

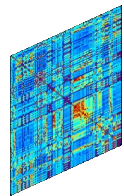
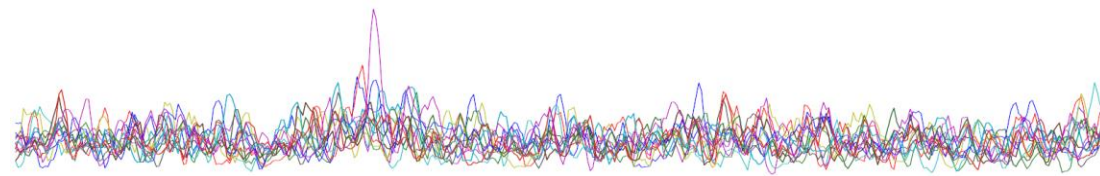
# GLHMM workshop

Introductory module

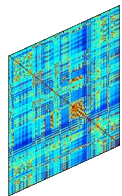
Laura Masaracchia, PhD

# HMM recap

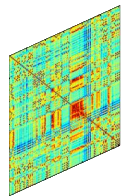
HMM finds recurring patterns in the data (states)



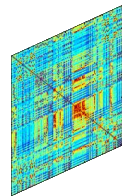
State 1



State 2

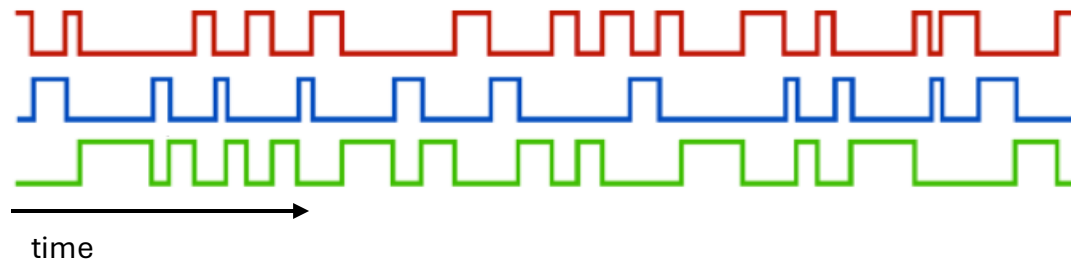


State 3



State 4

State time  
courses



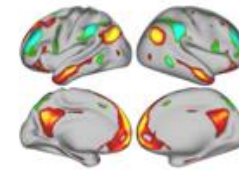
State 1

State 2

State 3

Key elements of HMM states:

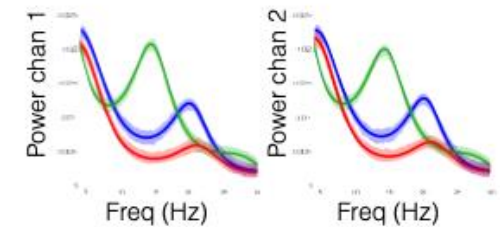
Mean activation



Functional connectivity



Spectral properties



# HMM families: flexible state definitions

Different HMM families: flexible state models

- Gaussian (aka standard) HMM, [Baker et al., 2014, eLife](#)
- Gaussian Linear (aka decoding) HMM, [Vidaurre et al., 2025, Imaging Neuroscience](#)
- Multivariate autoregressive (MAR) HMM, [Vidaurre et al., 2016, NeuroImage](#)
- Time-delay embedded (TDE) HMM, [Vidaurre et al., 2018, Nature Communications](#)

Choice of HMM family depends on

- Data characteristics
- Scope of research

# Gaussian (aka standard) HMM

[Baker et al., 2014, eLife](#)

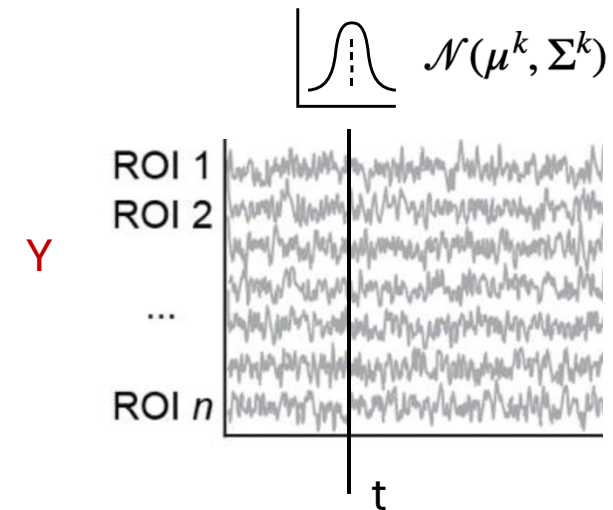
Definition:

- For each time point  $t$  in data  $\mathbf{Y}$ : computes probability of  $\mathbf{Y}_t$  coming from a **Gaussian** distribution.
- Focus on instantaneous changes in the mean of the signal

$$Y_t | s_t = k \sim \mathcal{N}(\mu^k, \Sigma^k)$$

Application:

- Most appropriate for whole-brain fMRI data
- States interpreted as functional connectivity



# Gaussian-Linear (aka Decoding) HMM

[Vidaurre et al., 2025, Imaging Neuroscience](#)

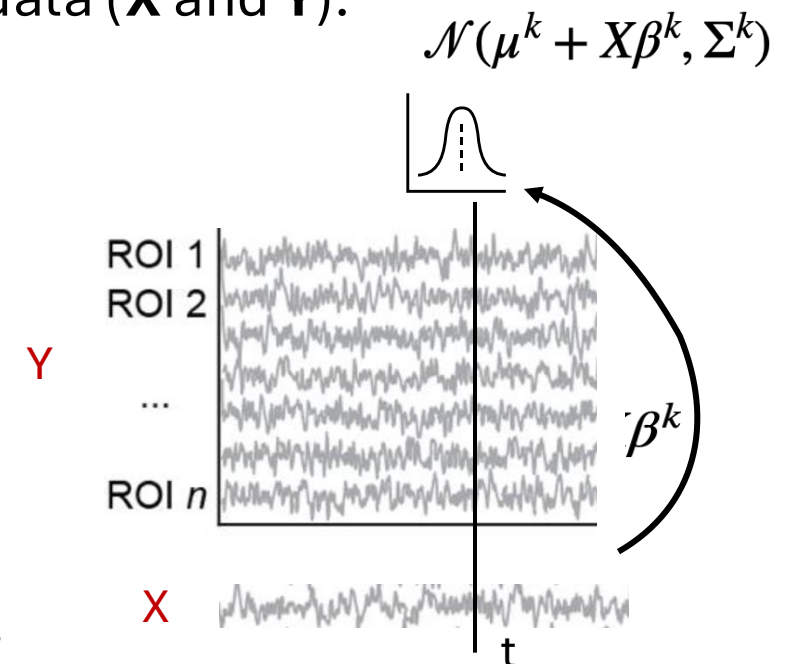
Definition:

- Models the relationship between two sets of timeseries data (**X** and **Y**).
- Models **Y<sub>t</sub>** like the standard HMM + predicting **Y<sub>t</sub>** from **X**

$$Y_t | s_t = k \sim \mathcal{N}(\mu^k + X\beta^k, \Sigma^k)$$

Application:

- Useful to link behavioural and fMRI timeseries, or
- neural data across different brain regions / spatial scales



# Multivariate Autoregressive (MAR) HMM

[Vidaurre et al., 2016, NeuroImage](#)

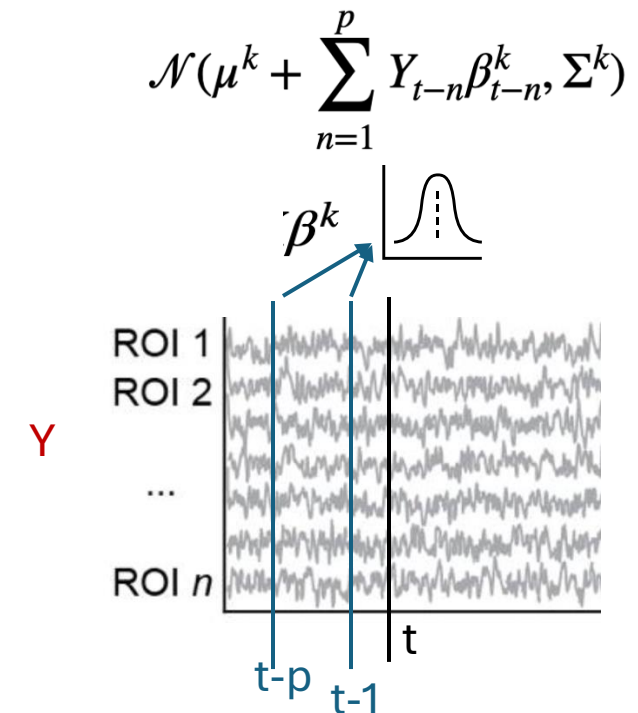
Definition:

- Predicts  $\mathbf{Y}_t$  from  $p$  previous time points
- Focus on temporal changes in the signal

$$Y_t | s_t = k \sim \mathcal{N}(\mu^k + \sum_{n=1}^p Y_{t-n} \beta_{t-n}^k, \Sigma^k)$$

Application:

- Best to use low-dimensional data (MEG, LFP, EEG) for computational reasons
- Most appropriate to detect frequency changes in the data



# Time-delay embedded (TDE) HMM

[Vidaurre et al., 2018, Nature Communications](#)

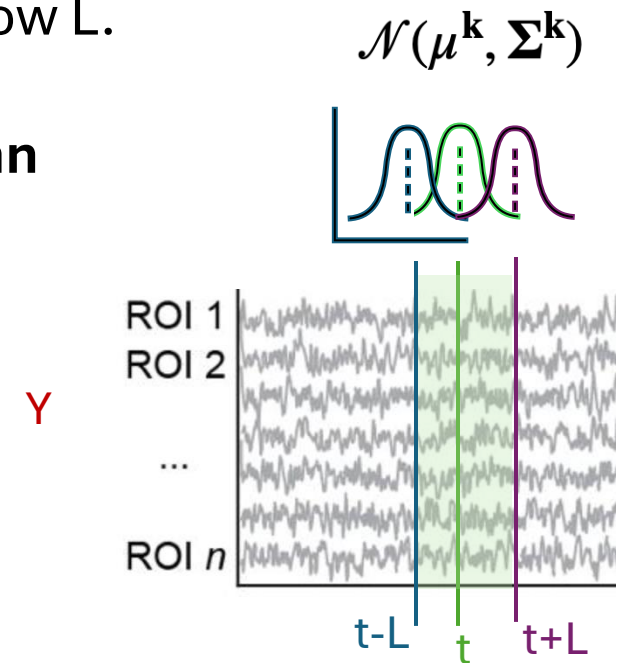
Definition:

- Models the autocovariance of the signal within a time window  $L$ .
- For each  $t$  in the data  $\mathbf{Y}$ : computes the probability of the **autocovariance** of  $\mathbf{Y}_t$  to come from a **multivariate Gaussian** distribution.

$$Y_{t-L}, \dots, Y_t, \dots, Y_{t+L} | s_t = k \sim \mathcal{N}(\mu^k, \Sigma^k)$$

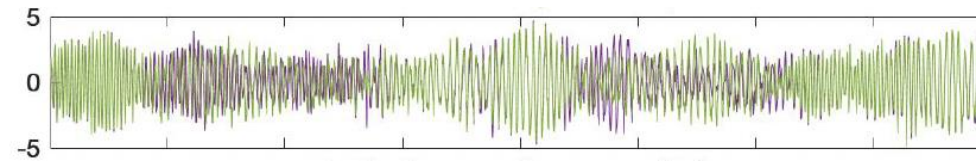
Application:

- Most appropriate for MEG multi-channel (whole-brain) data
- Most sensitive to frequency changes and cross-channel coherence in the data.

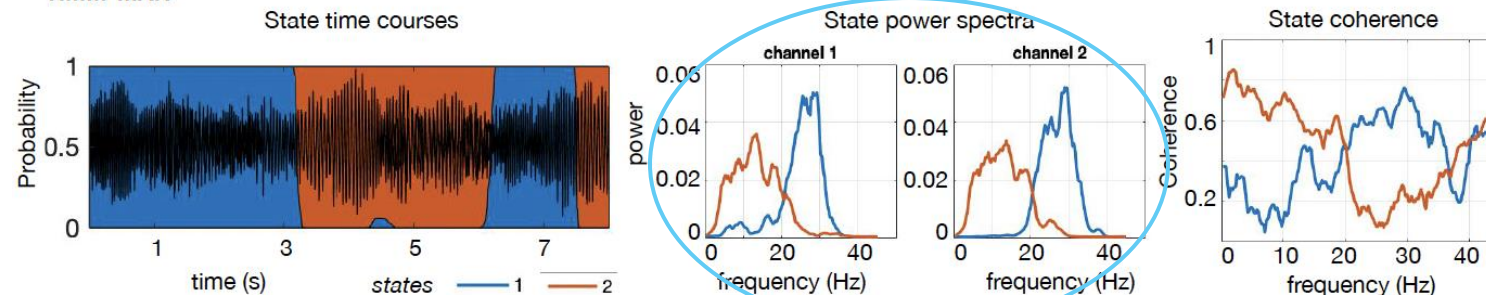


# Practical example: HMM-MAR vs HMM-TDE

Two-channel synthetic signal

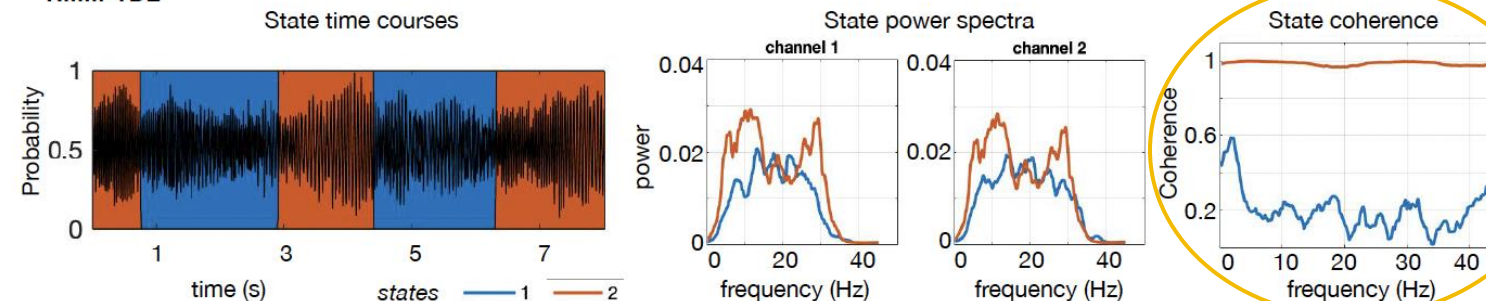


HMM-MAR



HMM-MAR : states  
focus on frequency

HMM-TDE



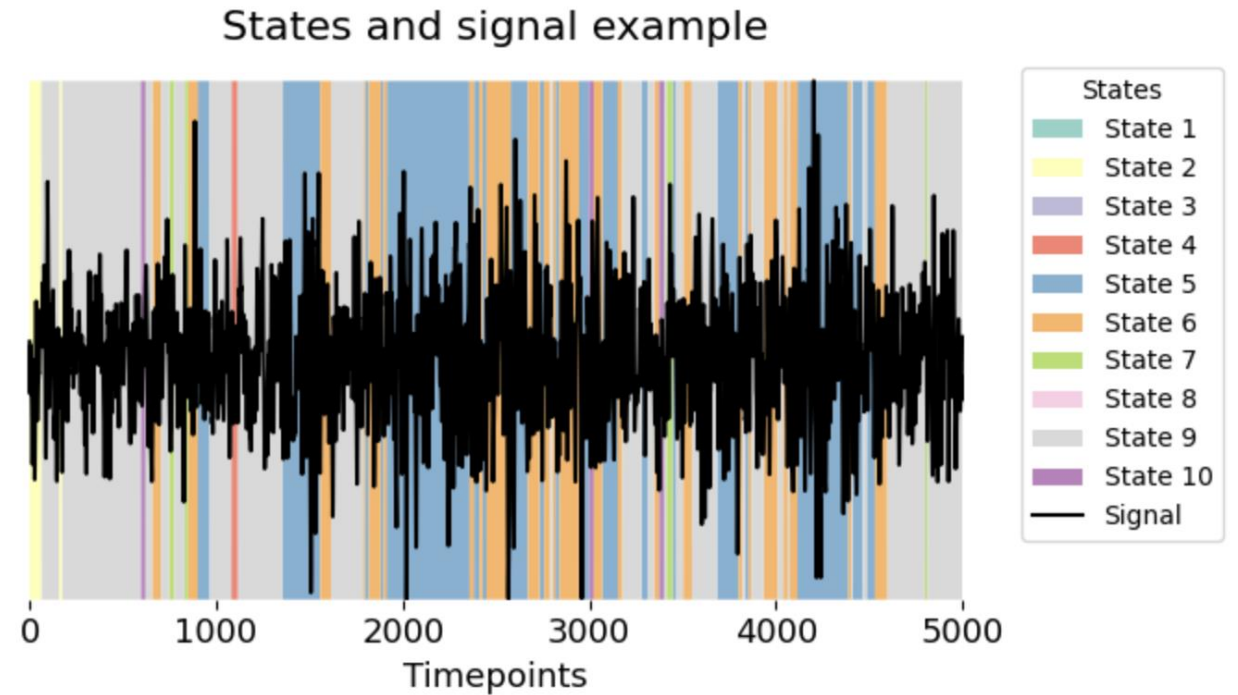
HMM-TDE: states focus on  
cross-channel coherence

Masaracchia et al., 2023.  
Journal of Neurophysiology



# The HMM output: State time courses

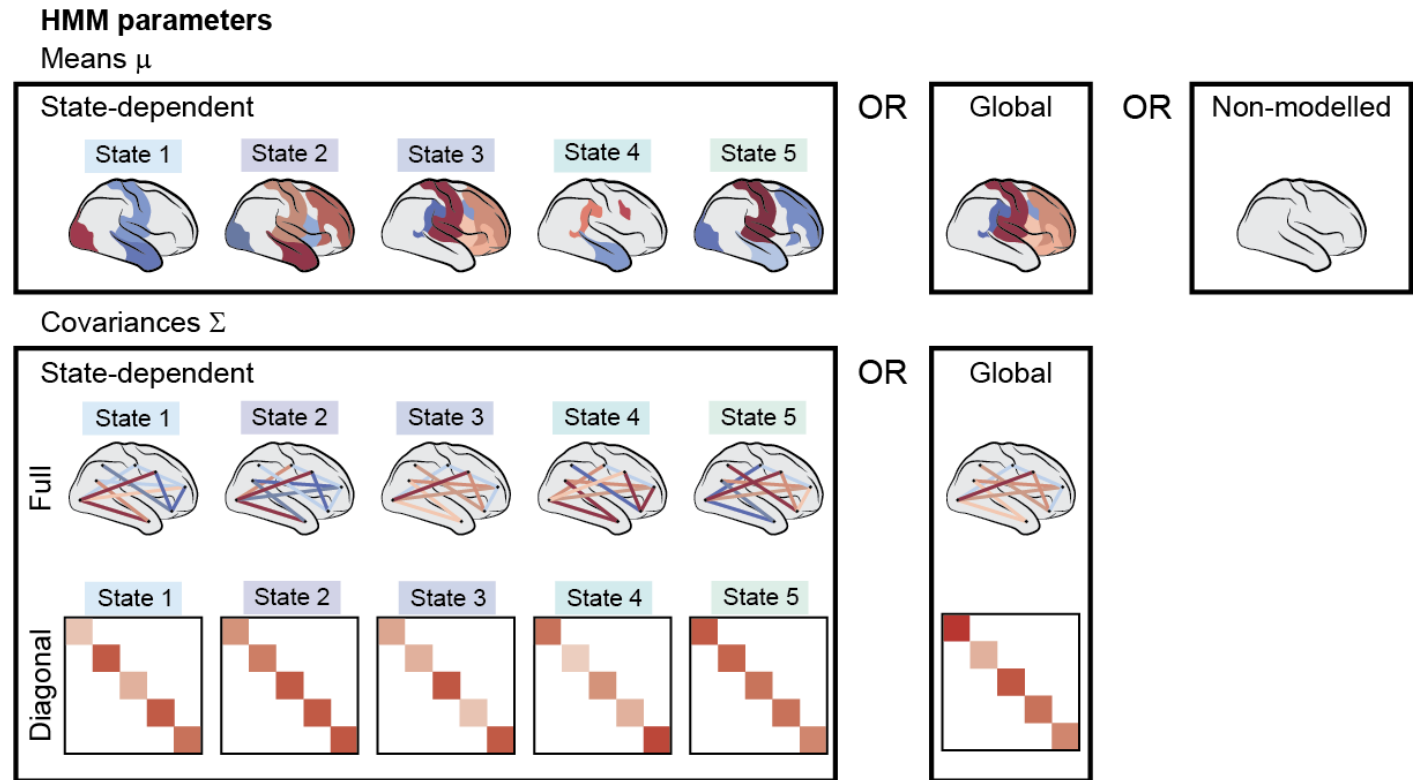
- State time courses (**Gamma**): the probability of each time point to belong to a state
- Viterbi path (**vpath**): a categorical version of the Gamma



# The HMM output: States

- States:

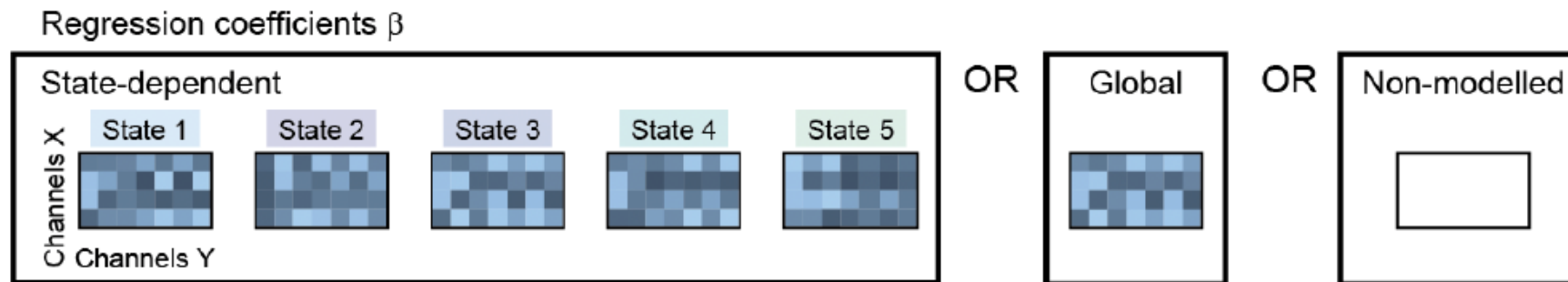
- Mean ( $\mu$  /  $\mu$ ), when included : amplitude of the state
- Covariance ( $\Sigma$  /  $\Sigma$ ) : Functional Connectivity – patterns of activity across channels defining a state



Source: [Vidaurre et al., 2025, Imaging Neuroscience](#)

# The HMM output: Regression Coefficients

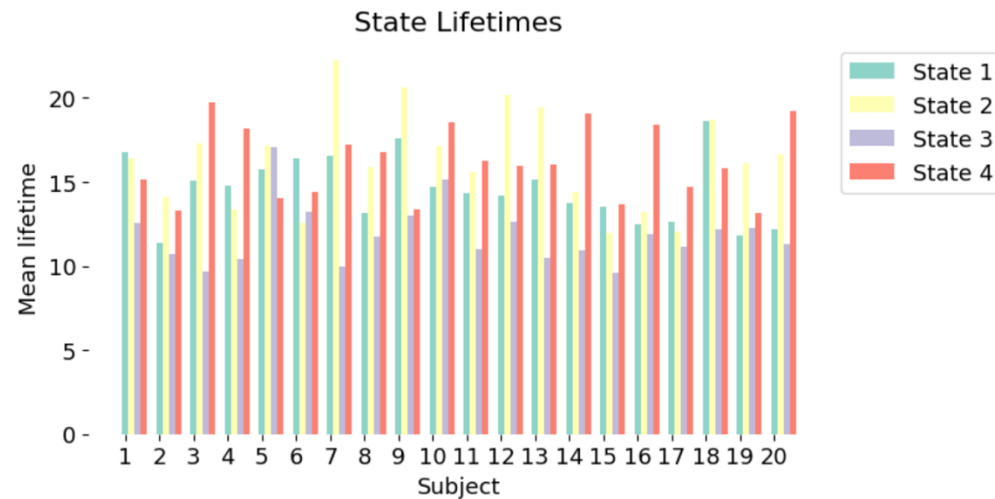
- Beta ( $\beta$ ), when included: link to previous time points or to another time series



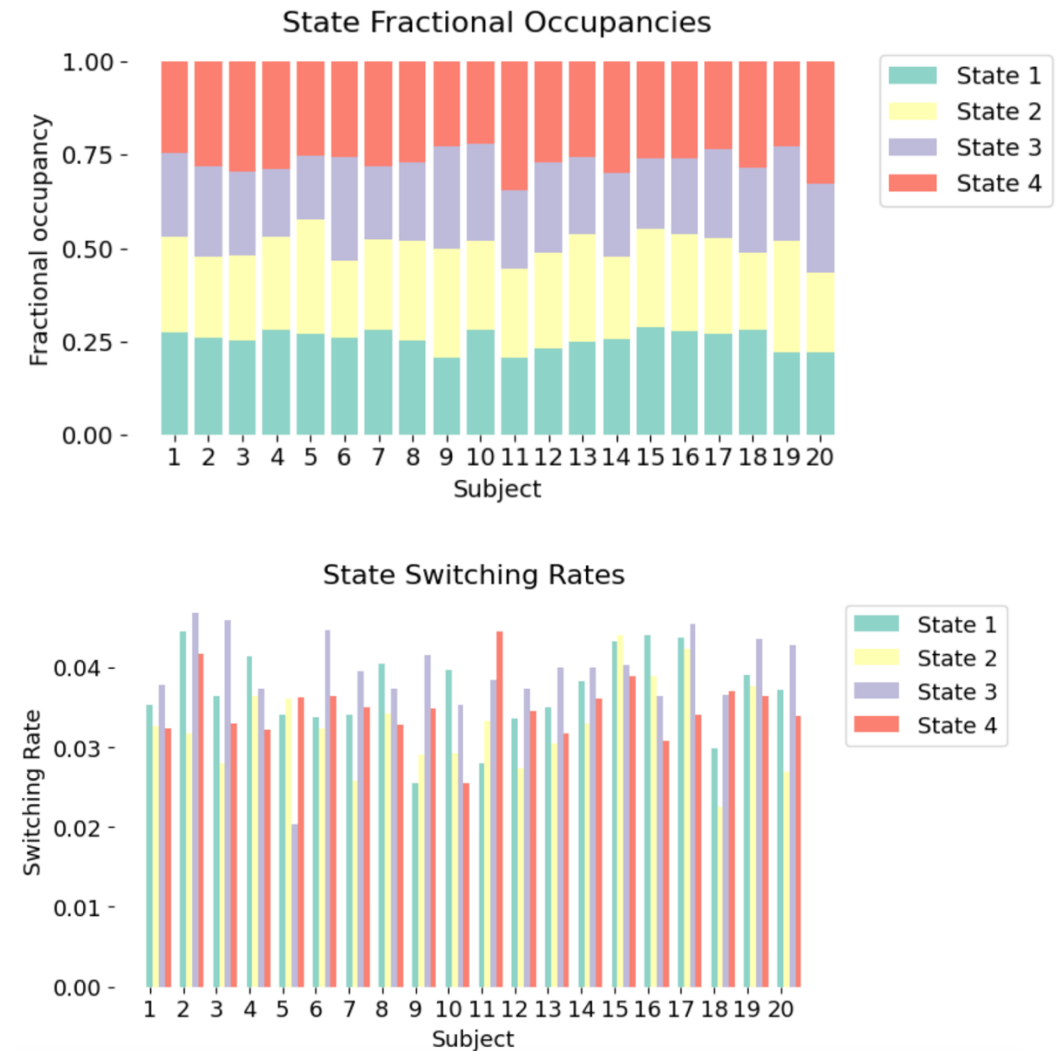
Source: [Vidaurre et al., 2025, Imaging Neuroscience](#)

# Summary metrics

- States Fractional Occupancy (FO) – how much on average each state is active
- States Lifetime (LT) – average time each state is active

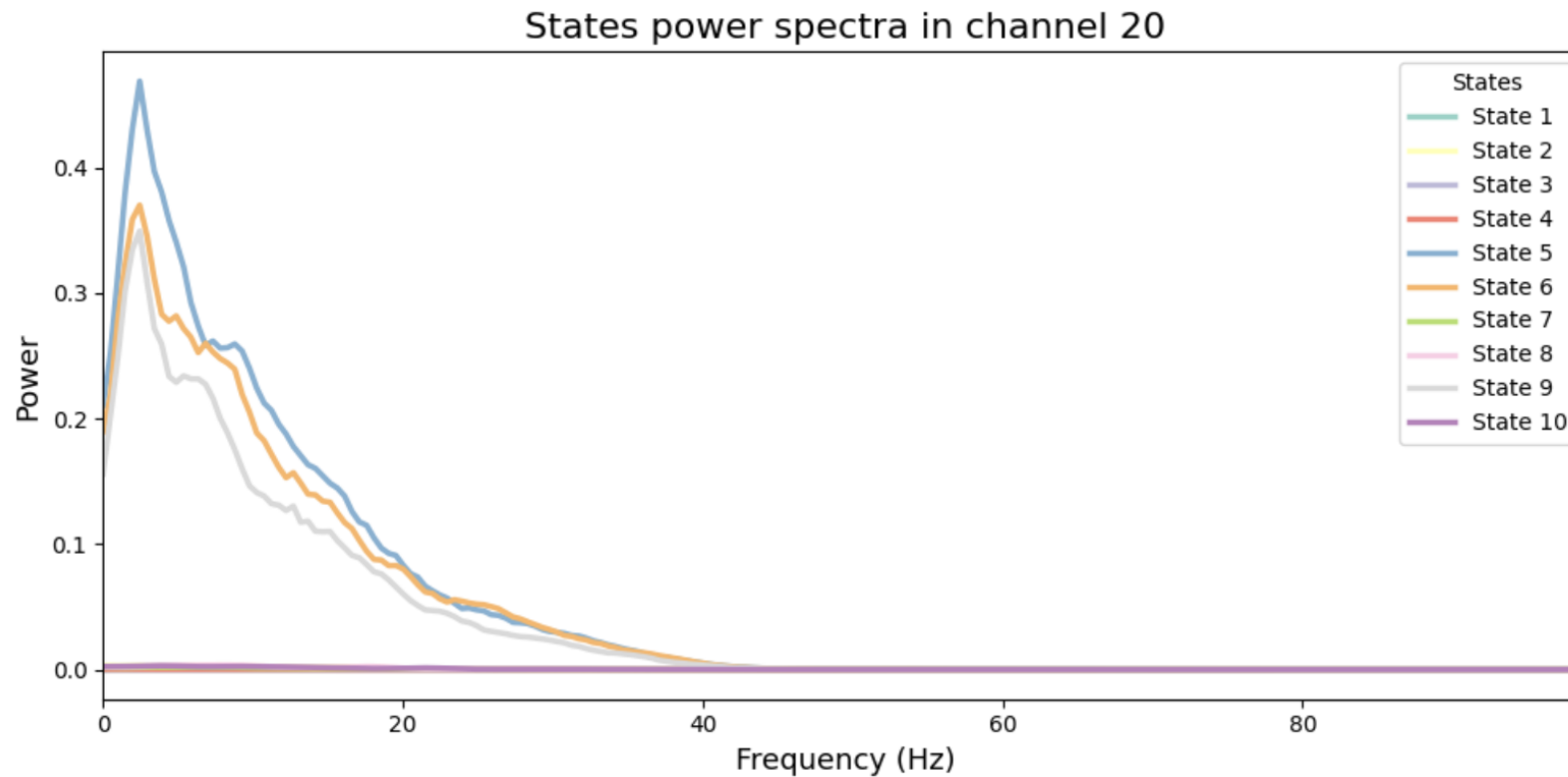


- States Switching Rate (SR) – how often a state switch occurs



# Spectral characteristics

Computing the power spectrum and cross-channel coherence of the states

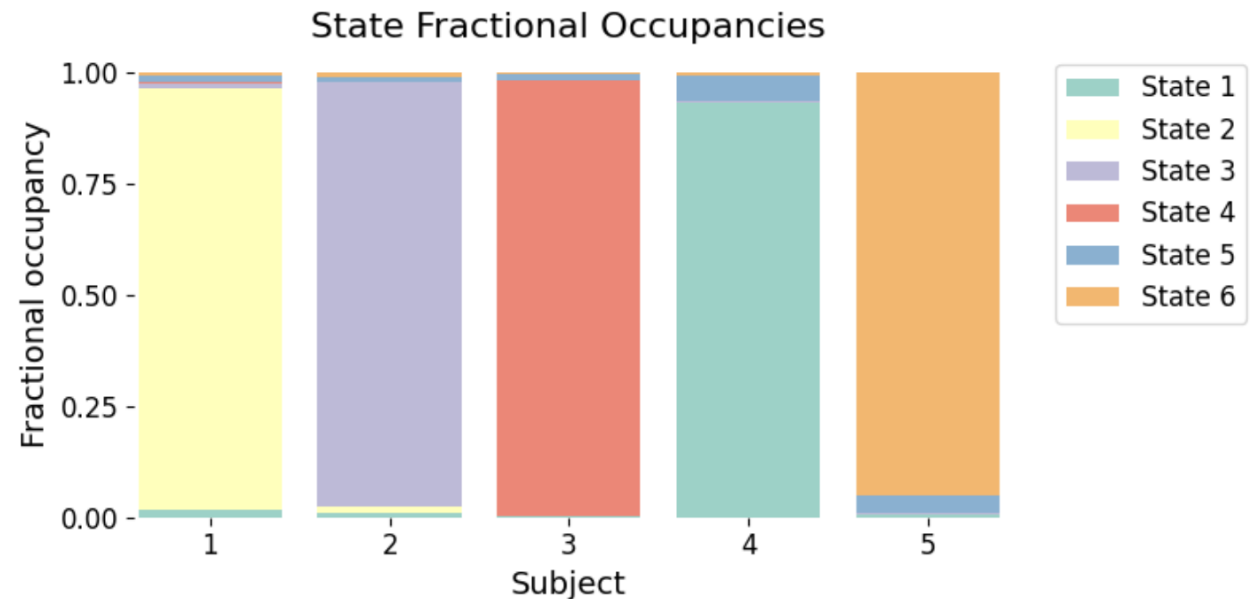


# Sanity checks and visualisations

*!!! Inspect your HMM after training*

Useful things to plot:

- Some examples of state time courses (vpath) with signal
- per-subject fractional occupancy, states lifetime and switching rate
- overall transition probability of the states



See [Ahrends et al., 2022, NeuroImage](#) for considerations on data and HMM parameters for good estimations

# Dealing with big data: stochastic learning

HMM can deal with large amount of data, performing *stochastic training* ([Vidaurre et al., 2018, NeuroImage](#))

## *When to use stochastic training?*

- Too big dataset to be loaded in memory
- Too long training time for the complete dataset

## *How does it work?*

- The HMM loads randomly selected chunks of data
- Learns recursively from the data that handles step by step

# GLHMM paper & python toolbox

The Gaussian Linear Hidden Markov Model (GLHMM) is a technique designed to characterise brain dynamics across different modalities ([Vidaurre et al., 2025, Imaging Neuroscience](#)). With the paper, we introduce a **python toolbox**.

The toolbox implements various HMMs and has options for:

- data preprocessing,
- analysis and visualization of the HMM outputs,
- prediction and statistical testing

Read the paper at [https://doi.org/10.1162/imag\\_a\\_00460](https://doi.org/10.1162/imag_a_00460)

Find the toolbox at <https://github.com/vidaurre/ghmm>

Find the documentation at: <https://ghmm.readthedocs.io/en/latest/index.html>



# The GLHMM toolbox: tutorials

The GLHMM toolbox includes **tutorials** sketching typical neuroscience projects, for example:

- Hypothetical fMRI study, with decoding HMM and prediction of phenotypes
- Hypothetical MEG study, with TDE-HMM and states spectral analysis
- Various types of statistical testing on HMM outputs
- ... and more!

Find the tutorials at: <https://github.com/vidaurre/ghmm/tree/main/docs/notebooks>

# The remaining time

- Go through the first tutorial at your own pace  
Tutorial's content:
  - Download example data
  - Basic preprocessing of the data
  - Instantiate and train appropriate HMM
  - Plot summary metrics and basic sanity checks
  - Spectral analysis, plot states power spectra
- Ask questions
- Get Help