\ E_2 \end{array} $	1 1 1	$\begin{array}{c} 1 \\ \varepsilon_3 \\ \varepsilon_3^* \end{array}$	$\begin{bmatrix} 1 \\ \varepsilon_3^* \\ \varepsilon_3 \end{bmatrix}$	$\begin{array}{c} 1\\ \varepsilon_3\\ \varepsilon_3^* \end{array}$	$\begin{bmatrix} 1 \\ \varepsilon_3^* \\ \varepsilon_3 \end{bmatrix}$
$T \mid$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \mid \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$	$ \begin{vmatrix} 0 & 1 \\ 0 & 0 \\ 1 & 0 \end{vmatrix} \begin{vmatrix} 0 & 1 \\ 0 & 0 \\ 1 & 0 \end{vmatrix} $	$ \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}  \begin{pmatrix} 0 & 0 \\ -1 & 0 \\ 0 & -1 \end{pmatrix} $	$ \begin{vmatrix} 1 \\ 0 \\ 0 \end{vmatrix} \begin{vmatrix} 0 & -1 \\ 0 & 0 \\ 1 & 0 \end{vmatrix} $	$\begin{pmatrix} 0 \\ -1 \\ 0 \end{pmatrix}  \bigg  $
$\mathbf{T}$	$\hat{C}_{2}(\gamma)$	$\hat{C}_2^2(\gamma)$	$\hat{C}_3(\delta)$ .	$\hat{C}_2^2(\delta)$	$\hat{C}_2(x)$
$A$ $E_1$ $E_2$	$\begin{array}{c c} \varepsilon_3(7) \\ \hline 1 \\ \varepsilon_3 \\ \varepsilon_2^* \end{array}$	$\frac{\varepsilon_3(7)}{1}$	$ \begin{array}{c}                                     $	$\begin{array}{c c} \hat{C}_{3}^{2}(\delta) & \\ & 1 \\ & \varepsilon_{3}^{*} \\ & \varepsilon_{3} \\ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} \end{array}$	1 1 1
$T \mid $	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \left(\begin{array}{ccc} 0 & 1 & 0 \\ 0 & 0 & -1 \end{array}\right) $	$ \left(\begin{array}{cccc} 0 & 0 & -1 \\ -1 & 0 & 0 \end{array}\right) $	$ \left(\begin{array}{ccc} 0 & -1 & 0 \\ 0 & 0 & 1 \end{array}\right) $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ \end{pmatrix}$
'	(0 -1 0)	$(-1 \ 0 \ 0)$	(0 1 0)	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$(0 \ 0 \ -1)$

${f T}$	$\hat{C}_2(y)$	$\hat{C}_2(z)$
$\overline{A}$	1	1
$E_1$	1	1
$E_2$	1	1
	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$
T	$\begin{bmatrix} 0 & 1 & 0 \end{bmatrix}$	$\begin{bmatrix} 0 & -1 & 0 \end{bmatrix}$
	$\begin{pmatrix} 0 & 0 & -1 \end{pmatrix}$	$  \begin{array}{cccc} 0 & 0 & 1 \end{array}  $

Th	$\hat{E}$	$\hat{C}_3(lpha)$	$\hat{C}_3^2(lpha)$	$\hat{C}_3(eta)$	$\hat{C}_3^2(eta)$
Ag	1	1	1	1	1
Eg1	1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$
Eg2	1	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$
Tg	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $
Au	1	1	1	1	1
Eu1	1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$
Eu2	1	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$
Tu	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $

$\mathbf{Th}$	$\hat{C}_3(\gamma)$	$\hat{C}_3^2(\gamma)$	$\hat{C}_3(\delta)$	$\hat{C}_3^2(\delta)$	$\hat{C}_2(x)$
Ag	1	1	1	1	1
Eg1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	1
Eg2	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	1
Tg	$ \left  \begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} \right  $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \left       \begin{pmatrix}       0 & -1 & 0 \\       0 & 0 & 1 \\       -1 & 0 & 0     \end{pmatrix}     \right  $	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $
Au	1	1	1	1	1
Eu1	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	1
Eu2	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	1
Tu	$ \left  \begin{array}{ccc} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{array} \right  $	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \left       \begin{pmatrix}       0 & -1 & 0 \\       0 & 0 & 1 \\       -1 & 0 & 0     \end{pmatrix}     \right  $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$

$\mathbf{T}\mathbf{h}$	$\hat{C}_2(y)$	$\hat{C}_2(z)$	$\hat{i}$	$\hat{S}_6(\alpha)$	$\hat{S}_6^5(\alpha)$
$egin{array}{c} Ag \ Eg1 \ Eg2 \end{array}$	1 1 1	1 1 1	1 1 1 (1 0 0)	$\begin{array}{c} 1 \\ \varepsilon_3^* \\ \end{array}$	(0, 0, 1)
Tg $Au$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$
Eu1 $Eu2$	$\begin{pmatrix} 1 & 1 & 1 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 1 & 1 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & -1 & -1 \\ -1 & 0 & 0 \end{pmatrix}$	$ \begin{array}{c cccc} \varepsilon_6 \\ \varepsilon_6^* \\ \end{array} $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Tu	$ \left(\begin{array}{ccc} 0 & 1 & 0 \\ 0 & 0 & -1 \end{array}\right) $	$ \left(\begin{array}{ccc} 0 & -1 & 0 \\ 0 & 0 & 1 \end{array}\right) $	$ \left(\begin{array}{ccc} 0 & -1 & 0 \\ 0 & 0 & -1 \end{array}\right) $	$\left  \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} \right $	$\left  \begin{array}{ccc} -1 & 0 & 0 \\ 0 & -1 & 0 \end{array} \right $
$\frac{\text{Th}}{4}$	$\hat{S}_6(eta)$	$\hat{S}_6^5(eta)$	$\hat{S}_6(\gamma)$	$\hat{S}_6^5(\gamma)$	$\hat{S}_6(\delta)$
Ag $Eg1$	$rac{1}{arepsilon_3^*}$	$1 \ arepsilon_3$	$egin{array}{c c} 1 & & & & & & & & & & & & & & & & & & $	$egin{array}{c c} 1 & & & & & & & & & & & & & & & & & & $	$egin{array}{c} 1 \ arepsilon_3^* \ \end{array}$
Eg2	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$	$arepsilon_3^*$	$arepsilon_3$
Tg	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
	$\begin{pmatrix} 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} \mid \begin{pmatrix} 1 & 0 \\ 0 & 1$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$
$\begin{bmatrix} Au \\ Eu1 \end{bmatrix}$	-1	$-1$ $\varepsilon_6^*$	-1	$\begin{bmatrix} -1 \\ \varepsilon_6^* \end{bmatrix}$	-1
$\begin{bmatrix} Eu1 \\ Eu2 \end{bmatrix}$	$arepsilon_6 \ arepsilon_6^*$	$arepsilon_{6}^{arepsilon_{6}}$	$arepsilon_6^*$	$arepsilon_{6}^{arepsilon_{6}}$	$arepsilon_6^*$
Tu	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $
${f Th}$	$\hat{S}_{6}^{5}(\delta)$	$\hat{\sigma}_h(x)$	$\hat{\sigma}_h(y)$	$\hat{\sigma}_h(z)$	
Ag	1	1	1	1	
$\begin{bmatrix} Eg1 \\ Ea2 \end{bmatrix}$	$arepsilon_3$	1	1	1   1	
292	$\begin{pmatrix} 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	
Tg	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\left(\begin{array}{ccc} 0 & 1 & 0 \\ 0 & 0 & 1 \end{array}\right)$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	
Au	$\begin{pmatrix} 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \end{pmatrix}$	-1	
Eu1	$arepsilon_6^*$	-1	-1	-1	
Eu2	$\epsilon_6$	$\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 \\ 1 \\ 0 \\ 0 \end{pmatrix}$	$\begin{bmatrix} -1 \\ 1 & 0 & 0 \end{bmatrix}$	
Tu	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$\left(\begin{array}{ccc} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array}\right)$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $\begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $	

-1

Oh	$\hat{C}_2(y)$	$\hat{C}_4^3(y)$	$\hat{C}_4(z)$	$\hat{C}_2(z)$	$\hat{C}_4^3(z)$
$\overline{A1g}$	1	1	1	1	1
A2g	1	-1	-1	1	-1
Eg	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
T1g	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $
T2g	$     \begin{pmatrix}       -1 & 0 & 0 \\       0 & 1 & 0 \\       0 & 0 & -1     \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix} $
A1u	1	1	1	1	1
A2u	1	-1	-1	1	-1
Eu	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
T1u	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $
T2u	$ \left  \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \right  $	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix} $

Oh	$\hat{C}_3(lpha)$	$\hat{C}_3^2(lpha)$	$\hat{C}_3(eta)$	$\hat{C}_3^2(eta)$	$\hat{C}_3(\gamma)$
A1g	1	1	1	1	1
A2g	1	1	1	1	1
Eg	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{pmatrix} 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
T1g	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \left(\begin{array}{ccc} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{array}\right) $
T2g	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$   \begin{pmatrix}     0 & 1 & 0 \\     0 & 0 & -1 \\     -1 & 0 & 0   \end{pmatrix} $
A1u	1	1	1	1	1
A2u	1	1	$1 \mid$	$\lfloor 1 \rfloor$	$1$
Eu	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
T1u	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$\left  \begin{array}{ccc} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{array} \right $
T2u	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \left  \begin{array}{cccc} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{array} \right  $

Oh	$\hat{C}_3^2(\gamma)$	$\hat{C}_3(\delta)$	$\hat{C}_3^2(\delta)$	$\hat{C}_2(xzp)$	$\hat{C}_2(xzm)$
A1g	1	1	1	1	1
A2g	1	1	1	-1	-1
Eg	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
T1g	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $
T2g	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} $
A1u	1	1	1	1	
A2u	1	1		-1	-1
Eu	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$ $\begin{pmatrix} 0 & 0 & -1 \end{pmatrix}$
T1u	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $
T2u	$ \begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} $

Oh	$\hat{C}_2(xyp)$	$\hat{C}_2(xym)$	$\hat{C}_2(yzp)$	$\hat{C}_2(yzm)$	$\hat{i} \mid$
A1g	1	1	1	1	1
A2g	-1	-1	-1	-1	1
Eg	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
T1g	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
T2g	$ \begin{bmatrix} \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}$	$\left( egin{array}{ccc} 0 & -1 & 0 \ 1 & 0 & 0 \ 0 & 0 & 1 \ 0 & 1 & 0 \end{array}  ight)$	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
A1u	1	1	1	1	$\begin{bmatrix} & & & \\ & & -1 \end{bmatrix}$
A2u	-1	-1	-1	-1	-1
Eu	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
T1u	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix} $	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $
T2u	$ \left  \begin{array}{cccc} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{array} \right  $	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} $

Oh	$\hat{S}_4(x)$	$\hat{\sigma}_h(x)$	$\hat{S}_4^3(x)$	$\hat{S}_4(y)$	$\hat{\sigma}_h(y)$
A1g	1	1	1	1	1
A2g	-1	1	-1	-1	1
Eg	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$
T1g	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2g	$     \begin{pmatrix}       -1 & 0 & 0 \\       0 & 0 & -1 \\       0 & 1 & 0     \end{pmatrix}   $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
A1u	-1	-1	-1	-1	-1
A2u	1	-1	1	1	-1
Eu	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$ $\begin{pmatrix} -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$
T1u	$   \begin{pmatrix}     -1 & 0 & 0 \\     0 & 0 & -1 \\     0 & 1 & 0   \end{pmatrix} $	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} $
T2u	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & 1 & 0 \end{pmatrix} \mid$	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} \mid$	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} $

Oh	$\hat{S}_4^3(y)$	$\hat{S}_4(z)$	$\hat{\sigma}_h(z)$	$\hat{S}_4^3(z)$	$\hat{S}_6(\alpha)$
A1g	1	1	1	1	1
A2g	-1	-1	1	-1	1
Eg	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
T1g	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$
T2g	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$
A1u	-1	-1	-1	-1	-1
A2u	1	1	-1	1	-1
Eu	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
T1u	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} $
T2u	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \mid$	$\begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} $

Oh	$\hat{S}_6^5(lpha)$	$\hat{S}_6(eta)$	$\hat{S}^{5}_{6}(eta)$	$\hat{S}_6(\gamma)$	$\hat{S}_6^5(\gamma)$
$\overline{A1g}$	1	1	1	1	1
A2g	1	1	1	1	1
Eg	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$ \begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix} $ $ \begin{pmatrix} 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
T1g	$ \begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} $
T2g	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} $
A1u	-1	-1	-1	-1	-1
A2u	-1	-1	-1	-1	-1
Eu	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
T1u	$\begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$
T2u	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & 1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$     \begin{pmatrix}       0 & -1 & 0 \\       0 & 0 & 1 \\       1 & 0 & 0     \end{pmatrix}     $

Oh	$\hat{S}_6(\delta)$	$\hat{S}^{5}_{6}(\delta)$	$\hat{\sigma}_d(xzp)$	$\hat{\sigma}_d(xzm)$	$\hat{\sigma}_d(xyp)$
A1g	1	1	1	1	1
A2g	1	1	-1	-1	-1
Eg	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$ $\begin{pmatrix} 0 & -1 & 0 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$
T1g	$     \begin{pmatrix}       0 & -1 & 0 \\       0 & 0 & 1 \\       -1 & 0 & 0     \end{pmatrix}   $	$\begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$ \left  \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} \right  $	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2g	$ \left(\begin{array}{cccc} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{array}\right) $	$ \begin{pmatrix} 0 & 0 & -1 \\ -1 & 0 & 0 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $
A1u	-1	-1	-1	-1	-1
A2u	-1	-1	1	1	1
Eu	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$
T1u	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} $
T2u	$ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & 0 \\ 1 & 0 & 0 \end{pmatrix} $	$ \left  \begin{pmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{pmatrix} \right  $	$ \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix} $

Oh	$\hat{\sigma}_d(xym)$	$\hat{\sigma}_d(yzp)$	$\hat{\sigma}_d(yzm)$
A1g	1	1	1
A2g	-1	-1	-1
Eg	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} \frac{1}{2} & -\frac{\sqrt{3}}{2} \\ -\frac{\sqrt{3}}{2} & -\frac{1}{2} \end{pmatrix}$
T1g	$\begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $\begin{pmatrix} 0 & 1 & 0 \end{pmatrix}$	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$	$ \left(  \begin{array}{ccc} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{array}  \right) $
T2g	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$
A1u	-1	-1	$\begin{pmatrix} & & & \\ & & -1 \end{pmatrix}$
A2u	1	1	1
Eu	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$	$\begin{pmatrix} -\frac{1}{2} & \frac{\sqrt{3}}{2} \\ \frac{\sqrt{3}}{2} & \frac{1}{2} \end{pmatrix}$
T1u	$\begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix}$	$ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} $
T2u	$\begin{pmatrix} 0 & -1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}$	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} $	$ \begin{pmatrix} -1 & 0 & 0 \\ 0 & 0 & -1 \\ 0 & -1 & 0 \end{pmatrix} $

$$\begin{array}{c|cccc} \mathbf{I} & & & & \hat{E} \\ \hline A & & & & 1 \\ T1 & & \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ T2 & & \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ G & & \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \\ H & & \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

 $-0.5 - 0.1\sqrt{5}$ 

 $0.5\sqrt{0.1\sqrt{5}+0.5}$ 

 $0.25 - 0.05\sqrt{5}$ 

 $-0.25 + 0.25\sqrt{5}$ 

0

0

H

 $0.5\sqrt{0.5\sqrt{5}} + 2.5$ 

0

0

 $-0.25\sqrt{5} - 0.25$   $-0.5\sqrt{2.5 - 0.5\sqrt{5}}$ 

 $0.5\sqrt{2.5} - 0.5\sqrt{5}$   $-0.25\sqrt{5} - 0.25$ 

 $-0.5\sqrt{0.5\sqrt{5}} + 2.5 \quad -0.25 + 0.25\sqrt{5}$ 

 $0.1 - \frac{\sqrt{5}}{5} \\ 0.1\sqrt{2\sqrt{5} + 5}$ 

 $-0.2\sqrt{10-2\sqrt{5}}$ 

G

Ι	$\hat{C}_2(14)$	
$\overline{A}$		1
T1	$ \begin{pmatrix} 1 & 0 \\ 0 & -1 \\ 0 & 0 \end{pmatrix} $	$\begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix}$
T2	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \\ 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ -1 \end{pmatrix}$
G	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 0 \\ 0 \\ -1 \end{pmatrix}$
Н	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$	$ \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ -1 \end{pmatrix} $

Ih	$\hat{E}$
$\overline{Ag}$	1
T1g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
T2g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Gg	$ \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} $
Hg	/1 0 0 0 0\
	$     \begin{pmatrix}       0 & 0 & 0 & 1 & 0 \\       0 & 0 & 0 & 0 & 1     \end{pmatrix}   $
Au	1
T1u	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
T2u	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Gu	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$
Hu	$ \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{pmatrix} $
	$(0 \ 0 \ 0 \ 0 \ 1)$

```
{\rm Ih}
                                                                                                                                                              \hat{C}_{5}(2)
 Ag
                                                                                        -0.25 + 0.25\sqrt{5} -0.5\sqrt{0.1\sqrt{5} + 0.5} \sqrt{0.1\sqrt{5} + 0.5}
T1g
                                                                                       0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                     0.05\sqrt{5} + 0.75
                                                                                                                                                0.5 - 0.1\sqrt{5}
                                                                                                                                                       \frac{\sqrt{5}}{5}
                                                                                         -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                      0.5 - 0.1\sqrt{5}
                                                                                                              -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                             0.1\sqrt{5} + 0.5
T2g
                                                                                                              -0.25\sqrt{5} - 0.25 -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                       0.1\sqrt{5} + 0.5
                                                                                                             0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                           0.75 - 0.05\sqrt{5}
                                                                                  0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                            -\sqrt{0.5-0.1\sqrt{5}}
                                                       -0.25\sqrt{5}-0.25
                                                                                                                          0
                                                      -0.5\sqrt{0.5-0.1\sqrt{5}} -0.25+0.15\sqrt{5}
                                                                                                                -\sqrt{0.1\sqrt{5}+0.5}
Gg
                                                                                     \sqrt{0.1\sqrt{5}+0.5}
                                                                                                               -0.25 + 0.25\sqrt{5}
                                                                                                                                           0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                              -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                           -0.15\sqrt{5}-0.25
                                            0.04\sqrt{5} \left( \sqrt{5} + 5 \right)
                                                                       -0.2\sqrt{7.5} - 1.5\sqrt{5} -0.04\sqrt{5}\left(-5 + \sqrt{5}\right) -0.2\sqrt{1.5\sqrt{5}} + 7.5
                       -0.2
                                                                        -0.1\sqrt{5.5\sqrt{5}+12.5}
              0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                                           0.2\sqrt{5-2\sqrt{5}}
                                             0.35 - 0.05\sqrt{5}
                \sqrt{0.3 - 0.06\sqrt{5}}
                                           0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                           -0.25 + 0.15\sqrt{5}
Hg
                                                                                                            0.2\sqrt{2\sqrt{5}} + 5
                                                                           -0.2\sqrt{2\sqrt{5}+5}
                                                                                                           0.05\sqrt{5} + 0.35
                                                                                                                                       -0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                                        0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                          -0.15\sqrt{5} - 0.25
                                                                                    \frac{\sqrt{5}}{5}
                 \sqrt{0.06\sqrt{5}+0.3}
 Au
                                                                                       -0.25 + 0.25\sqrt{5} -0.5\sqrt{0.1\sqrt{5}} + 0.5 \sqrt{0.1\sqrt{5}} + 0.5
                                                                                      0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                    0.05\sqrt{5} + 0.75
T1u
                                                                                                                                                0.5 - 0.1\sqrt{5}
                                                                                        -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                      0.5 - 0.1\sqrt{5}
                                                                                                              -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                             0.1\sqrt{5} + 0.5
T2u
                                                                                                             -0.25\sqrt{5} - 0.25 -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                       \sqrt{0.5-0.1\sqrt{5}}
                                                                                        0.1\sqrt{5} + 0.5
                                                                                                             0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                                           0.75 - 0.05\sqrt{5}
                                                                                  0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                            -\sqrt{0.5-0.1\sqrt{5}}
                                                       -0.25\sqrt{5}-0.25
                                                     -0.5\sqrt{0.5}-0.1\sqrt{5}
                                                                                   -0.25 + 0.15\sqrt{5}
                                                                                                                -\sqrt{0.1\sqrt{5}+0.5}
Gu
                                                                                     \sqrt{0.1\sqrt{5} + 0.5}
                                                                                                               -0.25 + 0.25\sqrt{5}
                                                                                                                                           0.5\sqrt{0.1\sqrt{5}+0.5}
                                                        \sqrt{0.5-0.1\sqrt{5}}
                                                                                                             -0.5\sqrt{0.1\sqrt{5}+0.5} -0.15\sqrt{5}-0.25
                                            0.04\sqrt{5}(\sqrt{5}+5)
                                                                         -0.2\sqrt{7.5-1.5\sqrt{5}}
                                                                                                      -0.04\sqrt{5}\left(-5+\sqrt{5}\right) -0.2\sqrt{1.5\sqrt{5}+7.5}
                                                                        -0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                           0.2\sqrt{5-2\sqrt{5}}
                                           0.35 - 0.05\sqrt{5}
                                           0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                            0.2\sqrt{2\sqrt{5}+5}
                                                                           -0.25 + 0.15\sqrt{5}
                                                                           -0.2\sqrt{2\sqrt{5}} + 5
                                                                                                           0.05\sqrt{5} + 0.35
                                                                                                                                       -0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                                        0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                         -0.15\sqrt{5} - 0.25
```

```
\mathbf{Ih}
                                                                                                                                                             \hat{C}_{2}(8)
 Aq
                                                                                       -0.25 + 0.25\sqrt{5} -0.5\sqrt{0.1\sqrt{5} + 0.5} \sqrt{0.1\sqrt{5} + 0.5}
T1g
                                                                                      -0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                 -0.75 - 0.05\sqrt{5}
                                                                                                                                              -0.5 + 0.1\sqrt{5}
                                                                                                                                                     -\frac{\sqrt{5}}{5}
                                                                                         \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                 -0.5 + 0.1\sqrt{5}
                                                                                                              \sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                                           -0.5 - 0.1\sqrt{5}
T2g
                                                                                                             -0.25\sqrt{5} - 0.25 -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                      -0.5 - 0.1\sqrt{5} -0.5\sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                                          -0.75 + 0.05\sqrt{5}
                                                            -0.25\sqrt{5} - 0.25 0.5\sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                       0
                                                                                                                                           -\sqrt{0.5}-0.1\sqrt{5}
                                                           0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                      0.25 - 0.15\sqrt{5}
                                                                                                                  \sqrt{0.1\sqrt{5}+0.5}
Gq
                                                                                        \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                 -0.25 + 0.25\sqrt{5}
                                                                                                                                          0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                0.5\sqrt{0.1\sqrt{5}+0.5}
                                                             -\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                                          0.25 + 0.15\sqrt{5}
                                          0.04\sqrt{5}\left(\sqrt{5}+5\right)
                                                                         -0.2\sqrt{7.5} - 1.5\sqrt{5}
                                                                                                      -0.04\sqrt{5}\left(-5+\sqrt{5}\right) -0.2\sqrt{1.5\sqrt{5}}+7.5
             0.04\sqrt{5}\left(\sqrt{5}+5\right)
                                                                                                                                           0.2\sqrt{5-2\sqrt{5}}
                                           0.35 - 0.05\sqrt{5}
                                                                        -0.1\sqrt{5.5\sqrt{5}} + 12.5
                                          -0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                         0.25 - 0.15\sqrt{5}
                                                                                                          -0.2\sqrt{2\sqrt{5}+5}
Hg
                                                                            -0.2\sqrt{2\sqrt{5}+5}
                                                                                                         0.05\sqrt{5} + 0.35
                                                                                                                                      -0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                                        -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                          0.25 + 0.15\sqrt{5}
 Au
                                                                                       -0.25 + 0.25\sqrt{5} -0.5\sqrt{0.1\sqrt{5}} + 0.5 \sqrt{0.1\sqrt{5}} + 0.5
                                                                                     -0.5\sqrt{0.1\sqrt{5}+0.5} -0.75-0.05\sqrt{5}
T1u
                                                                                                                                               -0.5 + 0.1\sqrt{5}
                                                                                        \sqrt{0.1\sqrt{5}+0.5}
                                                                                                               -0.5 + 0.1\sqrt{5}
                                                                                                              \sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                                         -0.5 - 0.1\sqrt{5}
                                                                                                            -0.25\sqrt{5} - 0.25 -0.5\sqrt{0.5 - 0.1\sqrt{5}}
T2u
                                                                                      -0.5 - 0.1\sqrt{5} -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                                          -0.75 + 0.05\sqrt{5}
                                                            -0.25\sqrt{5} - 0.25 0.5\sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                                            -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                  \sqrt{0.1\sqrt{5}+0.5}
                                                           0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                       0.25 - 0.15\sqrt{5}
Gu
                                                                                        \sqrt{0.1\sqrt{5}+0.5}
                                                                                                              -0.25 + 0.25\sqrt{5} 0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                            -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                              0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                                          0.25 + 0.15\sqrt{5}
                                                                         -0.2\sqrt{7.5-1.5\sqrt{5}}
                                            0.04\sqrt{5}\left(\sqrt{5}+5\right)
                                                                                                       -0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                                                                                                     -0.2\sqrt{1.5\sqrt{5}} + 7.5
                                           0.35 - 0.05\sqrt{5}
                                                                        -0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                           0.2\sqrt{5-2\sqrt{5}}
                                                                         0.25 - 0.15\sqrt{5}
                                                                                                          -0.2\sqrt{2\sqrt{5}+5}
                                                                            -0.2\sqrt{2\sqrt{5}+5}
                                                                                                         0.05\sqrt{5} + 0.35
                                                                                                                                      -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                        -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                          0.25 + 0.15\sqrt{5}
```

Ih	$\hat{C}_2(14)$
Ag	1
T1g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2g	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$ $/1  0  0  0$
Gg	$ \begin{pmatrix} 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} $
Hg	$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix}$
Au	1
T1u	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2u	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Gu	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$
Hu	$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix}$

$\mathbf{Ih}$	$\hat{i}$
$\overline{Ag}$	1
T1g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
T2g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Gg	$\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$
Hg	$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$
Au	-1
T1u	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2u	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Gu	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$
Hu	$\begin{pmatrix} -1 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix}$

```
\hat{S}_10^7(2)
 {\rm Ih}
 \overline{Ag}
                                                                                            -0.25 + 0.25\sqrt{5} -0.5\sqrt{0.1\sqrt{5} + 0.5}
                                                                                                                                                       \sqrt{0.1}\sqrt{5} + 0.5
T1g
                                                                                           0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                           0.05\sqrt{5} + 0.75
                                                                                                                                                        0.5 - 0.1\sqrt{5}
                                                                                                                                                               \frac{\sqrt{5}}{5}
                                                                                              -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                             0.5 - 0.1\sqrt{5}
                                                                                                                    -\sqrt{0.5}-0.1\sqrt{5}
                                                                                                                                                     0.1\sqrt{5} + 0.5
T2g
                                                                                                                    -0.25\sqrt{5}-0.25
                                                                                                                                               -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                            0.1\sqrt{5} + 0.5
                                                                                                                   0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                   0.75 - 0.05\sqrt{5}
                                                                                    -0.5\sqrt{0.5-0.1\sqrt{5}}
                                                         0.25 + 0.25\sqrt{5}
                                                                                                                                                   \sqrt{0.5-0.1\sqrt{5}}
                                                                                                                               0
                                                        0.5\sqrt{0.5-0.1}\sqrt{5}
                                                                                        0.25 - 0.15\sqrt{5}
                                                                                                                      \sqrt{0.1\sqrt{5}+0.5}
 Gg
                                                                                       -\sqrt{0.1\sqrt{5}+0.5}
                                                                    0
                                                                                                                     0.25 - 0.25\sqrt{5}
                                                                                                                                                 -0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                         -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                   0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                   0.25 + 0.15\sqrt{5}
                                               0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                                               -0.2\sqrt{1.5\sqrt{5}} + 7.5
                        -0.2
                                                                             -0.2\sqrt{7.5} - 1.5\sqrt{5}
                                                                                                            -0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                                                                                                                   0.2\sqrt{5-2\sqrt{5}}
               0.04\sqrt{5}(\sqrt{5}+5)
                                                0.35 - 0.05\sqrt{5}
                                                                            -0.1\sqrt{5.5\sqrt{5}} + 12.5
                                              0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                                           \sqrt{5}
                \sqrt{0.3-0.06\sqrt{5}}
Hg
                                                                               -0.25 + 0.15\sqrt{5}
                                                                                                                 0.2\sqrt{2\sqrt{5}} + 5
                                                                                -0.2\sqrt{2\sqrt{5}+5}
               0.04\sqrt{5}(-5+\sqrt{5})
                                                                                                                 0.05\sqrt{5} + 0.35
                                                                                                                                              -0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                                                                                 -0.15\sqrt{5} - 0.25
                                                                                         \frac{\sqrt{5}}{5}
                  \sqrt{0.06\sqrt{5}+0.3}
                                                                                                              0.1\sqrt{12.5-5.5\sqrt{5}}
 Au
                                                                                                                       0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                    -\sqrt{0.1\sqrt{5}+0.5}
                                                                                            0.25 - 0.25\sqrt{5}
                                                                                          -0.5\sqrt{0.1\sqrt{5}+0.5}
T1u
                                                                                                                       -0.75 - 0.05\sqrt{5}
                                                                                                                                                      -0.5 + 0.1\sqrt{5}
                                                                                             \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                            -\frac{\sqrt{5}}{5}
                                                                                                                          -0.5 + 0.1\sqrt{5}
                                                                                                                       \sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                     -0.5 - 0.1\sqrt{5}
T2u
                                                                                                                      0.25 + 0.25\sqrt{5}
                                                                                                                                                  0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                              \sqrt{0.5-0.1\sqrt{5}}
                                                                                           -0.5 - 0.1\sqrt{5}
                                                                                                                    -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                                                   -0.75 + 0.05\sqrt{5}
                                                                                                                                                   -\sqrt{0.5-0.1\sqrt{5}}
                                                          -0.25\sqrt{5}-0.25
                                                                                       0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                        -0.5\sqrt{0.5}-0.1\sqrt{5}
                                                                                                                      -\sqrt{0.1\sqrt{5}+0.5}
                                                                                        -0.25 + 0.15\sqrt{5}
Gu
                                                                                         \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                  0.5\sqrt{0.1\sqrt{5}} + 0.\overline{5}
                                                                     0
                                                                                                                     -0.25 + 0.25\sqrt{5}
                                                            \sqrt{0.5-0.1\sqrt{5}}
                                                                                                                   -0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                                                   -0.15\sqrt{5} - 0.25
                                                  -0.04\sqrt{5}(\sqrt{5}+5)
                                                                                    \sqrt{0.3-0.06\sqrt{5}}
                                                                                                                 0.04\sqrt{5} \left(-5+\sqrt{5}\right)
                                                                                                                                                   \sqrt{0.06\sqrt{5}+0.3}
                              0.2
                                                                                 0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                                   -0.2\sqrt{5-2\sqrt{5}}
                   -0.04\sqrt{5}(\sqrt{5}+5)
                                                    -0.35 + 0.05\sqrt{5}
                  -0.2\sqrt{7.5-1.5\sqrt{5}}
                                                  -0.1\sqrt{5.5\sqrt{5}+12.5}
Hu
                                                                                     0.25 - 0.15\sqrt{5}
                                                                                                                   -0.2\sqrt{2\sqrt{5}} + 5
                  0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                                                     0.2\sqrt{2\sqrt{5}} + 5
                                                                                                                   -0.35 - 0.05\sqrt{5}
                                                                                                                                                0.1\sqrt{12.5} - 5.5\sqrt{5}
                    -0.2\sqrt{1.5\sqrt{5}+7.5}
                                                                                                                -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                                   0.25 + 0.15\sqrt{5}
```

```
\hat{S}_10^9(2)
 {\rm Ih}
 Ag
                                                                                            -0.25\sqrt{5} - 0.25 -0.5\sqrt{0.5 - 0.1\sqrt{5}} \sqrt{0.5 - 0.1\sqrt{5}}
T1g
                                                                                           0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                          0.75 - 0.05\sqrt{5}
                                                                                                                                                       0.1\sqrt{5} + 0.5
                                                                                                                                                            -\frac{\sqrt{5}}{5}
                                                                                             -\sqrt{0.5}-0.1\sqrt{5}
                                                                                                                            0.1\sqrt{5} + 0.5
                                                                                                                      \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                     0.5-0.1\sqrt{5}
T2g
                                                                                            \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                     -0.25 + 0.25\sqrt{5}
                                                                                                                                                 0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                           0.5 - 0.1\sqrt{5}
                                                                                                                   -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                   0.05\sqrt{5} + 0.75
                                                                                       0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                 -\sqrt{0.1\sqrt{5}+0.5}
                                                           0.25 - 0.25\sqrt{5}
                                                         -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                        0.25 + 0.15\sqrt{5}
                                                                                                                     \sqrt{0.5-0.1\sqrt{5}}
Gg
                                                                                        -\sqrt{0.5}-0.1\sqrt{5}
                                                                                                                                               -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                    0.25 + 0.25\sqrt{5}
                                                            \sqrt{0.1\sqrt{5}+0.5}
                                                                                                  \sqrt{5}
                                                                                                                  0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                  0.25 - 0.15\sqrt{5}
                                                                                                                                                \sqrt{0.3-0.06\sqrt{5}}
                            -0.2
                                                 0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                                                -0.2\sqrt{1.5\sqrt{5}} + 7.5
                                                                                                              -0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                                                 -0.2\sqrt{2\sqrt{5}+5}
                 0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                   0.05\sqrt{5} + 0.35
                                                                                 0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                -0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                  -0.15\sqrt{5} - 0.25
                    \sqrt{0.06\sqrt{5}+0.3}
                                                                                                                  0.2\sqrt{5}-2\sqrt{5}
                                                                                                                                                        -\sqrt{5}
Hg
                                                                                   -0.2\sqrt{5-2\sqrt{5}}
                  -0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                 0.35 - 0.05\sqrt{5}
                                                                                                                                              -0.1\sqrt{5.5\sqrt{5}}+12.5
                                                                                                               0.1\sqrt{5.5\sqrt{5}+12.5}
                    0.2\sqrt{7.5} - 1.5\sqrt{5}
                                                                                                                                                -0.25 + 0.15\sqrt{5}
 Au
                                                                                                                       0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                  -\sqrt{0.5-0.1\sqrt{5}}
                                                                                            0.25 + 0.25\sqrt{5}
                                                                                           -0.5\sqrt{0.5-0.1\sqrt{5}}
T1u
                                                                                                                       -0.75 + 0.05\sqrt{5}
                                                                                                                                                    -0.5-0.1\sqrt{5}
                                                                                                                         -0.5-0.1\sqrt{5}
                                                                                                                    -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                   -0.5 + 0.1\sqrt{5}
T2u
                                                                                                                    0.25 - 0.25\sqrt{5}
                                                                                                                                               -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                              0.1\sqrt{5} + 0.5
                                                                                             -0.5 + 0.1\sqrt{5}
                                                                                                                  0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                                                 -0.75 - 0.05\sqrt{5}
                                                                                    -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                                                    \sqrt{0.1\sqrt{5}+0.5}
                                                         -0.25 + 0.25\sqrt{5}
                                                        0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                       -0.15\sqrt{5}-0.25
                                                                                                                     -\sqrt{0.5-0.1\sqrt{5}}
Gu
                                                                                        \sqrt{0.5-0.1\sqrt{5}}
                                                                                                                     -0.25\sqrt{5} - 0.25
                                                                                                                                                 0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                         -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                   -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                                                  -0.25 + 0.15\sqrt{5}
                                             -0.04\sqrt{5}\left(-5+\sqrt{5}\right)
                                                                                  \sqrt{0.06\sqrt{5}+0.3}
                                                                                                                0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                                               -0.2\sqrt{7.5-1.5\sqrt{5}}
                                                -0.35 - 0.05\sqrt{5}
                                                                              -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                                  0.2\sqrt{2\sqrt{5}+5}
                                               0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                  -0.2\sqrt{5}-2\sqrt{5}
               -0.2\sqrt{1.5\sqrt{5}} + 7.5
                                                                                  0.25 + 0.15\sqrt{5}
               0.04\sqrt{5}\left(\sqrt{5}+5\right)
                                                                                  0.2\sqrt{5}-2\sqrt{5}
                                                                                                                 -0.35 + 0.05\sqrt{5}
                                                                                                                                               0.1\sqrt{5.5\sqrt{5}} + 12.5
                                                                                           \frac{\sqrt{5}}{5}
                                                                                                              -0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                                  0.25 - 0.15\sqrt{5}
```

```
\mathbf{Ih}
                                                                                                                                                                            \hat{\sigma}(8)
 \overline{Ag}
                                                                                                                           -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                              -0.25 + 0.25\sqrt{5}
                                                                                                                                                          \sqrt{0.1\sqrt{5}+0.5}
T1g
                                                                                              -0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                             -0.75 - 0.05\sqrt{5}
                                                                                                                                                          -0.5 + 0.1\sqrt{5}
                                                                                                                                                                 -\frac{\sqrt{5}}{5}
                                                                                                                               -0.5 + 0.1\sqrt{5}
                                                                                                                        \sqrt{0.5 - 0.1\sqrt{5}}
                                                                                                                                                       -0.5 - 0.1\sqrt{5}
                                                                                                                      -0.25\sqrt{5} - 0.25
T2g
                                                                                               0.5 - 0.1\sqrt{5}
                                                                                                                                                   -0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                    -0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                             -0.5 - 0.1\sqrt{5}
                                                                                                                                                      -0.75 + 0.05\sqrt{5}
                                                                                     -0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                       \sqrt{0.5-0.1\sqrt{5}}
                                                         0.25 + 0.25\sqrt{5}
                                                                                                                       -\sqrt{0.1\sqrt{5}+0.5}
                                                                                       -0.25 + 0.15\sqrt{5}
 Gg
                                                                                       -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                       0.25 - 0.25\sqrt{5}
                                                                                                                                                    -0.5\sqrt{0.1\sqrt{5}}+0.5
                                                                                                                    -0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                                                      -0.15\sqrt{5}-0.25
                                                0.04\sqrt{5}(\sqrt{5}+5)
                                                                                                                                                  -0.2\sqrt{1.5\sqrt{5}+7.5}
                        -0.2
                                                                                -0.2\sqrt{7.5} - 1.5\sqrt{5}
                                                                                                                -0.04\sqrt{5}\left(-5+\sqrt{5}\right)
               0.04\sqrt{5}\left(\sqrt{5}+5\right)
                                                                               -0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                                      0.2\sqrt{5-2\sqrt{5}}
                                                  0.35 - 0.05\sqrt{5}
                                                                                                                                                             -\frac{\sqrt{5}}{5}
                                               -0.1\sqrt{5.5\sqrt{5}} + 12.5
                                                                                   0.25 - 0.15\sqrt{5}
Hg
                                                                                                                    -0.2\sqrt{2\sqrt{5}} + 5
                                                                                   -0.2\sqrt{2\sqrt{5}+5}
                                                                                                                    0.05\sqrt{5} + 0.35
                                                                                                                                                  -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                           -\frac{\sqrt{5}}{5}
                                                                                                                -0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                                      0.25 + 0.15\sqrt{5}
 Au
                                                                                                                           0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                 0.25 - 0.25\sqrt{5}
                                                                                                                                                       -\sqrt{0.1\sqrt{5}+0.5}
T1u
                                                                                               0.5\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                             0.05\sqrt{5} + 0.75
                                                                                                                                                          0.5 - 0.1\sqrt{5}
                                                                                                                                                                 \frac{\sqrt{5}}{5}
                                                                                                 -\sqrt{0.1\sqrt{5}+0.5}
                                                                                                                              0.5 - 0.1\sqrt{5}
                                                                                                                          -\sqrt{0.5}-0.1\sqrt{5}
                                                                                                                                                          0.1\sqrt{5} + 0.5
T2u
                                                                                                    0.5 - 0.1 \sqrt{5}
                                                                                                                                                      0.5\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                           0.25 + 0.25\sqrt{5}
                                                                                                 0.1\sqrt{5} + 0.5
                                                                                                                         0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                        0.75 - 0.05\sqrt{5}
                                                                 -0.25\sqrt{5} - 0.25
                                                                                            0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                                       -\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                                     0
                                                                0.5\sqrt{0.5-0.1\sqrt{5}}
                                                                                                                            \sqrt{0.1\sqrt{5}+0.5}
                                                                                               0.25 - 0.15\sqrt{5}
Gu
                                                                                                \sqrt{0.1\sqrt{5}+0.5}
                                                                                                                          -0.25 + 0.25\sqrt{5}
                                                                                                                                                      0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                  -\sqrt{0.5} - 0.1\sqrt{5}
                                                                                                                         0.5\sqrt{0.1\sqrt{5}} + 0.5
                                                                                                                                                        0.25 + 0.15\sqrt{5}
                                                        -0.04\sqrt{5}(\sqrt{5}+5)
                                     0.2
                                                                                          \sqrt{0.3-0.06\sqrt{5}}
                                                                                                                     0.04\sqrt{5} \left(-5+\sqrt{5}\right)
                                                                                                                                                       \sqrt{0.06\sqrt{5}+0.3}
                                                                                       0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                                                                                       -0.2\sqrt{5-2\sqrt{5}}
                          -0.04\sqrt{5}(\sqrt{5}+5)
                                                          -0.35 + 0.05\sqrt{5}
Hu
                             \sqrt{0.3-0.06\sqrt{5}}
                                                        0.1\sqrt{5.5\sqrt{5}+12.5}
                                                                                         -0.25 + 0.15\sqrt{5}
                                                                                                                         0.2\sqrt{2\sqrt{5}} + 5
                                                                                           0.2\sqrt{2\sqrt{5}+5}
                                                                                                                       -0.35 - 0.05\sqrt{5}
                                                                                                                                                    0.1\sqrt{12.5} - 5.5\sqrt{5}
                                                                                                   \frac{\sqrt{5}}{5}
                             \sqrt{0.06\sqrt{5}+0.3}
                                                                                                                     0.1\sqrt{12.5-5.5\sqrt{5}}
                                                                                                                                                      -0.15\sqrt{5} - 0.25
```

Ih	$\hat{\sigma}(14)$
$\overline{Ag}$	1
T1g	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
T2g	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$
Gg	$\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$
Hg	$ \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & -1 \end{pmatrix} $
Au	-1
T1u	$\begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
T2u	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
Gu	$ \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix} $
Hu	$ \begin{pmatrix} -1 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} $