## Generalized model

## 1 Equations

These are the equations for the model:

$$\frac{dS}{dt} = -(\Lambda^{1} + \Lambda^{2} + \Lambda^{3})S + \omega^{1}R^{1} + \omega^{2}R^{2} + \omega^{3}R^{3} - \delta^{1} - \delta^{2} - \delta^{3}$$
(1)

$$\frac{dE^1}{dt} = -\nu^1 E^1 + \Lambda^1 S + \delta^1 + \Lambda_1^1 R^1 + \Lambda_2^1 R^2 + \Lambda_3^1 R^3 \qquad (2)$$

$$\frac{dE^2}{dt} = -\nu^2 E^2 + \Lambda^2 S + \delta^2 + \Lambda_1^2 R^1 + \Lambda_2^2 R^2 + \Lambda_3^2 R^3 \qquad (3)$$

$$\frac{dE^3}{dt} = -\nu^3 E^3 + \Lambda^3 S + \delta^3 + \Lambda_1^3 R^1 + \Lambda_2^3 R^2 + \Lambda_3^3 R^3 \qquad (4)$$

$$\frac{dI_{pre}^{1}}{dt} = -\gamma_{pre}^{1}I_{pre}^{1} + \nu^{1}E^{1}$$
 (5)

$$\frac{dI_{pre}^{2}}{dt} = -\gamma_{pre}^{2}I_{pre}^{2} + \nu^{2}E^{2} \tag{6}$$

$$\frac{dI_{pre}^3}{dt} = -\gamma_{pre}^3 I_{pre}^3 + \nu^3 E^3 \tag{7}$$

$$\frac{dI_s^1}{dt} = -\gamma_s^1 I_s^1 + f_{pre,s}^1 \gamma_{pre}^1 I_{pre}^1 \tag{8}$$

$$\frac{dI_s^2}{dt} = -\gamma_s^2 I_s^2 + f_{pre,s}^2 \gamma_{pre}^2 I_{pre}^2 \tag{9}$$

$$\frac{dI_s^3}{dt} = -\gamma_s^3 I_s^3 + f_{pre,s}^3 \gamma_{pre}^3 I_{pre}^3 \tag{10}$$

$$\frac{dI_m^1}{dt} = -\gamma_m^1 I_m^1 + f_{pre,m}^1 \gamma_{pre}^1 I_{pre}^1 \tag{11}$$

$$\frac{dI_m^2}{dt} = -\gamma_m^2 I_m^2 + f_{pre,m}^2 \gamma_{pre}^2 I_{pre}^2$$
 (12)

$$\frac{dI_m^3}{dt} = -\gamma_m^3 I_m^3 + f_{pre,m}^3 \gamma_{pre}^3 I_{pre}^3 \tag{13}$$

$$\frac{dI_a^1}{dt} = -\gamma_a^1 I_a^1 + f_{pre,a}^1 \gamma_{pre}^1 I_{pre}^1 \tag{14}$$

$$\frac{dI_a^2}{dt} = -\gamma_a^2 I_a^2 + f_{pre,a}^2 \gamma_{pre}^2 I_{pre}^2 \tag{15}$$

$$\frac{dI_a^3}{dt} = -\gamma_a^3 I_a^3 + f_{pre,a}^3 \gamma_{pre}^3 I_{pre}^3 \tag{16}$$

$$\frac{dH_m^1}{dt} = -\theta_m^1 H_m^1 + f_{m,H}^1 \gamma_m^1 I_m^1 \tag{17}$$

$$\frac{dH_m^2}{dt} = -\theta_m^2 H_m^2 + f_{m,H}^2 \gamma_m^2 I_m^2 \tag{18}$$

$$\frac{dH_m^3}{dt} = -\theta_m^3 H_m^3 + f_{m,H}^3 \gamma_m^3 I_m^3 \tag{19}$$

$$\frac{dH_s^1}{dt} = -\theta_s^1 H_s^1 + f_{s,H}^1 \gamma_s^1 I_s^1 \tag{20}$$

$$\frac{dH_s^2}{dt} = -\theta_s^2 H_s^2 + f_{s,H}^2 \gamma_s^2 I_s^2 \tag{21}$$

$$\frac{dH_s^3}{dt} = -\theta_s^3 H_s^3 + f_{s,H}^3 \gamma_s^3 I_s^3 \tag{22}$$

$$\frac{dR^1}{dt} = -\omega^1 R^1 + f_{s,R}^1 \gamma_s^1 I_s^1 + f_{m,R}^1 \gamma_m^1 I_m^1 + \gamma_a^1 I_a^1 + \theta_m^1 H_m^1 + \theta_s^1 H_s^1 - \Lambda_1^1 R^1 - \Lambda_2^1 R^1$$

$$\frac{dR^2}{dt} = -\omega^2 R^2 + f_{s,R}^2 \gamma_s^2 I_s^2 + f_{m,R}^2 \gamma_m^2 I_m^2 + \gamma_a^2 I_a^2 + \theta_m^2 H_m^2 + \theta_s^2 H_s^2 - \Lambda_2^1 R^2 - \Lambda_2^2 R^2 + \frac{1}{2} (24)$$

$$\frac{dR^3}{dt} = -\omega^3 R^3 + f_{s,R}^3 \gamma_s^3 I_s^3 + f_{m,R}^3 \gamma_m^3 I_m^3 + \gamma_a^3 I_a^3 + \theta_m^3 H_m^3 + \theta_s^3 H_s^3 - \Lambda_3^1 R^3 - \Lambda_3^1 R^3$$