

Lab 5: Sea-Level Rise

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1 Load packages

```
1 using CSV
2 using DataFrames
3 using DataFramesMeta
4 using Distributions
5 using Plots
6 using StatsPlots
7 using Unitful
8
9 Plots.default(; margin=5Plots.mm)
```

1.1 Local package

```
1 using Revise
2 using HouseElevation
```

2 Building object

The information from previous labs is integrated in a `Building` object with the following parameters:

Area 33 000 ft²

Offset from gauge 6 ft

Valuation 5'445 000 USD (*Structure + Contents*)

Offset (measure from gauge) 6 ft

```
1 offset = 6
2 building = let
3     haz_fl_dept = CSV.read("data/haz_fl_dept.csv", DataFrame)
4     desc = "Average Light Industrial, Contents (Equipment/Inventory)"
5     row = @rsubset(haz_fl_dept, :Description == desc)[1,:]
6     area = 33000u"ft^2"
7     height_above_gauge = (offset)u"ft"
8     House(
9         row;
```

```

10     area = area,
11     height_above_gauge = height_above_gauge,
12     value_usd = 5_445_000,
13 )
14 end

```

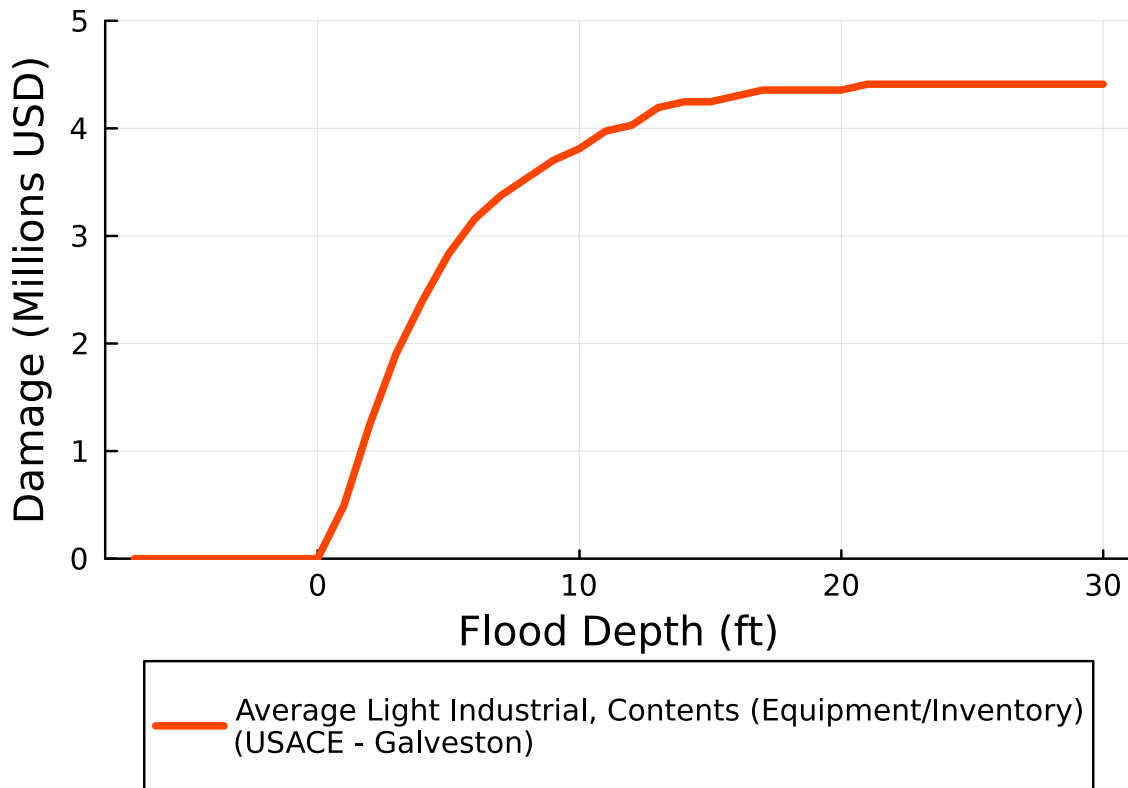
2.1 Building Depth-Damage function

The following Depth-Damage function (DDF) is use from the USACI-Galveston data for light industrial buildings

```

1  let
2      depths = uconvert.(u"ft", (-7.0u"ft"):(1.0u"inch"):(30.0u"ft"))
3      damages = building.ddf.(depths) ./ 100
4      damages_1e6_usd = damages .* building.value_usd ./ 1e6
5      plot(
6          depths,
7          damages_1e6_usd;
8          xlabel = "Flood Depth",
9          ylabel = "Damage (Millions USD)",
10         ylims = [0, trunc(maximum(damages_1e6_usd)) + 1],
11         label = "$(building.description)\n$(building.source)",
12         legend = :outerbottom,
13         size = (500, 400),
14         yformatter=:plain, # prevents scientific notation
15         color = "orangered",
16         linewidth = 3,
17     )
18 end

```



2.2 Building Elevation cost function

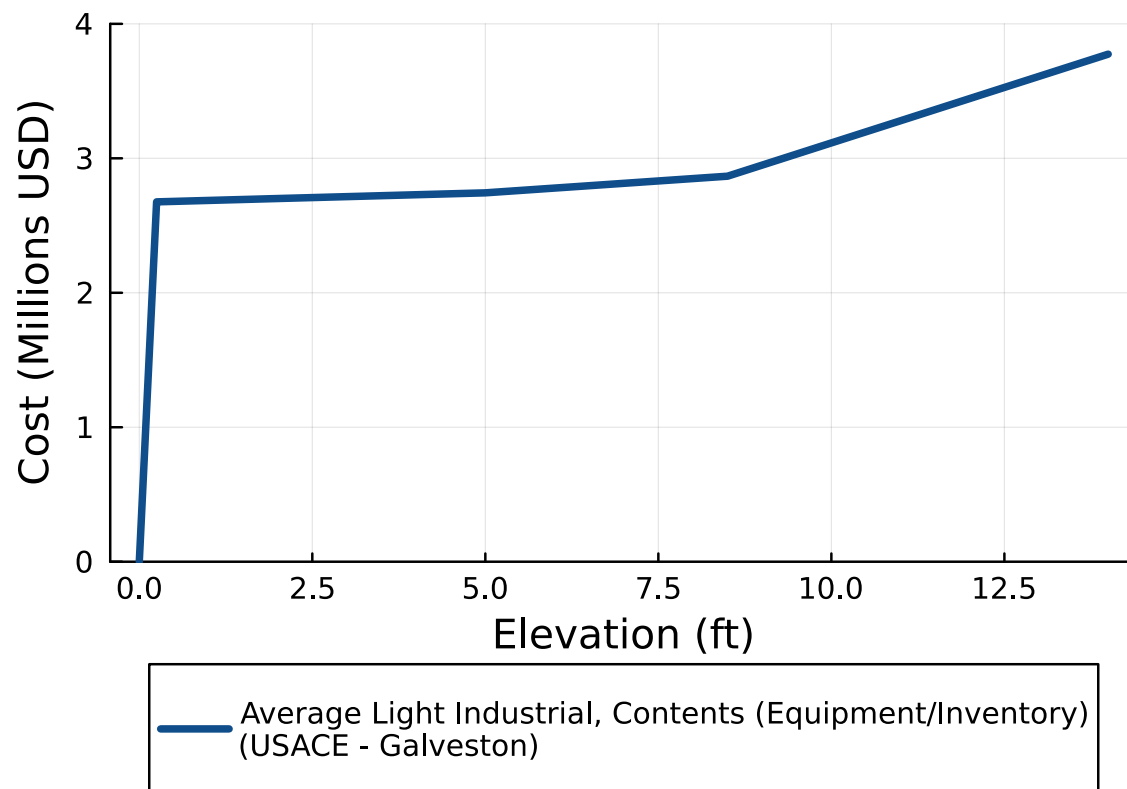
The elevation costs considered are the following for every elevation:

```

1  let
2      elevations = 0u"ft":0.25u"ft":14u"ft"
3      costs = [elevation_cost(building, e) for e in elevations]
4      plot(
5          elevations,
6          costs ./ 1e6;
7          xlabel="Elevation",
8          ylabel="Cost (Millions USD)",
9          ylims = [0, trunc(maximum(costs ./ 1e6)) + 1],
10         label="$ (building.description) \n $ (building.source)",
11         legend=:outerbottom,
12         size=(500, 400),
13         yformatter=:plain, # prevents scientific notation
14         color = "dodgerblue4",
15         linewidth = 3,
16     )

```

17 end



2.3 Sea-level rise model

The Sea-level rise (SLR) is adapted from Oddo et al. (2017)

```
1 slr_scenarios = let
2   df = CSV.read("data/slr_oddo.csv", DataFrame)
3   [Oddo17SLR(a, b, c, tstar, cstar) for (a, b, c, tstar, cstar) in eachrow(df)]
4 end
5 println("There are $(length(slr_scenarios)) parameter sets")
```

There are 34895 parameter sets

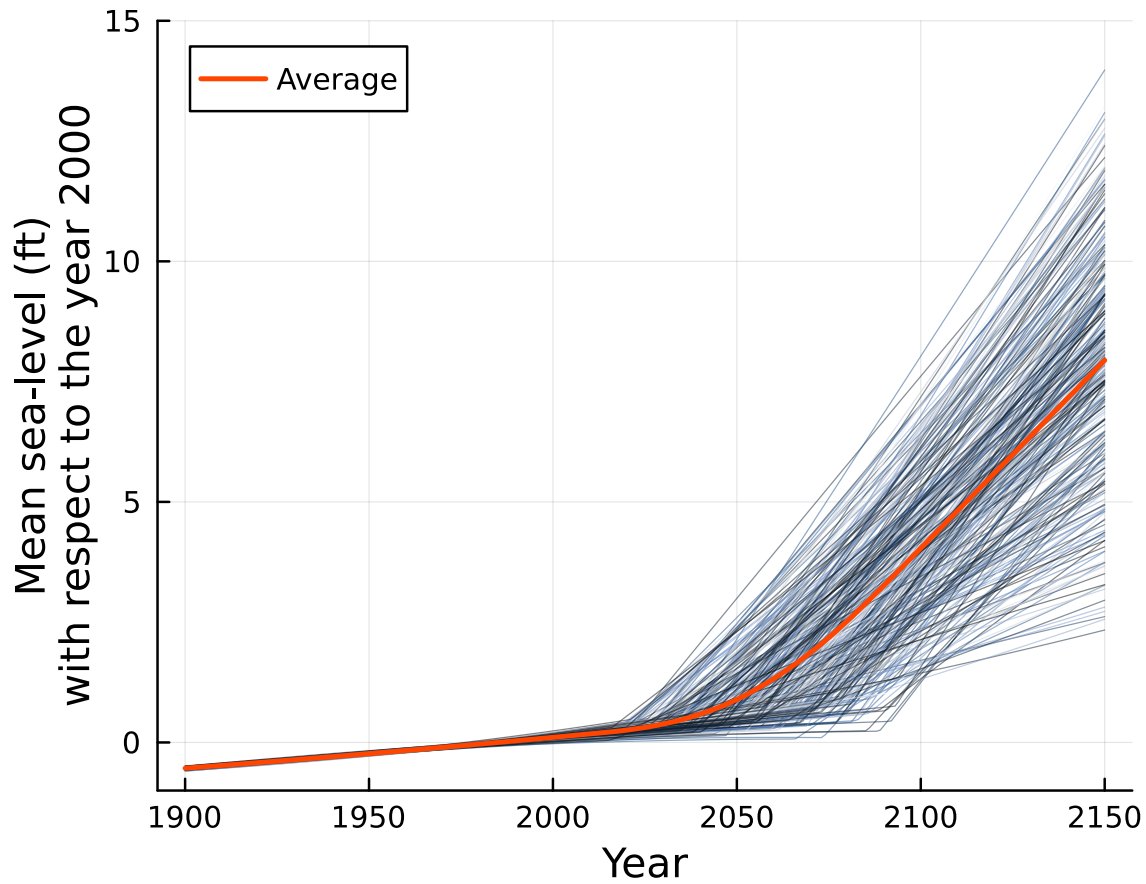
The following are 300 random samples (realizations) using the model. The average trend of these simulations is also included.

```
1 let
2   years = 1900:2150
3   p = plot(;
4     xlabel = "Year",
```

```

5         ylabel = "Mean sea-level (ft)\nwith respect to the year 2000",
6         label = "Oddo et al. (2017)",
7         legend = :topleft,
8         size=(500, 400),)
9     s_average = years.*0
10    for s in rand(slr_scenarios,300)
11        plot!(p,
12            years,
13            s.(years);
14            palette = :oslo,
15            alpha = 0.5,
16            linewidth = 0.5,
17            label = nothing,
18            )
19        s_average += s.(years)
20    end
21    s_average /= 300
22    plot!(years,
23        s_average;
24        ylims = [-1,15],
25        color = "orangered",
26        label = "Average",
27        linewidth = 2,
28        )
29    p
30 end

```



2.4 Storm surge hazard model

A General Extreme Value (GEV) distribution for the gauge is selected to represent the flood hazard, that is, the flood depth intensity probability. The following are the distribution parameters (, and) that can be randomly sampled from normal distributions around average values. The plot shows 100 random realizations and the based distribution for the gauge and for the building (subtracting the offset height).

```

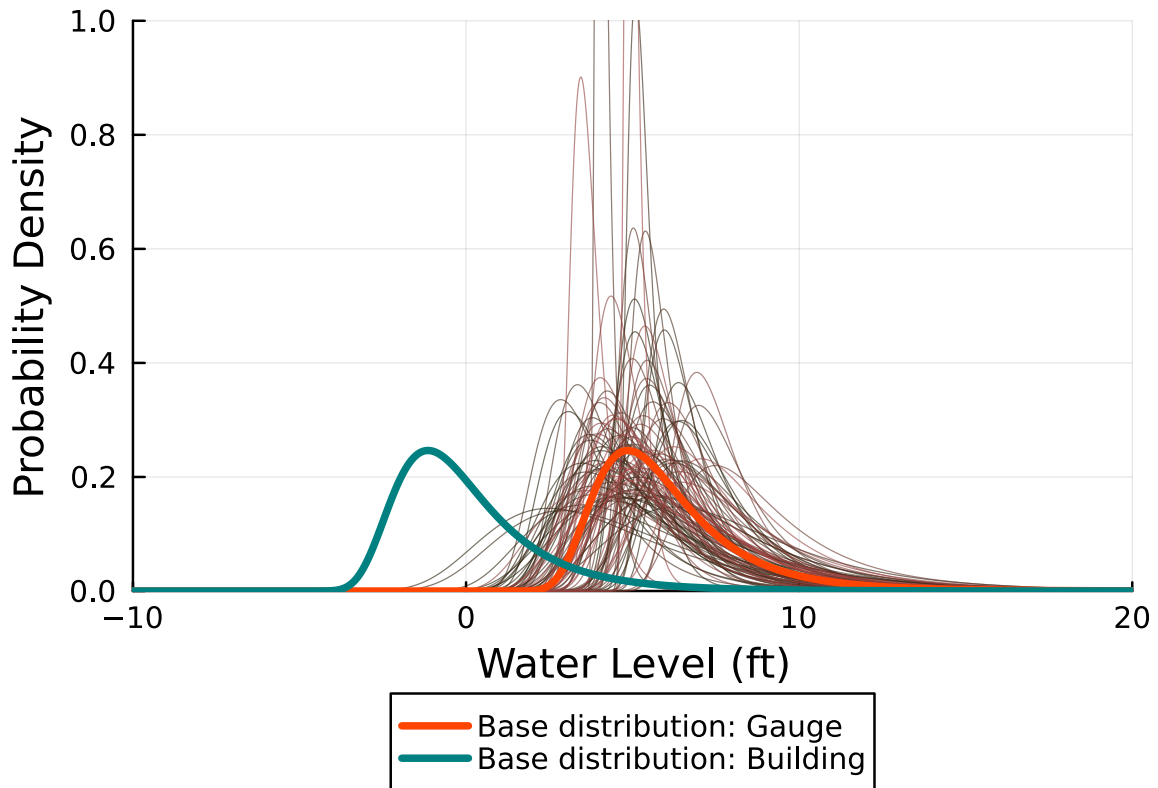
1 function draw_surge_distribution()
2     = rand(Normal(5, 1))
3     = rand(truncated(Normal(1.5,0.5),0,Inf))
4     = rand(Normal(0.1, 0.05))
5     GeneralizedExtremeValue( , , )
6 end
7 let
8     p = plot(;
9         xlabel = "Water Level (ft)",
10        ylabel = "Probability Density",
11        xlims = [-10,20],
12        ylims = [0,1],

```

```

13     size=(500, 400),
14 )
15 plot!(p,
16     [draw_surge_distribution() for _ in 1:100];
17     palette = :lajolla,
18     linewidth = 0.5,
19     alpha = 0.6,
20     label = nothing,
21 )
22 plot!(p,
23     GeneralizedExtremeValue(5, 1.5, 0.1);
24     color = "orangered",
25     linewidth = 3,
26     label = "Base distribution: Gauge",
27     legend = :outerbottom,
28 )
29 plot!(p,
30     GeneralizedExtremeValue(5-offset, 1.5, 0.1);
31     color = "Teal",
32     linewidth = 3,
33     label = "Base distribution: Building",
34     legend = :outerbottom,
35 )
36 end

```



2.5 Discount rate

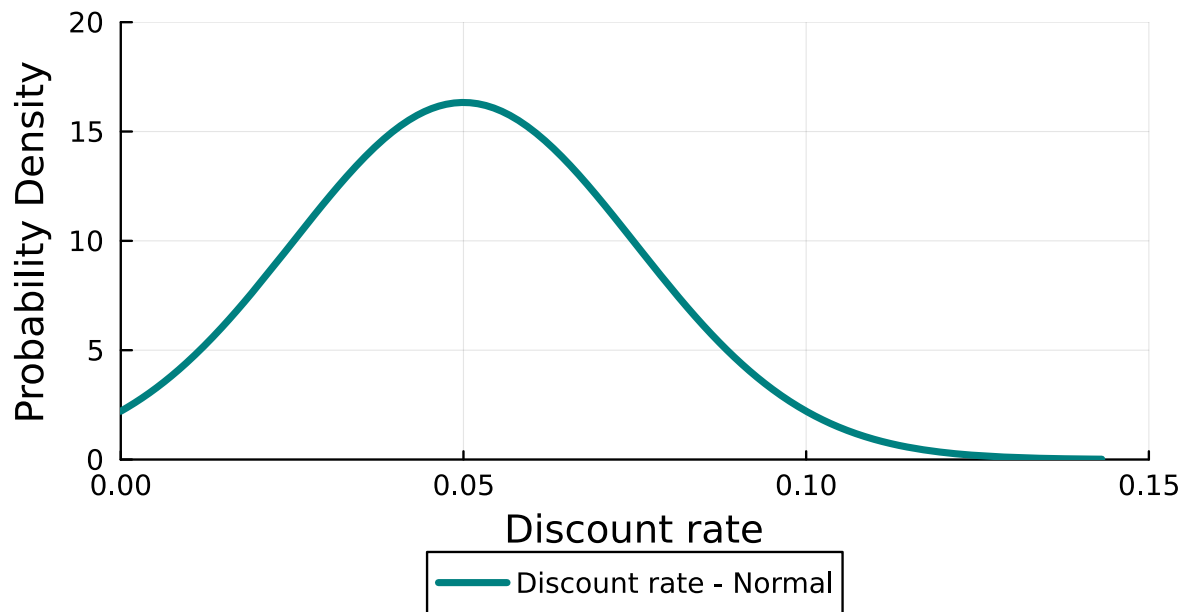
The discount rate is generated following normal distributions with a mean value of 5%. This higher value could be appropriate for industrial stakeholders (even larger) considering that their cost of opportunity can be higher than those for house holders.

```

1 function draw_discount_rate()
2     return rand(truncated(Normal(0.05, 0.025),0,Inf))
3 end
4 let
5     p = plot(truncated(Normal(0.05, 0.025),0,Inf);
6             xlabel = "Discount rate",
7             ylabel = "Probability Density",
8             ylims = [0,20],
9             xlims = [0,0.15],
10            color = "teal",
11            linewidth = 3,
12            label = "Discount rate - Normal",
13            legend = :outerbottom,
14            )

```


15 end



2.6 Simulations

The following is an example simulation considering a 50-year time window and random realizations of the hazard distribution, discount rate and SLR model. The action is elevating the building by 3 ft.

```
1 let
2   p = ModelParams(
3     house = building,
4     years = 2024:2034
5   )
6
7   sow = SOW(
8     rand(slr_scenarios),
9     draw_surge_distribution(),
10    draw_discount_rate()
11  )
12
13  a = Action(3.0u"ft")
14
15  res = run_sim(a, sow, p)/1e6
16
17  print("The NPV cost for the action a = 3 ft and a realization of the SOW is \n $(round(res
```

18 end

The NPV cost for the action $a = 3$ ft and a realization of the SOW is
-2.77 USD Millions

2.7 Exploratory modeling

The actions correspond to incremental elevation heights: Actions $a : [0: 1: 14]$ ft

There is no elevation cost above 14 ft and would be more than one-story elevation. For each action, 100 SOWs are going to be considered to form the “*large ensemble*”. Inside the functions, there are 10000 Monte Carlo Sampling realizations.

```
1 df = let
2   action_scheme = 0:1:14
3   time_frame = [25,50,100]
4   realizations = 100
5   simulations = 0
6   for t in 1:size(time_frame)[1]
7     for e in 1:size(action_scheme)[1]
8       p = ModelParams(
9         house = building,
10        years = 2024:(2024 + time_frame[t])
11      )
12
13      sows = [SOW(rand(slr_scenarios),
14        draw_surge_distribution(),
15        draw_discount_rate())
16        for _ in 1:realizations]
17
18      actions = [Action((action_scheme[e])u"ft") for _ in 1:realizations]
19
20      results = [run_sim(a, s, p) for (a, s) in zip(actions, sows)]
21
22      if t == 1 && e == 1
23        simulations = DataFrame(
24          npv = results,
25          Δh_ft = [a.Δh_ft for a in actions],
26          slr_a = [s.slr.a for s in sows],
27          slr_b = [s.slr.b for s in sows],
28          slr_c = [s.slr.c for s in sows],
29          slr_tstar = [s.slr.tstar for s in sows],
30          slr_cstar = [s.slr.cstar for s in sows],
31          surge_ = [s.surge_dist. for s in sows],
32          surge_ = [s.surge_dist. for s in sows],
33          surge_ = [s.surge_dist. for s in sows],
34          discount_rate = [s.discount_rate for s in sows],
35          years_frame = time_frame[t])
36      else
```

```

37         for r_i in 1:realizations
38             push!(simulations,[results[r_i],
39                 [a.Δh_ft for a in actions][r_i],
40                 [s.slr.a for s in sows][r_i],
41                 [s.slr.b for s in sows][r_i],
42                 [s.slr.c for s in sows][r_i],
43                 [s.slr.tstar for s in sows][r_i],
44                 [s.slr.cstar for s in sows][r_i],
45                 [s.surge_dist. for s in sows][r_i],
46                 [s.surge_dist. for s in sows][r_i],
47                 [s.surge_dist. for s in sows][r_i],
48                 [s.discount_rate for s in sows][r_i],
49                 time_frame[t]])
50         end
51     end
52 end
53 end
54 simulations
55 end

```

The following are some general statistics of the resulting from the simulations:

2.8 25 year life-span

```

1 describe(df[df.years_frame .== 25,[1,3,6,7,8,9,11]])

```

	variable	mean	min	median	max	nmissing	eltype
	Symbol	Float64	Float64	Float64	Float64	Int64	DataType
1	npv	-4.69235e6	-2.9013e7	-3.62476e6	-15436.1	0	Float64
2	slr_a	32.4006	-11.4581	32.7133	75.8202	0	Float64
3	slr_tstar	2050.53	2015.02	2050.87	2103.05	0	Float64
4	slr_cstar	20.2251	-14.5416	20.499	34.9954	0	Float64
5	surge__	5.00626	1.82769	5.00637	9.25888	0	Float64
6	surge__	1.51909	0.0555552	1.51772	3.32977	0	Float64
7	discount_rate	0.0524076	0.00025258	0.0518289	0.139236	0	Float64

2.9 50 year life-span

```

1 describe(df[df.years_frame .== 50,[1,3,6,7,8,9,11]])

```

	variable	mean	min	median	max	nmissing	eltype
	Symbol	Float64	Float64	Float64	Float64	Int64	DataType
1	npv	-5.71229e6	-7.41289e7	-3.77133e6	-615265.0	0	Float64
2	slr_a	32.8267	-17.0328	33.278	66.4874	0	Float64
3	slr_tstar	2050.95	2015.02	2051.1	2101.82	0	Float64
4	slr_cstar	20.5063	-1.61623	20.9171	34.9699	0	Float64
5	surge__	4.99408	1.61044	4.98551	8.49184	0	Float64
6	surge__	1.49318	0.0739012	1.49517	3.22325	0	Float64
7	discount_rate	0.0505592	5.85605e-5	0.0492426	0.126207	0	Float64

2.10 100 year life-span

```
1 describe(df[df.years_frame .== 100,[1,3,6,7,8,9,11]])
```

	variable	mean	min	median	max	nmissing	eltype
	Symbol	Float64	Float64	Float64	Float64	Int64	DataType
1	npv	-7.59944e6	-1.72541e8	-3.79911e6	-7.92874e5	0	Float64
2	slr_a	32.7464	-1.68561	32.9757	67.375	0	Float64
3	slr_tstar	2050.69	2015.03	2050.2	2102.95	0	Float64
4	slr_cstar	20.8201	-7.37344	21.1071	34.9978	0	Float64
5	surge__	4.94174	1.70614	4.929	8.24849	0	Float64
6	surge__	1.49305	0.215862	1.47805	3.12566	0	Float64
7	discount_rate	0.0506664	0.000515111	0.0493965	0.141629	0	Float64

2.11 Multi-year NPV averages

The following are the statistics of NPV results for Actions a : [0,2,4,6,8,10,12,14] ft

```
1 let
2     df_stats = DataFrame(a0 = df.npv[(df.Δh_ft .== 0)]./1e6,
3                          a2 = df.npv[(df.Δh_ft .== 2)]./1e6,
4                          a4 = df.npv[(df.Δh_ft .== 4)]./1e6,
5                          a6 = df.npv[(df.Δh_ft .== 6)]./1e6,
6                          a8 = df.npv[(df.Δh_ft .== 8)]./1e6,
7                          a10 = df.npv[(df.Δh_ft .== 10)]./1e6,
8                          a12 = df.npv[(df.Δh_ft .== 12)]./1e6,)
9     describe(df_stats)
10 end
```

	variable	mean	min	median	max	nmissing	eltype
	Symbol	Float64	Float64	Float64	Float64	Int64	DataType
1	a0	15.4514	0.0154361	10.9463	168.654	0	Float64
2	a2	10.1668	2.70336	7.17584	172.541	0	Float64
3	a4	5.91409	2.72912	4.24558	117.935	0	Float64
4	a6	3.93333	2.7786	3.42053	19.6506	0	Float64
5	a8	3.54774	2.84932	3.19785	8.32253	0	Float64
6	a10	3.41918	3.11449	3.22788	5.92	0	Float64
7	a12	3.60853	3.44449	3.51953	5.09027	0	Float64

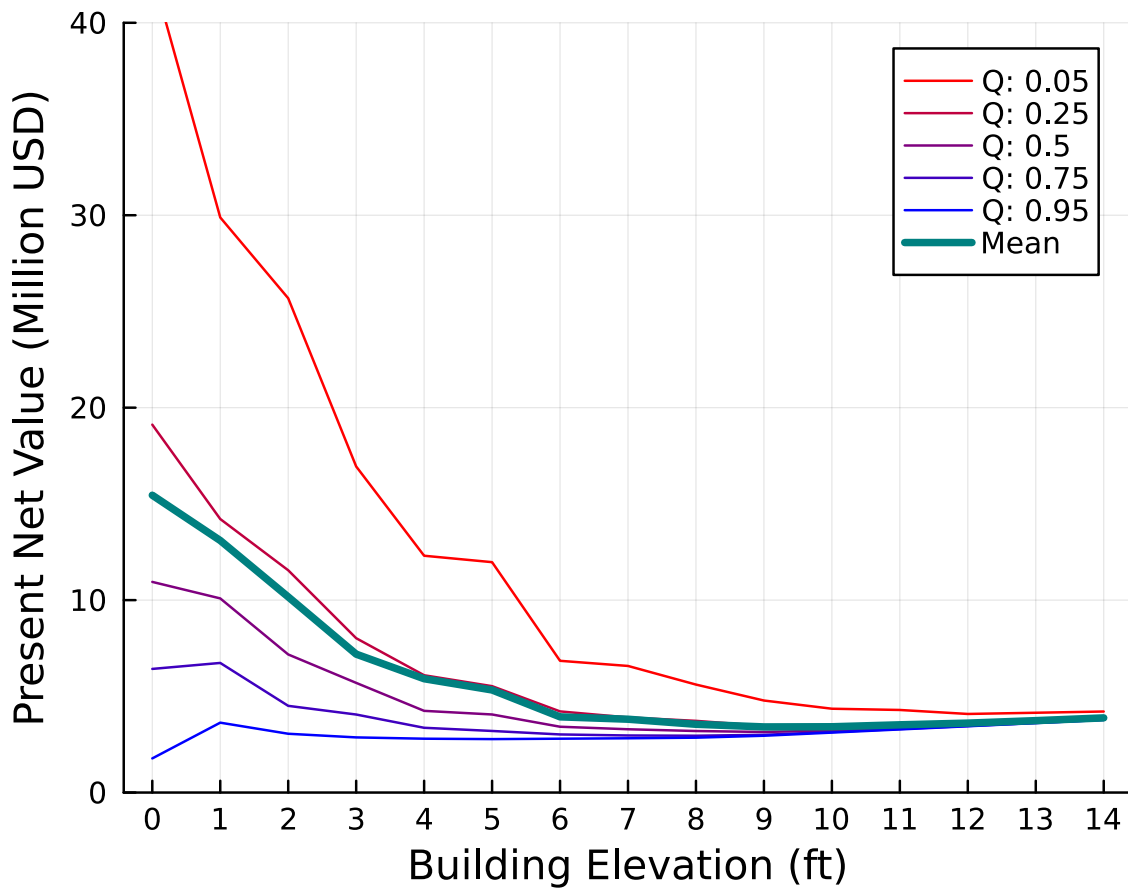
The results can also be visualized for every action and their corresponding statistics. For example,

the following is the NPV of the cost for all 25-, 50- and 100-year lifespans. It can be concluded that for the modeled SOW's the large majority shows that elevating the building led to lower NPVs.

```

1 action_scheme = 0:1:14
2 let
3   p = plot(
4     xlabel = "Building Elevation (ft)",
5     ylabel = "Present Net Value (Million USD)",
6     ylims = [0, trunc(quantile(-df.npv ./ 1e6, 0.99)) + 5],
7     xticks = 0:1:14,
8     legend = :topright,
9     size=(500, 400),)
10
11   quan = [0.05, 0.25, 0.50, 0.75, 0.95]
12   statistic = ones(size(action_scheme)[1], 1)
13   for q in 1:size(quan)[1]
14     for e in 1:size(action_scheme)[1]
15       statistic[e, 1] = quantile(df.npv[(df.Δh_ft .== action_scheme[e])], quan[q])
16     end
17
18     plot!(p,
19           action_scheme,
20           -statistic / 1e6;
21           label = "Q: $(quan[q])",
22           palette = palette([:red, :blue], 5),)
23   end
24   for e in 1:size(action_scheme)[1]
25     statistic[e, 1] = mean(df.npv[(df.Δh_ft .== action_scheme[e])])
26   end
27   plot!(p,
28         action_scheme,
29         -statistic / 1e6;
30         label = "Mean",
31         linewidth = 3,
32         color = "teal",)
33   p
34 end

```



These values can be appreciated using some boxplots for every lifespan. Some conclusions are the following: 1. The uncertainty grows with the lifespan mainly due to the SRL model that contains large uncertainties for longer timeframes. 2. From these graphs, it is also evident that the longer lifespan is considered, the NPV grows. 3. Following the 50% quantile, there is evidence of a convex behavior having a minimum at ~8 ft of elevation

```

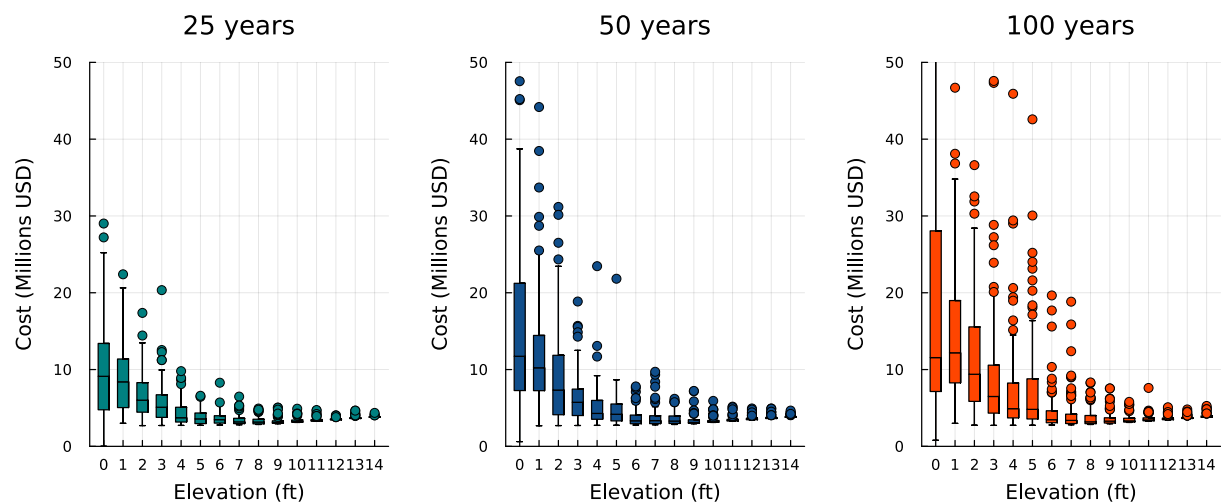
1 let
2   y25 = boxplot(
3       xlabel="Elevation (ft)",
4       ylabel="Cost (Millions USD)",
5       legend = false,
6       ylims = [0,50],
7       title = "25 years",
8       size=(1000, 400),
9   )
10  for e in 1:size(action_scheme)[1]
11  boxplot!(y25,["$ (action_scheme[e])"],
12          -df.npv[(df.Δh_ft .== action_scheme[e]).*(df.years_frame .== 25)]./1e6,
13          color = "teal",
14  )

```

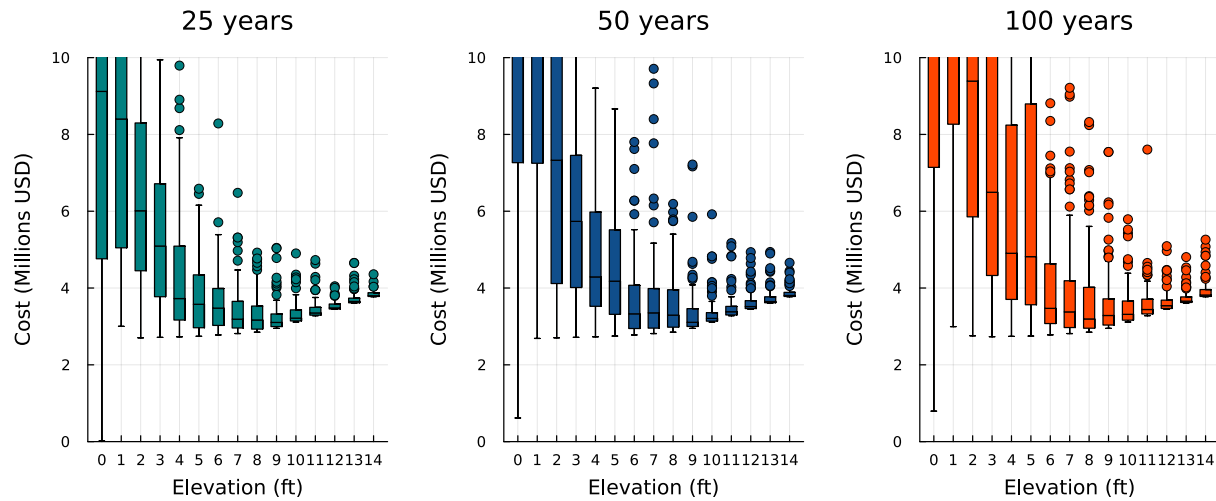
```

15 end
16 y50 = boxplot(
17     xlabel="Elevation (ft)",
18     ylabel="Cost (Millions USD)",
19     legend = false,
20     ylims = [0,50],
21     title = "50 years",
22 )
23 for e in 1:size(action_scheme)[1]
24     boxplot!(["$(action_scheme[e])"],
25         -df.npv[(df.Δh_ft .== action_scheme[e]).*(df.years_frame .== 50)]./1e6,
26         color = "dodgerblue4",
27     )
28 end
29 y100 = boxplot(
30     xlabel="Elevation (ft)",
31     ylabel="Cost (Millions USD)",
32     legend = false,
33     ylims = [0,50],
34     title = "100 years",
35 )
36 for e in 1:size(action_scheme)[1]
37     boxplot!(["$(action_scheme[e])"],
38         -df.npv[(df.Δh_ft .== action_scheme[e]).*(df.years_frame .== 100)]./1e6,
39         color = "orangered",
40     )
41 end
42 p = plot(y25,y50,y100, layout = (1,3))
43 end

```



Detail



Considering that the highest variability correspond to the action of 0 ft elevation, some analysis can be done to understand the source of these uncertainty and the parameters for which variation the model is more sensible.

2.12 Discount rate

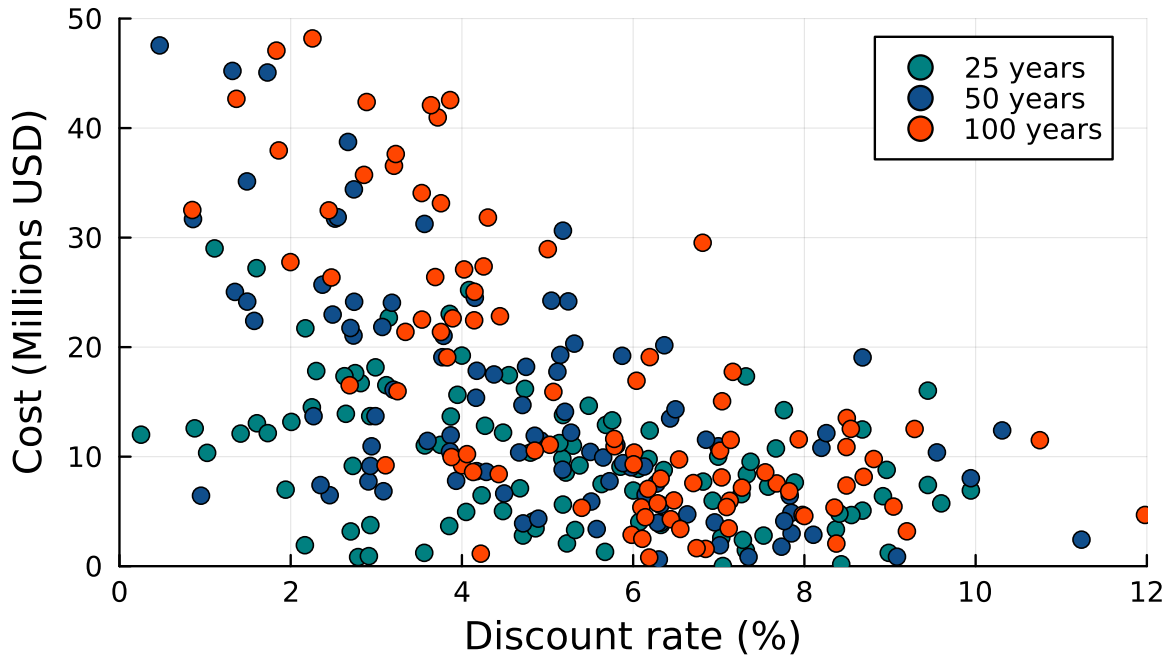
The discount rate for every analyzed lifespan has a negative trend where the NPV decreases as the DR grows.

```

1 let
2     s = scatter(
3         xlabel="Discount rate (%)",
4         ylabel="Cost (Millions USD)",
5         ylims = [0,50],
6         xlims = [0,12],
7         title = "No elevation policy",)
8     years = [25,50,100]
9     colors = ["teal","dodgerblue4","orangered"]
10    for y in 1:3
11        scatter!(s,100 .* df.discount_rate[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])],
12                -df.npv[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])]/ 1e6;
13                label = "$ (years[y]) years",
14                color = colors[y],
15                )
16    end
17    s
18 end

```


No elevation policy



2.13 Flood frequency

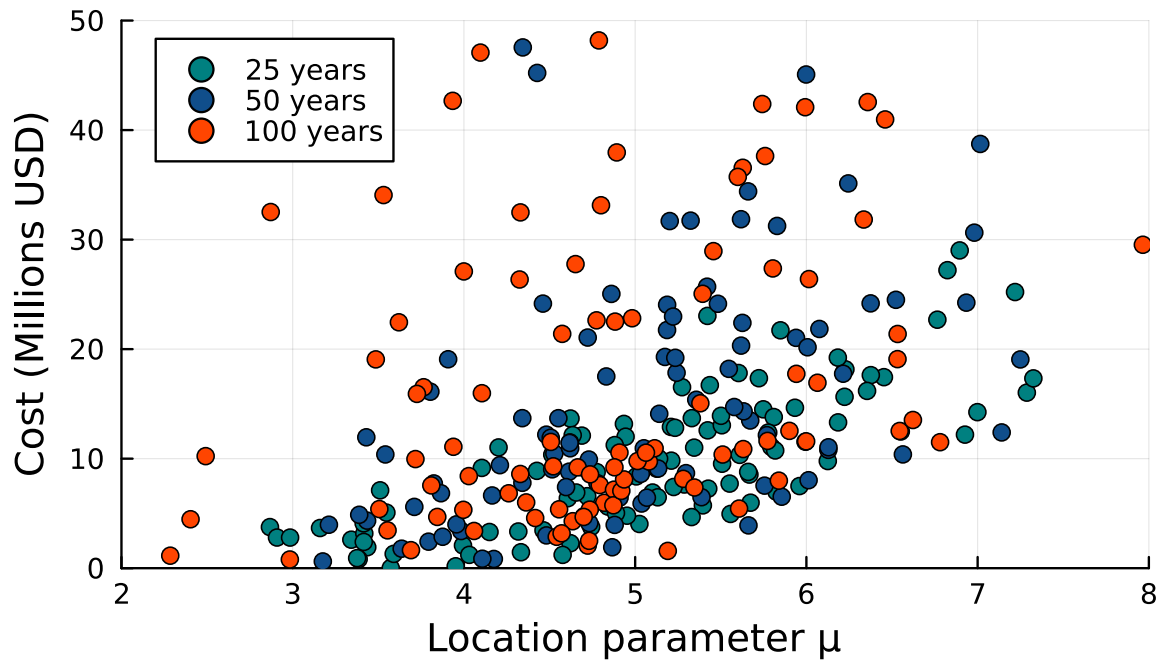
The higher the location parameter of the GEV distribution is the bigger is the NPV. This trend is more evident for shorter lifespans.

```

1  let
2      s = scatter(
3          xlabel="Location parameter ",
4          ylabel="Cost (Millions USD)",
5          ylims = [0,50],
6          xlims = [2,8],
7          title = "No elevation policy",)
8      years = [25,50,100]
9      colors = ["teal","dodgerblue4","orangered"]
10     for y in 1:3
11         scatter!(s, df.surge_[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])],
12             -df.npv[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])]/ 1e6;
13             label = "$(years[y]) years",
14             color = colors[y],
15             )
16     end
17     s
18 end

```

No elevation policy



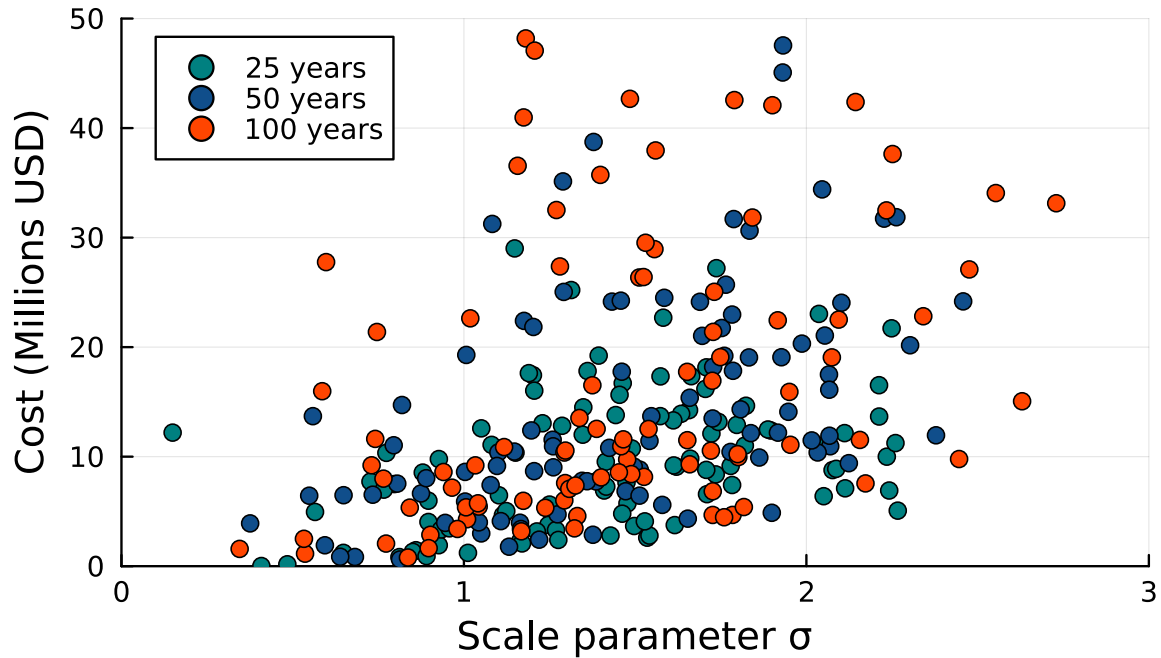
Similarly, the shape factor α , also has a important positive trend.

```

1 let
2   s = scatter(
3       xlabel="Scale parameter ",
4       ylabel="Cost (Millions USD)",
5       ylims = [0,50],
6       xlims = [0,3],
7       title = "No elevation policy",)
8   years = [25,50,100]
9   colors = ["teal","dodgerblue4","orangered"]
10  for y in 1:3
11      scatter!(s, df.surge_[(df.Δh_ft .== 0) .* (df.      years_frame .==years[y])],
12                -df.npv[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])]/ 1e6;
13                label = "$(years[y]) years",
14                color = colors[y],
15                )
16  end
17  s
18 end

```

No elevation policy



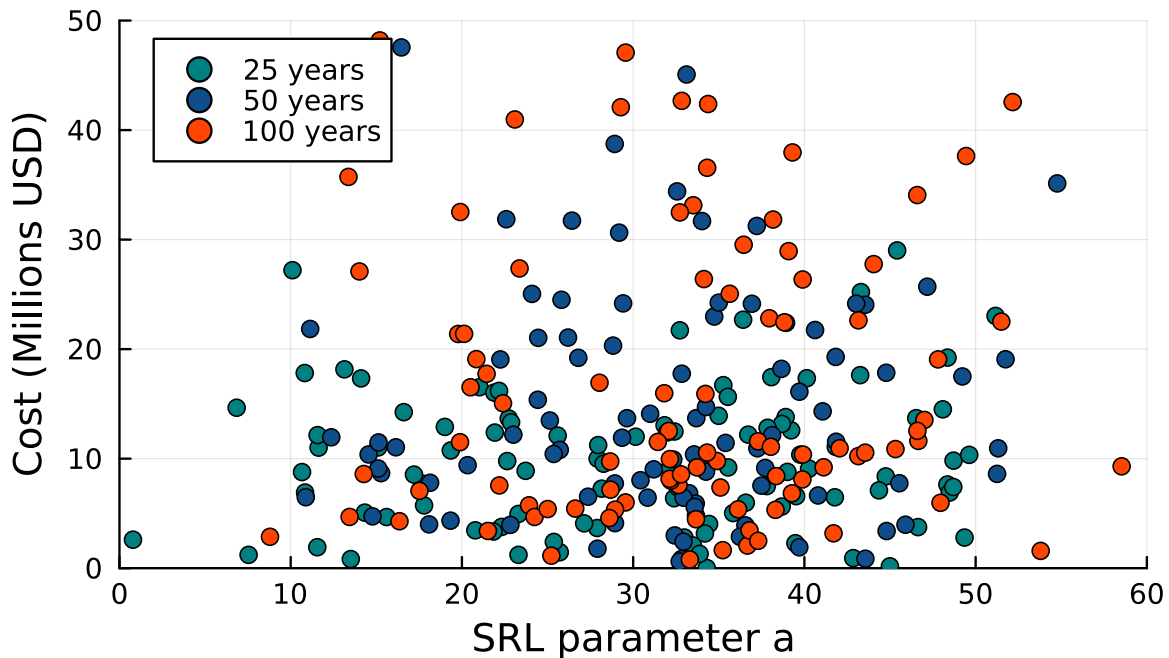
There is no identifiable trend regarding the SLR model parameters considering perhaps its large variation.

```

1  let
2      s = scatter(
3          xlabel="SRL parameter a",
4          ylabel="Cost (Millions USD)",
5          ylims = [0,50],
6          xlims = [0,60],
7          title = "No elevation policy",
8      )
9      years = [25,50,100]
10     colors = ["teal","dodgerblue4","orangered"]
11     for y in 1:3
12         scatter!(s, df.slr_a[(df.Δh_ft .== 0) .* (df.          years_frame .==years[y])],
13             -df.npv[(df.Δh_ft .== 0) .* (df.years_frame .==years[y])]/ 1e6;
14             label = "$ (years[y]) years",
15             color = colors[y],
16         )
17     end
18     s
19 end

```

No elevation policy



3 Analysis

When do you get the best results?

As previously identified (past lab), the best overall results is around 8 ft of elevation (no important difference in 7-9 ft interval).

When do you get the worst results? The worst results are concentrated in the 0 and 1 ft elevation actions for all the lifespans considered.

What are the most important parameters? The flood frequency GEV parameters are very important in the modeling as well as the discount rate. As also shown, the time window considered is also a huge source of both uncertainty and NPV difference.

If you had unlimited computing power, would you run more simulations? How many?

I would not run that many simulations considering that the identified trend is already giving good information. The number 1000 or 10000 sounds enough. Similarly, for the present case study the alternative of not-elevating is clearly the one with the worst outcome for any timeframe.

What are the implications of your results for decision-making?

The exploratory modeling shows that for the majority of possible SOW, the building is expected to experience major losses if no action is taken. When considering elevating the building, the prevented losses are more important than the elevation costs. From a financial, cost-benefit analysis there are enough arguments to support the elevation project. Regarding the ammount of elevation, there is enough evidence to elevate the bulding ~ 7 ft to reach cost optimallity.

Oddo, Perry C., Ben S. Lee, Gregory G. Garner, Vivek Srikrishnan, Patrick M. Reed, Chris E. Forest, and Klaus Keller. 2017. “Deep Uncertainties in Sea-Level Rise and Storm Surge Projections: Implications for Coastal Flood Risk Management.” *Risk Analysis* 0 (0). <https://doi.org/ghkp82>.