ADS 503 Final Project

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The Data

Our target variable "Risk Performance" along with the first 13 predictor columns

```
file_loc <- '/Volumes/GoogleDrive/My Drive/503/Project 503/Fico Data/heloc_dataset_v1.csv'
heloc <- read.csv(file_loc)

# sort col names for readability purposes
heloc <- heloc[ , order(names(heloc))]
heloc$RiskPerformance <- as.factor(heloc$RiskPerformance)

knitr::kable(heloc[1:4,c(24,1:13)]) %>%
   kableExtra::kable_styling("striped", full_width = F) %>%
   kableExtra::row_spec(0, angle = -90)
```

Predictor columns 14 to 23

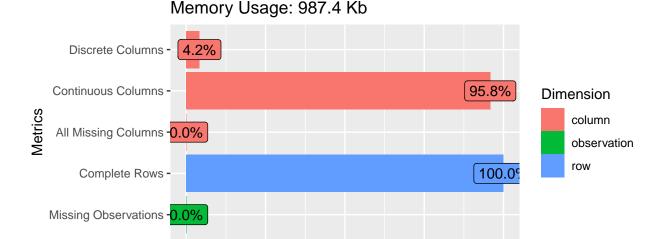
```
knitr::kable(heloc[1:4,c(24,14:23)]) %>%
  kableExtra::kable_styling("striped", full_width = F) %>%
  kableExtra::row_spec(0, angle = -90)
```

EDA

DataExplorer::plot_intro(heloc)

0%

25%



50%

Value

75%

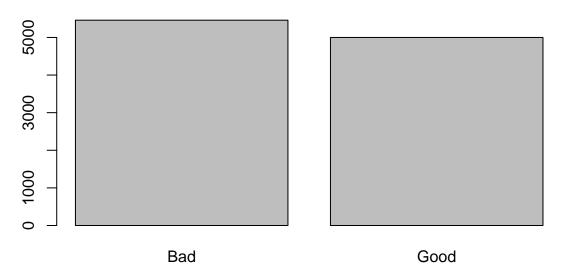
100%

RiskPerformance	AverageMInFile	ExternalRiskEstimate	MaxDelq2PublicRecLast12M	MaxDelqEver	${\it MSinceMostRecentDelq}$	MSinceMostRecentInqexcl7days	MS ince MostRecent Trade Open	${\it MSinceOldestTradeOpen}$	NetFractionInstallBurden	NetFractionRevolvingBurden	NumBank2NatlTradesWHighUtilization	NumInqLast6M	NumInqLast6Mexcl7days
Bad	84	55	3	5	2	0	4	144	-8	33	1	0	0
Bad	41	61	0	8	-7	0	15	58	-8	0	-8	0	0
Bad	24	67	7	8	-7	0	5	66	66	53	1	4	4
Bad	73	66	6	6	76	0	1	169	83	72	3	5	4

RiskPerformance	NumInstallTradesWBalance	NumRevolvingTradesWBalance	${\bf NumSatis factory Trades}$	NumTotalTrades	${\rm NumTrades 60 Ever 2 Derog Pub Rec}^{\circ}$	NumTrades90Ever2DerogPubRec	NumTradesOpeninLast12M	PercentInstallTrades	${\bf Percent Trades Never Delq}$	PercentTradesWBalance
Bad	1	8	20	23	3	0	1	43	83	69
Bad	-8	0	2	7	4	4	0	67	100	0
Bad	2	4	9	9	0	0	4	44	100	86
Bad	4	6	28	30	1	1	3	57	93	91

```
# bar plot of response variable; RiskPerformance
barplot(table(heloc$RiskPerformance),
       main="Plot of Response Variable: RiskPerformance",
       xlab="RiskPerformance")
```

Plot of Response Variable: RiskPerformance



RiskPerformance

```
table(heloc$RiskPerformance)
```

-7

Interesting to see that 13,534 values are -9 (no history)

-8 ## 13534 6114 6519

Bad Good

##

-9

```
## 5459 5000
A 51:47 split! Nearly a 50:50 balance!
# copy heloc data fore explority purposes
xplore_df <- data.frame(heloc)</pre>
noY_bool <- names(xplore_df) != 'RiskPerformance'</pre>
xplore_df <- data.frame(xplore_df[, noY_bool])</pre>
# No credit history
bool1 <- xplore_df == -9</pre>
# No activity in the last year
bool2 <- xplore_df == -8
# No soft hits (those with a O assigned have had soft hits)
bool3 <- xplore_df == -7</pre>
bool0 <- bool1 | bool2 | bool3
table(xplore_df[bool0])
```

```
xplore_df <- data.frame(heloc)
bool1 <- xplore_df == -9

xplore_df[bool1] <- 0
nines_across_d_board <- xplore_df[rowSums(xplore_df[,noY_bool]) == 0,]
dim(nines_across_d_board)[1]</pre>
```

[1] 588

We have 588 rows that are complete -9 across all features.

```
table(nines_across_d_board$RiskPerformance)
```

```
## Bad Good
## 323 265
```

Interesting to see the data setregarding -9s across all features has a 55:45 split. Taking a chance on anything without any background knowledge is a 50/50 split, this was probably intentionally baked into the HELOC data set to skew results in some way.

```
# the definition of -7 and -8 are similar though not identical
xplore_df <- data.frame(heloc)
bool1 <- xplore_df == -8
bool2 <- xplore_df == -7

xplore_df[bool1] <- NA
xplore_df[bool2] <- NA

inactive_records <- xplore_df[rowSums(is.na(xplore_df)) > 0,]
table(inactive_records$RiskPerformance)
```

Bad Good ## 3574 3792

As we see, the dataset has a nearly balanced mixture of those with an inactive credit history; though this lens is through a macroscope and not further dividing the data based on certain features which will be shown via histograms and box plots.

```
bool1 <- inactive_records == NA
inactive_records[bool1] <- 0
inactive_records <- inactive_records[,noY_bool]
inactive_records <- inactive_records[(rowSums(inactive_records)) == 0,]
# dim(inactive_records)[1]
# unable to figure out how to fix all NA dataframe.
# Code should return a dataframe dim of 0,23.</pre>
```

*Note: Cell above changes inactive_records returns a dataframe filled with NAs but with the same structure as HELOC. After further analysis, we concluded there are no records completely filled with -8s or -7s.

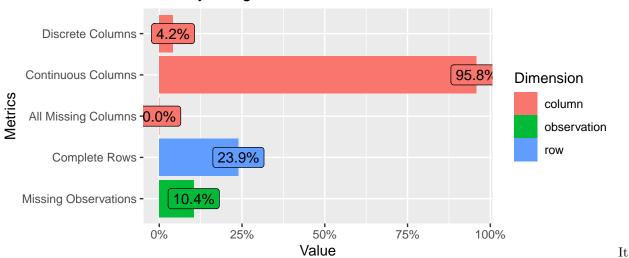
This makes sense, for the fact that it is highly likely that people with such records have a mature financial history, while those with a -9 are those starting their financial history; meaning that it is more likely for an individual with a -9 to have -9s across the board.

Data Pre-Processing

We are going to preprocess the data to get quality data insights.

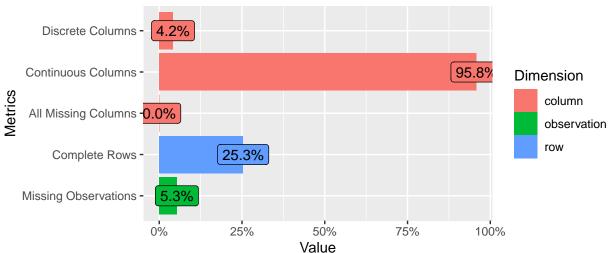
```
# -9 = No Credit History
# -8 and -7 = No recent activity
heloc[heloc == -9] <- NA
heloc[heloc == -8] <- NA
heloc[heloc == -7] <- NA
DataExplorer::plot_intro(heloc)</pre>
```

Memory Usage: 987.4 Kb



appears that only 76.1% of our data had one or more predictors had a -9,-8,-7. Thus the following code removes all missing values that span across all columns.

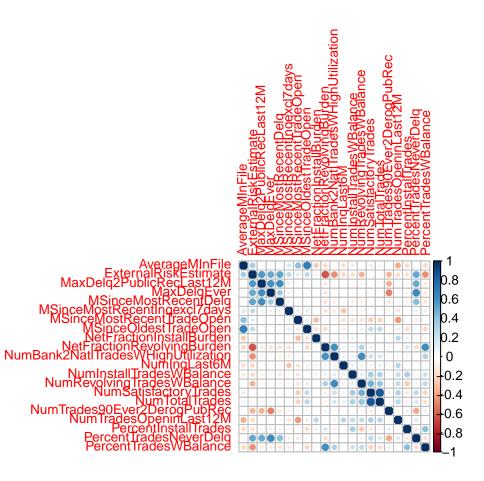
Memory Usage: 932.3 Kb



```
# create training indices
set.seed(3)
```

```
heloc_training <- caret::createDataPartition(heloc_No_NA$RiskPerformance,
                                                list=FALSE)
# training/set sets
heloc_train <- heloc_No_NA[heloc_training, ]</pre>
heloc_test <- heloc_No_NA[-heloc_training, ]</pre>
# knn imputation
heloc_impute <- caret::preProcess(heloc_train,
                                    method = 'knnImpute')
heloc_train <- stats::predict(heloc_impute,
                                newdata=heloc_train)
heloc_test <- stats::predict(heloc_impute,</pre>
                              newdata=heloc_test)
# remove highly correlated predictors
high_corr <- caret::findCorrelation(stats::cor(heloc_train[, -24]),
                                      0.85)
# removal of high cor predictors
heloc_train <- heloc_train[, -(high_corr)]
heloc_test <- heloc_test[, -(high_corr)]</pre>
names(heloc_test[high_corr])
## [1] "NumTradesOpeninLast12M"
                                    "NumInstallTradesWBalance"
We keep the heloc_train/test dataframes for formula based functions.
no_risk_bool <- names(heloc_train) != 'RiskPerformance'</pre>
\# x = predictors
heloc train x <- heloc train[,no risk bool]
heloc_test_x <- heloc_test[,no_risk_bool]</pre>
# y = response/target
heloc_train_y <- heloc_train[,'RiskPerformance']</pre>
heloc_test_y <- heloc_test[,'RiskPerformance']</pre>
```

EDA

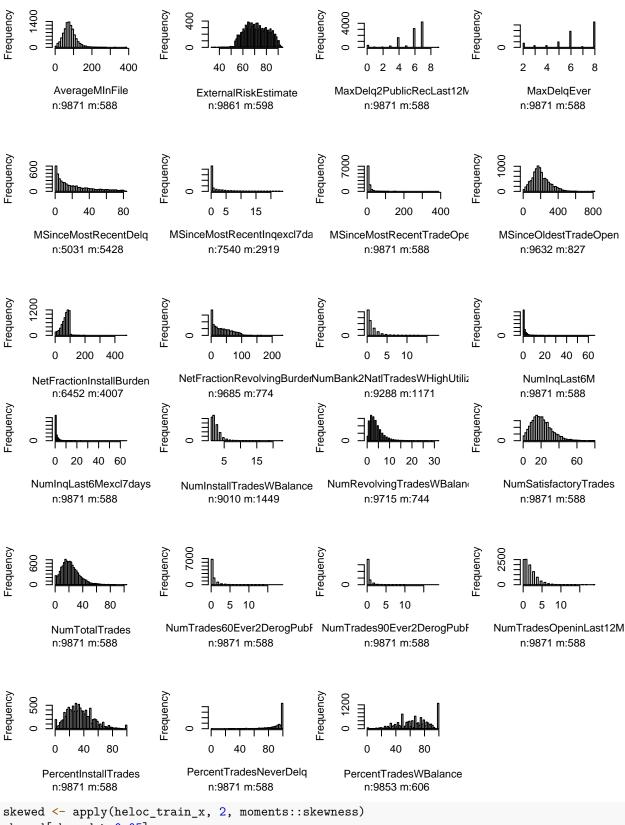


Correlation Plot

Histograms

Overall w/out imputation

```
# histograms to view predictor variable frequencies
par(mfrow=c(3,4))
Hmisc::hist.data.frame(heloc[,1:23])
```



skewed[skewed > 0.05]

##

AverageMInFile

MSinceMostRecentDelq

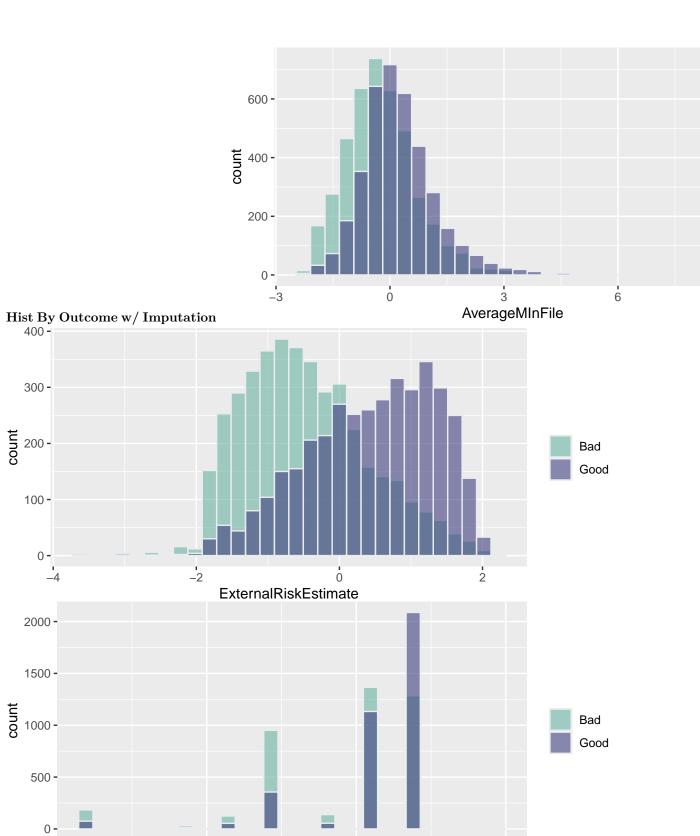
```
0.1609974
##
                             0.9496409
##
         MSinceMostRecentInqexcl7days
                                                 MSinceMostRecentTradeOpen
##
                             2.3532412
                                                                   7.2717628
##
                MSinceOldestTradeOpen
                                                NetFractionRevolvingBurden
##
                             0.7011420
                                                                   0.6041554
## NumBank2NatlTradesWHighUtilization
                                                               NumInqLast6M
##
                             2.5735333
                                                                   6.8037482
             NumInstallTradesWBalance
                                                {\tt NumRevolvingTradesWBalance}
##
##
                             2.6761977
                                                                   1.7068060
                {\tt NumSatisfactoryTrades}
                                                             NumTotalTrades
##
##
                             0.7914751
                                                                   0.9172071
          NumTrades90Ever2DerogPubRec
##
                                                     NumTradesOpeninLast12M
                             5.3998292
                                                                   1.4957987
##
##
                  PercentInstallTrades
##
                             0.6749753
skew_count <- length(skewed[skewed > 0.05])
cat('We have', skew_count,'skewed variables.')
```

We have 15 skewed variables.

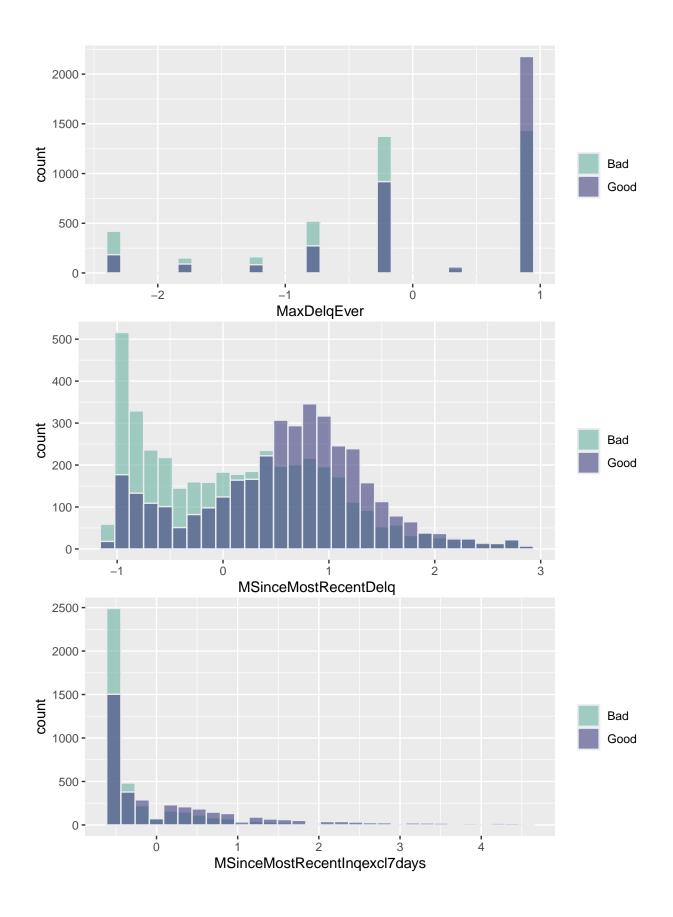
```
# Deselect Bool Outcome/Response/Target variable
no_risk_bool <- names(heloc_train) != 'RiskPerformance'

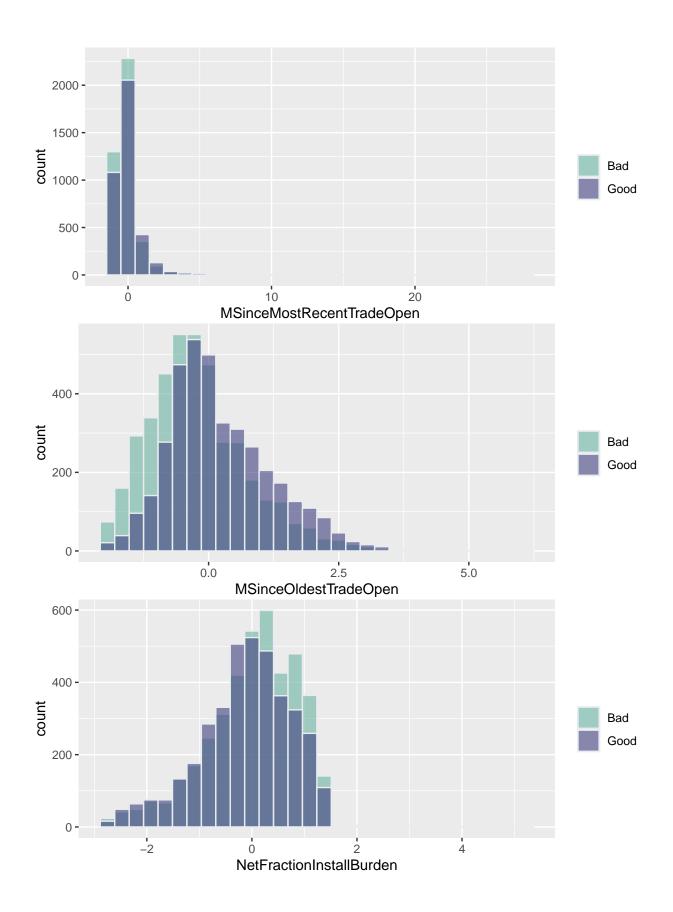
# heloc_imputed_full_set <- dplyr::as_tibble(heloc_imputed_full_set)
heloc_ifs_names <- colnames(heloc_train[,no_risk_bool])

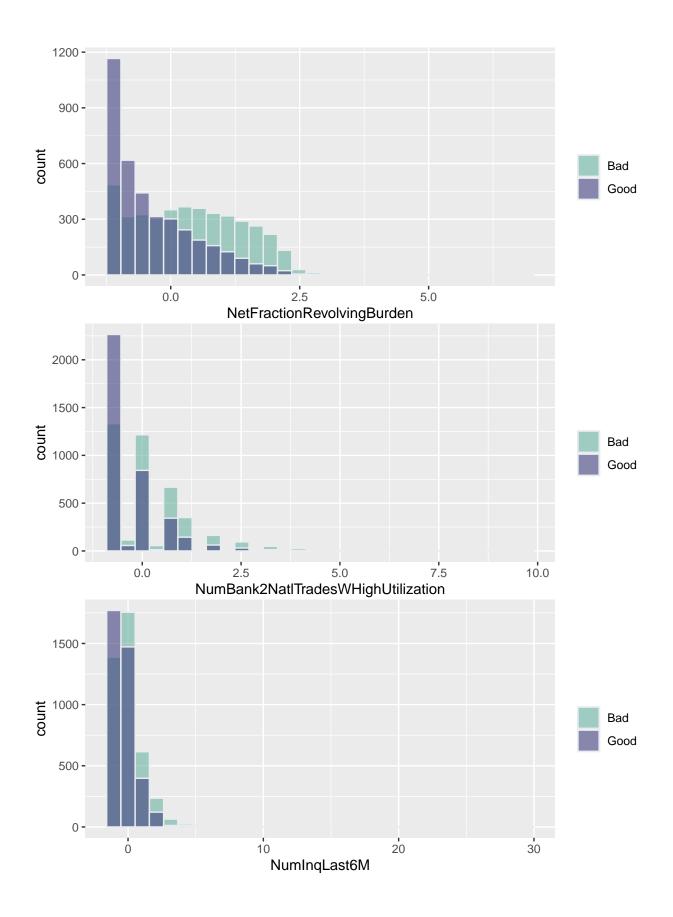
# empty list to gather all
plot_list <- list()
for (name in heloc_ifs_names){
    p <- heloc_train %>%
        ggplot( aes(x=heloc_train[,name], fill=RiskPerformance)) +
        geom_histogram( bins=30, color="#e9ecef", alpha=0.6, position = 'identity') +
        scale_fill_manual(values=c("#69b3a2", "#404080")) +
        xlab(name) +
        labs(fill="")
    print(p)
}
```

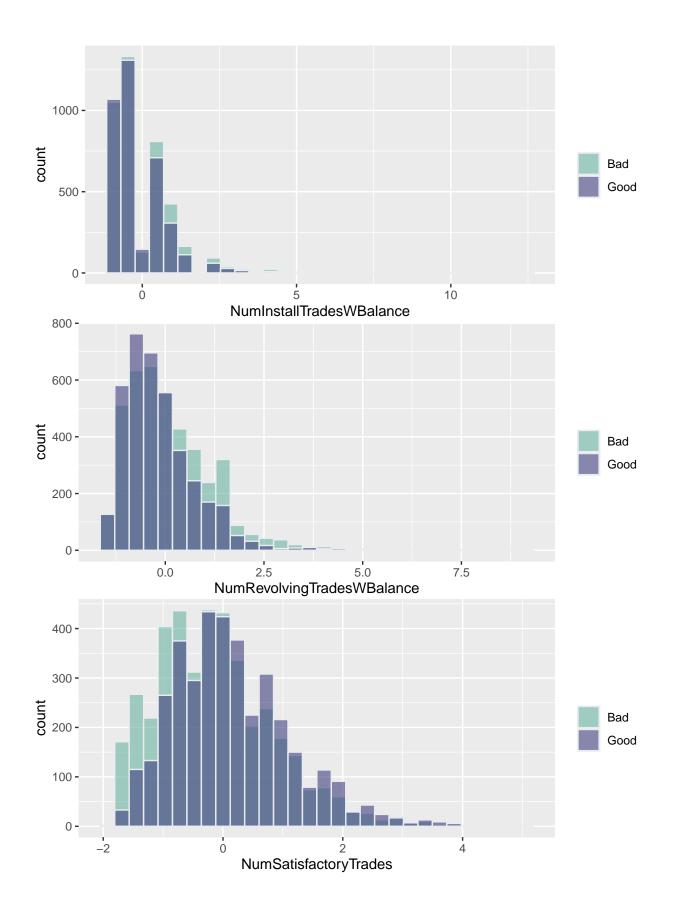


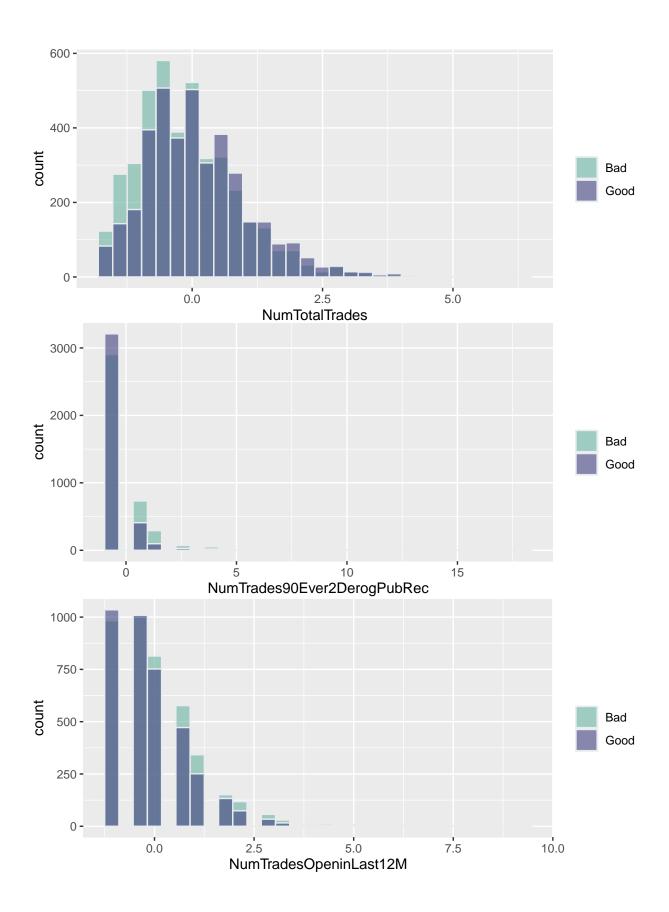
MaxDelq2PublicRecLast12M

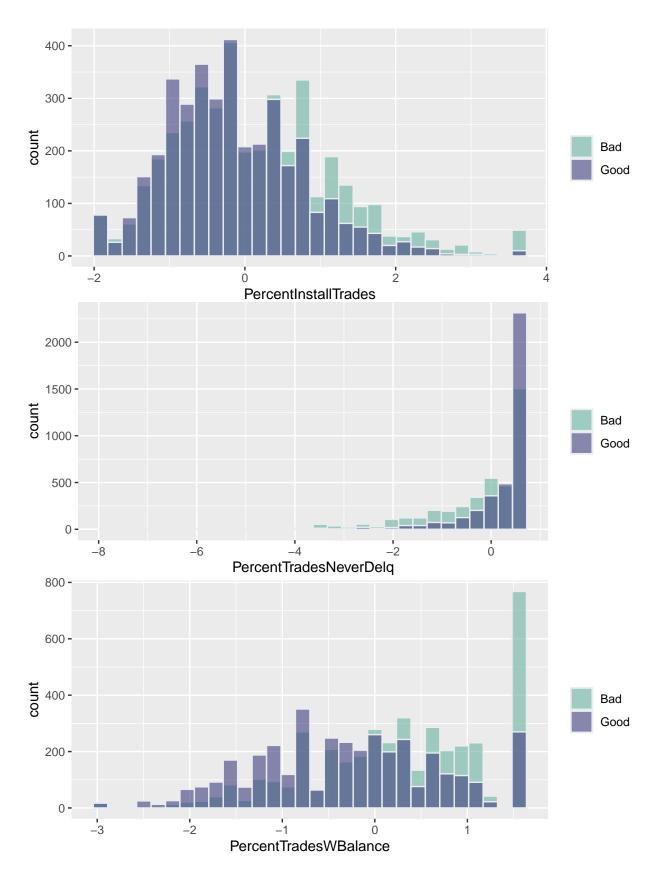






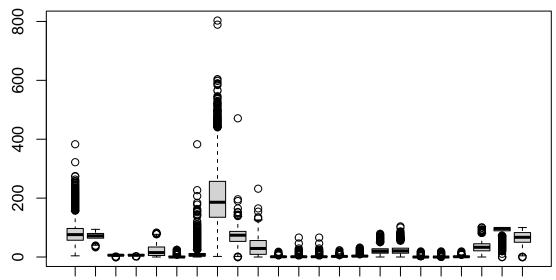




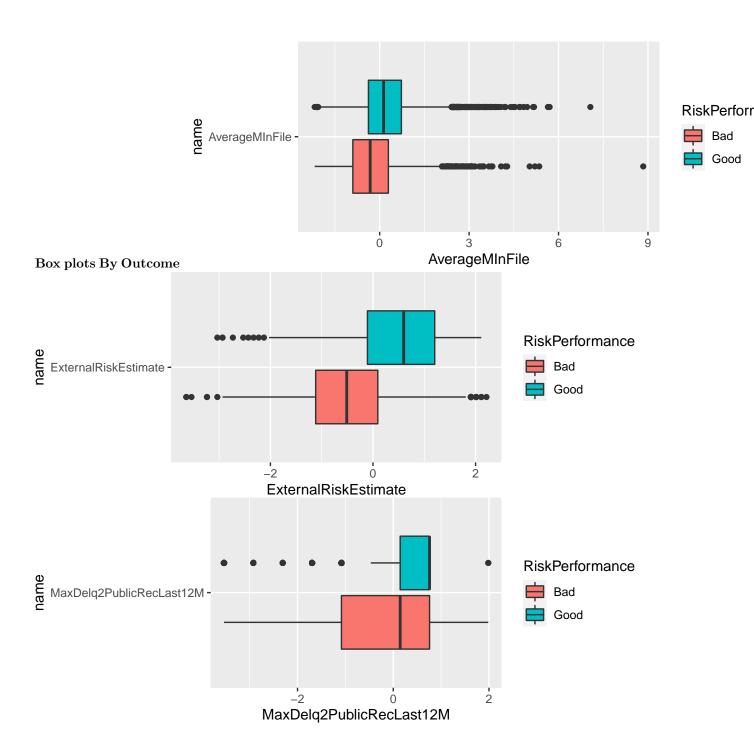


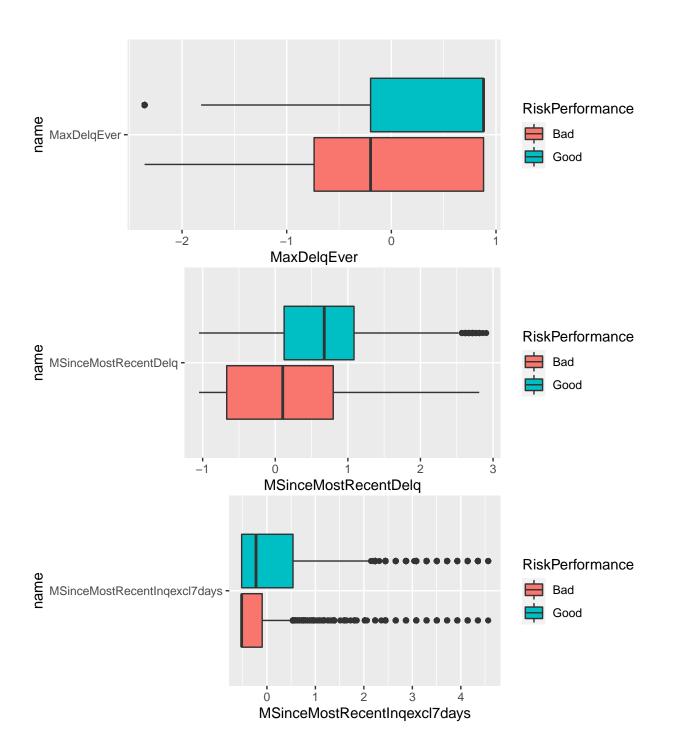
BoxPlots

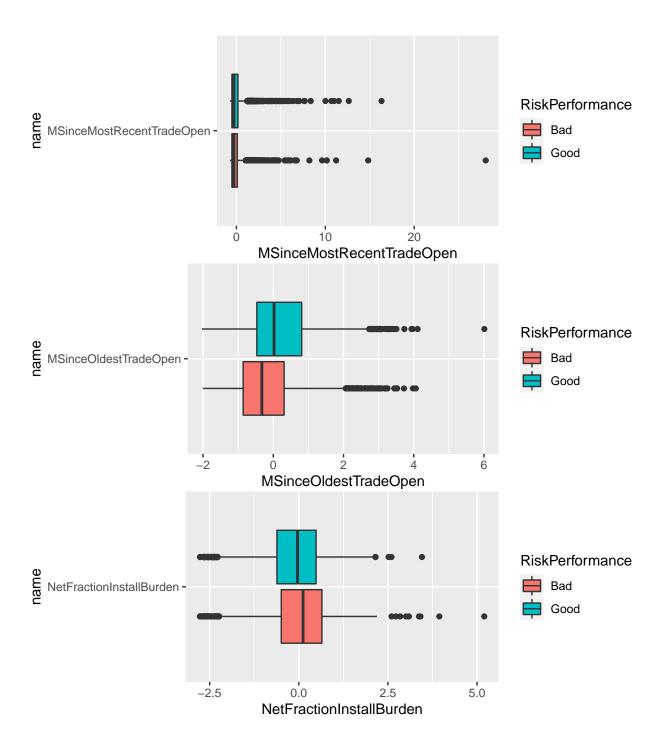
```
# boxplot to view outliers
boxplot(heloc[, 1:23])
```

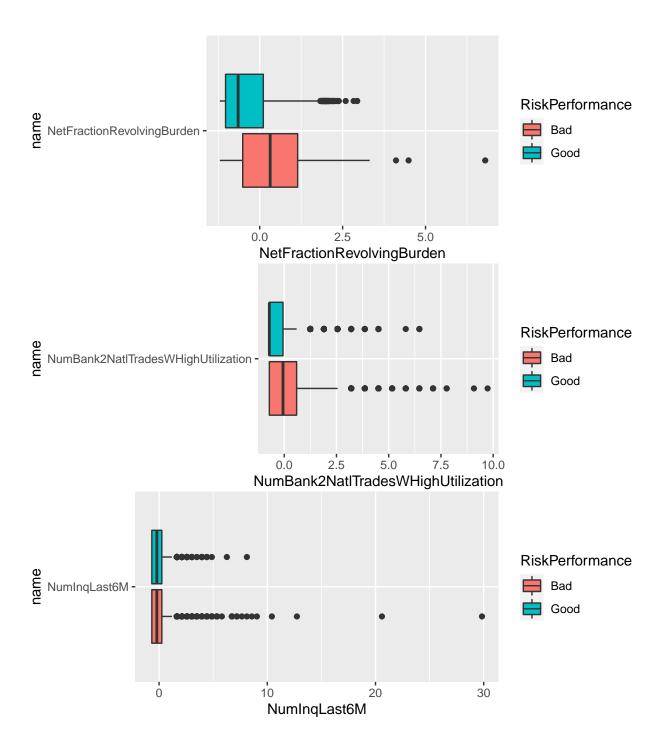


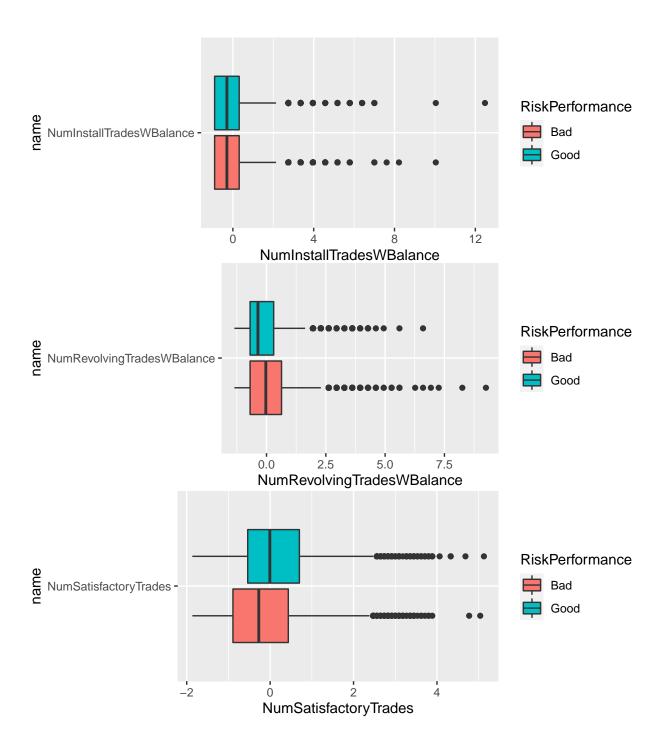
${\color{blue} \mathbf{Overall}} \quad \text{AverageMInFile} \quad \text{NetFractionInstallBurden} \quad \text{NumTotalTrades}$

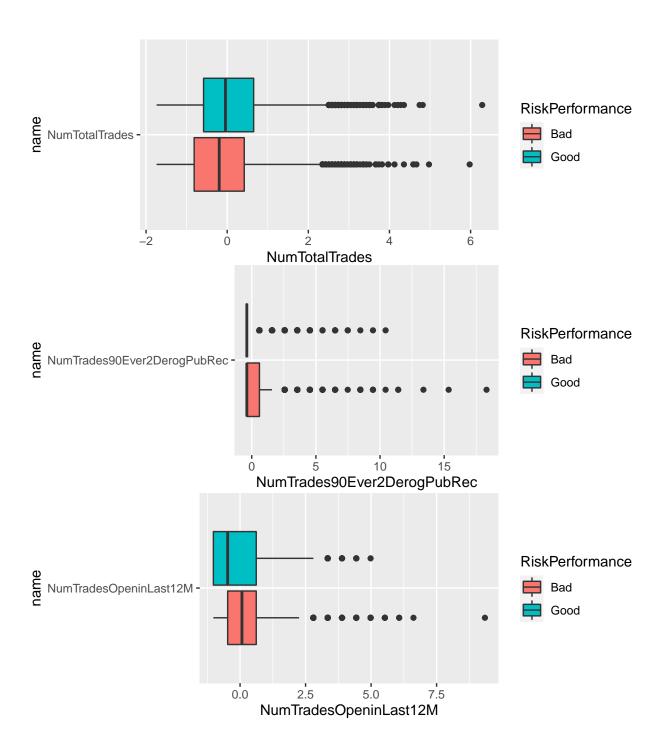


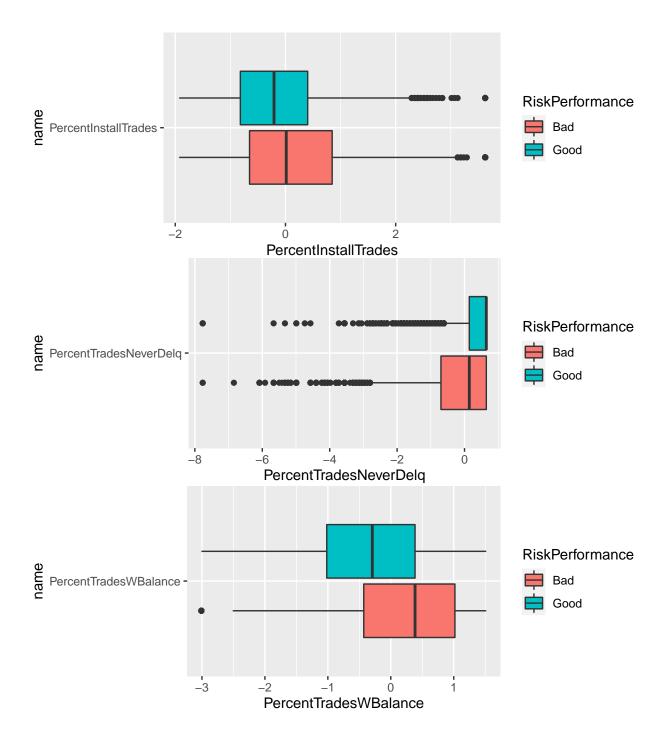












Models

With the following models, we are trying to maximize the SPECIFICITY of the models to prevent any non-qualified loanees being presented with a HELOC loan.

Specificity is defined as: "The specificity is defined as the rate that nonevent samples are predicted as nonevents" (Kuhn & Johnson, 2013)

summaryFunction=twoClassSummary)

```
bestIndex <- function(model){</pre>
  # returns top ROC value and surrounding indices from model
  highest_score <- max(model$results$ROC)</pre>
  # get row index and convert to type Int
  best_index <- rownames(model$results[model$results$ROC == highest_score,])</pre>
  best_index <- as.integer(best_index)</pre>
  return(best_index)
confusionMatrix <- function(testResults.model){</pre>
  caret::confusionMatrix(testResults.model,
                         as.factor(testResults$obs),
                         positive="Good")
}
importanceRanker <- function(model_varImp.importance, name){</pre>
  # coerce ranking into dataframe structure for manipulation
  df <- data.frame(model_varImp.importance)</pre>
  df_column_count <- dim(df)[2]</pre>
  # if dataframe has 2 columns, reduce to 1
  # NOTE: Values in both columns are the same
  if (df_column_count == 2){
    # grab only 1 column
    df <- df[,1, drop=FALSE]</pre>
  }
  # overwrite name
  names(df) <- name</pre>
  # reverse order ranking (highest num ranked = 1)
  df[,name] <- rank(-df[,name])</pre>
  df \leftarrow t(df)
  return(df)
}
modelScoreBoard <- function(testResults){</pre>
  # feed in testResults dataframe and out comes a model scoreboard!
  scoreboard <- data.frame()</pre>
  bool <- names(testResults) != 'obs'</pre>
  col_names <- colnames(testResults[,bool])</pre>
  for (colname in col_names){
    testResults.model <- testResults[,colname]</pre>
    cf <- caret::confusionMatrix(testResults.model,</pre>
                                    as.factor(testResults$obs),
                                    positive="Good")
    # gather testResults
```

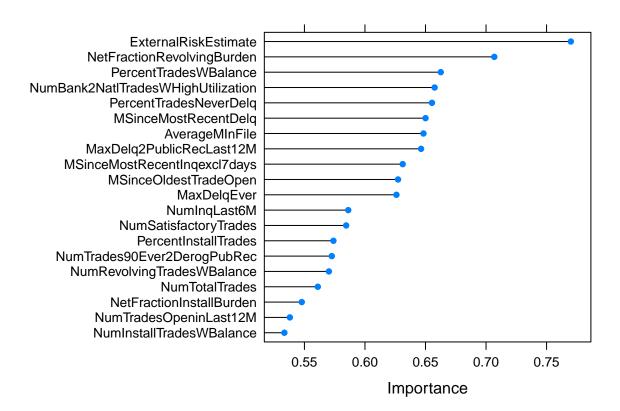
```
acc <- data.frame(metric=cf$overall[1])</pre>
    # qather Precision, Sensitivity, Specificity, & F1
    metrics <- list(cf$byClass[c(5,1,2,7)])</pre>
    metrics <- data.frame(Metrics=metrics)</pre>
    names(metrics) <- 'metric'</pre>
    # gather all metrics in 1 df
    metrics <- rbind(acc,metrics)</pre>
    names(metrics) <- colname</pre>
    metrics <- t(metrics)</pre>
    scoreboard <- rbind(scoreboard, metrics)</pre>
  }
  return(scoreboard)
}
# helper function for roc
roc_build <- function(model) {</pre>
  THE_ROC <- roc(response = model$pred$obs,</pre>
                   predictor = model$pred$Bad,
                   levels = rev(levels(model$pred$obs)))
  return(THE_ROC)
```

Discriminant Classification Models

LDA

```
set.seed(100)
lda_model <- caret::train(x=heloc_train_x,</pre>
                           y=heloc_train_y,
                           method="lda",
                           metric="ROC",
                           trControl=control)
lda_modelRoc <- roc_build(lda_model)</pre>
## Setting direction: controls < cases
lda_model
## Linear Discriminant Analysis
## 7897 samples
##
     21 predictor
      2 classes: 'Bad', 'Good'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 7107, 7107, 7107, 7108, 7107, 7108, ...
## Resampling results:
##
##
    ROC
                Sens
                            Spec
    0.7998689 0.7527435 0.7114538
##
```

```
lda_predictions <- stats::predict(lda_model, heloc_test_x)</pre>
# create dataframe to store
testResults <- data.frame(obs=heloc_test_y,</pre>
                           lda_model=lda_predictions)
# confusion matrix
confusionMatrix(testResults$lda_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
         Bad 768 288
##
         Good 259 659
##
##
##
                  Accuracy : 0.7229
                    95% CI : (0.7026, 0.7426)
##
##
       No Information Rate: 0.5203
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa : 0.4442
##
##
   Mcnemar's Test P-Value: 0.2312
##
##
               Sensitivity: 0.6959
##
               Specificity: 0.7478
##
            Pos Pred Value: 0.7179
            Neg Pred Value: 0.7273
##
##
                Prevalence: 0.4797
            Detection Rate: 0.3338
##
      Detection Prevalence: 0.4650
##
##
         Balanced Accuracy: 0.7218
##
##
          'Positive' Class : Good
##
lda_varImp <- caret::varImp(lda_model, scale=FALSE)</pre>
lda_varImpRanks <- importanceRanker(lda_varImp$importance, 'lda')</pre>
plot(lda_varImp, top=20)
```



Logistic Regression

```
set.seed(100)
logreg_model <- caret::train(x=heloc_train_x,</pre>
                              y=heloc_train_y,
                              method="glm",
                              metric="ROC",
                              trControl=control)
testResults$log_reg_model <- stats::predict(logreg_model, heloc_test_x)</pre>
logreg_modelRoc <- roc_build(logreg_model)</pre>
## Setting direction: controls < cases
logreg_model
## Generalized Linear Model
##
## 7897 samples
     21 predictor
##
##
      2 classes: 'Bad', 'Good'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 7107, 7107, 7107, 7108, 7107, 7108, ...
## Resampling results:
##
##
                Sens
                            Spec
     0.8000842 0.7554216 0.7130383
##
```

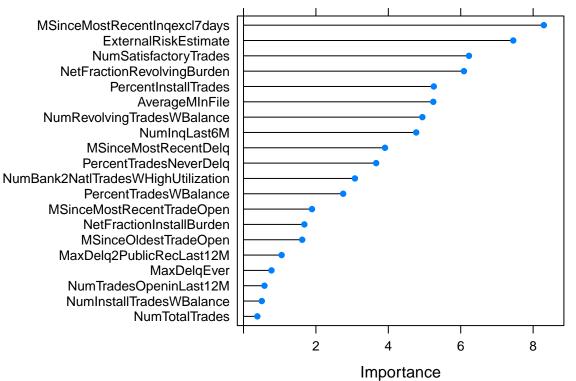
logreg_model\$finalModel\$coefficients

```
##
                           (Intercept)
                                                              AverageMInFile
                         -0.1803777116
                                                                0.2470129097
##
##
                  ExternalRiskEstimate
                                                   MaxDelq2PublicRecLast12M
##
                          0.4763324385
                                                                0.0454362796
##
                           MaxDelqEver
                                                       MSinceMostRecentDelq
                          0.0320452303
                                                                0.1630765084
##
##
         MSinceMostRecentInqexcl7days
                                                 MSinceMostRecentTradeOpen
                          0.2726958674
                                                              -0.0650335190
##
                                                   NetFractionInstallBurden
##
                MSinceOldestTradeOpen
##
                          0.0649987498
                                                              -0.0543543815
##
           {\tt NetFractionRevolvingBurden~NumBank2NatlTradesWHighUtilization}
                         -0.2929249411
##
                                                               -0.1376246387
##
                          NumInqLast6M
                                                   NumInstallTradesWBalance
##
                         -0.1638154810
                                                                0.0167061783
##
           {\tt NumRevolvingTradesWBalance}
                                                      NumSatisfactoryTrades
                         -0.2278121804
                                                                0.3689635005
##
                        NumTotalTrades
                                               NumTrades90Ever2DerogPubRec
##
                          0.0194119014
                                                                0.0001783062
##
##
               NumTradesOpeninLast12M
                                                       PercentInstallTrades
##
                         -0.0196622137
                                                               -0.1878716750
##
               PercentTradesNeverDelq
                                                      PercentTradesWBalance
                          0.1716749452
                                                                0.1173618900
```

confusionMatrix(testResults\$log_reg_model)

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
##
         Bad 766
##
         Good 261
                   659
##
##
                  Accuracy: 0.7219
                    95% CI: (0.7015, 0.7416)
##
       No Information Rate: 0.5203
##
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.4422
##
    Mcnemar's Test P-Value : 0.2671
##
##
##
               Sensitivity: 0.6959
##
               Specificity: 0.7459
##
            Pos Pred Value: 0.7163
            Neg Pred Value: 0.7268
##
                Prevalence: 0.4797
##
            Detection Rate: 0.3338
##
##
      Detection Prevalence: 0.4661
##
         Balanced Accuracy: 0.7209
##
          'Positive' Class : Good
##
##
```

```
lr_varImp <- caret::varImp(logreg_model, scale=FALSE)
lr_varImpRanks <- importanceRanker(lr_varImp$importance, 'lr')
plot(lr_varImp, top=20)</pre>
```

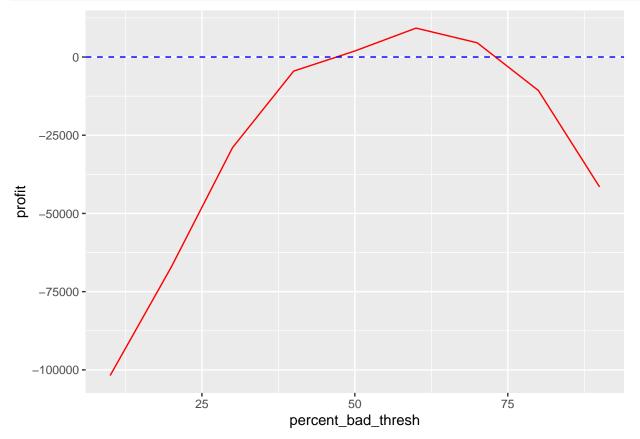


```
#get raw probs from model
predictions <- predict(logreg_model, heloc_test_x, type = 'prob')</pre>
predictions$OBS <- as.factor(heloc_test$RiskPerformance)</pre>
predictions <- predictions %>%
  mutate(lr10 = as.factor(if_else(Bad > 0.1, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr20 = as.factor(if_else(Bad > 0.2, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr30 = as.factor(if_else(Bad > 0.3, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr40 = as.factor(if_else(Bad > 0.4, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr50 = as.factor(if_else(Bad > 0.5, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr60 = as.factor(if_else(Bad > 0.6, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr70 = as.factor(if_else(Bad > 0.7, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr80 = as.factor(if_else(Bad > 0.8, 'Bad', 'Good')))
predictions <- predictions %>%
  mutate(lr90 = as.factor(if_else(Bad > 0.9, 'Bad', 'Good')))
# cf function
cost_confusionMatrix <- function(prediction.rate){</pre>
```

```
cm <- caret::confusionMatrix(prediction.rate,</pre>
                                 predictions $OBS,
                                 positive = "Bad")
  return(cm)
}
CF10 <- cost_confusionMatrix(predictions$lr10)</pre>
CF20 <- cost_confusionMatrix(predictions$1r20)</pre>
CF30 <- cost_confusionMatrix(predictions$1r30)</pre>
CF40 <- cost_confusionMatrix(predictions$1r40)</pre>
CF50 <- cost_confusionMatrix(predictions$1r50)</pre>
CF60 <- cost_confusionMatrix(predictions$1r60)</pre>
CF70 <- cost_confusionMatrix(predictions$1r70)</pre>
CF80 <- cost_confusionMatrix(predictions$1r80)</pre>
CF90 <- cost_confusionMatrix(predictions$1r90)</pre>
Costs = matrix(c(0,-1000*.85,-60,60), ncol=2, nrow=2)
Prev = matrix(c(9.6/50, 9.6/50, 2, 2), ncol=2, nrow=2)
CF10$table
Cost Matrix Threshold Analysis
##
              Reference
## Prediction Bad Good
##
         Bad 1023 895
##
         Good
sum(CF10$table*Costs*Prev)
## [1] -101812.8
CF20$table
##
              Reference
## Prediction Bad Good
         Bad 993 730
         Good 34 217
##
sum(CF20$table*Costs*Prev)
## [1] -67108.8
CF30$table
              Reference
## Prediction Bad Good
##
         Bad 934 531
##
         Good 93 416
sum(CF30$table*Costs*Prev)
## [1] -28977.6
CF40$table
              Reference
## Prediction Bad Good
```

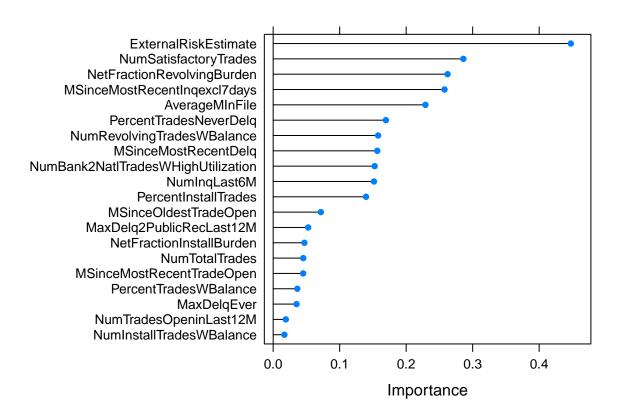
```
##
         Bad 859 378
##
         Good 168 569
sum(CF40$table*Costs*Prev)
## [1] -4497.6
CF50$table
##
            Reference
## Prediction Bad Good
##
        Bad 766 288
##
         Good 261 659
sum(CF50$table*Costs*Prev)
## [1] 1924.8
CF60$table
            Reference
## Prediction Bad Good
##
        Bad 652 180
        Good 375 767
sum(CF60$table*Costs*Prev)
## [1] 9240
CF70$table
           Reference
## Prediction Bad Good
       Bad 510 103
        Good 517 844
##
sum(CF70$table*Costs*Prev)
## [1] 4545.6
CF80$table
            Reference
## Prediction Bad Good
        Bad 318 36
##
##
        Good 709 911
sum(CF80$table*Costs*Prev)
## [1] -10708.8
CF90$table
##
            Reference
## Prediction Bad Good
##
        Bad 85
        Good 942 941
sum(CF90$table*Costs*Prev)
## [1] -41534.4
PlotProf < -data.frame(percent_bad_thresh = c(10,20,30,40,50,60,70,80,90),
                    profit = c(sum(CF10$table*Costs*Prev),
```

```
sum(CF20$table*Costs*Prev),
sum(CF30$table*Costs*Prev),
sum(CF40$table*Costs*Prev),
sum(CF50$table*Costs*Prev),
sum(CF60$table*Costs*Prev),
sum(CF70$table*Costs*Prev),
sum(CF70$table*Costs*Prev),
sum(CF80$table*Costs*Prev),
sum(CF90$table*Costs*Prev))
ggplot(PlotProf, aes(y=profit, x=percent_bad_thresh)) +
geom_line(colour = 'red') +
geom_hline(yintercept=0, linetype='dashed', color='blue')
```



Penalized Logistic Regression

```
# bestIndex(logreg_penalized_model)
logreg_penalized_model$results[3:7,1:5]
##
     alpha lambda
                         ROC
                                   Sens
                                             Spec
## 3
       0.0 0.1050 0.7987157 0.7583402 0.7043291
## 4
       0.0 0.1525 0.7981792 0.7607732 0.7024836
       0.0 0.2000 0.7976588 0.7619904 0.7011636
## 6
       0.1 0.0100 0.8001371 0.7551771 0.7114524
## 7
       0.1 0.0575 0.7992612 0.7551777 0.7043277
logreg_penalized_modelRoc <- roc_build(logreg_penalized_model)</pre>
## Setting direction: controls < cases
Based on the best ROC, has the best specificity, our main metric. This enables us to insure that we only
accept best qualified candidates, thus reducing the risk of a loanee defaulting on a $100,000 loan.
# Utilizing Best Model
testResults$logreg_penalized_model <- stats::predict(logreg_penalized_model,</pre>
                                                        heloc_test_x)
# confusion matrix
confusionMatrix(testResults$logreg_penalized_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
         Bad 773 282
##
         Good 254 665
##
##
##
                  Accuracy: 0.7285
                     95% CI : (0.7083, 0.748)
##
       No Information Rate: 0.5203
##
##
       P-Value [Acc > NIR] : <2e-16
##
##
                      Kappa: 0.4554
##
##
    Mcnemar's Test P-Value: 0.2435
##
##
               Sensitivity: 0.7022
##
               Specificity: 0.7527
            Pos Pred Value: 0.7236
##
            Neg Pred Value: 0.7327
##
##
                 Prevalence: 0.4797
##
            Detection Rate: 0.3369
##
      Detection Prevalence: 0.4656
##
         Balanced Accuracy: 0.7274
##
##
          'Positive' Class : Good
##
lr_penalized_varImp <- caret::varImp(logreg_penalized_model, scale=FALSE)</pre>
lr_pen_varImpRanks <- importanceRanker(lr_penalized_varImp$importance, 'lr_penalized')</pre>
plot(lr_penalized_varImp, top=20)
```



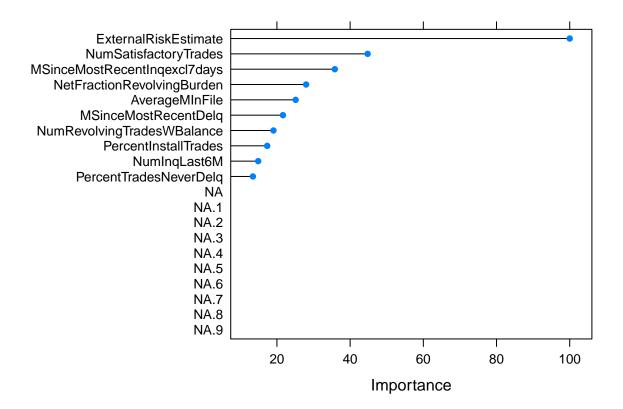
Nonlinear Classification Models

Flexibble Discriminant Analysis

```
# set.seed(100)
# fdaGrid <- expand.grid(degree=c(1,2),</pre>
#
                           nprune=seq(14, 20, 1))
#
# set.seed(100)
# fdaModel <- caret::train(x = heloc_train_x,</pre>
                             y = heloc_train_y,
#
                             method = "fda",
#
                             metric = "ROC",
#
                             trControl=control,
                             tuneGrid=fdaGrid)
# # bestIndex(fdaModel)
# fdaModel$results[1:18,1:5]
```

As we see, the best is that of nprune 16 with a specificity of 72.15% (index = 15).

```
## Loading required package: earth
## Loading required package: Formula
## Loading required package: plotmo
## Loading required package: plotrix
## Loading required package: TeachingDemos
fda_modelRoc <- roc_build(fdaModel)</pre>
## Setting direction: controls < cases
testResults$fda_model <- predict(fdaModel,</pre>
                                  heloc_test_x)
# confusion matrix
confusionMatrix(testResults$fda_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
         Bad 762 265
##
##
         Good 265 682
##
##
                  Accuracy: 0.7315
##
                    95% CI: (0.7114, 0.751)
##
       No Information Rate: 0.5203
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.4621
##
##
    Mcnemar's Test P-Value : 1
##
##
               Sensitivity: 0.7202
##
               Specificity: 0.7420
##
            Pos Pred Value : 0.7202
##
            Neg Pred Value: 0.7420
##
                Prevalence: 0.4797
##
            Detection Rate: 0.3455
##
      Detection Prevalence: 0.4797
##
         Balanced Accuracy: 0.7311
##
##
          'Positive' Class : Good
##
fda_varImp <- caret::varImp(fdaModel, scale=FALSE)</pre>
fda_varImpRanks <- importanceRanker(fda_varImp$importance, 'fda_penalized')</pre>
plot(fda_varImp, top=20)
```

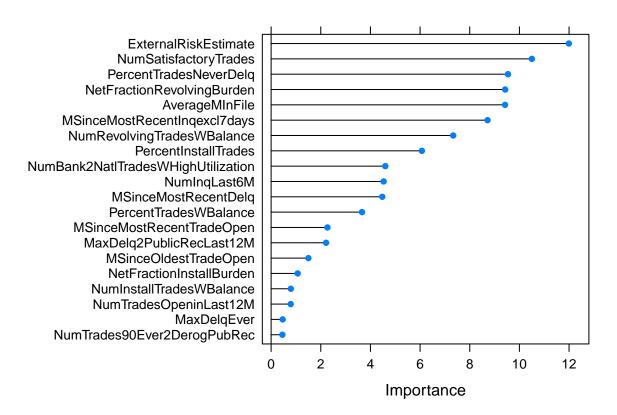


Neural Network

```
# set.seed(100)
# nnetGrid <- expand.grid(size = 1:2,
#
                           decay = c(0, 0.1, 0.25, 0.5, 0.75, 1))
#
# nnetModel <- caret::train(x = heloc_train_x,</pre>
                             y = heloc_train_y,
#
                              method = "nnet",
#
                              tuneGrid = nnetGrid,
#
                              metric = "ROC",
#
                              trace = FALSE,
                              maxit = 2000,
                              trControl = control)
# nnetModel$bestTune$results[1:6,1:5]
```

It appears that the model starts to over fit once the decay goes to 0.1. The nnet model chose size=2 with decay of 2, with nearly identical ROC, Sensitivity, and Specificity scores and thus size 1 with decay 0 is our choice.

```
maxit = 2000,
                    trControl = control)
nnet_modelRoc <- roc_build(nnetModel)</pre>
## Setting direction: controls < cases
testResults$nnet_model <- predict(nnetModel,</pre>
                                   heloc_test_x)
# confusion matrix
confusionMatrix(testResults$nnet_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
##
         Bad 769 291
         Good 258 656
##
##
##
                  Accuracy: 0.7219
                    95% CI : (0.7015, 0.7416)
##
##
       No Information Rate: 0.5203
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa : 0.4421
##
##
    Mcnemar's Test P-Value: 0.172
##
               Sensitivity: 0.6927
##
##
               Specificity: 0.7488
            Pos Pred Value : 0.7177
##
##
            Neg Pred Value: 0.7255
                Prevalence: 0.4797
##
##
            Detection Rate: 0.3323
##
      Detection Prevalence: 0.4630
##
         Balanced Accuracy: 0.7207
##
##
          'Positive' Class : Good
nn_varImp <- caret::varImp(nnetModel, scale=FALSE)</pre>
nn_varImpRanks <- importanceRanker(nn_varImp$importance, 'nn')</pre>
plot(nn_varImp, top=20)
```



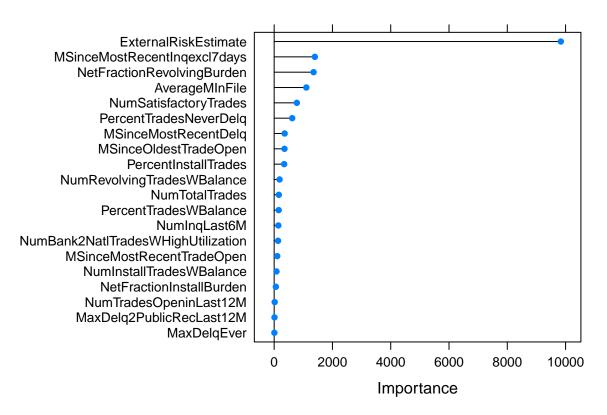
Classification Trees

Boosted Tree

```
# gbmGrid <- expand.grid(interaction.depth = c(2,3),
                          n.trees = c(1000, 2000, 3000, 4000), #default val = 1000
#
                          shrinkage = c(0.01, 0.1),
#
                          n.minobsinnode = c(5,10)) \# default val = 10
# set.seed(100)
# gbmModel <- caret::train(x = heloc_train_x,
                            y = heloc_train_y,
#
                            method = "gbm",
#
#
                            tuneGrid = qbmGrid,
#
                            verbose = FALSE,
#
                            metric = "ROC",
                            trControl= control)
# gbmModel$results
gbmGrid <- expand.grid(interaction.depth = 2,</pre>
                        n.trees = 1000,
                        shrinkage = 0.01,
                        n.minobsinnode = 5)
set.seed(100)
gbmModel <- caret::train(x = heloc_train_x,</pre>
                          y = heloc_train_y,
                          method = "gbm",
                          tuneGrid = gbmGrid,
                          verbose = FALSE,
                          metric = "ROC",
                          trControl= control)
```

```
gbm_modelRoc <- roc_build(gbmModel)</pre>
## Setting direction: controls < cases
testResults$gbm_model <- predict(gbmModel,</pre>
                                  heloc_test_x)
# confusion matrix
confusionMatrix(testResults$gbm_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
         Bad 775 285
##
##
         Good 252 662
##
##
                  Accuracy: 0.728
                    95% CI: (0.7078, 0.7475)
##
##
       No Information Rate: 0.5203
       P-Value [Acc > NIR] : <2e-16
##
##
##
                      Kappa: 0.4543
##
    Mcnemar's Test P-Value: 0.1673
##
##
               Sensitivity: 0.6990
##
##
               Specificity: 0.7546
##
            Pos Pred Value: 0.7243
            Neg Pred Value: 0.7311
##
                Prevalence: 0.4797
##
##
            Detection Rate: 0.3354
##
      Detection Prevalence: 0.4630
##
         Balanced Accuracy: 0.7268
##
##
          'Positive' Class : Good
gbm_varImp <- caret::varImp(gbmModel, scale=FALSE)</pre>
gbm_varImpRanks <- importanceRanker(gbm_varImp$importance, 'gbm')</pre>
```

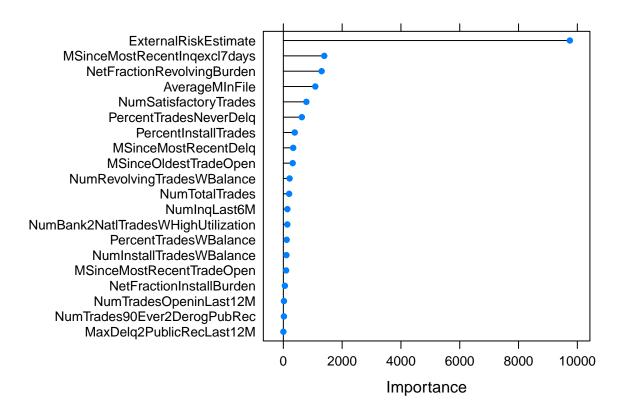
plot(gbm_varImp, top=20)



```
# gbmGrid <- expand.grid(interaction.depth = c(2,3),
#
                         n.trees = c(1000, 2000),
#
                         shrinkage = c(0.01, 0.1),
#
                         n.minobsinnode = c(5,10))
# set.seed(100)
# gbmMono_model <- caret::train(x = heloc_train_x,</pre>
                                y = heloc_train_y,
                                method = "qbm",
#
#
                                #
                                                 1,1,1,1,0,0,-1,0,-1,1,
#
                                                 0,-1,1).
                                tuneGrid = gbmGrid,
#
#
                                verbose = FALSE,
#
                                metric = "ROC",
                                trControl= control)
# qbmMono_model$results
gbmGrid <- expand.grid(interaction.depth = 2,</pre>
                       n.trees = 1000,
                       shrinkage = 0.01,
                       n.minobsinnode = 5)
set.seed(100)
gbmMono_model <- caret::train(x = heloc_train_x,</pre>
                         y = heloc_train_y,
                         var.monotone = c(-1,-1,-1,-1,-1,-1,-1,-1,
                                          1,1,1,1,0,0,-1,0,-1,1,
                                          0,-1,1),
```

```
method = "gbm",
                         tuneGrid = gbmGrid,
                         verbose = FALSE,
                         metric = "ROC",
                         trControl= control)
gbmMono_modelRoc <- roc_build(gbmMono_model)</pre>
GBM with monotonic constraints
## Setting direction: controls < cases
testResults$gbmMono model <- predict(gbmMono model,</pre>
                                      heloc_test_x)
confusionMatrix(testResults$gbmMono_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
         Bad 772 281
##
         Good 255 666
##
##
##
                  Accuracy : 0.7285
                    95% CI: (0.7083, 0.748)
##
       No Information Rate: 0.5203
##
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.4555
##
    Mcnemar's Test P-Value: 0.2802
##
##
##
               Sensitivity: 0.7033
##
               Specificity: 0.7517
##
            Pos Pred Value: 0.7231
            Neg Pred Value : 0.7331
##
##
                Prevalence: 0.4797
            Detection Rate: 0.3374
##
##
      Detection Prevalence: 0.4666
##
         Balanced Accuracy: 0.7275
##
##
          'Positive' Class : Good
gmbMono_varImp <- caret::varImp(gbmMono_model, scale=FALSE)</pre>
gbmMono_varImpRanks <- importanceRanker(gmbMono_varImp$importance, 'gbmMono')</pre>
```

plot(gmbMono_varImp, top=20)

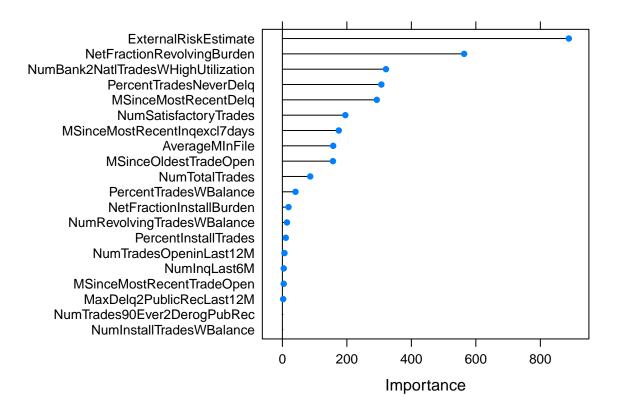


CART

```
# set.seed(100)
# rpart_grid <- expand.grid(cp=c(0.0005, 0.001250, 0.0015, 0.00175, 0.002))
#
 rpart_model <- caret::train(x=heloc_train_x,</pre>
                                y=heloc_train_y,
                                method="rpart",
#
#
                                metric="ROC",
#
                                trControl=control,
#
                                tuneGrid = rpart_grid)
#
# testResults$rpart_model <- predict(rpart_model, heloc_test_x)</pre>
# rpart model
```

As we see, specificity for this model is one of the worst out of all the models we have.

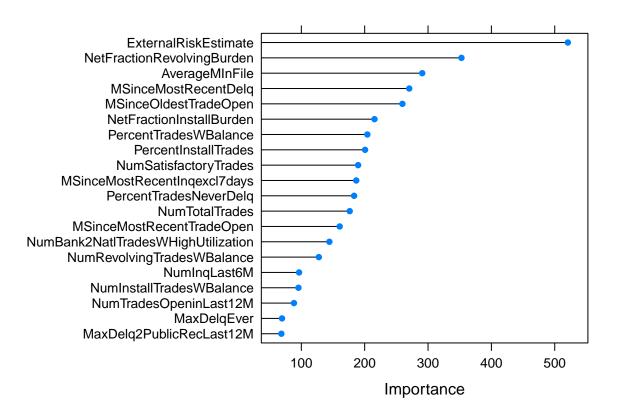
```
## Setting direction: controls < cases
rpart_model
## CART
##
## 7897 samples
##
     21 predictor
      2 classes: 'Bad', 'Good'
##
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 7107, 7107, 7107, 7108, 7107, 7108, ...
## Resampling results:
##
     ROC
##
                Sens
                            Spec
##
     0.7558931 0.7551742 0.671846
## Tuning parameter 'cp' was held constant at a value of 0.00175
testResults$rpart_model <- predict(rpart_model, heloc_test_x)</pre>
confusionMatrix(testResults$rpart_model)
## Confusion Matrix and Statistics
##
             Reference
## Prediction Bad Good
         Bad 748 282
##
         Good 279 665
##
##
                  Accuracy : 0.7158
##
##
                    95% CI: (0.6953, 0.7356)
##
       No Information Rate: 0.5203
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.4306
##
##
    Mcnemar's Test P-Value: 0.9327
##
##
               Sensitivity: 0.7022
##
               Specificity: 0.7283
##
            Pos Pred Value: 0.7044
            Neg Pred Value: 0.7262
##
                Prevalence: 0.4797
##
##
            Detection Rate: 0.3369
##
      Detection Prevalence: 0.4782
##
         Balanced Accuracy: 0.7153
##
##
          'Positive' Class : Good
##
rpart_varImp <- caret::varImp(rpart_model, scale=FALSE)</pre>
rpart_varImpRanks <- importanceRanker(rpart_varImp$importance, 'RPart')</pre>
plot(rpart_varImp, top=20)
```



Random Forest

```
# set.seed(100)
\# rf\_grid \leftarrow expand.grid(mtry=c(5,10,15))
#
# randomForest_model <- caret::train(x=heloc_train_x,</pre>
#
                               y=heloc_train_y,
                               method="rf",
#
#
                               metric="ROC",
#
                               trControl=control,
#
                               tuneGrid = rf\_grid)
#
# randomForest model
set.seed(100)
rf_grid <- expand.grid(mtry=5)</pre>
randomForest_model <- caret::train(x=heloc_train_x,</pre>
                                      y=heloc_train_y,
                                      method="rf",
                                      metric="ROC",
                                      trControl=control,
                                      tuneGrid = rf_grid)
randomForest_modelRoc <- roc_build(randomForest_model)</pre>
## Setting direction: controls < cases
randomForest_model
```

```
## Random Forest
##
## 7897 samples
##
     21 predictor
##
      2 classes: 'Bad', 'Good'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 7107, 7107, 7107, 7108, 7107, 7108, ...
## Resampling results:
##
##
     ROC
                            Spec
     0.7951729 0.7736746 0.6847978
##
##
## Tuning parameter 'mtry' was held constant at a value of 5
testResults$randomForest_model <- predict(randomForest_model, heloc_test_x)</pre>
confusionMatrix(testResults$randomForest_model)
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction Bad Good
##
         Bad 790 291
         Good 237 656
##
##
##
                  Accuracy: 0.7325
##
                    95% CI: (0.7124, 0.7519)
       No Information Rate: 0.5203
##
       P-Value [Acc > NIR] : < 2e-16
##
##
##
                     Kappa: 0.463
##
##
    Mcnemar's Test P-Value: 0.02108
##
##
               Sensitivity: 0.6927
##
               Specificity: 0.7692
##
            Pos Pred Value: 0.7346
##
            Neg Pred Value: 0.7308
##
                Prevalence: 0.4797
##
            Detection Rate: 0.3323
##
      Detection Prevalence: 0.4524
##
         Balanced Accuracy: 0.7310
##
##
          'Positive' Class : Good
##
rf_varImp <- caret::varImp(randomForest_model, scale=FALSE)</pre>
rf_varImpRanks <- importanceRanker(rf_varImp$importance, 'RF')</pre>
plot(rf_varImp, top=20)
```

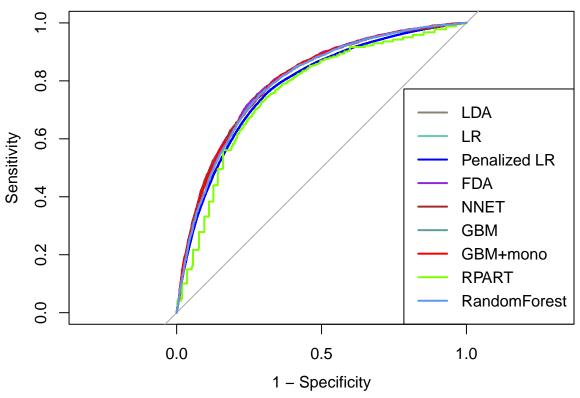


Results & Discussion

```
varImpRanks_df <- plyr::rbind.fill.matrix(fda_varImpRanks,gbm_varImpRanks)</pre>
# rbind fill removes row names
rownames(varImpRanks_df) <- c('fda','gbm')</pre>
# base::rbind preserves row names
varImpRanks_df <- rbind(varImpRanks_df, gbmMono_varImpRanks)</pre>
varImpRanks_df <- rbind(varImpRanks_df, lda_varImpRanks)</pre>
varImpRanks_df <- rbind(varImpRanks_df, lr_varImpRanks)</pre>
varImpRanks_df <- rbind(varImpRanks_df, lr_pen_varImpRanks)</pre>
varImpRanks_df <- rbind(varImpRanks_df, nn_varImpRanks)</pre>
varImpRanks_df <- rbind(varImpRanks_df, rpart_varImpRanks)</pre>
varImpRanks df <- rbind(varImpRanks df, rf varImpRanks)</pre>
varImpRanks_df <- data.frame(varImpRanks_df)</pre>
# num of columns is hard to print, thus transpose for printing purposes
varImpRanks_df <- t(varImpRanks_df)</pre>
knitr::kable(varImpRanks df) %>%
  kableExtra::kable_styling("striped", full_width = F) %>%
  kableExtra::row_spec(0, angle = -90)
plot(lda_modelRoc, type='s', col='antiquewhite4', legacy.axes=TRUE)
plot(logreg_modelRoc, type='s', col='aquamarine3', legacy.axes=TRUE, add=TRUE)
plot(logreg_penalized_modelRoc, type='s', col='blue', legacy.axes=TRUE, add=TRUE)
plot(fda_modelRoc, type='s', col='blueviolet', legacy.axes=TRUE, add=TRUE)
plot(nnet_modelRoc, type='s', col='brown', legacy.axes=TRUE, add=TRUE)
plot(gbm_modelRoc, type='s', col='cadetblue', legacy.axes=TRUE, add=TRUE)
plot(gbmMono_modelRoc, type='s', col='red', legacy.axes=TRUE, add=TRUE)
plot(rpart_modelRoc, type='s', col='chartreuse', legacy.axes=TRUE, add=TRUE)
plot(randomForest_modelRoc, type='s', col='cornflowerblue', legacy.axes=TRUE, add=TRUE)
```

	fda	gbm	gbmMono	lda	lr	lr_penalized 10	nn	RPart	RF
ExternalRiskEstimate	1	1	4	7	6	5	5	8	3
NumSatisfactoryTrades	2	5	1	1	2	1	1	1	1
MSinceMostRecentInqexcl7days	3	2	20	8	16	13	14	18	20
NetFractionRevolvingBurden	4	3	21	11	17	18	19	5	19
AverageMInFile	5	4	8	6	9	8	11	7	4
MSinceMostRecentDelq	6	7	2	9	1	4	6	17	10
${\bf Num Revolving Trades WB a lance}$	7	10	16	21	13	16	13	9	13
PercentInstallTrades	8	9	9	10	15	12	15	12	5
NumInqLast6M	9	13	17	18	14	14	16	2	6
PercentTradesNeverDelq	10	6	3	2	4	3	4	3	2
MaxDelq2PublicRecLast12M	NA	19	13	4	11	9	9	16	14
MaxDelqEver	NA	20	12	12	8	10	10	13	16
${\bf MSinceMostRecentTradeOpen}$	NA	15	15	20	19	20	17	6	17
MSinceOldestTradeOpen	NA	8	10	16	7	7	7	10	15
NetFractionInstallBurden	NA	17	5	13	3	2	2	15	9
NumBank2NatlTradesWHighUtilization	NA	14	11	17	20	15	21	14	12
NumInstallTradesWBalance	NA	16	19	15	21	21	20	4	21
NumTotalTrades	NA	11	18	19	18	19	18	11	18
NumTrades90Ever2DerogPubRec	NA	21	7	14	5	11	8	20	8
NumTradesOpeninLast12M	NA	18	6	5	10	6	3	20	11
PercentTradesWBalance	NA	12	14	3	12	17	12	20	7

Compare KOC curves from unferent models



```
##
                           Accuracy Precision Sensitivity Specificity
                          0.7228977 0.7178649
## lda_model
                                                            0.7478092 0.7067024
                                                0.6958817
## log_reg_model
                                                            0.7458617 0.7059454
                          0.7218845 0.7163043
                                                0.6958817
## logreg_penalized_model 0.7284701 0.7236126
                                                0.7022175
                                                            0.7526777 0.7127546
## fda_model
                          0.7315096 0.7201690
                                                0.7201690
                                                            0.7419669 0.7201690
## nnet_model
                          0.7218845 0.7177243
                                                            0.7487829 0.7049973
                                                0.6927138
## gbm_model
                          0.7279635 0.7242888
                                                0.6990496
                                                            0.7546251 0.7114455
## gbmMono model
                          0.7284701 0.7231270
                                                0.7032735
                                                            0.7517040 0.7130621
## rpart_model
                          0.7158055 0.7044492
                                                0.7022175
                                                            0.7283350 0.7033316
## randomForest model
                          0.7325228 0.7346025
                                                0.6927138
                                                            0.7692308 0.7130435
##
                                AUC
```

```
## lda_model
                          0.7998810
## log_reg_model
                          0.8002390
## logreg_penalized_model 0.7820838
## fda_model
                          0.8032575
## nnet_model
                          0.8001313
## gbm_model
                          0.7998948
## gbmMono_model
                          0.8003082
## rpart_model
                          0.7554376
## randomForest_model
                          0.7950744
```

REFERENCES:

Kuhn, M., & Johnson, K. (2013). Applied Predictive Modeling. New York: Springer.