

Computer Architecture: MIPS Multi-Cycle Datapath

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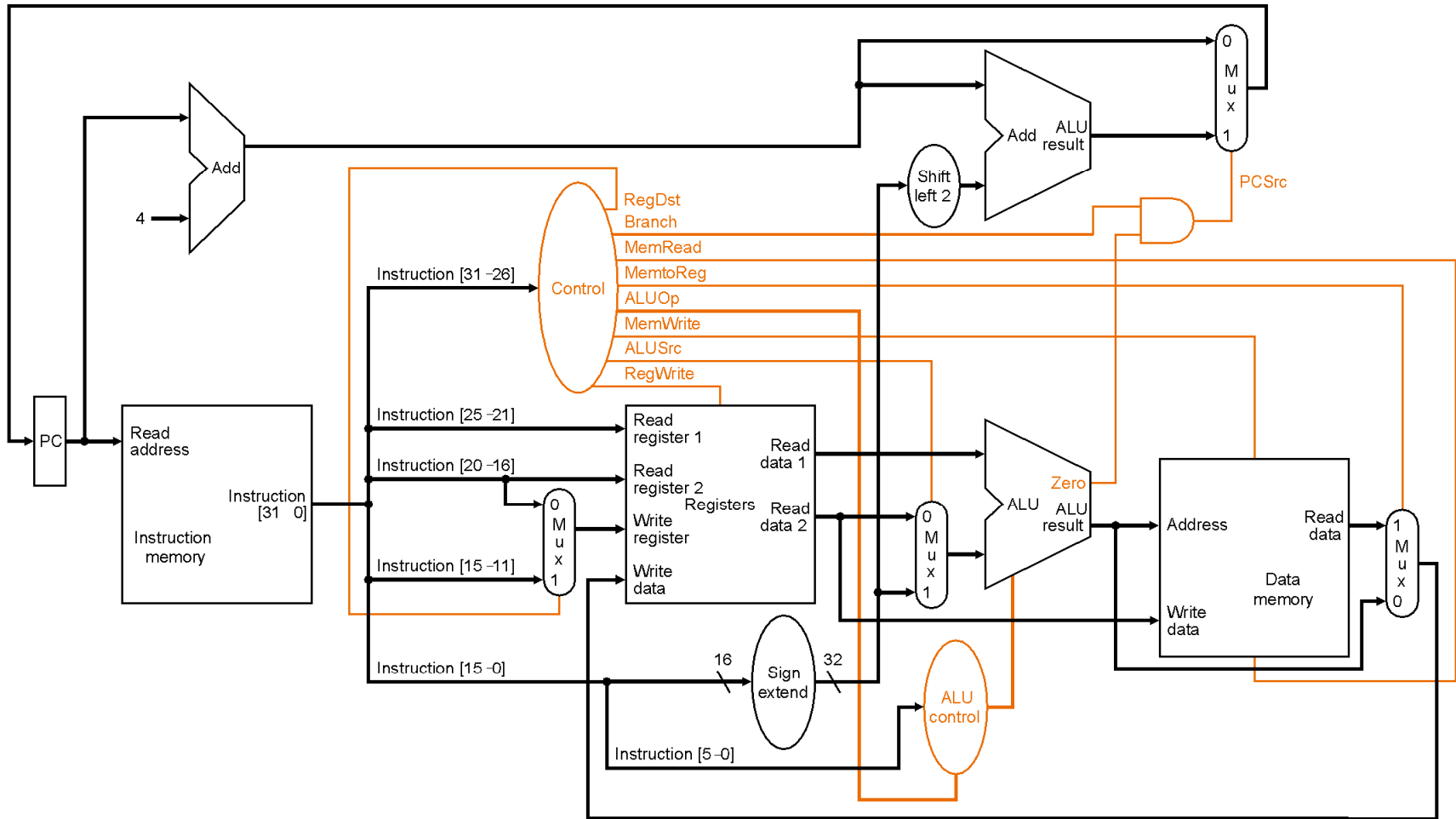
- Some Parts (text & figures) of this Lecture adopted from following:
 - D.A. Patterson and J.L. Hennessy, “[Computer Organization and Design: the Hardware/Software Interface](#)” (MIPS), 6th Edition, 2020.
 - J.L. Hennessy and D.A. Patterson, “[Computer Architecture: A Quantitative Approach](#)”, 6th Edition, Nov. 2017.
 - “Intro to Computer Architecture” handouts, by Prof. Hoe, CMU, Spring 2009.
 - “Computer Architecture & Engineering” handouts, by Prof. Kubiawicz, UC Berkeley, Spring 2004.
 - “Intro to Computer Architecture” handouts, by Prof. Hoe, UWisc, Spring 2021.
 - “Computer Arch I” handouts, by Prof. Garzarán, UIUC, Slide 2,



Quick Reminder from Previous Lecture



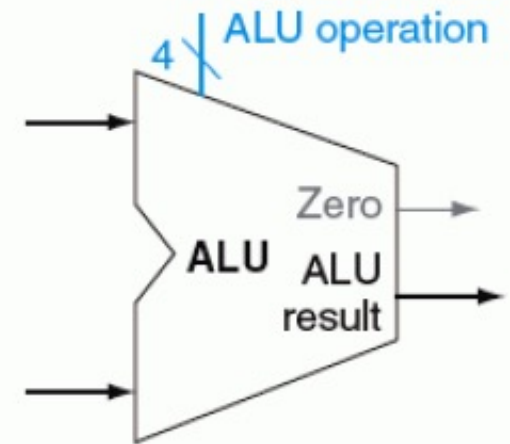
Adding Control Signals



ALU Control

- ALU Control Lines
 - Four control lines

ALU Control Lines	Function
0000	AND
0001	OR
0010	add
0110	sub
0111	set on less than
1100	NOR



ALU Control (cont.)

- ALUop
 - Used to distinguish R-type, lw/sw, beq

ALUop	Instruction	ALU Operation
00	Load/Store	Add
01	Beq	Sub
10	R-type	Determined by funct. Code (F5~F0)



ALU Control (cont.)

- ALU Control Inputs in terms of:
 - ALUop, funct field

Instruction opcode	ALUOp	Instruction operation	Funct field	Desired ALU action	ALU control input
LW	00	load word	XXXXXX	add	0010
SW	00	store word	XXXXXX	add	0010
Branch equal	01	branch equal	XXXXXX	subtract	0110
R-type	10	add	100000	add	0010
R-type	10	subtract	100010	subtract	0110
R-type	10	AND	100100	and	0000
R-type	10	OR	100101	or	0001
R-type	10	set on less than	101010	set on less than	0111



ALU Control (cont.)

- Truth Table of ALU Control Inputs
 - 8 inputs
 - 4 outputs

ALUOp		Funct field						Operation
ALUOp1	ALUOp0	F5	F4	F3	F2	F1	F0	
0	0	X	X	X	X	X	X	0010
X	1	X	X	X	X	X	X	0110
1	X	X	X	0	0	0	0	0010
1	X	X	X	0	0	1	0	0110
1	X	X	X	0	1	0	0	0000
1	X	X	X	0	1	0	1	0001
1	X	X	X	1	0	1	0	0111

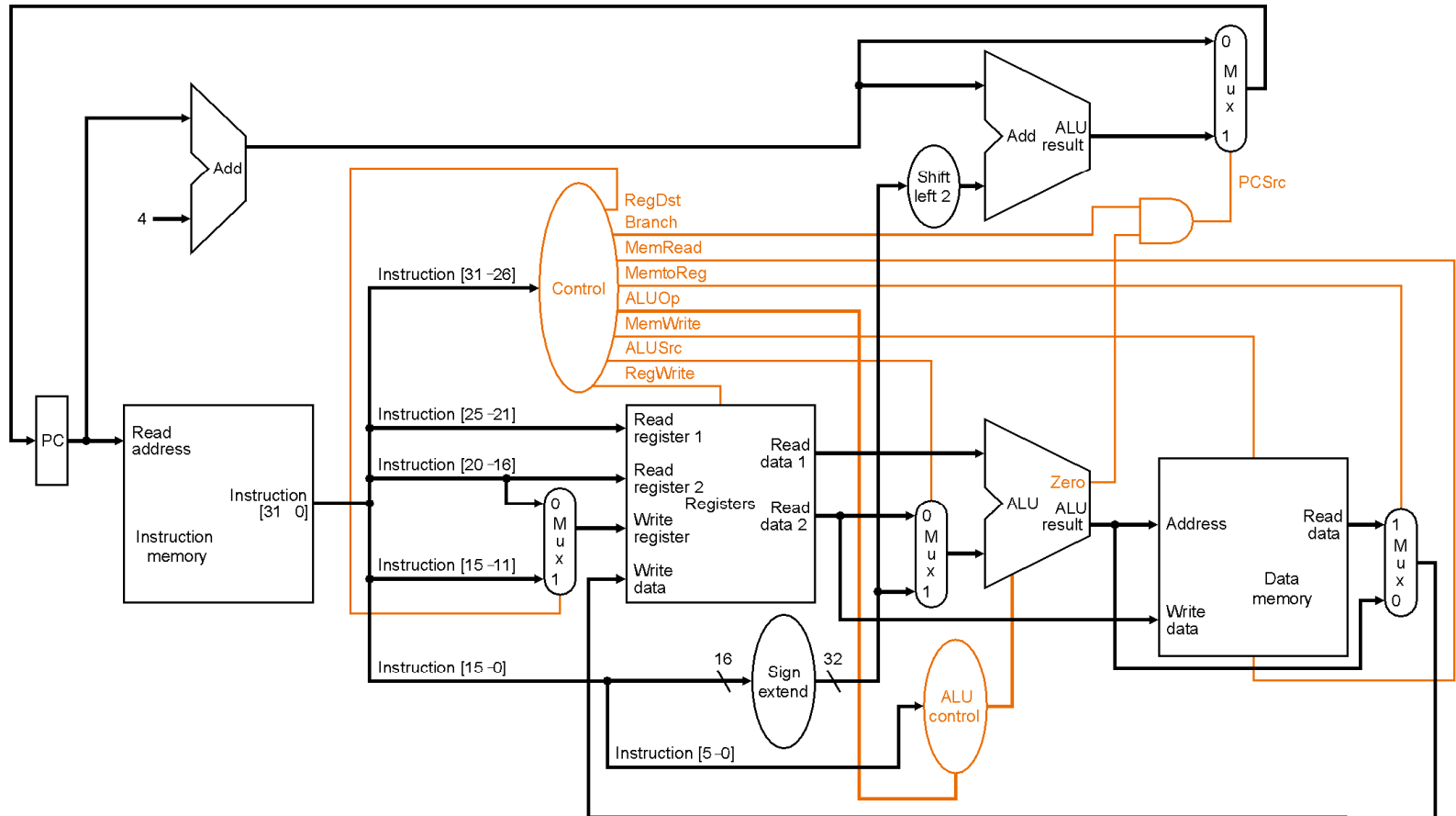


Designing Main Control Unit

- Steps
 - Identify fields of instructions
 - Identify control lines needed for datapath
 - Figure out how to generate control lines from fields of instructions



Beq Control



Instruction	RegDst	ALUSrc	Memto-Reg	Reg Write	Mem Read	Mem Write	Branch	ALUOp1	ALUp0
R-format	1	0	0	1	0	0	0	1	0
lw	0	1	1	1	1	0	0	0	0
sw	X	1	X	0	0	1	0	0	0
beq	X	0	X	0	0	0	1	0	1

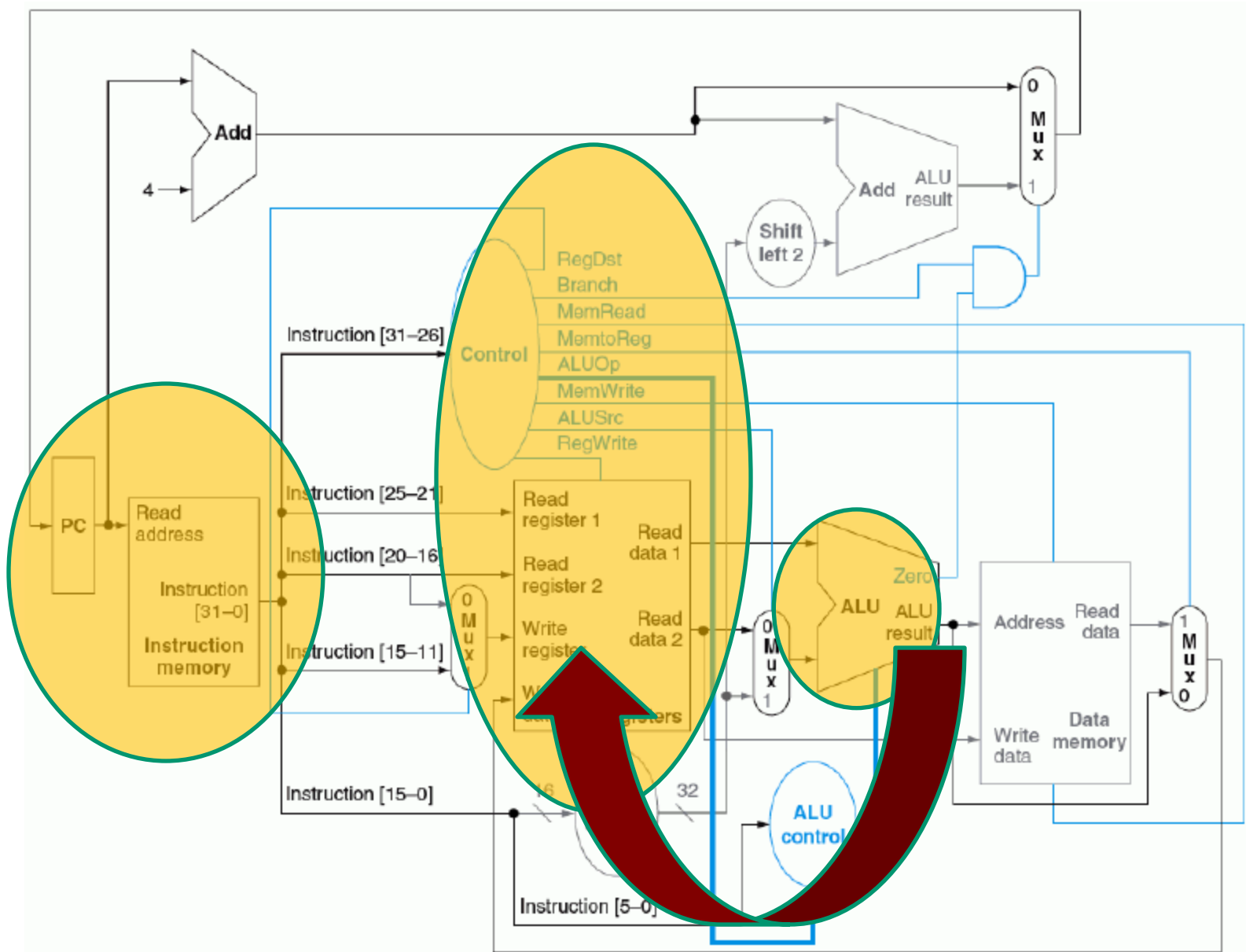


Operation of Datapath: R-Type

- Step 1:
 - Instruction fetched
 - PC incremented
- Step 2:
 - Two regs read from GPR
 - Main CU computes setting of control lines
- Step 3:
 - ALU control determined by funct. Code
 - Then, ALU operates on data read from GPR
- Step 4:
 - Results from ALU written into RF using bits 15:11



Operation of Datapath: R-Type (cont.)

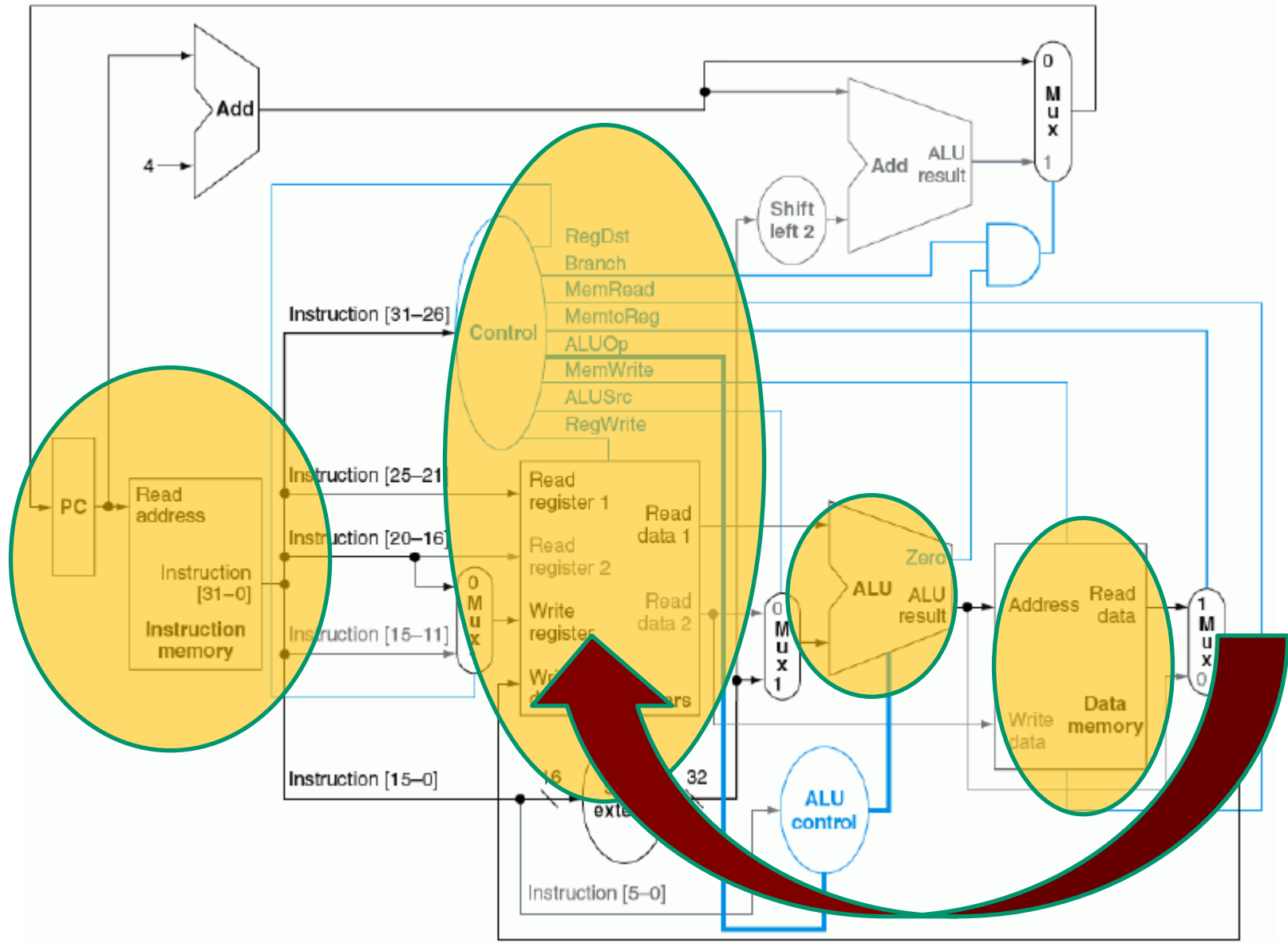


Operation of Datapath: Load

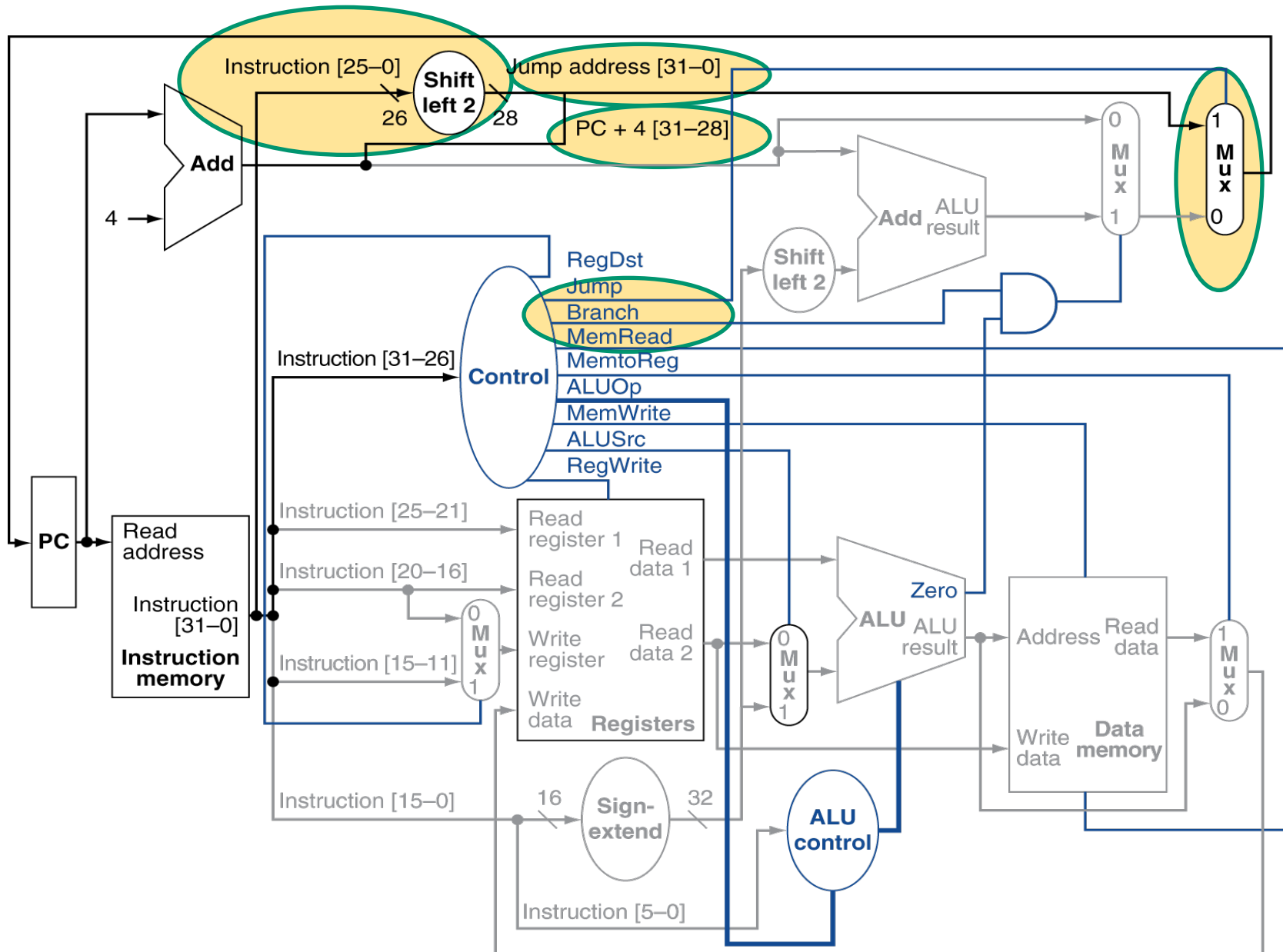
- Step 1:
 - Instruction fetched
 - PC incremented
- Step 2:
 - A reg read from GPR (e.g. \$t1)
 - CU computes setting of control lines
- Step 3:
 - ALU computes target memory address
 - Based on \$t1 and sign-extended value in bits 15:0
- Step 4:
 - 32-bit data read from Memory based on calculated addr.
- Step 5:
 - Data written into GPR (destination reg: bits 20:16)



Operation of Datapath: Load (cont.)



Jump Datapath



Our Lectur Today



Topics Covered Today

- **MIPS Multicycle Design**
 - **Shortcomings of single-cycle datapath**
 - **Basics of multicycle datapath**
 - **Major modules in multicycle**
 - **Control unit design for multicycle datapath**



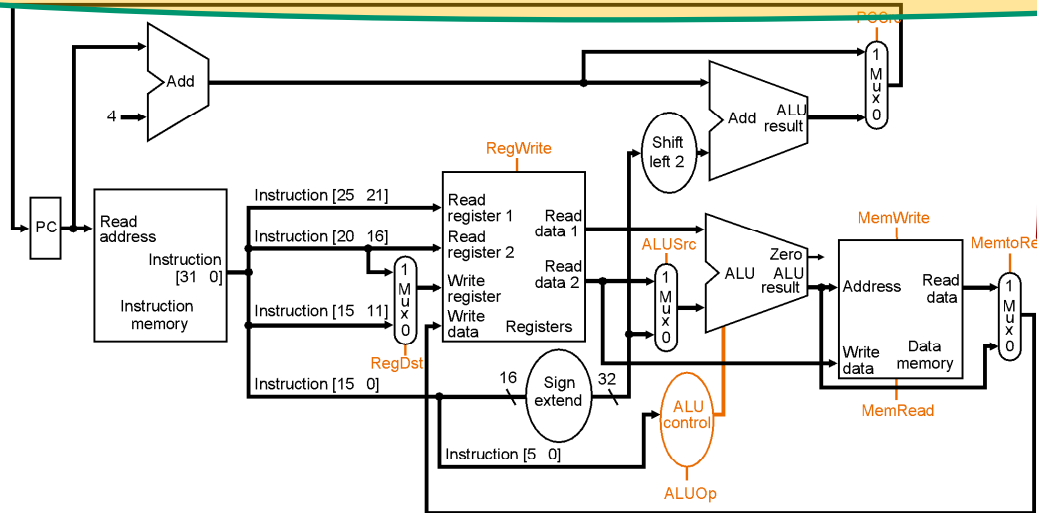
Performance of Single-Cycle uArch

- Simple but Inefficient Performance
- Why?
 - Clock cycle determined by longest possible path
 - Clock cycles of all instructions same length
 - $CPI = 1$
- Longest Possible Path?
 - Load datapath



Single-Cycle CPU Clock Cycle Time

	I-cache	Decode, R-Read	ALU	PC update	D-cache	R-Write	Total
R-type	1	1	.9	-	-	.8	3.7
Load	1	1	.9	-	1	.8	4.7
Store	1	1	.9	-	1	-	3.9
beq	1	1	.9	.1	-	-	3.0



Clock cycle time
= 4.7 + setup + hold

Load on critical path

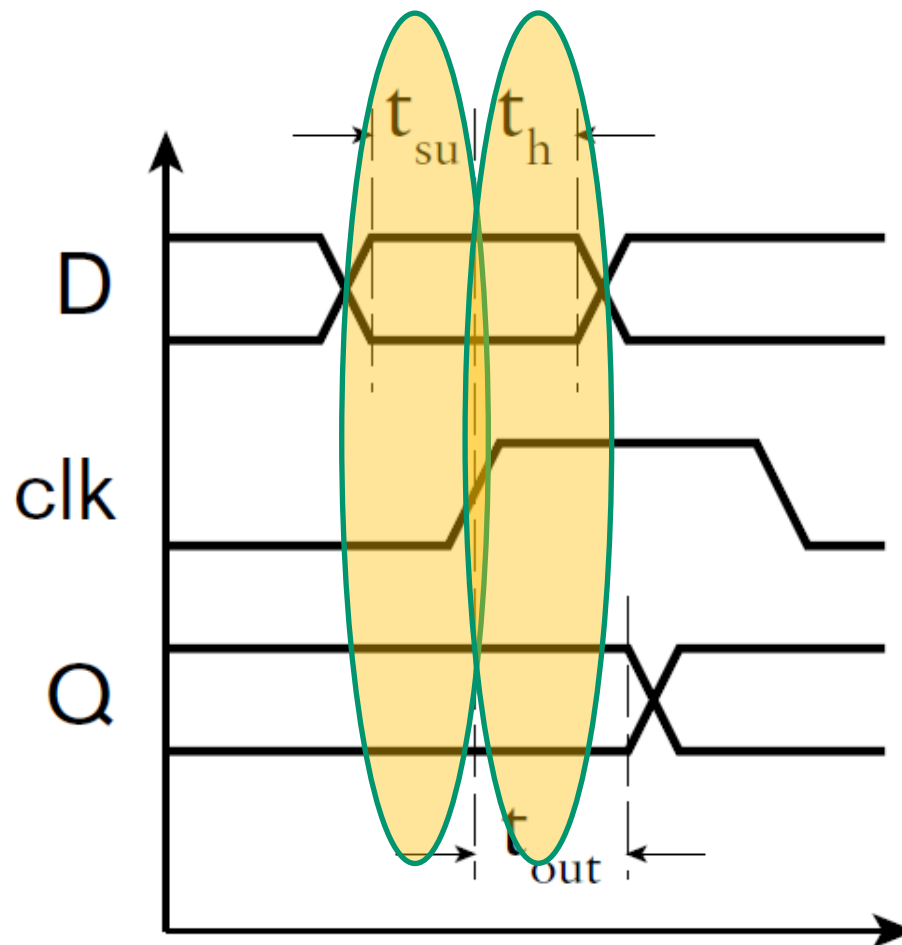
Setup time?

Hold time?

Critical path?

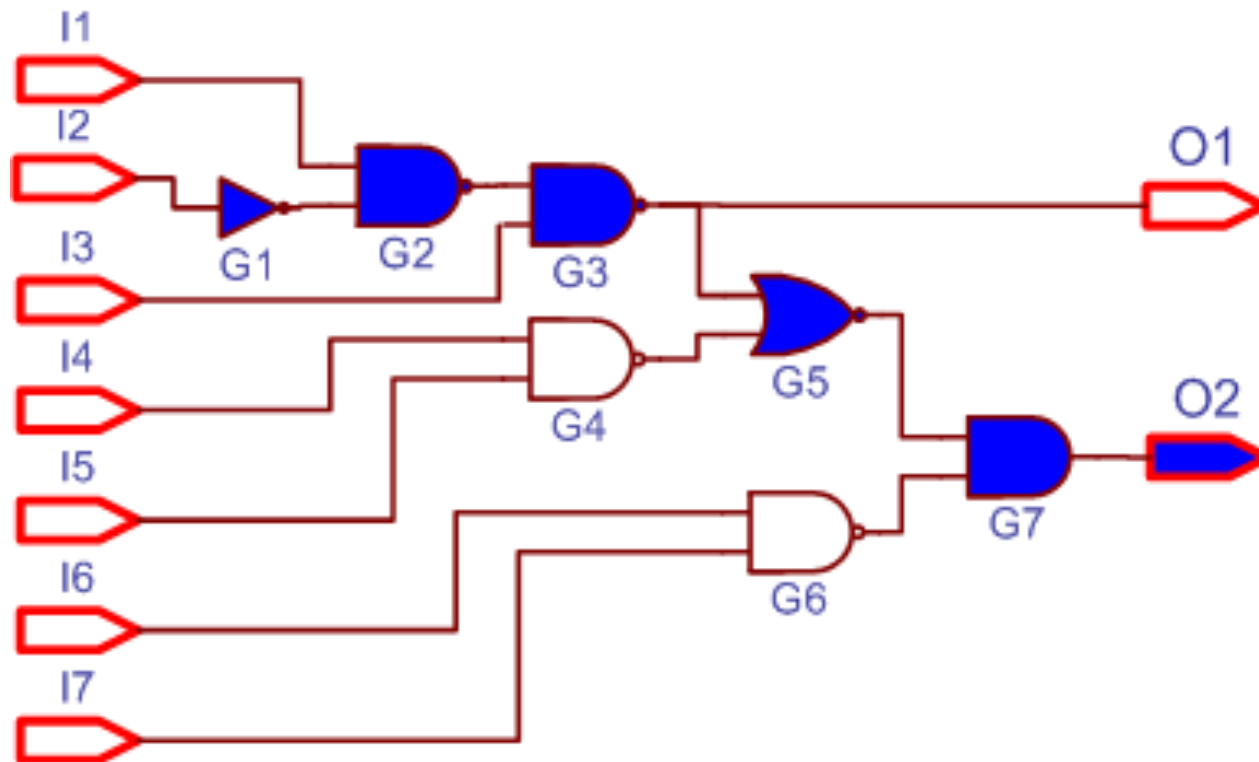


Setup Time & Hold Time



Critical Path Delay

- Definition:
 - A path through combinational circuit that takes as long or longer than any other



Multicycle Implementation

Goal: Balance amount of work done each cycle

	I cache	Decode, R-Read	ALU	PC update	D cache	R- Write	Total
R-type	1	1	.9	-	-	.8	3.7
Load	1	1	.9	-	1	.8	4.7
Store	1	1	.9	-	1	-	3.9
beq	1	1	.9	.1	-	-	3.0

- Load needs 5 cycles
- Store and R-type need 4
- beq needs 3



Will Multi-Cycle Design be Faster?

	I cache	Decode, R-read	ALU	PC update	D cache	R-write	Total
R-type	1	1	.9	-	-	.8	3.7
Load	1	1	.9	-	1	.8	4.7
Store	1	1	.9	-	1	-	3.9
beq	1	1	.9	.1	-	-	3.0

Let's assume setup + hold time = 100ps = 0.1 ns

Single Cycle Design:

Clock cycle time = 4.7 + 0.1 = 4.8 ns

time/inst = 1 cycle/inst * 4.8 ns/cycle = 4.8 ns/inst

Multicycle Design:

Clock cycle time = 1.0 + 0.1 = 1.1

time/inst = CPI * 1.1 ns/cycle



Will Multi-Cycle Design be Faster? (cont.)

	Cycles needed	Instruction frequency
R-type	4	60%
Load	5	20%
Store	4	10%
beq	3	10%

What is **CPI** assuming this instruction mix?

$$\text{CPI} = 4 * 0.6 + 5 * 0.2 + 4 * 0.1 + 3 * 0.1 = 4.1$$

Let's assume setup + hold time = 0.1 ns

Single Cycle Design:

$$\text{Clock cycle time} = 4.7 + 0.1 = 4.8 \text{ ns}$$

$$\text{time/inst} = 1 \text{ cycle/inst} * 4.8 \text{ ns/cycle} = 4.8 \text{ ns/inst}$$

Multicycle Design:

$$\text{Clock cycle time} = 1.0 + 0.1 = 1.1$$

$$\text{time/inst} = \text{CPI} * 1.1 \text{ ns/cycle} = 4.1 * 1.1 = 4.5$$

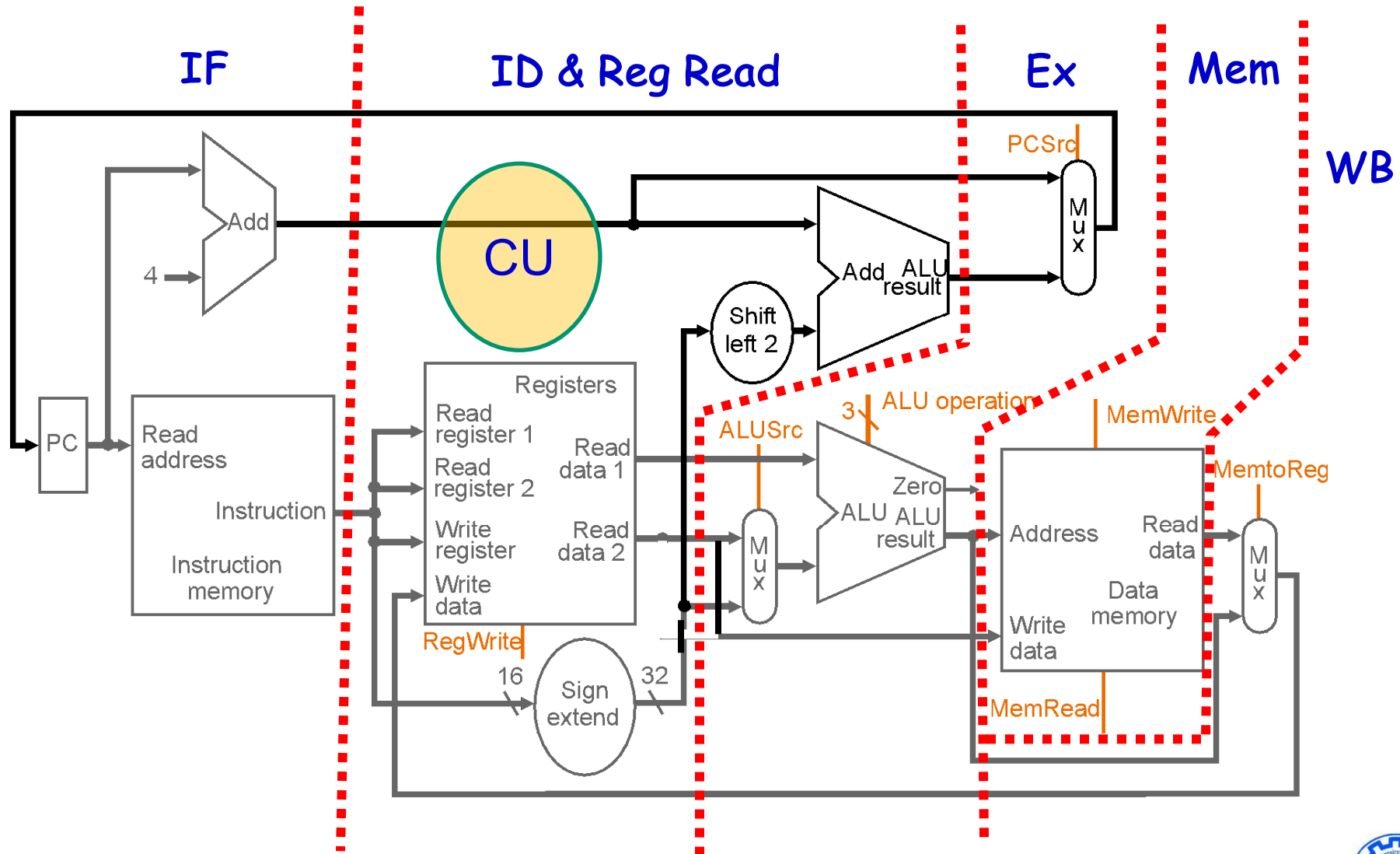


Will Multi-Cycle Design be Faster? (cont.)

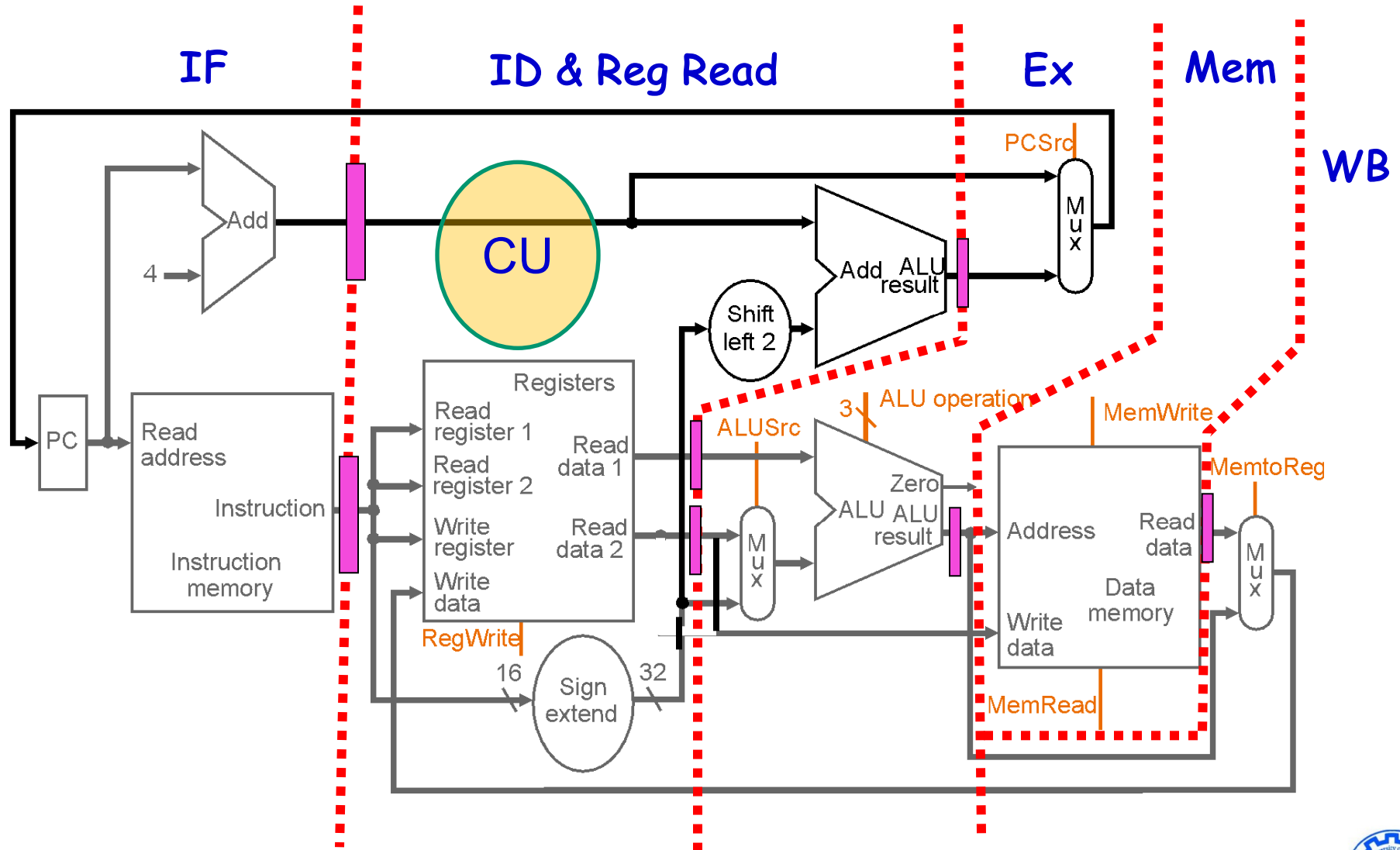
- Much Smaller Clock Cycle Time
 - Compared to single-cycle datapath
- **Possibly** Faster Runtime
 - Compared to single-cycle datapath
- Depends on:
 - How **partitioning** is performed
 - **Frequency of instructions** in benchmark programs



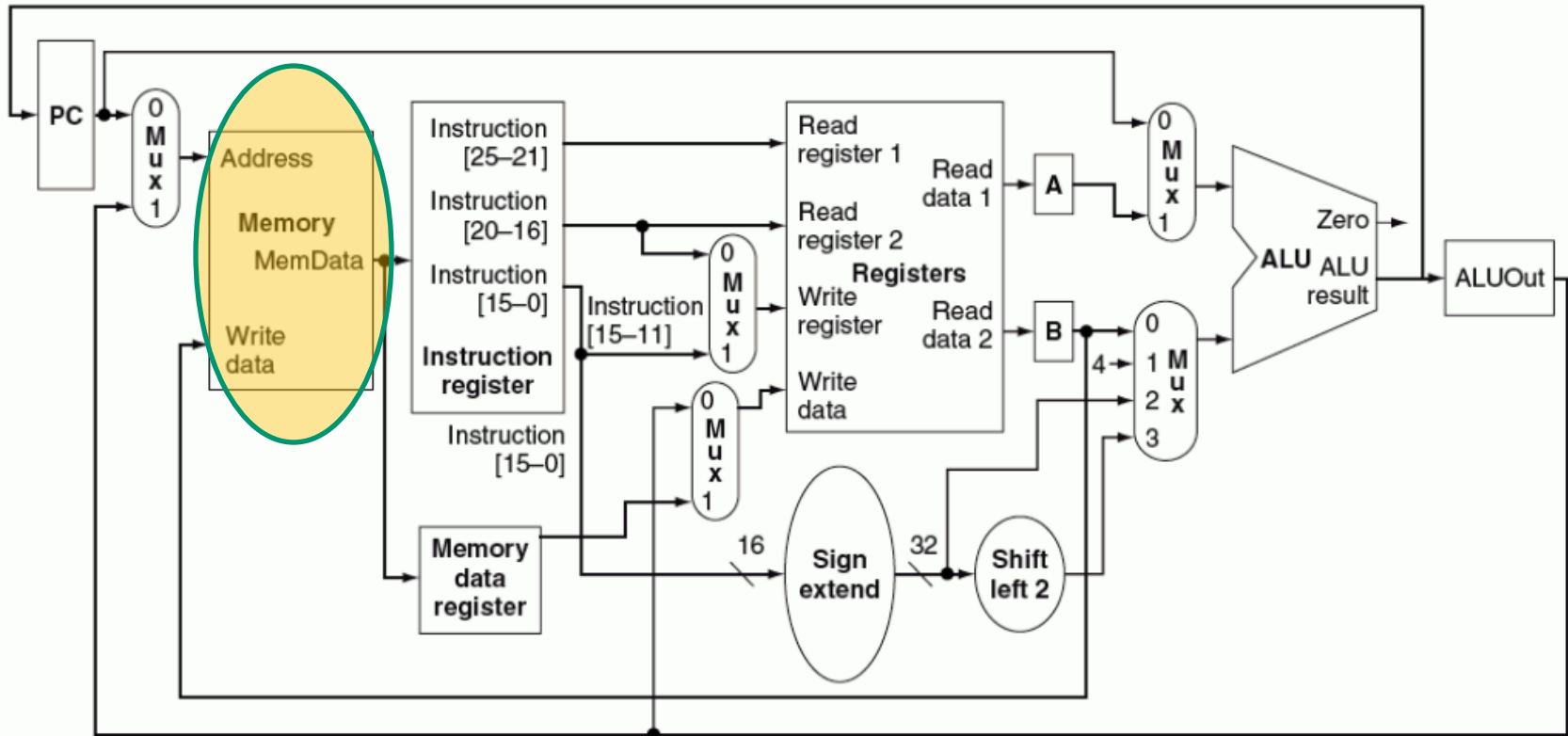
Partitioning Single-Cycle Design



Where to Add Registers?



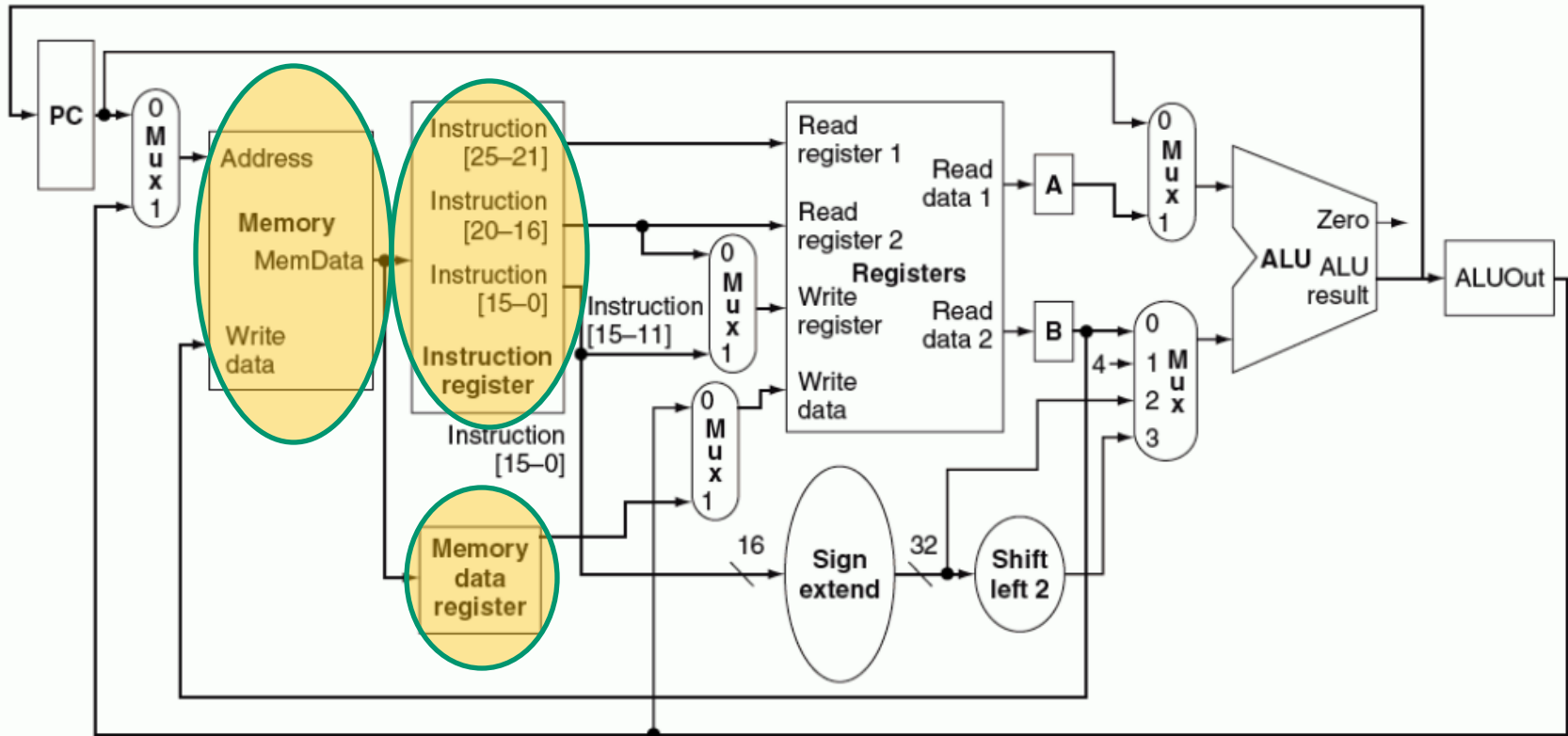
Multicycle Datapath



- Unified Memory
 - Used as both I-cache & D-cache
- Combines address busses of single-cycle datapath
 - Uses a MUX to select PC or ALU output



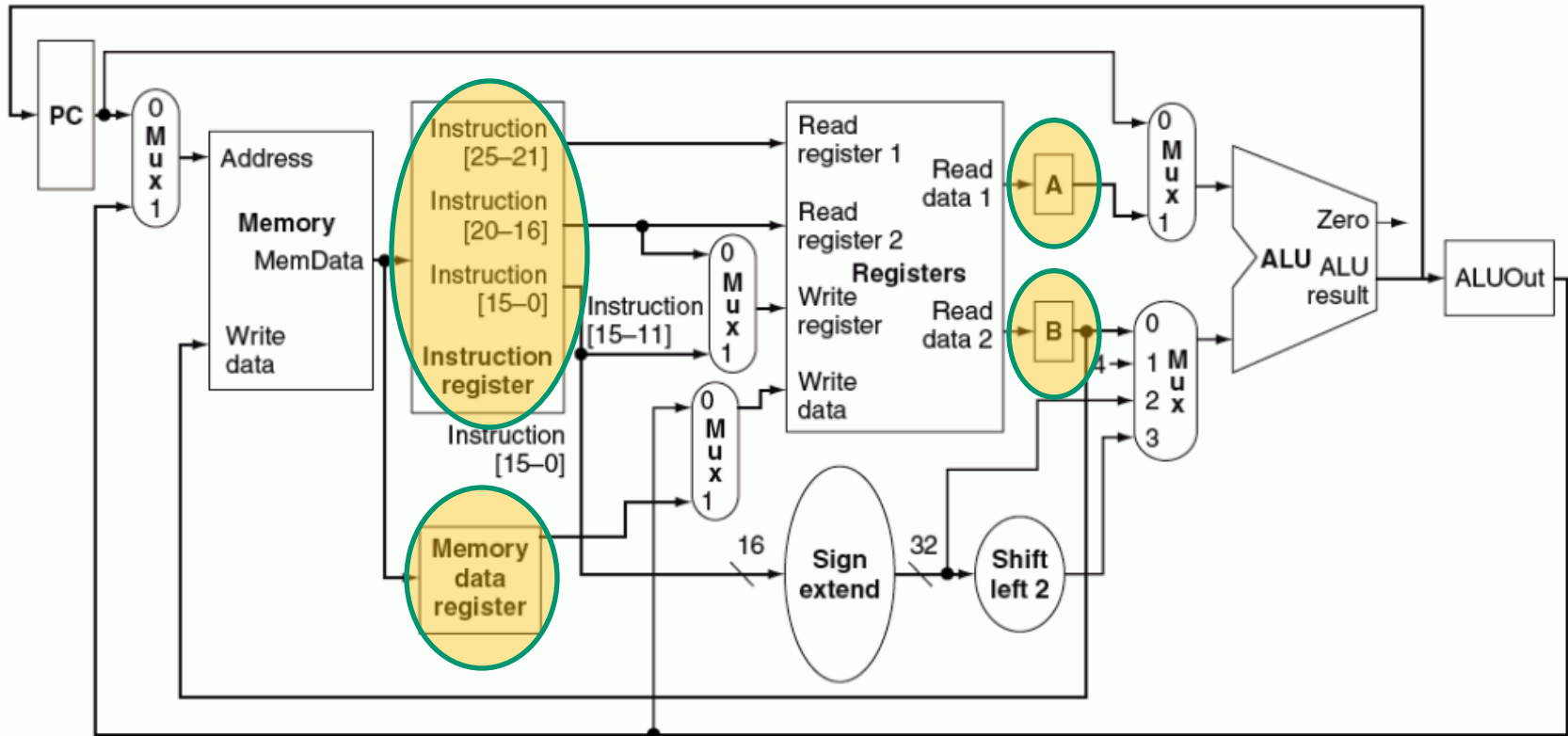
Multicycle Datapath (cont.)



- Instruction Register
 - $IR \leftarrow Mem[PC]$
- Memory Data Register
 - $MDR \leftarrow Mem[ALUOut]$



Multicycle Datapath (cont.)

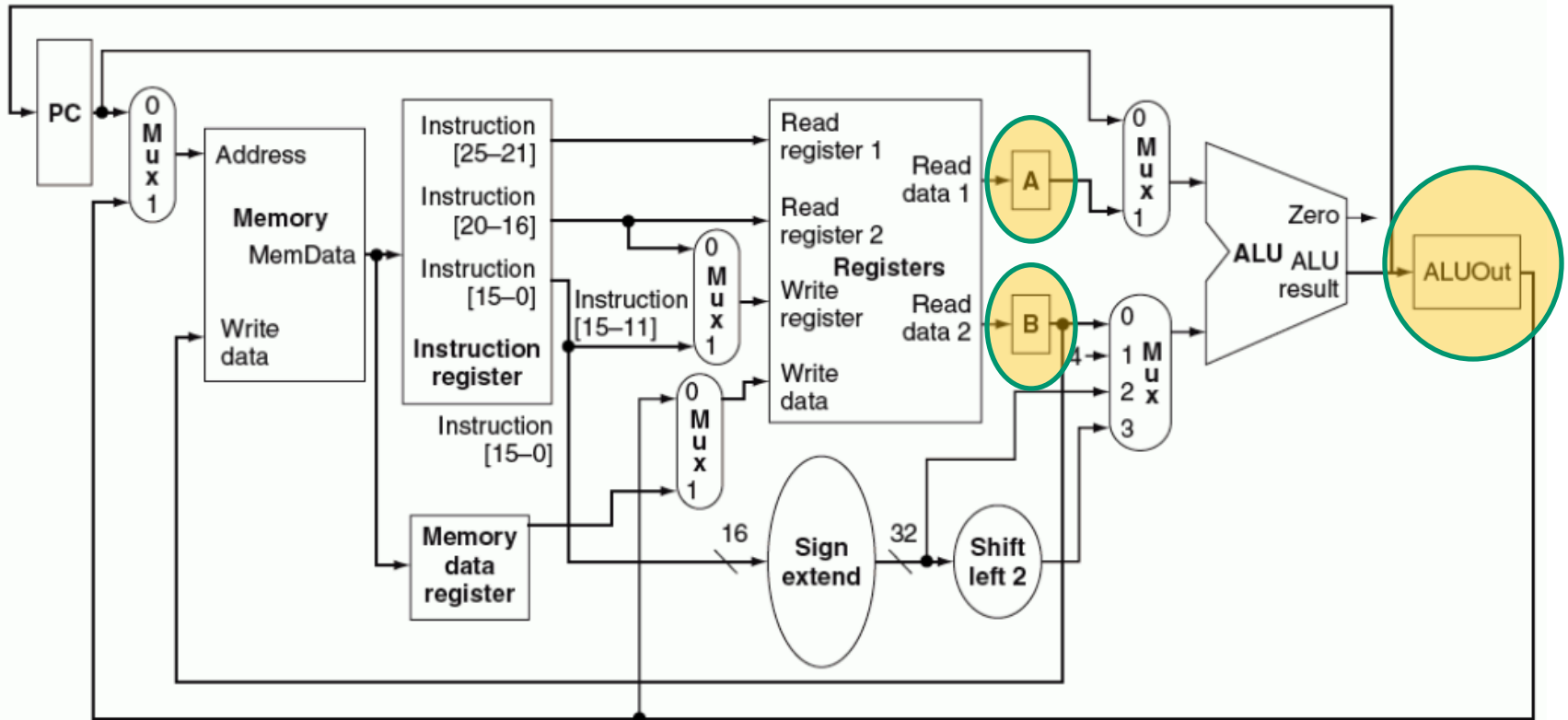


•Reg A & B

- $A \leftarrow \text{GPR}[\text{IR}[25:21]]$
- $B \leftarrow \text{GPR}[\text{IR}[20:16]]$



Multicycle Datapath (cont.)



- **ALUOut** \leftarrow ALU result
- **ALUOut** is then either
 - Written to GPR
 - Or used as an address for Memory

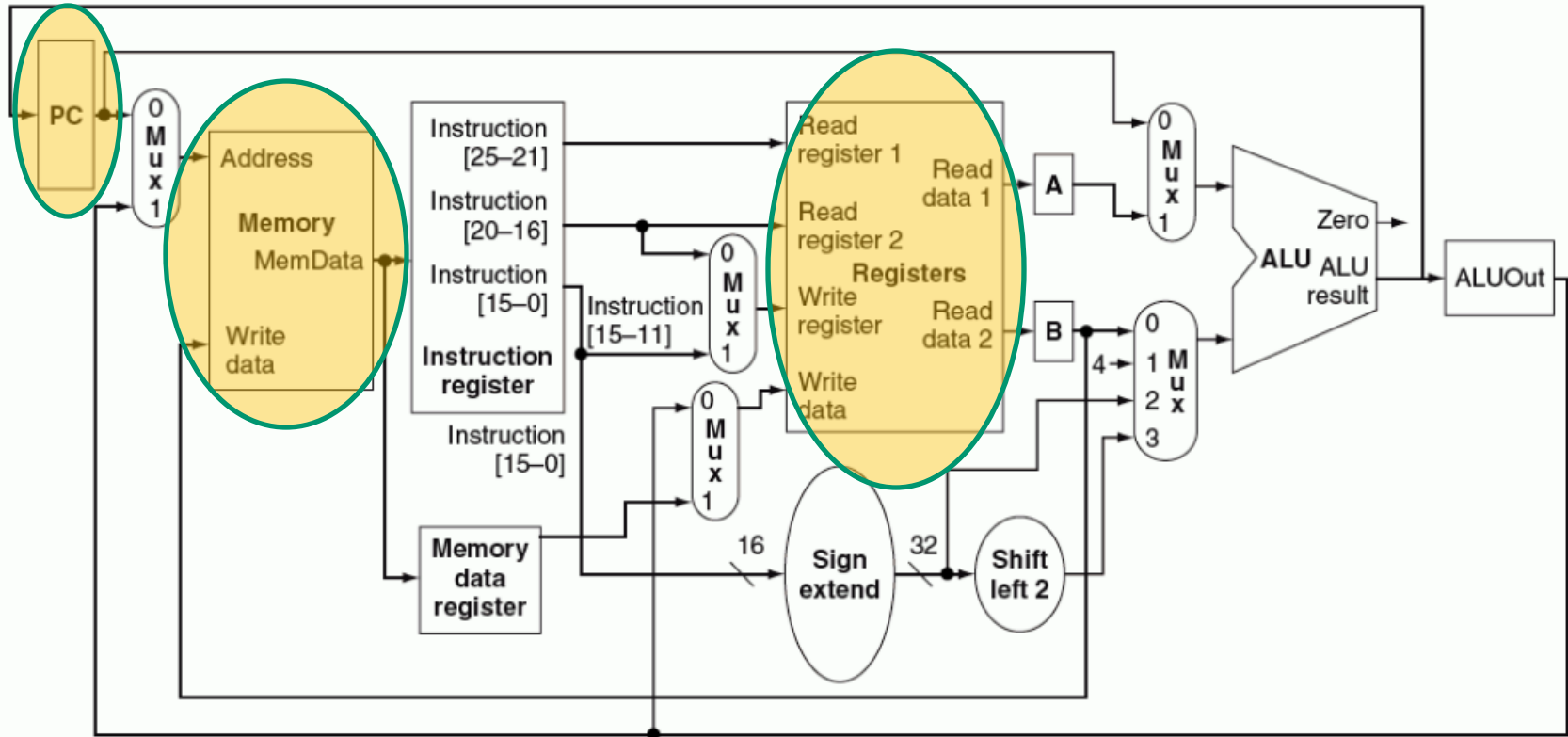


Multi-Cycle vs. Single-Cycle Datapath

- Hardware Elements
 - Single memory unit
 - Used for **both** in **instruction** & **data**
 - **Instruction & data** must be accessed in **different clock** cycles
 - Single ALU unit
 - Rather than Using **ALU** and **two adders**
 - One or more **registers** added after every major functional unit



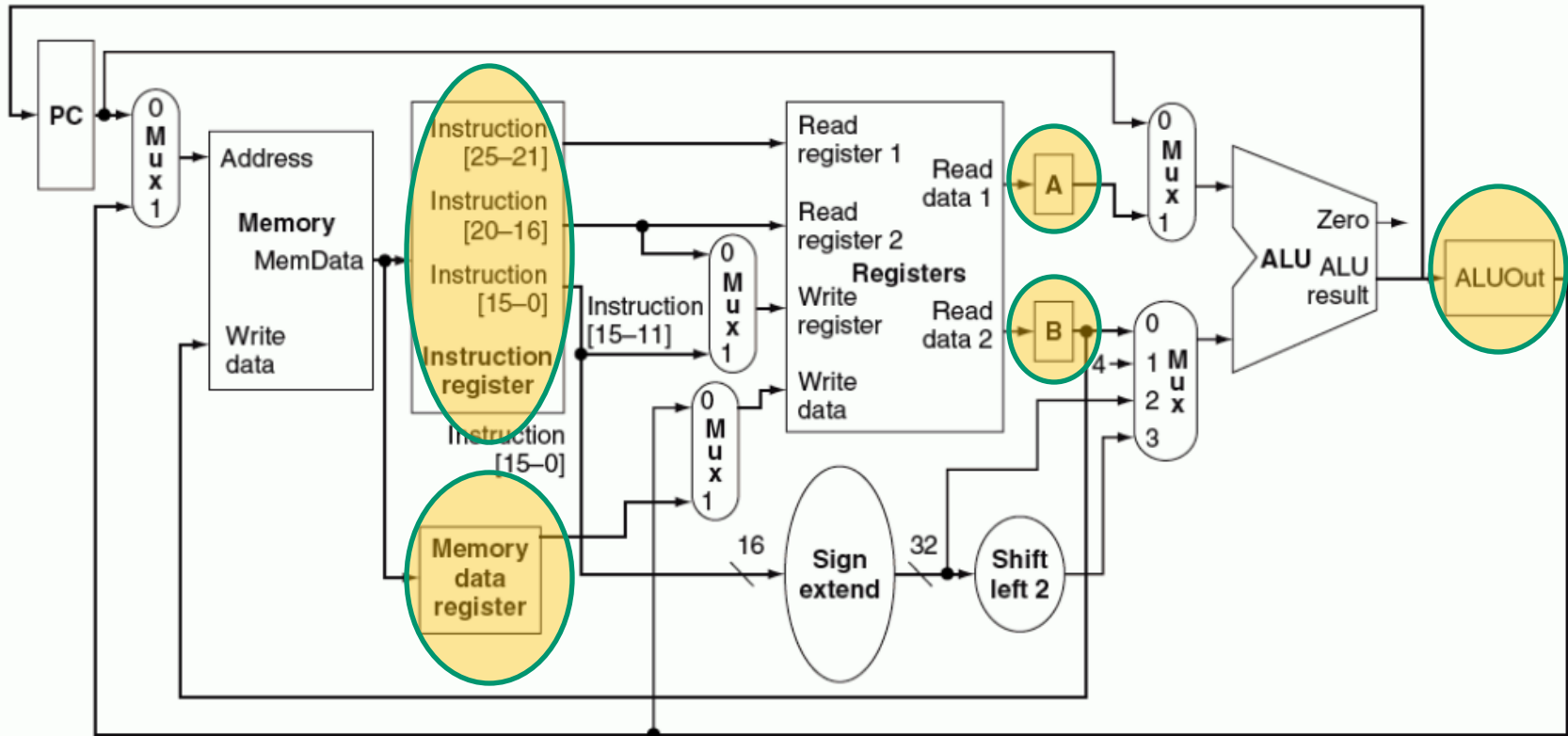
Multicycle Datapath (cont.)



- User-Visible State Elements
 - PC
 - Memory
 - Register file



Multicycle Datapath (cont.)

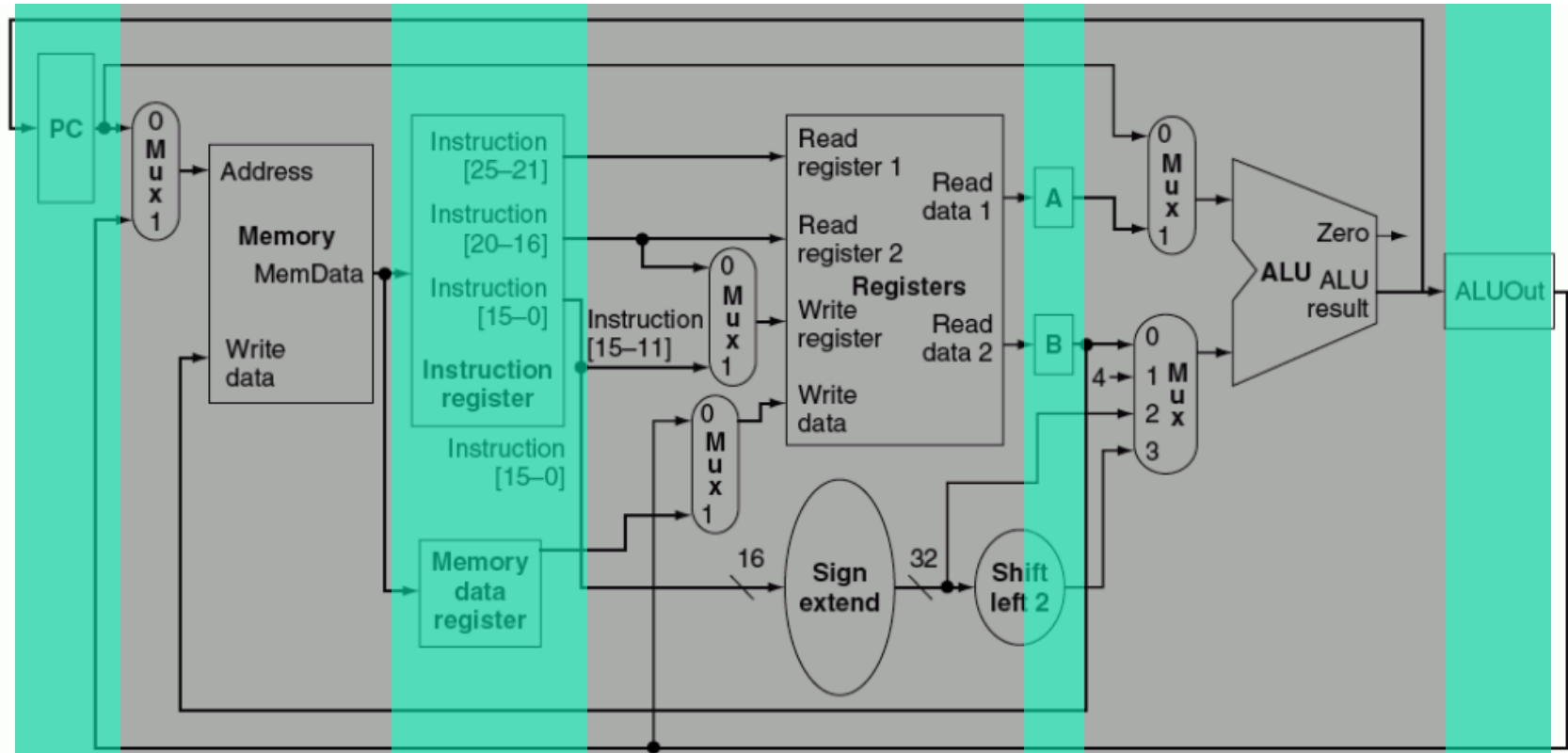


• Non-User-Visible State Elements

- Instruction Register (IR)
- Memory Data Register (MDR)
- Reg A & Reg B
- ALUOut



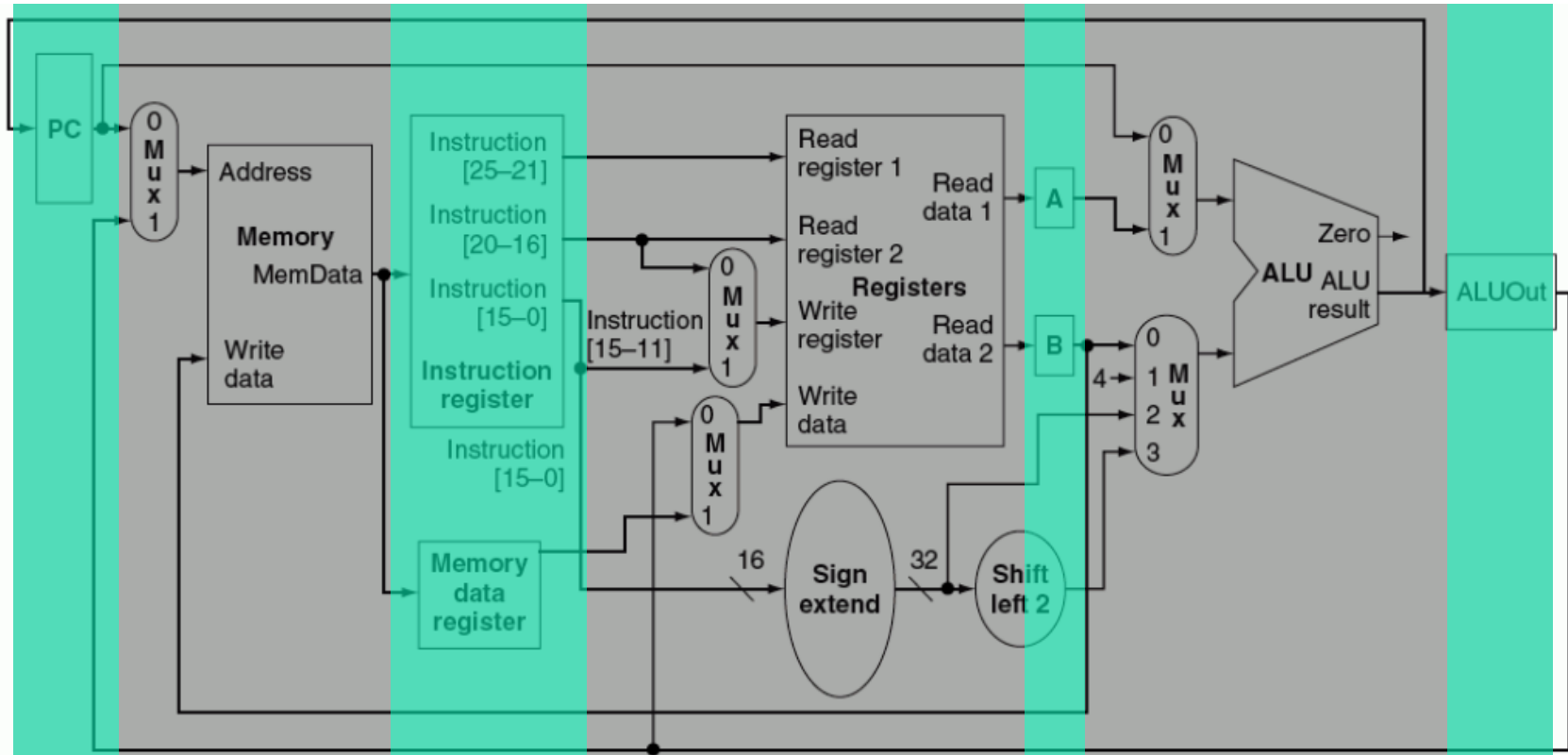
Multicycle Datapath (cont.)



- Note: registers hold data only between a pair of adjacent clock cycles
- Question: Do we need to have write or read control signals for registers, memory, & GPR?



Multicycle Datapath (cont.)



- No WR/RD control signal for non-visible regs (MDR, A, B, ...)
 - WR=1, RD=1
- But IR needs to hold instr. until end of exec. of that instr.
- How about PC, memory, and GPR?
- How about read signal?

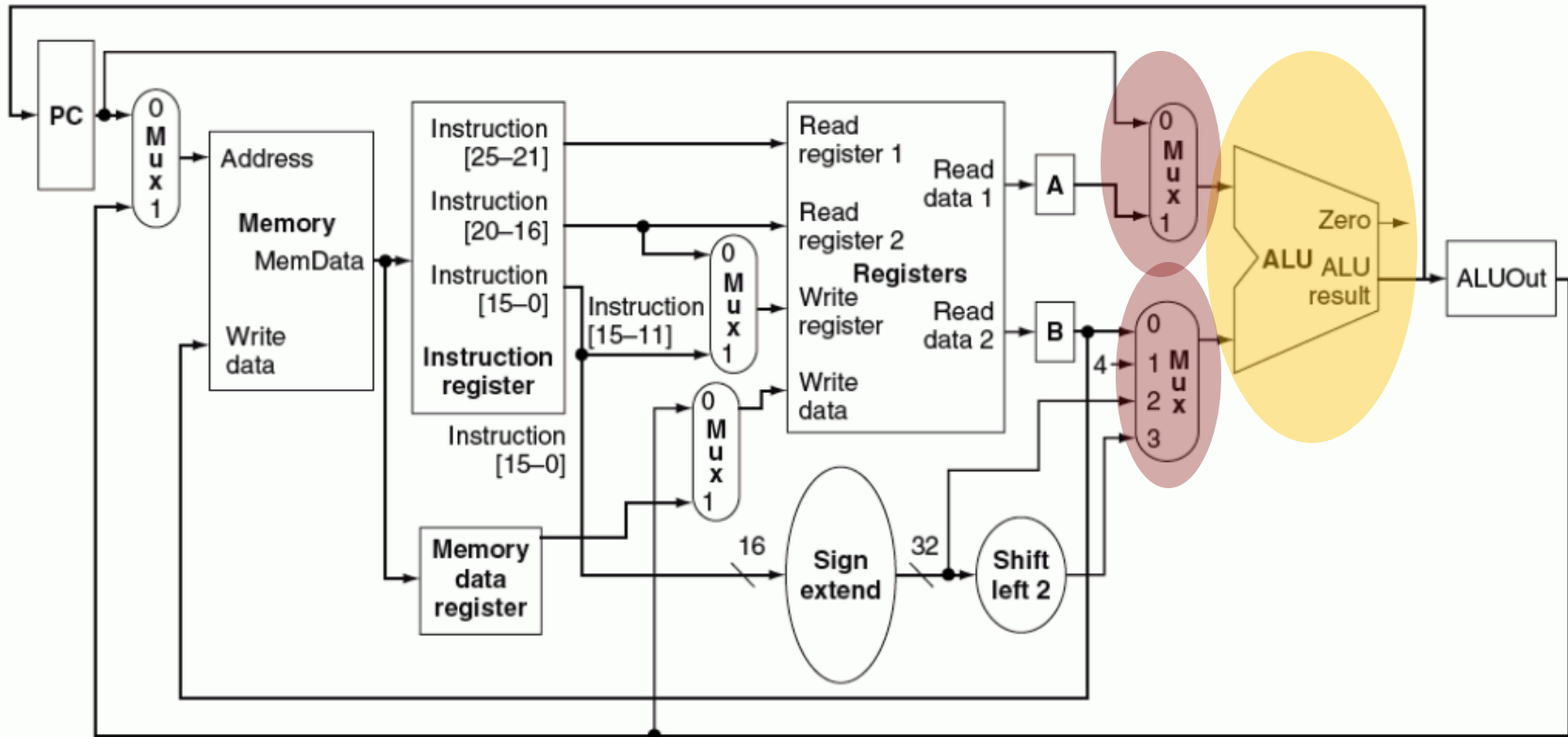


Read & Write Control Signals

- Memory
 - Write signal required
 - Read signal required
 - If simultaneous read and write not possible
 - Twice decode circuitry for simultaneous RD/WR
- PC
 - If write signal = 1 →
 - PC incremented by 4 in IF & ID cycles
 - PC may capture wrong address in other cycles



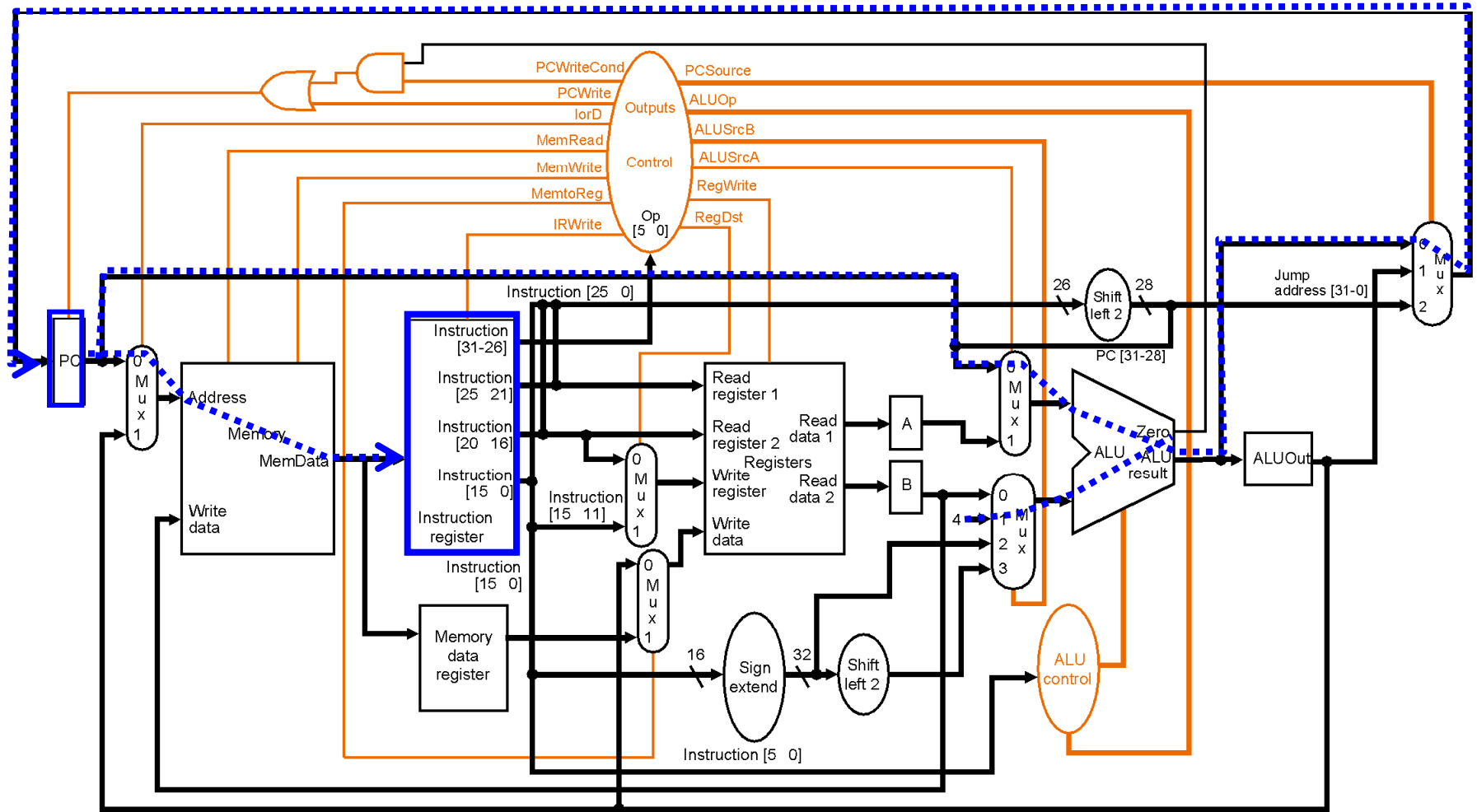
Multicycle Datapath (cont.)



- Three ALUs replaced by a single ALU
- ALU must accommodate all inputs
 - Which go to three ALUs in single-cycle datapath
 - $A \text{ op } B$ / $PC+4$ / $PC+addr.$ / $A+immediate$



Cycle 1: Instruction Fetch



Datapath:

$IR \leftarrow Mem[PC]$

$PC \leftarrow PC + 4$



The diagram illustrates the internal components and data flow of a processor. Key elements include:

- PC (Program Counter):** Receives the next instruction address from the ALU output or a jump address. It feeds into a 1-to-2 multiplexer for the Memory Address.
- Memory:** Receives the Memory Address and provides MemData to the Instruction Register and Memory Data Register.
- Instruction Register:** Holds the current instruction, providing fields for Op, Register Indices (Rt, Rs, Rd), and Immediate values.
- Registers:** A set of 32 registers. Read data 1 and 2 are selected via multiplexers from registers specified in the instruction. Write data is selected via a multiplexer to be written to the register specified by Rt.
- ALU (Arithmetic Logic Unit):** Performs operations on Read data 1 and 2 based on the ALUOp field. It includes a Zero flag and an ALU control unit.
- Control Logic:** A central control unit that generates signals for PCWriteCond, PCWrite, IorD, MemRead, MemWrite, MemtoReg, IRWrite, ALUOp, ALUSrcB, ALUSrcA, RegWrite, and RegDst based on the instruction's Op field.
- Jump Logic:** A 4-to-1 multiplexer selects between the ALU result, the sign-extended and shifted immediate, or the PCWriteCond signal to determine if the PC should be updated with the jump address.

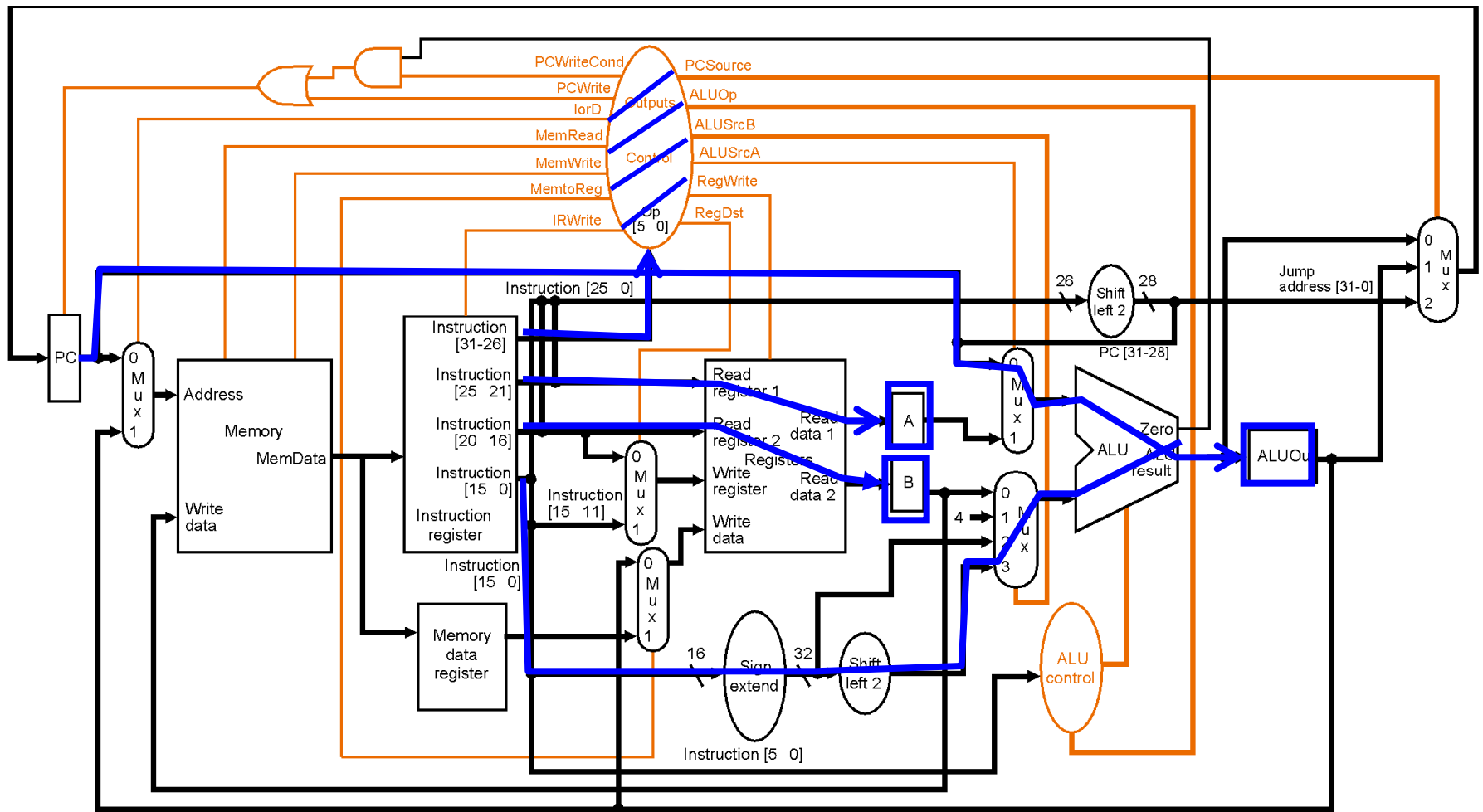
lorD=0, MemRead=1, MemWrite=0, IRwrite=1, ALUsrcA=0
ALUsrcB=01, PCWrite=1, ALUop=00, PCsource=00

Control for IF Cycle

MemRead
ALUsrcA = 0
IorD = 0
IRwrite
ALUsrcB = 01
ALUop = 00
Pcwrite
PCsource = 00



Cycle 2: ID & RF Cycle



$A \leftarrow \text{GPR}[\text{IR}[25-21]]$

$B \leftarrow \text{GPR}[\text{IR}[20-16]]$

$\text{ALUOut} \leftarrow \text{PC} + (\text{sign-extend}(\text{IR}[15-0]) \ll 2)$



Cycle 2: ID & RF Cycle

$A \leq \text{GPR}[\text{IR}[25-21]]$

$B \leq \text{GPR}[\text{IR}[20-16]]$

$\text{ALUout} \leq \text{PC} + (\text{SignEx}(\text{IR}[15-0]) \ll 2)$

- Question 1:
 - We fetch A & B from GPR even though we don't know if they will be used.
 - Why?



Cycle 2: ID & RF Cycle

$A \leq \text{GPR}[\text{IR}[25-21]]$

$B \leq \text{GPR}[\text{IR}[20-16]]$

$\text{ALUout} \leq \text{PC} + (\text{SignEx}(\text{IR}[15-0]) \ll 2)$

- Question 2:
 - We compute target address even though we don't know if it will be used.
 - Operation may not be branch
 - Even if it is, branch may not be taken
 - Why?



Cycle 2: ID & RF Cycle

$A \leq \text{GPR}[\text{IR}[25-21]]$

$B \leq \text{GPR}[\text{IR}[20-16]]$

$\text{ALUout} \leq \text{PC} + (\text{SignEx}(\text{IR}[15-0]) \ll 2)$

- Question 3:
 - Control signals computed in Cycle 2. However, `lorD` signal used in Cycle 1. How this is possible?



Cycle 2: ID & RF Cycle

$A \leq \text{GPR}[\text{IR}[25-21]]$

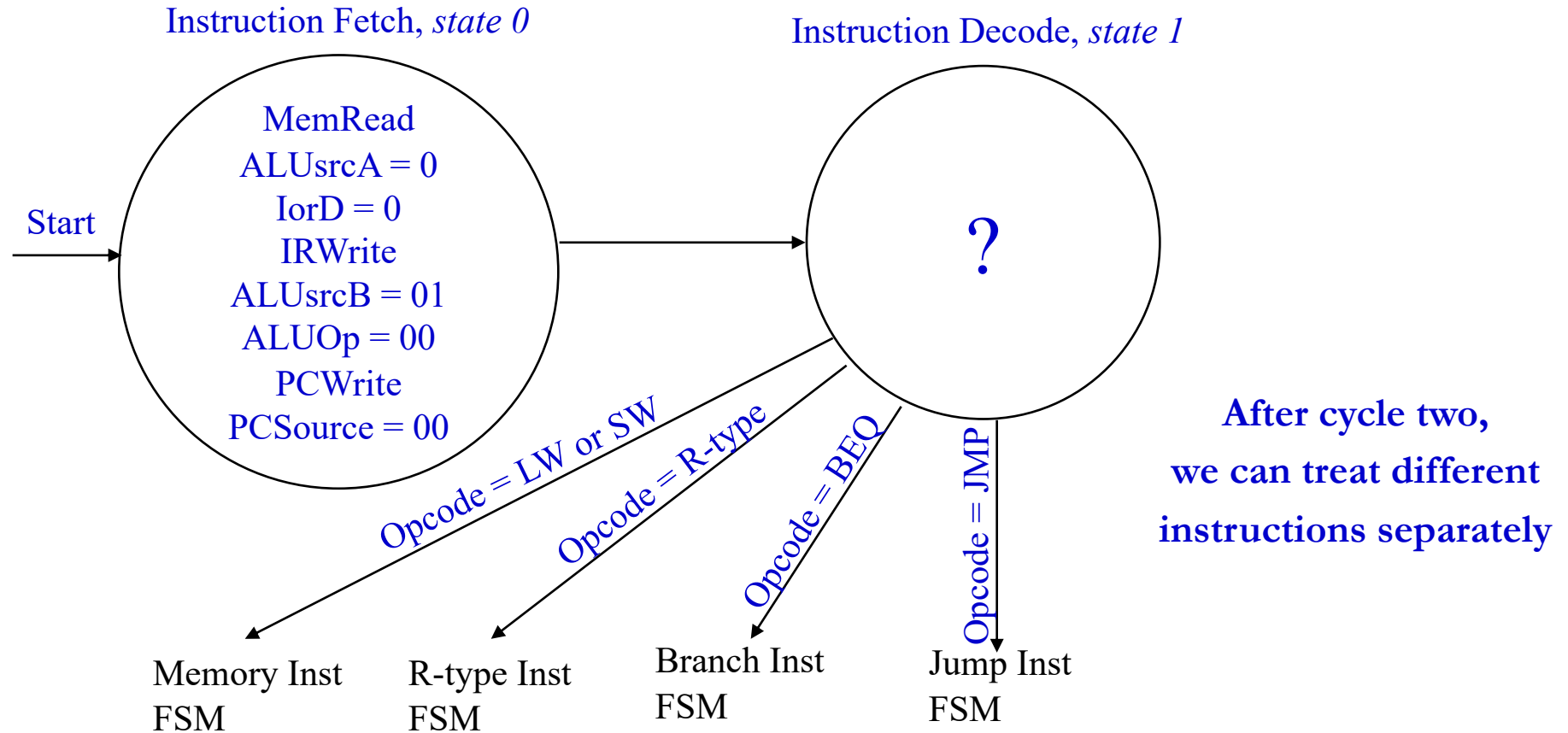
$B \leq \text{GPR}[\text{IR}[20-16]]$

$\text{ALUout} \leq \text{PC} + (\text{SignEx}(\text{IR}[15-0]) \ll 2)$

- Answer:
 - Everything up to this point must be instruction-independent
 - Because we haven't decoded instruction
 - GPR and ALU are available in cycle 2 so we can use them up to fetch A & B and to calculate target branch address



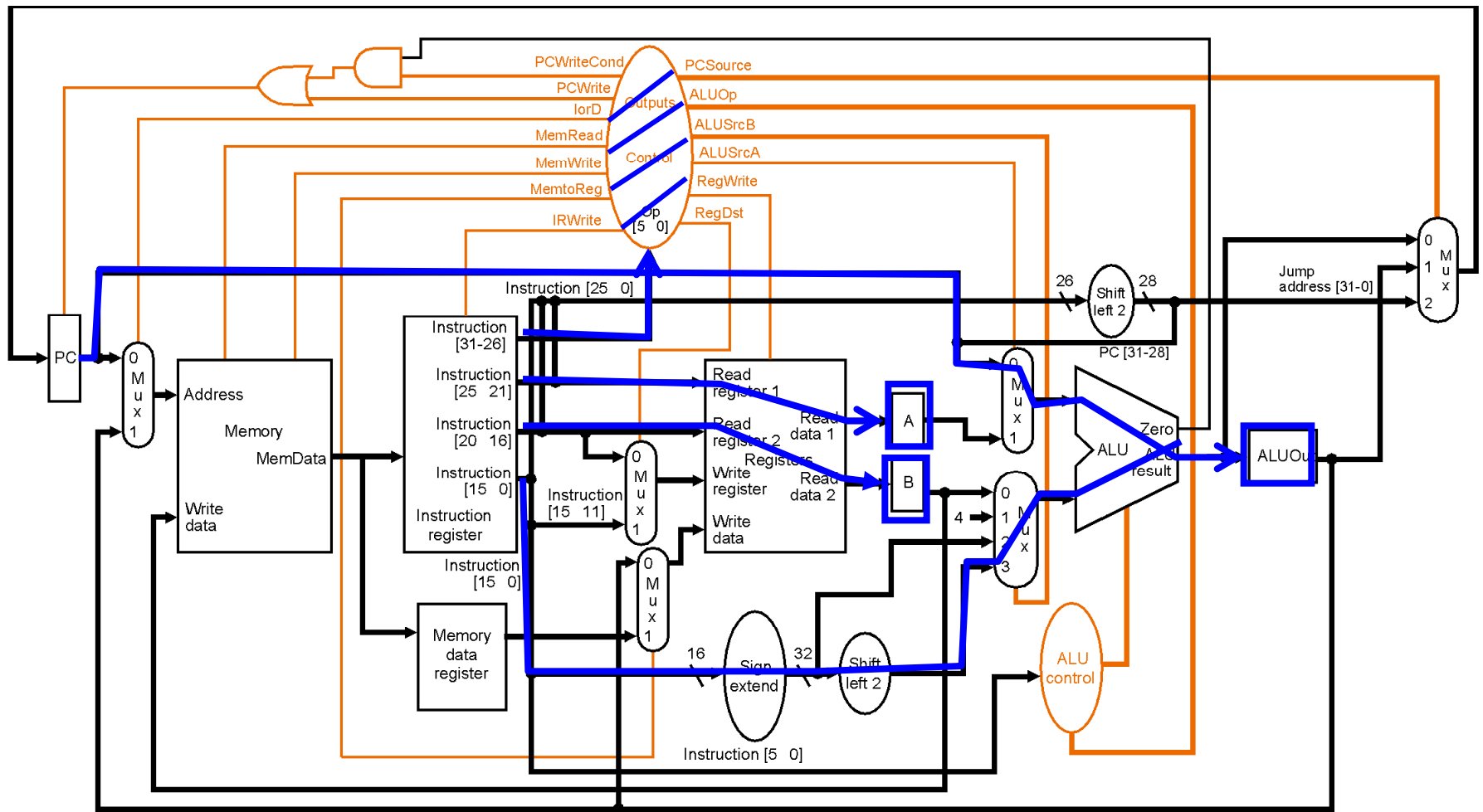
Control for First Two Cycles



- Specification of Control
 - Using a Finite State Machine (FSM)



Cycle 2: ID & RF Cycle



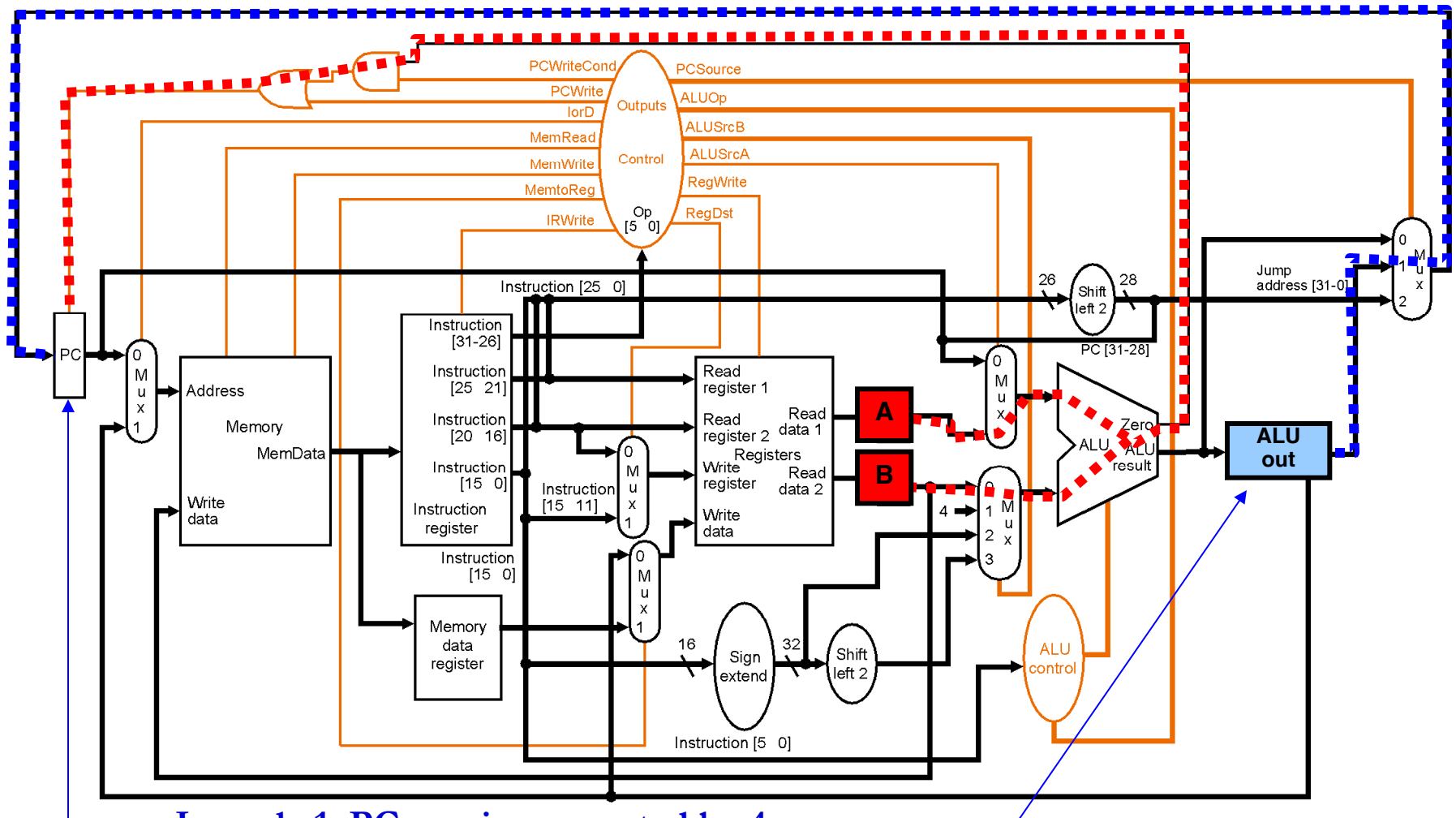
Control:

ALUSrcA=0, ALUSrcB=11, ALUOp=00

How about other signals? RegWrite, MemWrite, RegDest?



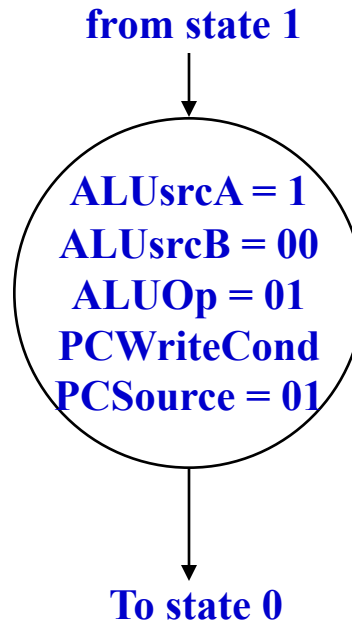
Cycle 3 for beq: Execute



- In cycle 1, PC was incremented by 4
- In cycle 2, ALUout was set to branch target
- This cycle, we conditionally update PC: if (A==B) PC=ALUout



FSM State for Cycle 3 of beq



R-type Instructions

- Cycle 3 (EXecute)

$$\mathbf{ALUout = A \ op \ B}$$

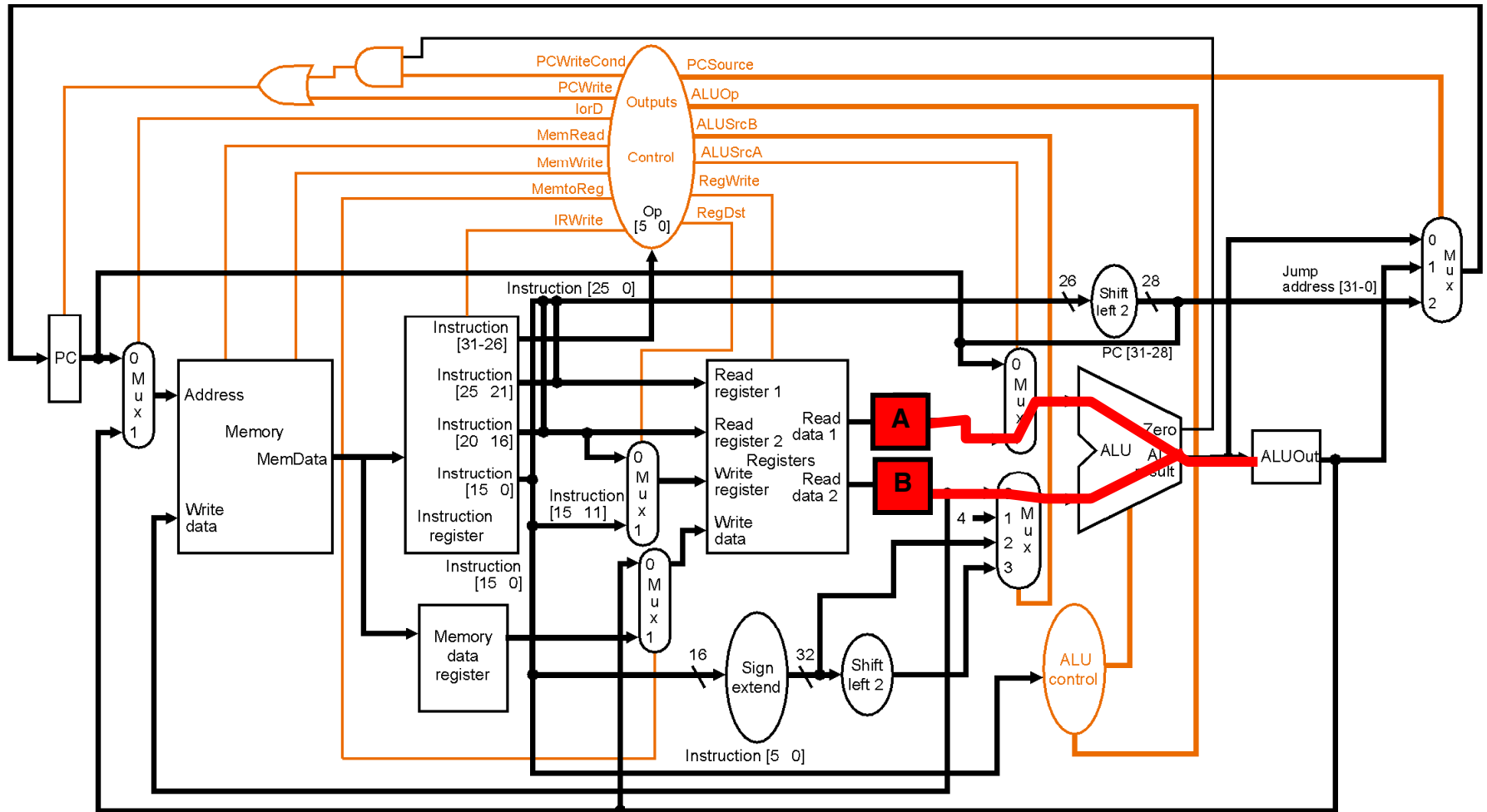
- Cycle 4 (WriteBack)

$$\mathbf{GPR[IR[15-11]] = ALUout}$$

R-type instruction is finished



R-Type Execution

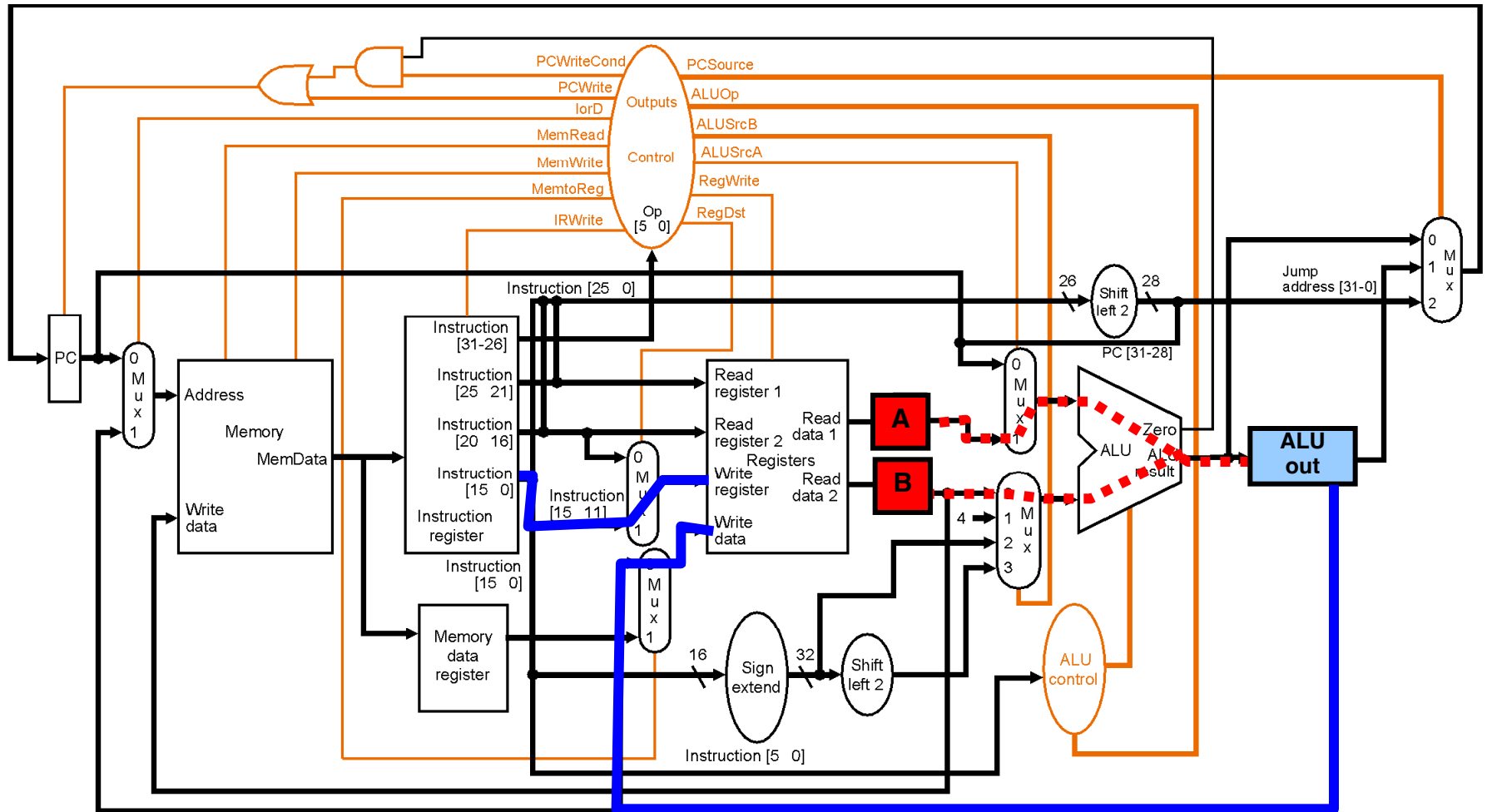


Cycle 3: **ALUout = A op B**

Cycle 4: **GPR[IR[15-11]] = ALUout**



R-Type Execution & WB

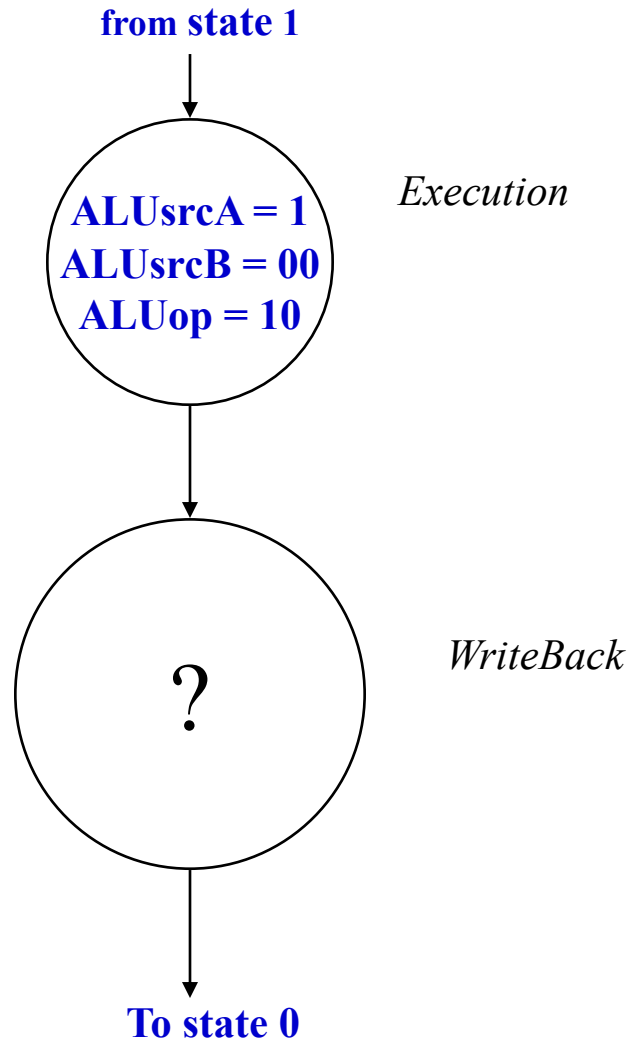


Cycle 3: $ALUout = A \text{ op } B$

Cycle 4: $GPR[IR[15-11]] = ALUout$



FSM States for R-type Instructions



Load and Store

- **EXecute (cycle 3):**

- Compute memory address

$$\text{ALUout} = A + \text{sign-extend}(\text{IR}[15-0])$$

- **Mem (cycle 4):**

- Access memory (read or write)

Store: $\text{Mem}[\text{ALUout}] = B$ (store finished)

Load: $\text{MDR} = \text{Mem}[\text{ALUout}]$

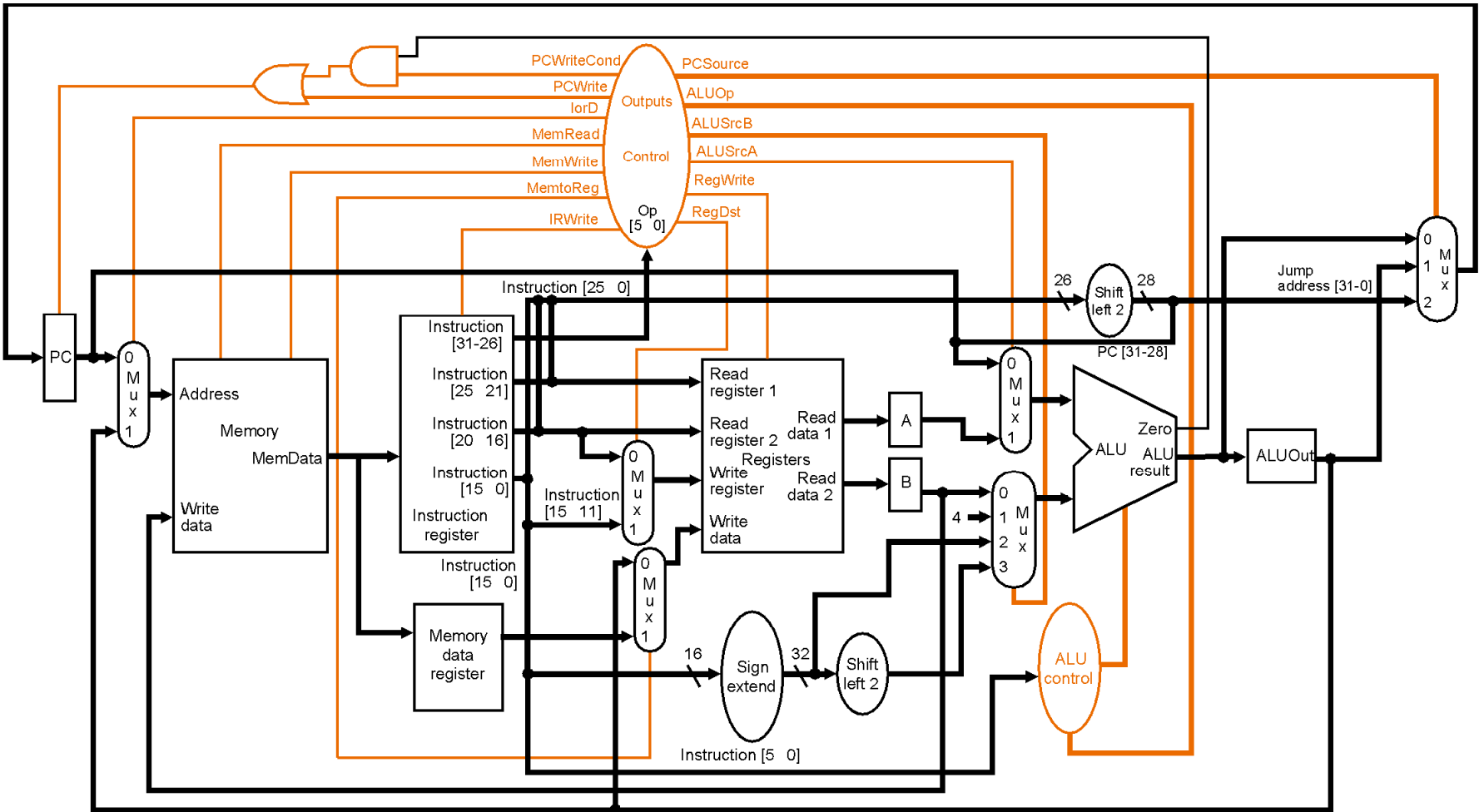
- **WB (cycle 5):**

- Write register (only for load))

$$\text{GPR}[\text{IR}[20-16]] = \text{MDR}$$

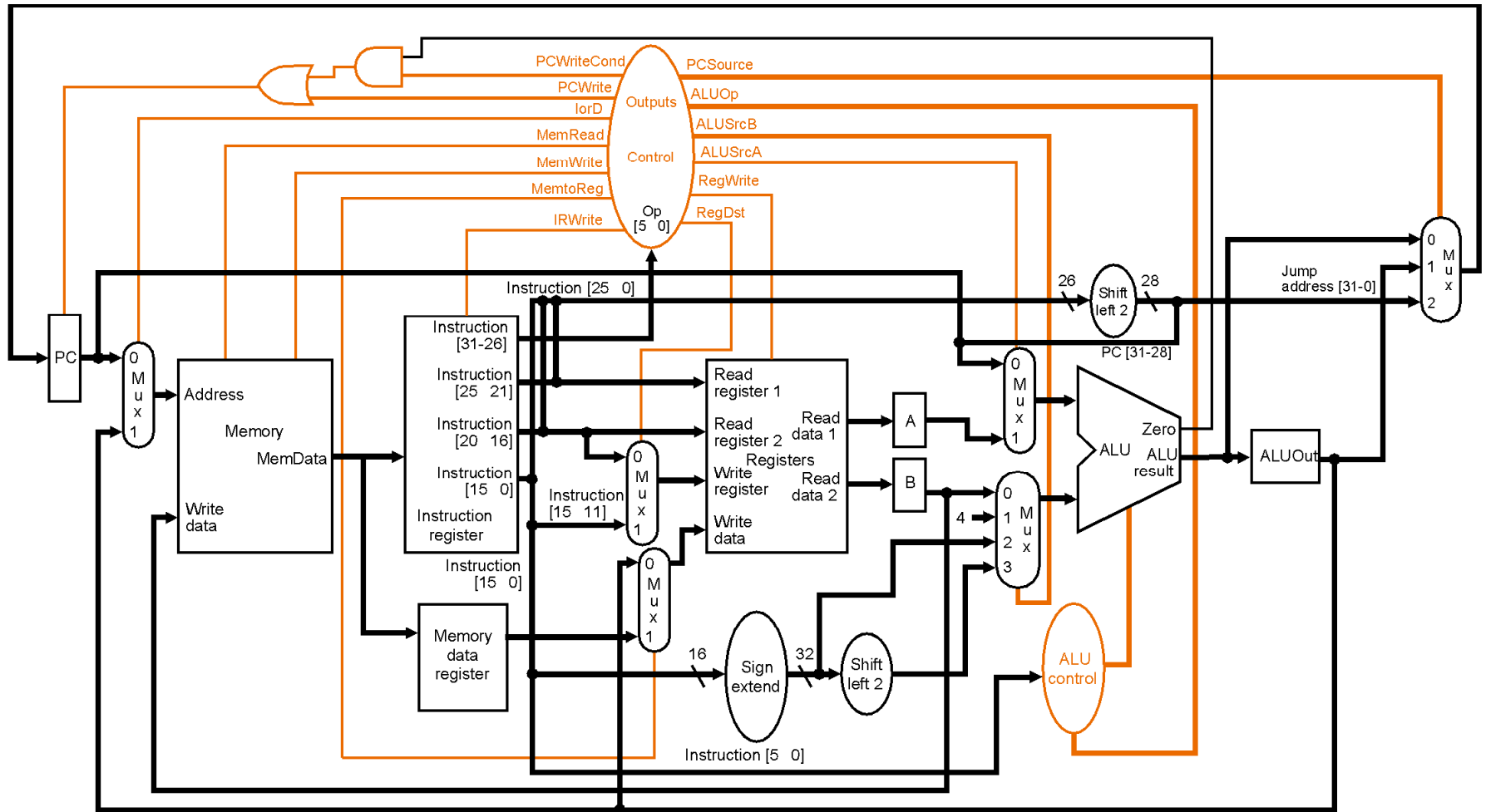


Cycle 3 for lw/sw: Address Computation



ALUout = A + sign-extend(IR[15-0])

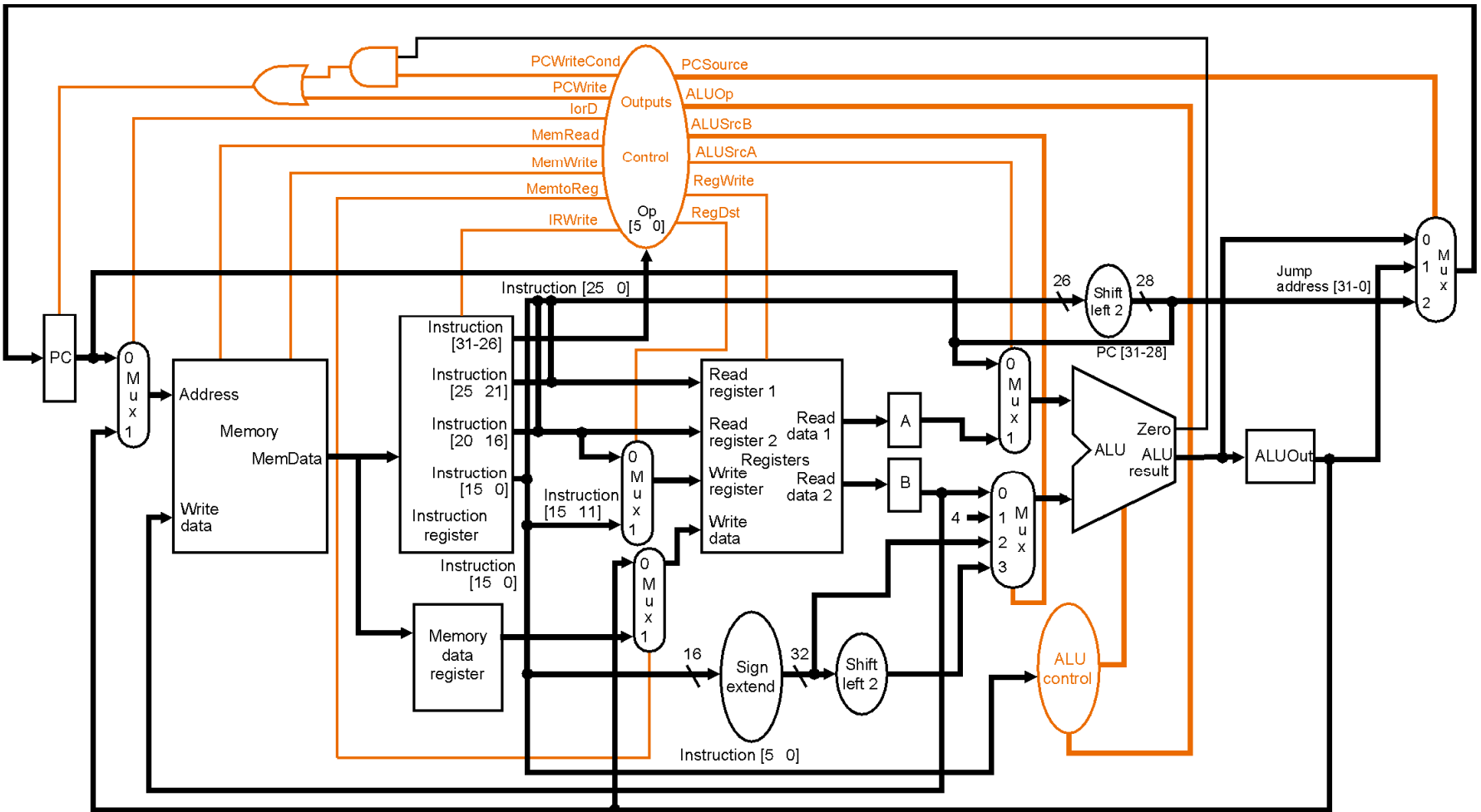
Cycle 4 for Store: Memory Access



Memory[ALUout] = B



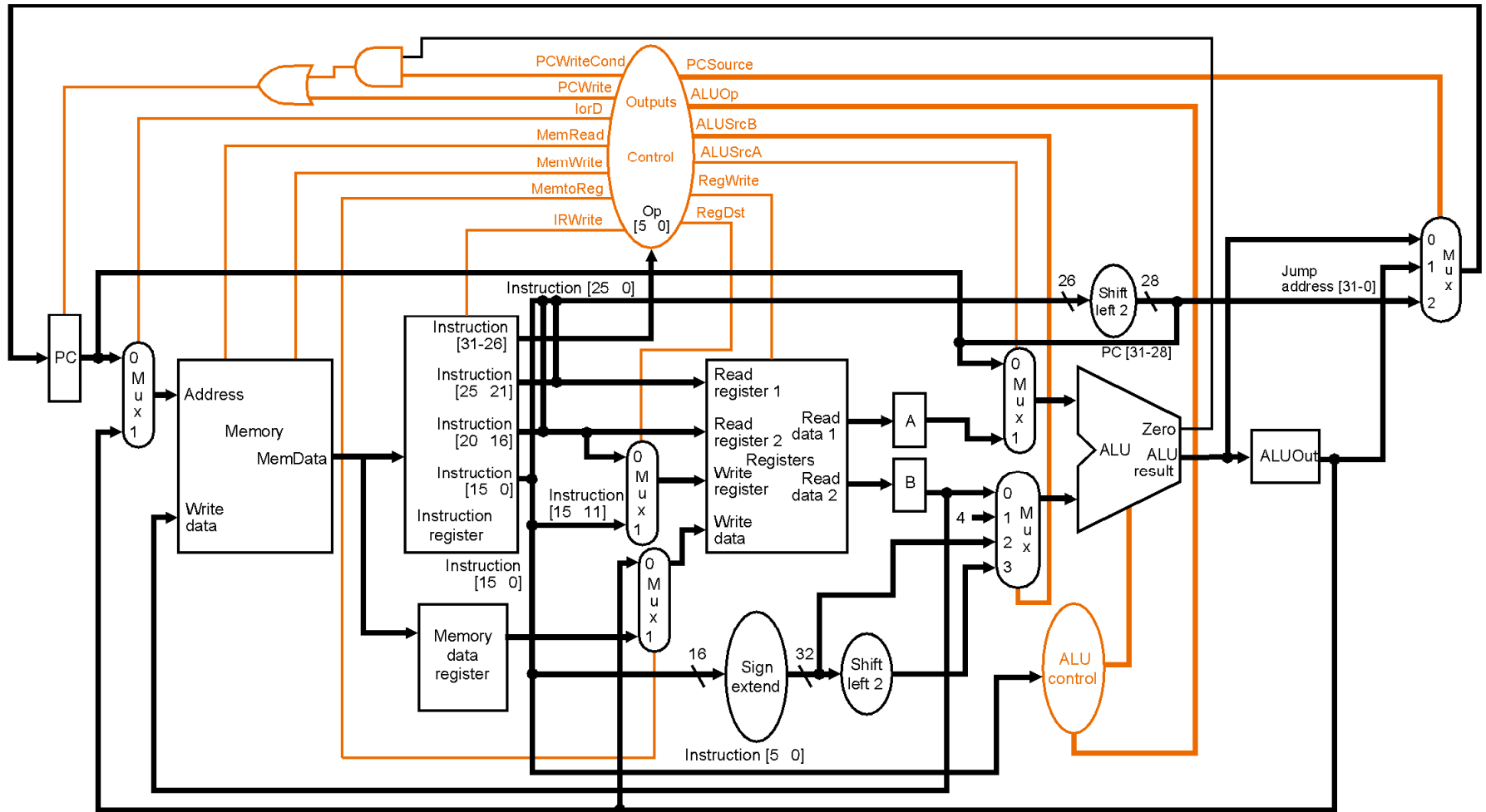
Cycle 4 for Load: Memory Access



MDR = Memory[ALUout]



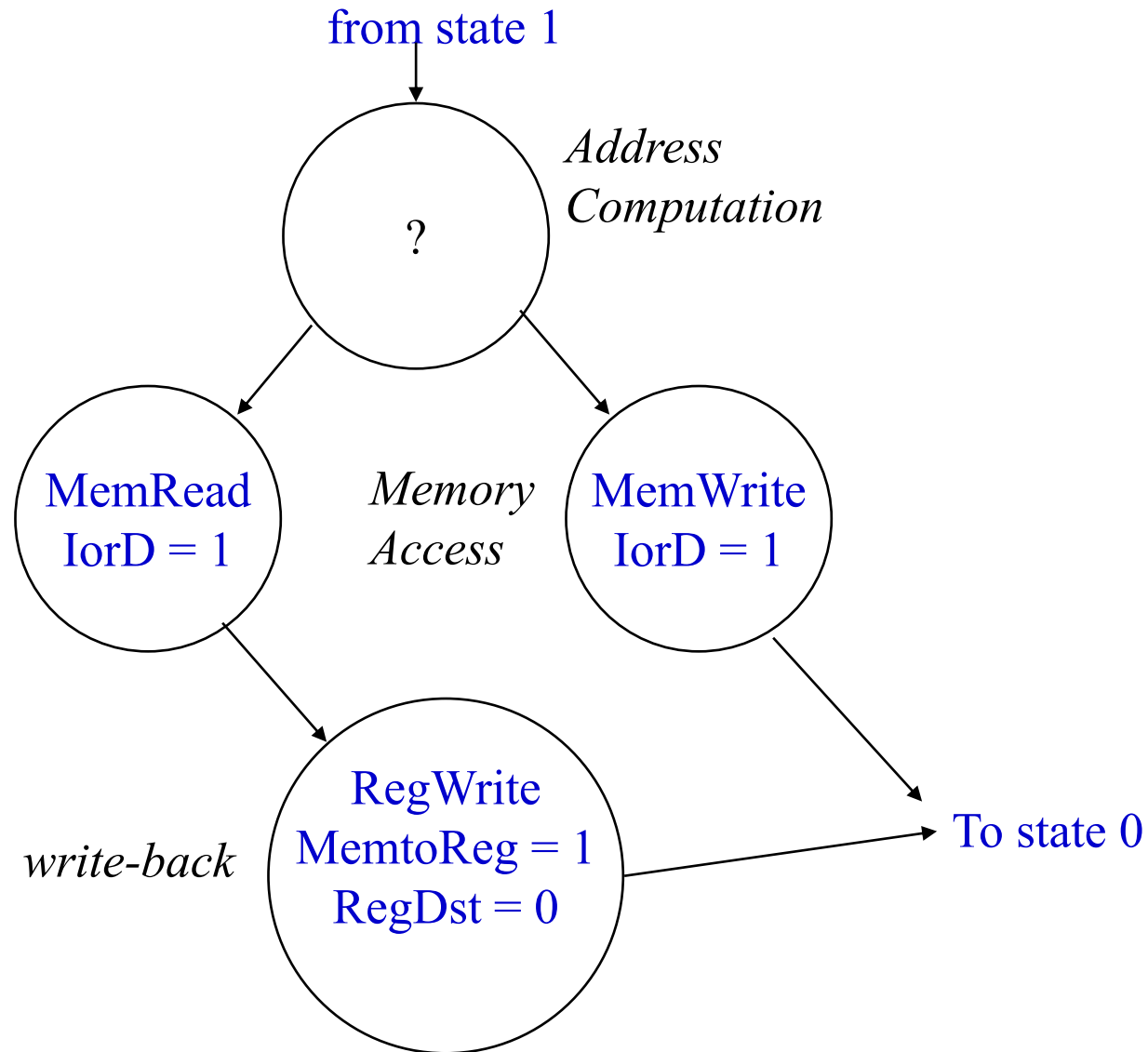
Cycle 5 for load: WriteBack



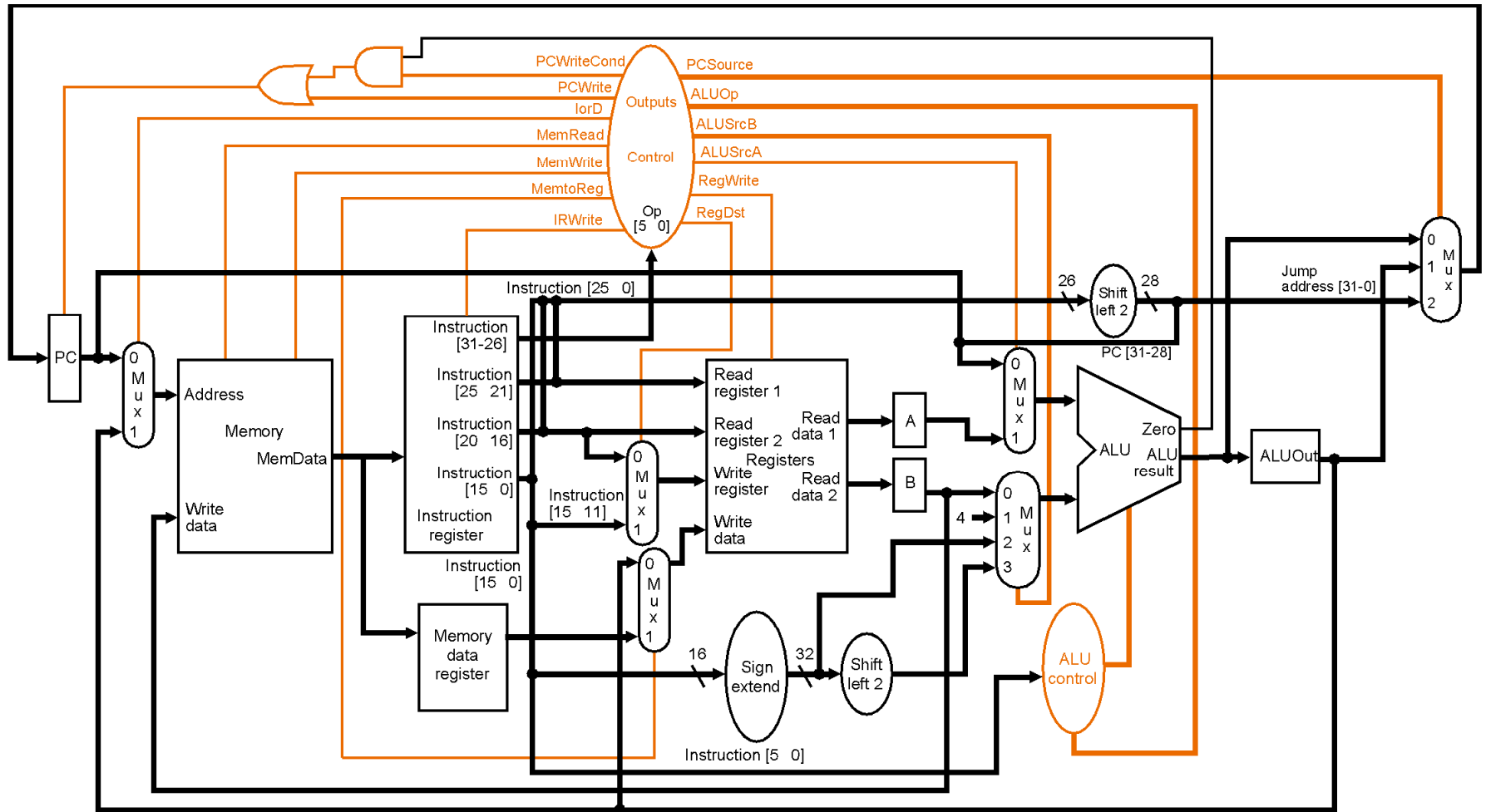
GPR[IR[20-16]] = MDR



Memory Instruction States



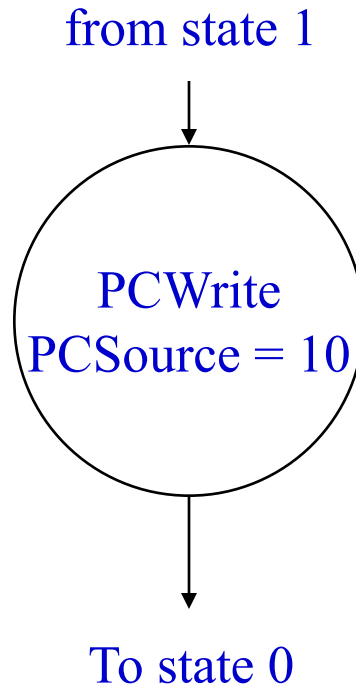
Cycle 3 for Jump



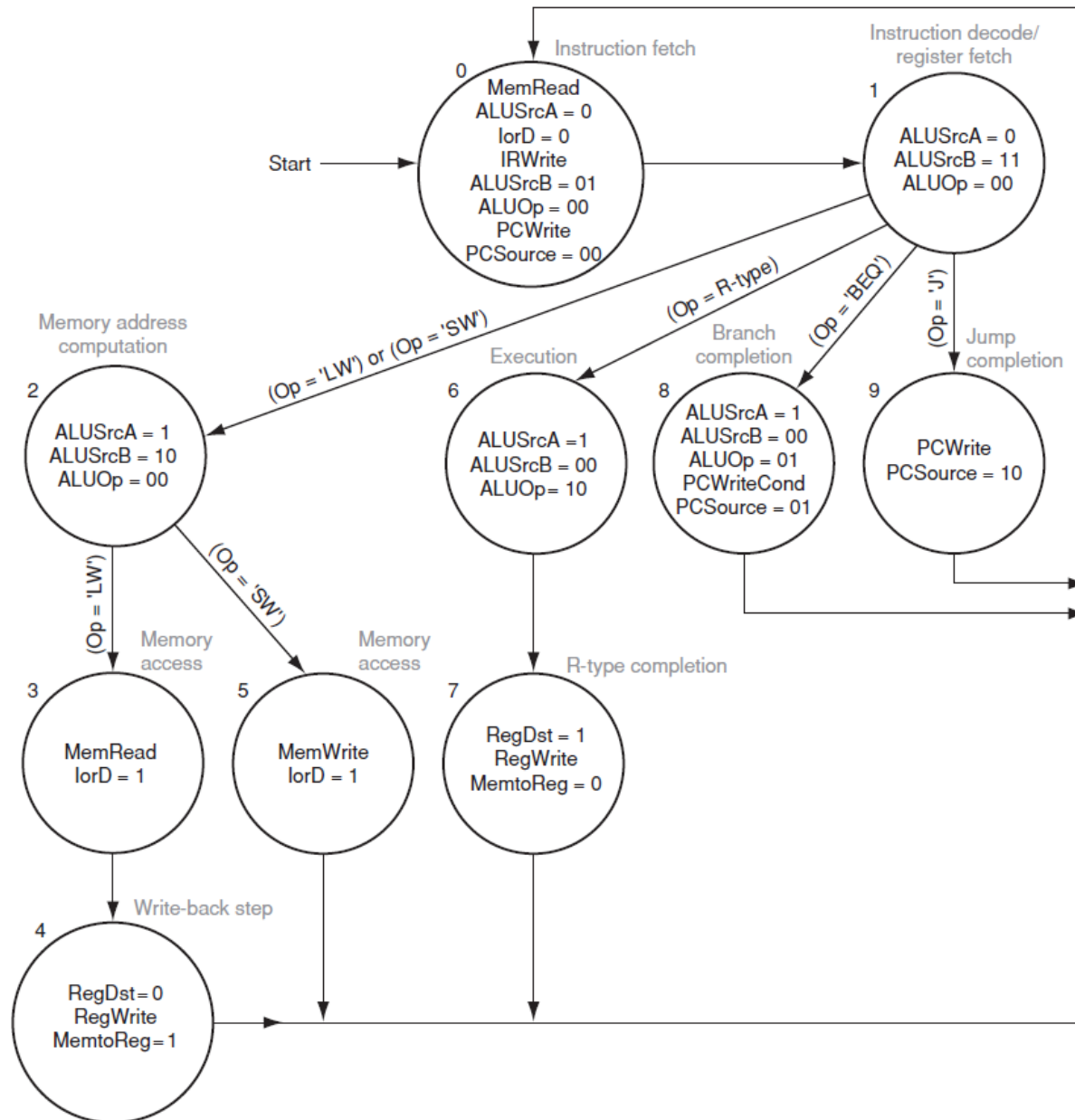
$$PC = PC[31-28] \mid (IR[25-0] \ll 2)$$



Cycle 3 Jump FSM state

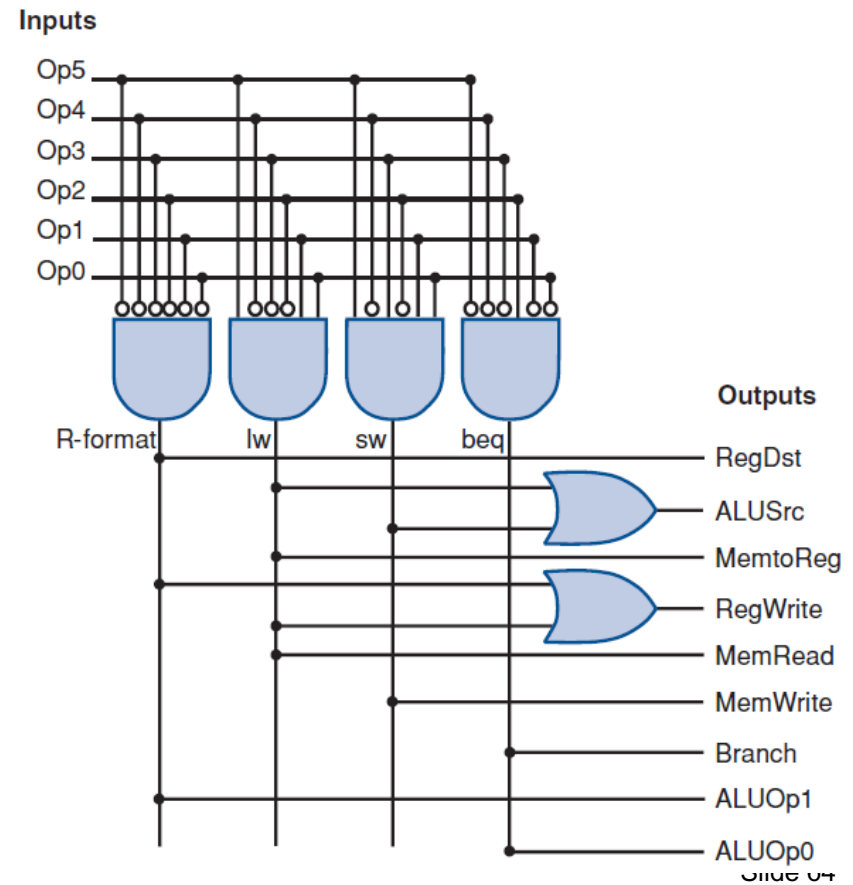


Complete FSM



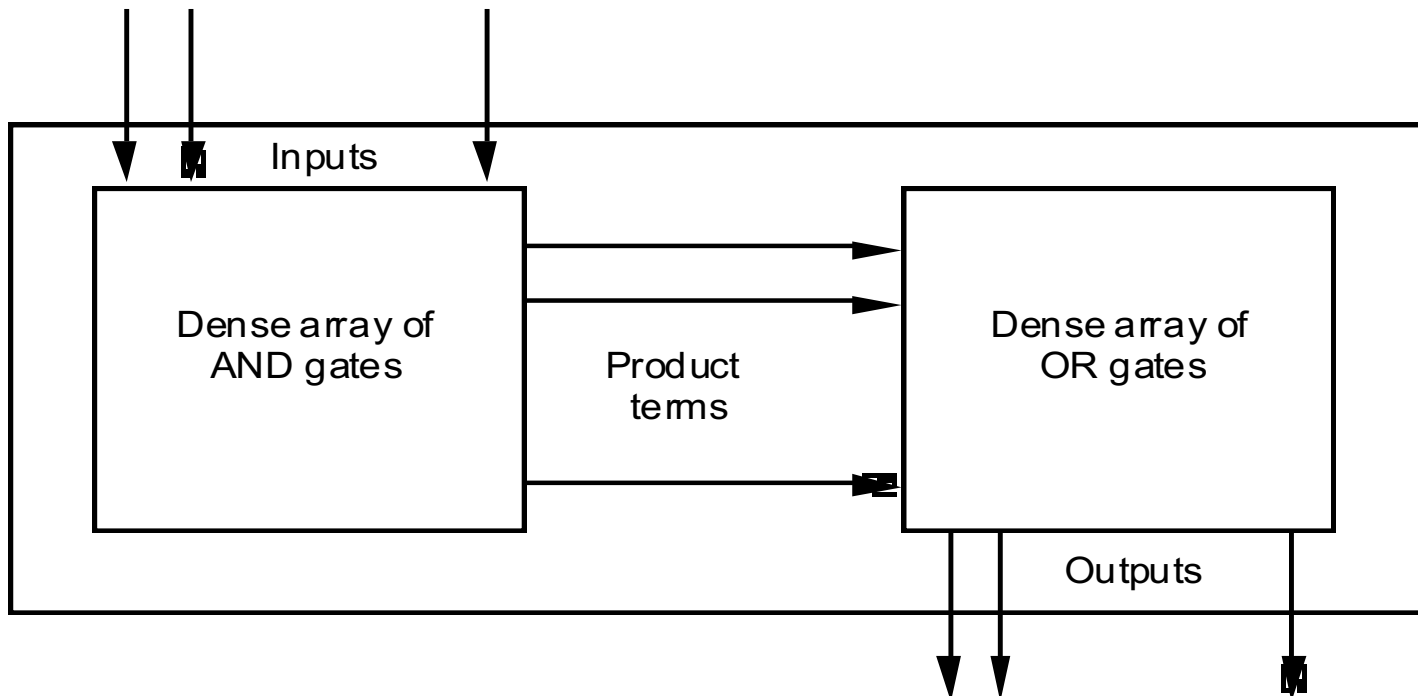
Single-Cycle Control Unit Implementation

- Unstructured LogicDesign
 - By Karnaugh Map
- PLA/PAL

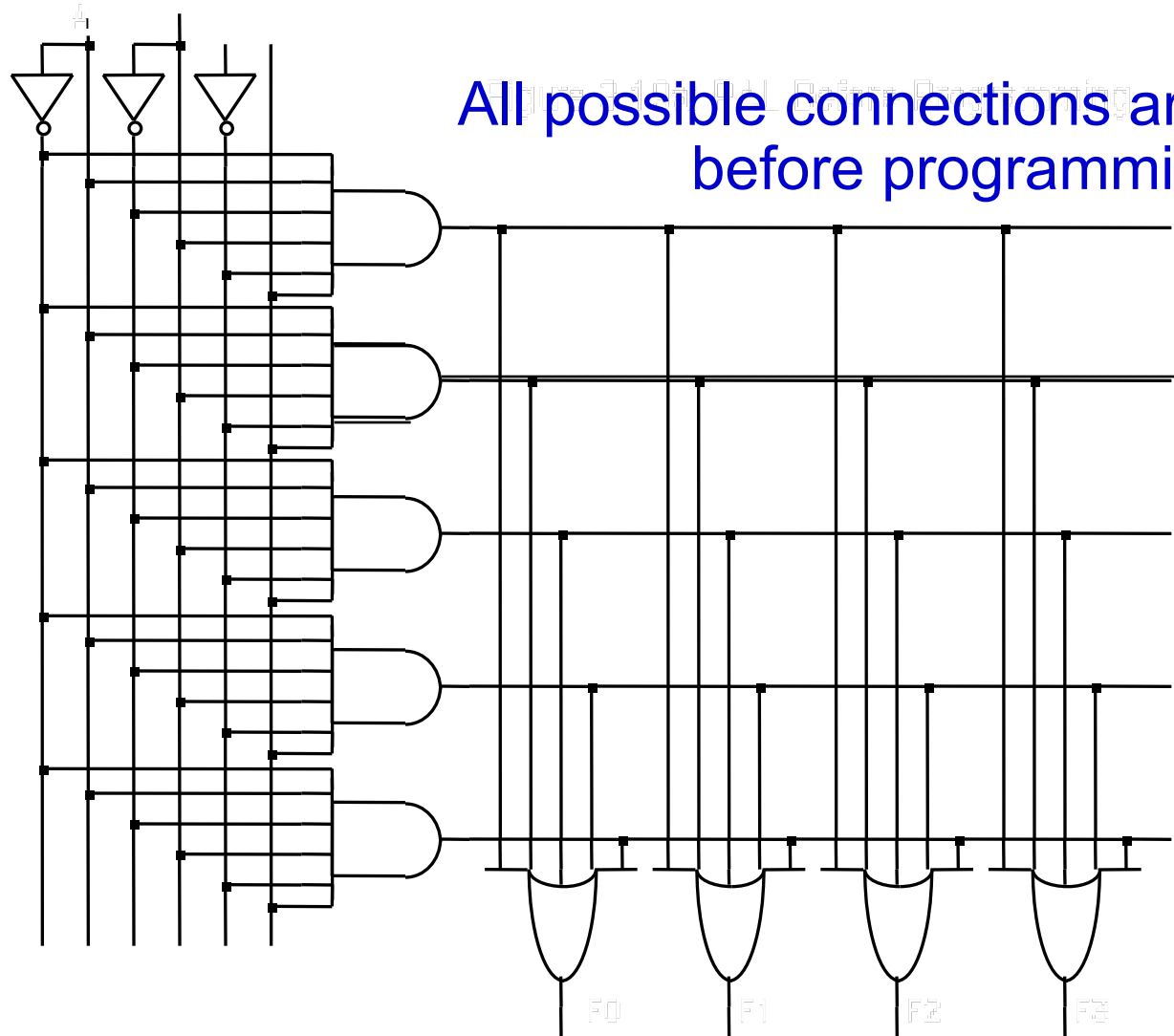


PAL/PLA

- What is PAL/PLA?
 - Pre-fabricated building block of many AND/OR gates (or NOR/NAND)
 - Personalized by making or breaking connections among gates



PLA



All possible connections are available before programming

PLA Example

$$F1 = A B C$$

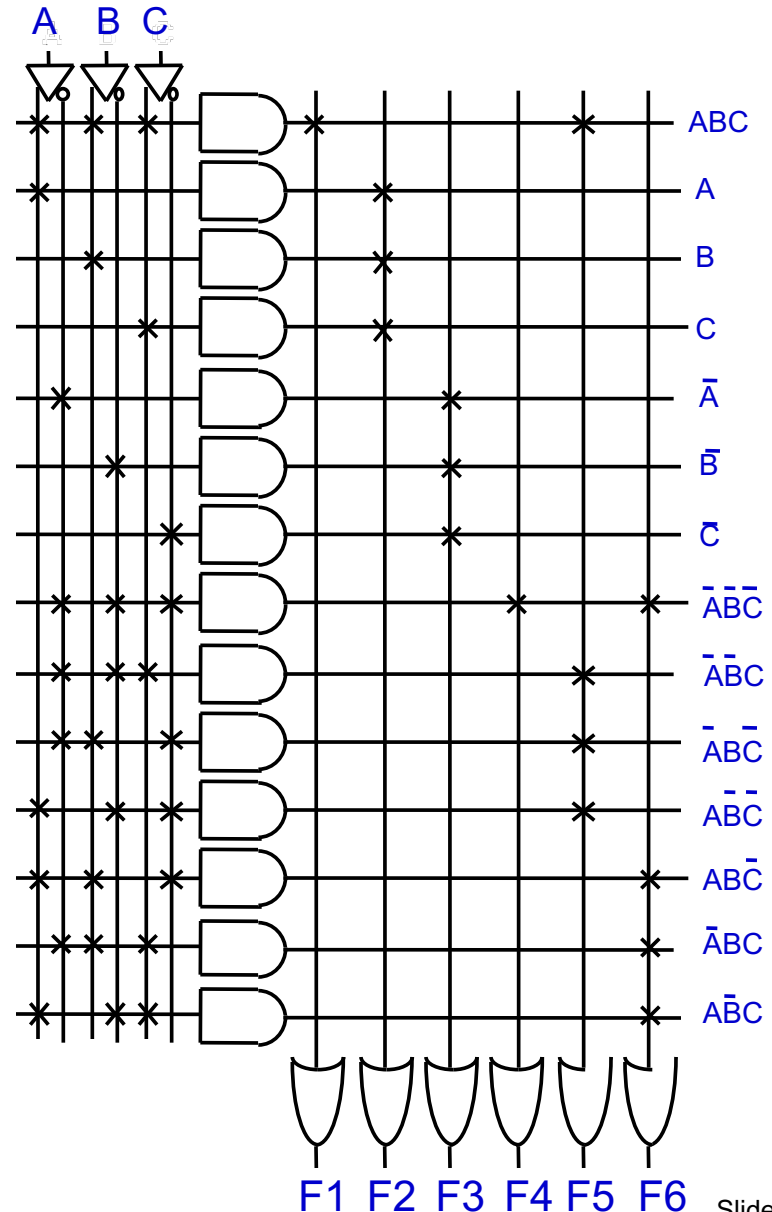
$$F2 = A + B + C$$

$$F3 = \overline{A B C}$$

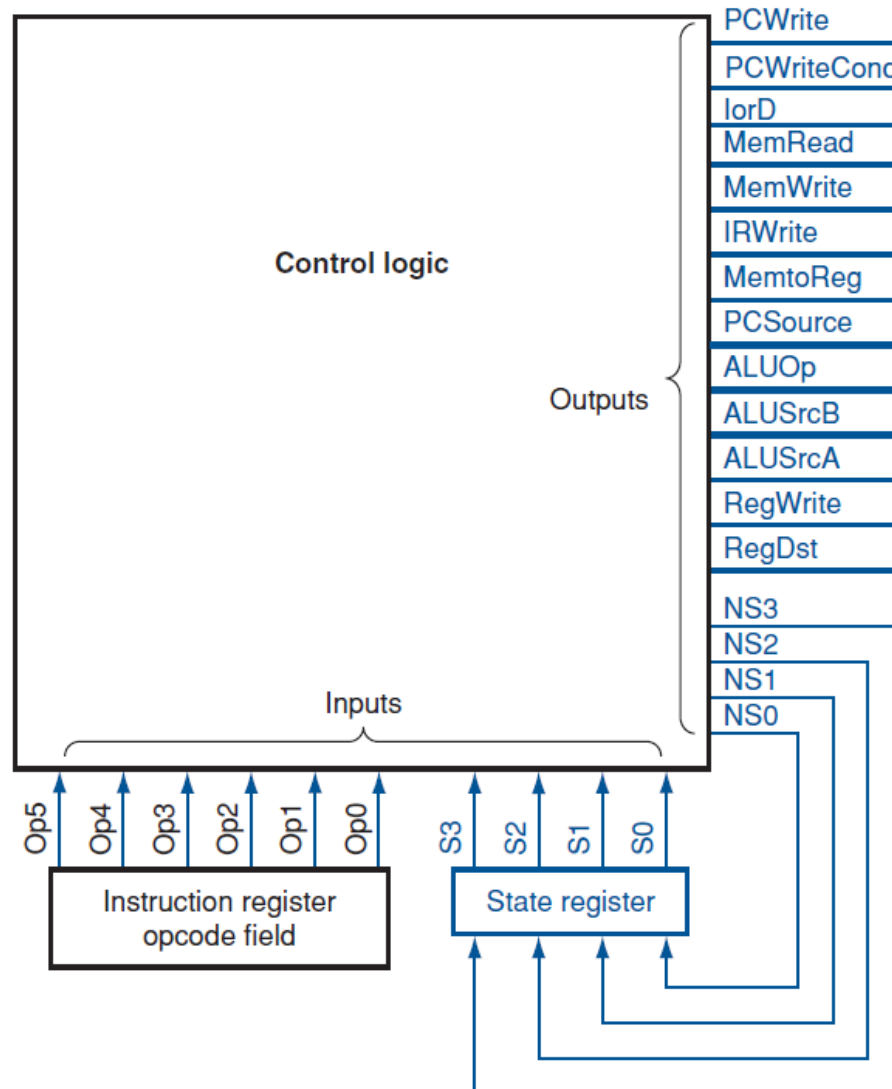
$$F4 = \overline{A + B + C}$$

$$F5 = A \text{ xor } B \text{ xor } C$$

$$F6 = A \text{ xnor } B \text{ xnor } C$$



Multi-Cycle Control Unit Implementation



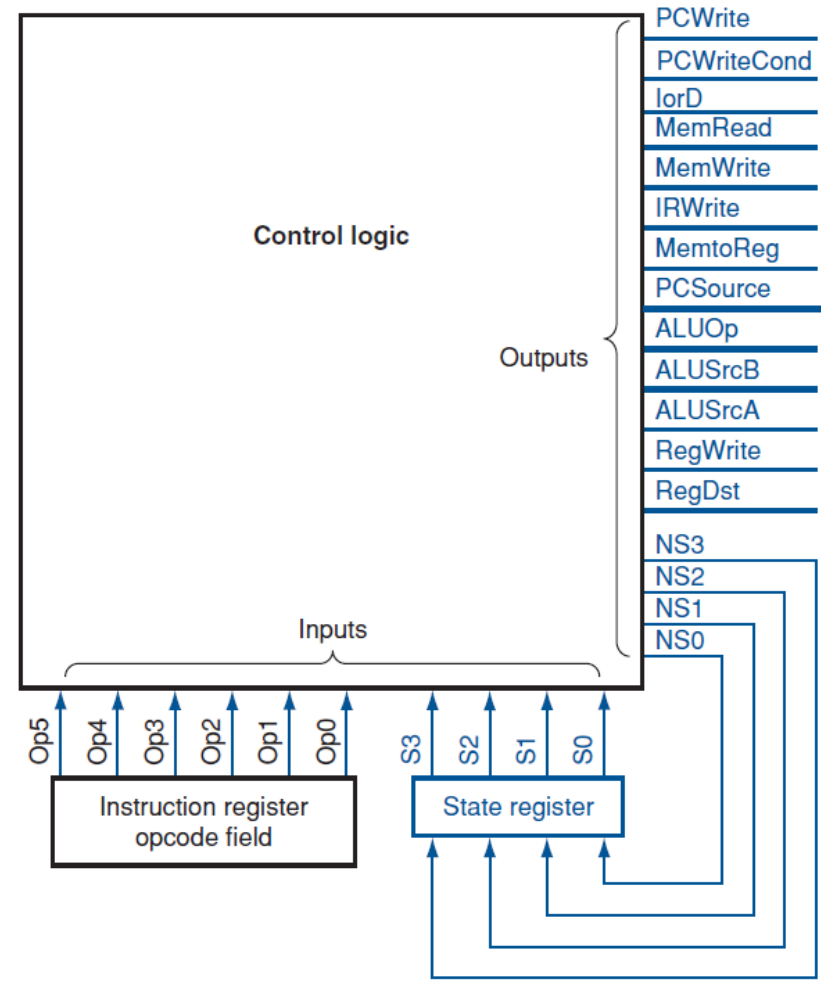
Multi-Cycle Control Unit Implementation (cont.)

- State Register (S3~S0)
- Control Logic
 - Combinational logic
 - Inputs ?
 - Outputs ?



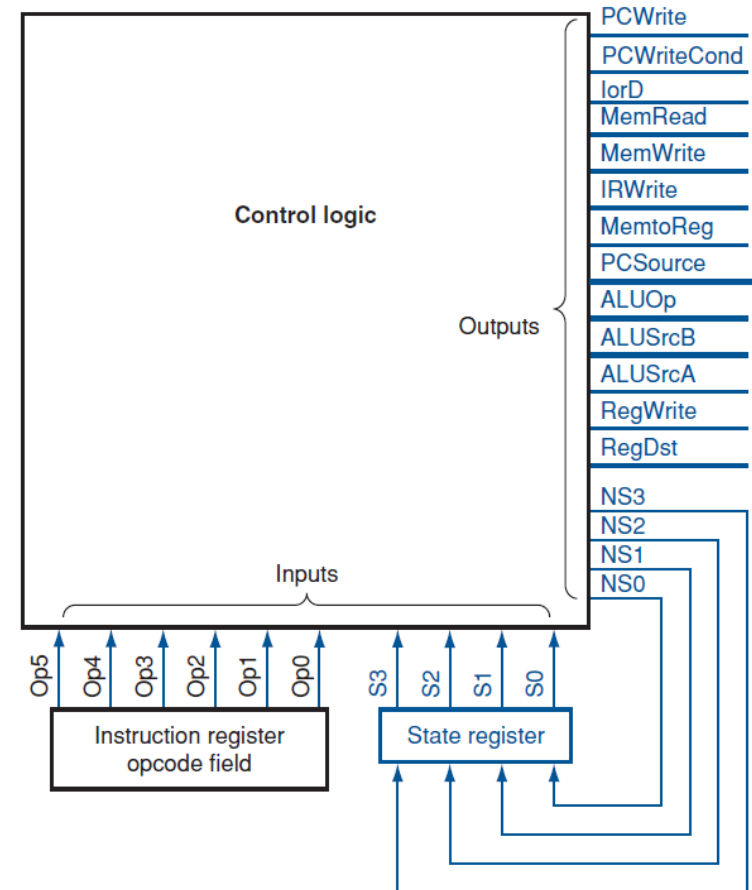
Multi-Cycle Control Unit Implementation (cont.)

- Control Logic **Inputs**
 - Opcode bits: Op5~Op0
 - S3~S0

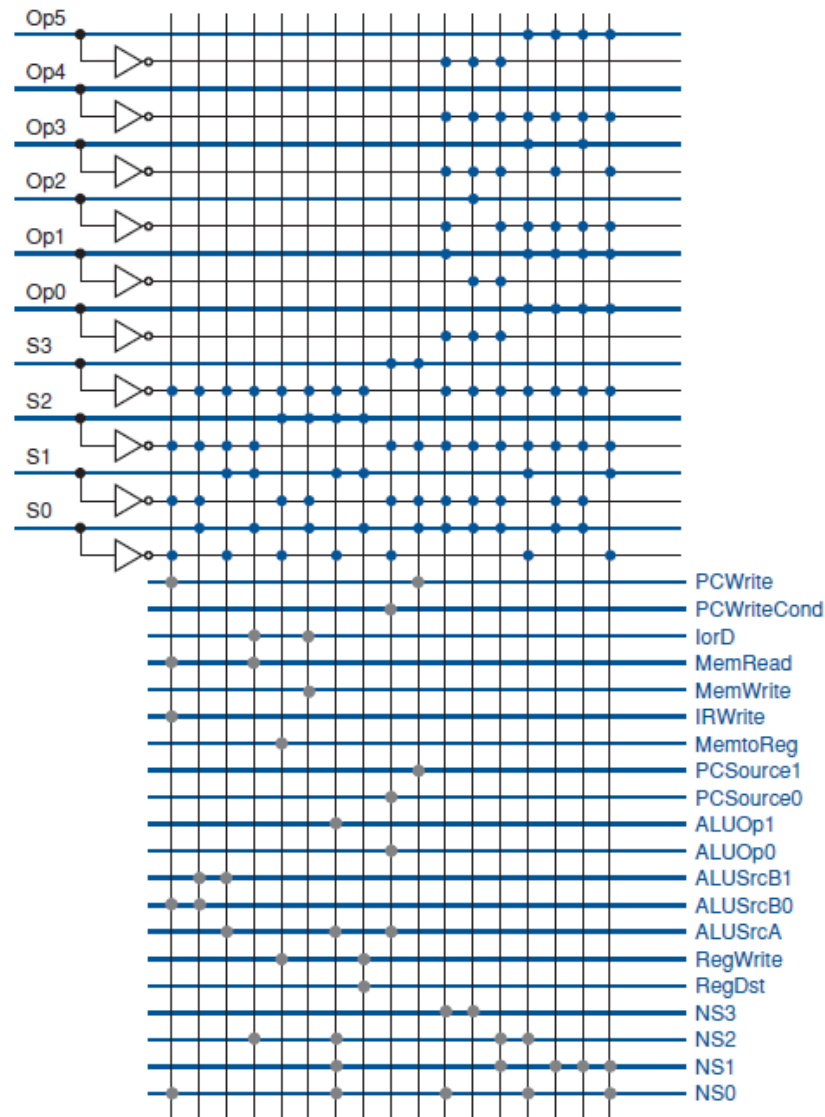


Multi-Cycle Control Unit Implementation (cont.)

- Control Logic **Outputs**
 - Control signals: PCWrite, lorD, ...
 - Depends only on current state
 - NS3~NS0
 - Depends on both current state & opcode bits



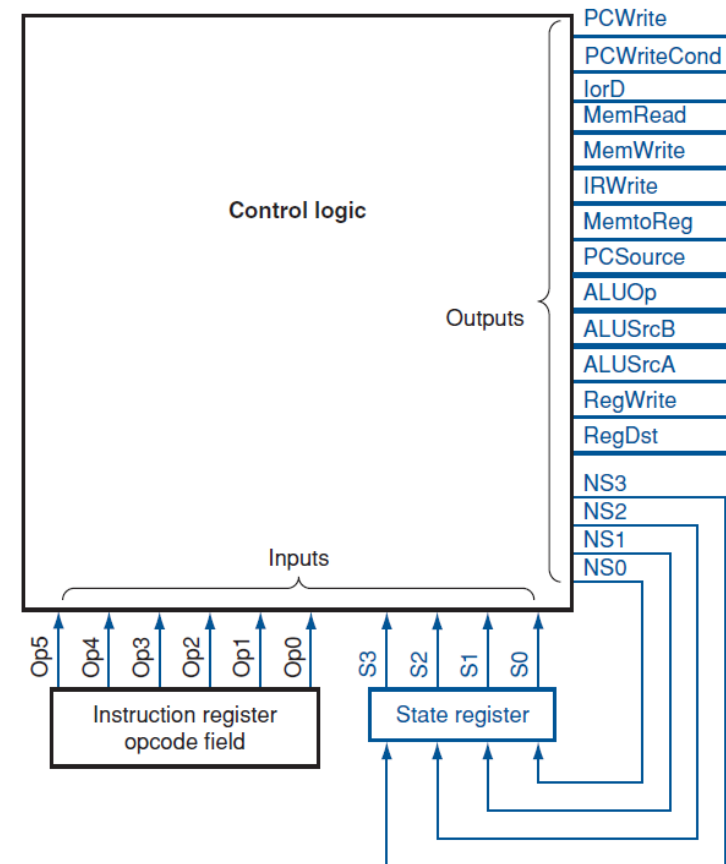
Multi-Cycle Control Unit Implementation in PLA



Multi-Cycle Control Unit Implementation in ROM

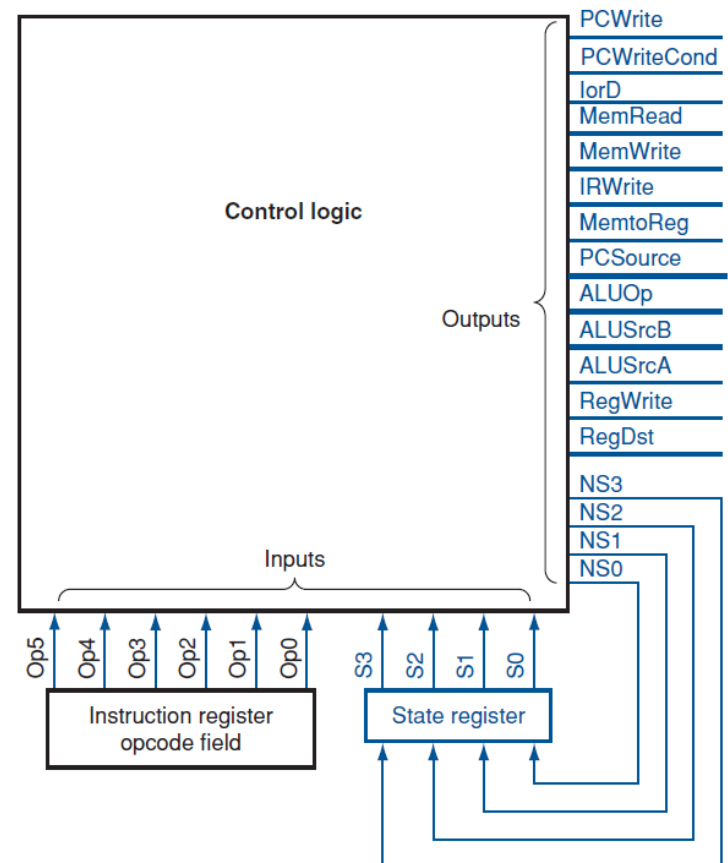
- ROM

- Can be used to implement control unit
- # of inputs: 10
- # of outputs: 20
- Use a ROM with:
 - Address width: 10
 - Data width: 20
 - ROM size: $20 \times 2^{10} = 20\text{Kb}$
 - 1024 entries



Multi-Cycle Control Unit Implementation in ROM (cont.)

- Question:
 - Can we use smaller ROM(s) to implement control unit?
- Answer: 2 Separate ROMs
 - First ROM: $16 \times 2^4 = 256b$
 - # of inputs: 4
 - # of outputs: 16
 - Second ROM: $4 \times 2^{10} = 4Kb$
 - # of inputs: 10
 - # of outputs: 4
 - Total ROM size: 4.3Kb



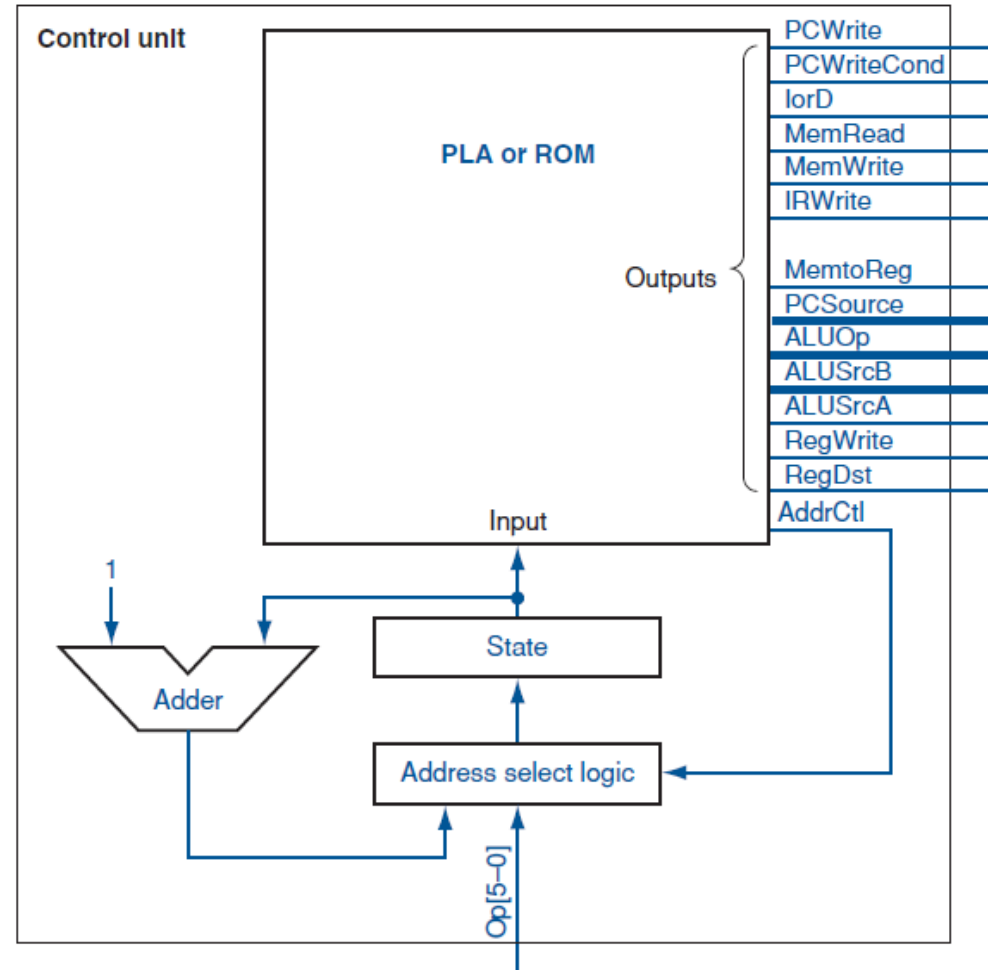
Implementing Multi-Cycle Control Using Micro-Program

- Cons of ROM Implementation
 - 95% of ROM used to indicate next state
 - 4Kbits
 - What if we have more complex ISA?
 - FP instructions which may take several cycles
- Example:
 - Consider an FSM which requires 10 FFs
 - What would be size of ROM?
- What's Solution?

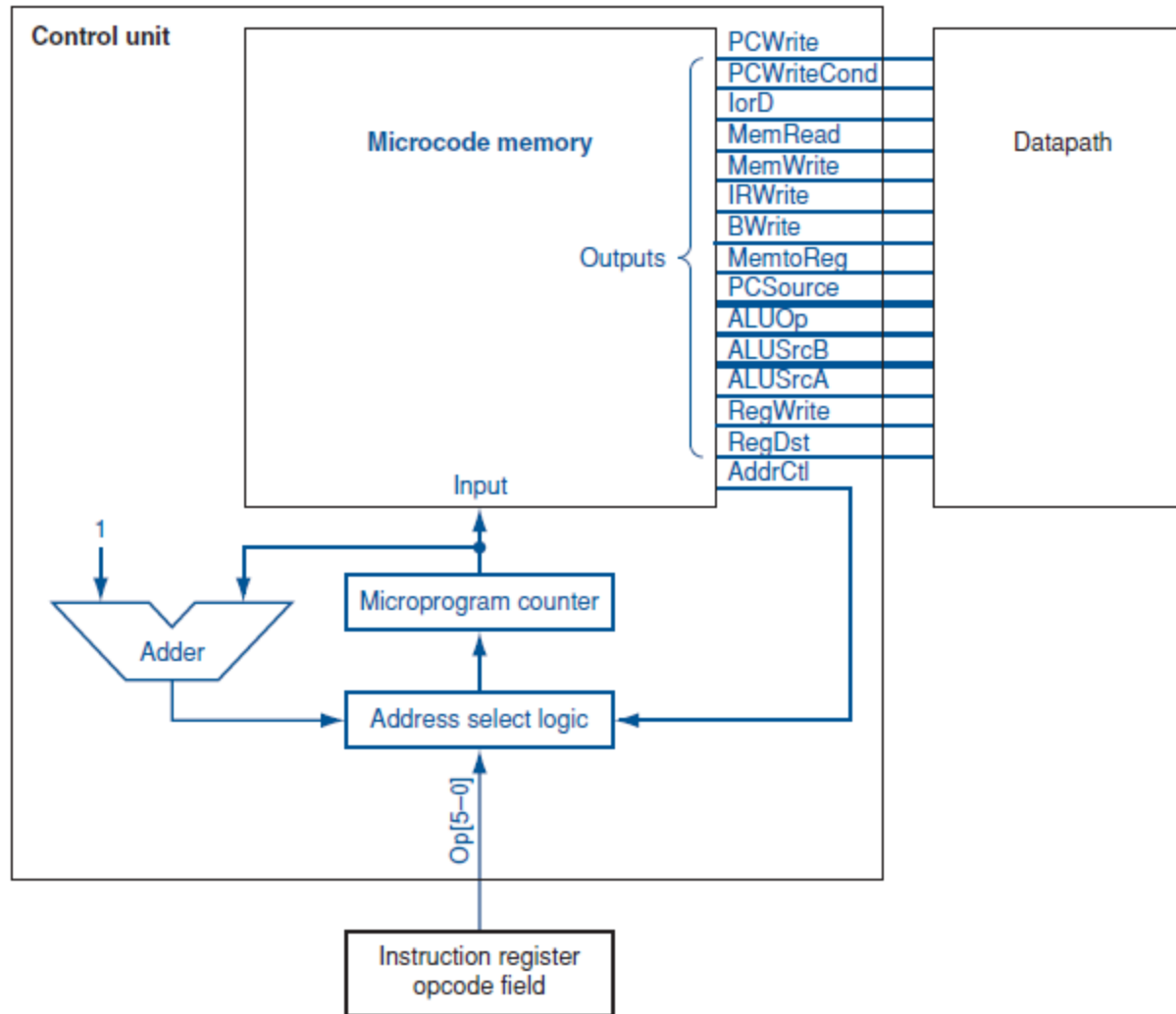


Implementing Multi-Cycle Control Using Micro-Program (cont.)

- ROM Control Words
 - Micro-instructions
- State Register
 - Micro-program counter
 - Also called:
 - Microcode sequencer



Implementing Multi-Cycle Control Using Micro-Program (cont.)

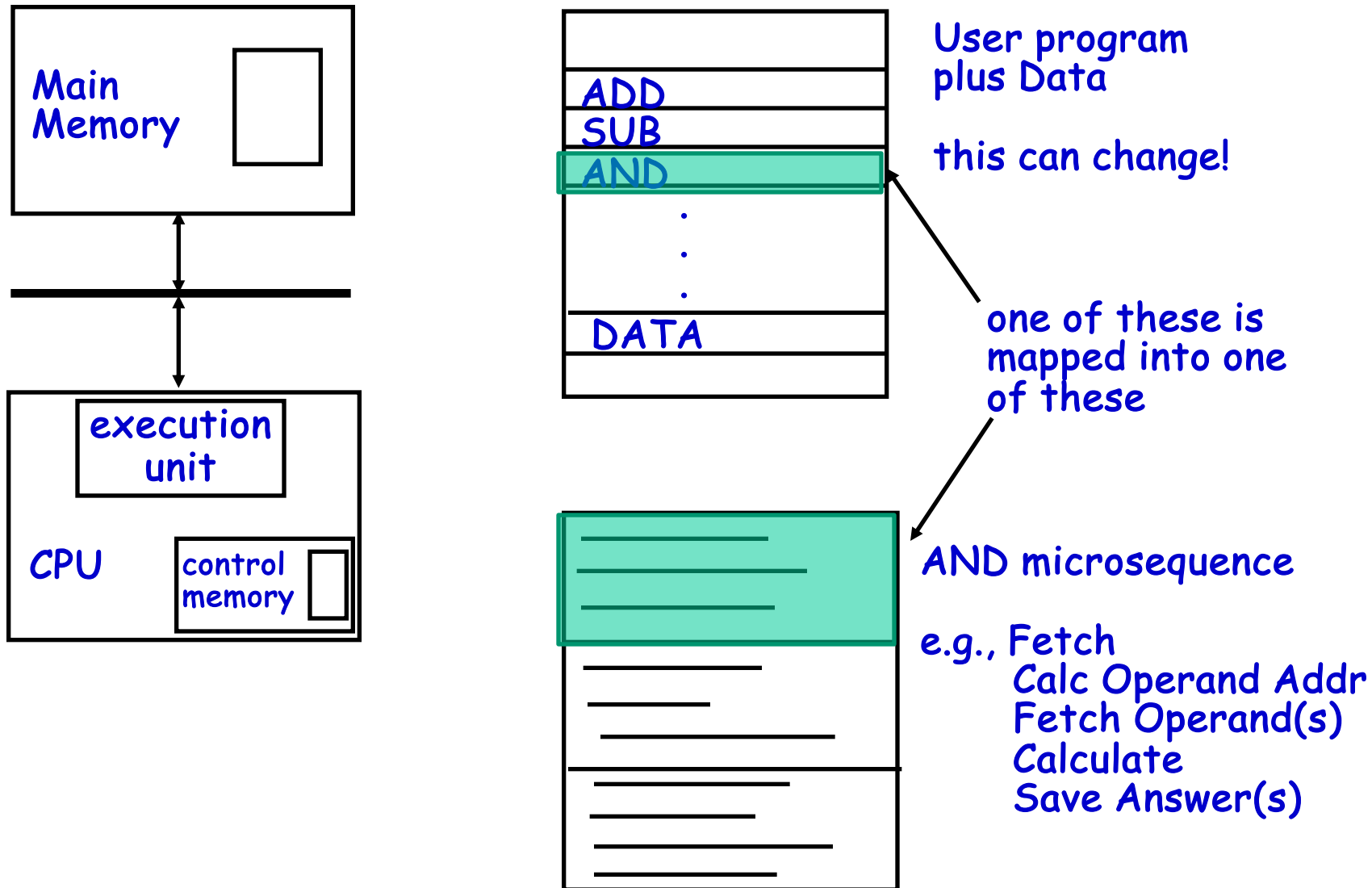


Microprogramming (cont.)

- A Convenient Method to Implement *structured* control state diagrams
 - Random logic replaced by μ -PC sequencer and ROM
 - Each line of ROM called a μ -instruction
 - Limited state transitions:
 - Branch to zero, next sequential, branch to μ instruction address from dispatch ROM



Macro-Instruction Interpretation



Microprogramming (cont.)

- 80x86 Instructions
 - Instructions translate to 1 to 4 micro-operations
- Complex 80x86 Instructions
 - Executed by a conventional microprogram (8K x 72 bits) that issues long sequences of micro-operations



Hardwired vs. Micro-Programmed

- Micro-Programmed
 - Can change micro-operations without changing circuit (just by reprogramming ROM)
 - Easier design approach
 - More disciplined control logic
 - Easier to debug
 - Enables more complex ISA
 - Enables family of machines with same ISA
- Hard-Wired
 - Area efficient
 - Probably less delay



