- 1. Explain why the maximum excitation level of the wavefunction increases by +2 with each order in perturbation theory.
- 2. Prove that the leading contribution to the k-tuples CI operator has order $\lceil k/2 \rceil$ in perturbation theory.
- 3. Write down the CI energy and singles and doubles equations in terms of C_k operators. Identify the leading order of each term in perturbation theory with and without Brillouin's theorem.
- 4. Prove that CIS···m is correct to order $\lfloor m/2 \rfloor$ in the wavefunction and $2 \lfloor m/2 \rfloor + 1$ in the energy.
- 5. Write down the CC energy and singles and doubles equations in terms of T_k operators. Identify the leading order of each term in perturbation theory with and without Brillouin's theorem.
- 6. Explain why the leading contribution to the k-tuples cluster operator has order k-1.
- 7. Prove that $CCS \cdots m$ is correct to order m-1 in the wavefunction and $m+\lfloor m/2 \rfloor$ in the energy.
- 8. "Derive" the [T] correction and evaluate it, showing both the diagrams and their algebraic interpretation. You may write your answer in terms of $^{[2]}t_{abc}^{ijk}$ amplitudes and evaluate those separately.

$$E_{[T]} = \langle \Phi | T_2^{\dagger} V_c T_3^{[2]} | \Phi \rangle \qquad T_3^{[2]} = (\frac{1}{3!})^2 \sum_{\substack{abc \ ijk}} \tilde{a}_{ijk}^{abc} \langle \Phi_{ijk}^{abc} | R_0 V_c T_2 | \Phi \rangle$$
 (1)

9. Prove that the left and right EOM-CC wave operators are given by

$${}^{k}R = \exp(-T)({}^{k}C_{0} + {}^{k}C)$$
 ${}^{k}L = ({}^{k}C_{0} + {}^{k}C)^{\dagger} \exp(T)$ (2)

where ${}^kC_0 + {}^kC$ is the CI wave operator for the k^{th} state. Use this to show that we can determine excited state expectation values and transition matrix elements for an observable W as $\langle \Psi_k | W | \Psi_k \rangle = \langle \Phi | L_k \overline{W} R_k | \Phi \rangle$ and $\langle \Psi_k | W | \Psi_l \rangle = \langle \Phi | L_k \overline{W} R_l | \Phi \rangle$ where $\overline{W} \equiv \exp(-T) W \exp(T)$.

- 10. Evaluate the CCD lambda equations, showing both the diagrams and their interpretation.
- 11. Derive the $(m+1)_{\Lambda}$ correction from the coupled-cluster Löwdin functional.
- 12. "Derive" the (T) correction as an approximation to $(T)_{\Lambda}$ correction and evaluate it.

$$E_{(\mathrm{T})} = E_{[\mathrm{T}]} + \langle \Phi | T_1^{\dagger} V_c T_3^{[2]} | \Phi \rangle \tag{3}$$

¹ "Derive" here means "give detailed motivation for".

²The operator Q_3 here simply projects onto the space of triply substituted determinants.