## OMP2

- 1. Build  $h_p^q$  and  $\overline{g}_{pq}^{rs}$  in the Hartree-Fock spin-orbital basis.
- 2. Build an empty array of amplitudes,  $t_{ab}^{ij}=0$ .
- 3. Build the Fock matrix.

$$f_p^q = h_p^q + \overline{g}_{pi}^{qi} \tag{1}$$

4. Build the off-diagonal Fock matrix and the orbital energies.

$$\epsilon_p = f_p^p \qquad \qquad f_p'^q = (1 - \delta_p^q) f_p^q \qquad (2)$$

5. Update the amplitudes.

$${}^{(1)}t^{ij}_{ab} = (\mathcal{E}^{ij}_{ab})^{-1} \left( \overline{g}^{ij}_{ab} + P_{(a/b)} f'^{c}_{a} t^{ij}_{cb} - P^{(i/j)} f'^{i}_{k} t^{kj}_{ab} \right)$$

$$\tag{3}$$

6. Build the one- and two-particle density matrices.

$$\gamma_q^p = \tilde{\gamma}_q^p + \mathring{\gamma}_q^p \qquad \qquad \gamma_{rs}^{pq} = \tilde{\gamma}_{rs}^{pq} + P_{(r/s)}^{(p/q)} \tilde{\gamma}_r^p \mathring{\gamma}_s^q + P_{(r/s)} \mathring{\gamma}_r^p \mathring{\gamma}_s^q \qquad \qquad \mathring{\gamma}_q^p = \begin{cases} \delta_j^i & \text{for } p = i, \ q = j \\ 0 & \text{otherwise} \end{cases}$$
(4)

$$\tilde{\gamma}^{a}_{b} = \frac{1}{2} t^{ac*}_{ij} t^{ij}_{bc} \qquad \qquad \tilde{\gamma}^{i}_{j} = -\frac{1}{2} t^{ab*}_{jk} t^{ik}_{ab} \qquad \qquad \tilde{\gamma}^{ab}_{cd} = \frac{1}{2} t^{ab*}_{ij} t^{ij}_{cd} \qquad \qquad \tilde{\gamma}^{ij}_{kl} = \frac{1}{2} t^{ab*}_{kl} t^{ij}_{ab} \qquad \qquad (5)$$

$$\tilde{\gamma}_{ib}^{aj} = -\tilde{\gamma}_{bi}^{aj} = -\tilde{\gamma}_{ib}^{ja} = \tilde{\gamma}_{bi}^{ja} = t_{ik}^{ac*} t_{cb}^{kj} \qquad \qquad \tilde{\gamma}_{ij}^{ab} = t_{ij}^{ab*} \qquad \qquad \tilde{\gamma}_{ab}^{ij} = t_{ab}^{ij} \qquad \qquad (6)$$

7. Compute the Newton-Raphson step.

$$x_a^i = \frac{(\mathbf{F} - \mathbf{F}^\dagger)_a^i}{\epsilon_i - \epsilon_a} \qquad (\mathbf{F})_p^q \equiv h_p^r \gamma_r^q + \frac{1}{2} \overline{g}_{pr}^{st} \gamma_{st}^{qr}$$
 (7)

8. Build the Newton-Raphson orbital rotation matrix.

$$\mathbf{U} = \exp(\mathbf{X} - \mathbf{X}^{\dagger}) \qquad \qquad \mathbf{X}_{\text{vo}} = [x_a^i]$$
 (8)

9. Rotate the spin-orbital coefficients.

$$\mathbf{C} \leftarrow \mathbf{C}\mathbf{U}$$
 (9)

10. Transform the one- and two-electon integrals to the spin-orbital basis using the new coefficient matrix.

$$h_{p}^{q} = \sum_{\mu\nu} C_{\mu p}^{*} h_{\mu\nu} C_{\nu q} \qquad \bar{g}_{pq}^{rs} = \sum_{\mu\nu\rho\sigma} C_{\mu p}^{*} C_{\nu q}^{*} \langle \mu\nu || \rho\sigma \rangle C_{\rho r} C_{\sigma s}$$
 (10)

11. Evaluate the energy.

$$E = h_p^q \gamma_q^p + \frac{1}{4} \overline{g}_{pq}^{rs} \gamma_{rs}^{pq} \tag{11}$$

12. If the energy is converged, quit. Otherwise, return to step 3.