Identification of protoneutron star g-modes in gravitational-wave data [PCD: alt. title]Inference of proto-neutron star properties from gravitational wave data in core-collapse supernovae.

I. INTRODUCTION

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The life of massive stars (those born with masses be-57 tween $\sim 8~{\rm M}_{\odot}$ and $\sim 120~{\rm M}_{\odot}$) ends with the collapse of 58 the iron core under its own gravity, leading to the for-59 mation of a neutron star (NS) or a black hole (BH), and 60 followed (typically but not necessarily in the BH case) by 61 a supernova explosion. Nearby core-collapse supernova 62 (CCSN) explosions are expected to be sources of gravi-63 tational waves (GW) and are one of the main candidates 64 for the next great discovery by current ground-based ob-65 servatories. However, these are relative rare events. A 66 neutrino-driven explosion [1] is the most likely outcome 67 in the case of slow rotating cores, which are present in 68 the bulk of CCSN progenitors. This event could be de- 69 tected with advanced ground-based GW detectors within 70 5 kpc [2, 3]. Such a galactic event has a rate of about 71 2-3 per century [4, 5]. For the case of fast rotating 72 progenitor cores the result is likely a magneto-rotational 73 explosion, with a more powerful signal that could be de-74 tected within 50 kpc and for some extreme models up to 75 $5-30~\mathrm{Mpc}$ [2, 3]. However, only about 1% of the elec- 76 tromagnetically observed events show signatures of fast 77 rotation (broad-lined type Ic SNe [6] or events associated 78 to long GRBs [7]), making this possibility a subdominant 79 channel of detection with an event rate of $\sim 10^{-4} \mathrm{vr}^{-1}$. 80 Therefore, we focus this work only in neutrino-driven 81 CCSNe. Despite the low rates, CCSN are of great scien- 82 tific interest because they produce a complex GW signals 83 which could provide significant clues about the physical 84 processes that occur in the moments after the collapse. $_{85}$

In the last decade, a significant progress has been 86 made in the development of numerical codes, in par- 87 ticular in the treatment of multidimensioal effects [8]. 88 PCD: I don't think the next sentence is necessary 89 since we have already discarded magneto-rotational 90 events for this work. The waveforms produced by the 91 magneto-rotational mechanism in particular is well 92 understood. The core-bounce signal can be directly 93 related with the rotational properties of the core [9-94 11]. However, the low rate of this kind of events and 95 its expected low amplitude in the slow-rotation case, will 96 probably impede its detection. In the case of neutrino- 97 driven explosions, the GW emission is primarly induced 98 by instabilities developed at the newly formed proto-99 neutron star (PNS) and by the non-spherical accreting 100 flow of hot matter over its surface [12]. This dynam-101 ics excite the different modes of oscillation of the PNS, 102 which ultimately leads to the emission of GWs. The fre-103 quency and time evolution of these modes carry informa-104 tion about the properties of the GW emitter and could $_{105}$ allow to perform PNS asteroseismology.

[PCD: I would remove the discussion on the inference of the progenitor properties (commented now).]

The main feature appearing systematically in the GW spectrum of multidimensional numerical simulations is a strong and relatively narrow feature in the post bounce evolution with raising frequency from about 100 Hz up to a few kHz (at most) and a typical duration of 0.5 – 1 s. This feature has been interpreted as a continuously excited gravity mode (g-mode, see [13, 14] for a definition in this context) of the PNS [15–20]. In these models the monotonic raise of the frequency of the mode is related to the contraction of the PNS. The typical frequencies of these modes make them a promising source for ground-based interferometers (aLIGO, aVirgo, KAGRA).

The properties of g-modes in hot PNSs have been studied since the end of last century by means of linear perturbation analysis of background PNS models. The oscillation modes associated to the surface of hot PNSs was first considered by McDermott, van Horn & Scholl [21]. Additionally, the stratified structure of the PNS allows the presence of different types of g-modes related with the fluid core [22]. Many posterior works used simplified neutron star models assuming an equilibrium configuration as a background, to study the effect of rotation [23], general relativity [24], non-linearities [25], phase transition [26] and realistic equation of state [27]. Only recently, there has been an effort to incorporate realistic backgrounds based in numerical simulations in the computation of the mode structure and evolution [28–36].

We base this work in the PNS mode analysis performed by [29, 31], which explored the eigenmode spectrum of the region within the shock (including the PNS and the post-shock region) using results from 2D CCSN numerical simulations as a background. Their results show a good match of the mode frequencies computed and the features observed in the GW spectrum of the same simulation (specially when space-time perturbations are included [31]). This result reveals that it is possible to perform CCSN asteroseismology under realistic conditions and serves as a starting point to carry out inference of astrophysical parameters of PNSs. [32] went one step further showing that it was possible to derive simple relations between the instantaneous frequency of the g-mode and the mass and radius of the PNS at each time of the evolution. These relations are universal in the sense that they do not depend on the equation of state (EOS) used or the mass of the progenitor, and only weakly on the numerical code used (see discussion in section II). Similar relations have been found by [35, 36], which also found that the universal relations do not depend on the dimensionality (1D, 2D or 3D) of the numerical simulation used as a background.

In this work, we present a method to infer from the GW data alone, the time evolution of some properties or the PNS, namely a combination of its mass and radius. For this purpose we have developed an algorithm to extract the time-frequency evolution of the main feature in the spectrograms of the GW emission of 2D simulations of CCSN. This feature corresponds to the 2 g₂ mode, according to the nomenclature used in [32] (different authors may have slightly different naming convection). Next, we use the universal relations obtained by [32], based on a set of 1D simulations, to infer the time evolution of the ratio $M_{\rm PNS}/R_{\rm PNS}^2$, being $M_{\rm PNS}$ and $R_{\rm PNS}$ the mass and radius of the PNS. Using 2D CCSN waveform corresponding to different progenitor masses we estimate the performance of the algorithm for current and future generation of ground-based GW detectors.

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This paper is organised as follows. Section II describes the details of the CCSN simulations used in the paper. Section III focuses on the algorithm that extracts the time evolution of a combination of the mass and radius of the PNS corresponding to a g-mode. Section IV shows the performance of the data analysis method for different GW detectors. Finally, we discuss the results in section V.

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II. CORE COLLAPSE SUPERNOVA SIMULATIONS

Unless other methods used GW astronomy, the al-173 gorithm proposed in this work does not require accu-174 rate waveforms in order to infer the properties of the 175 PNS. Instead, it relies on the evolution of the frequency 176 of oscillation of some particular modes, as seen in the 177 GW spectrum. The frequency of these modes depends,178 in a universal way, on the surface gravity of the PNS179 $(r = M_{\rm PNS}/R_{\rm PNS}^2)$, in the sense that if at a given time we observe GW emission at a certain frequency f we can de-181 termine univocally the value of the surface gravity, within 182 a certain error, regardless of the details of the numerical 1833 simulation. In this work we use two sets of simulations:184 i) The model set, composed by 1D simulations, which is 185 used to build the universal relation (model), r(f), link-186 ing the ratio r with the observed frequency f, and ii) the 187 test set, composed by 2D simulations, for which we know 188 both the GW signal and the evolution of the ratio, r(t), 189 and that is used to test performance of the algorithm. 190

We have used two different numerical codes in our nu-191 merical simulations. CoCoNuT [37, 38] is a code for 192 general relativistic hydrodynamics coupled to the Fast 193 Multigroup Transport scheme [39] providing an approxi-194 mate description of the emission and transport of neutri-195 nos. AENUS-ALCAR [40] combines special relativistic 196 (magneto-)hydrodynamics, a modified Newtonian grav-197 itational potential approximating the effects of general 198 relativity [41], and a spectral two-moment neutrino trans-199 port solver [40]. We included the relevant reactions be-200

Model	$M_{ m ZAMS}$	progenitor	EOS	$t_{ m f}$	$t_{\rm explosion}$	$M_{ m PNS,f}$
name	$[M_{\odot}]$	model		[s]		$[M_{\odot}]$
s11	11.2	[42]	LS220	1.86	×	1.47
s15	15.0	[42]	LS220	1.66	×	2.00
s15S	15.0	[42]	SFHo	1.75	×	2.02
s15G	15.0	[42]	GShen	0.97	×	1.86
s20	20.0	[42]	LS220	1.53	×	1.75
s20S	20.0	[46]	SFHo	0.87	×	2.05
s25	25.0	[42]	LS220	1.60	0.91	2.33
s40	40.0	[42]	LS220	1.70	1.52	2.23

TABLE I. List of axisymmetric simulations used for the *test set*. The last three columns show, the post-bounce time at the end of the simulation, the one at the onset of the explosion (non exploding models marked with \times), and the PNS mass at the end of the simulation.

tween matter and neutrinos of all flavours, i.e., emission and absorption by nucleons and nuclei, electron-positron pair annihilation, nucleonic bremsstrahlung, and scattering off nucleons, nuclei, and electrons.

For the model set, we use the 25 spherically symmetric (1D) simulations of [31] including progenitors with zero-age main sequence (ZAMS) masses in the range $M_{\rm ZAMS} = 11.2 - 75\,M_{\odot}$. The set contains simulations using the two numerical codes and six different equations of state. Details can be found in [31]. The reason to use one dimensional simulations for the model set is that the computational cost of those is significantly smaller than the cost of multidimensional simulations, so is easier to accumulate the statistics necessary to build a good model for r(f).

For the test set, we use 8 axisymmetric (2D) simulations using the AENUS-ALCAR code (see Table I for a list of models). 7 of these simulations use a selection of progenitors with masses in the range $M_{\rm ZAMS} =$ $11.2-40\,M_{\odot}$ evolved through the hydrostatic phases by [42]. We performed one simulation of each stellar model using the equation of state of [43] with an incompressibility of $K = 220 \,\mathrm{MeV}$ (LS220) and added comparison simulations with the SFHo EOS [44] and the EOS of [45] (GShen) for the progenitor with $M_{\rm ZAMS} = 15\,M_{\odot}$. To this set of simulations, we add the waveform of a twodimensional model used in [31], denoted \$20S. It corresponds to a star with the same initial mass, $M_{\rm ZAMS} =$ $20 M_{\odot}$, as for one of the other 7 axisymmetric simulations, but was taken from a newer set of stellar-evolution models [46]. It was evolved with the SFHo EOS.

For all the simulations, we mapped the pre-collapse state of the stars to a spherical coordinate system with $n_r=400$ zones in radial direction distributed logarithmically with a minimum grid width of $(\Delta r)_{\rm min}=400\,{\rm m}$ and an outer radius of $r_{\rm max}=8.3\times10^9\,{\rm cm}$ and $n_\theta=128$ equidistant cells in angular direction. For the neutrino energies, we used a logarithmic grid with $n_e=10$ bins up to $240\,{\rm MeV}$.

All spherical and most axisymmetric models fail to

achieve shock revival during the time of our simulations. Only the two stars with the highest masses, \$25 and \$40, develop relatively late explosions in axisymmetry. Consequently, mass accretion onto the PNSs proceeds at high rates for a long time in all cases and causes them to oscillate with their characteristic frequencies. The final masses of the PNSs are in the range of $M_{\rm PNS}=1.47-2.33\,M_{\odot}$, i.e., insufficient for producing a black hole.

III. METHODS DESCRIPTION

In this section, we outline a strategy for estimating the time evolution of the ratio $r = M_{\rm PNS}/R_{\rm PNS}^2$ of the mass of the PNS and its squared radius (in units of solar mass and km) from the observation of the 2g_2 oscillation mode in the gravitational wave detector data. An integral part of this strategy is the universal relations that relate the characteristic frequency of the PNS oscillation f, g and p modes with the mass and the radius of the PNS, the shock radius and the total mass inside the shock as demonstrated in [32].

Using 25 spherically symetric (1D) simulations obtained with the AENUS-ALCAR code [40] and the Co-CoNuT [47] code, we parametrize the ratio with a cubic polynomial regression with heteroscedastic errors

$$r_i = \beta_1 f_i + \beta_2 f_i^2 + \beta_3 f_i^3 + \epsilon_i \tag{1}$$

where ϵ_i are assumed to be independent zero-mean Gaussian errors with variances σ_i^2 that increase with frequency f_i . The model for frequency-dependent variances is

$$\log \sigma_i = \alpha_0 + \alpha_1 f_i + \alpha_2 f_i^2 + \delta_i \tag{2}$$

with independent and identically zero-mean Gaussian errors δ_i . The R-package lmvar [48] that implements a maximum likelihood approach was used to fit the model.

The best fitting model amongst polynomials of degree 1, 2, and 3 was chosen according to the Aikaike information criterion with coefficients given in Table II, which is actually the model defined in (1). The data and fit of the model including 95% confidence bands are displayed in Figure 1.

To develop the method we considered the gravitational²⁵³ wave signal \$20S described in Section II, originally sam-²⁵⁴ pled at 16384 Hz but resampled at 4096 Hz. A spectro-²⁵⁵ gram of this signal is shown in Figure 2 based on autore-²⁵⁶ gressive estimates of the local spectra for successive time²⁵⁷ intervals of length 200 with a 90% overlap. The domi-²⁵⁸ nant emission mode corresponds to the PNS oscillation²⁵⁹ 2g_2 -mode. We have developed a time-frequency method²⁶⁰ to track the ridge m(t) in the spectrogram, taking into²⁶¹ account that it is monotonically increasing as time goes,²⁶² a property of the 2g_2 -mode. Starting from either the²⁶³ left- or right-most column of the time-frequency matrix²⁶⁴

Coefficient	Estimate	Standard error
β_1	1.00×10^{-06}	2.12×10^{-08}
eta_2	-8.22×10^{-10}	5.00×10^{-11}
β_3	1.01×10^{-12}	2.70×10^{-14}
$lpha_0$	$-1.02 \times 10^{+01}$	6.80×10^{-02}
$lpha_1$	7.24×10^{-04}	1.56×10^{-04}
α_2	6.23×10^{-07}	8.15×10^{-08}

TABLE II. Estimate and standard error of the coefficients of the best fit model describing the ratio $r = M_{\rm PNS}/R_{\rm PNS}^2$ as function of the frequency of the 2g_2 mode.

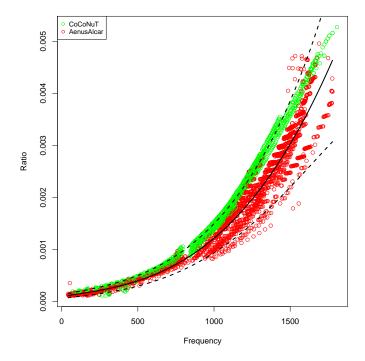


FIG. 1. Ratio $M_{\rm PNS}/R_{\rm PNS}^2$ from 25 1D simulations AENUS-ALCAR (red) and CoCoNuT (green) code. The solid line is the maximum likelihood estimate of heteroscedastic cubic model with 95% confidence bands (dashed lines) considering the AENUS-ALCAR data points.

we identify and trace the sequence of amplitude peaks within a certain frequency band given the monotonicity constraint. Appendix $\bf A$ is providing more details on the reconstruction of the g mode ridge.

We collect the instantaneous frequency $f(t_i)$ corresponding to the ridge $m(t_i)$ for the midpoint t_i of each local time interval of the spectrogram and interpolating f(t) for values in between the t_i . We then use equation (1) to obtain estimates of the time evolution of the ratio together with 95% confidence intervals. An exemple is given in Figure 3 where the red points are the point estimates and the grey bands represent 95% confidence bands. Ratio values computed using the mass and radius values obtained from the simulation code are shown in black.

In this case, for a GW signal without any noise, the

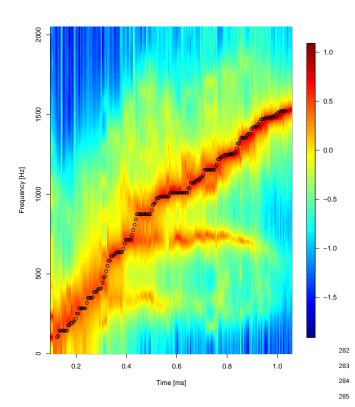


FIG. 2. Spectrogram of the gravitational wave signal ${
m s}20S^{289}$ sampled at 4096 Hz. The spectrogram is obtained using data²⁹⁰ streach of 200 samples overlapping at 90% with each other. ²⁹¹

coverage of our 95% confidence band is 94%. In the next²⁹⁴ section we investigate the performance of reconstruction²⁹⁵ of r(t) when the gravitational wave signal is embedded²⁹⁶ in noise.

IV. DETECTION SENSITIVITY WITH ADVANCED GRAVITATIONAL WAVE DETECTORS

To estimate how accurately we can infer the time evolution of $r = M_{\rm PNS}/R_{\rm PNS}^2$ in the gravitational wave detector data, we have added \$20S GW signal to 100 Gaus-303 sian noise realisations whose power spectral density fol-304 lows advanced LIGO (aLIGO) spectrum [49] shown on305 Figure 5. We have varied the distance to the source, cov-306 ering a large range of distances for which a detection in307 second generation of gravitational wave detectors is fea-308 sible. The source is optimally oriented with respect to309 the gravitational wave detector. We are assuming a GW310

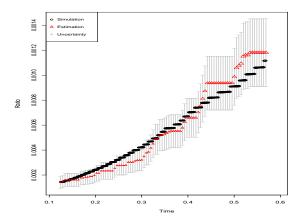


FIG. 3. Ratio $M_{\rm PNS}/R_{\rm PNS}^2$ as function of time extracted from the 2g_2 -mode of the s20S signal (red points and the 95% confidence belt in grey) compared to the ratio value derived from the PNS mass and radius given by the simulation code (black points).

signal from a core collapse phenomena has been identified in the data and that the beginning of the GW signal is known within $O(10\ ms)$. The data (signal embedded in noise) are whitened using the function *prewhiten* of the R-package TSA. An auto-regressive model with maximal 100 coefficients has been used.

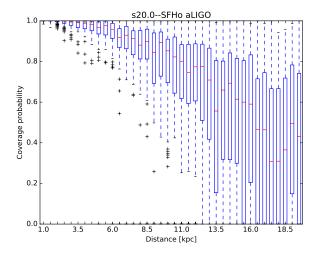
For each of the noise realisations, we reconstruct the ratio time series r_i of length N starting from the left side of the spectrogram and constraining the beginning of the track to be smaller than 200 Hz. The reconstructed ratio is then compare to the "true" ratio r_i^0 derived from the PNS mass and radius generated by the simulation code that produced s20S.

Figure 4 is showing the fraction of the ratio r_i^0 values that fall within the 95% confidence interval of r_i . This quantity, *coverage*, is taking maximal values when the source is located within few kpc and then decreases with the distance.

To better quantify how well we reconstruct the ratio, we have also considered Δ the mean over the track of the relative error of r_i .

$$\Delta = \frac{1}{N} \sum_{i=1}^{N} \frac{|r_i - r_i^0|}{r_i^0} \tag{3}$$

 Δ values of each of the 100 noise realisation are shown as well as function of the distance on Figure 4. For a source located up to ~10 kpc the relative error remains smaller than 20%. At small distance Δ is small but not null. This reflects the approximation of the model used for r. It is nevertheless remarkable that one can reconstruct the ratio time series with a good precision at distance up to ~ 10 kpc for this particular waveform, with



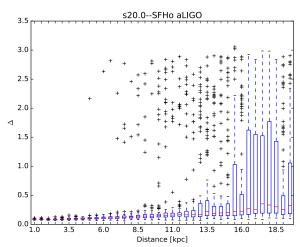


FIG. 4. Boxplots of coverage (upper panel) and Δ (lower panel) for \$20S signal embedded in aLIGO noise at different distances from the Earth. 100 noise realisations is considered for each distance.

coverage value larger than 80%. We have tested that the method does not depend on features of $\tt s20S$ using 7 other waveforms described in section II covering a large range of progenitor masses. Figure 6 shows that apart $\tt s11.2-LS220$, the ratio is well reconstructed for all waveforms up to $\sim 10 \rm kpc$. On this figure we also show the coverage value in case of absence of signal. The median value is significantly different from 0 because the g-mode reconstruction algorithm is looking for a continuously frequency increasing track in the spectrogram, starting between 0 and 200 Hz. In Table ?? we are reporting the distance at which coverage median is lower than 80%.

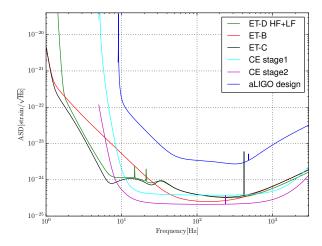


FIG. 5.

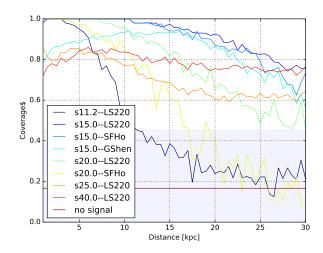


FIG. 6. Median of *coverage* for 8 CCSN waveforms embedded in aLIGO noise and located at different distance from the Earth. The "no signal" line and band show the median and first and third quartile of *coverage* in absence of any signal.

Simulation	s11	s15	s15S	s15G	s20	s20S	s25	s40
aLIGO char.	7	26	25	21	16	11	9	12
distance (kpc)								
SNR in aLIGO	19.5	55.4	59.0	60.0	34.3	35.8	116.5	98.5
CE2 char.								
distance (kpc)								
SNR in CE2								

TABLE III. Matched filter signal-to-noise ratio (SNR) of the simulated waveforms for the different GW detectors considered in this study. The source is located at 10 kpc and is optimally oriented with respect to the detector.

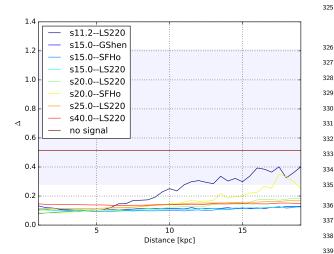


FIG. 7. Median of *Delta* for 8 CCSN waveforms embedded in aLIGO noise and located at different distance from the Earth. The "no signal" line and band show the median and first and third quartile of *Delta* in absence of any signal.

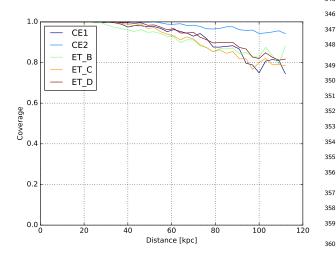


FIG. 8. Median of coverage for s20.0–SFHo CCSN waveform³⁶² embedded in 3G detectors noise and located at different dis-³⁶³ tance from the Earth.

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V. DISCUSSION

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Appendix A G-MODE RECONSTRUCTION

Given the spectrogram and an specified time interval for the g-mode reconstruction, our proposal method works as follows. The starting point must be specified. It can be either at the beginning or at the end of the signal. Then, in one of these extremes, the maximum energy value is identified, registering its frequency. This is done independently for a number of consecutive time intervals. Then we calculate the median of these frequency values, providing a robust starting value for the g-mode reconstruction.

The starting frequency value is the first g-mode estimate for the first or the last time interval, depending on the specified starting location. If the reconstruction is set to start at the beginning of the signal, the reconstruction will be done progressively over the time intervals, where each maximum frequency value will be calculated within a frequency range specified by the previous g-mode estimate. Given the non-decreasing behaviour of the true g-mode values, the g-mode estimates will be forced to be greater or equal than the one estimated for its previous time interval, and lower than a specified upper limit. As a result, the g-modes estimates will be a non-decreasing sequence of frequency values.

If the reconstruction is set to start at the end of the signal, the g-modes will be estimated backward in time. Each maximum frequency is calculated within a range determined by its successor (in time) g-mode estimate. These estimates are forced to be lower or equal than its successor (in time) estimate, but greater than a specified lower limit. Thus, a non-decreasing sequence of g-mode estimates is guaranteed.

This g-mode reconstruction method works if and only if the signal is strong enough to provide information about the g-mode, which is reflected in the spectrogram.

Given the sequence of g-mode estimates, the confidence band will be calculated by using the model defined in (??). The g-mode estimates are frequency values which we use as predictors in the model in order to generate confidence intervals for the ratios. Since the g-mode estimates are indexed by time, the confidence intervals for the ratios are too. Thus, we generate the confidence band by interpolating the lower and upper limits of the collection of consecutive confidence intervals, which will be valid for the time range of the g-mode estimates. This confidence band is used to estimate the coverage probabilities in our simulation studies presented below.

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