

Data Structures

Queues

DataLab

November 12, 2016

Outline

- 1 A little bit more about Recursion
 - Changing the Order of Recursion
- 2 The Queues
 - Introduction
 - The Queue Interface
- 3 Basic Applications
 - Some Basic Applications
 - Change the Order of Recursion
 - Radix Sort
 - Simulating Waiting Lines
 - Wire Routing
- 4 Implementation
 - Implementing Queues
 - Derive From ArrayList
 - From Scratch
 - Operations
 - Circular Array

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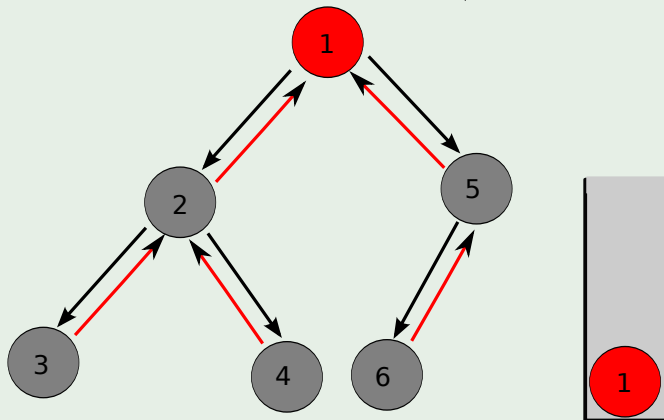
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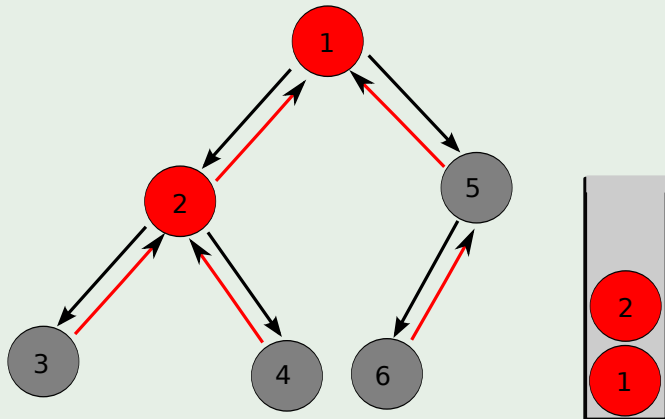
Imagine the following

Stack Order



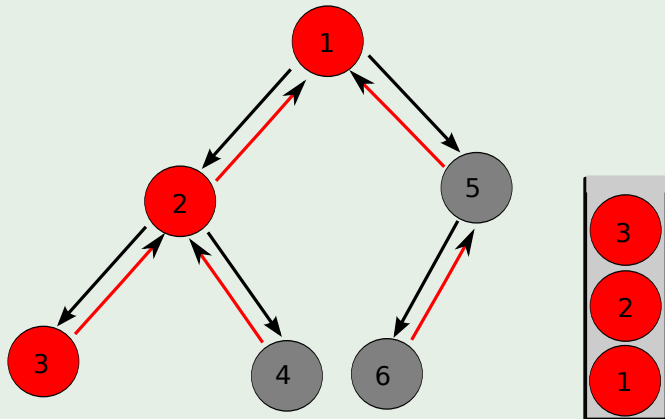
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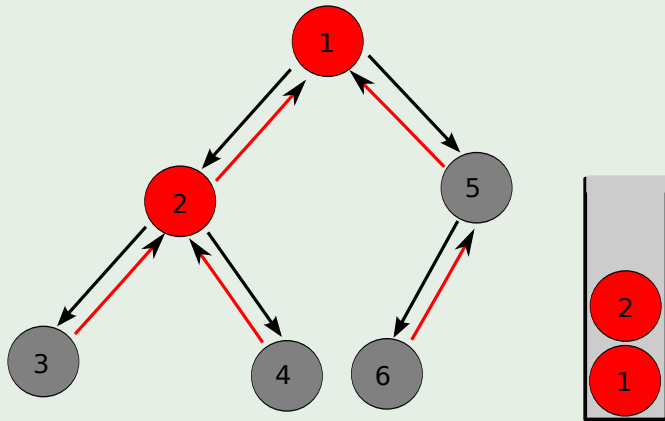
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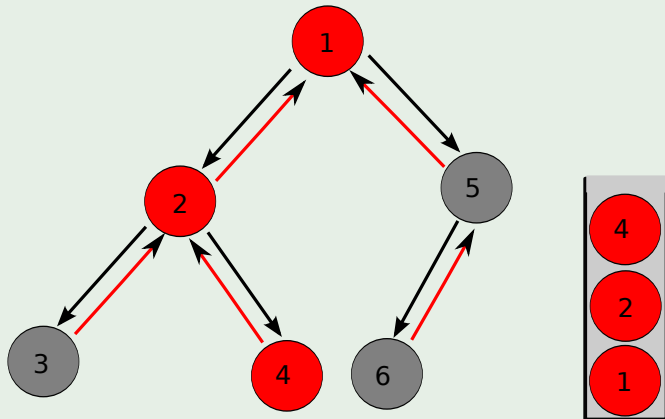
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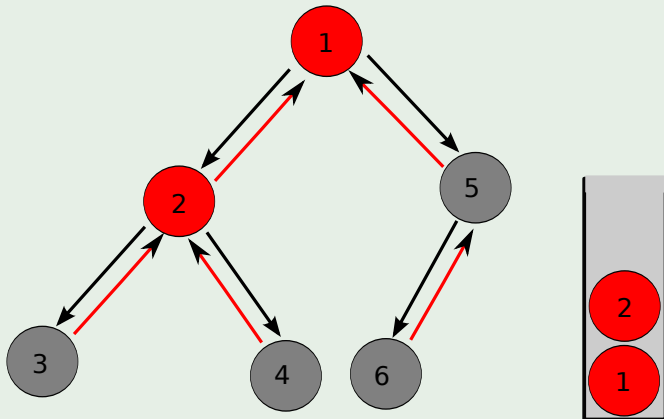
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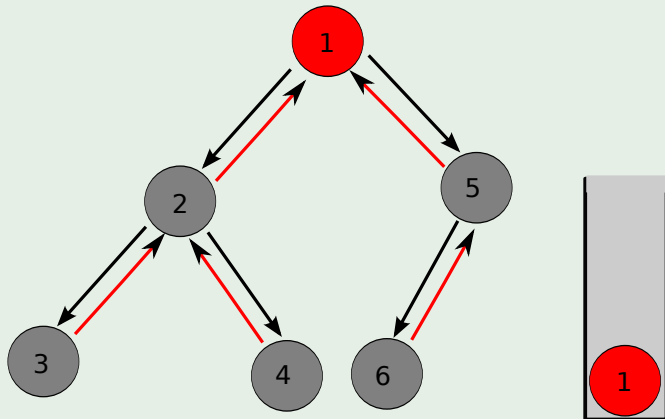
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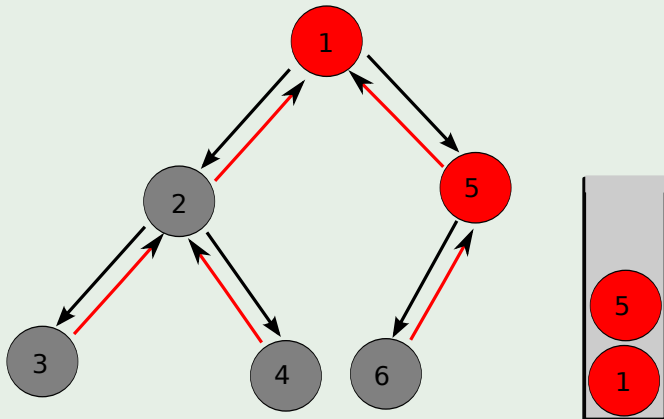
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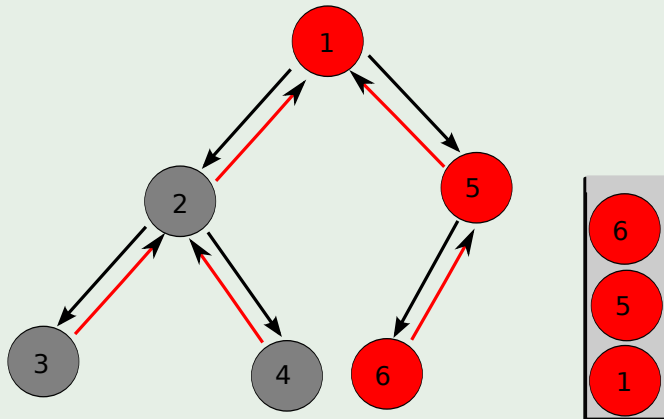
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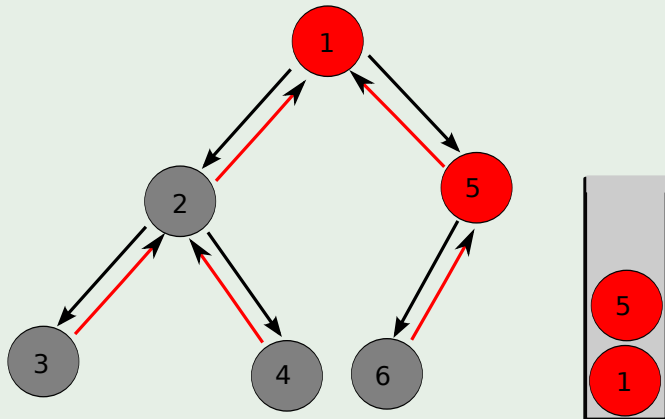
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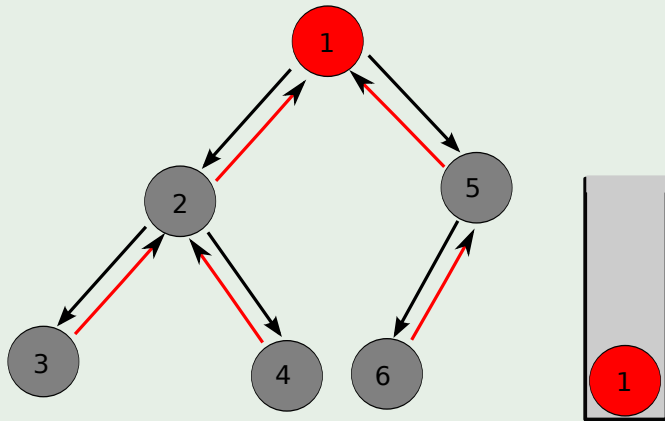
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Recursion \approx Depth First Search

Actually

This is the classic order when recursion is done!!!

What if...

We need a different order?

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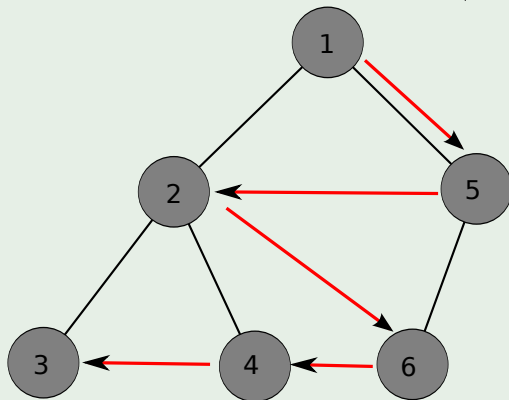
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Level Order

How?



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Queues

Definition of Queues

- A queue is an abstract data structure that models/enforces the **first-come first-serve order**, or equivalently the First-In First-Out (FIFO) order.

This

Using ADT Which is the first thing that comes to your mind to implement a queue?

IMPORTANT

- IN A QUEUE, THE FIRST ITEM INSERTED WILL BE THE FIRST ITEM DELETED: FIFO (FIRST-IN, FIRST-OUT)

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We have then

- A linear list.

Entry Points

- One end is called front.
- Other end is called rear.

Insertion and Deletions

- Additions are done at the rear only.
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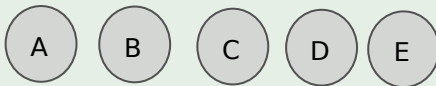
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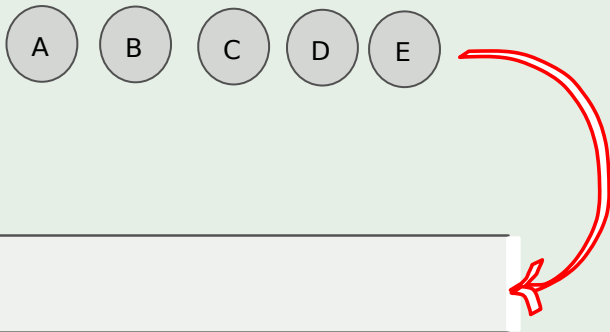
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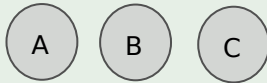
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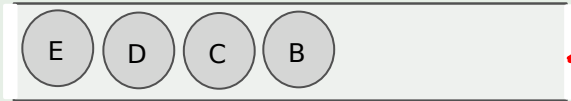
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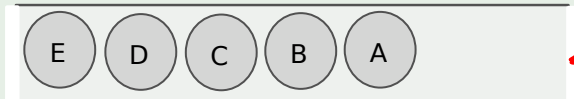
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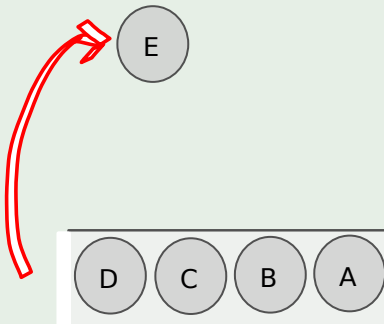
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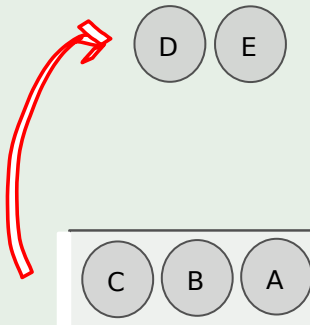
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Deque - Remove



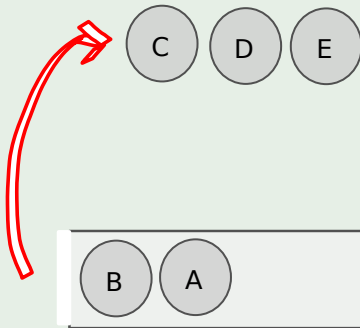
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Deque - Remove



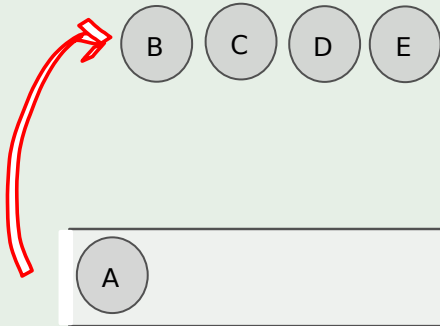
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Queue Interface

Code

```
interface Queue{  
    public boolean empty();  
    public Item front();  
    public Item rear();  
    public Item Dequeue();  
    public void Enqueue(theObject);  
    public int size();  
}
```

Explanation

```
public boolean empty()
```

- Check whether the queue is empty.
- Return TRUE if it is empty and FALSE otherwise.

Example

```
public Item front()
```

- Return the value of the item at the front of the queue without removing it.

Precondition: The queue is not empty.

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public Item rear()
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public void Enqueue(Item theObject)
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- Insert the argument item at the back of the queue.

Postcondition: The queue has a new item at the back

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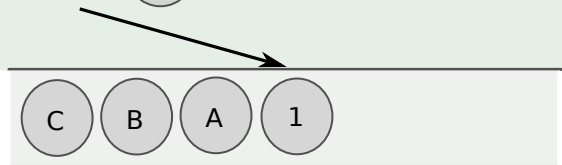
Enqueue()



Explanation

Example

Enqueue(**1**)



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public Item Dequeue()
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- Remove the item from the front of the queue.

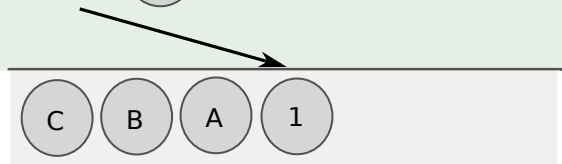
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Postcondition: The element at the front of the queue is the element that was added immediately after the element just popped or the queue is empty.

Explanation

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Enqueue()



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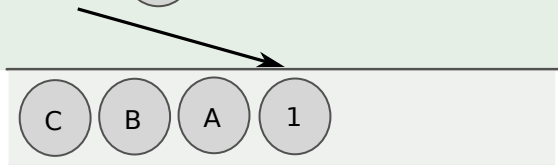
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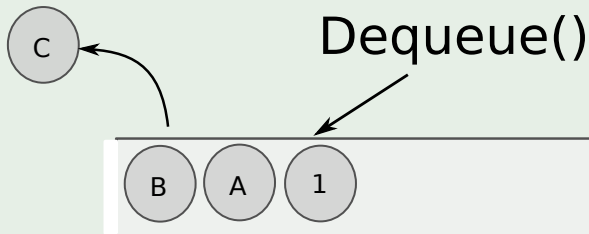
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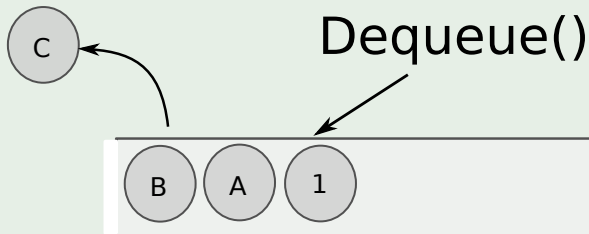


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public int size()
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It returns the size.

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Applications of Queues

Direct applications

- Waiting lists
 - ▶ Queue Theory for Networking
- Bureaucracy Access to shared resources (e.g., printer)
- Multiprogramming
 - ▶ Schedulers

Indirect applications

- Auxiliary data structure for algorithms
- Component of other data structures

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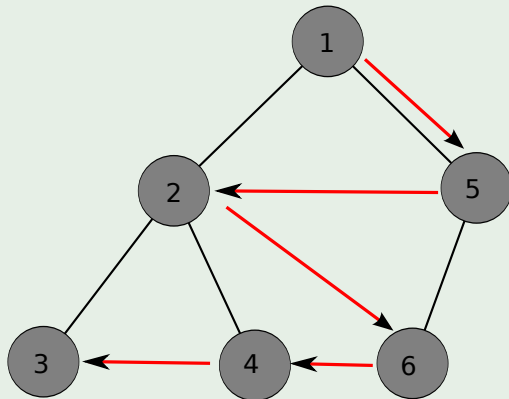
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Change the Order of Recursion

Remember



Thus, Using a Trick

and Queue

- We can change the direction of the recursion!!!
- Look at the board

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Radix Sort Using Bins

Example

Order ten 2 digit numbers in 10 bins (0-9) from least significant number to most significant number.

Digits

91,06,85,15,92,35,30,22,39

Let us do it

In the board!!!

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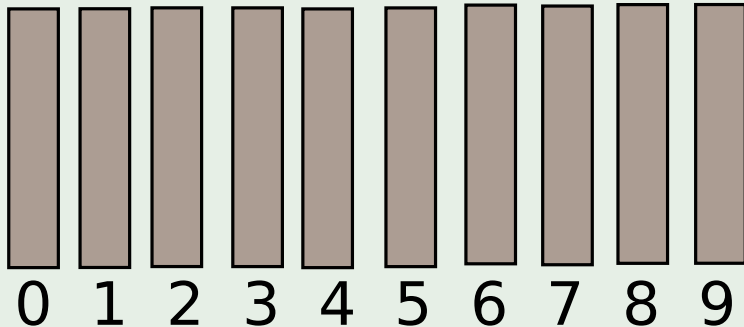
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In the board!!!

Example

Pass 0: Distribute the digits into bins according to the 1's digit (10^0).



Finally

Next

- Dequeue the values from the queue 0 to queue 9.

• Put values in a list in that order.

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Pass 1: Take the new sequence and distribute the cards into bins determined by the 10's digit (10^1)

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Radix Sort: Complexity

Lemma 1

Given n d -digit numbers in which each digit can take on up to k possible values, RADIX-SORT correctly sorts these numbers in $O(d(n+k))$ time.

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Simulating Waiting Lines

Simulation is used to study the performance

- Of a physical (“real”) system.
- By using a physical, mathematical, or computer model of the system.

Simulation allows designers to estimate performance

- Before building a system

Simulation can lead to design improvements

- Giving better expected performance of the system

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Queuing Theory

Constraints

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At each tick

- Frequent flyer (FF) passenger arrives in line
- Regular (R) passenger arrives in line
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 - ① Agent finishes, then serves next FF passenger
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Desired Output

- Statistics on waiting times, agent idle time, etc.
- Optionally, a detailed trace

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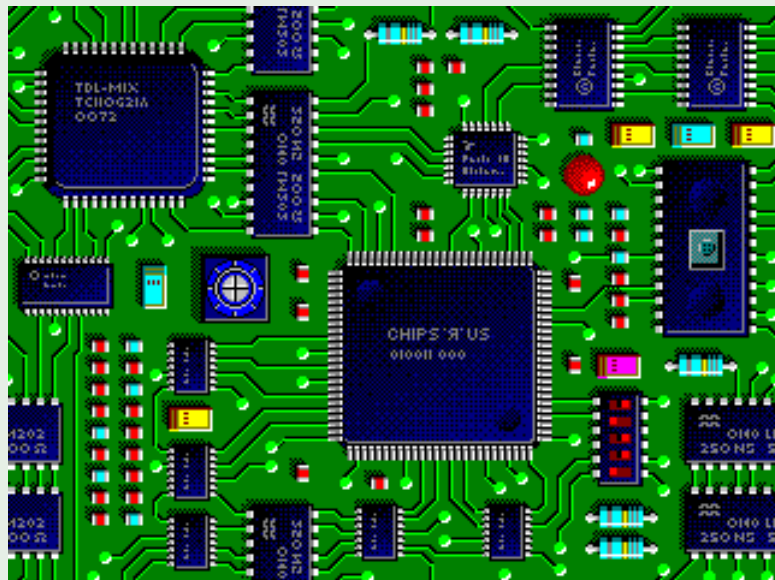
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Circuit Board

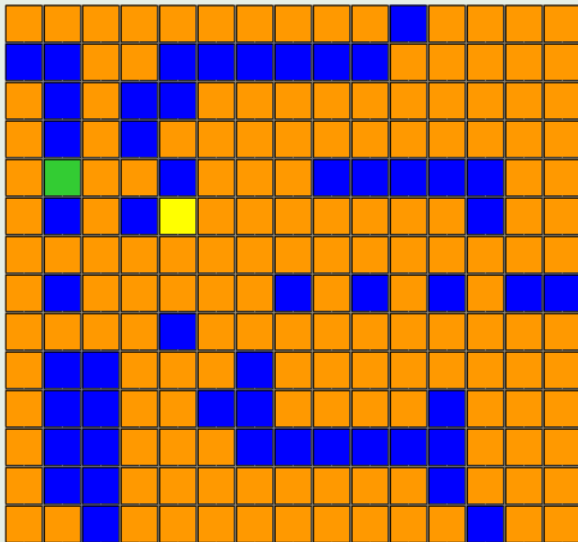


Example

Circuit Board - Label all reachable squares 1 unit from start


 start pin


 end pin

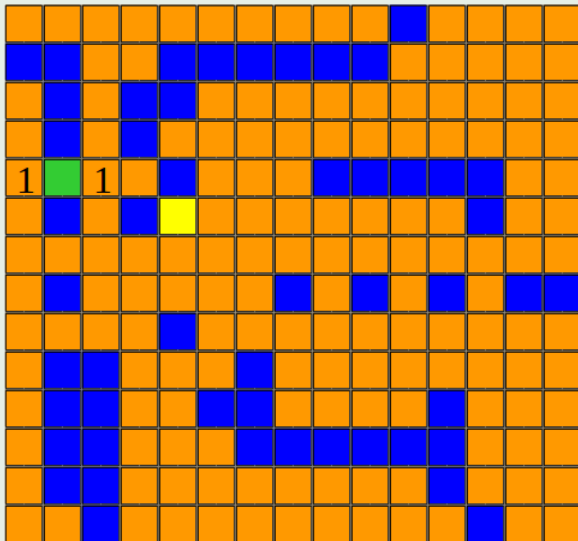


Example

Circuit Board - Label all reachable unlabeled squares 2 units from start.


 start pin


 end pin

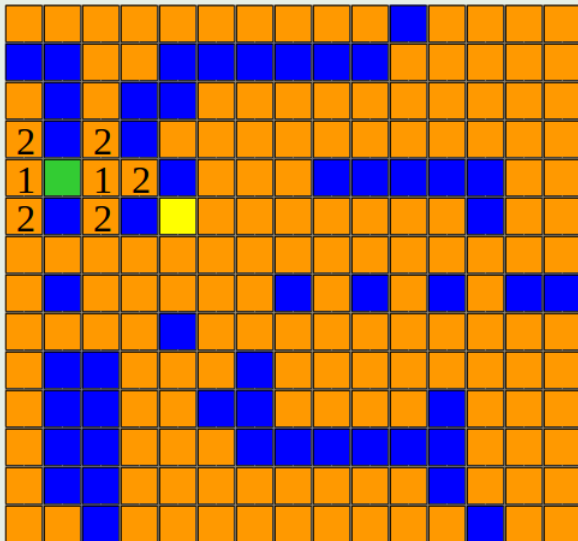


Example

Circuit Board - Label all reachable unlabeled squares 3 units from start.


 start pin


 end pin

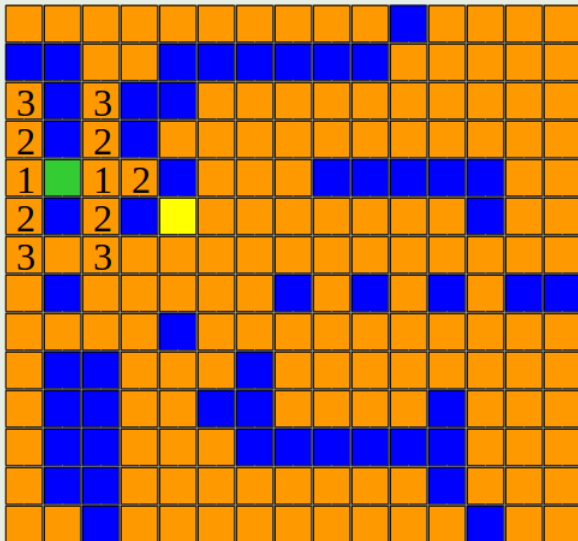


Example

Circuit Board - Label all reachable unlabeled squares 4 units from start.

 start pin

 end pin



Example

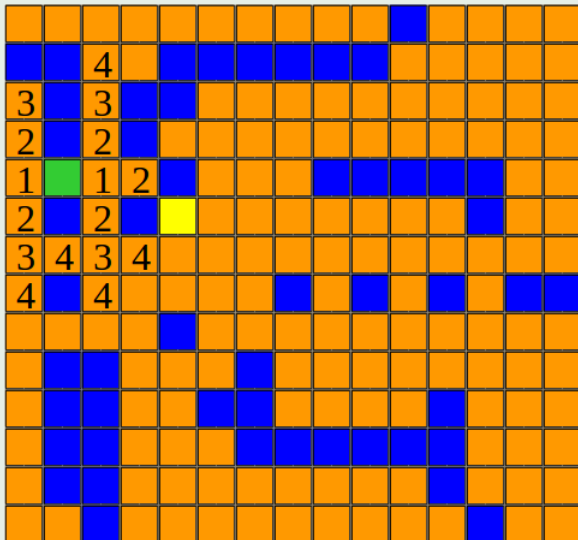
Circuit Board - Label all reachable unlabeled squares 5 units from start.



start pin



end pin



Example

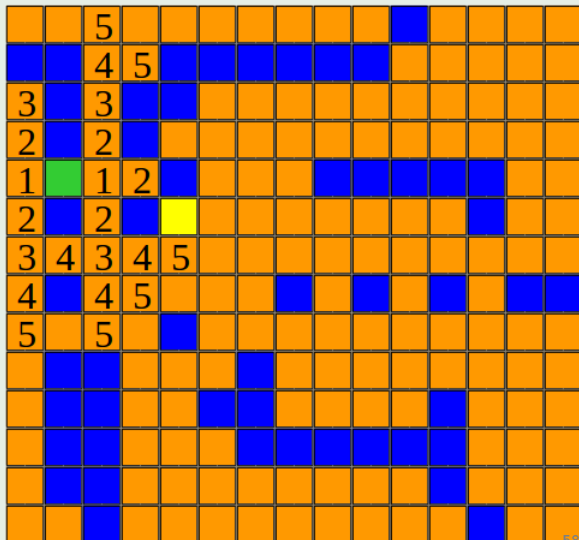
Circuit Board - Label all reachable unlabeled squares 6 units from start.



start pin





end pin

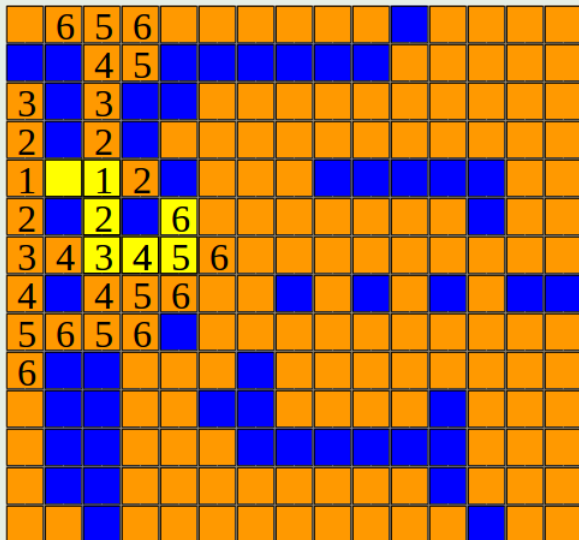


Example

Circuit Board - Traceback.

 start pin

 end pin



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Derive from ArrayLinearList

Here

We do not extend our data structure.

Simply use

Whatever is available in the base class.

Derive from ArrayLinearList

Here

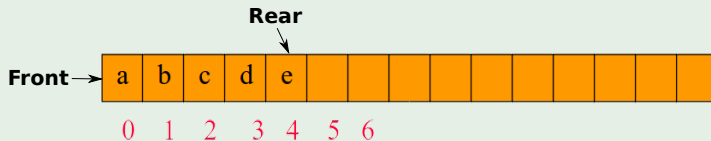
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Derive from ArrayLinearList

We have then

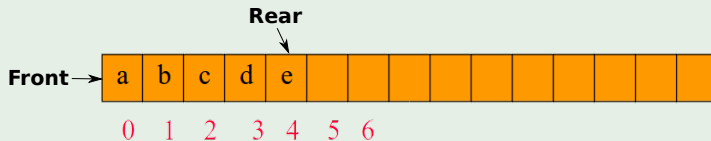


- When the front is the left end of list and the rear is the right end

Operation in Queue	Supporting method from parent class	Complexity
empty()	super.isEmpty()	$O(1)$
front()	get(0)	$O(1)$
rear()	get(size()-1)	$O(1)$
Enqueue(TheObject)	add(size(),theObject)	$O(1)$
Dequeue()	remove(0)	$O(\text{size})$

Derive from ArrayLinearList

We have then

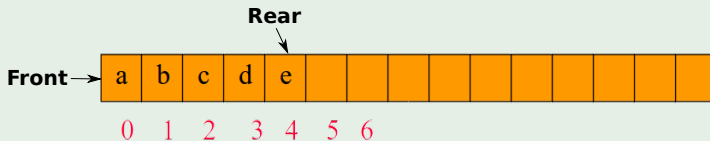


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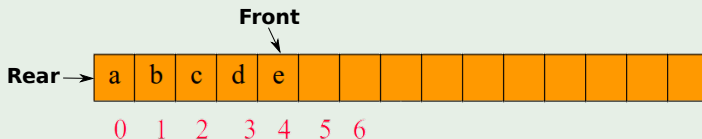


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Dequeue()	remove(0)	O(size)

Shift the front and rear pointers!!!

We have

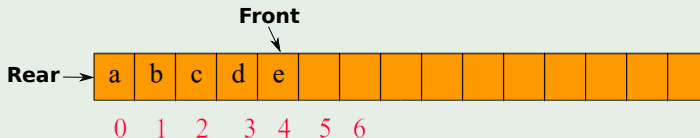


- When the rear is the left end of list and the front is the right end

Operation in Queue	Supporting method from parent class	Complexity
empty()	super.isEmpty()	O(1)
front()	get(size()-1)	O(1)
rear()	get(0)	O(1)
Enqueue(TheObject)	add(0,theObject)	O(size)
Dequeue()	remove(size()-1)	O(1)

Shift the front and rear pointers!!!

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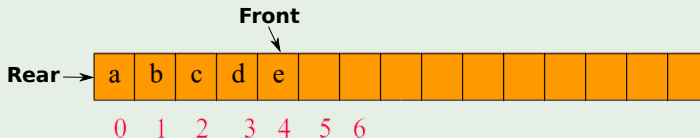


- When the **rear** is the left end of list and the **front** is the right end

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Dequeue()	remove(size()-1)	O(1)

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We have



- When the **rear** is the **left end** of list and the **front** is the **right end**

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empty()	super.isEmpty()	O(1)
front()	get(size()-1)	O(1)
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Moral of the Story

We have

to perform each operation in $O(1)$ time (excluding array doubling), we need a customized array representation.

We need to extend the data structure

We can do that using the circular idea!!!

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A Linked Implementation of a Queue

From our experience extending the Chain Class

- We use two pointer for the front and the back of the chain:
 - ▶ `firstNode ==` at the beginning of the Chain
 - ▶ `lastNode ==` the end of the Chain

This

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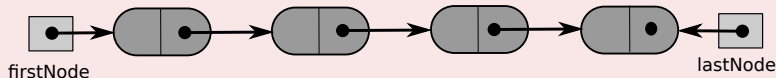
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A Linked Implementation of a Queue

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Some Operations: Enqueue

We have always two cases

➊ Adding to an empty Queue

➋ Adding to a non-empty Queue

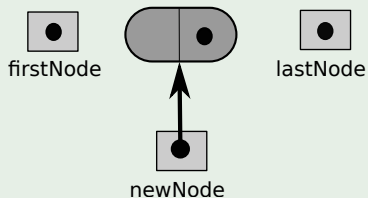
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Example: Adding to an Empty List

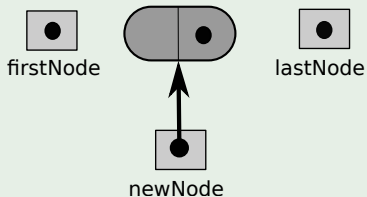
Before Inserting



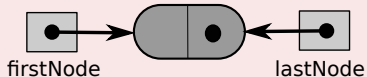
After Inserting

Example: Adding to an Empty List

Before Inserting

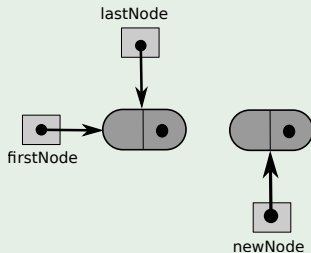


After Inserting



Example: Adding to a Non-Empty List

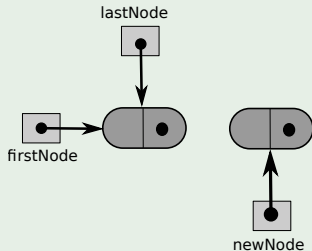
Create New Node



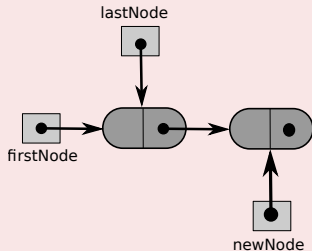
Make next from lastNode...

Example: Adding to a Non-Empty List

Create New Node

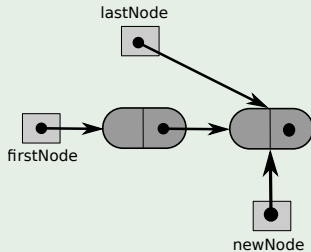


Make next from lastNode...



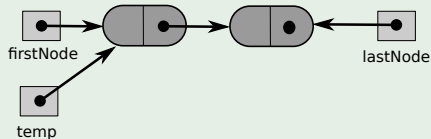
Example: Adding to a Non-Empty List

Move lastNode



What about Dequeue?

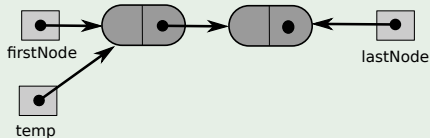
Point a temporary node to the front node



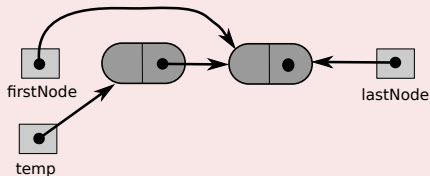
Point firstNode to temp.next

What about Dequeue?

Point a temporary node to the front node

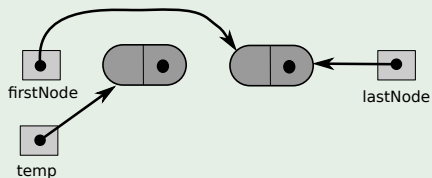


Point firstNode to temp.next



Empty

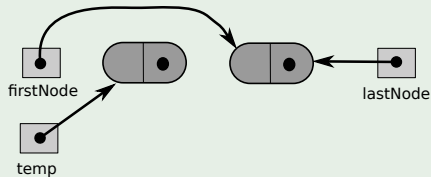
Make temp.next = null



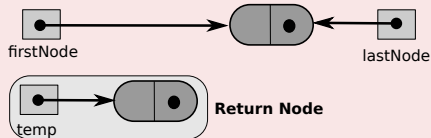
Return Node

Empty

Make temp.next = null



Return Node



Thus...

The Rest of Operations

You can think about them... they are not complex...

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The Rest of Operations

You can think about them... they are not complex...

Complexities

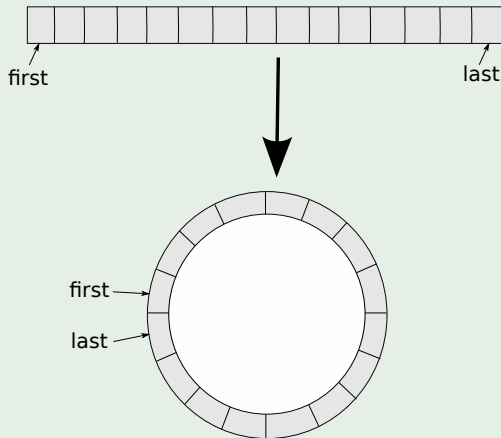
Operation in Scratch Queue using Chains	Complexity
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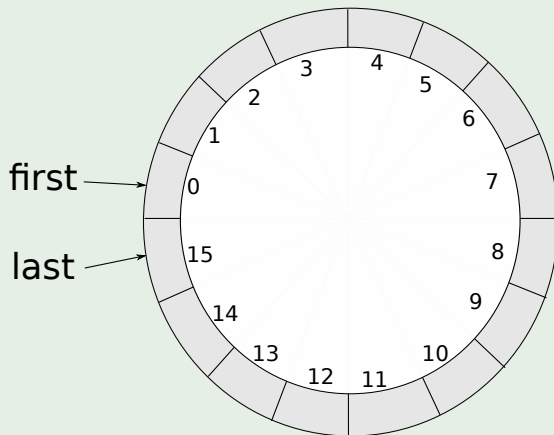
From Scratch Using an Array!!!

If we can do the following...



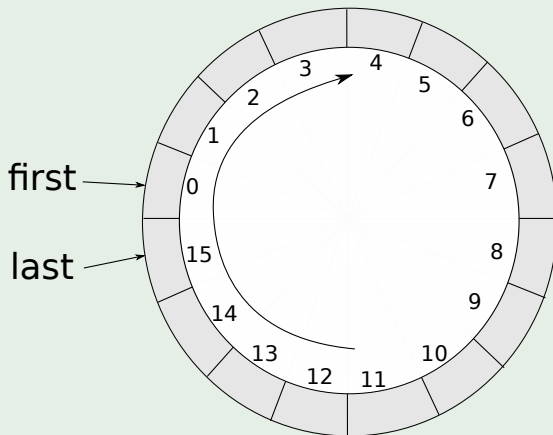
A closer Look...

Somebody can notice something?



Direction of Reading

Repeating numbers in a certain range



How we can simulate this number repetition?

Actually there is function that can help

$$\text{mod } m : \mathbb{N} \rightarrow \{0, 1, 2, \dots, m-1\} \quad (1)$$

Example for $m = 5$

n	$n \bmod m$
0	0
1	1
2	2
3	3
4	4
5	0
6	1
7	2
8	3
etc...	...

How we can simulate this number repetition?

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etc...	...

Thus, we still we have two indexes

frontIndex

We need to know where to remove!!!

backIndex

We need to know where to add!!

Thus, we still we have two indexes

frontIndex

We need to know where to remove!!!

backIndex

We need to know where to add!!

Thus

If we want to add

```
backIndex = (backIndex + 1)% queue.length
```

If we want to remove

```
frontIndex = (frontIndex + 1)% queue.length
```

Thus

If we want to add

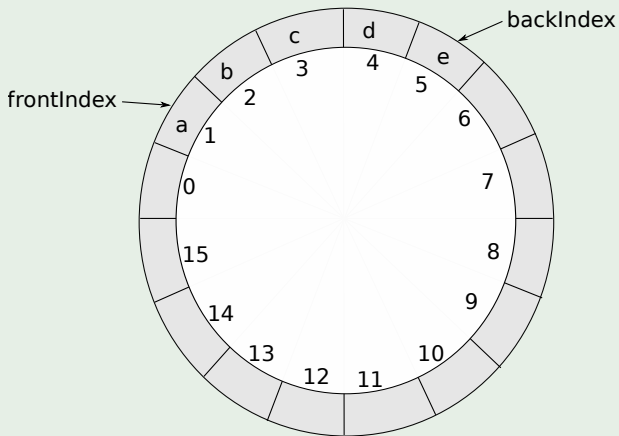
$$\text{backIndex} = (\text{backIndex} + 1) \% \text{queue.length}$$

If we want to remove

$$\text{frontIndex} = (\text{frontIndex} + 1) \% \text{queue.length}$$

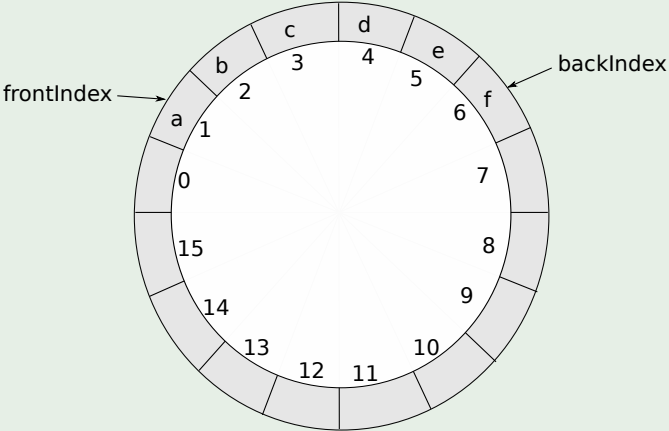
Example

Adding stuff into the back



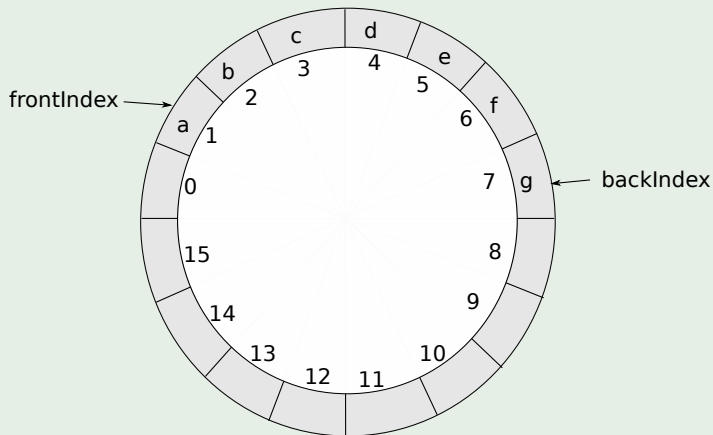
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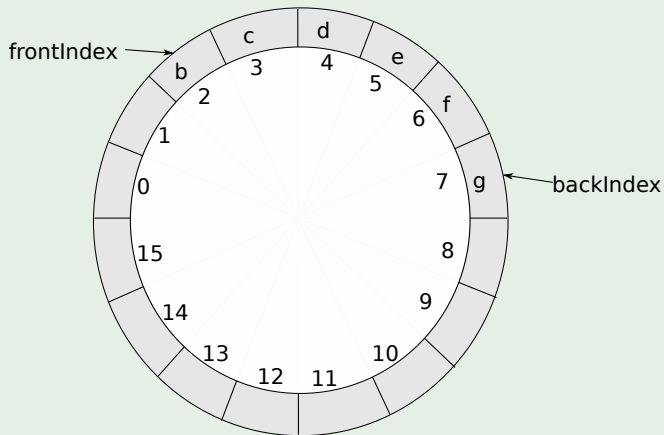
Example

Adding stuff into the back



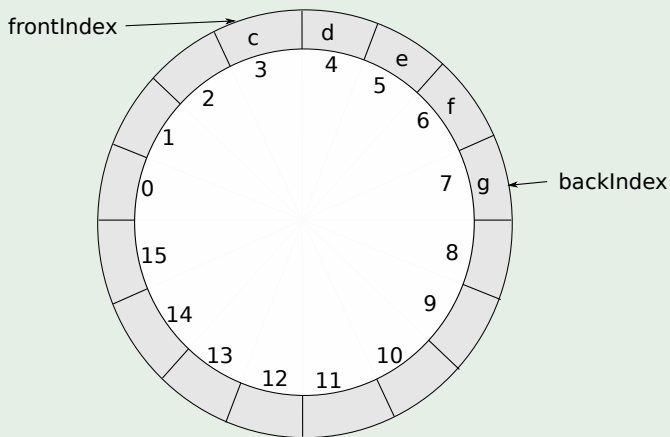
Example

Remove stuff from the front



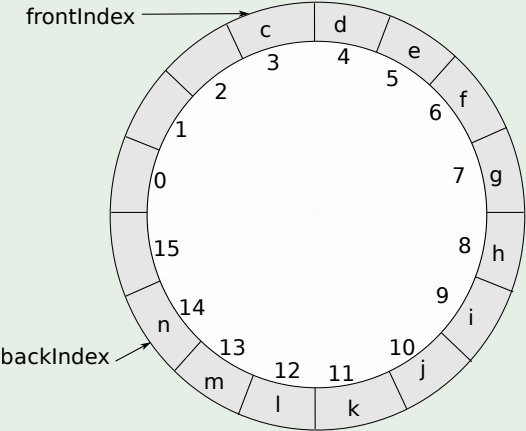
Example

Remove stuff from the front



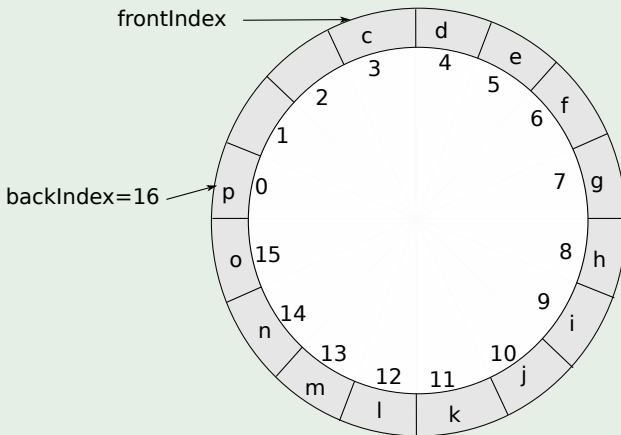
Example

Keep Adding



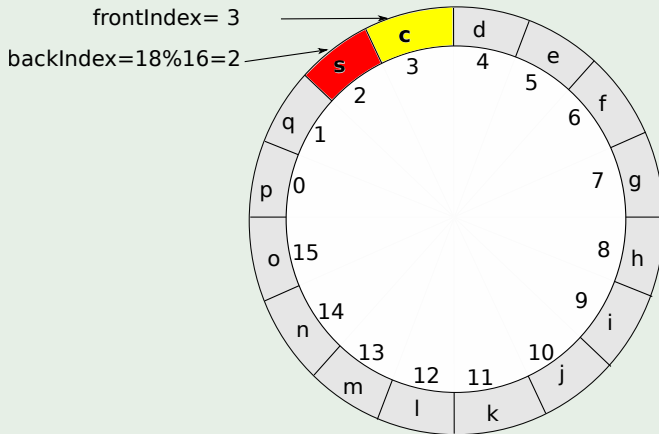
Example

The modulo helps here



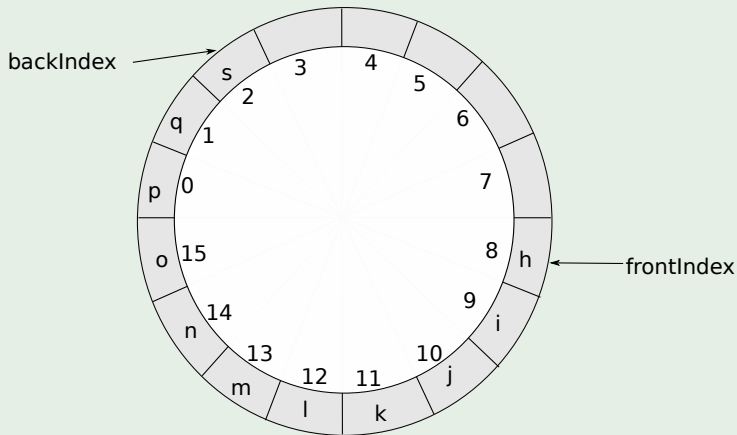
It looks Cool, but...

Problem 1 when full



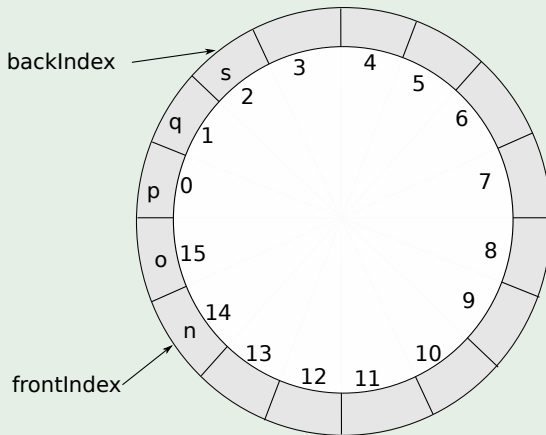
But when we remove all elements

We go...



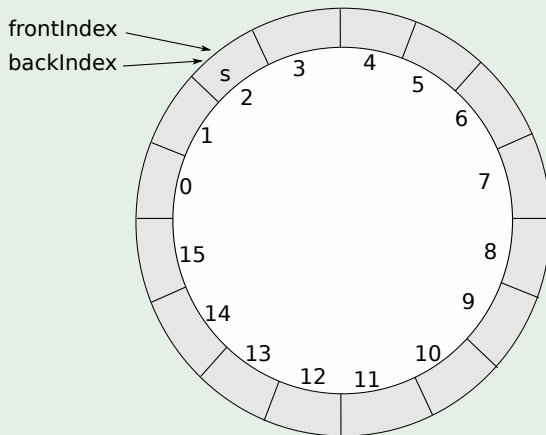
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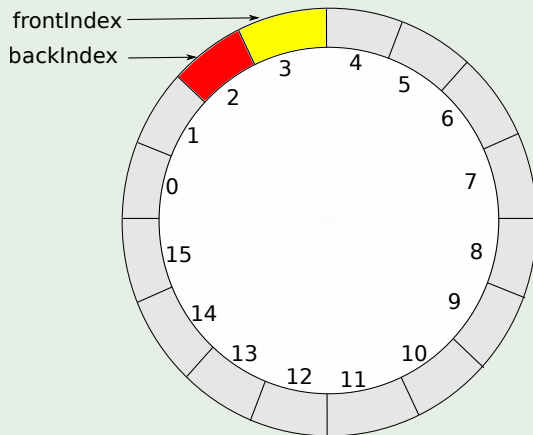
This is the main problem

And here is the problem when removing s



This is the main problem

Then full an empty cases cannot be identified!!!



Thus

The Problem

```
frontIndex == (backIndex + 1) % queue.length
```

A possible solution

Somewhat simple

- Use an extra field “size”

A possible solution

Somewhat simple

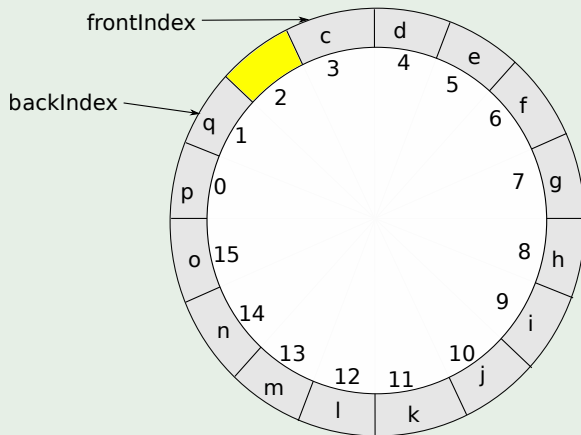
- Use an extra field “size”

Then each time

- If $\text{frontIndex} == (\text{backIndex} + 1) \% \text{queue.length} \Rightarrow$ check **size**
 - ▶ Then do something what?

Another solution!!!

Assume an space between the frontIndex and backIndex



Thus,

When the queue is full

```
frontIndex == (backIndex + 2) % queue.length
```

When the queue is empty

```
frontIndex == (backIndex + 1) % queue.length
```

Thus,

When the queue is full

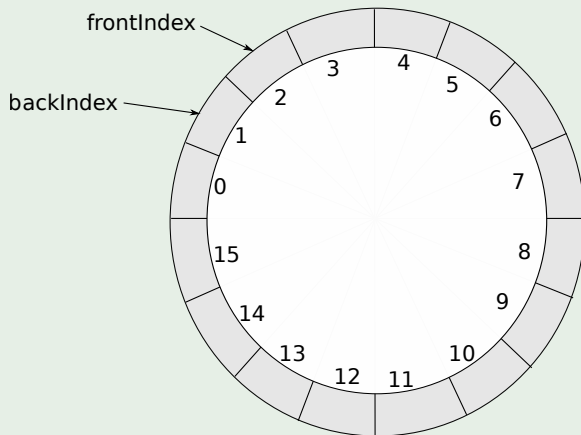
```
frontIndex == (backIndex + 2) % queue.length
```

When the queue is empty

```
frontIndex == (backIndex + 1) % queue.length
```

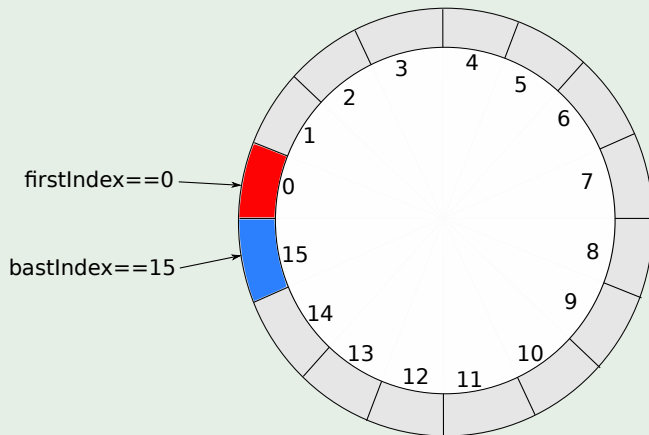
A solution!!!

Then for an empty queue



At the Beginning

At the Instantiation of the Object Queue



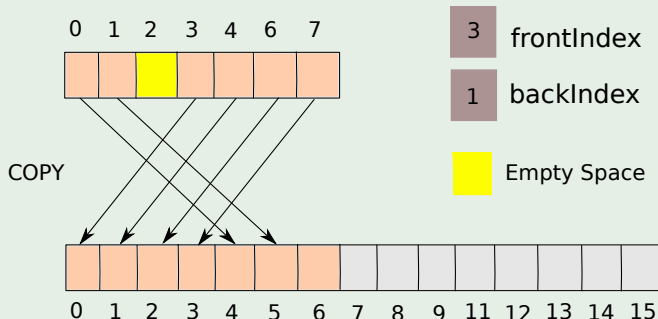
Enqueue in a circular array

Code

```
def enqueue(newEntry):  
  
    if (frontIndex == ((backIndex + 2) % queue.length))  
        <Something Here....>  
  
    backIndex = (backIndex + 1) % queue.length;  
    queue[backIndex] = newEntry;
```

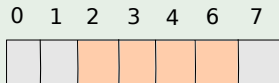
What is this “Something Here”?

Expanding Array and Copying values



Deque

At the beginning

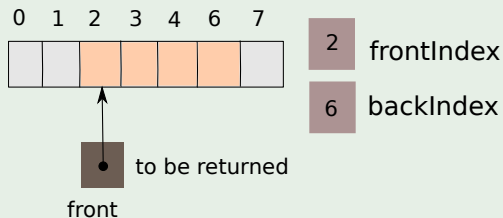


2 frontIndex

6 backIndex

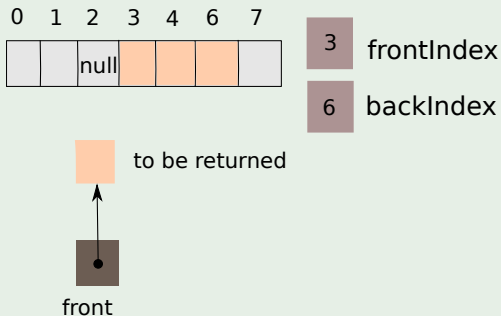
Deque

Use a temporary pointer "front"



Deque

Remove the element



Enqueue in a circular array

Code

```
public Item dequeue()
{
    Item front = null;
    if (!empty())
    {
        front = queue[frontIndex];
        queue[frontIndex] = null;
        frontIndex = (frontIndex + 1) % queue.length;
    } // End If
    return front;
} // end dequeue
```

Thus...

The Rest of Operations

You can think about them... they are not so complex...

Complexities

Operation in Scratch Queue using Chains	Complexity
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