Identification of protoneutron star g-modes in gravitational-wave data [PCD: alt. title]Inference of proto-neutron star properties from gravitational wave data in core-collapse supernovae.

## I. INTRODUCTION

2

8

10

11

12

13

14

15

17

18

19

20

21

22

23

24

26

27

29

30

31

32

33

35

36

37

39

40

42

43

45

46

47

48

49

51

52

The life of massive stars (those born with masses between  $\sim 8 \text{ M}_{\odot}$  and  $\sim 120 \text{ M}_{\odot}$ ) ends with the collapse of 58 the iron core under its own gravity, leading to the for-59 mation of a neutron star (NS) or a black hole (BH), and 60 followed (typically but not necessarily in the BH case) by 61 a supernova explosion. Nearby core-collapse supernova 62 (CCSN) explosions are expected to be sources of gravi- 63 tational waves (GW) and are one of the main candidates 64 for the next great discovery by current ground-based ob- 65 servatories. However, these are relative rare events. A 66 neutrino-driven explosion [1] is the most likely outcome 67 in the case of slow rotating cores, which are present in 68 the bulk of CCSN progenitors. This event could be de-69 tected with advanced ground-based GW detectors within 70 5 kpc [2, 3]. Such a galactic event has a rate of about 71 2-3 per century [4, 5]. For the case of fast rotating <sup>72</sup> progenitor cores the result is likely a magneto-rotational 73 explosion, with a more powerful signal that could be de-74 tected within 50 kpc and for some extreme models up to 75 5-30 Mpc [2, 3]. However, only about 1% of the electromagnetically observed events show signatures of fast 77 rotation (broad-lined type Ic SNe [6] or events associated 78 to long GRBs [7]), making this possibility a subdominant 79 channel of detection with an event rate of  $\sim 10^{-4} {\rm yr}^{-1}$ . 80 Therefore, we focus this work only in neutrino-driven 81 CCSNe. Despite the low rates, CCSN are of great scien- 82 tific interest because they produce a complex GW signals 83 which could provide significant clues about the physical 84 processes that occur in the moments after the collapse. 85

In the last decade, a significant progress has been made <sup>86</sup> in the development of numerical codes, in particular in <sup>87</sup> the treatment of multidimensioal effects [8]. In the case of <sup>88</sup> neutrino-driven explosions, the GW emission is primarly <sup>89</sup> induced by instabilities developed at the newly formed <sup>90</sup> proto-neutron star (PNS) and by the non-spherical ac-<sup>91</sup> creting flow of hot matter over its surface [12]. This dy-<sup>92</sup> namics excite the different modes of oscillation of the <sup>93</sup> PNS, which ultimately leads to the emission of GWs. <sup>94</sup> The frequency and time evolution of these modes carry <sup>95</sup> information about the properties of the GW emitter and <sup>96</sup> could allow to perform PNS asteroseismology.

The main feature appearing systematically in the GW 98 spectrum of multidimensional numerical simulations is a 99 strong and relatively narrow feature in the post bounce 100 evolution with raising frequency from about 100 Hz up 101 to a few kHz (at most) and a typical duration of 0.5 – 102 1 s. This feature has been interpreted as a continuously 103 excited gravity mode (g-mode, see [13, 14] for a definition 104 in this context) of the PNS [15–20]. In these models the 105 monotonic raise of the frequency of the mode is related 106

to the contraction of the PNS. The typical frequencies of these modes make them a promising source for groundbased interferometers (aLIGO, aVirgo, KAGRA).

The properties of g-modes in hot PNSs have been studied since the end of last century by means of linear perturbation analysis of background PNS models. The oscillation modes associated to the surface of hot PNSs was first considered by McDermott, van Horn & Scholl [21]. Additionally, the stratified structure of the PNS allows the presence of different types of g-modes related with the fluid core [22]. Many posterior works used simplified neutron star models assuming an equilibrium configuration as a background, to study the effect of rotation [23], general relativity [24], non-linearities [25], phase transition [26] and realistic equation of state [27]. Only recently, there has been an effort to incorporate realistic backgrounds based in numerical simulations in the computation of the mode structure and evolution [28–36].

We base this work in the PNS mode analysis performed by [29, 31], which explored the eigenmode spectrum of the region within the shock (including the PNS and the post-shock region) using results from 2D CCSN numerical simulations as a background. Their results show a good match of the mode frequencies computed and the features observed in the GW spectrum of the same simulation (specially when space-time perturbations are included [31]). This result reveals that it is possible to perform CCSN asteroseismology under realistic conditions and serves as a starting point to carry out inference of astrophysical parameters of PNSs. [32] went one step further showing that it was possible to derive simple relations between the instantaneous frequency of the g-mode and the mass and radius of the PNS at each time of the evolution. These relations are universal in the sense that they do not depend on the equation of state (EOS) used or the mass of the progenitor, and only weakly on the numerical code used (see discussion in section II). Similar relations have been found by [35, 36], which also found that the universal relations do not depend on the dimensionality (1D, 2D or 3D) of the numerical simulation used as a background.

In this work, we present a method to infer from the GW data alone, the time evolution of some properties or the PNS, namely a combination of its mass and radius. For this purpose we have developed an algorithm to extract the time-frequency evolution of the main feature in the spectrograms of the GW emission of 2D simulations of CCSN. This feature corresponds to the  $^2$ g<sub>2</sub> mode, according to the nomenclature used in [32] (different authors may have slightly different naming convection). Next, we use the universal relations obtained by [32], based on a set of 1D simulations, to infer the time evolution of

the ratio  $M_{\rm PNS}/R_{\rm PNS}^2$ , being  $M_{\rm PNS}$  and  $R_{\rm PNS}$  the mass and radius of the PNS. Using 2D CCSN waveform corresponding to different progenitor masses we estimate the performance of the algorithm for current and future generation of ground-based GW detectors.

107

108

109

110

111

112

114

115

116

117

118

119

120

121

122

123

124

125

126

127

128

129

130

131

132

133

134

135

136

137

138

139

140

141

142

143

145

146

147

148

149

150

151

152

153

154

156

157

159

This paper is organised as follows. Section II describes the details of the CCSN simulations used in the paper. Section III focuses on the algorithm that extracts the time evolution of a combination of the mass and radius of the PNS corresponding to a g-mode. Section IV shows the performance of the data analysis method for different GW detectors. Finally, we discuss the results in section V.

## II. CORE COLLAPSE SUPERNOVA SIMULATIONS

Unless other methods used GW astronomy, the al-162 gorithm proposed in this work does not require accu-163 rate waveforms in order to infer the properties of the 164 PNS. Instead, it relies on the evolution of the frequency 165 of oscillation of some particular modes, as seen in the 166 GW spectrum. The frequency of these modes depends, 167 in a universal way, on the surface gravity of the PNS<sub>168</sub>  $(r = M_{\rm PNS}/R_{\rm PNS}^2)$ , in the sense that if at a given time we observe GW emission at a certain frequency f we can de-170 termine univocally the value of the surface gravity, within 171 a certain error, regardless of the details of the numerical 172 simulation. In this work we use two sets of simulations:173 i) The model set, composed by 1D simulations, which is 174 used to build the universal relation (model), r(f), link-175 ing the ratio r with the observed frequency f, and ii) the 176 test set, composed by 2D simulations, for which we know 177 both the GW signal and the evolution of the ratio, r(t), 178 and that is used to test performance of the algorithm. 179

We have used two different numerical codes in our nu-180 merical simulations. CoCoNuT [37, 38] is a code for 181 general relativistic hydrodynamics coupled to the Fast 182 Multigroup Transport scheme [39] providing an approxi-183 mate description of the emission and transport of neutri-184 nos. AENUS-ALCAR [40] combines special relativistic (magneto-)hydrodynamics, a modified Newtonian grav-186 itational potential approximating the effects of general 187 relativity [41], and a spectral two-moment neutrino trans-188 port solver [40]. We included the relevant reactions be-189 tween matter and neutrinos of all flavours, i.e., emission 190 and absorption by nucleons and nuclei, electron-positron 191 pair annihilation, nucleonic bremsstrahlung, and scatter-192 ing off nucleons, nuclei, and electrons.

For the *model set*, we use the 25 spherically symmet-<sup>194</sup> ric (1D) simulations of [31] including progenitors with<sup>195</sup> zero-age main sequence (ZAMS) masses in the range<sup>196</sup>  $M_{\rm ZAMS} = 11.2 - 75 \, M_{\odot}$ . The set contains simulations<sup>197</sup> using the two numerical codes and six different equations<sup>198</sup> of state. Details can be found in [31]. The reason to use<sup>199</sup> one dimensional simulations for the model set is that the<sup>200</sup>

Model	$M_{ m ZAMS}$	progenitor	EOS	$t_{ m f}$	$t_{\rm explosion}$	$M_{ m PNS,f}$	
name	$[M_{\odot}]$	model		[s]		$[M_{\odot}]$	
s11	11.2	[42]	LS220	1.86	×	1.47	
s15	15.0	[42]	LS220	1.66	×	2.00	
s15S	15.0	[42]	SFHo	1.75	×	2.02	
s15G	15.0	[42]	$\operatorname{GShen}$	0.97	×	1.86	
s20	20.0	[42]	LS220	1.53	×	1.75	
s20S	20.0	[46]	SFHo	0.87	×	2.05	
s25	25.0	[42]	LS220	1.60	0.91	2.33	
s40	40.0	[42]	LS220	1.70	1.52	2.23	

TABLE I. List of axisymmetric simulations used for the *test set*. The last three columns show, the post-bounce time at the end of the simulation, the one at the onset of the explosion (non exploding models marked with  $\times$ ), and the PNS mass at the end of the simulation.

computational cost of those is significantly smaller than the cost of multidimensional simulations, so is easier to accumulate the statistics necessary to build a good model for r(f). For each time of each simulation we compute the ratio r and the frequency of the  $^2g_2$  mode by means of the linear analysis described in [29, 31, 32].

For the test set, we use 8 axisymmetric (2D) simulations using the AENUS-ALCAR code (see Table I for a list of models). 7 of these simulations use a selection of progenitors with masses in the range  $M_{\rm ZAMS} =$  $11.2-40\,M_{\odot}$  evolved through the hydrostatic phases by [42]. We performed one simulation of each stellar model using the equation of state of [43] with an incompressibility of  $K = 220 \,\mathrm{MeV}$  (LS220) and added comparison simulations with the SFHo EOS [44] and the EOS of [45] (GShen) for the progenitor with  $M_{\rm ZAMS} = 15 \, M_{\odot}$ . To this set of simulations, we add the waveform of a twodimensional model used in [31], denoted \$20S. It corresponds to a star with the same initial mass,  $M_{\rm ZAMS} =$  $20 M_{\odot}$ , as for one of the other 7 axisymmetric simulations, but was taken from a newer set of stellar-evolution models [46]. It was evolved with the SFHo EOS.

For all the simulations, we mapped the pre-collapse state of the stars to a spherical coordinate system with  $n_r = 400$  zones in radial direction distributed logarithmically with a minimum grid width of  $(\Delta r)_{\min} = 400$  m and an outer radius of  $r_{\max} = 8.3 \times 10^9$  cm and  $n_{\theta} = 128$  equidistant cells in angular direction. For the neutrino energies, we used a logarithmic grid with  $n_e = 10$  bins up to 240 MeV. Unlike the model set, the simulations in the test set cannot be 1D becase we need to extract the gravitational wave signal, which is a multi-dimensional effect. For each simulation we extract the gravitational wave signal,  $h_+(t)$ , by means of the quadrupole formula and compute the time evolution of the surface gravity, r(t).

All spherical and most axisymmetric models fail to achieve shock revival during the time of our simulations. Only the two stars with the highest masses, \$25 and \$40, develop relatively late explosions in axisym-

metry. Consequently, mass accretion onto the PNSs proceeds at high rates for a long time in all cases and causes them to oscillate with their characteristic frequencies. The final masses of the PNSs are in the range of  $M_{\rm PNS}=1.47-2.33\,M_{\odot}$ , i.e., insufficient for producing a black hole.

#### III. METHODS DESCRIPTION

In this section, we outline a strategy for estimating the time evolution of the ratio  $r = M_{\rm PNS}/R_{\rm PNS}^2$  of the mass of the PNS and its squared radius (in units of solar mass and km) from the observation of the  $^2g_2$  oscillation mode in the gravitational wave detector data. An integral part of this strategy is the universal relations that relate the characteristic frequency of the PNS oscillation f, g and p modes with the mass and the radius of the PNS, the shock radius and the total mass inside the shock as demonstrated in [32].

To build the model of the ratio r as a function of the frequency f we use the spherically symetric (1D) simulations of the  $model\ set$ . Figure 1 shows the data for the 25 numerical simulations. As identified by [32], the only systematic deviation from a single universal relation is the numerical code used in the simulations. To avoid any systematic effect, we only use to build our model the 18 simulations performed with the ALCAR-AENUS code, which is the same code that was used in our test set. The consequences of this choice are discussed in the conclusions. Using this data, we parametrize the ratio with a cubic polynomial regression with heteroscedastic errors

$$r_i = \beta_1 f_i + \beta_2 f_i^2 + \beta_3 f_i^3 + \epsilon_i \tag{1}$$

where  $\epsilon_i$  are assumed to be independent zero-mean Gaussian errors with variances  $\sigma_i^2$  that increase with frequency  $f_i$ . The model for frequency-dependent variances is

$$\log \sigma_i = \alpha_0 + \alpha_1 f_i + \alpha_2 f_i^2 + \delta_i \tag{2}$$

with independent and identically zero-mean Gaussian er-250 rors  $\delta_i$ . The R-package lmvar [48] that implements a251 maximum likelihood approach was used to fit the model.252

The best fitting model amongst polynomials of degree<sub>253</sub> 1, 2, and 3 was chosen according to the Aikaike informa-<sup>254</sup> tion criterion with coefficients given in Table II, which is<sup>255</sup> actually the model defined in (1). The data and fit of the<sup>256</sup> model including 95% confidence bands are displayed in<sup>257</sup> Figure 1.

We use this model to infer the properties of the simula-259 tions in the *test set* described in in Section II. To develop260 describe the method we considered focus on the gravita-261 tional wave signal of \$20\$S, originally sampled at 16384 Hz262 but resampled at 4096 Hz. A spectrogram of this signal263 is shown in Figure 2 based on autoregressive estimates264

Coefficient	Estimate	Standard error			
$\beta_1$	$1.00 \times 10^{-06}$	$2.12 \times 10^{-08}$			
$eta_2$	$-8.22 \times 10^{-10}$	$5.00 \times 10^{-11}$			
$\beta_3$	$1.01 \times 10^{-12}$	$2.70 \times 10^{-14}$			
$lpha_0$	$-1.02 \times 10^{+01}$	$6.80 \times 10^{-02}$			
$\alpha_1$	$7.24 \times 10^{-04}$	$1.56 \times 10^{-04}$			
$\alpha_2$	$6.23 \times 10^{-07}$	$8.15 \times 10^{-08}$			

TABLE II. Estimate and standard error of the coefficients of the best fit model describing the ratio  $r=M_{\rm PNS}/R_{\rm PNS}^2$  as function of the frequency of the  $^2g_2$  mode.

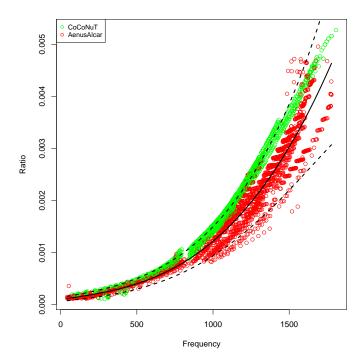
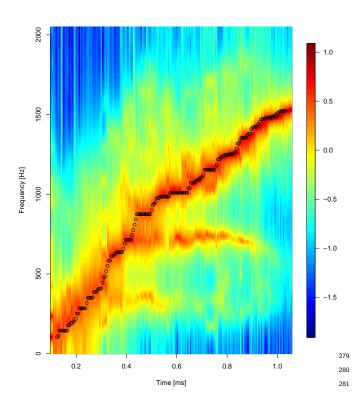
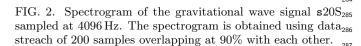


FIG. 1. Ratio  $M_{\rm PNS}/R_{\rm PNS}^2$  from 25 1D simulations AENUS-ALCAR (red) and CoCoNuT (green) code. The solid line is the maximum likelihood estimate of heteroscedastic cubic model with 95% confidence bands (dashed lines) considering only the AENUS-ALCAR data points (18 simulations).

[CITATION?] of the local spectra for successive time intervals of length 200 with a 90% overlap. The dominant emission mode corresponds to the PNS oscillation  $^2g_2$ -mode. We have developed a time-frequency method to track the ridge m(t) in the spectrogram, taking into account that it is monotonically increasing as time goes. This is a property of the  $^2g_2$ -mode, the frequency of which increases as the object becomes more massive and compact. Starting from either the left- or right-most column of the time-frequency matrix we identify and trace the sequence of amplitude peaks within a certain frequency band given the monotonicity constraint. Appendix A is providing more details on the reconstruction of the g mode ridge.

We collect the instantaneous frequency  $f(t_i)$  corresponding to the ridge  $m(t_i)$  for the midpoint  $t_i$  of each





282

283

288

289

307

308

310

local time interval of the spectrogram and interpolating f(t) for values in between the  $t_i$ . We then use our model given by Eq. (1) to obtain estimates of the time evolution of the ratio together with 95% confidence intervals. An exemple is given in Figure 3 where the red points are the point estimates and the grey bands represent  $95\%^{296}$  confidence bands. Ratio values computed using the mass and radius values obtained from the simulation code (true values) are shown in black.

265

267

268

270

271

272

273

274

276

277

In this case, for a GW signal without any noise, the<sup>301</sup> coverage of our 95% confidence band is 94% of the true<sup>302</sup> values. In the next section we investigate the perfor-<sup>303</sup> mance of the reconstruction of r(t) when the gravita-<sup>304</sup> tional wave signal is embedded in noise.

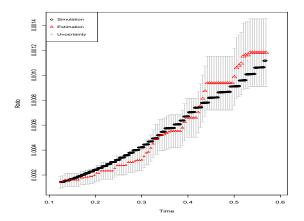


FIG. 3. Ratio  $M_{\rm PNS}/R_{\rm PNS}^2$  as function of time extracted from the  $^2g_2$ -mode of the s20S signal (red points and the 95% confidence belt in grey) compared to the ratio value derived from the PNS mass and radius given by the simulation code (black points).

# IV. DETECTION SENSITIVITY WITH ADVANCED GRAVITATIONAL WAVE DETECTORS

To estimate how accurately we can infer the time evolution of  $r = M_{PNS}/R_{PNS}^2$  in the gravitational wave detector data, we have added the GW signal from \$20S to 100 Gaussian noise realisations whose power spectral density follows the advanced LIGO (aLIGO) spectrum [49] shown on Figure 5. We have varied the distance to the source, covering a large range of distances for which a detection in second generation of gravitational wave detectors is feasible. The source is optimally oriented with respect to the gravitational wave detector. We are assuming a GW signal from a core collapse phenomena has been identified in the data and that the beginning of the GW signal is known within O(10 ms). The data (signal embedded in noise) are whitened using the function prewhiten of the R-package TSA. An auto-regressive model with maximal 100 coefficients has been used.

For each of the noise realisations, we reconstruct the ratio time series  $r_i$  of length N starting from the left side of the spectrogram and constraining the beginning of the track to be smaller than 200 Hz. The reconstructed ratio is then compare to the "true" ratio  $r_i^0$  derived from the PNS mass and radius computed from the generated by the simulation code that produced s20S simulation.

Figure 4 is showing the fraction of the ratio  $r_i^0$  values that fall within the 95% confidence interval of  $r_i$ . This quantity, *coverage*, is taking maximal values when the source is located within few kpc and then decreases with the distance.

To better quantify how well we reconstruct the ratio,

		s11	s15	s15S	s15G	s20	s20S	s25	s40
aLIGO	$d_{max}$ (kpc)	7.3	26.3	24.8	22.3	16.3	10.8	7.8	14.8
	SNR	13.0	37.0	38.7	39.2	22.9	23.3	75.6	63.6

TABLE III. Matched filter signal-to-noise ratio (SNR) of the simulated waveforms for the different GW detectors considered in this study. The source is located at 10 kpc and is optimally oriented with respect to the detector.

we have also considered  $\Delta$  the mean over the track of the relative error of  $r_i$ .

312

313

314

315

316

317

319

320

322

323

325

328

329

330

331

332

334

336

337

338

340

341

343

$$\Delta = \frac{1}{N} \sum_{i=1}^{N} \frac{|r_i - r_i^0|}{r_i^0}$$
 (3)

 $\Delta$  values of each of the 100 noise realisation are shown as well as function of the distance on Figure 4. For a source located up to  $\sim 10\,\mathrm{kpc}$  the relative error remains smaller than 20% [PCD: should we comment on the outliers?]. At small distance  $\Delta$  is small but not null. This reflects the approximation of the model used for r. It is nevertheless remarkable that one can reconstruct the ratio time series with a good precision at distance up to  $\sim$ 10 kpc for this particular waveform, with coverage value larger than 80%. We have tested that the method does not depend on features of \$20S using the 7 other waveforms of the test set described in section II covering a large range of progenitor masses. Figure 6 shows that apart s11.2-LS220, the ratio is well reconstructed for all waveforms up to  $\sim 10 \text{kpc}$ . On this figure we also show the coverage value in case of absence of signal. The median value is significantly different from 0 because the g-mode reconstruction algorithm is looking for a continuously frequency increasing track in the spectrogram, starting between 0 and 200 Hz. In Table III we are reporting the distance at which *coverage* median is lower than 80%.

#### V. DISCUSSION

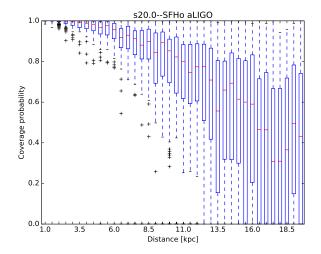
Acknowledgments —

## Appendix A G-MODE RECONSTRUCTION

345

346

Given the spectrogram and an specified time inter-350 val for the g-mode reconstruction, our proposal method351 works as follows. The starting point must be specified.352 It can be either at the beginning or at the end of the353 signal. Then, in one of these extremes, the maximum en-354 ergy value is identified, registering its frequency. This is 355 done independently for a number of consecutive time in-356 tervals. Then we calculate the median of these frequency357



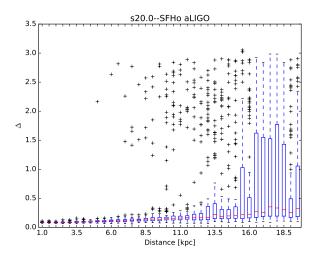


FIG. 4. Boxplots of coverage (upper panel) and  $\Delta$  (lower panel) for \$20S signal embedded in aLIGO noise at different distances from the Earth. 100 noise realisations is considered for each distance. [PCD: I guess you use "coverage probability" because we are showing the box plots. Shouln't we say  $\Delta$  probability as well? Or just "coverage"? Also, how are outliers computed? Why are there so many outliers in |delta? If they are a significant fraction of the data points why are they considered outliers?]

values, providing a robust starting value for the g-mode reconstruction.

The starting frequency value is the first g-mode estimate for the first or the last time interval, depending on the specified starting location. If the reconstruction is set to start at the beginning of the signal, the reconstruction will be done progressively over the time intervals, where each maximum frequency value will be calculated within a frequency range specified by the previous g-mode estimate. Given the non-decreasing behaviour of the true g-mode values, the g-mode estimates will be forced to be greater or equal than the one estimated for its previous time interval, and lower than a specified upper limit. As

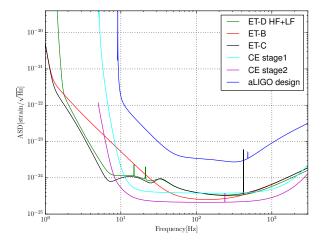


FIG. 5.

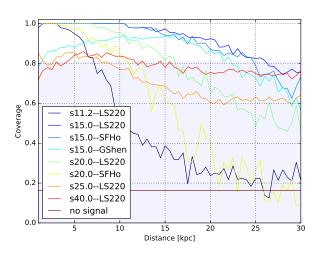


FIG. 6. Median of *coverage* for 8 CCSN waveforms embedded in aLIGO noise and located at different distance from the Earth. The "no signal" line and band show the median and first and third quartile of *coverage* in absence of any signal.

a result, the g-modes estimates will be a non-decreasing sequence of frequency values.

If the reconstruction is set to start at the end of the signal, the g-modes will be estimated backward in time. Each maximum frequency is calculated within a range determined by its successor (in time) g-mode estimate.<sup>373</sup> These estimates are forced to be lower or equal than its<sup>374</sup> successor (in time) estimate, but greater than a specified<sup>375</sup> lower limit. Thus, a non-decreasing sequence of g-mode<sup>376</sup> estimates is guaranteed.

This g-mode reconstruction method works if and only if  $_{378}$  the signal is strong enough to provide information about  $_{379}$  the g-mode, which is reflected in the spectrogram.

Given the sequence of g-mode estimates, the confidence<sub>381</sub> band will be calculated by using the model defined in (1).382

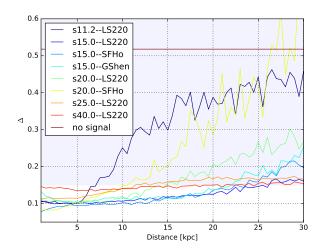


FIG. 7. Median of Delta for 8 CCSN waveforms embedded in aLIGO noise and located at different distance from the Earth. The "no signal" line and band show the median and first and third quartile of Delta in absence of any signal.

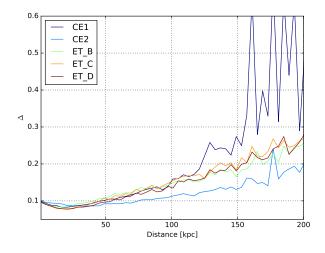


FIG. 8. Median of *coverage* for s20.0–SFHo CCSN waveform embedded in 3G detectors noise and located at different distance from the Earth.

The g-mode estimates are frequency values which we use as predictors in the model in order to generate confidence intervals for the ratios. Since the g-mode estimates are indexed by time, the confidence intervals for the ratios are too. Thus, we generate the confidence band by interpolating the lower and upper limits of the collection of consecutive confidence intervals, which will be valid for the time range of the g-mode estimates. This confidence band is used to estimate the coverage probabilities in our simulation studies presented below above.

[1] H. A. Bethe, "Supernova mechanisms," Rev. Mod. Phys. 44462, 801–866 (1990).

383

384

385

386

387

388

389

390

391

392

393

394

395

396

397

398

399

400

401

402

403

404

405

406

407

408

409

410

411

412

413

414

415

416

417

418

419

420

421

422

423

424

425

426

427

428

429

430

431

432

433

434

435

436

437

438

439

440

441

442

- [2] S.E. Gossan, P. Sutton, A. Stuver, M. Zanolin, K. Gill,<sup>446</sup> and C. Ott, "Observing gravitational waves from core-<sup>447</sup> collapse supernovae in the advanced detector era," Phys-<sup>448</sup> ical Review D 93 (2016), 10.1103/physrevd.93.042002. <sup>449</sup>
- [3] B. P. Abbott and et al, "Optically targeted search for<sub>450</sub> gravitational waves emitted by core-collapse supernovae<sub>451</sub> during the first and second observing runs of advanced<sub>452</sub> LIGO and advanced Virgo," Phys. Rev. D **101**, 084002<sub>453</sub> (2020), arXiv:1908.03584 [astro-ph.HE].
- [4] Scott M. Adams, C. S. Kochanek, John F. Beacom, 455
   Mark R. Vagins, and K. Z. Stanek, "OBSERVING THE 456
   NEXT GALACTIC SUPERNOVA," The Astrophysical 457
   Journal 778, 164 (2013).
- [5] Karolina Rozwadowska, Francesco Vissani, and En-459 rico Cappellaro, "On the rate of core collapse super-460 novae in the milky way," New A 83, 101498 (2021),461 arXiv:2009.03438 [astro-ph.HE].
- [6] Weidong Li, Jesse Leaman, Ryan Chornock, Alexei V.463 Filippenko, Dovi Poznanski, Mohan Ganeshalingam, Xi-464 aofeng Wang, Maryam Modjaz, Saurabh Jha, Ryan J.465 Foley, and Nathan Smith, "Nearby supernova rates from466 the Lick Observatory Supernova Search - II. The ob-467 served luminosity functions and fractions of supernovae468 in a complete sample," MNRAS 412, 1441-1472 (2011),469 arXiv:1006.4612 [astro-ph.SR].
- [7] R. Chapman, N. R. Tanvir, R. S. Priddey, and A. J.<sub>471</sub> Levan, "How common are long Gamma-Ray Bursts in<sub>472</sub> the Local Universe?" Mon. Not. R. Astron. Soc. L21,<sub>473</sub> 382 (2007).
- [8] Bernhard Müller, "Hydrodynamics of core-collapse super-475 novae and their progenitors," Living Reviews in Com-476 putational Astrophysics 6, 3 (2020), arXiv:2006.05083477 [astro-ph.SR].
- [9] C. D. Ott, H. Dimmelmeier, A. Marek, H.-T. Janka, 479
   B. Zink, I. Hawke, and E. Schnetter, "Rotating col-480 lapse of stellar iron cores in general relativity," Classi-481
   cal and Quantum Gravity 24, 139-+ (2007), arXiv:astro-482
   ph/0612638.
- [10] E. Abdikamalov, S. Gossan, A. M. DeMaio, and C. D. 484 Ott, "Measuring the angular momentum distribution in 485 core-collapse supernova progenitors with gravitational 486 waves," Phys. Rev. D 90, 044001 (2014), arXiv:1311.3678487 [astro-ph.SR].
- [11] Sherwood Richers, Christian D. Ott, Ernazar Abdika-489 malov, Evan O'Connor, and Chris Sullivan, "Equation of 490 state effects on gravitational waves from rotating core col-491 lapse," Phys. Rev. D 95, 063019 (2017), arXiv:1701.02752492 [astro-ph.HE].
- [12] Kei Kotake and Takami Kuroda, "Gravita-494 tional Waves from Core-Collapse Supernovae," in 495

  Handbook of Supernovae, edited by Athem W. Alsabti496 and Paul Murdin (2017) p. 1671.
- [13] K.D. Kokkotas and B.G. Schmidt, "Quasi-normal modes<sub>498</sub> of stars and black holes," Living Rev. Rel. **2**, 2 (1999). 499
- [14] John L. Friedman and Nikolaos Stergioulas, 500 Rotating Relativistic Stars (2013).
- [15] J. W. Murphy, C. D. Ott, and A. Burrows, "A Model<sub>502</sub> for Gravitational Wave Emission from Neutrino-Driven<sub>503</sub> Core-Collapse Supernovae," ApJ **707**, 1173 (2009).

- [16] B. Müller, H.-T. Janka, and A. Marek, "A New Multidimensional General Relativistic Neutrino Hydrodynamics Code of Core-collapse Supernovae. III. Gravitational Wave Signals from Supernova Explosion Models," ApJ 766, 43 (2013), arXiv:1210.6984 [astro-ph.SR].
- [17] Pablo Cerdá-Durán, Nicolas DeBrye, Miguel A. Aloy, José A. Font, and Martin Obergaulinger, "Gravitational Wave Signatures in Black Hole Forming Core Collapse," Astrophys. J. Lett. 779, L18 (2013), arXiv:1310.8290 [astro-ph.SR].
- [18] Konstantin N. Yakunin, Anthony Mezzacappa, Pedro Marronetti, Shin'ichirou Yoshida, Stephen W. Bruenn, W. Raphael Hix, Eric J. Lentz, O. E. Bronson Messer, J. Austin Harris, Eirik Endeve, John M. Blondin, and Eric J. Lingerfelt, Phys. Rev. D 92, 084040 (2015), arXiv:1505.05824 [astro-ph.HE].
- [19] Takami Kuroda, Kei Kotake, and Tomoya Takiwaki, "A New Gravitational-wave Signature from Standing Accretion Shock Instability in Supernovae," Astrophys. J. Lett. 829, L14 (2016), arXiv:1605.09215 [astro-ph.HE].
- [20] H. Andresen, B. Müller, E. Müller, and H. Th. Janka, "Gravitational wave signals from 3D neutrino hydrodynamics simulations of core-collapse supernovae," MNRAS 468, 2032–2051 (2017), arXiv:1607.05199 [astro-ph.HE].
- [21] P. N. McDermott, H. M. van Horn, and J. F. Scholl, "Nonradial g-mode oscillations of warm neutron stars," ApJ 268, 837–848 (1983).
- [22] A. Reisenegger and P. Goldreich, "A new class of g-modes in neutron stars," ApJ 395, 240–249 (1992).
- [23] V. Ferrari, L. Gualtieri, J. A. Pons, and A. Stavridis, "Gravitational waves from rotating proto-neutron stars," Classical and Quantum Gravity 21, S515–S519 (2004), astro-ph/0409578.
- [24] A. Passamonti, M. Bruni, L. Gualtieri, and C. F. Sopuerta, "Coupling of radial and nonradial oscillations of relativistic stars: Gauge-invariant formalism," Phys. Rev. D 71, 024022 (2005), gr-qc/0407108.
- [25] H. Dimmelmeier, N. Stergioulas, and J. A. Font, "Non-linear axisymmetric pulsations of rotating relativistic stars in the conformal flatness approximation," MNRAS 368, 1609–1630 (2006), astro-ph/0511394.
- [26] C. J. Krüger, W. C. G. Ho, and N. Andersson, "Seismology of adolescent neutron stars: Accounting for thermal effects and crust elasticity," Phys. Rev. D 92, 063009 (2015), arXiv:1402.5656 [gr-qc].
- [27] G. Camelio, A. Lovato, L. Gualtieri, O. Benhar, J. A. Pons, and V. Ferrari, "Evolution of a proto-neutron star with a nuclear many-body equation of state: neutrino luminosity and gravitational wave frequencies," ArXiv eprints (2017), arXiv:1704.01923 [astro-ph.HE].
- [28] H. Sotani and T. Takiwaki, "Gravitational wave asteroseismology with protoneutron stars," Phys. Rev. D 94, 044043 (2016), arXiv:1608.01048 [astro-ph.HE].
- [29] A. Torres-Forné, P. Cerdá-Durán, A. Passamonti, and J. A. Font, "Towards asteroseismology of core-collapse supernovae with gravitational-wave observations - I. Cowling approximation," MNRAS 474, 5272–5286 (2018), arXiv:1708.01920 [astro-ph.SR].
- [30] Viktoriya Morozova, David Radice, Adam Burrows, and David Vartanyan, "The Gravitational Wave Signal from Core-collapse Supernovae," ApJ 861, 10 (2018),

arXiv:1801.01914 [astro-ph.HE].

505

506

507

508

509

510

511

512

513

514

515

516

517

518

519

520

521

522

523

524

525

526

527

528

529

530

531

532

533

534

535

536

537

538

539

540

541

542

- [31] A. Torres-Forné, P. Cerdá-Durán, A. Passamonti,544 M. Obergaulinger, and J. A. Font, "Towards as-545 teroseismology of core-collapse supernovae with grav-546 itational wave observations II. Inclusion of space-547 time perturbations," MNRAS 482, 3967–3988 (2019),548 arXiv:1806.11366 [astro-ph.HE].
- [32] A. Torres-Forné, P. Cerdá-Durán, M. Obergaulinger, 550 B. Müller, and J. Font, "Universal relations for 551 gravitational-wave asteroseismology of proto-neutron 552 stars," Physical Review Letters 123, 051102 (2019). 553
- [33] Hajime Sotani, Takami Kuroda, Tomoya Takiwaki,554 and Kei Kotake, "Dependence of the outer boundary555 condition on protoneutron star asteroseismology with556 gravitational-wave signatures," Phys. Rev. D 99, 123024557 (2019), arXiv:1906.04354 [astro-ph.HE].
- [34] John Ryan Westernacher-Schneider, Evan O'Connor,559 Erin O'Sullivan, Irene Tamborra, Meng-Ru Wu, Sean M.560 Couch, and Felix Malmenbeck, "Multimessenger aster-561 oseismology of core-collapse supernovae," Phys. Rev. D562 100, 123009 (2019), arXiv:1907.01138 [astro-ph.HE]. 563
- [35] Hajime Sotani and Tomoya Takiwaki, "Dimension depen-564 dence of numerical simulations on gravitational waves565 from protoneutron stars," Phys. Rev. D 102, 023028566 (2020), arXiv:2004.09871 [astro-ph.HE].
- [36] Hajime Sotani and Tomoya Takiwaki, "Avoided cross-568 ing in gravitational wave spectra from protoneu-569 tron star," MNRAS (2020), 10.1093/mnras/staa2597,570 arXiv:2008.00419 [astro-ph.HE].
- [37] H. Dimmelmeier, J. A. Font, and E. Müller, "Relativis-572 tic simulations of rotational core collapse I. Methods, ini-573 tial models, and code tests," A&A 388, 917–935 (2002),574 arXiv:astro-ph/0204288 [astro-ph].
- [38] Harald Dimmelmeier, Jérôme Novak, José A. Font,576 José M. Ibáñez, and Ewald Müller, "Combining spec-577 tral and shock-capturing methods: A new numerical578 approach for 3D relativistic core collapse simulations,"579 Phys. Rev. D 71, 064023 (2005), arXiv:astro-ph/0407174580

[astro-ph].

- [39] B. Müller and H. Th. Janka, "Non-radial instabilities and progenitor asphericities in core-collapse supernovae," MNRAS 448, 2141–2174 (2015), arXiv:1409.4783 [astro-ph.SR].
- [40] O. Just, M. Obergaulinger, and H.-T. Janka, "A new multidimensional, energy-dependent two-moment transport code for neutrino-hydrodynamics," MNRAS 453, 3386–3413 (2015), arXiv:1501.02999.
- [41] A. Marek, H. Dimmelmeier, H.-T. Janka, E. Müller, and R. Buras, "Exploring the relativistic regime with Newtonian hydrodynamics: an improved effective gravitational potential for supernova simulations," A&A 445, 273–289 (2006).
- [42] S. E. Woosley, A. Heger, and T. A. Weaver, "The evolution and explosion of massive stars," Reviews of Modern Physics 74, 1015–1071 (2002).
- [43] J. M. Lattimer and F. Douglas Swesty, "A generalized equation of state for hot, dense matter," Nuclear Physics A 535, 331–376 (1991).
- [44] A. W. Steiner, M. Hempel, and T. Fischer, "Corecollapse Supernova Equations of State Based on Neutron Star Observations," ApJ 774, 17 (2013), arXiv:1207.2184 [astro-ph.SR].
- [45] G. Shen, C. J. Horowitz, and S. Teige, "New equation of state for astrophysical simulations," Phys. Rev. C 83, 035802 (2011), arXiv:1101.3715 [astro-ph.SR].
- [46] S. E. Woosley and A. Heger, "Nucleosynthesis and remnants in massive stars of solar metallicity," Phys. Rep. 442, 269–283 (2007), astro-ph/0702176.
- [47] P. Cerdá-Durán, J. A. Font, L. Antón, and E. Müller, "A new general relativistic magnetohydrodynamics code for dynamical spacetimes," A&A 492, 937–953 (2008), arXiv:0804.4572.

[48]

[49] Lisa Barsotti, Peter Fritschel, Matthew Evans, and Slawomir Gras, "Updated advanced ligo sensitivity design curve," (2018).