

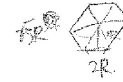
**Engineering Materials, Course No. 4202402, CCU ME**  
**Mid-term Exam (I) 99. 10. 28.**

Lectured by: 敦仲寧

1. Total score: 120, 2. Close-book, 3. Using calculator is allowed, 4. Keep question sheets and return answering sheets.

1. (a) List all primary and secondary interatomic bonds and give a sketch example of each bond. (15%)

(b) Briefly describe the conditions for the formation of an ionic bond between atoms. (5%)



$$\frac{\sqrt{3}}{4} \times 4R^2 = \sqrt{3}R^2$$

$$2a^2 = 4 \times 16R^2$$

$$a = 2\sqrt{2}R$$

$$3a^2 = 16R^2$$

$$a = \frac{4}{\sqrt{3}}R$$

2. (a) Sketch a tetragonal unit cell and a monoclinic unit cell and give for each crystal system the lattice constants (a, b, c) relationship and interaxial angles ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) relationship. (8 %)

(b) How many bravais crystal systems are there? (2 %)

3. (a) What is the atomic packing factor APF of an FCC and a HCP atomic structure? (3 %)

(b) If the APF of an FCC and a HCP atomic structure has the same value, explain why they have the same value? (6 %)

(c) In spite of having the same value of APF, why FCC and HCP looks different? (6 %)

(To answer b and c, you have to sketch the features of the atomic arrangement in FCC and in HCP to give your explanations.)

4. (a) Show that the minimum cation-to-anion radius ratio  $r/R$  for the  $CN=3$  is 0.155 (6%)

(b) List all the polymorphic forms of carbon (either in English or Chinese). (Do not sketch atomic structure.) (6%)

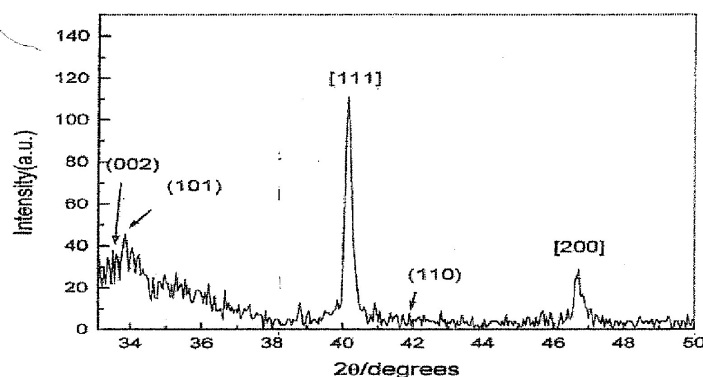
(c) To what contribution was the Nobel Prize of Physics 2010 granted? (3%)

5. (a) Determine the angle between crystallographic planes (1 1 1) and direction  $[1 \ 1 \ 0]$ . (5%)

(b) Find the Miller indices of a plane determined by the crystallographic direction  $[1 \ \underline{1} \ 1]$  and  $[2 \ \underline{1} \ 0]$ . (5%)

$$\frac{1}{2} \quad -1 \quad 0$$

6. X-ray diffraction on a pure metal reveals diffraction patterns with first five peaks at  $2\theta = 32.3^\circ, 37.5^\circ, 54.1^\circ, 64.4^\circ$ , and  $67.6^\circ$ , the wavelength of X-ray from a Co target is  $\lambda = 0.17902 \text{ nm}$ .
- Index the planes (h k l) of these five peaks. (10%)
  - Determine the interplanar spacing of the first peak (5%)
  - For the first peaks, determine the atomic radius of this metal. (5%)
  - What should this metal be? (Check table) (3%)
  - In the figure below, which index (or which indices) of the diffraction peak (or peaks) may be wrong? Briefly give your reasons. (7%)



Characteristics of Selected Elements

Element	Symbol	Atomic Number	Atomic Weight (amu)	Density of Solid, 20°C (g/cm³)	Crystal Structure, 20°C	Atomic Radius (nm)	Ionic Radius (nm)	Most Common Valence	Melting Point (°C)
Aluminum	Al	13	26.98	2.71	FCC	0.143	0.053	3+	660.4
Argon	Ar	18	39.95	—	—	—	—	Inert	-189.2
Barium	Ba	56	137.33	3.5	BCC	0.217	0.136	2+	725
Beryllium	Be	4	9.012	1.85	HCP	0.114	0.035	2+	1278
Boron	B	5	10.81	2.34	Rhomb.	—	0.023	3+	2300
Bromine	Br	35	79.90	—	—	—	0.196	1-	-7.2
Cadmium	Cd	48	112.41	8.65	HCP	0.149	0.095	2+	321
Calcium	Ca	20	40.08	1.55	FCC	0.197	0.100	2+	839
Carbon	C	6	12.011	2.25	Hex.	0.071	~0.016	4+	(sublimes at 3367)
Cesium	Cs	55	132.91	1.87	BCC	0.265	0.170	1+	28.4
Chlorine	Cl	17	35.45	—	—	—	0.181	1-	-101
Chromium	Cr	24	52.00	7.19	BCC	0.125	0.063	3+	1875
Cobalt	Co	27	58.93	8.9	HCP	0.125	0.072	2+	1495
Copper	Cu	29	63.55	8.94	FCC	0.128	0.096	1+	1085
Fluorine	F	9	19.00	—	—	—	0.133	1-	-220
Gallium	Ga	31	69.72	5.90	Ortho.	0.122	0.062	3+	29.8
Germanium	Ge	32	72.59	5.32	Dia. cubic	0.122	0.053	4+	937
Gold	Au	79	196.97	19.32	FCC	0.144	0.137	1+	1064
Helium	He	2	4.003	—	—	—	—	Inert	-272 (at 26 atm)

試卷編號	CCUME 99A - 4202402 - M001			任課老師	
學年	學期	日期	20__/__/__	試別	<input type="checkbox"/> 平時考 <input type="checkbox"/> 期中考 <input type="checkbox"/> 學期考
科目	工程材料			評分	
姓名	詹聲聰	班別	機械2A	學號	498420013

1. (a) primary: 金屬鍵, 共價鍵, 離子鍵 +6  
ex. Cu CO<sub>2</sub> NaCl

secondary: 凡德瓦爾力, 氫鍵 +1  
ex. CO<sub>2</sub> 分子間 H<sub>2</sub>O 分子間

59

(b) 正離子有顆電子跑到負離子那, 與正離子的電子形成離子鍵, 形成穩定態 ex. Na → Cl

2. (a) tetragonal



$$a \neq b \neq c$$

$$\alpha = \beta = \gamma = 90^\circ$$

+1

monoclinic (b)



$$a \neq b \neq c$$

$$\alpha = \beta = 90^\circ$$

$$\gamma \neq 90^\circ$$

14 種

+2

3. (a)

FCC and HCP 的 APF = 0.74

(b) 它們有同樣的配位數, 且 FCC 在某特定角度看跟 HCP 一樣

HCP



FCC



+1 皆為最密堆積

(c)

FCC → ACBACB



HCP → ABABAB



+6

(a)

(b)

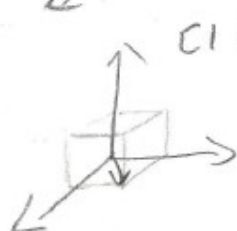
X

+0

(c)

$C_{60}$

5. (a)  $[111]$   $\alpha = \beta = \gamma = 60^\circ$

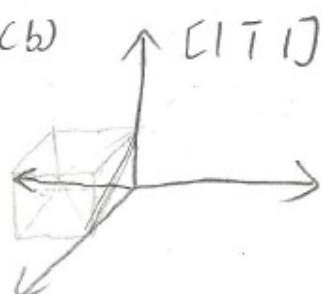


$[110]$

$\alpha = \beta = 45^\circ$   $\gamma = 0^\circ$

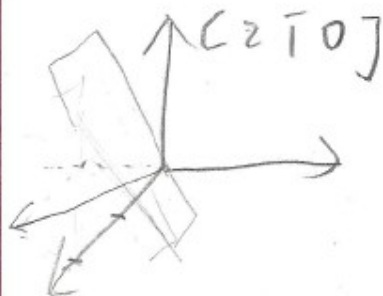
+0

(b)



$[1\bar{1}1]$

plane =  $(1\bar{1}1)$



$[2\bar{1}0]$

plane =  $(2\bar{1}0)$

$2\theta$	$\theta$	$\sin\theta$	$\sin^2\theta$	$h^2+k^2+l^2$	$(hkl)$	K
32.3	16.15	0.2781	0.0774	3	(111)	38.7597
37.5	18.75	0.3214	0.1033	4	(200)	38.7222
54.1	27.05	0.4548	0.2068	8	(220)	38.6847
64.4	32.2	0.5329	0.2840	11	(311)	38.7324
67.6	33.8	0.5563	0.3095	12	(222)	38.7722

+10

(a)

(111) (200) (220) (311) (222)

(b)

(111)

$$n\lambda = 2d\sin\theta$$

$$d = \frac{a}{\sqrt{h^2+k^2+l^2}}$$

$$d = \frac{0.17902}{2 \times \sin 16.15^\circ} = 0.3218 \text{ (nm)}$$

$$a = 0.3218 \times \sqrt{3} = 0.5574 \text{ (nm)}$$

$$\text{面積} = a^2 = 0.3107 \text{ (nm}^2\text{)}$$

+5

(c)

$$\text{FCC} \Rightarrow a = \frac{4}{\sqrt{2}} R$$

$$R = \frac{\sqrt{2}}{4} \times 0.5574 = 0.1971 \text{ (nm)}$$

+5

(d)

Ca

+5

(e)

(002), (110) are wrong

因為 (002) 跟 (200) 是 family 但它卻在 (111) 之前  
(110) 也在 (111) 之後

且由於 (111) 和 (200) 相當明顯, 所以應是 FCC

A: 品 (002), (101), (110) are wrong #

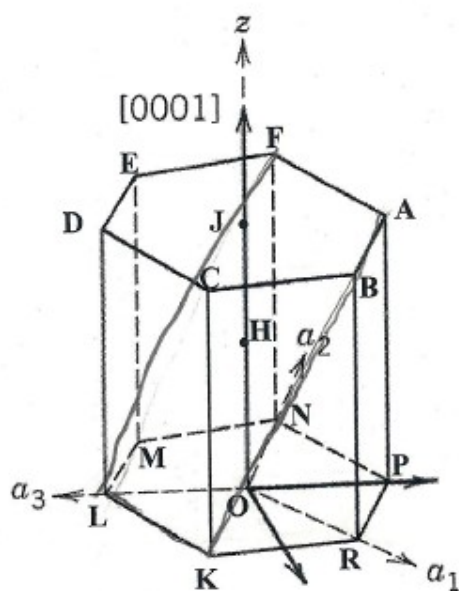
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7. Determine Miller-Bravais indices *step by step!*

(a) Plane FAKL (this plane also passes through point H) (5%)

(b) Plane APKC (5%)

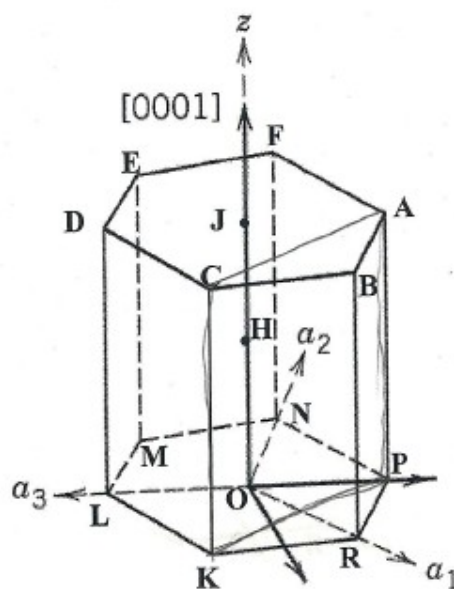


(a)

$$(a_1, a_2, a_3, z)$$

$$\Rightarrow (\infty, \bar{1}, 1, \frac{1}{2}) \quad \text{因難}$$

$$\Rightarrow (0, \bar{1}, 2)$$



(b)

$$(a_1, a_2, a_3, z)$$

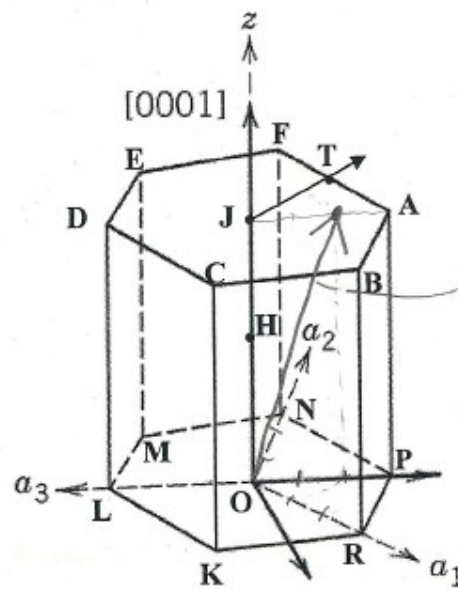
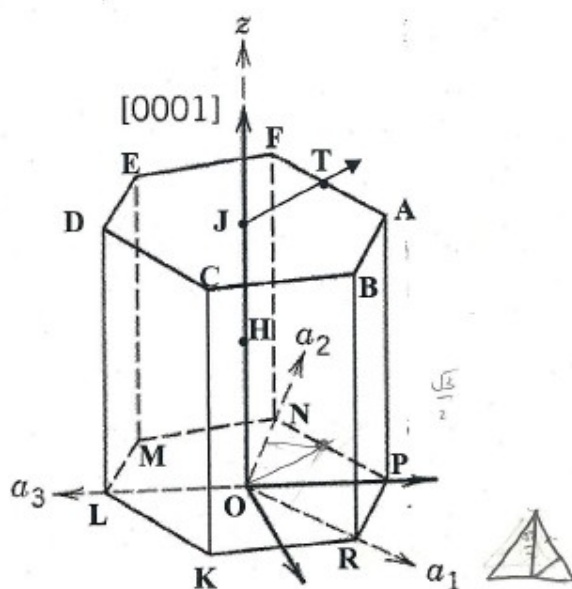
$$\Rightarrow (\frac{1}{2}, \bar{1}, \bar{1}, \infty)$$

$$\Rightarrow (2, \bar{1}, \bar{1}, 0)$$

+8

7. (c) Determine Miller-Bravais indices of direction JT as indicated. (5%)

(d) Sketch the  $[1\ 1\ \bar{2}\ 3]$  direction. (5%)



$$\begin{aligned} & (c) (a_1, a_2, a_3, z) \\ & \Rightarrow \left( \frac{1}{3}, \frac{2}{3}, \frac{\bar{2}}{3}, 0 \right) \end{aligned}$$

$$\begin{aligned} & (d) (1\ 1\ \bar{2}\ 3) \\ & = \left( \frac{1}{6}, \frac{1}{6}, \frac{\bar{2}}{3}, \frac{1}{2} \right) \\ & = \left( \frac{1}{3}, \frac{1}{3}, \frac{\bar{2}}{3}, 1 \right) \end{aligned}$$

+5