

# Definitions

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## Sentence

- Is grammatically correct

## Statement

- Sentence
- Asserts something being true or false
  - Either true or false

## Proposition

- The meaning of a statement regardless of syntax or presentation of the sentence

## Argument

- Propositions (**Premises + Conclusion**)
  - One claims to be supported by the rest accepted premises
  - **Premise (Accepted fact) --prove--> Conclusion**
- Hidden premise
  - Assumed premise

## Explanation

- Propositions
  - One claims to be shed light on by the rest
  - **Explanan --explain--> Explanandum (Accepted fact)**

# Deductive/Inductive arguments

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## Deductive arguments

- If all premises are true -> **Impossible** to be false
- Can **conclusively** support conclusions

## Inductive arguments

- If all premises are true -> **Improbable** to be false
- Can **strongly** support conclusions

# Possibilities

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- **Technological**: Within current technological constraints
- **Physical**: Within physical constraints

- **Logical:** Within logical constraints
  - No logical contradictions
  - Within all possible worlds
- Technological  $\in$  Physical  $\in$  Logical

## Proposition types

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- **Tautological:** Necessarily true
  - Proves itself
- **Self-contradictory:** Necessarily false
  - Disproves itself
- **Contingent:** Neither
  - Requires external knowledge to be proven

## Argument evaluation standards

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### Deductive standard

Validity (valid/invalid?)

- Truth-preserving?
  - **Invalid:** True premise + False conclusion  $\rightarrow$  Possible
    - **Conditionally valid** (!!!)
  - **Valid:** True premise + False conclusion  $\rightarrow$  Impossible
    - **Self-contradictory premise** (Impossible true premise)
    - **Tautological conclusion** (Impossible false conclusion)

Soundness (sound/unsound?)

- Valid argument + True premise

### Inductive standard

Strength (**strong/weak**?)

- Probable conclusion?
- Not binary/all-or-nothing

Cogency (cogent/uncogent?)

- Strong argument + True premise

## Categorical syllogism

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### Syntax

- *Quantifier - subject term - copula - predicate term*

- All A are B
- Types:
  - **A**: All X are Y
  - **E**: No X are Y
  - **I**: Some X are Y
  - **O**: Some X are not Y
  - Affirmative: **A, I**; Negative: **E, O**
  - Universal: **A, E**; Particular: **I, O**
- Some = Not zero
- Terms = **NOUNS**
- "All x identical to x" | "所有與 x 等同的 x"

## Venn diagrams

- /// = Emptiness
- **X** = Existence

## Standardisation

### Conversion

- *Only* truth-preserving for **E, I**
- 1. Switch subject and predicate term

### Contraposition

- *Only* truth-preserving for **A, O**
- 1. Switch subject with predicate
- 2. Toggle "non-" to both terms

### Obversion

- *Always* truth-preserving
- 1. Negate the quality (**No** <-> **All** | **Some** <-> **Some...not**)
- 2. Toggle "non-" to both terms

## Syllogism

- Two-premise argument
  - Three terms total
  - Each term appears twice
  - None term appears twice in a single proposition
- **Major term**: Predicate term of conclusion
- **Minor term**: Subject term of conclusion
- **Middle term**: Not present in conclusion

## Mood & Figure

Figure

1	2	3	4
<i>M P</i>	<i>P M</i>	<i>M P</i>	<i>P M</i>
<i>S M</i>	<i>S M</i>	<i>M S</i>	<i>M S</i>
S P	S P	S P	S P

Mood

Valid

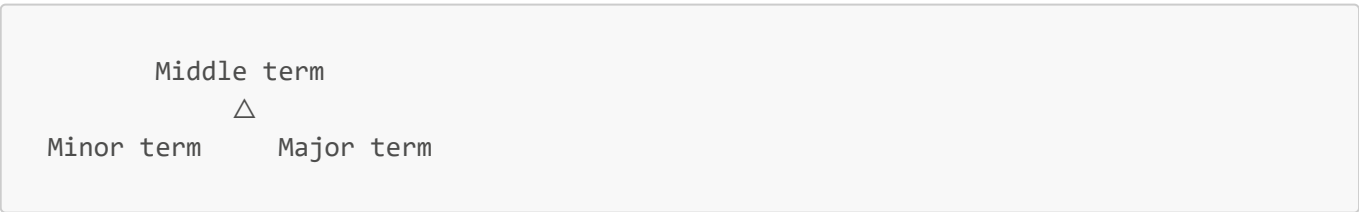
1	2	3	4
AAA	AEE	AII	AEE
AII	AOO	EIO	EIO
EAE	EAE	IAI	IAI
EIO	EIO	AOO	

Invalid (Conditionally valid)

1	2	3	4
AAI	AEO	AAI	AAI
EAO	EAO	EAO	EAO
			EAO

Venn diagram

- $\Delta$ ; circles at vertices



Opposition

- **Contradictory**
  - Cannot be both true + Cannot be both false
  - **A**  $\leftrightarrow$  **O**
  - **E**  $\leftrightarrow$  **I**
- **Contrary**
  - Cannot be both true + Can be both false
  - **A**  $\leftrightarrow$  **E**

- **Subcontrary**
  - Can be both true + Cannot be both false
  - **I**  $\leftrightarrow$  **O**
- **Subaltern**
  - For  $b$  is a subaltern of  $a$  ( $b \rightarrow a$ ),
    - True  $a \rightarrow$  True  $b$
    - False  $b \rightarrow$  False  $a$
  - **I**  $\rightarrow$  **A**
  - **O**  $\rightarrow$  **E**

## Propositional Logic

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- **Simple proposition:** Proposition
- **Compound proposition:** Proposition + Logic (not, if, unless, ...)

### Logical Operators

Operator	Function	Translation	T/T	T/F	F/T	F/F
$\sim$	Negation	not, not the case, ...				
$\cdot$	Conjunction	and, also, but, ...	<b>T</b>	<i>F</i>	<i>F</i>	<i>F</i>
$\vee$	Disjunction ( <b>Inclusive</b> )	either...or...	<b>T</b>	<b>T</b>	<b>T</b>	<i>F</i>
$\supset$	Conditional	if...then..., only if...	<b>T</b>	<i>F</i>	<b>T</b>	<b>T</b>
$\equiv$	Bi-conditional	if and only if...	<b>T</b>	<i>F</i>	<i>F</i>	<b>T</b>

### Conditional

- $P \supset Q$ :
  - **P**: antecedent
  - **Q**: consequent
- **Sufficient Condition**
  - $A$  is *sufficient* for  $B$  to occur
  - $\sim A$  does not necessitate for  $\sim B$
  - $A \supset B$
- **Necessary Condition**
  - $A$  is *necessary* for  $B$  to occur
  - $A$  does not necessitate  $B$
  - $B \supset A$
- **Sufficient  $\supset$  Necessary**

### Bi-conditional

- Logically Equivalent
- $P \supset Q == (P \supset Q) \cdot (P \supset Q)$

## Well-formed Formulas

1. Capital letters
2.  $\sim\alpha$
3.  $\alpha \cdot \beta$
4.  $\alpha \vee \beta$
5.  $\alpha \supset \beta$
6.  $\alpha \equiv \beta$
7. Nothing else

## Truth table

- **All False:** Self-contradictory
- **All True:** Tautological
- **True + False:** Contingent
- *Premise / Premise / ... // Conclusion*

## Indirect truth table

- Check validity
  - Assume invalid (true premises + false conclusion)
    - Main operators only
  - Backwards deduction
    - Additional assumptions if necessary
    - All cases contradiction  $\rightarrow$  Contradiction
  - Check contradictions
    - $\geq 1$  contradiction:
      - Wrong assumption
      - $\therefore$  Argument is **valid**
    - 0 contradiction:
      - $\therefore$  Argument is **invalid**
- Check consistency
  - Assume both true
  - ...

## Proposition Relations

- **Logical Equivalent**
  - Always  $\equiv$
- **Contradictory**
  - Always  $\sim$
- **Consistent**
  - $\geq 1$  both true
- **Inconsistent**
  - 0 both true

## Natural Deduction

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## Rules of Inference

- No Implication + Replacement in one step

### Implication

- e.g. (1,2 MT)
- $\alpha * \beta \neq \beta * \alpha$

### Replacement

- $::$  equivalent
- $\leq 3$  replacements in one step

## Proofs

- Indent deduction steps

### Conditional Proof

- Conclusion:  $\alpha \supset \beta$
- Assume premise  $\alpha$  (**ACP**)
- Do until  $\beta$  (**show explicitly**)
- Unindent  $\alpha \supset \beta$  (*Step numbers, CP*)

### Indirect Proof

- Assume  $\sim$ conclusion  $\sim\alpha$  (**AIP**)
- Do until contradiction (**show explicitly**)
- Unindent  $\sim\sim\alpha$  (*Step numbers, IP*)

## Fallacies

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### Formal Fallacy

- Typical errors
- Can be identified from argument structure
- **Affirming the consequent**
- **Denying the antecedent**
- ...

### Informal Fallacy

- Can only be identified from argument content

#### *Fallacies of Relevance*

- Argument irrelevant to conclusion
- **Appeal to force**

- **Appeal to people**
- **Argument against the person**
- **Straw man**
  - Unreasonable exaggeration
- **Red herring**
  - Attention diversion

### *Fallacies of Presumption*

- **Begging the question**
  - Circular argument
- **Complex question**
  - Merge multiple questions
- **False dichotomy**
  - Pretend there are only 2 options

### *Fallacies of Weak Induction*

- **Hasty generalisation**
  - Unrepresentative sample
    - Small sample size
    - Non-random sampling
- **Appeal to unqualified authority**
  - Forged authority
- **Weak analogy**
  - Irrelevant similarities
    - **X:**  $p, q, s$
    - **Y:**  $p, q$
    - $\therefore$  **Y:**  $s$
- **Appeal to ignorance**
  - Not proven false = True
  - Not proven true = false
- **False cause**
- **Slippery slope**
  - Unlikely chain reaction