Modeling latent changes in COVID-19 transmission over time

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Overview

The current *Georgia stochostic model* of COVID-19 tranmission incorporates a metric of human movement ($\phi(t)$) that moderates the baseline tranmission rate (β): $\beta(t) = \phi(t)\beta$. This formulation is meant to represent the impact of social distancing. Social distancing, while powerful, is not the only practice that can reduce transmission. Other practices, such as wearing face coverings, maintaining social distance in public spaces, and enhanced cleaning practices, can also reduce transmission. These practices are difficult to quantify in data and, in turn, are difficult to model explicitly. Nonetheless, we expect that mobility data will become less informative of transmission over time and that other practices will play a larger role.

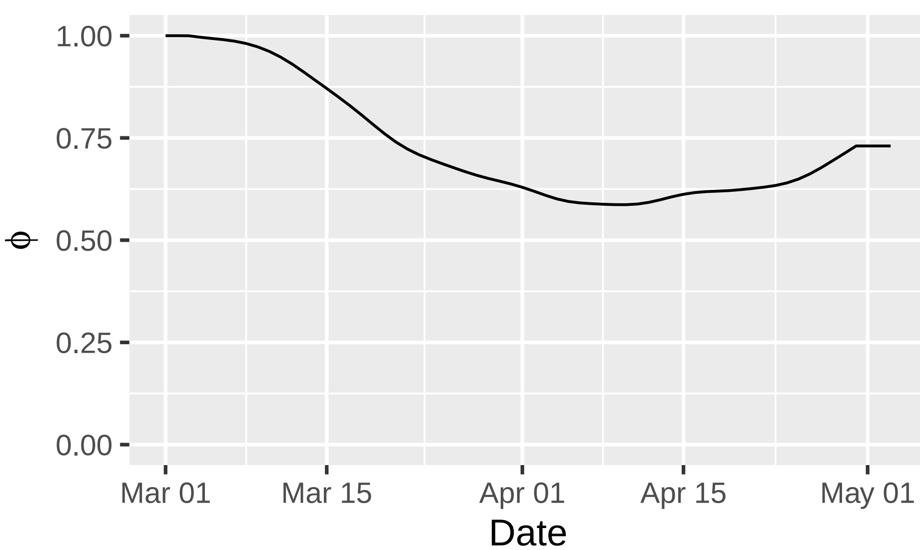
I used a basis function approach (spline modeling) to model a latent temporal process that mediates baseline tranmission rate. The idea is to include a smooth temporal function in the model that stands in for all unobserved processes that can reduce transmission.

Implementation

We currently model the force of infection (f) at time t as:

$$f(t) = \phi(t)\frac{\beta}{N}(I(t)),$$

where, for simplicity, I stands for all infectious individuals at time t. The mobility index ϕ looks like this:

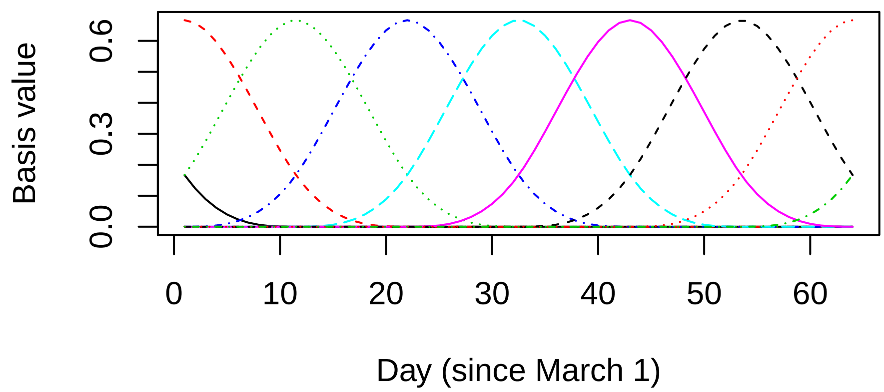


I proposed to add a temporal basis function to incorporate additional tranmission reduction over time that we cannot observe. Let the new temporal term be ψ, which is modeled as:

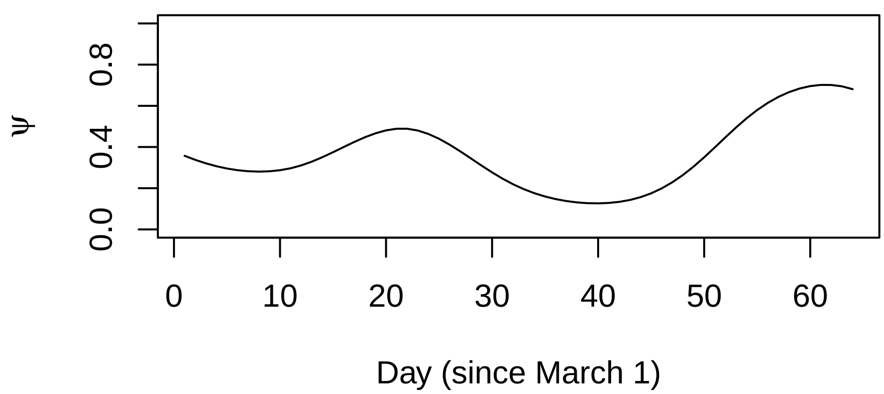
$$\text{logit}\,(\psi(t)) = \sum_{i=1}^{K} q_i \xi_{i_t},$$

where K is the number of knots, $\mathbf{q}$ is a vector of spline coefficients (to be fitted), and ξ is a matrix basis functions. I define the number of knots (K) as the number of days in the data set divided by 7 (so, one knot per week). Note the logit transformation to go from the linear scale to the 0 - 1 scale. Thus, $f(t)$ becomes: $f(t) = \psi(t)\phi(t)\frac{\beta}{N}(I(t))$.

Assuming $K = 9$, the basis functions are:



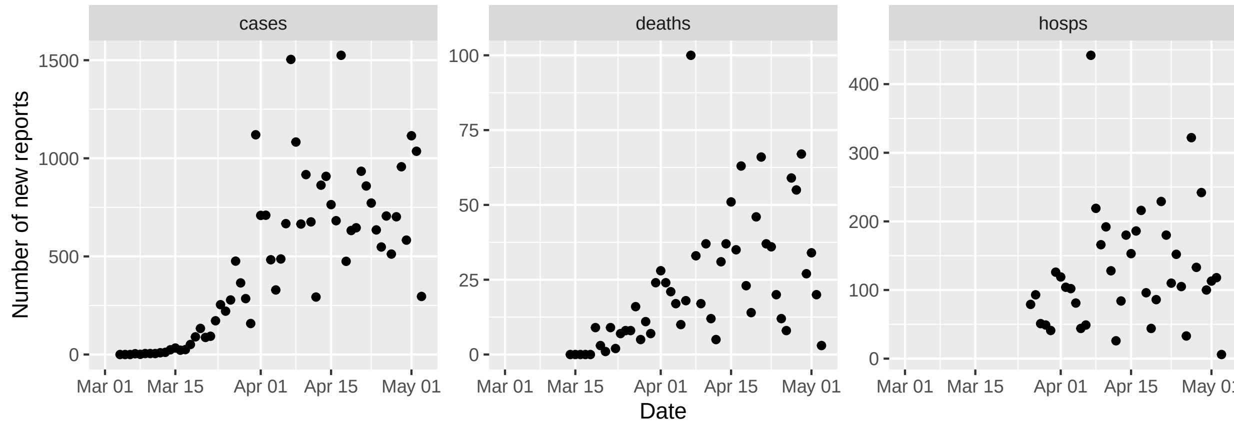
Assuming a vector of $\mathbf{q}$ values drawn from a normal distribution with mean 0 and unit variance, the resulting function can look like this:



Using MIF, we actually fit the $\mathbf{q}$ values to find the best ψ trend.

Results

I fit two models to data through May 3, 2020, one model with the new basis function and one without. Here are the data:



The fitted spline coefficients produce a trend over time, which I plot with the mobility trend and their combined influence on tranmission. Recall that "phi" is the mobility metric and "psi" is the latent metric produced by the spline fit.