

Midpoint $y_{i+\frac{1}{2}} = y_i + \frac{h}{2} f(t_{i+\frac{1}{2}}, y_{i+\frac{1}{2}})$

$$y_{i+\frac{1}{2}} = 3 + \frac{1}{2} \left(3e^0 - \frac{7 \times 3}{4} \right) = \frac{15}{8}$$

$$y_{i+1} = 3 + \frac{3e^{1/2} - \frac{7 \times 15/8}{4}}{32} = 4.665$$

$$y_{i+\frac{1}{2}} = 4.665 + \frac{1}{2} \left(3e - \frac{7 \times 4.665}{4} \right) = 12.327$$

$$y_2 = 4.665 + \frac{3e^{1.5} - \frac{7 \times 4.665}{4}}{4} = 9.954$$

$$y_{i+\frac{1}{2}} = 9.954 + \frac{1}{2} \left(3e^2 - \frac{7 \times 9.954}{4} \right) = 12.3278$$

$$y_3 = 9.954 + \left(3e^{2.5} - \frac{7 \times 12.3278}{8} \right) = 16.47$$

Euler

$$y_1 = 3 + \left(3e^0 - \frac{7 \times 3}{4} \right) \\ = 0.75$$

$$y_2 = 0.75 + \left(3e - \frac{7 \times 0.75}{4} \right) \\ = 7.592$$

$$y_3 = 7.592 + \left(3e^2 - \frac{7 \times 7.592}{4} \right) \\ = 16.473$$

Heun.

$$y_0 = y_i + h f(t_i, y_i) \quad y_{i+1} = y_i + h (f(t_i, y_i) + f(t_{i+1}, y_{i+1}))$$

$$y_0 = 3 + \left(3e^0 - \frac{7 \times 3}{4} \right) = 0.75$$

$$y_1 = 3 + \left(3e^0 - \frac{7 \times 3}{4} \right) + \left(3e^1 - \frac{7 \times 0.75}{4} \right) \\ = 5.296$$

$$y_0 = 5.296 + \left(3e^1 - \frac{7 \times 5.296}{4} \right) = 4.18$$

$$y_2 = 5.296 + \left(3e^1 - \frac{7 \times 5.296}{4} + 3e^2 - \frac{7 \times 4.18}{4} \right) \\ = 12.163$$

$$y_0 = 12.163 + \left(3e^2 - \frac{7 \times 12.163}{4} \right) = 13.044$$

$$y_3 = 12.163 + \left(3e^2 - \frac{7 \times 12.163}{4} + 3e^3 - \frac{7 \times 13.044}{4} \right) \\ = 31.318$$