## Generalized model

## 1 Equations

These are the equations for the model:

$$\frac{dS}{dt} = -(\Lambda^{1} + \Lambda^{2} + \Lambda^{3})S + \omega^{1}R^{1} + \omega^{2}R^{2} + \omega^{3}R^{3} - \delta^{1} - \delta^{2} - \delta^{3}$$
(1)

$$\frac{dE^1}{dt} = -\nu^1 E^1 + \Lambda^1 S + \delta^1 + \Lambda_1^1 R^1 + \Lambda_2^1 R^2 + \Lambda_3^1 R^3$$
 (2)

$$\frac{dE^2}{dt} = -\nu^2 E^2 + \Lambda^2 S + \delta^2 + \Lambda_1^2 R^1 + \Lambda_2^2 R^2 + \Lambda_3^2 R^3$$
 (3)

$$\frac{dE^3}{dt} = -\nu^3 E^3 + \Lambda^3 S + \delta^3 + \Lambda_1^3 R^1 + \Lambda_2^3 R^2 + \Lambda_3^3 R^3$$
 (4)

$$\frac{dI_{pre}^{1}}{dt} = -\gamma_{pre}^{1}I_{pre}^{1} + \nu^{1}E^{1}$$
 (5)

$$\frac{dI_{pre}^{2}}{dt} = -\gamma_{pre}^{2}I_{pre}^{2} + \nu^{2}E^{2}$$
 (6)

$$\frac{dI_{pre}^{3}}{dt} = -\gamma_{pre}^{3} I_{pre}^{3} + \nu^{3} E^{3} \tag{7}$$

$$\frac{dI_s^1}{dt} = -\gamma_s^1 I_s^1 + f_{pre,s}^1 \gamma_{pre}^1 I_{pre}^1$$
 (8)

$$\frac{dI_s^2}{dt} = -\gamma_s^2 I_s^2 + f_{pre,s}^2 \gamma_{pre}^2 I_{pre}^2$$
 (9)

$$\frac{dI_s^3}{dt} = -\gamma_s^3 I_s^3 + f_{pre,s}^3 \gamma_{pre}^3 I_{pre}^3 \tag{10}$$

$$\frac{dI_{m}^{1}}{dt} = -\gamma_{m}^{1}I_{m}^{1} + f_{pre,m}^{1}\gamma_{pre}^{1}I_{pre}^{1} \tag{11}$$

$$\frac{dI_{m}^{2}}{dt} = -\gamma_{m}^{2} I_{m}^{2} + f_{pre,m}^{2} \gamma_{pre}^{2} I_{pre}^{2}$$
(12)

$$\frac{dI_m^3}{dt} = -\gamma_m^3 I_m^3 + f_{pre,m}^3 \gamma_{pre}^3 I_{pre}^3$$
 (13)

$$\frac{dI_a^1}{dt} = -\gamma_a^1 I_a^1 + f_{pre,a}^1 \gamma_{pre}^1 I_{pre}^1$$
 (14)

$$\frac{dI_{a}^{2}}{dt} = -\gamma_{a}^{2}I_{a}^{2} + f_{pre,a}^{2}\gamma_{pre}^{2}I_{pre}^{2}$$
 (15)

$$\frac{dI_a^3}{dt} = -\gamma_a^3 I_a^3 + f_{pre,a}^3 \gamma_{pre}^3 I_{pre}^3$$
 (16)

$$\frac{dH_m^1}{dt} = -\theta_m^1 H_m^1 + f_{m,H}^1 \gamma_m^1 I_m^1 \tag{17}$$

$$\frac{dH_m^2}{dt} = -\theta_m^2 H_m^2 + f_{m,H}^2 \gamma_m^2 I_m^2$$
 (18)

$$\frac{dH_m^3}{dt} = -\theta_m^3 H_m^3 + f_{m,H}^3 \gamma_m^3 I_m^3 \tag{19}$$

$$\frac{dH_s^1}{dt} = -\theta_s^1 H_s^1 + f_{s,H}^1 \gamma_s^1 I_s^1 \tag{20}$$

$$\frac{dH_s^2}{dt} = -\theta_s^2 H_s^2 + f_{s,H}^2 \gamma_s^2 I_s^2 \tag{21}$$

$$\frac{dH_s^3}{dt} = -\theta_s^3 H_s^3 + f_{s,H}^3 \gamma_s^3 I_s^3 \tag{22}$$

$$\frac{dR^1}{dt} = -\omega^1 R^1 + f_{s,R}^1 \gamma_s^1 I_s^1 + f_{m,R}^1 \gamma_m^1 I_m^1 + \gamma_a^1 I_a^1 + \theta_m^1 H_m^1 + \theta_s^1 H_s^1 - \Lambda_1^1 R^1 - \Lambda_1^2 R^1 - \Lambda_1^3 R^1 \qquad (23)$$

$$\frac{dR^2}{dt} = -\omega^2 R^2 + f_{s,R}^2 \gamma_s^2 I_s^2 + f_{m,R}^2 \gamma_m^2 I_m^2 + \gamma_a^2 I_a^2 + \theta_m^2 H_m^2 + \theta_s^2 H_s^2 - \Lambda_2^1 R^2 - \Lambda_2^2 R^2 - \Lambda_2^3 R^2$$
 (24)

$$\frac{dR^3}{dt} = -\omega^3 R^3 + f_{s,R}^3 \gamma_s^3 I_s^3 + f_{m,R}^3 \gamma_m^3 I_m^3 + \gamma_a^3 I_a^3 + \theta_m^3 H_m^3 + \theta_s^3 H_s^3 - \Lambda_3^1 R^3 - \Lambda_3^2 R^3 - \Lambda_3^3 R^3$$
 (25)