

CCC '23 S5 - The Filter

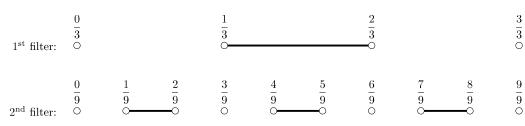


Canadian Computing Competition: 2023 Stage 1, Senior #5

Alice, the mathematician, likes to study real numbers that are between 0 and 1. Her favourite tool is the *filter*.

A filter covers part of the number line. When a number reaches a filter, two events can happen. If a number is not covered by the filter, the number will pass through. If a number is covered, the number will be removed.

Alice has infinitely many filters. Her first 3 filters look like this:



Submit solution

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Best submissions

Read editorial

✔ Points: 20 (partial)

② Time limit: 2.0s

I Memory limit: 1G

Author:

d

> Problem types



In general, the k-th filter can be defined as follows:

- Consider the number line from 0 to 1.
- Split this number line into 3^k equal-sized pieces. There are 3^k+1 points and 3^k intervals.
- The k-th filter consists of the $2^{
 m nd}$ interval, $5^{
 m th}$ interval, $8^{
 m th}$ interval, and in general, the $(3i-1)^{
 m th}$ interval. The points are **not** part of the k-th filter.

Alice has instructions for constructing the *Cantor set*. Start with the number line from 0 to 1. Apply all filters on the number line, and remove the numbers that are covered. The remaining numbers form the Cantor set.

Alice wants to research the Cantor set, and she came to you for help. Given an integer N, Alice would like to know which fractions $\frac{x}{N}$ are in the Cantor set.

Input Specification

The first line contains the integer N.

The following table shows how the available 15 marks are distributed:

Marks Awarded	Bounds on N	Additional Constraints
3 marks	$3 \leq N \leq 3^{18}$	N is a power of 3
4 marks	$2 \leq N \leq 10^5$	None

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8 marks	$2 \leq N \leq 10^9$	None
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Output Specification

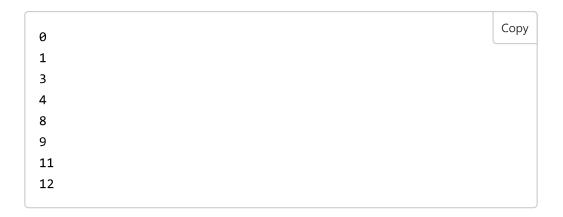
Output all integers x where $0 \leq x \leq N$ and $\frac{x}{N}$ is in the Cantor set.

Output the answers in increasing order. The number of answers will not exceed $10^6\,$

Sample Input

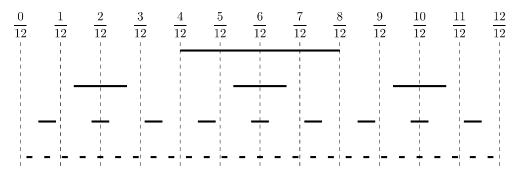
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Output for Sample Input



Explanation of Sample Output

Here is a diagram of the fractions and the first 4 filters. In reality, there are infinitely many filters.



 $\frac{5}{12},\,\frac{6}{12},$ and $\frac{7}{12}$ are not in the Cantor set because they were covered by the 1^{st} filter.

Furthermore, $\frac{2}{12}$ and $\frac{10}{12}$ are not in the Cantor set because they were covered by the 2^{nd} filter.



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https://dmoj.ca/problem/ccc23s5