

CHEM 8950

ADVANCED QUANTUM CHEMISTRY

This assignment is due May 1 at 5PM by email.

Coupled Cluster with Double Excitations (CCD)

CCD energy equation:

$$E_c = \langle \Phi | H_c (1 + T_2 + \frac{1}{2} T_2^2) | \Phi \rangle$$

$$= \frac{\left(\begin{array}{c} \text{diagram: } \otimes + \text{diagram: } \text{---} \end{array} \right)}{\left(1 + \begin{array}{c} \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} \end{array} \right)} = \begin{array}{c} \text{diagram: } \text{---} \end{array}$$

CCD amplitude equation:

$$t_{ab}^{ij} = (\mathcal{E}_{ab}^{ij})^{-1} \langle \Phi_{ij}^{ab} | (H_c - f_p^p \tilde{a}_p^p) \exp(T_2) | \Phi \rangle_L$$

$$\mathcal{E}_{ab}^{ij} \equiv \epsilon_i + \epsilon_j - \epsilon_a - \epsilon_b$$

$$= \frac{\left(\begin{array}{c} \text{diagram: } \otimes + \text{diagram: } \text{---} \end{array} \right)}{\left(1 + \begin{array}{c} \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} \end{array} \right)}$$

$$= \begin{array}{c} \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} \\ + \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} + \text{diagram: } \text{---} \end{array}$$

Determine the programmable equations from the diagrams above. For any terms that have $\hat{P}_{(\dots)}^{(\dots)}$ it will need to be explicitly expanded out.

Using your existing UHF code, spin-orbital setup, and integral transformation, perform the following steps:

- Use a zero-filled tensor for your initial t_{ab}^{ij} .
- Iterations:
 1. Solve for the new t_{ab}^{ij} using the old amplitudes.
 2. Print the CCD correlation energy using the new t_{ab}^{ij} .
 3. Test the convergence of the energy and t_{ij}^{ab} (using the norm of the new and old t_{ij}^{ab}), breaking the loop, if converged. Be converged to at least 10^{-6} .
- Print the final CCD correlation energy in addition to the total energy.