$$\binom{p}{2} x^2 \, y^{p-2} - \frac{1}{1-x} \frac{1}{1-x^2}$$