

## 1 No PEC backing

The computed zeros for the structure with no PEC backing as shown in 1 are obtained through Halley's method performed on the denominator expression:

$$\mathcal{D} = 1 - \overleftarrow{\Gamma}_2 \overrightarrow{\Gamma}_2 e^{-2jk_z d_1} \quad (1)$$

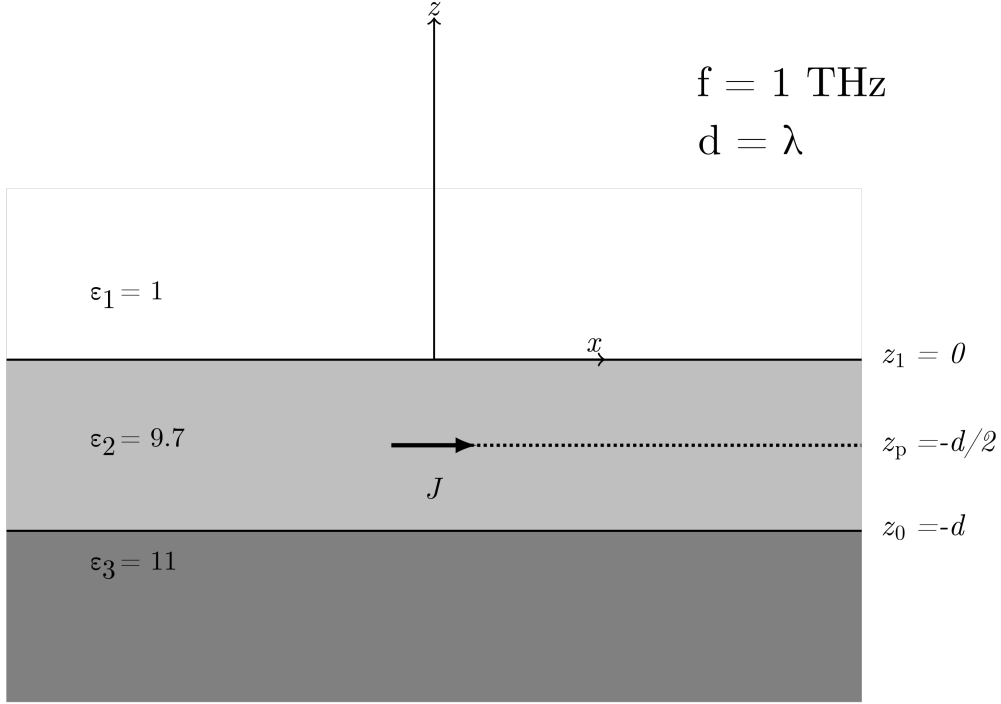


Figure 1: Structure with no PEC base

where  $d_1 = z_1 - z_0$  and  $\overleftarrow{\Gamma}_2$  and  $\overrightarrow{\Gamma}_2$  are the left and right looking reflection coefficients from the middle layer:

$$\overleftarrow{\Gamma}_2 = \frac{Z_3 - Z_2}{Z_3 + Z_2} \quad (2a)$$

$$\overrightarrow{\Gamma}_2 = \frac{Z_1 - Z_2}{Z_1 + Z_2} \quad (2b)$$

An evaluation of  $\mathcal{D}$  as in (1) computed zeros is shown in Fig. 2.

## 2 PEC backing

With PEC backing as shown in 3:

$\overleftarrow{\Gamma}_2$  now becomes:

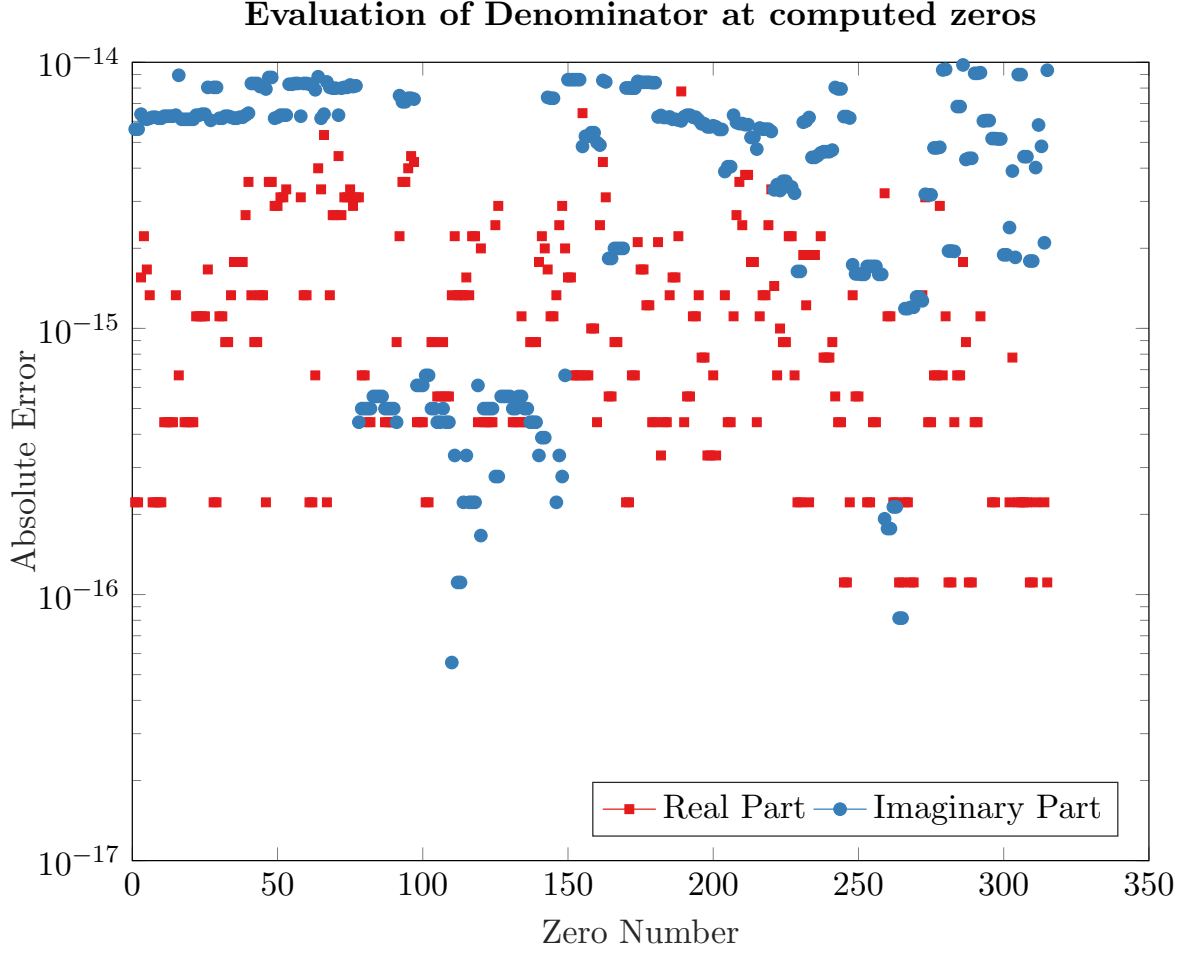


Figure 2: Evaluation of (1) at computed zeros

$$\overleftarrow{\Gamma}_2 = \frac{\Gamma_{3,2} - \exp(-4jk_{z3}d)}{1 - \Gamma_{3,2}\exp(-4jk_{z3}d)} \quad (3)$$

where  $\Gamma_{3,2}$  is:

$$\Gamma_{3,2} = \frac{Z_3 - Z_2}{Z_3 + Z_2} \quad (4)$$

The evaluation of  $\mathcal{D}$  with a PEC base is shown in Fig. 4.

A comparison of zeros of two cases in the complex  $k_\rho$ -plane is illustrated in Fig. 5

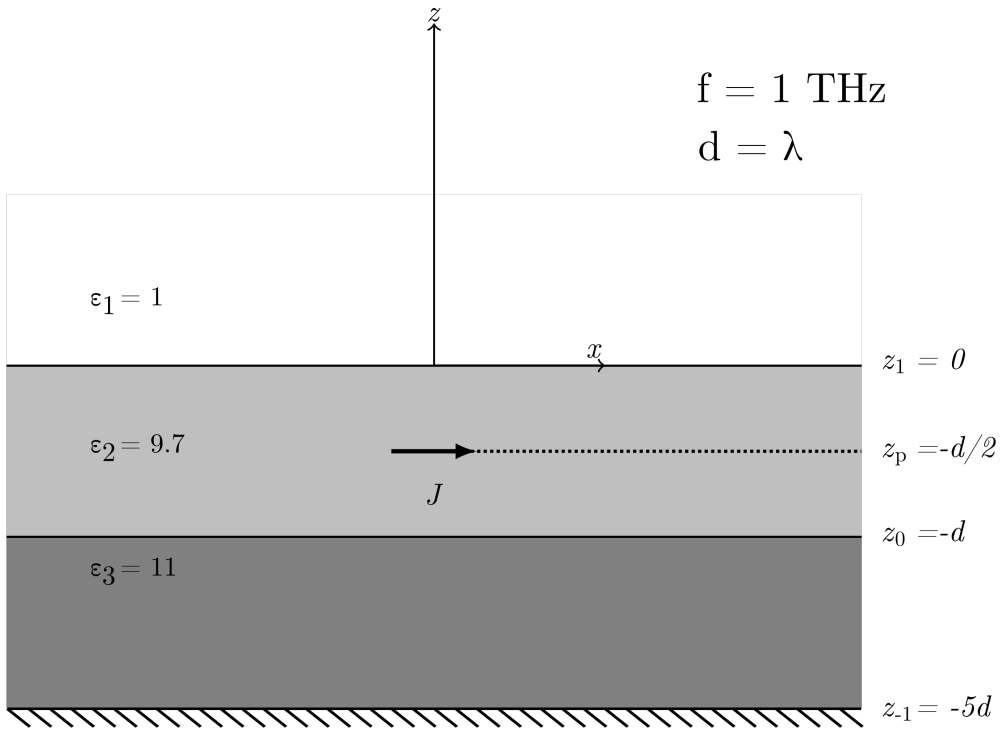


Figure 3: Structure with PEC base

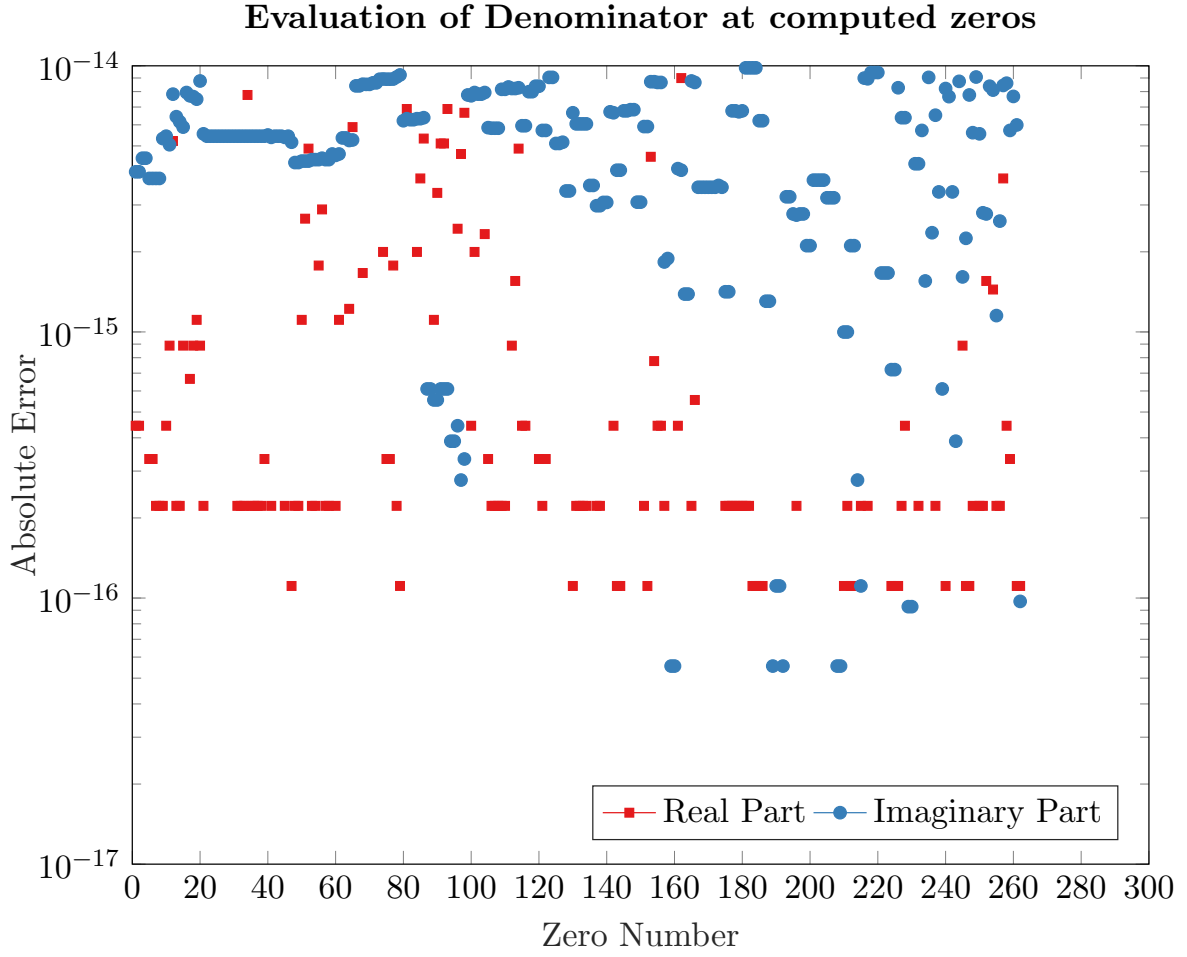


Figure 4: Evaluation of (1) at computed zeros with PEC

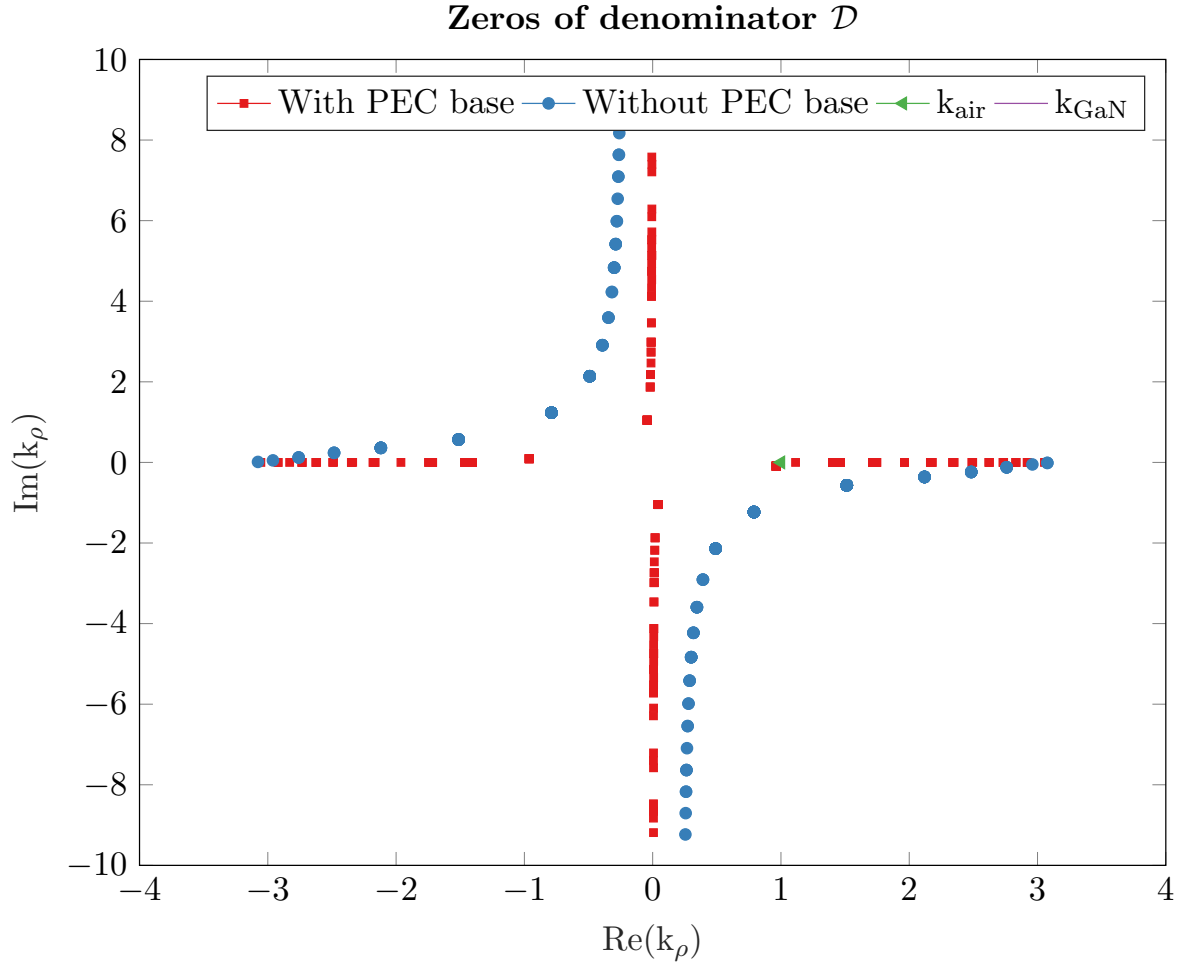


Figure 5: Zeros in the complex plane