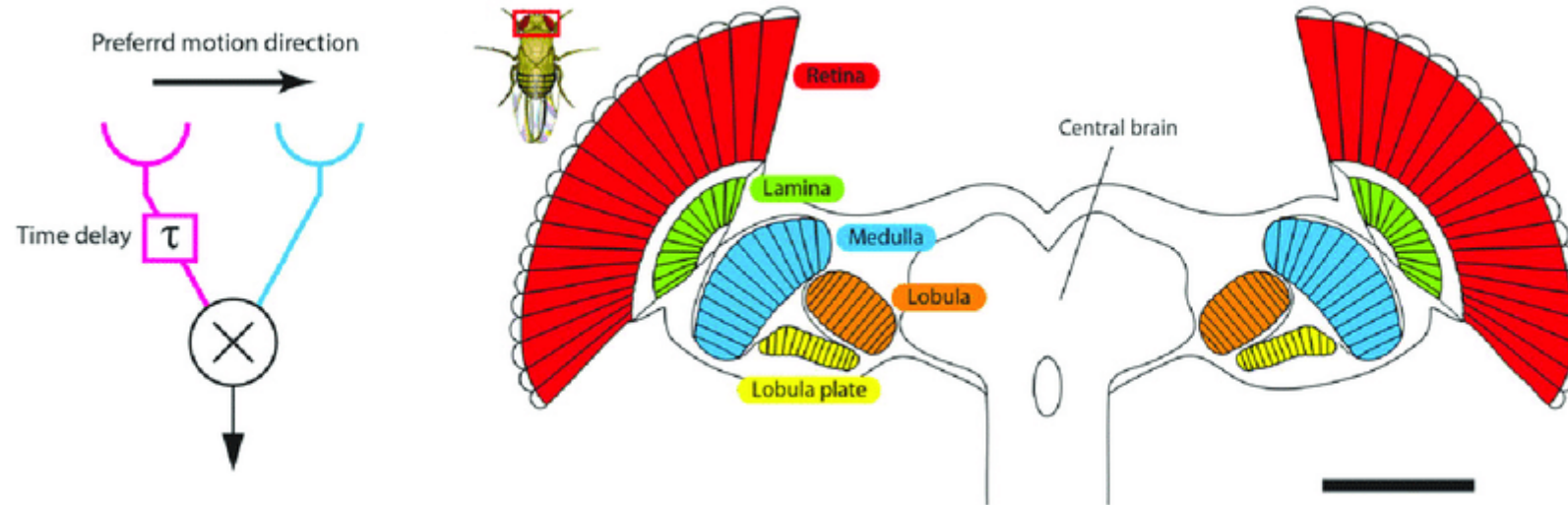


# Insect-Inspired Motion Detection System



Speaker: Wei-Tse Kao  
Advisor: Chung-Chuan Lo  
Date: 2019.11.28



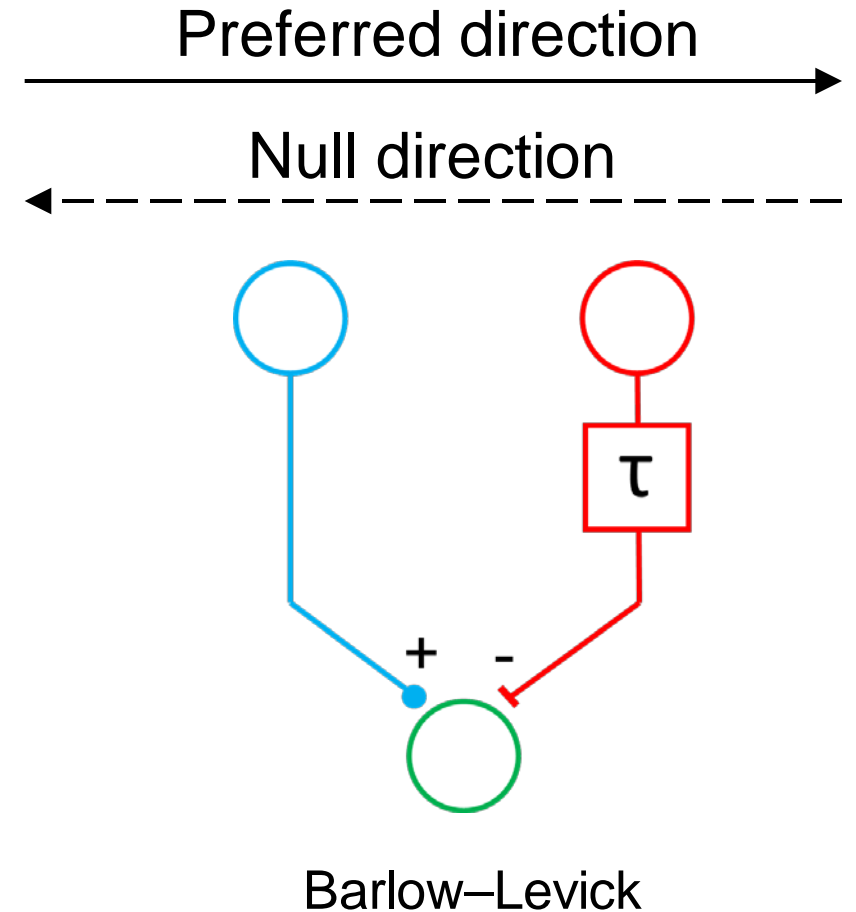
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# Motion vision: How we detect a moving object?



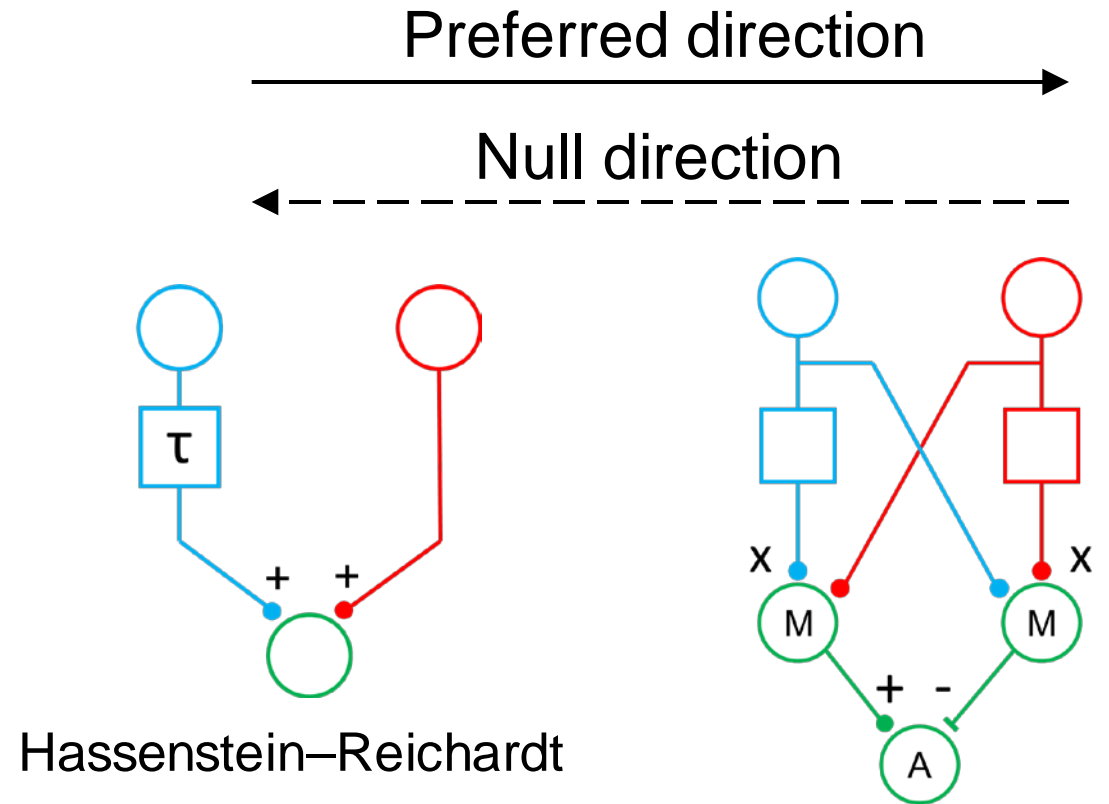
# Introduction : motion detection in biological system

- Modeling the neuron connectivity in retina and visual cortex.
- Response in preferred direction.
- Principles of visual motion detection :
  - Two inputs
  - Non-linear Interaction (time delay)
  - Asymmetry

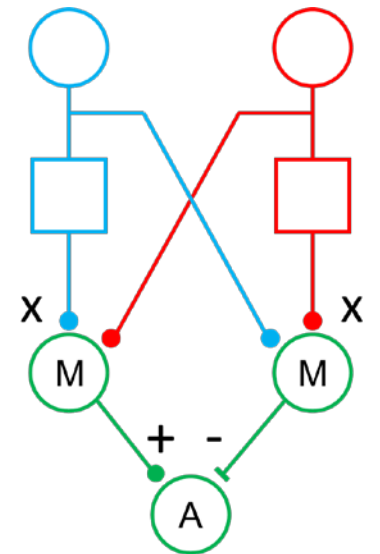


# Motion detection in biological system

- Modeling the neuron connectivity in retina and visual cortex.
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- Principles of visual motion detection :
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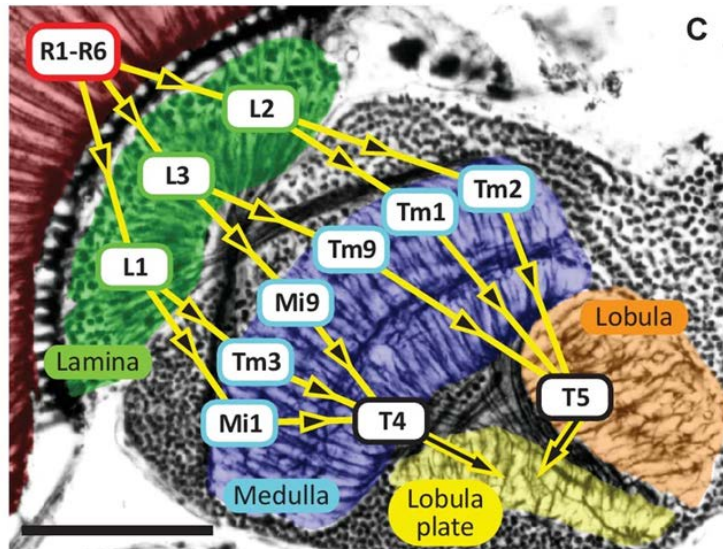


Full Hassenstein-Reichardt

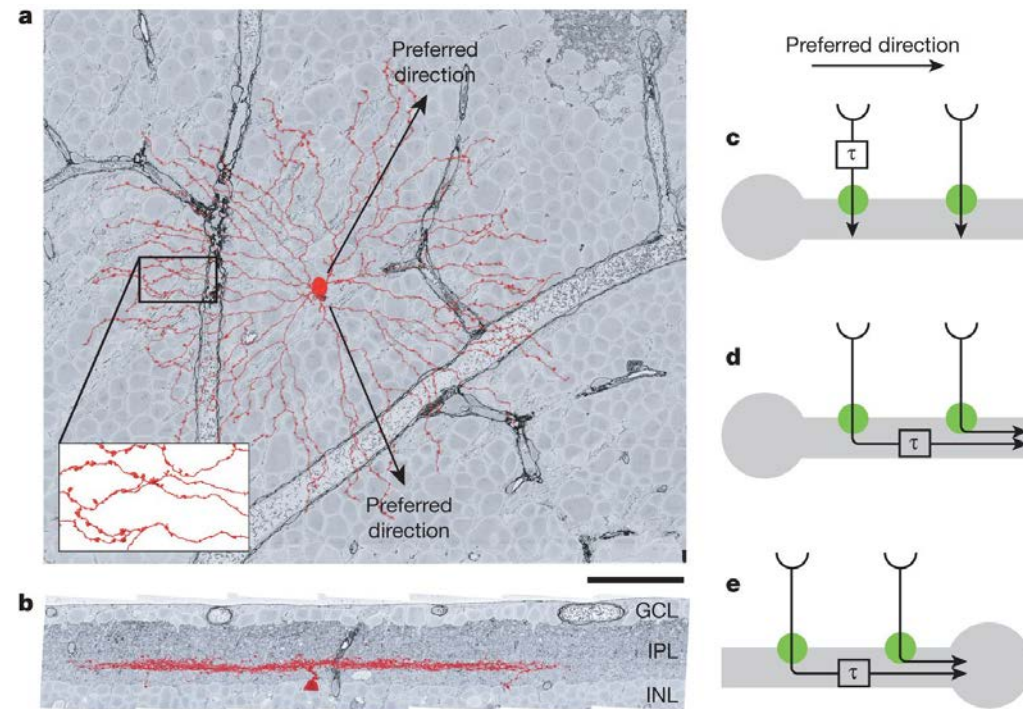


# Motion detection in biological system

- Evidence found in fly optic lobe and rabbit retina.

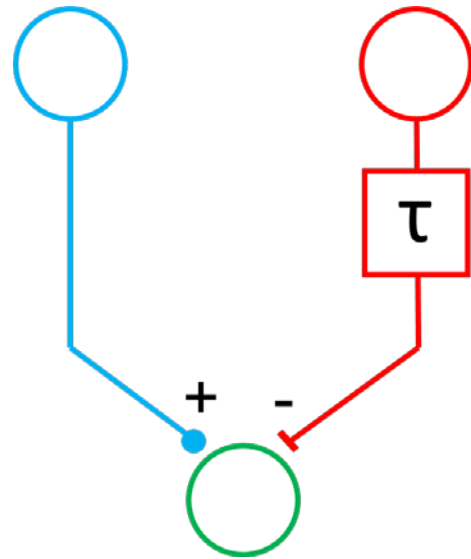
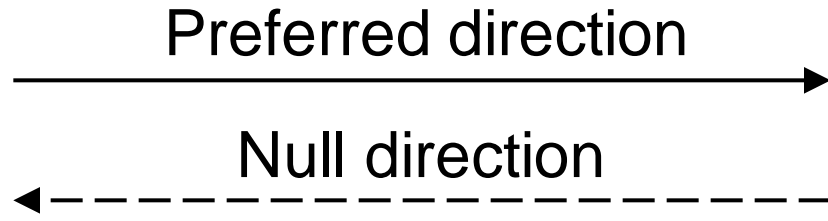


Takemura, Shin-ya, et al. *Elife* 6 (2017)

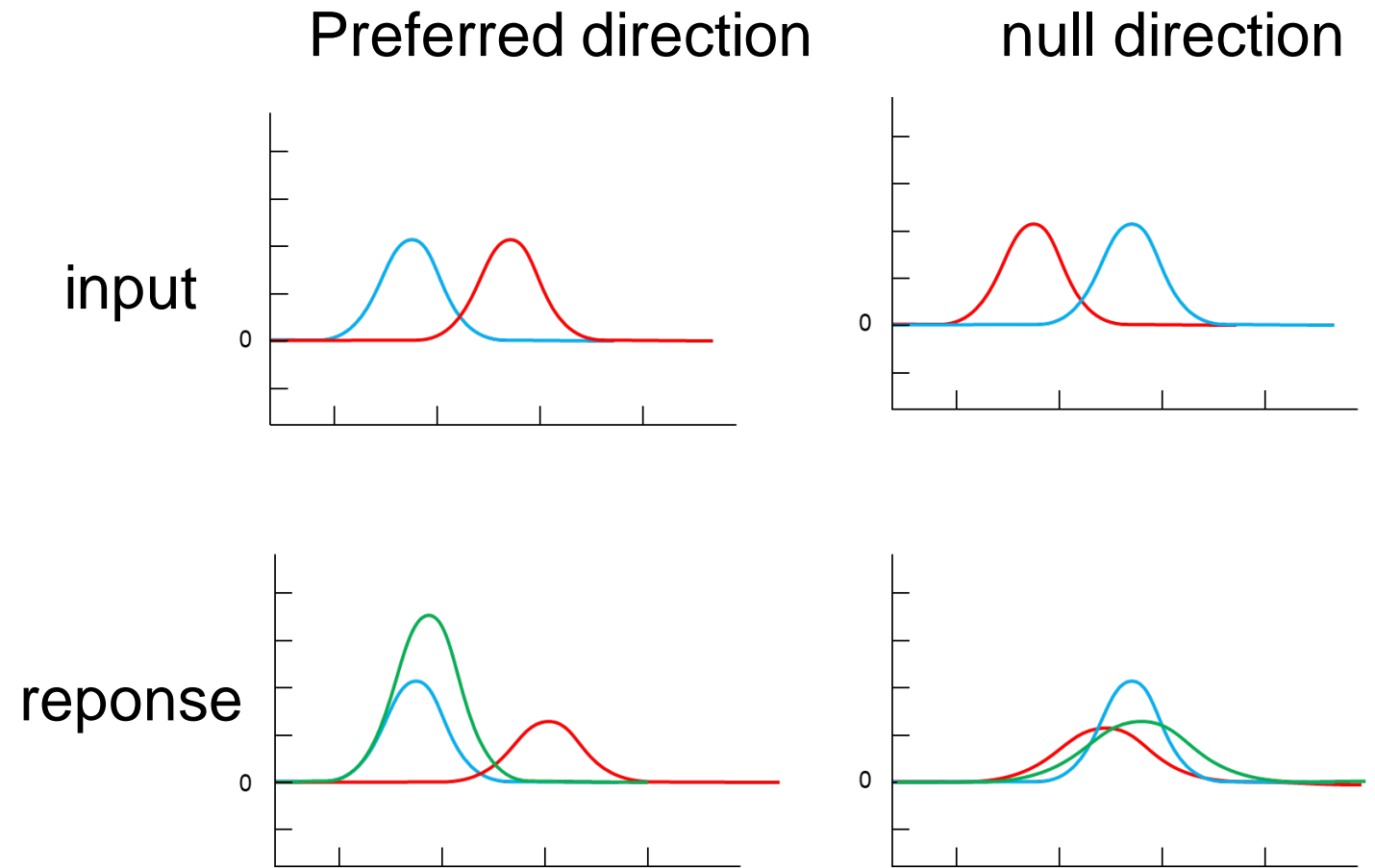


Kim, J. S., et al *Nature* (2014).

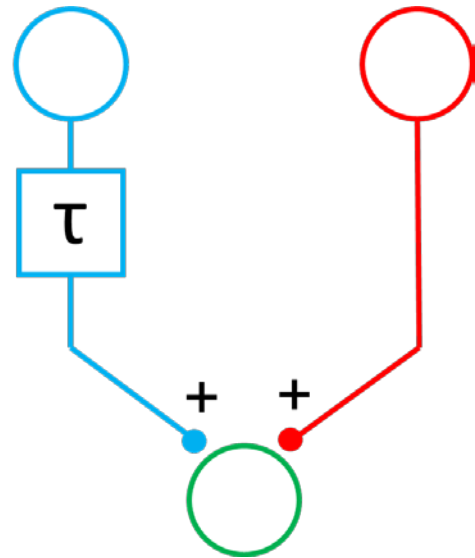
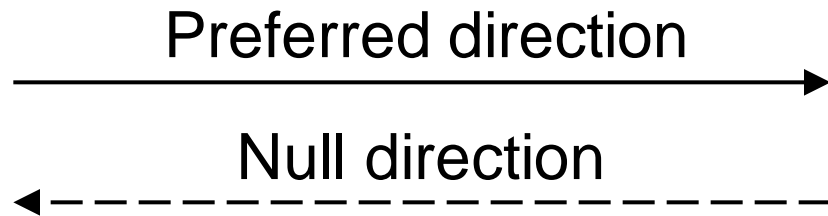
# Motion detection model and its response



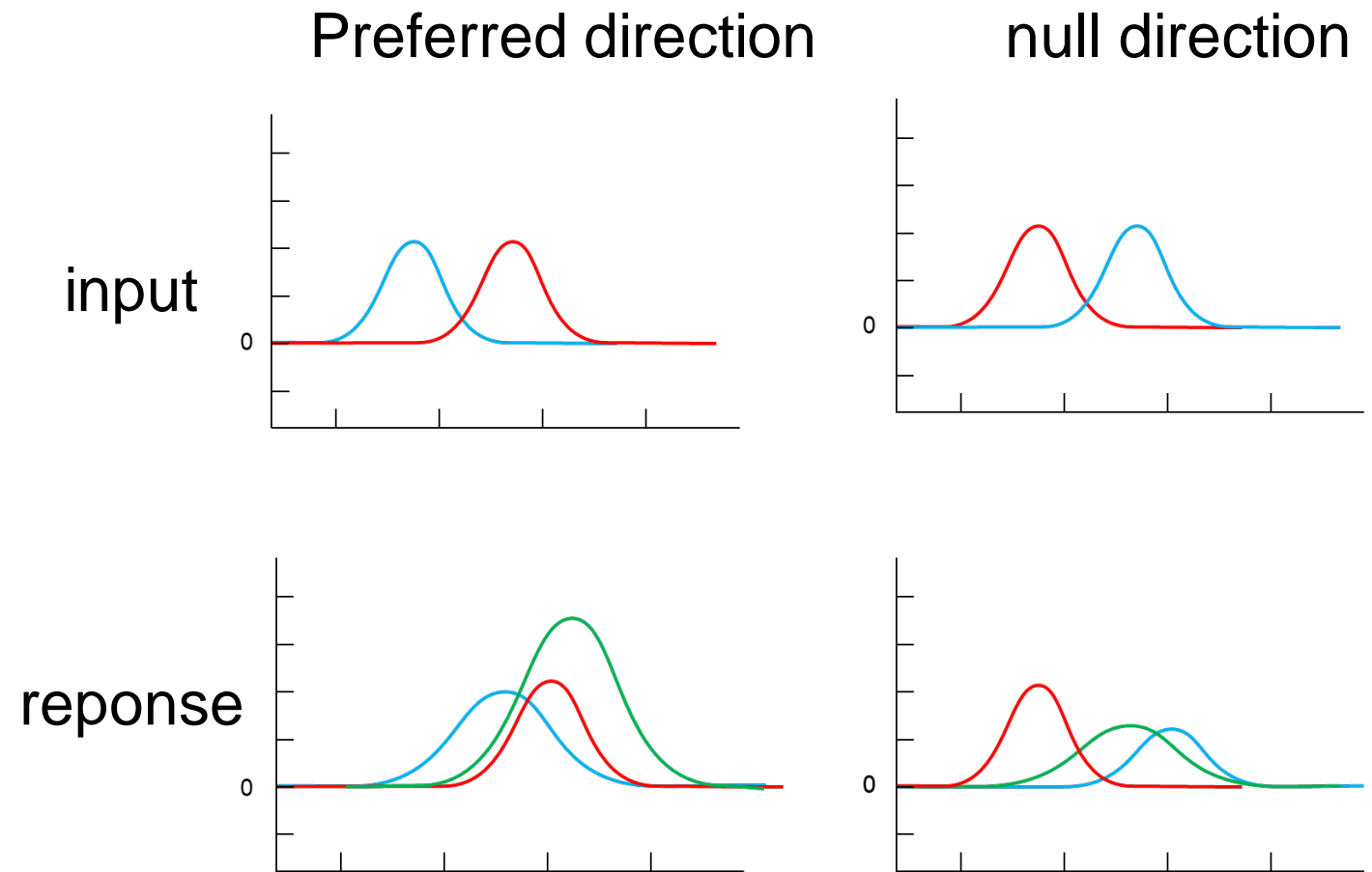
Barlow-Levick



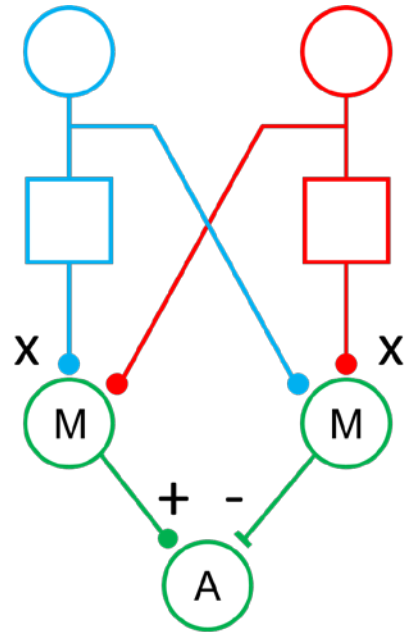
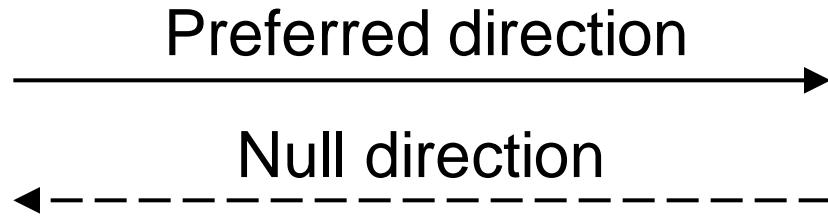
# Motion detection model and its response



Hassenstein-Reichardt



# Motion detection model and its response

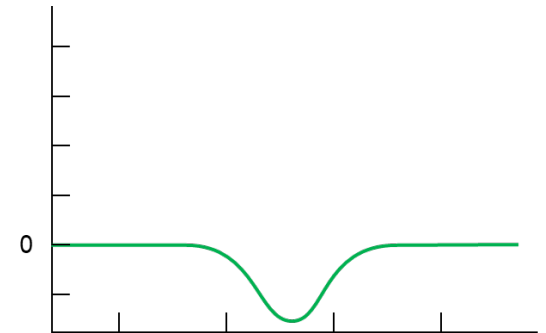
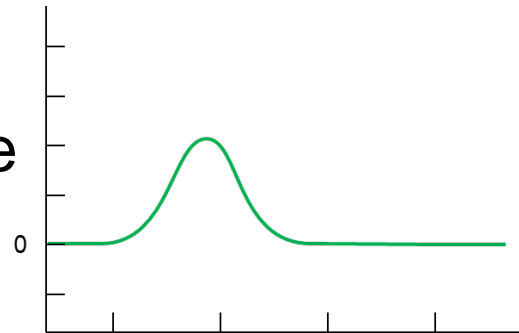


Full Hassenstein-Reichardt

Preferred direction

null direction

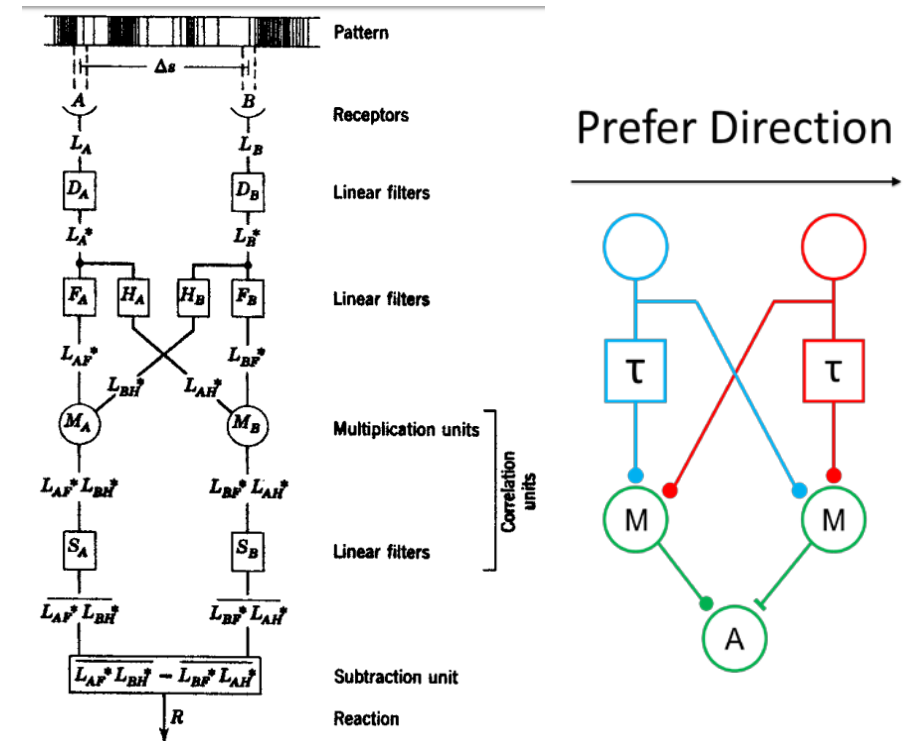
reponse





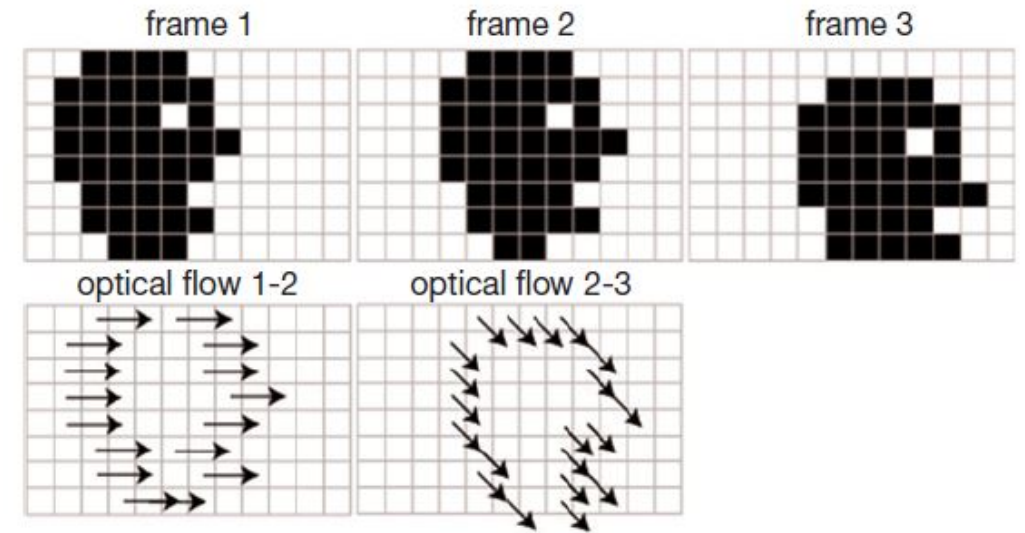
# Reichardt-Hassenstein Model (1956)

- Detect correlation between the two adjacent points.
- Consists of two symmetrical subunits.
- Computed by following processing steps:
  - Time delay with low-pass filter.
  - Multiplication other subunit.
  - Compute correlation by subtractor.



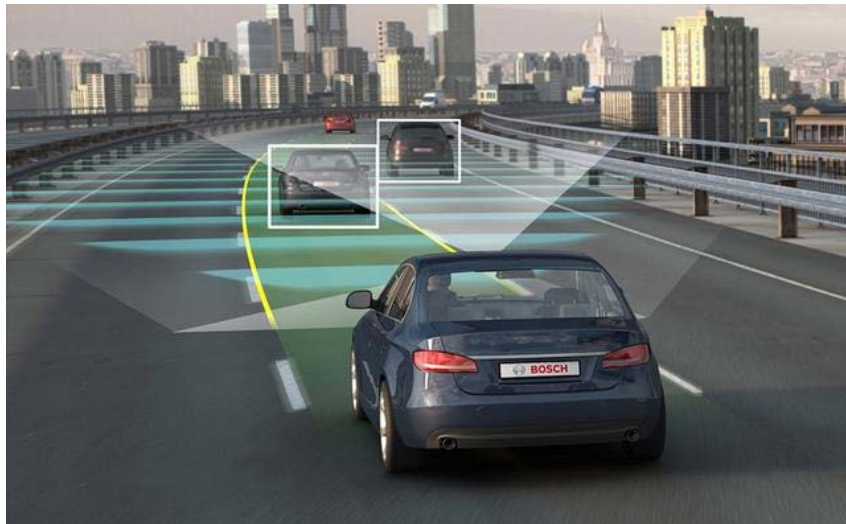
# Introduction: Optical Flow

- Optical Flow (OF) describes the relative motion field caused by camera relative to the objects.
- Calculate the motion between two image frames.
- Widely use in robotic navigation control, video processing.



# Motivation

- Investigate the difference between motion detection model and optical flow.
- Design a low power consumption motion estimation method.

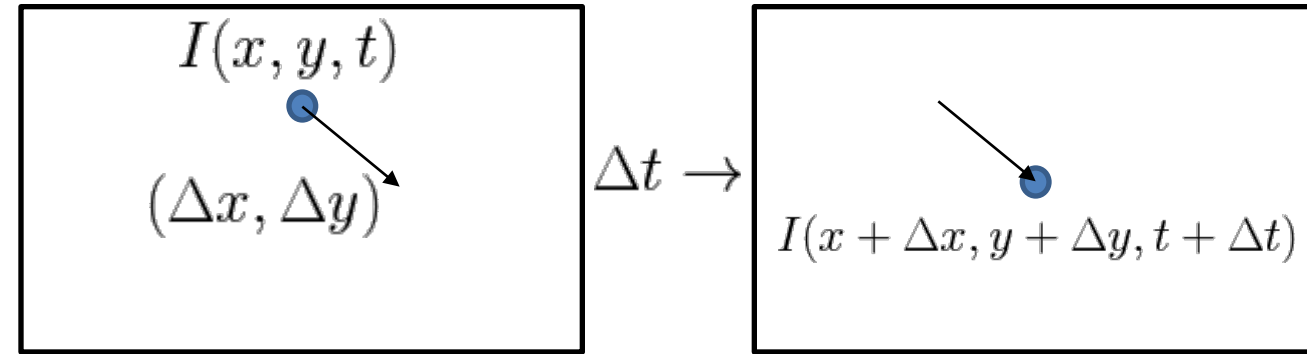


# Preliminary: Lucas-Kanade method

- Brightness constancy constraint:

- Constraint equation:

$$I(x, y, t) = I(x + \Delta x, y + \Delta y, t + \Delta t)$$



- Take Taylor expansion:

$$I(x + \Delta x, y + \Delta y, t + \Delta t) = I(x, y, t) + \frac{\partial I}{\partial x} \Delta x + \frac{\partial I}{\partial y} \Delta y + \frac{\partial I}{\partial t} \Delta t$$

$$I_x V_x + I_y V_y = -I_t$$

# Lucas–Kanade method

- Assumption: The flow is essentially constant in a local neighbourhood of the pixel.

$$I_x(q_1)V_x + I_y(q_1)V_y = -I_t(q_1)$$

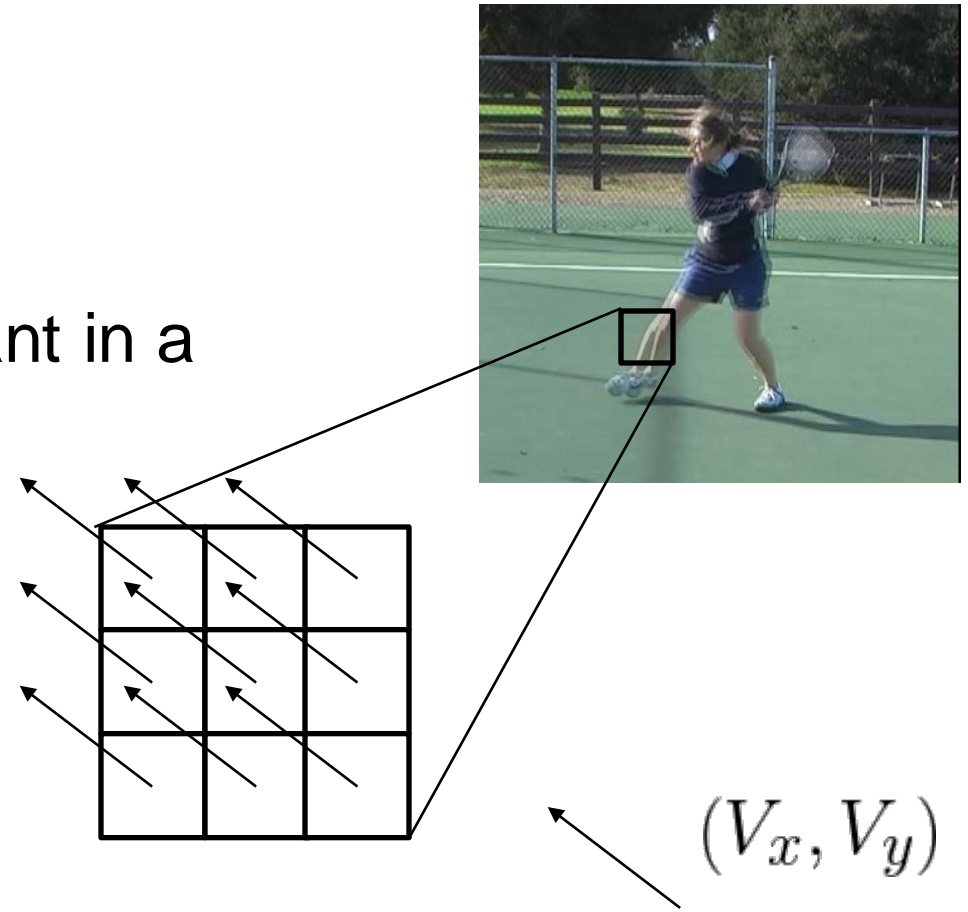
$$I_x(q_2)V_x + I_y(q_2)V_y = -I_t(q_2)$$

$\vdots$

$$I_x(q_n)V_x + I_y(q_n)V_y = -I_t(q_n)$$

- Solved by least squares method.

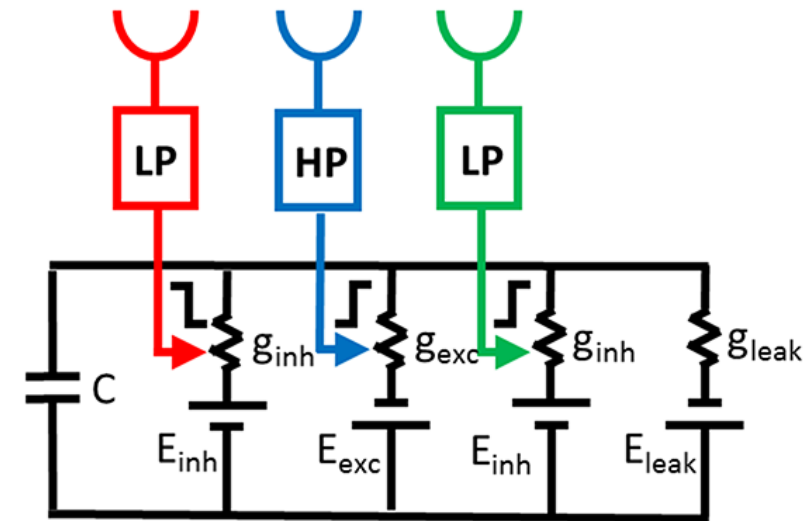
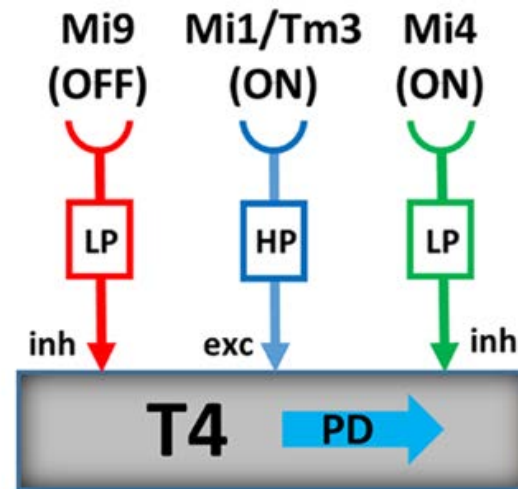
$$\begin{bmatrix} V_x \\ V_y \end{bmatrix} = \begin{bmatrix} \sum_i I_x(q_i)^2 & \sum_i I_x(q_i)I_y(q_i) \\ \sum_i I_y(q_i)I_x(q_i) & \sum_i I_y(q_i)^2 \end{bmatrix}^{-1} \begin{bmatrix} -\sum_i I_x(q_i)I_t(q_i) \\ -\sum_i I_y(q_i)I_t(q_i) \end{bmatrix}$$



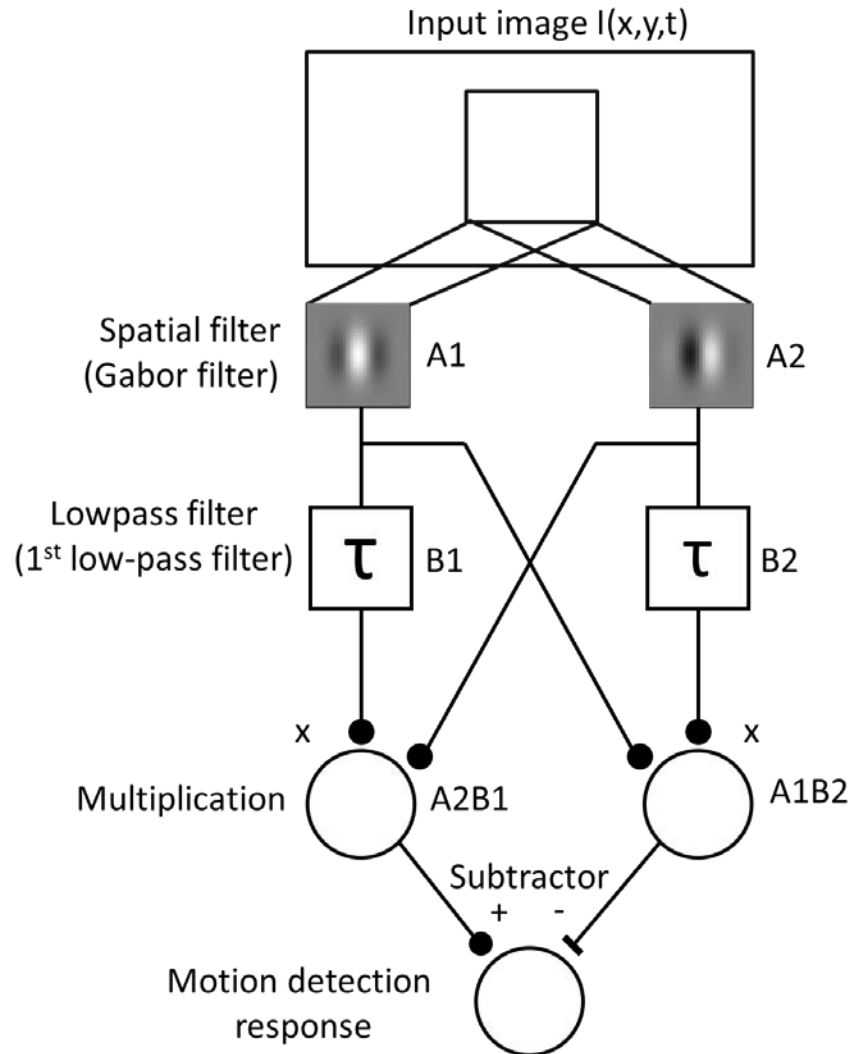
# Preliminary: Borst's Model(2018)

- Biophysics model base on connectome data.
- Describe as a passive membrane circuit.
- Visual signal process through high-pass and low-pass filter.

$$V_m = \frac{E_{exc}g_{exc} + E_{inh}g_{inh}}{g_{exc} + g_{inh} + g_{leak}}$$

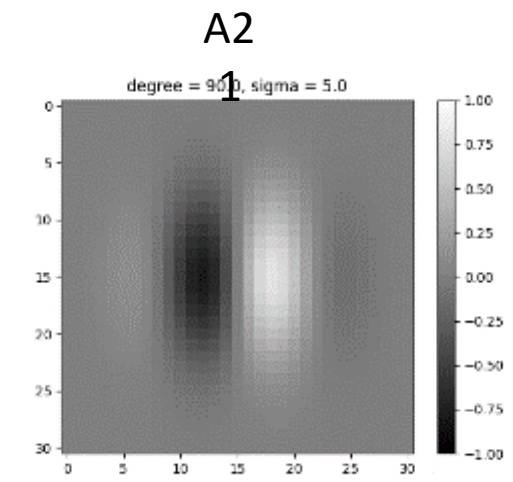
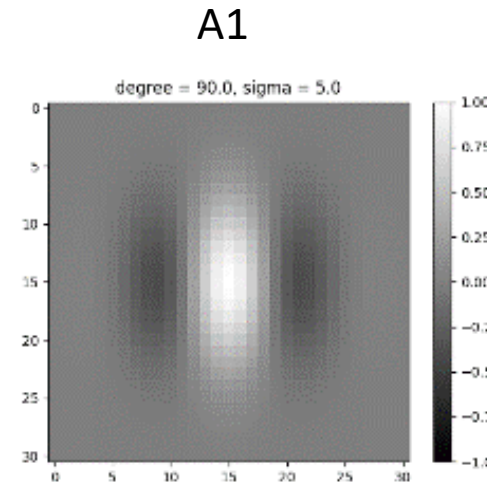
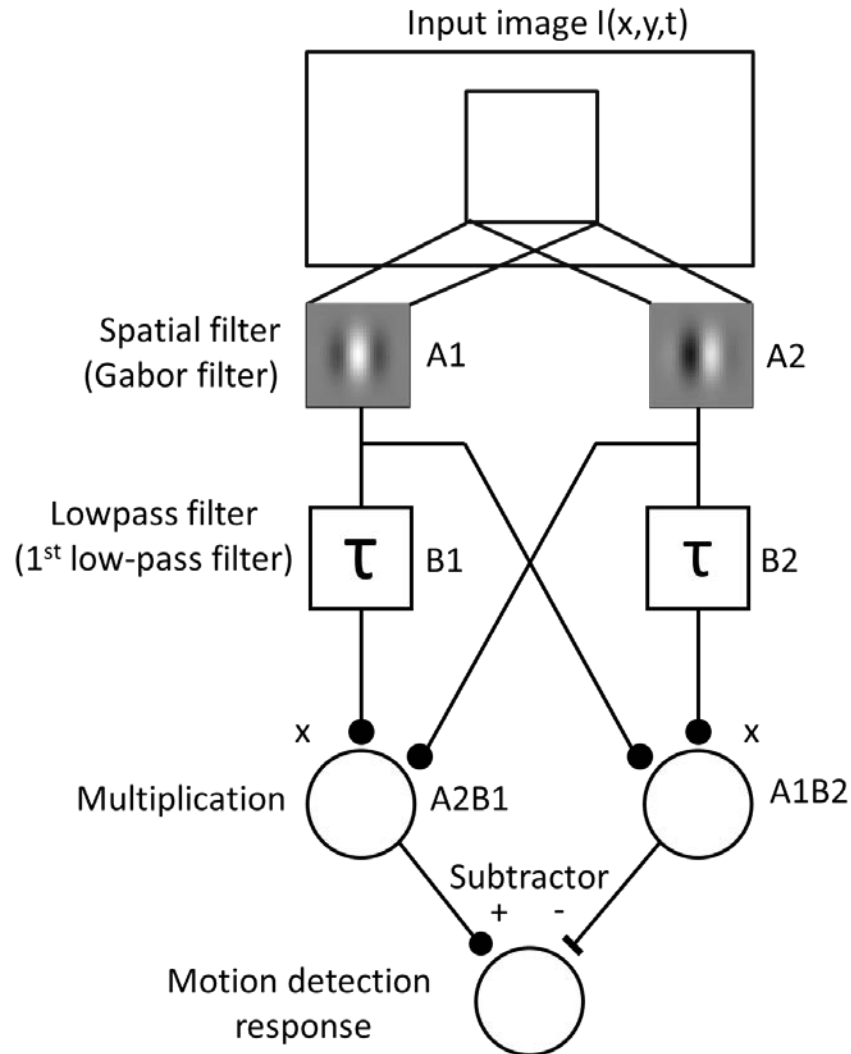


# Spatial-temporal filter Reichardt (STR) model



- (1) Spatial filter with Gabor filter.
- (2) Time-delay by 1st low-pass filter.
- (3) Correlation by multiplication.
- (4) Subtractor to computer motion response.

# Spatial filter – Gabor function



$$g(x, y; \lambda, \theta, \psi, \sigma, \gamma) = \exp\left(-\frac{x'^2 + \gamma^2 y'^2}{2\sigma^2}\right) \cos\left(2\pi \frac{x'}{\lambda} + \psi\right)$$

$\lambda$ : sinusoidal wave

$\theta$ : orientation of Gabor function.

$\psi$ : the phase of sinusoidal function

$\sigma$ : standard deviation of the Gaussian function

$\gamma$ : ellipticity



# Spatial-temporal filter Reichardt (STR) model

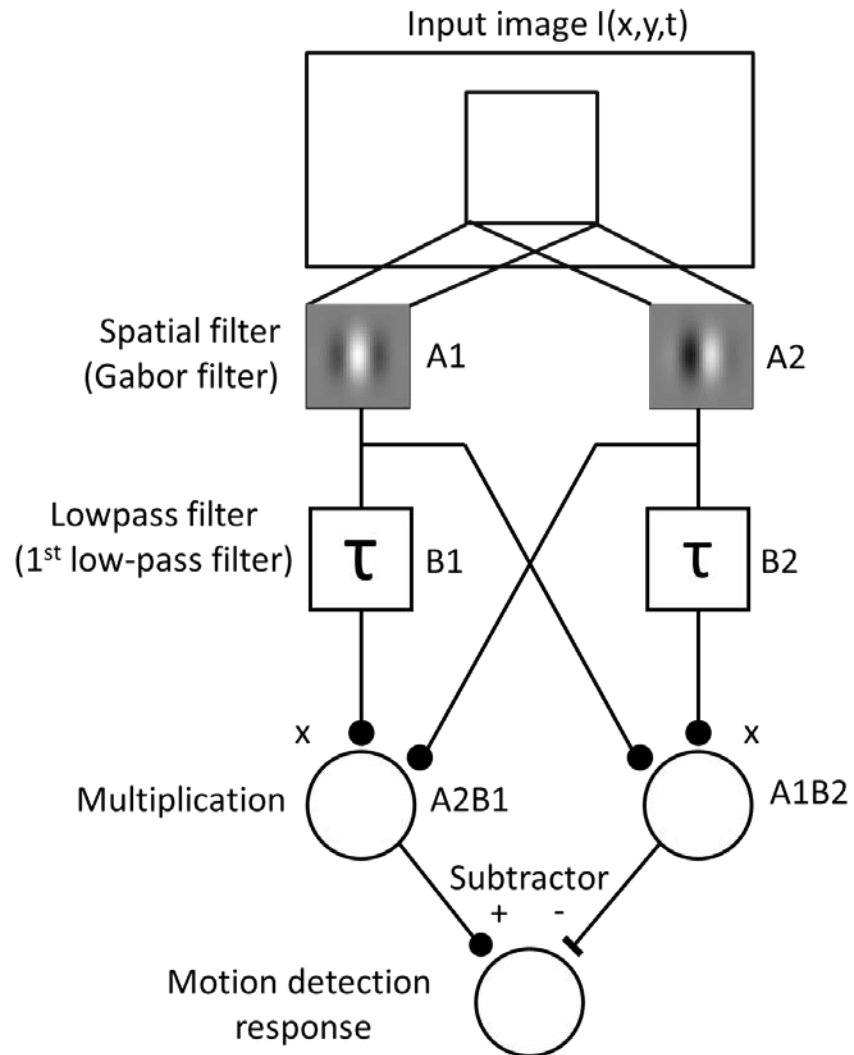


Image processed by Gabor filter

$$A(x, y, t) = I(x, y, t) * g(x, y)$$

temporal filter – 1<sup>st</sup> lowpass filter

$$B(t) = A(t)/\tau + (1/\tau)B(t - 1)$$

Multiplication and Subtractor

$$R(t) = A_2(t) \cdot B_1(t) - A_1(t) \cdot B_2(t)$$

# Design a STR model with velocity selectivity

- Low-pass filter have cutoff frequency

$$f_c = \frac{1}{2\pi\tau_a}$$

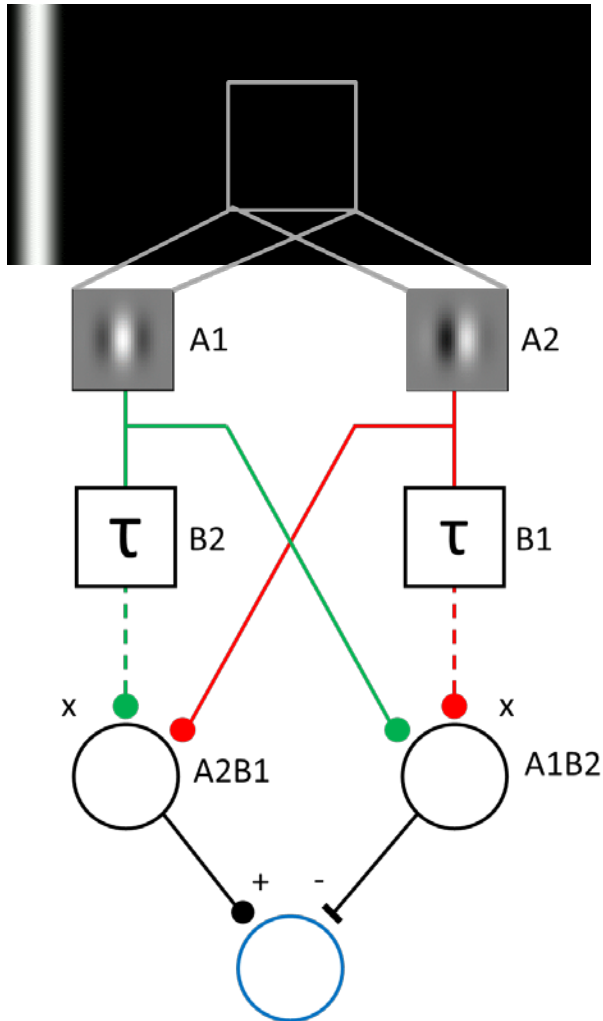
- In digital filter time constat

$$\tau_a = \frac{T_s(1 - \tau)}{\tau}$$

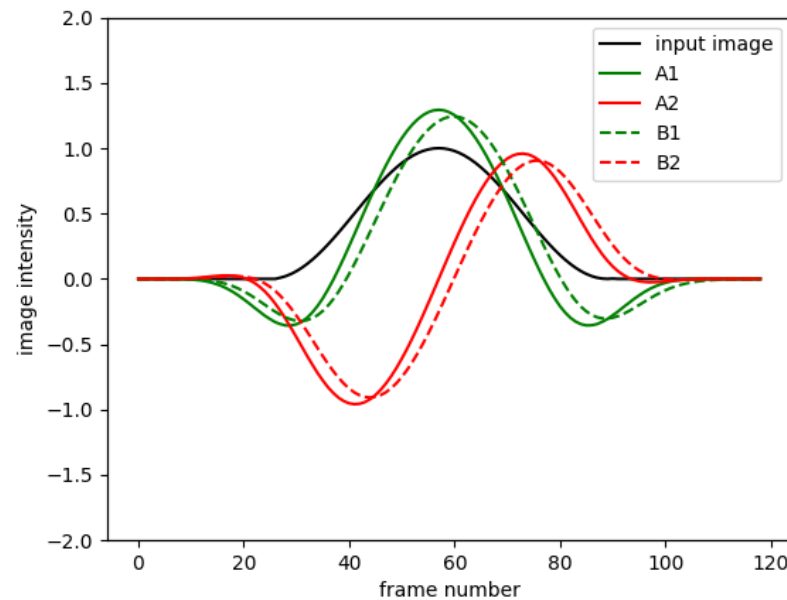
- Velocity  $v = \frac{f_t}{f_x}$  STR model with velocity selectivity  $v = \frac{\lambda_g \tau}{2\pi T_s(1 - \tau)}$

# Internal response and output -Prefer direction

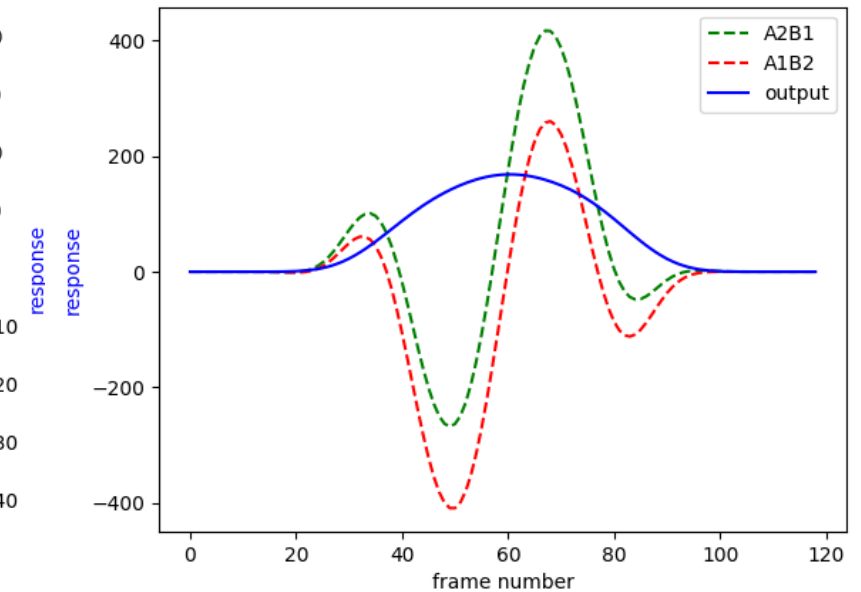
Visual stimuli input



Internal response

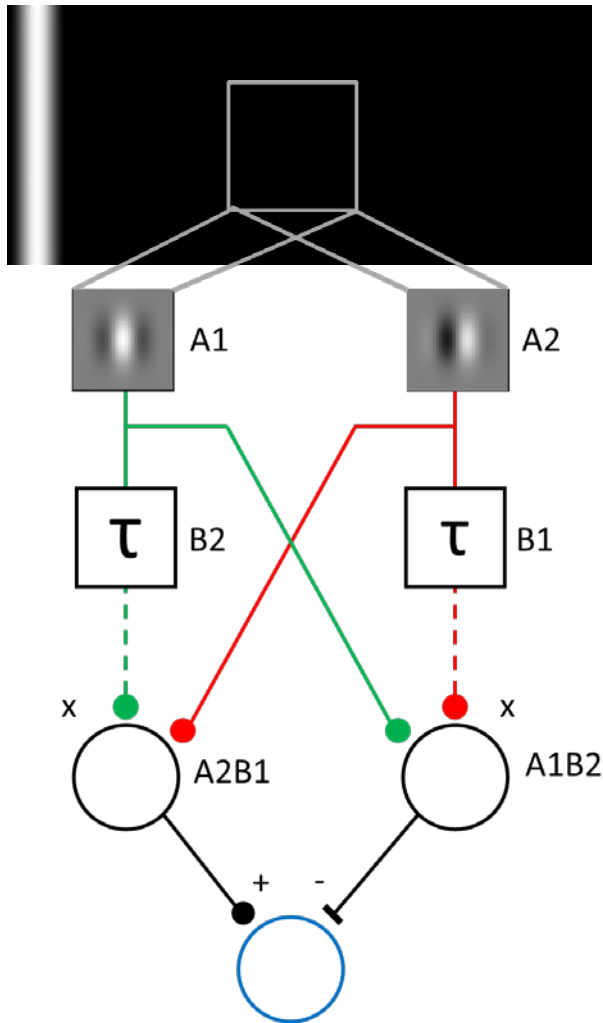


output

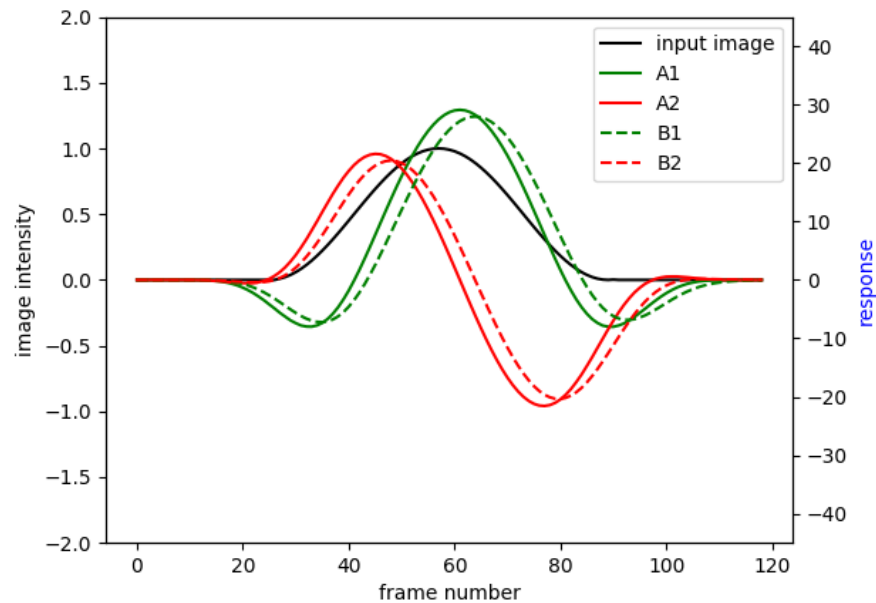


# Internal response and output -null direction

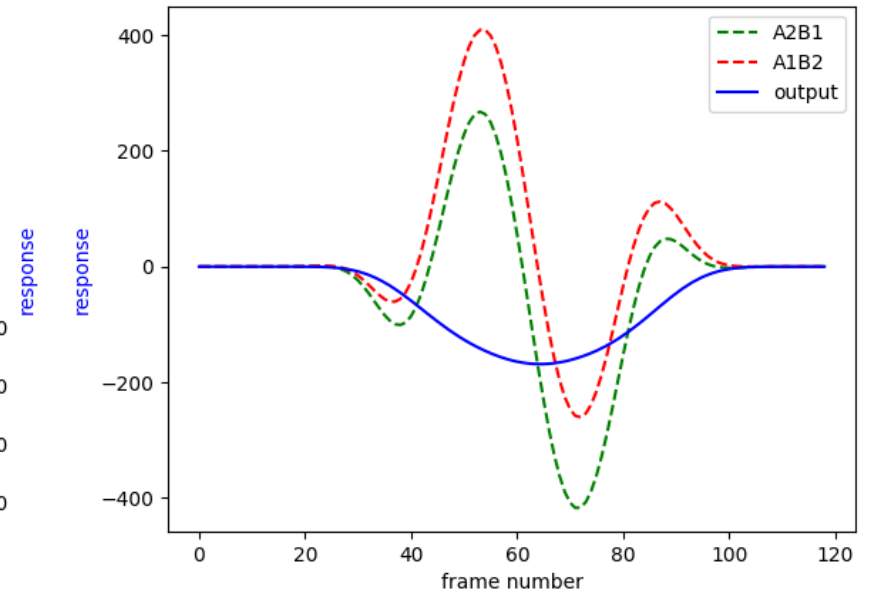
Visual stimuli input



Internal response

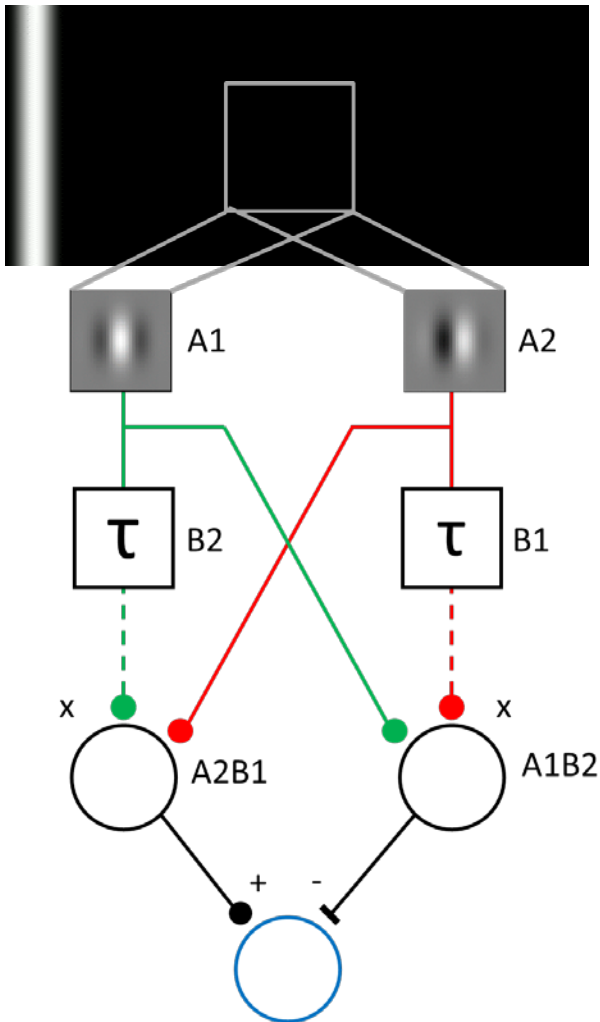


output

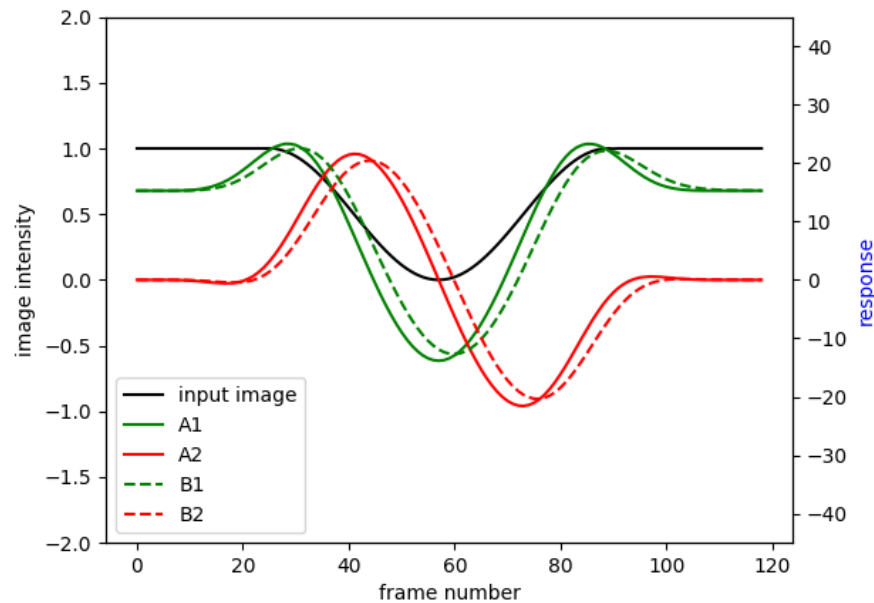


# Internal response and output -Prefer direction

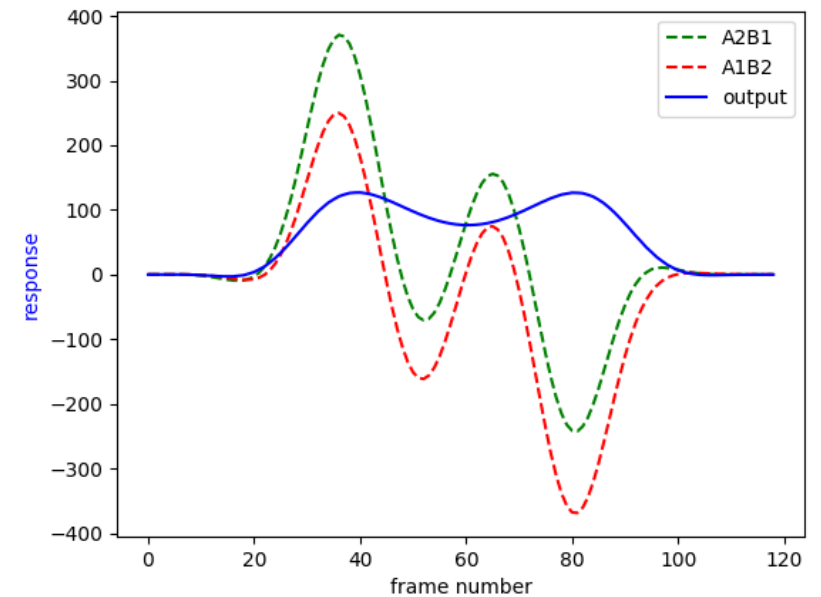
Visual stimuli input



Internal response

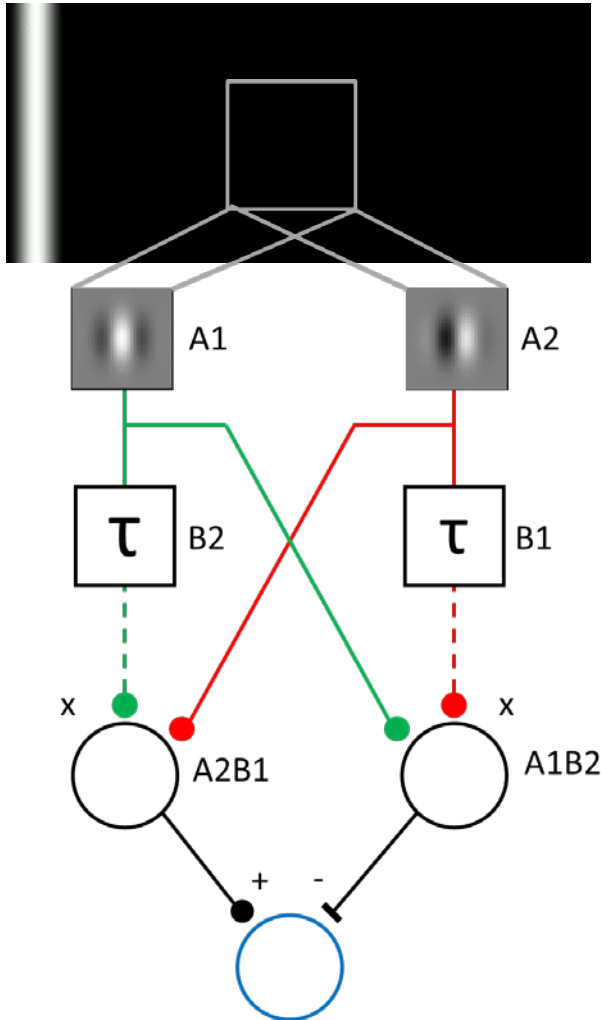


output

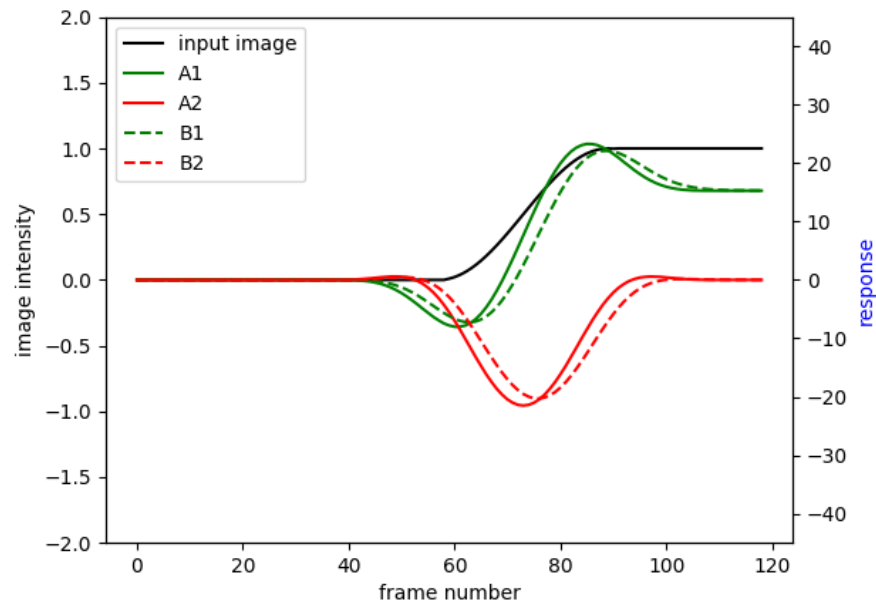


# Internal response and output -Prefer direction

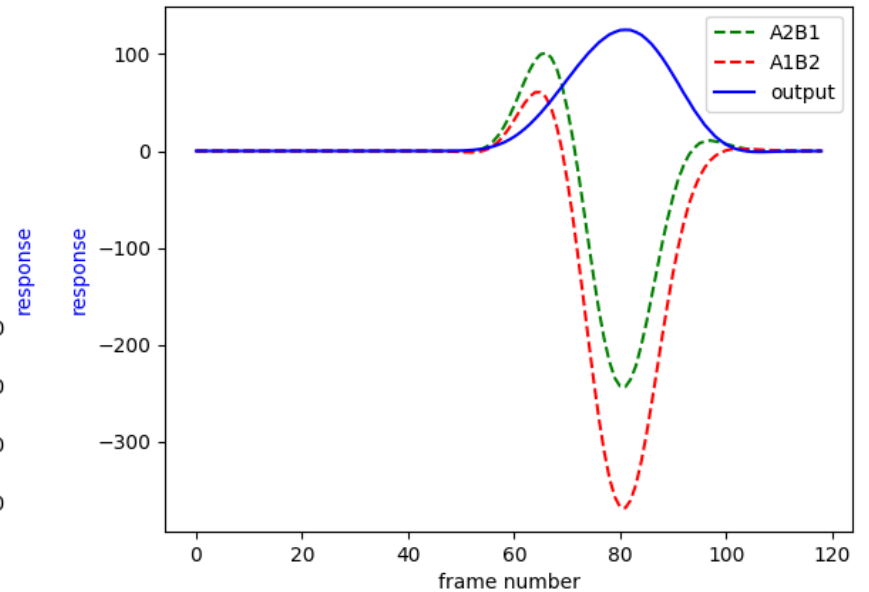
Visual stimuli input



Internal response



output

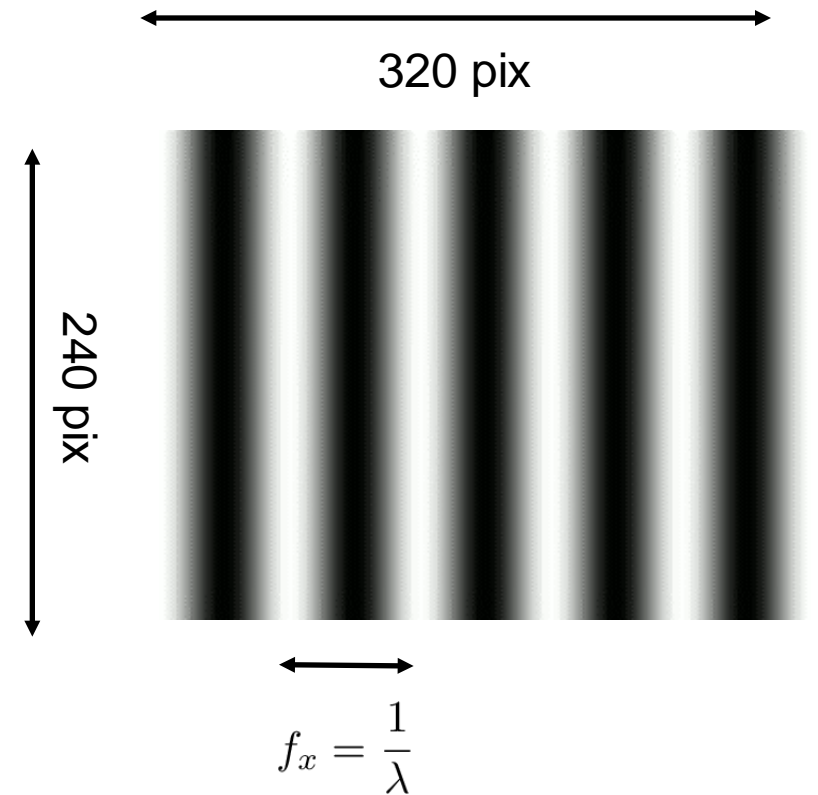


# Visual Stimulus Method

- We apply 320 x 240 sine grating video.
- Velocity (pixel per frame) equals the temporal frequency divided by the spatial frequency.

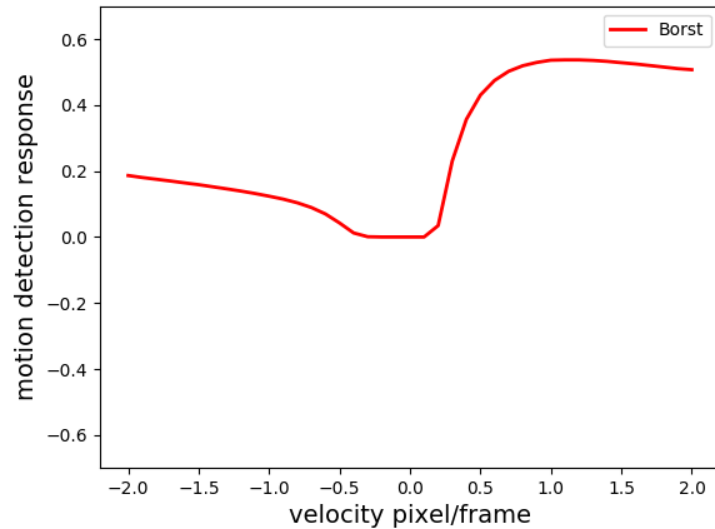
$$v = \frac{f_t}{f_x}$$

	Range
temporal frequency ( $f_t$ )	$2^{-10} \sim 2^{-1}$ (1/frame)
spatial frequency ( $f_x$ )	$2^{-7} \sim 2^{-2}$ (1/pixel)
velocity( $v$ )	$2^{-6} \sim 2^4$ (pixel/frame)

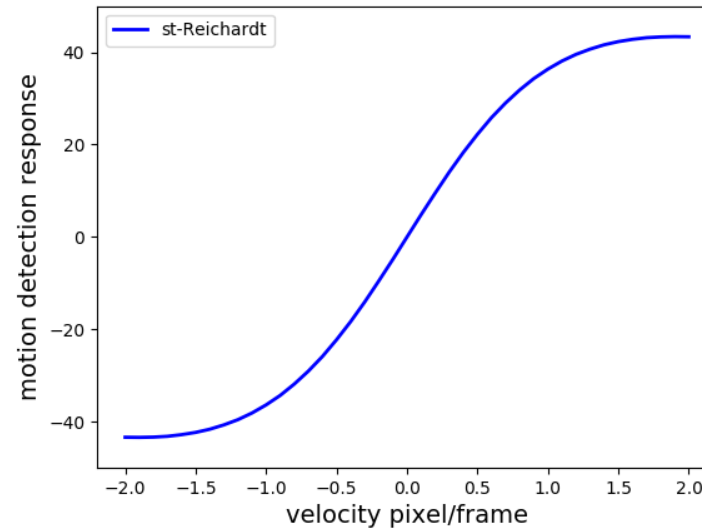


# Linearity of each method

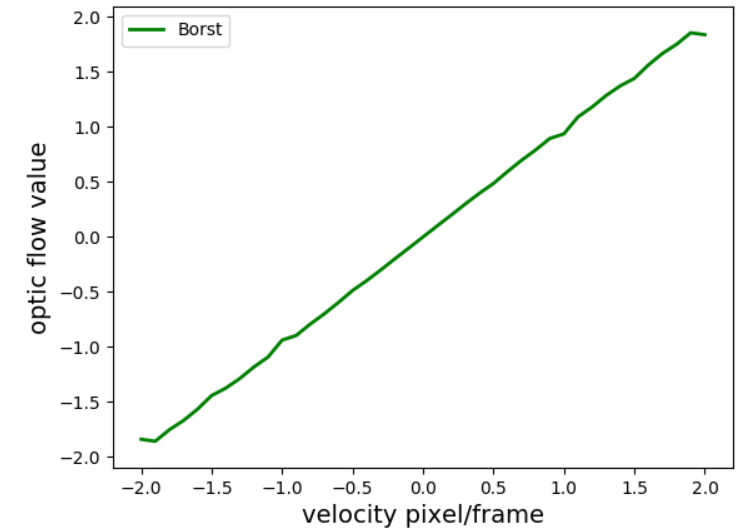
Borst's model



Reichardt model

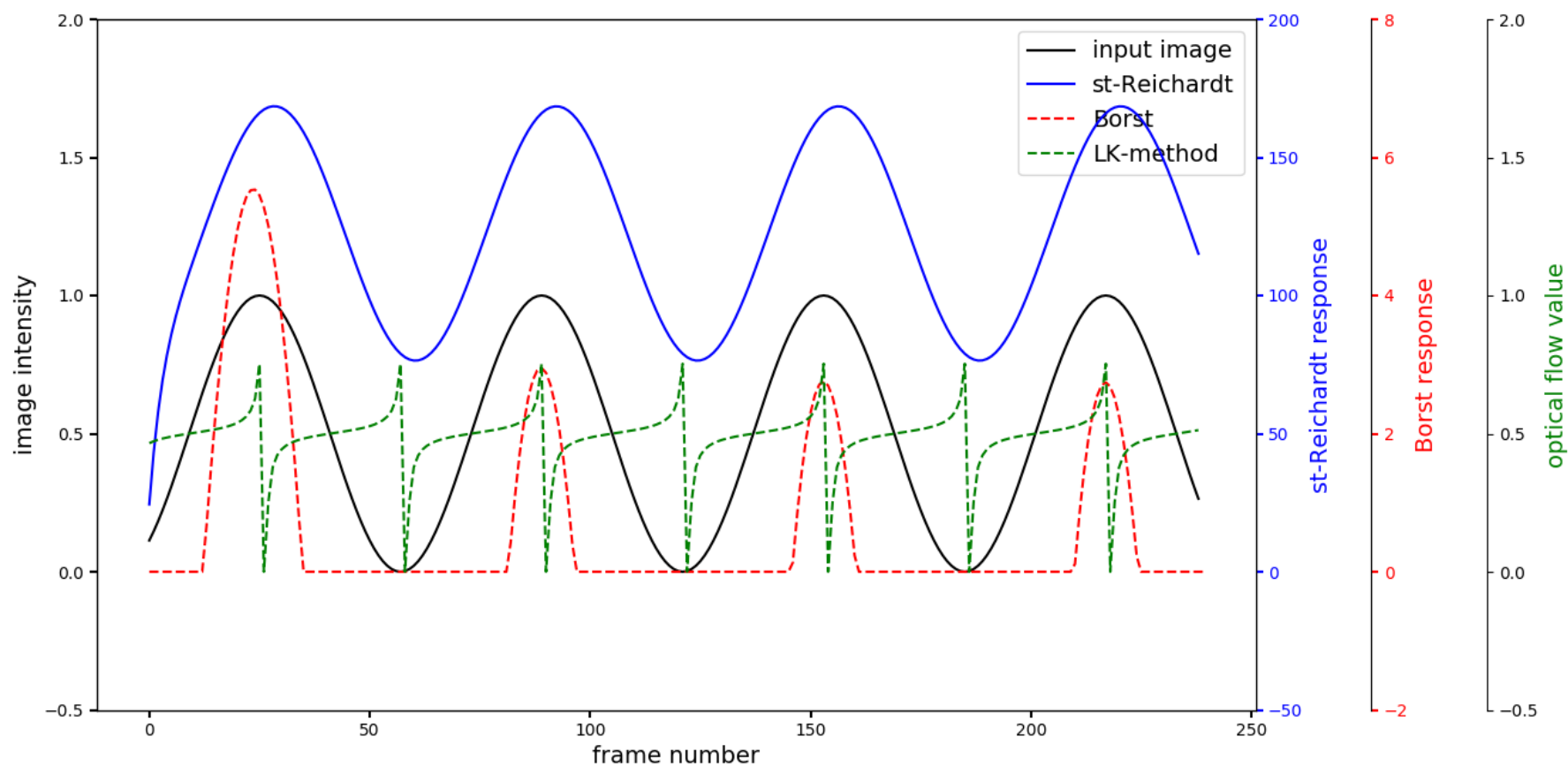


LK-method model





# Response of each method



# Working dynamic range of each method

Borst's model

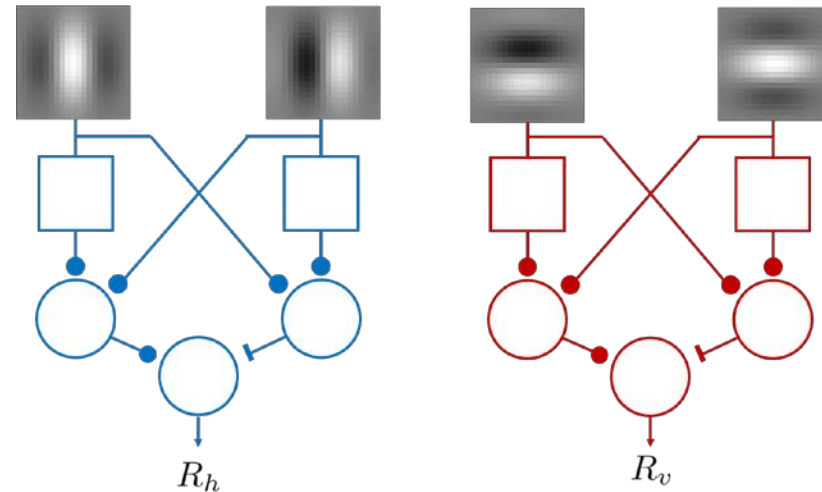
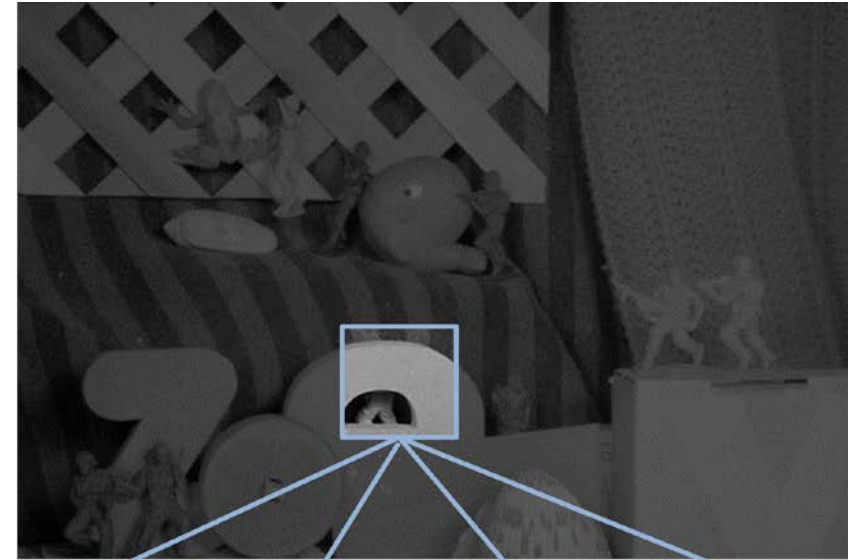
Reichardt model

LK-method model

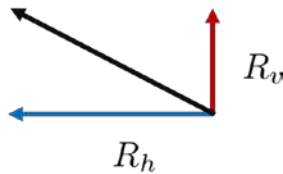
# Velocity selectivity of STR model

# Testing with real image sequence

- Use two STR model to estimate vertical and horizontal motion



Motion estimation

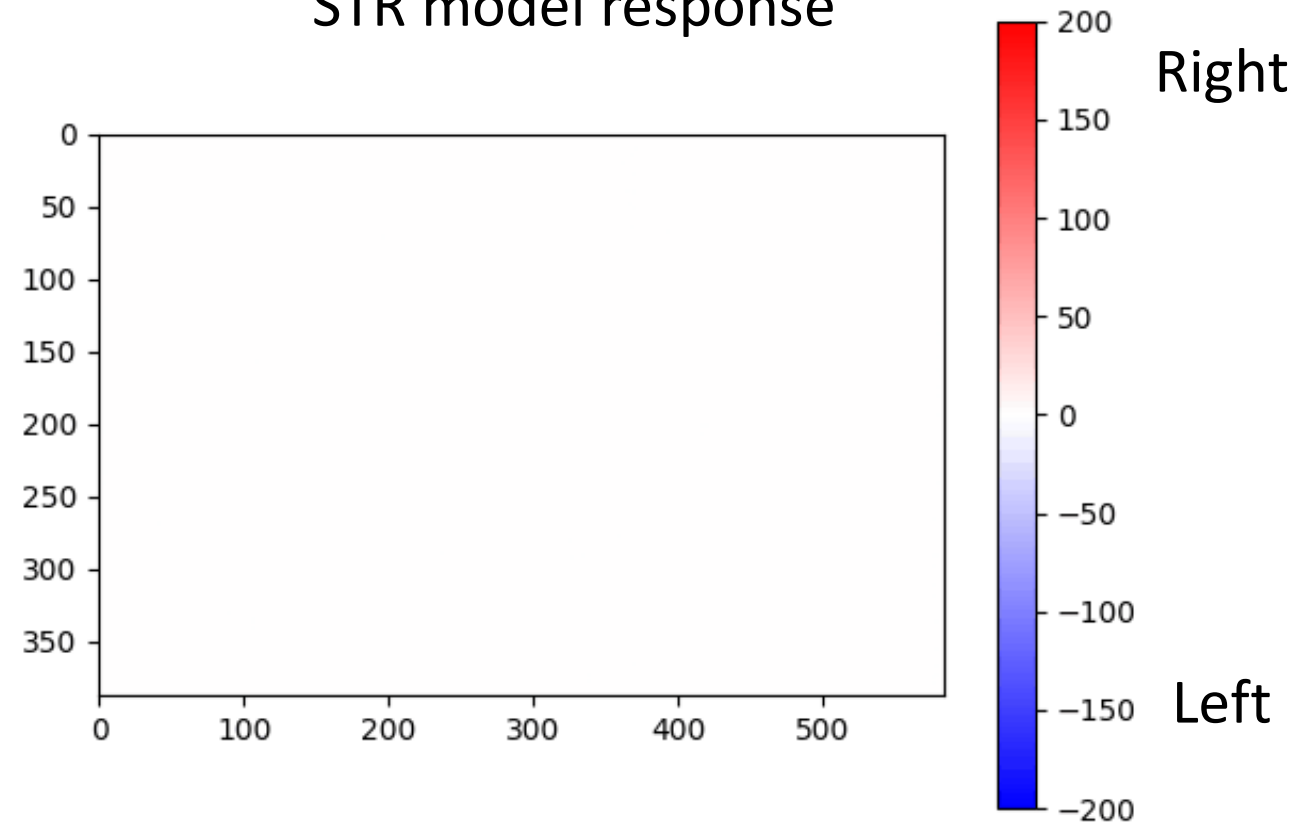


# Motion detection with real image

Original image



STR model response

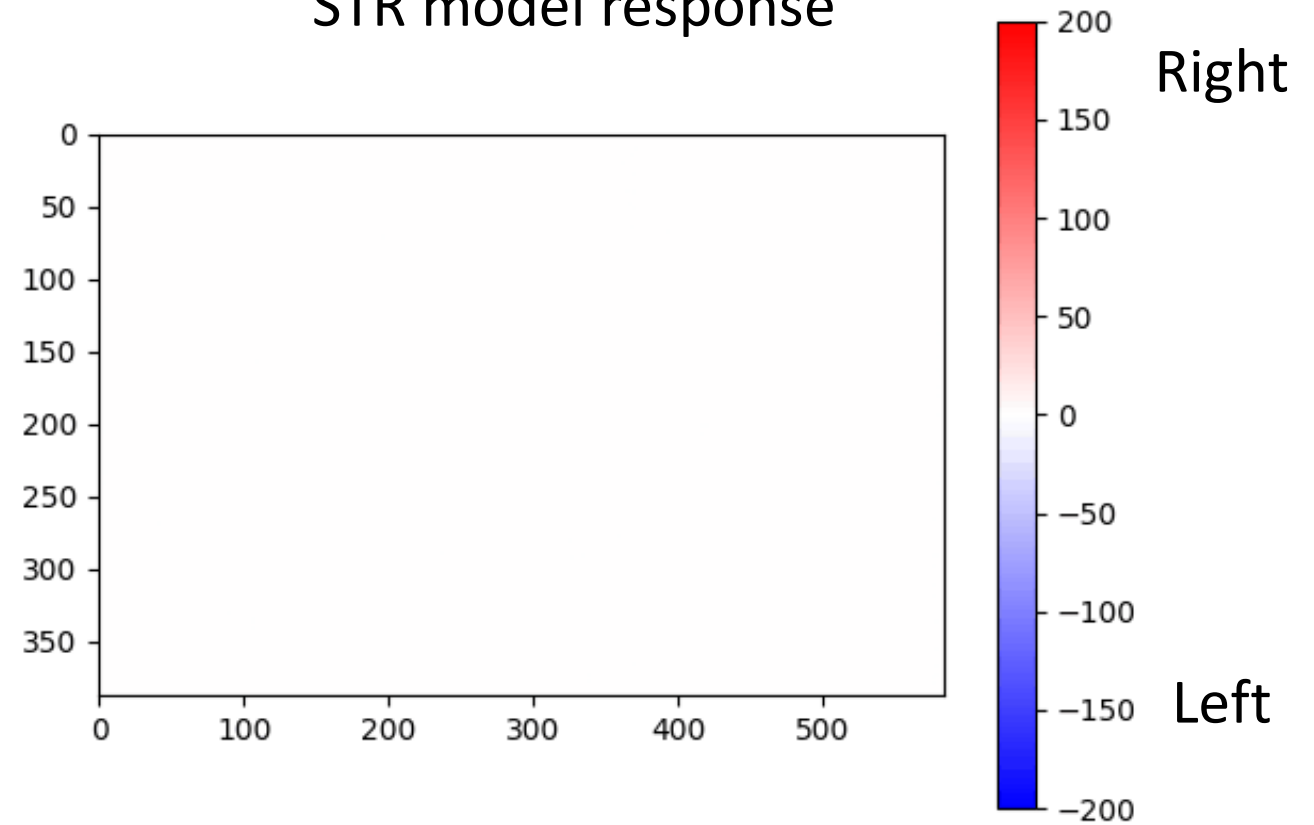


# Motion detection with real image

Original image



STR model response



# Motion detection with real image

Original image



STR model response



# Time complexity analyze

A  $m \times n$  image with window size  $w$

Solution of Lucas-Kanade method:

$$\begin{bmatrix} V_x \\ V_y \end{bmatrix} = \begin{bmatrix} \sum_i I_x^2 & \sum_i I_x I_y \\ \sum_i I_y I_x & \sum_i I_y^2 \end{bmatrix}^{-1} \begin{bmatrix} -\sum_i I_x I_t \\ -\sum_i I_y I_t \end{bmatrix}$$

the time complexity is  $O(5mnw^2)$

For a STR model, calculating Gabor filter with window size  $w$ , the the time complexity is  $O(4mnw^2)$



# Discussion

- Drawback:
  - Brightness contrast effect the accuracy of detection model .
  - Low frame rate cause the distortion
- Different from optical flow, motion detection model response at a range of spatiotemporal frequency.
- Have higher efficiency, suitable parallel computing.

# Acknowledgement



# Thanks for listening!

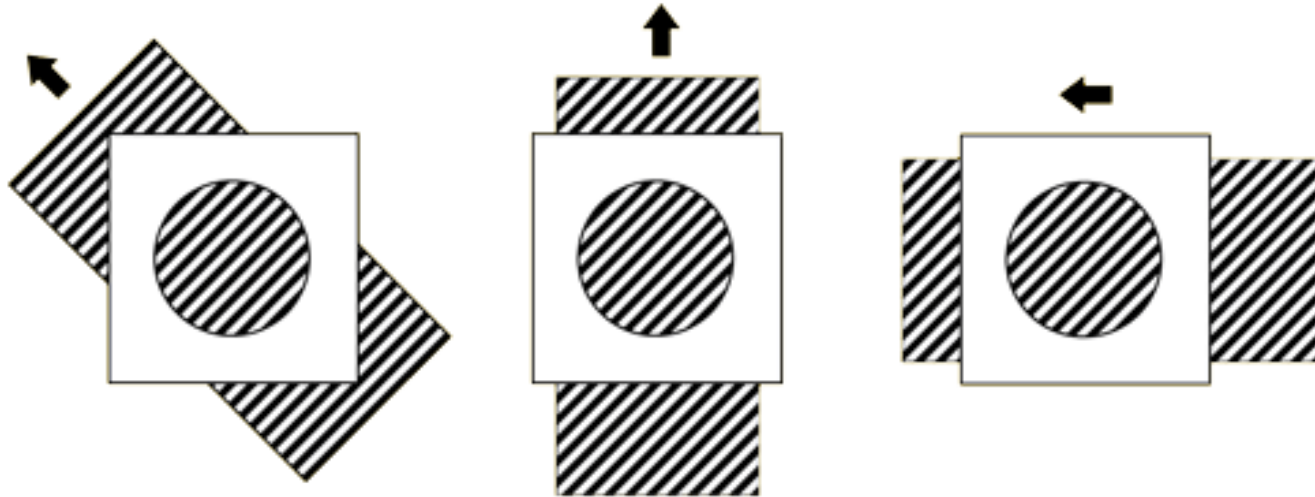
Speaker: Wei-Tse Kao  
Advisor: Chung-Chuan Lo  
Date: 2019.12.23



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# Limitation of optical Flow: Aperture Problem

- The motion of a one-dimensional spatial structure cannot be determined unambiguously if it is viewed through a small aperture.

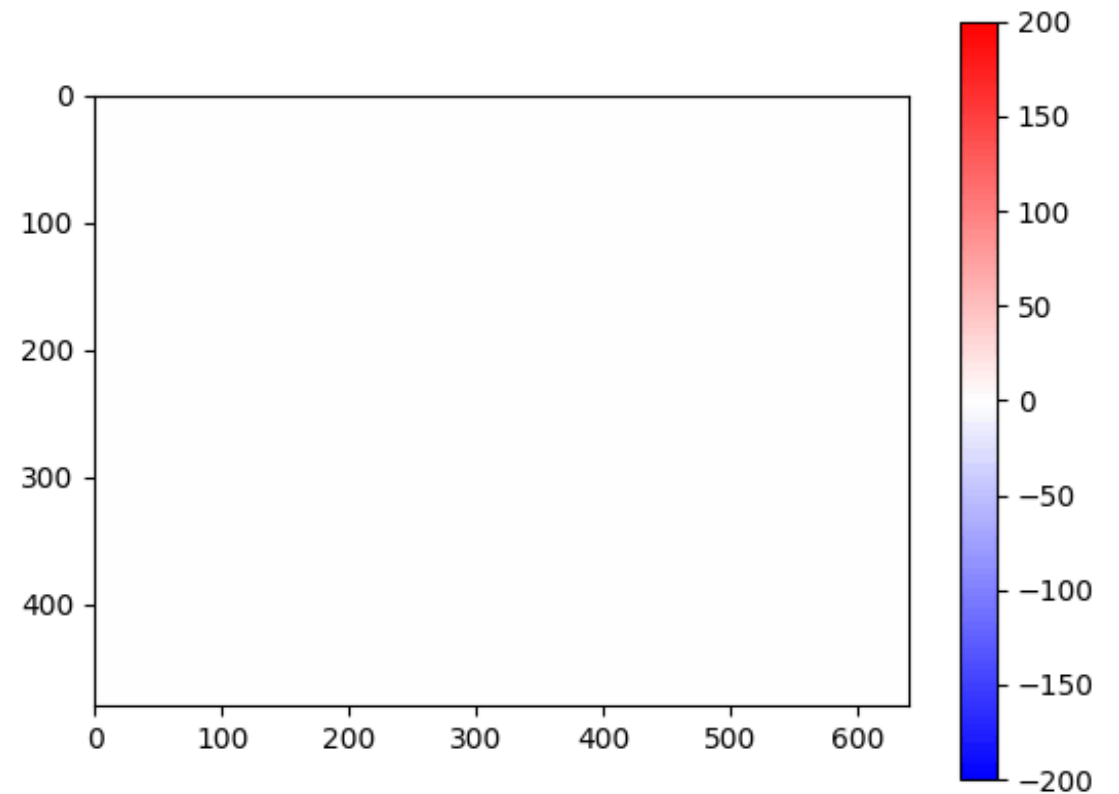


# Motion detection with real image

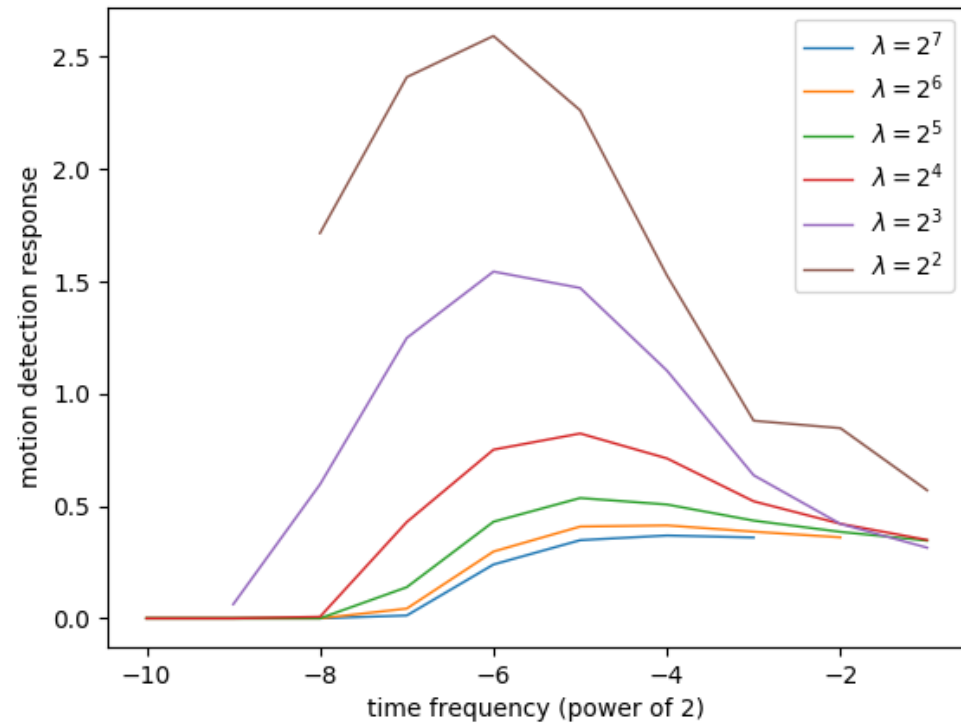
Original image



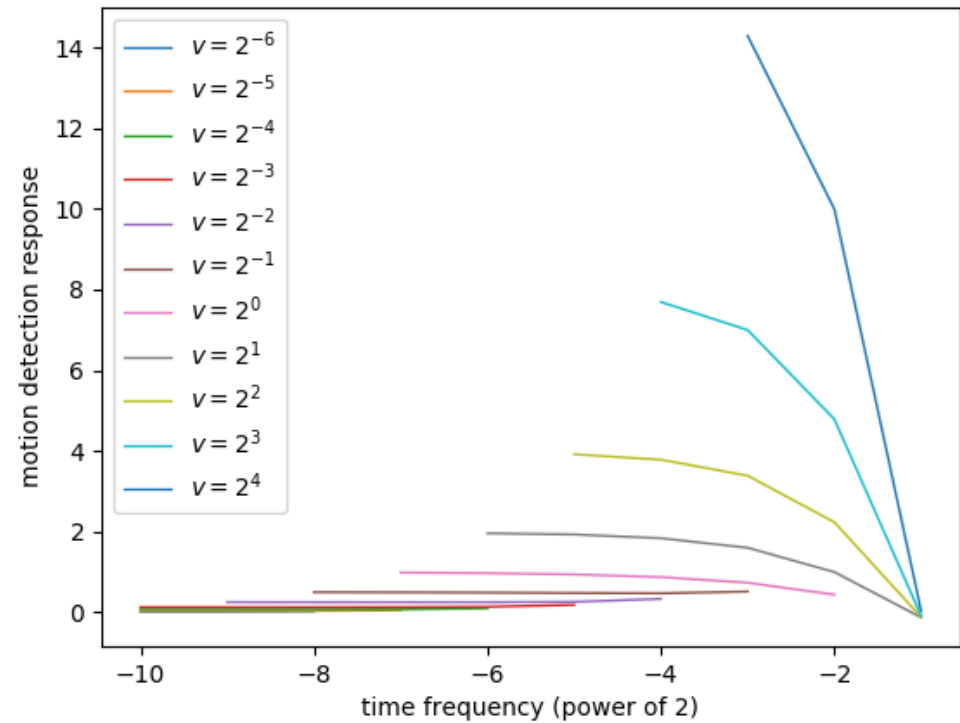
RH model response



# Result 1: Motion Detection V.S. Optical Flow (wavelength)

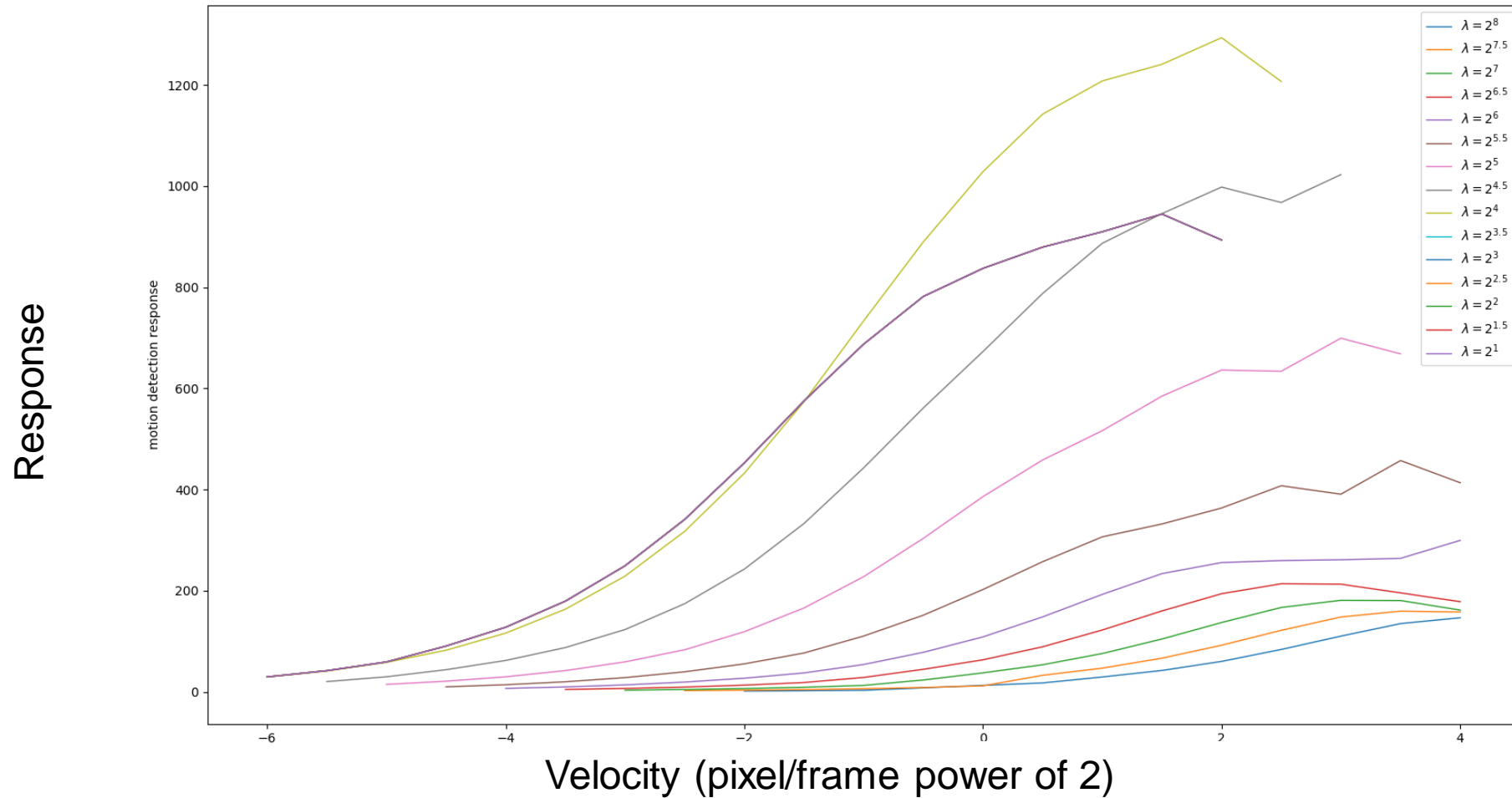


Borst's model



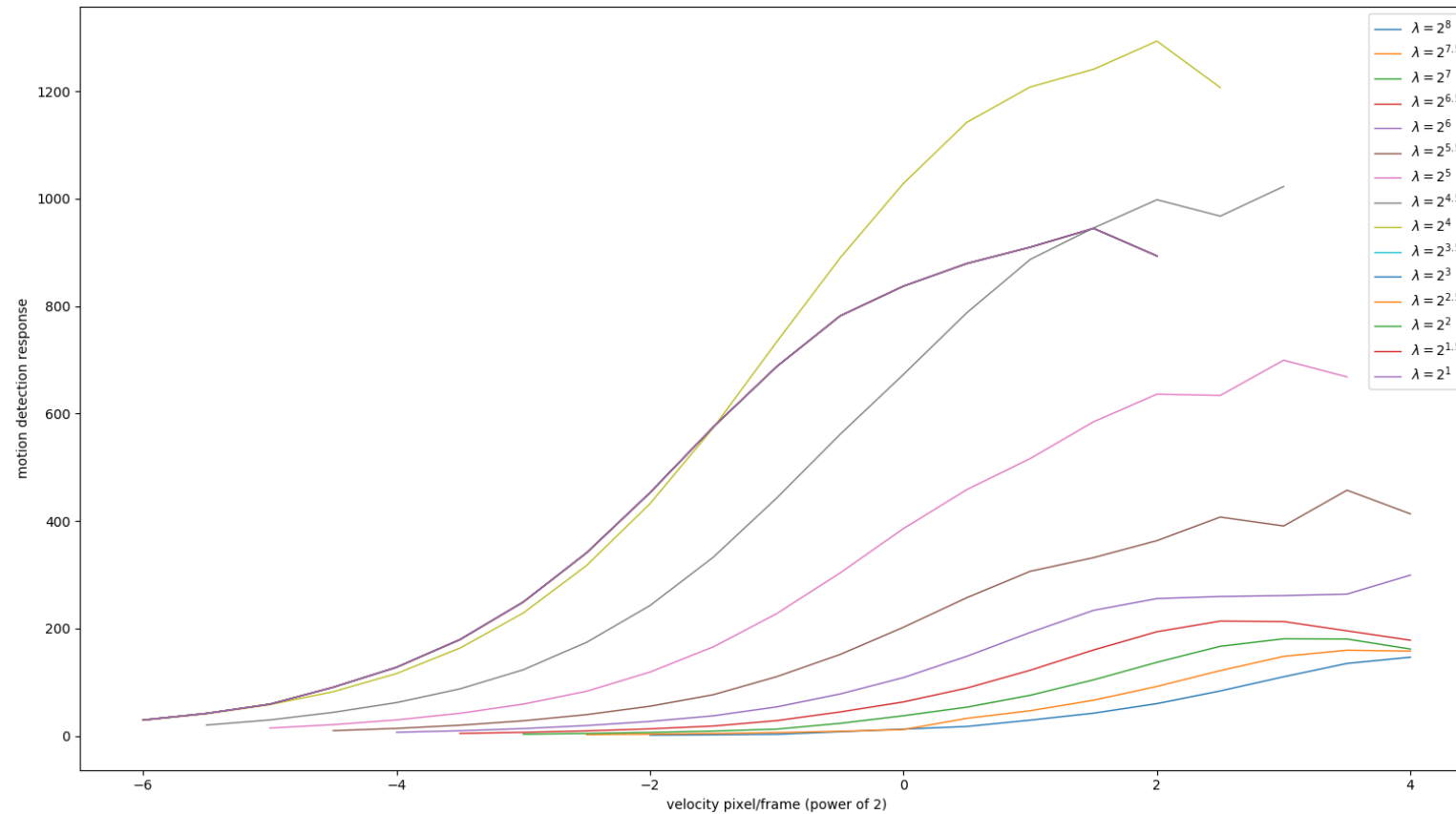
Normal flow

## Result 1: Motion Detection V.S. Optical Flow (wavelength)

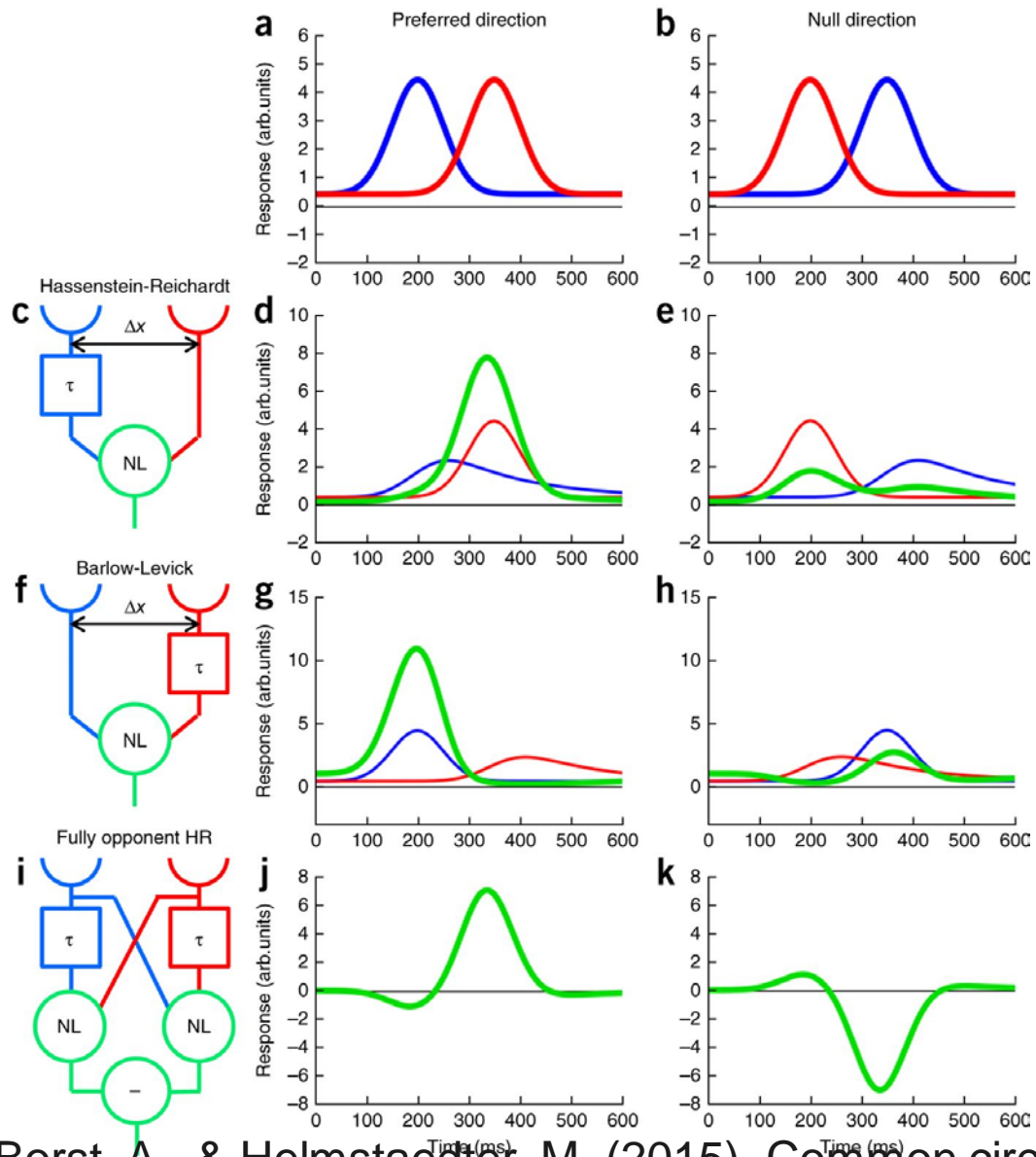




## Result 1: Motion Detection V.S. Optical Flow (wavelength)

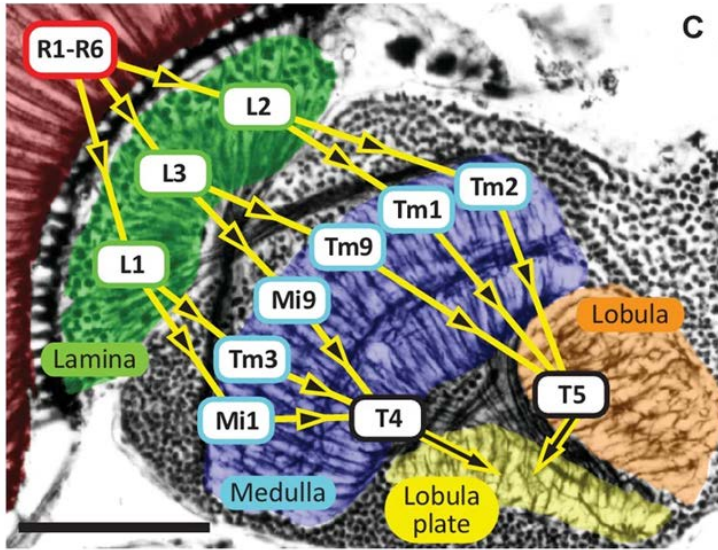




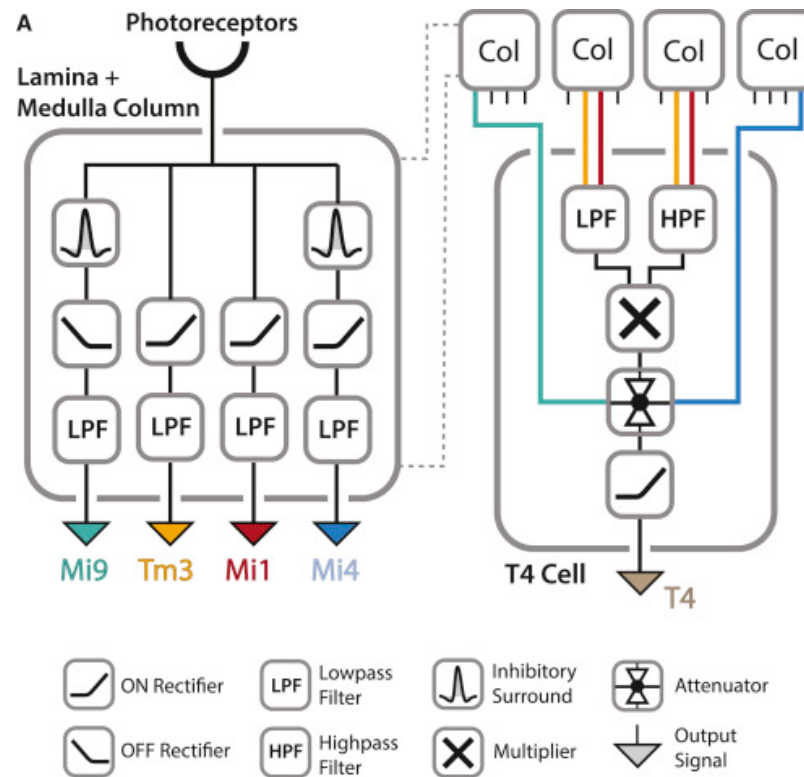


Borst, A., & Helmstaedter, M. (2015). Common circuit design in fly and mammalian motion vision. *nature neuroscience*, 18(8), 1067.

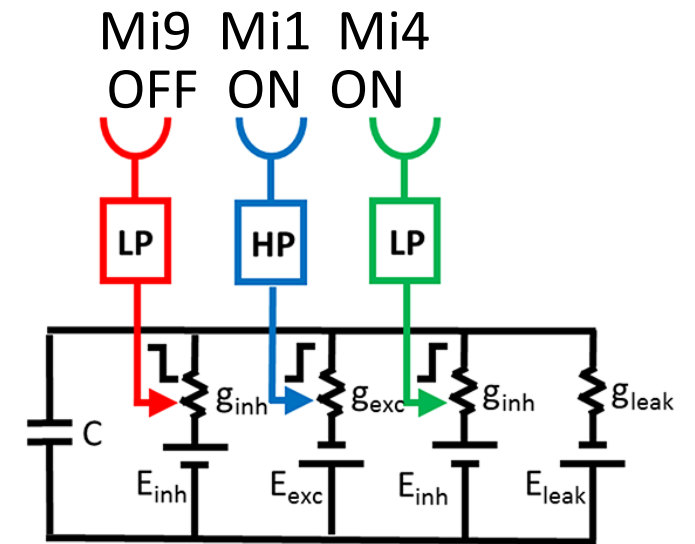
# Motion Detection Model: Borst(2018) and Strother, et al(2017).



Takemura, Shin-ya, et al. *Elife* 6 (2017)



Strother, A. et al. *Neuron*, **14(6)** (2017).



Borst, A. et al. *PLoS computational biol*, **14(6)** (2018).