#### I. INTRODUCTION

2

10

11

12

13

15

16

17

18

19

20

21

22

23

24

25

26

27

28

29

31

32

33

34

35

37

40

41

42

43

45

46

47

48

51

52

The life of massive stars  $(8M_{\odot} - 100M_{\odot})$  ends with the collapse of their iron core under their own gravity, leading the formation of a neutron star or a black hole (BH), followed (typically but not necessarily in the BH case) by the explosion of the star as a supernova. Core-collapse supernova (CCSN) explosions are one most important sources of gravitational-waves (GW) that have not yet been detected by current ground-based observatories. This is because even the most common type of CCSN, the neutrino-driven explosion, have a rate about three per century [1] within our galaxy. The other main type of explosion, those produced by the magneto-rotational mechanism, can produce a more powerful signal and can be detected at distances up to  $\sim 5$  Mpc [1]. However, the rate of events of this kind is much lower than the one for the neutrino driven mechanism  $\sim 10^{-4} {\rm yr}^{-1}$ , which represents less than 1% of all CCSNe. Despite all this, collapsing stars produces a complex GW signal which could provide significant clues about the physical processes that occur in the moments after the explosion.

In the past years an impressive progress has been made 78 in the development of numerical codes, which allows to 79 obtain more accurate CCSN simulations. The waveforms 80 produced by the magneto-rotational mechanism in particular is well understood. The core-bounce signal can 82 be directly related with the rotational properties of the 83 core [2–4]. However, the low rate of this kind of events 84 and is low amplitude and high frequency of the bounce 85 signal in the slow-rotation case will probably impede its 86 detection.

In the case of most common neutrino-driven mecha-88 nism, the GW emission is manly produced during the 89 hydrodynamical bounce and the unstable evolution of 90 the fluid inside the region formed by the recently formed 91 proto-neutron star (PNS) and the accretion shock. The 92 dynamics excite the different modes of oscillation of the 93 PNS [5, 6]. Unluckily, in this case is not possible to re-94 late the GW emission with the properties (mass, rota-95 tion rate, metallicity or magnetic fields) of the progeni- 96 tor stars. There are many reasons that explain this is- 97 sue. The large number of physical processes involved 98 whose role in the escenario is not completely understood. 99 For instance, exist uncertainties in the stellar evolution<sup>100</sup> of massive stars or in the nuclear and weak interactions<sup>101</sup> necessary for the equation of state (EoS) or the neutrino 102 interactions. Furthermore, the stochastic and chaotic na-103 ture of the instabilities is transferred to the GW emission, 104 resulting in the same progenitor leading to a significantly 105 different waveform. These large number of physical in-106 gredients in addition to the necessary accuracy of the 107 modelling of complex multidimensional interactions re-108 quires large computational resources. One simulation of

one single progenitor in 3D with accurate neutrino transport and realistic equation of state (EoS) can take several months of intense calculations on a scientific supercomputer facility, which complicates the systematic exploration of the progenitor parameters.

Common features in the GW signal, that have been interpreted as g modes of the PNS, have been reported in many works [7–12]. Typically, the frequencies associated with the modes rise monotonically with time during the contraction of the PNS. The characteristic frequencies of the modes associated to the PNS make them promising candidates for detection in ground-based interferometers. The presence of g-methods in hot PNS has been studied since the end of last century. The oscillation modes related with the surface of hot PNS was first considered by McDermott, van Horn & Scholl [13]. Additionally, the stratified structure of the PNS allow the presence of different kinds of g-modes related with the core [14]. Many posterior works used simplified background neutron star models (equilibrium configurations), to study different variations of the equilibrium system, like rotation [15], general relativity [16], non-linearities [17], phase transition [18] and realistic equation of state [19]. Sotani & Takiwaki [20] studied the oscillation modes before the explosion using a simplified fits to numerical simulations.

In previous works [21, 22], we explore the eigenmode spectrum using as background results of CCSN numerical simulations and the cavity form by the PNS and the shock. We showed that the GW time-frequency distribution correspond with the frequencies of oscillation of different families of p- and g-modes. These works reveal that is posible to perform CCSN asteroseismology and serves as a starting point to carry out inference of astrophysical parameters of PNSs. In this line of research, in [23] we derived the relations between the different types of modes with some with the evolution of mass and radius of the PNS. These relations are universal in the sense that they not depend of the EOS, the mass of the progenitor or the code used to perform the simulation.

In this paper, we present a method to extract from the GW data the mass and the radius of the PNS as function of time using the universal relations. We inject a GW signal, obtained from a 2D CCSN simulation, into simulated non-white Gaussian noise which spectrum follows the AdLIGO sensitivity curve. We show how the algorithm is able to extract the time-frequency evolution of the main arc of GW emission, which corresponds to the universal relation for this mode is inverted to obtain the time evolution of the ratio  $r = M_{\rm PNS}/R_{\rm PNS}^2$ . The evolution of the estimated ratio and the true ratio obtained from the simulation is remarkably similar.

#### Paper organisation

#### II. CORE COLLAPSE SUPERNOVA SIMULATIONS

109

110

111

112

113

114

115

116

117

118

119

121

122

124

125

126

127

129

130

131

132

133

135

136

137

138

139

141

142

143

144

145

147

148

149

150

151

152

153

155

156

157

158

159

160

Martin's simulations and code description 1D similation data to fit the ratio vs frequency model -AA and CoConut outputs

We apply our analysis to a set of 25 spherically symmetric [?] and 7 two-dimensional axisymmetric models of stellar core collapse simulated with two codes, Co-CoNuT (one-dimensional models) and AENUS-ALCAR [24] (one- and two-dimensional models). CoCoNuT [25] is a code for general relativistic hydrodynamics coupled to the Fast Multigroup Transport scheme [26] providing an approximate description of the emission and transport of neutrinos. AENUS-ALCAR [24] combines special relativistic (magneto-)hydrodynamics, a modified Newtonian gravitational potential approximating the effects of general relativity [27], and a spectral twomoment neutrino transport solver [24]. We included<sup>161</sup> the relevant reactions between matter and neutrinos of all flavours, i.e., emission and absorption by nucleons 162 and nuclei, electron-positron pair annihilation, nucleonic 163 bremsstrahlung, and scattering off nucleons, nuclei, and 164 electrons.

Our spherically symmetric simulations cover the range of initial stellar masses  $M_{\rm ZAMS}=11.2-75\,M_{\odot}$ . They were carried out using six equations of state (EOSs). They are complemented by a set of two-dimensional axisymmetric models consisting of stellar core collapse of five stars with zero-age main-sequence masses of  $M_{\rm ZAMS}=11.2-40\,M_{\odot}$  evolved through the hydrostatic phases by [28]. We performed one simulation of each stellar model using the equation of state of [29] with an incompressibility of  $K=220\,{\rm MeV}$  and added comparison models with the SFHo EOS [30] and the EOS of [31] for the one with  $M_{\rm ZAMS}=15\,M_{\odot}$  (see Table I for a list of models).

We mapped the pre-collapse state of the stars to a<sup>176</sup> spherical coordinate system with  $n_r=400$  zones in ra-<sup>177</sup> dial direction distributed logarithmically with a mini-<sup>178</sup> mum grid width of  $(\Delta r)_{\rm min}=400$  m and an outer radius of  $r_{\rm max}=8.3\times10^9$  cm and  $n_\theta=128$  equidistant cells in angular direction. For the neutrino energies, we used a logarithmic grid with  $n_e=10$  bins up to 240 MeV.

All spherical and most axisymmetric models fail to 181 achieve shock revival during the time of our simula-182 tions. Only the two stars with the highest masses, \$25183 and \$40, develop relatively late explosions in axisym-184 metry. Consequently, mass accretion onto the PNSs185 proceeds at high rates for a long time in all cases and 186 causes them to oscillate with their characteristic frequen-187 cies. The final masses of the PNSs are in the range of 188  $M_{\rm PNS}=1.47-2.33\,M_{\odot}$ , i.e., insufficient for producing a189 black hole.

Simulation	$M_{ m ZAMS}[M_{\odot}]$	EOS	$t_{ m f}[ m s]$	explosion	$M_{\rm PNS}[M_{\odot}]$
s11	11.2	LS220	1.86	×	1.47
s15	15.0	LS220	1.66	×	2.00
s15S	15.0	SFHo	1.75	×	2.02
s15G	15.0	$\operatorname{GShen}$	0.97	×	1.86
s20	20.0	LS220	1.53	×	1.75
s25	25.0	LS220	1.60	0.91	2.33
s40	40.0	LS220	1.70	1.52	2.23

TABLE I. List of axisymmetric simulations. We present the name of the models, the initial mass of the progenitors, and the EOS used, and the final post-bounce time of the simulations. For models which explode, we list the time at which the shock starts to expand in column "explosion"; otherwise, a  $\times$  sign is displayed. The final column indicates the mass of the PNS at the end of the simulation.

#### III. METHODS DESCRIPTION

In this section, we outline a strategy for estimating the time evolution of the ratio  $r = M_{\rm PNS}/R_{\rm PNS}^2$  of the mass of the PNS and its squared radius (in units of solar mass and km) from the observation of the  $^2g_2$  oscillation mode in the gravitational wave detector data. An integral part of this strategy is the universal relations that relate the characteristic frequency of the PNS oscillation f, g and p modes with the mass and the radius of the PNS, the shock radius and the total mass inside the shock as demonstrated in [?].

Using 25 spherically symetric (1D) simulations obtained with the AENUS-ALCAR code [24] and the Co-CoNuT [25] code, we parametrize the ratio with a cubic polynomial regression with heteroscedastic errors

$$r_i = \beta_1 f_i + \beta_2 f_i^2 + \beta_3 f_i^3 + \epsilon_i \tag{1}$$

where  $\epsilon_i$  are assumed to be independent zero-mean Gaussian errors with variances  $\sigma_i^2$  that increase with frequency  $f_i$ . The model for frequency-dependent variances is

$$\log \sigma_i = \alpha_0 + \alpha_1 f_i + \alpha_2 f_i^2 + \delta_i \tag{2}$$

with independent and identically zero-mean Gaussian errors  $\delta_i$ . The R-package lmvar [32] that implements a maximum likelihood approach was used to fit the model.

The best fitting model amongst polynomials of degree 1, 2, and 3 was chosen according to the Aikaike information criterion with coefficients given in Table II, which is actually the model defined in (1). The data and fit of the model including 95% confidence bands are displayed in Figure 1.

To develop the method we considered the gravitational wave signal s20-gw-10kpc described in Section II, originally sampled at 16384 Hz but resampled at 4096 Hz. A spectrogram of this signal is shown in Figure 2 based on autoregressive estimates of the local spectra for successive time intervals of length 200 with a 90% overlap.

Coefficient	Estimate	Standard error	
$\beta_1$	$1.00 \times 10^{-06}$	$2.12 \times 10^{-08}$	
$eta_2$	$-8.22 \times 10^{-10}$	$5.00 \times 10^{-11}$	
$eta_3$	$1.01 \times 10^{-12}$	$2.70 \times 10^{-14}$	
$lpha_0$	$-1.02 \times 10^{+01}$	$6.80 \times 10^{-02}$	
$lpha_1$	$7.24 \times 10^{-04}$	$1.56 \times 10^{-04}$	
$\alpha_2$	$6.23 \times 10^{-07}$	$8.15 \times 10^{-08}$	

TABLE II. Estimate and standard error of the coefficients of the best fit model describing the ratio  $r = M_{\rm PNS}/R_{\rm PNS}^2$  as function of the frequency of the  $^2g_2$  mode.

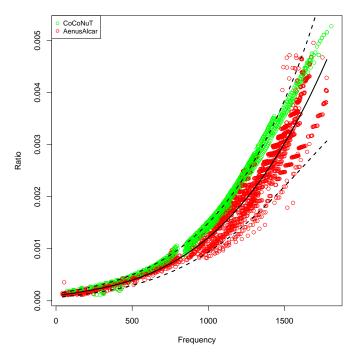


FIG. 1. Ratio  $M_{\rm PNS}/R_{\rm PNS}^2$  from 25 1D simulations AENUS-ALCAR (red) and CoCoNuT (green) code. The solid line is the maximum likelihood estimate of heteroscedastic cubic<sup>210</sup> model with 95% confidence bands (dashed lines) considering<sup>211</sup> the AENUS-ALCAR data points.

The dominant emission mode corresponds to the PNS os- $_{215}$  cillation  $^2g_2$ -mode. We have developed a time-frequency  $_{216}$  method to track the ridge m(t) in the spectrogram, tak- $_{217}$  ing into account that it is monotonically increasing as  $_{218}$  time goes, a property of the  $^2g_2$ -mode. Starting from either the left- or right-most column of the time-frequency  $_{219}$  matrix we identify and trace the sequence of amplitude peaks within a certain frequency band given the monotonicity constraint. Appendix A is providing more details on the reconstruction of the g mode ridge.

We collect the instantaneous frequency  $f(t_i)$  corresponding to the ridge  $m(t_i)$  for the midpoint  $t_i$  of each<sub>222</sub> local time interval of the spectrogram and interpolating<sub>223</sub> f(t) for values in between the  $t_i$ . We then use equation<sub>224</sub> (??) to obtain estimates of the time evolution of the ra-<sub>225</sub> tio together with 95% confidence intervals. An exemple<sub>226</sub>

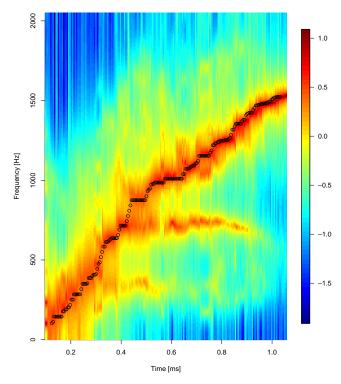


FIG. 2. Spectrogram of the gravitational wave signal s20-gw-10kpc sampled at 4096 Hz. The spectrogram is obtained using data streach of 200 samples overlapping at 90% with each other.

is given in Figure 3 where the red points are the point estimates and the grey bands represent 95% confidence bands. Ratio values computed using the mass and radius values obtained from the simulation code are shown in black.

In this case, for a GW signal without any noise, the coverage of our 95% confidence band is 94%. In the next section we investigate the performance of reconstruction of r(t) when the gravitational wave signal is embedded in noise.

# IV. DETECTION SENSITIVITY WITH ADVANCED GRAVITATIONAL WAVE DETECTORS

To estimate how accurately we can infer the time evolution of  $r = M_{\rm PNS}/R_{\rm PNS}^2$  in the gravitational wave detector data, we have added s20-gw-10kpc GW signal to Gaussian noise realisations whose power spectral density follows advanced LIGO spectrum [33]. We have varied

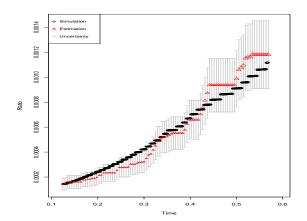


FIG. 3. Ratio  $M_{\rm PNS}/R_{\rm PNS}^2$  as function of time extracted from the  $^2g_2$ -mode of the s20-gw-10kpc signal (red points and the 95% confidence belt in grey) compared to the ratio value derived from the PNS mass and radius given by the simulation code (black points).

the distances to the source, covering a large range of distances for which a detection in second generation of gravitational wave detectors is feasible. The source is optimally oriented with respect to the gravitational wave detector. We are assuming a GW signal from a core collapse phenomena has been identified in the data and that the beginning of the GW signal is known. The data<sup>253</sup> (signal embedded in noise) are whitened using the func-<sup>254</sup> tion *prewhiten* of the R-package TSA. An auto-regressive<sup>255</sup> model with maximal 100 coefficients has been used.

For each of the noise realisations, we reconstruct the ra- $_{258}$  tio time series  $r_i$  of length N and compute two quantities  $_{259}$  that compare  $r_i$  to ratio  $r_i^0$  derived from the PNS  ${\rm mass}_{260}$  and radius generated by the simulation code that  ${\rm pro-}_{261}$  duces \$20-gw-10kpc. measure the estimation accuracy. The first quantity is the coverage probability  $(covpbb)_{263}$  which is the fraction of the ratio  $r_i^0$  values that fall within the 95% confidence interval of  $r_i$ . We also compute the precision value given by

$$precision = \sum_{1}^{N} \frac{|r_i - r_i^0|}{r_i^0}$$
 (3)

Figure 4 is showing the median of covpbb and  $precision^{273}$  as function of the distance of the source as well as the<sup>274</sup> confidence belt corresponding to the median absolute de-<sup>275</sup> viation.

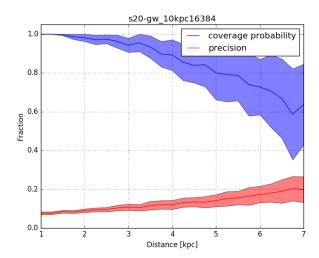


FIG. 4. covpbb and precision for  $\verb"s20-gw-10kpc"$  signal embedded in aLIGO noise at different distance from the Earth. The shaded regions are given by the median absolute deviation.

### V. DISCUSSION

Acknowledgments —

## Appendix A G-MODE RECONSTRUCTION

Given the spectrogram and an specified time interval for the g-mode reconstruction, our proposal method works as follows. The starting point must be specified. It can be either at the beginning or at the end of the signal. Then, in one of these extremes, the maximum energy value is identified, registering its frequency. This is done independently for a number of consecutive time intervals. Then we calculate the median of these frequency values, providing a robust starting value for the g-mode reconstruction.

The starting frequency value is the first g-mode estimate for the first or the last time interval, depending on the specified starting location. If the reconstruction is set to start at the beginning of the signal, the reconstruction will be done progressively over the time intervals, where each maximum frequency value will be calculated within a frequency range specified by the previous g-mode estimate. Given the non-decreasing behaviour of the true g-mode values, the g-mode estimates will be forced to be greater or equal than the one estimated for its previous time interval, and lower than a specified upper limit. As a result, the g-modes estimates will be a non-decreasing sequence of frequency values.

If the reconstruction is set to start at the end of the signal, the g-modes will be estimated backward in time. Each maximum frequency is calculated within a range determined by its successor (in time) g-mode estimate.

These estimates are forced to be lower or equal than its<sub>289</sub> successor (in time) estimate, but greater than a specified<sub>290</sub> lower limit. Thus, a non-decreasing sequence of g-mode<sub>291</sub> estimates is guaranteed.

281

282

284

285

287

299

300

301

302

303

304

305

306

307

308

309

310

311

312

313

314

315

316

317

318

319

320

321

322

323

324

325

326

327

328

329

330

331

332

333

334

335

336

337

338

339

340

341

342

343

344

345

346

347

This g-mode reconstruction method works if and only if the signal is strong enough to provide information about the g-mode, which is reflected in the spectrogram.

Given the sequence of g-mode estimates, the confidence<sub>297</sub> band will be calculated by using the model defined in<sub>298</sub>

- (??). The g-mode estimates are frequency values which we use as predictors in the model in order to generate confidence intervals for the ratios. Since the g-mode estimates are indexed by time, the confidence intervals for the ratios are too. Thus, we generate the confidence band by interpolating the lower and upper limits of the collection of consecutive confidence intervals, which will be valid for the time range of the g-mode estimates. This confidence band is used to estimate the coverage probabilities in our simulation studies presented below.
- S.E. Gossan, P. Sutton, A. Stuver, M. Zanolin, K. Gill,<sup>348</sup> and C. Ott, "Observing gravitational waves from core-<sup>349</sup> collapse supernovae in the advanced detector era," Phys-<sup>350</sup> ical Review D 93 (2016), 10.1103/physrevd.93.042002. <sup>351</sup>
- [2] C. D. Ott, H. Dimmelmeier, A. Marek, H.-T. Janka, 352
   B. Zink, I. Hawke, and E. Schnetter, "Rotating col-353 lapse of stellar iron cores in general relativity," Classi-354
   cal and Quantum Gravity 24, 139-+ (2007), arXiv:astro-355
   ph/0612638.
- [3] E. Abdikamalov, S. Gossan, A. M. DeMaio, and C. D.357 Ott, "Measuring the angular momentum distribution in358 core-collapse supernova progenitors with gravitational359 waves," Phys. Rev. D **90**, 044001 (2014), arXiv:1311.3678360 [astro-ph.SR].
- [4] Sherwood Richers, Christian D. Ott, Ernazar Abdika-362 malov, Evan O'Connor, and Chris Sullivan, "Equation of 363 state effects on gravitational waves from rotating core col-364 lapse," Phys. Rev. D 95, 063019 (2017), arXiv:1701.02752365 [astro-ph.HE].
- [5] K.D. Kokkotas and B.G. Schmidt, "Quasi-normal modes<sub>367</sub> of stars and black holes," Living Rev. Rel. 2, 2 (1999). 368
- [6] John L. Friedman and Nikolaos Stergioulas, Rotating Rel-369 ativistic Stars (2013).
- [7] J. W. Murphy, C. D. Ott, and A. Burrows, "A<sub>371</sub> Model for Gravitational Wave Emission from Neutrino-<sub>372</sub> Driven Core-Collapse Supernovae," Astrophys. J. **707**,<sub>373</sub> 1173 (2009).
- [8] Pablo Cerdá-Durán, Nicolas DeBrye, Miguel A. Aloy,375 José A. Font, and Martin Obergaulinger, "Gravitational376 Wave Signatures in Black Hole Forming Core Collapse,"377 Astrophys. J. Lett. 779, L18 (2013), arXiv:1310.8290378 [astro-ph.SR].
- [9] B. Müller, H.-T. Janka, and A. Marek, "A New Multi-380 dimensional General Relativistic Neutrino Hydrodynam-381 ics Code of Core-collapse Supernovae. III. Gravitational382 Wave Signals from Supernova Explosion Models," Astro-383 phys. J. 766, 43 (2013), arXiv:1210.6984 [astro-ph.SR]. 384
- [10] Konstantin N. Yakunin, Anthony Mezzacappa, Pedro385
   Marronetti, Shin'ichirou Yoshida, Stephen W. Bruenn,386
   W. Raphael Hix, Eric J. Lentz, O. E. Bronson Messer,387
   J. Austin Harris, Eirik Endeve, John M. Blondin, and388
   Eric J. Lingerfelt, Phys. Rev. D 92, 084040 (2015),389
   arXiv:1505.05824 [astro-ph.HE].
- [11] Takami Kuroda, Kei Kotake, and Tomoya Takiwaki, "A<sub>391</sub> New Gravitational-wave Signature from Standing Accre-<sub>392</sub> tion Shock Instability in Supernovae," Astrophys. J. Lett.<sub>393</sub> 829, L14 (2016), arXiv:1605.09215 [astro-ph.HE].
- [12] H. Andresen, B. Müller, E. Müller, and H. Th. Janka, 395
  "Gravitational wave signals from 3D neutrino hydrody-396

- namics simulations of core-collapse supernovae," MNRAS 468, 2032–2051 (2017), arXiv:1607.05199 [astro-ph.HE].
- [13] P. N. McDermott, H. M. van Horn, and J. F. Scholl, "Nonradial g-mode oscillations of warm neutron stars," Astrophys. J. 268, 837–848 (1983).
- [14] A. Reisenegger and P. Goldreich, "A new class of g-modes in neutron stars," Astrophys. J. 395, 240–249 (1992).
- [15] V. Ferrari, L. Gualtieri, J. A. Pons, and A. Stavridis, "Gravitational waves from rotating proto-neutron stars," Classical and Quantum Gravity 21, S515–S519 (2004), astro-ph/0409578.
- [16] A. Passamonti, M. Bruni, L. Gualtieri, and C. F. Sopuerta, "Coupling of radial and nonradial oscillations of relativistic stars: Gauge-invariant formalism," Phys. Rev. D 71, 024022 (2005), gr-qc/0407108.
- [17] H. Dimmelmeier, N. Stergioulas, and J. A. Font, "Non-linear axisymmetric pulsations of rotating relativistic stars in the conformal flatness approximation," MNRAS 368, 1609–1630 (2006), astro-ph/0511394.
- [18] C. J. Krüger, W. C. G. Ho, and N. Andersson, "Seismology of adolescent neutron stars: Accounting for thermal effects and crust elasticity," Phys. Rev. D 92, 063009 (2015), arXiv:1402.5656 [gr-qc].
- [19] G. Camelio, A. Lovato, L. Gualtieri, O. Benhar, J. A. Pons, and V. Ferrari, "Evolution of a proto-neutron star with a nuclear many-body equation of state: neutrino luminosity and gravitational wave frequencies," ArXiv eprints (2017), arXiv:1704.01923 [astro-ph.HE].
- [20] H. Sotani and T. Takiwaki, "Gravitational wave asteroseismology with protoneutron stars," Phys. Rev. D 94, 044043 (2016), arXiv:1608.01048 [astro-ph.HE].
- [21] A. Torres-Forné, P. Cerdá-Durán, A. Passamonti, and J. A. Font, "Towards asteroseismology of core-collapse supernovae with gravitational-wave observations - I. Cowling approximation," MNRAS 474, 5272–5286 (2018), arXiv:1708.01920 [astro-ph.SR].
- [22] A. Torres-Forné, P. Cerdá-Durán, A. Passamonti, M. Obergaulinger, and J. A. Font, "Towards asteroseismology of core-collapse supernovae with gravitational wave observations - II. Inclusion of space-time perturbations," MNRAS 482, 3967–3988 (2019), arXiv:1806.11366 [astro-ph.HE].
- [23] A. Torres-Forné, P. Cerdá-Durán, M. Obergaulinger, B. Müller, and J. Font, "Universal relations for gravitational-wave asteroseismology of proto-neutron stars," Physical Review Letters 123, 051102 (2019).
- [24] O. Just, M. Obergaulinger, and H.-T. Janka, "A new multidimensional, energy-dependent two-moment transport code for neutrino-hydrodynamics," MNRAS 453,

3386-3413 (2015), arXiv:1501.02999.

397

398

399

400

401

402

403

404

405

406

407

408

409

410

411

412

- [25] P. Cerdá-Durán, J. A. Font, L. Antón, and E. Müller,<sup>414</sup> "A new general relativistic magnetohydrodynamics code<sup>415</sup> for dynamical spacetimes," A&A 492, 937–953 (2008),<sup>416</sup> arXiv:0804.4572.
- [26] B. Müller and H. Th. Janka, "Non-radial instabilities<sup>418</sup> and progenitor asphericities in core-collapse supernovae,"<sup>419</sup> MNRAS 448, 2141–2174 (2015), arXiv:1409.4783 [astro-420 ph.SR].
- [27] A. Marek, H. Dimmelmeier, H.-T. Janka, E. Müller, and 222 R. Buras, "Exploring the relativistic regime with Newto-423 nian hydrodynamics: an improved effective gravitational 424 potential for supernova simulations," A&A 445, 273–289 425 (2006).
- [28] S. E. Woosley, A. Heger, and T. A. Weaver, "The evolu-427 tion and explosion of massive stars," Reviews of Modern

- Physics 74, 1015–1071 (2002).
- [29] J. M. Lattimer and F. Douglas Swesty, "A generalized equation of state for hot, dense matter," Nuclear Physics A 535, 331–376 (1991).
- [30] A. W. Steiner, M. Hempel, and T. Fischer, "Corecollapse Supernova Equations of State Based on Neutron Star Observations," Astrophys. J. 774, 17 (2013), arXiv:1207.2184 [astro-ph.SR].
- [31] G. Shen, C. J. Horowitz, and S. Teige, "New equation of state for astrophysical simulations," Phys. Rev. C 83, 035802 (2011), arXiv:1101.3715 [astro-ph.SR].
- [32]
- [33] Lisa Barsotti, Peter Fritschel, Matthew Evans, and Slawomir Gras, "Updated advanced ligo sensitivity design curve," (2018).