

I. INTRODUCTION

The life of massive stars ($8M_{\odot} - 100M_{\odot}$) ends with the collapse of their iron core under their own gravity, leading the formation of a neutron star or a black hole (BH), followed (typically but not necessarily in the BH case) by the explosion of the star as a supernova. Core-collapse supernova (CCSN) explosions are one most important sources of gravitational-waves (GW) that have not yet been detected by current ground-based observatories. This is because even the most common type of CCSN, the neutrino-driven explosion, have a rate about three per century [1] within our galaxy. The other main type of explosion, those produced by the magneto-rotational mechanism, can produce a more powerful signal and can be detected at distances up to ~ 5 Mpc [1]. However, the rate of events of this kind is much lower than the one for the neutrino driven mechanism $\sim 10^{-4}\text{yr}^{-1}$, which represents less than 1% of all CCSNe. Despite all this, collapsing stars produces a complex GW signal which could provide significant clues about the physical processes that occur in the moments after the explosion.

In the past years an impressive progress has been made in the development of numerical codes, which allows to obtain more accurate CCSN simulations. The waveforms produced by the magneto-rotational mechanism in particular is well understood. The core-bounce signal can be directly related with the rotational properties of the core [2–4]. However, the low rate of this kind of events and is low amplitude and high frequency of the bounce signal in the slow-rotation case will probably impede its detection.

In the case of most common neutrino-driven mechanism, the GW emission is mainly produced during the hydrodynamical bounce and the unstable evolution of the fluid inside the region formed by the recently formed proto-neutron star (PNS) and the accretion shock. The dynamics excite the different modes of oscillation of the PNS [5, 6]. Unluckily, in this case is not possible to relate the GW emission with the properties (mass, rotation rate, metallicity or magnetic fields) of the progenitor stars. There are many reasons that explain this issue. The large number of physical processes involved whose role in the scenario is not completely understood. For instance, exist uncertainties in the stellar evolution of massive stars or in the nuclear and weak interactions necessary for the equation of state (EoS) or the neutrino interactions. Furthermore, the stochastic and chaotic nature of the instabilities is transferred to the GW emission, resulting in the same progenitor leading to a significantly different waveform. These large number of physical ingredients in addition to the necessary accuracy of the modelling of complex multidimensional interactions requires large computational resources. One simulation of

one single progenitor in 3D with accurate neutrino transport and realistic equation of state (EoS) can take several months of intense calculations on a scientific supercomputer facility, which complicates the systematic exploration of the progenitor parameters.

Common features in the GW signal, that have been interpreted as g modes of the PNS, have been reported in many works [7–12]. Typically, the frequencies associated with the modes rise monotonically with time during the contraction of the PNS. The characteristic frequencies of the modes associated to the PNS make them promising candidates for detection in ground-based interferometers. The presence of g-methods in hot PNS has been studied since the end of last century. The oscillation modes related with the surface of hot PNS was first considered by McDermott, van Horn & Scholl [13]. Additionally, the stratified structure of the PNS allow the presence of different kinds of g-modes related with the core [14]. Many posterior works used simplified background neutron star models (equilibrium configurations), to study different variations of the equilibrium system, like rotation [15], general relativity [16], non-linearities [17], phase transition [18] and realistic equation of state [19]. Sotani & Takiwaki [20] studied the oscillation modes before the explosion using a simplified fits to numerical simulations.

In previous works [21, 22], we explore the eigenmode spectrum using as background results of CCSN numerical simulations and the cavity form by the PNS and the shock. We showed that the GW time-frequency distribution correspond with the frequencies of oscillation of different families of p- and g-modes. These works reveal that is possible to perform CCSN asteroseismology and serves as a starting point to carry out inference of astrophysical parameters of PNSs. In this line of research, in [23] we derived the relations between the different types of modes with some with the evolution of mass and radius of the PNS. These relations are universal in the sense that they not depend of the EOS, the mass of the progenitor or the code used to perform the simulation.

In this paper, we present a method to extract from the GW data the mass and the radius of the PNS as function of time using the universal relations. We inject a GW signal, obtained from a 2D CCSN simulation, into simulated non-white Gaussian noise which spectrum follows the AdLIGO sensitivity curve. We show how the algorithm is able to extract the time-frequency evolution of the main arc of GW emission, which corresponds to the 2g_2 , according to the nomenclature used in [23]. Then the universal relation for this mode is inverted to obtain the time evolution of the ratio $r = M_{\text{PNS}}/R_{\text{PNS}}^2$. The evolution of the estimated ratio and the true ratio obtained from the simulation is remarkably similar.

Paper organisation

II. CORE COLLAPSE SUPERNOVA SIMULATIONS

The algorithm proposed in the article does not require accurate waveforms but relies on the evolution of the frequencies of oscillations depending on the PNS mass and radius. To parametrize this dependence, we have considered spherically symmetric [22] and two-dimensional axisymmetric models of stellar core collapse simulated with two codes, CoCoNuT (one-dimensional models) and AENUS-ALCAR [24] (one- and two-dimensional models). CoCoNuT [25] is a code for general relativistic hydrodynamics coupled to the Fast Multigroup Transport scheme [26] providing an approximate description of the emission and transport of neutrinos. AENUS-ALCAR [24] combines special relativistic (magnetohydrodynamics, a modified Newtonian gravitational potential approximating the effects of general relativity [27], and a spectral two-moment neutrino transport solver [24]. We included the relevant reactions between matter and neutrinos of all flavours, i.e., emission and absorption by nucleons and nuclei, electron-positron pair annihilation, nucleonic bremsstrahlung, and scattering off nucleons, nuclei, and electrons.

To tune the parameters of the algorithm, we use two sets of 25 models in the range of initial stellar masses $M_{\text{ZAMS}} = 11.2 - 75 M_{\odot}$ simulated with the two codes. They were carried out using six equations of state (EOSs). They are complemented by a set of 7 two-dimensional axisymmetric models consisting of stellar core collapse of five stars with zero-age main-sequence masses of $M_{\text{ZAMS}} = 11.2 - 40 M_{\odot}$ evolved through the hydrostatic phases by [28]. We performed one simulation of each stellar model using the equation of state of [29] with an incompressibility of $K = 220 \text{ MeV}$ (LS220) and added comparison simulations with the SFHo EOS [30] and the EOS of [31] (GShen) for the one with $M_{\text{ZAMS}} = 15 M_{\odot}$ (see Table I for a list of models). To this set of simulations, we add the waveform of a two-dimensional model used in [22], denoted **s20S**. It corresponds to a star with the same initial mass, $M_{\text{ZAMS}} = 20 M_{\odot}$, as for one of the other 7 axisymmetric simulations, but was taken from a newer set of stellar-evolution models [32]. It was evolved with the SFHo EOS.

We mapped the pre-collapse state of the stars to a spherical coordinate system with $n_r = 400$ zones in radial direction distributed logarithmically with a minimum grid width of $(\Delta r)_{\text{min}} = 400 \text{ m}$ and an outer radius of $r_{\text{max}} = 8.3 \times 10^9 \text{ cm}$ and $n_{\theta} = 128$ equidistant cells in angular direction. For the neutrino energies, we used a logarithmic grid with $n_e = 10$ bins up to 240 MeV .

All spherical and most axisymmetric models fail to achieve shock revival during the time of our simulations. Only the two stars with the highest masses, **s25** and **s40**, develop relatively late explosions in axisymmetry. Consequently, mass accretion onto the PNSs proceeds at high rates for a long time in all cases and causes them to oscillate with their characteristic frequencies.

Simulation	$M_{\text{ZAMS}}[M_{\odot}]$	EOS	$t_{\text{f}}[\text{s}]$	explosion	$M_{\text{PNS}}[M_{\odot}]$
s11	11.2	LS220	1.86	×	1.47
s15	15.0	LS220	1.66	×	2.00
s15S	15.0	SFHo	1.75	×	2.02
s15G	15.0	GShen	0.97	×	1.86
s20	20.0	LS220	1.53	×	1.75
s20S	20.0	SFHo	0.87	×	2.05
s25	25.0	LS220	1.60	0.91	2.33
s40	40.0	LS220	1.70	1.52	2.23

TABLE I. List of axisymmetric simulations. We present the name of the models, the initial mass of the progenitors, and the EOS used, and the final post-bounce time of the simulations. For models which explode, we list the time at which the shock starts to expand in column “explosion”; otherwise, a \times sign is displayed. The final column indicates the mass of the PNS at the end of the simulation.

The final masses of the PNSs are in the range of $M_{\text{PNS}} = 1.47 - 2.33 M_{\odot}$, i.e., insufficient for producing a black hole.

III. METHODS DESCRIPTION

In this section, we outline a strategy for estimating the time evolution of the ratio $r = M_{\text{PNS}}/R_{\text{PNS}}^2$ of the mass of the PNS and its squared radius (in units of solar mass and km) from the observation of the 2g_2 oscillation mode in the gravitational wave detector data. An integral part of this strategy is the universal relations that relate the characteristic frequency of the PNS oscillation f , g and p modes with the mass and the radius of the PNS, the shock radius and the total mass inside the shock as demonstrated in [23].

Using 25 spherically symmetric (1D) simulations obtained with the AENUS-ALCAR code [24] and the CoCoNuT [25] code, we parametrize the ratio with a cubic polynomial regression with heteroscedastic errors

$$r_i = \beta_1 f_i + \beta_2 f_i^2 + \beta_3 f_i^3 + \epsilon_i \quad (1)$$

where ϵ_i are assumed to be independent zero-mean Gaussian errors with variances σ_i^2 that increase with frequency f_i . The model for frequency-dependent variances is

$$\log \sigma_i = \alpha_0 + \alpha_1 f_i + \alpha_2 f_i^2 + \delta_i \quad (2)$$

with independent and identically zero-mean Gaussian errors δ_i . The R-package **lmvar** [33] that implements a maximum likelihood approach was used to fit the model.

The best fitting model amongst polynomials of degree 1, 2, and 3 was chosen according to the Akaike information criterion with coefficients given in Table II, which is actually the model defined in (1). The data and fit of the

Coefficient	Estimate	Standard error
β_1	1.00×10^{-06}	2.12×10^{-08}
β_2	-8.22×10^{-10}	5.00×10^{-11}
β_3	1.01×10^{-12}	2.70×10^{-14}
α_0	$-1.02 \times 10^{+01}$	6.80×10^{-02}
α_1	7.24×10^{-04}	1.56×10^{-04}
α_2	6.23×10^{-07}	8.15×10^{-08}

TABLE II. Estimate and standard error of the coefficients of the best fit model describing the ratio $r = M_{\text{PNS}}/R_{\text{PNS}}^2$ as function of the frequency of the 2g_2 mode.

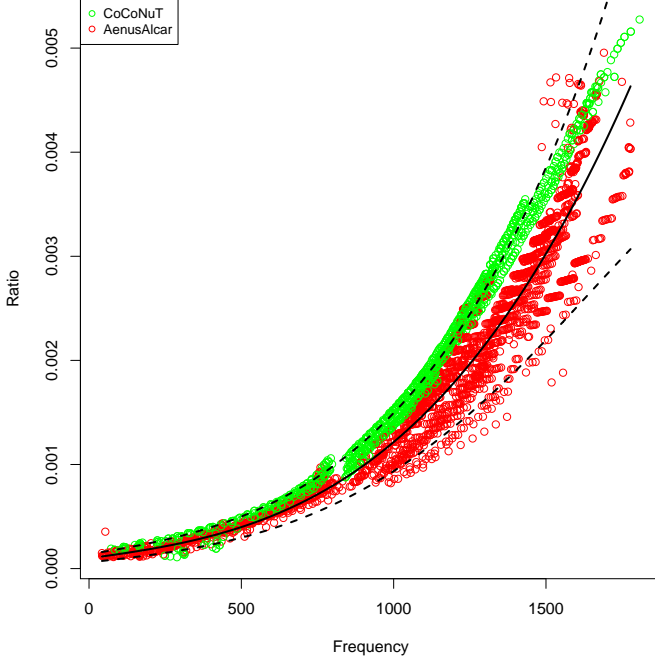


FIG. 1. Ratio $M_{\text{PNS}}/R_{\text{PNS}}^2$ from 25 1D simulations AENUS-ALCAR (red) and CoCoNuT (green) code. The solid line is the maximum likelihood estimate of heteroscedastic cubic model with 95% confidence bands (dashed lines) considering the AENUS-ALCAR data points.

model including 95% confidence bands are displayed in Figure 1.

To develop the method we considered the gravitational wave signal s20S described in Section II, originally sampled at 16384 Hz but resampled at 4096 Hz. A spectrogram of this signal is shown in Figure 2 based on autoregressive estimates of the local spectra for successive time intervals of length 200 with a 90% overlap. The dominant emission mode corresponds to the PNS oscillation 2g_2 -mode. We have developed a time-frequency method to track the ridge $m(t)$ in the spectrogram, taking into account that it is monotonically increasing as time goes, a property of the 2g_2 -mode. Starting from either the left- or right-most column of the time-frequency matrix we identify and trace the sequence of amplitude peaks within a certain frequency band given the monotonicity

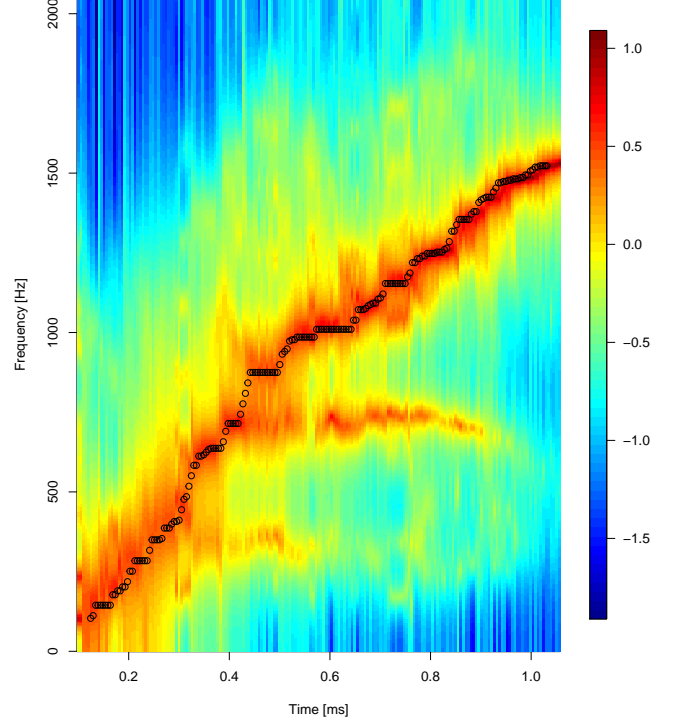


FIG. 2. Spectrogram of the gravitational wave signal s20S sampled at 4096 Hz. The spectrogram is obtained using data stretch of 200 samples overlapping at 90% with each other.

constraint. Appendix A is providing more details on the reconstruction of the g mode ridge.

We collect the instantaneous frequency $f(t_i)$ corresponding to the ridge $m(t_i)$ for the midpoint t_i of each local time interval of the spectrogram and interpolating $f(t)$ for values in between the t_i . We then use equation ((1)) to obtain estimates of the time evolution of the ratio together with 95% confidence intervals. An example is given in Figure 3 where the red points are the point estimates and the grey bands represent 95% confidence bands. Ratio values computed using the mass and radius values obtained from the simulation code are shown in black.

In this case, for a GW signal without any noise, the coverage of our 95% confidence band is 94%. In the next section we investigate the performance of reconstruction of $r(t)$ when the gravitational wave signal is embedded in noise.

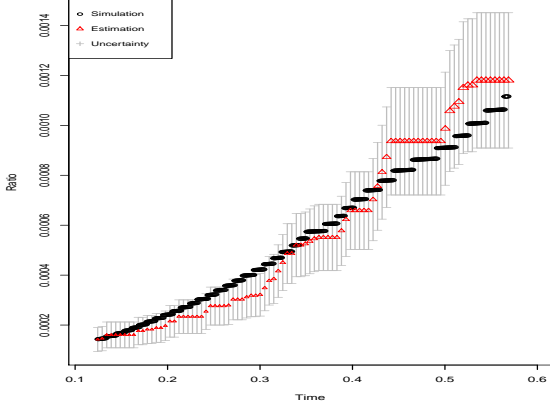


FIG. 3. Ratio $M_{\text{PNS}}/R_{\text{PNS}}^2$ as function of time extracted from the 2g_2 -mode of the s20S signal (red points and the 95% confidence belt in grey) compared to the ratio value derived from the PNS mass and radius given by the simulation code (black points).

IV. DETECTION SENSITIVITY WITH ADVANCED GRAVITATIONAL WAVE DETECTORS

To estimate how accurately we can infer the time evolution of $r = M_{\text{PNS}}/R_{\text{PNS}}^2$ in the gravitational wave detector data, we have added s20S GW signal to Gaussian noise realisations whose power spectral density follows advanced LIGO spectrum [34] shown on Figure 5. We have varied the distance to the source, covering a large range of distances for which a detection in second generation of gravitational wave detectors is feasible. The source is optimally oriented with respect to the gravitational wave detector. We are assuming a GW signal from a core collapse phenomena has been identified in the data and that the beginning of the GW signal is known within $O(10 \text{ ms})$. The data (signal embedded in noise) are whitened using the function *prewhiten* of the R-package TSA. An auto-regressive model with maximal 100 coefficients has been used.

For each of the noise realisations, we reconstruct the ratio time series r_i of length N and compute two quantities that compare r_i to ratio r_i^0 derived from the PNS mass and radius generated by the simulation code that produces s20S.

The first quantity, *coverage*, is the fraction of the ratio r_i^0 values that fall within the 95% confidence interval of r_i . We also compute the *precision* value given by

$$\text{precision} = \sum_1^N \frac{|r_i - r_i^0|}{r_i^0} \quad (3)$$

Figure 4 is showing the median of *coverage* and

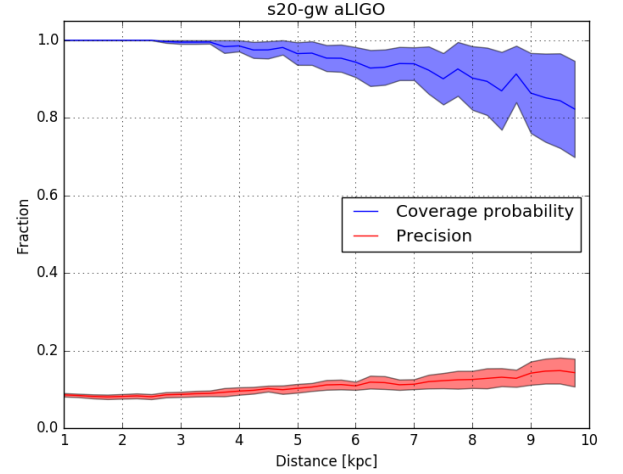


FIG. 4. *coverage* and *precision* for s20S signal embedded in aLIGO noise at different distance from the Earth. The shaded regions are given by the median absolute deviation.

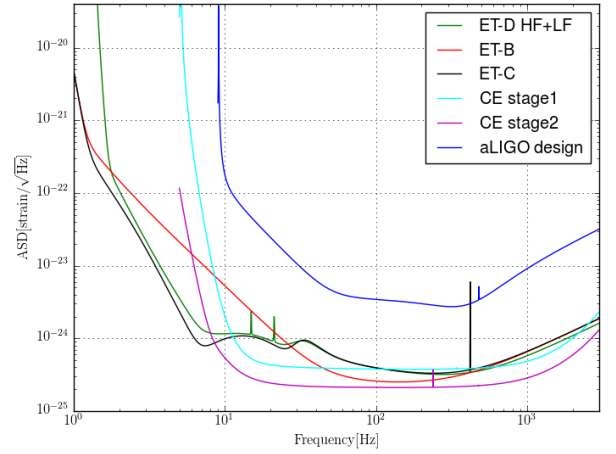


FIG. 5.

precision as function of the distance of the source as well as the confidence belt corresponding to the median absolute deviation. As expected, the estimation of r is maximal when the source is nearby and decreases with the distance. At small distance the *precision* value is small but not null. This reflects the approximation of the model used for r . It is nevertheless remarkable that one can reconstruct the ratio time series with a good precision at distance up to $\sim 10 \text{ kpc}$ for this particular waveform. We have tested that the method does not depend on features of s20S using 7 other waveforms described in section ?? covering a large range of progenitor masses. Figure 6 shows that apart s11.2-LS220, the ratio is well reconstructed for all waveforms up to $\sim 10 \text{ kpc}$.

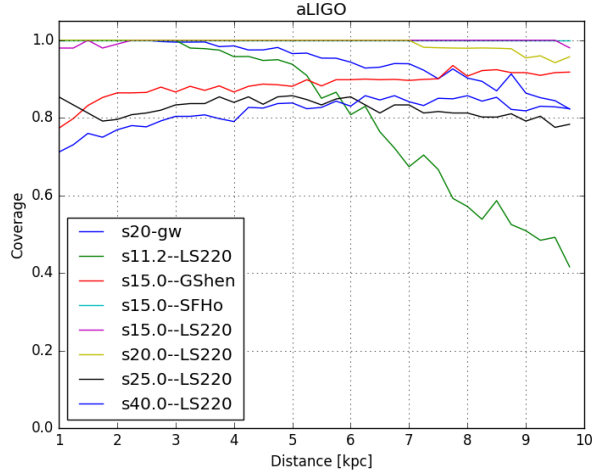


FIG. 6. *coverage* for 7 waveforms embedded in aLIGO noise at different distance from the Earth.

Simulation	s11	s15	s15S	s15G	s20	s20S	s25	s40
aLIGO	19.5	55.4	59.0	60.0	34.3	35.8	116.5	98.5
CE2								
ET-B								

TABLE III. Matched filter signal-to-noise ratio (SNR) of the simulated waveforms for the different GW detectors considered in this study. The source is located at 10 kpc and is optimally oriented with respect to the detector.

V. DISCUSSION

Acknowledgments —

Appendix A G-MODE RECONSTRUCTION

Given the spectrogram and an specified time interval for the g-mode reconstruction, our proposal method

works as follows. The starting point must be specified. It can be either at the beginning or at the end of the signal. Then, in one of these extremes, the maximum energy value is identified, registering its frequency. This is done independently for a number of consecutive time intervals. Then we calculate the median of these frequency values, providing a robust starting value for the g-mode reconstruction.

The starting frequency value is the first g-mode estimate for the first or the last time interval, depending on the specified starting location. If the reconstruction is set to start at the beginning of the signal, the reconstruction will be done progressively over the time intervals, where each maximum frequency value will be calculated within a frequency range specified by the previous g-mode estimate. Given the non-decreasing behaviour of the true g-mode values, the g-mode estimates will be forced to be greater or equal than the one estimated for its previous time interval, and lower than a specified upper limit. As a result, the g-modes estimates will be a non-decreasing sequence of frequency values.

If the reconstruction is set to start at the end of the signal, the g-modes will be estimated backward in time. Each maximum frequency is calculated within a range determined by its successor (in time) g-mode estimate. These estimates are forced to be lower or equal than its successor (in time) estimate, but greater than a specified lower limit. Thus, a non-decreasing sequence of g-mode estimates is guaranteed.

This g-mode reconstruction method works if and only if the signal is strong enough to provide information about the g-mode, which is reflected in the spectrogram.

Given the sequence of g-mode estimates, the confidence band will be calculated by using the model defined in (??). The g-mode estimates are frequency values which we use as predictors in the model in order to generate confidence intervals for the ratios. Since the g-mode estimates are indexed by time, the confidence intervals for the ratios are too. Thus, we generate the confidence band by interpolating the lower and upper limits of the collection of consecutive confidence intervals, which will be valid for the time range of the g-mode estimates. This confidence band is used to estimate the coverage probabilities in our simulation studies presented below.

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