

# CmdStan User's Guide

Version 2.24

Stan Development Team

# Contents

**Introduction** 4

**QuickStart Guide** 6

**1. CmdStan Installation** 7

- 1.1 GNU-Make Utility 7
- 1.2 Building CmdStan 10
- 1.3 Clone the GitHub CmdStan Repository 11
- 1.4 Trouble-shooting the installation 12

**2. Example Model and Data** 13

**3. Compiling a Stan Program** 14

- 3.1 Invoking the Make Utility 14
- 3.2 Dependencies 14
- 3.3 Compiler Errors 15
- 3.4 Troubleshooting 15

**4. MCMC Sampling** 16

- 4.1 Running the Sampler 16
- 4.2 Running Multiple Chains 17
- 4.3 Stan CSV Output File 19
- 4.4 Summarizing Sampler Output(s) with `stansummary` 20

**5. Optimization** 22

**6. Variational Inference** 25

**7. Generating Quantities of Interest from a Fitted Model** 29

**CmdStan Reference** 30

**8. Command-Line Interface Overview** 31

- 8.1 Input Data Argument 31
- 8.2 Output Control Arguments 32

8.3	Initialize Model Parameters Argument	32
8.4	Random Number Generator Arguments	33
8.5	Chain Identifier Argument: <code>id</code>	33
8.6	Command Line Help	34
<b>9.</b>	<b>MCMC Sampling using Hamiltonian Monte Carlo</b>	<b>35</b>
9.1	Iterations	36
9.2	Adaptation	37
9.3	Algorithm	38
9.4	Sampler Diagnostic File	41
9.5	Examples	41
<b>10.</b>	<b>Maximum Likelihood Estimation</b>	<b>47</b>
10.1	Optimization Algorithms	47
10.2	The quasi-Newton optimizers	48
10.3	The Newton optimizer	49
<b>11.</b>	<b>Variational Inference Algorithm: ADVI</b>	<b>50</b>
11.1	Variational Algorithms	51
11.2	Configuration	51
11.3	CSV Output	52
<b>12.</b>	<b>Standalone Generate Quantities</b>	<b>54</b>
<b>13.</b>	<b>Diagnosing HMC by Comparison of Gradients</b>	<b>55</b>
	<b>CmdStan Tools</b>	<b>56</b>
<b>14.</b>	<b><code>stanc</code>: Translating Stan to C++</b>	<b>57</b>
14.1	Instantiating the <code>stanc</code> Binary	57
14.2	The Stan Compiler Program	57
14.3	Command-Line Options for <code>stanc3</code>	58
14.4	Command-Line Options for <code>stanc2</code>	59
14.5	Using External C++ Code	60
<b>15.</b>	<b><code>stansummary</code>: MCMC Output Analysis</b>	<b>62</b>
15.1	Building the <code>stansummary</code> Command	62
15.2	Running the <code>stansummary</code> Command	62

15.3 Command-line Options 62

**16. diagnose: Diagnosing Biased Hamiltonian Monte Carlo Inferences 64**

16.1 Building the diagnose Command 64

16.2 Running the diagnose Command 64

16.3 diagnose Warnings and Recommendations 67

**17. print (deprecated): MCMC Output Analysis 69**

**Appendices 70**

**18. Stan CSV File Format 71**

18.1 MCMC Sampler CSV Output 71

18.2 Optimization Output 71

18.3 Variational Inference Output 71

18.4 Generate Quantities Outputs 72

18.5 Diagnose Method Outputs 72

**19. JSON Format for CmdStan 73**

19.1 JSON Syntax Summary 73

19.2 Stan Data Types in JSON Notation 74

**20. RDump Format for CmdStan 76**

20.1 Creating Dump Files 76

20.2 Scalar Variables 76

20.3 Sequence Variables 76

20.4 Array Variables 77

20.5 Matrix- and Vector-Valued Variables 78

20.6 Integer- and Real-Valued Variables 79

20.7 Quoted Variable Names 80

20.8 Line Breaks 80

20.9 BNF Grammar for Dump Data 81

**Bibliography 83**

# Introduction

This document is a user's guide for CmdStan, the command-line interface to the Stan statistical modeling language. CmdStan is the command-line interface for Stan. CmdStan provides the tools to compile a statistical model written in the Stan probabilistic programming language into a C++ executable program which can then be run to either: do inference on data, producing an estimate of the posterior; generate new quantities of interest from an existing estimate; or generate data from the model according to a given set of parameters

CmdStan provides the programs and tools to compile Stan programs into C++ executables that can be run directly from the command line, together with a few utilities to check and summarize the resulting outputs. CmdStan is one of several interfaces to Stan; there are also R, Python, Matlab, Julia, and Stata interfaces.

## *Stan Home Page*

For links to up-to-date code, examples, manuals, bug reports, feature requests, and everything else Stan related, see the Stan home page:

<http://mc-stan.org/>

## *Licensing*

CmdStan, Stan, and the Stan Math Library are licensed under the new BSD license (3-clause). See the Stan Reference Manual Licenses section for licensing terms for Stan and the dependent packages Boost, Eigen, Sundials, and Intel TBB.

## *Stan Documentation: User's Guide and Reference Manuals*

The Stan user's guide provides example models and programming techniques for coding statistical models in Stan. It also serves as an example-driven introduction to Bayesian modeling and inference:

<http://mc-stan.org/docs/stan-users-guide>

Stan's modeling language is shared across all of its interfaces. The Stan Language Reference Manual provides a concise definition of the language syntax for all elements in the language.

<http://mc-stan.org/docs/reference-manual>

The Stan Functions Reference provides definitions and examples for all the functions defined in the Stan math library and available in the Stan programming language, including all probability distributions.

<http://mc-stan.org/docs/functions-reference>.

### *Benefits of CmdStan*

- With every new Stan release, there is a corresponding CmdStan release, therefore CmdStan provides access to the latest version of Stan, and can be used to run the development version of Stan as well.
- Of the Stan interfaces, CmdStan has the lightest memory footprint, therefore it can fit larger and more complex models. It has the fewest dependencies, which makes it easier to run in limited environments such as clusters.
- The output generated is in CSV format and can be post-processed using other Stan interfaces or general tools.

# QuickStart Guide

This section is designed to help users install CmdStan and get acquainted with the CmdStan interface.

# 1. CmdStan Installation

To install CmdStan you need:

- A modern C++11 compiler. Supported versions are • Linux: g++ 4.9.3 or clang 6.0 • macOS: the XCode version of clang • Windows: g++ 8.1 (available with RTools 4.0) is recommended; alternatively, g++ 4.9.3 (available with RTools 3.5).
- The GNU-Make utility program or the Windows equivalent mingw32-make. On macOS, this is part of the XCode command line tools installed via `command xcode-select --install`. On Windows, mingw32-make is installed as part of RTools: <https://cran.rstudio.com/bin/windows/Rtools/>.
- The CmdStan C++ source code and libraries. The most recent CmdStan release is available as a single compressed tarfile containing all of the CmdStan tools and the Stan and math libraries from GitHub: <https://github.com/stan-dev/cmdstan/releases/latest> or you can clone the GitHub repo.

The CmdStan release unpacks into a directory called `cmdstan-<version>` where the version string consists of the major.minor.patch version numbers, e.g. `cmdstan-2.23.0`. Cloning CmdStan from GitHub creates a directory simply called `cmdstan`. Throughout this manual, we refer to this top-level CmdStan source directory as **<cmdstan-home>**.

## 1.1. GNU-Make Utility

CmdStan relies on the GNU-make utility to build both the Stan model executables and the CmdStan tools.

GNU-Make builds executable programs and libraries from source code by reading files called Makefiles which specify how to derive the target program. A Makefile consists of a set of recursive rules where each rule specifies a target, its dependencies, and the specific operations required to build the target. Specifying dependencies for a target provides a way to control the build process so that targets which depend on other files will be updated as needed *only* when there are changes to those other files. Thus Make provides an efficient way to manage complex software.

The CmdStan Makefile is in the `<cmdstan-home>` directory and is named `makefile`. This is one of the default GNU Makefile names, which allows you to omit the `-f makefile` argument to the Make command. Because the CmdStan Makefile includes several other Makefiles, **Make only works properly when invoked from the**



**<cmdstan-home> directory**; attempts to use this Makefile from another directory by specifying the full path to the file `makefile` won't work. For example, trying to call `Make` from another directory by specifying the full path the the `makefile` results in the following set of error messages:

```
make -f ~/github/stan-dev/cmdstan/makefile
/Users/mitzi/github/stan-dev/cmdstan/makefile:58: make/stanc: No such file or directory
/Users/mitzi/github/stan-dev/cmdstan/makefile:59: make/program: No such file or directory
/Users/mitzi/github/stan-dev/cmdstan/makefile:60: make/tests: No such file or directory
/Users/mitzi/github/stan-dev/cmdstan/makefile:61: make/command: No such file or directory
make: *** No rule to make target `make/command'. Stop.
```

Makefile rules can be written as general pattern rules based on file suffixes. The Stan makefile rules specify how to process Stan program files with suffix `.stan` into executable files. For example, to compile the Stan program `my_program.stan` in directory `../my_dir/`, the make target is `../my_dir/my_program` or `../my_dir/my_program.exe` (on Windows).

`Make` is invoked with a list of target names. Makefile targets can be preceded by zero or more Makefile variable `name=value` pairs. For example to compile `../my_dir/my_program.stan` for an OpenCL (GPU) machine, the makefile variable `STAN_OPENCL` is set to `TRUE`:

```
> make STAN_OPENCL=TRUE ../my_dir/my_program
```

Makefile variables can also be set by creating a file named `local` in the `CmdStan` `make` subdirectory which contains a list of `<VARIABLE>=<VALUE>` pairs, one per line. The complete set of Makefile variables can be found in file `cmdstan/stan/lib/stan_math/make/compiler_flags`.

When invoked without any arguments at all, `Make` prints a help message:

```
> make
```

```
-----
CmdStan v2.23.0 help
```

```
Build CmdStan utilities:
```

```
> make build
```

```
This target will:
```

1. Install the Stan compiler `bin/stanc` from `stanc3` binaries.
2. Build the print utility `bin/print` (deprecated; will be removed in v3).
3. Build the `stansummary` utility `bin/stansummary`

4. Build the diagnose utility `bin/diagnose`
5. Build all libraries and object files `compile` and link an executable `S`

Note: to build using multiple cores, use the `-j` option to `make`, e.g., for 4 cores:

```
> make build -j4
```

Build a Stan program:

Given a Stan program at `foo/bar.stan`, build an executable by typing:

```
> make foo/bar
```

This target will:

1. Install the Stan compiler (`bin/stanc` or `bin/stanc2`), as needed.
2. Use the Stan compiler to generate C++ code, `foo/bar.hpp`.
3. Compile the C++ code using `cc .` to generate `foo/bar`

Additional make options:

`STANCFLAGS`: defaults to `""`. These are extra options passed to `bin/stanc` when generating C++ code. If you want to allow undefined functions in Stan program, either add this to `make/local` or the command line:

```
STANCFLAGS = --allow_undefined
```

`USER_HEADER`: when `STANCFLAGS` has `--allow_undefined`, this is the name of header file that is included. This defaults to `"user_header.hpp"` in the directory of the Stan program.

`STANC2`: When set, use `bin/stanc2` to generate C++ code.

Example - bernoulli model: `examples/bernoulli/bernoulli.stan`

1. Build the model:
 

```
> make examples/bernoulli/bernoulli
```
2. Run the model:
 

```
> examples/bernoulli/bernoulli sample data file=examples/bernoulli/b
```
3. Look at the samples:
 

```
> bin/stansummary output.csv
```

Clean CmdStan:

```
Remove the built CmdStan tools:  
> make clean-all
```

---

## 1.2. Building CmdStan

Building CmdStan involves preparing a set of executable programs and compiling the command line interface and supporting libraries. The CmdStan tools are:

- **stanc**: the Stan compiler (translates Stan language to C++).
- **stansummary**: a basic posterior analysis tool. The **stansummary** utility processes one or more output files from a run or set of runs of Stan's HMC sampler. For all parameters and quantities of interest in the Stan program, **stansummary** reports a set of statistics including mean, standard deviation, percentiles, effective number of samples, and  $\hat{R}$  values.
- **diagnose**: a basic sampler diagnostic tool which checks for indications that the HMC sampler was unable to sample from the full posterior.

CmdStan releases include pre-built binaries of the Stan language compiler <https://github.com/stan-dev/stanc3>: **bin/linux-stanc**, **bin/mac-stanc** and **bin/windows-stanc**. The CmdStan makefile **build** task copies the appropriate binary to **bin/stanc**. For CmdStan installations which have been cloned or downloaded from the CmdStan GitHub repository, the makefile task will download the appropriate OS-specific binary from the stanc3 repository's nightly release.

Steps to build CmdStan:

- Download the latest release from <https://github.com/stan-dev/cmdstan/releases/latest> or clone the GitHub repo.
- Open a command-line terminal window and change directories to the CmdStan home directory.
- Run the makefile target **build** which instantiates the CmdStan utilities and compiles all necessary C++ libraries.

```
> cd <cmdstan-home>  
> make build
```

If your computer has multiple cores and sufficient ram, the build process can be parallelized by providing the **-j** option. For example, to build on 4 cores, type:

```
> make -j4 build
```

When `make build` is successful, the directory `<cmdstan-home>/bin/` will contain the executables `stanc`, `stansummary`, and `diagnose` (on Windows, corresponding `.exe` files) and the final lines of console output will show the version of CmdStan that has just been built, e.g.:

```
--- CmdStan v2.23.0 built ---
```

**Warning:** *The Make program may take 10+ minutes and consume 2+ GB of memory to build CmdStan.*

**Windows only:** CmdStan requires that the Intel TBB library, which is built by the above command, can be found by the Windows system. This requires that the directory `<cmdstan-home>/stan/lib/stan_math/lib/tbb` is part of the `PATH` environment variable. To permanently make this setting for the current user, you may execute:

```
> mingw32-make install-tbb
```

After changing the `PATH` environment variable, you must open a new shell in order for these settings to take effect. (This is not necessary on Mac and Linux systems because they can use the absolute path to the Intel TBB library when linking into Stan programs.)

### 1.3. Clone the GitHub CmdStan Repository

The CmdStan release tarfile contains all source files and libraries needed to build CmdStan. The CmdStan GitHub repo contains just the `cmdstan` module; the Stan inference engine algorithms and Stan math library functions are specified as submodules and stored in separate GitHub repositories. The CmdStan Makefile task `stan-update` assembles these submodules in the proper directory structure.

The following sequence of commands will check out the current CmdStan `develop` branch on GitHub and assemble and build the command line interface and supporting libraries:

```
> git clone https://github.com/stan-dev/cmdstan.git --recursive
> cd cmdstan
> make build
```

The resulting set of directories should have the same structure as the release:

- directory `cmdstan/stan` contains the sub-module `stan` (<https://github.com/stan-dev/stan>)
- directory `cmdstan/stan/lib/stan_math` contains the sub-module `math` (<https://github.com/stan-dev/math>)

## 1.4. Trouble-shooting the installation

To check that the CmdStan installation is complete and in working order, run the following series of commands:

```
# compile the example
> make examples/bernoulli/bernoulli

# fit to provided data (results of 10 trials, 2 out of 10 successes)
> ./examples/bernoulli/bernoulli sample data file=examples/bernoulli/bernoulli.json

# default output written to file `output.csv`,
# default num_samples is 1000, output file should have approx 1050 lines
> ls -l output.csv

# run the `bin/stansummary` utility to summarize parameter estimates
> bin/stansummary output.csv
```

The sample data in file `bernoulli.json.data` specifies 2 out of 10 successes, therefore the range `mean(theta)±sd(theta)` should include 0.2.

Updates to CmdStan or changes in compiler options may result in errors when trying to compile a Stan program. In some cases, these can be resolved by removing the existing CmdStan build and recompiling. The Makefile target `clean-all` should be run before rebuilding CmdStan:

```
> make clean-all
> make build
```

## 2. Example Model and Data

The following is a simple, complete Stan program for a Bernoulli model of binary data.<sup>1</sup> The model assumes the binary observed data  $y[1], \dots, y[N]$  are i.i.d. with Bernoulli chance-of-success  $\theta$ .

```
data {  
  int<lower=0> N;  
  int<lower=0,upper=1> y[N];  
}  
parameters {  
  real<lower=0,upper=1> theta;  
}  
model {  
  theta ~ beta(1,1); // uniform prior on interval 0,1  
  y ~ bernoulli(theta);  
}
```

The input data file contains definitions for the two variables  $N$  and  $y$  which are specified in the data block of program `bernoulli.stan` (above).

A data set of  $N=10$  observations is included in the example Bernoulli model directory in both JSON notation and Rdump data format where 8 out of 10 trials had outcome 0 (failure) and 2 trials had outcome 1 (success). In JSON, this data is:

```
{  
  "N" : 10,  
  "y" : [0,1,0,0,0,0,0,0,0,1]  
}
```

---

<sup>1</sup>The model is available with the CmdStan distribution at the path `<cmdstan-home>/examples/bernoulli/bernoulli.stan`.

## 3. Compiling a Stan Program

A Stan program must be in a file with extension `.stan`. The CmdStan makefile rules specify all necessary steps to translate files with suffix `.stan` to a CmdStan executable program. This is a two-stage process:

- first the Stan program is translated to C++ by the `stanc` compiler
- then the C++ compiler compiles all C++ sources and links them together with the CmdStan interface program and the Stan and math libraries.

### 3.1. Invoking the Make Utility

To compile Stan programs, you must invoke the Make program from the `<cmdstan-home>` directory. The Stan program can be in a different directory, but the directory path names cannot contain spaces - this limitation is imposed by Make.

```
> cd <cmdstan_home>
```

In the call to the Make program, the target is name of the CmdStan executable corresponding to the Stan program file. On Mac and Linux, this is the name of the Stan program with the `.stan` omitted. On Windows, replace `.stan` with `.exe`, and make sure that the path is given with slashes and not backslashes. To build the Bernoulli example, on Mac and Linux:

```
> make examples/bernoulli/bernoulli
```

On Windows, the command is the same with the addition of `.exe` at the end of the target (*note the use of forward slashes*):

```
> make examples/bernoulli/bernoulli.exe
```

The generated C++ code (`bernoulli.hpp`), object file (`bernoulli.o`) and the compiled executable will be placed in the same directory as the Stan program.

The compiled executable consists of the Stan model and the CmdStan command line interface which provides inference algorithms to do MCMC sampling, optimization, and variational inference. The following sections provide examples of doing inference using each method on the example model and data file.

### 3.2. Dependencies

When executing a make target, all its dependencies are checked to see if they are up to date, and if they are not, they are rebuilt. If the you call `make` with target `bernoulli`

twice, without any edits to `bernoulli.stan` or other changes to the system, the second call to `make` will be invoked a second time, it will see that it is up to date, and will not recompile the program:

```
> make examples/bernoulli/bernoulli
make: `examples/bernoulli/bernoulli' is up to date.
```

If the file containing the Stan program is updated, the next call to `make` will rebuild the `CmdStan` executable.

### 3.3. Compiler Errors

Stan probabilistic programming language is a programming language with a rich syntax, as such, it is often the case that a carefully written program contains errors, often simple syntax errors such as a misspelled variable name or missing semi-colon (;) statement termination.

For example, if in the `bernoulli.stan` program, we introduce a typo on line 9 by writing `thata` instead of `theta`, the `Make` command fails with the following

```
--- Translating Stan model to C++ code ---
bin/stanc --o=bernoulli.hpp bernoulli.stan
```

Semantic error in 'bernoulli.stan', line 9, column 2 to column 7:

```
-----
 7:  }
 8:  model {
 9:    thata ~ beta(1,1); // uniform prior on interval 0,1
    ^
10:    y ~ bernoulli(theta);
11:  }
-----
```

Identifier 'thata' not in scope.

```
make: *** [bernoulli.hpp] Error 1
```

### 3.4. Troubleshooting

The `stanc` compiler is also a program, and while it has been extensively tested, it may still contain errors such that the generated C++ code fails to compile. If this happens, report the error, together with the Stan program on either the Stan Forums or on the Stan compiler GitHub issues tracker.



## 4. MCMC Sampling

### 4.1. Running the Sampler

To generate a sample from the posterior distribution of the model conditioned on the data, we run the executable program with the argument `sample` or `method=sample` together with the input data. The executable can be run from any directory. Here, we run it in the directory which contains the Stan program and input data, `<cmdstan-home>/examples/bernoulli`:

```
> cd examples/bernoulli
```

To execute sampling of the model under Linux or Mac, use:

```
> ./bernoulli sample data file=bernoulli.data.json
```

In Windows, the `./` prefix is not needed:

```
> bernoulli.exe sample data file=bernoulli.data.json
```

The output is the same across all supported platforms. First, the configuration of the program is echoed to the standard output:

```
method = sample (Default)
sample
  num_samples = 1000 (Default)
  num_warmup = 1000 (Default)
  save_warmup = 0 (Default)
  thin = 1 (Default)
  adapt
    engaged = 1 (Default)
    gamma = 0.050000000000000003 (Default)
    delta = 0.80000000000000004 (Default)
    kappa = 0.75 (Default)
    t0 = 10 (Default)
    init_buffer = 75 (Default)
    term_buffer = 50 (Default)
    window = 25 (Default)
  algorithm = hmc (Default)
  hmc
    engine = nuts (Default)
```

```

nuts
  max_depth = 10 (Default)
  metric = diag_e (Default)
  metric_file = (Default)
  stepsize = 1 (Default)
  stepsize_jitter = 0 (Default)
id = 0 (Default)
data
  file = bernoulli.data.json
init = 2 (Default)
random
  seed = 3252652196 (Default)
output
  file = output.csv (Default)
  diagnostic_file = (Default)
  refresh = 100 (Default)

```

After the configuration has been displayed, a short timing message is given.

```
Gradient evaluation took 1.2e-05 seconds
```

```
1000 transitions using 10 leapfrog steps per transition would take 0.12 seconds
```

```
Adjust your expectations accordingly!
```

Next, the sampler reports the iteration number, reporting the percentage complete.

```
Iteration:    1 / 2000 [ 0%] (Warmup)
```

```
....
```

```
Iteration: 2000 / 2000 [100%] (Sampling)
```

Finally, the sampler reports timing information:

```

Elapsed Time: 0.007 seconds (Warm-up)
              0.017 seconds (Sampling)
              0.024 seconds (Total)

```

## 4.2. Running Multiple Chains

A Markov chain generates samples from the target distribution only after it has converged to equilibrium. In theory, convergence is only guaranteed asymptotically as the number of draws grows without bound. In practice, diagnostics must be applied to monitor convergence for the finite number of draws actually available. One way to monitor whether a chain has converged to the equilibrium distribution is to compare its behavior to other randomly initialized chains. For robust diagnostics, we recommend running 4 chains.

To run multiple chains given a model and data, either sequentially or in parallel, we use the Unix or DOS shell for loop to set up index variables needed to identify each chain and its outputs.

On MacOS or Linux, the for-loop syntax for both the bash and zsh interpreters is:

```
for NAME [in LIST]; do COMMANDS; done
```

The list can be a simple sequence of numbers, or you can use the shell expansion syntax `{1..N}` which expands to the sequence from 1 to  $N$ , e.g. `{1..4}` expands to 1 2 3 4. Note that the expression `{1..N}` cannot contain spaces.

To run 4 chains for the example bernoulli model on MacOS or Linux:

```
> for i in {1..4}
do
    ./bernoulli sample data file=bernoulli.data.json \
    output file=output_${i}.csv
done
```

The backslash (\) indicates a line continuation in Unix. The expression `${i}` substitutes in the value of loop index variable `i`. To run chains in parallel, put an ampersand (&) at the end of the nested sampler command:

```
> for i in {1..4}
do
    ./bernoulli sample data file=bernoulli.data.json \
    output file=output_${i}.csv &
done
```

This pushes each process into the background which allows the loop to continue without waiting for the current chain to finish.

On Windows, the DOS for-loop syntax is one of:

```
for %i in (SET) do COMMAND COMMAND-ARGUMENTS
for /l %i in (START, STEP, END) do COMMAND COMMAND-ARGUMENTS
```

To run 4 chains in parallel on Windows:

```
>for /l %i in (1, 1, 4) do start /b bernoulli.exe sample ^
    data file=bernoulli.data.json my_data ^
    output file=output_%i.csv
```

The caret (^) indicates a line continuation in DOS.

### 4.3. Stan CSV Output File

Each execution of the model results in draws from a single Markov chain being written to a file in comma-separated value (CSV) format. The default name of the output file is `output.csv`.

The first part of the output file records the version of the underlying Stan library and the configuration as comments (i.e., lines beginning with the pound sign (#)).

```
# stan_version_major = 2
# stan_version_minor = 23
# stan_version_patch = 0
# model = bernoulli_model
# method = sample (Default)
#   sample
#     num_samples = 1000 (Default)
#     num_warmup = 1000 (Default)
...
# output
#   file = output.csv (Default)
#   diagnostic_file = (Default)
#   refresh = 100 (Default)
```

This is followed by a CSV header indicating the names of the values sampled.

```
lp__,accept_stat__,stepsize__,treedepth__,n_leapfrog__,divergent__,energy__.
```

The first output columns report the HMC sampler information:

- `lp__` - the total log probability density (up to an additive constant) at each sample
- `accept_stat__` - the average Metropolis acceptance probability over each simulated Hamiltonian trajectory
- `stepsize__` - integrator step size
- `treedepth__` - depth of tree used by NUTS (NUTS sampler)
- `n_leapfrog__` - number of leapfrog calculations (NUTS sampler)
- `divergent__` - has value 1 if trajectory diverged, otherwise 0. (NUTS sampler)
- `energy__` - value of the Hamiltonian
- `int_time__` - total integration time (HMC sampler)

The remaining columns correspond to model parameters. For the Bernoulli model, it is just the final column, `theta`.

The header line is written to the output file before warmup begins. If option `save_warmup` is set to 1, the warmup draws are output directly after the header.

The total number of warmup draws saved is `num_warmup` divided by `thin`, rounded up (i.e., ceiling).

Following the warmup draws (if any), are comments which record the results of adaptation: the stepsize, and inverse mass metric used during sampling:

```
# Adaptation terminated
# Step size = 0.884484
# Diagonal elements of inverse mass matrix:
# 0.535006
```

The default sampler is NUTS with an adapted step size and a diagonal inverse mass matrix. For this example, the step size is 0.884484, and the inverse mass contains the single entry 0.535006 corresponding to the parameter `theta`.

Draws from the posterior distribution are printed out next, each line containing a single draw with the columns corresponding to the header.

```
-6.84097,0.974135,0.884484,1,3,0,6.89299,0.198853
-6.91767,0.985167,0.884484,1,1,0,6.92236,0.182295
-7.04879,0.976609,0.884484,1,1,0,7.05641,0.162299
-6.88712,1,0.884484,1,1,0,7.02101,0.188229
-7.22917,0.899446,0.884484,1,3,0,7.73663,0.383596
...
```

The output ends with timing details:

```
# Elapsed Time: 0.007 seconds (Warm-up)
#               0.017 seconds (Sampling)
#               0.024 seconds (Total)
```

#### 4.4. Summarizing Sampler Output(s) with `stansummary`

The `stansummary` utility processes one or more output files from a run or set of runs of Stan's HMC sampler given a model and data. For all columns in the Stan csv output file `stansummary` reports a set of statistics including mean, standard deviation, percentiles, effective number of samples, and  $\hat{R}$  values.

To run `stansummary` on the output files generated by the for loop above, by the above run of the `bernoulli` model on Mac or Linux:

```
<cmdstan-home>/bin/stansummary output_*.csv
```

On Windows, use backslashes to call the `stansummary.exe`.

```
<cmdstan-home>\bin\stansummary.exe output_*.csv
```

The stansummary output consists of one row of statistics per column in the Stan csv output file. Therefore, the first rows in the stansummary report statistics over the sampler state. The final row of output summarizes the estimates of the model variable theta:

Inference for Stan model: bernoulli\_model

4 chains: each with iter=(1000,1000,1000,1000); warmup=(0,0,0,0); thin=(1,1,1,1)

Warmup took (0.0070, 0.0070, 0.0070, 0.0070) seconds, 0.028 seconds total

Sampling took (0.020, 0.017, 0.021, 0.019) seconds, 0.077 seconds total

	Mean	MCSE	StdDev	5%	50%	95%	N_Eff	N_Eff/s
lp__	-7.3	1.8e-02	0.75	-8.8	-7.0	-6.8	1.8e+03	2.4e+04
accept_stat__	0.89	2.7e-03	0.17	0.52	0.96	1.0	3.9e+03	5.1e+04
stepsize__	1.1	7.5e-02	0.11	0.93	1.2	1.2	2.0e+00	2.6e+01
treedepth__	1.4	8.1e-03	0.49	1.0	1.0	2.0	3.6e+03	4.7e+04
n_leapfrog__	2.3	1.7e-02	0.98	1.0	3.0	3.0	3.3e+03	4.3e+04
divergent__	0.00	nan	0.00	0.00	0.00	0.00	nan	nan
energy__	7.8	2.6e-02	1.0	6.8	7.5	9.9	1.7e+03	2.2e+04
theta	0.25	2.9e-03	0.12	0.079	0.23	0.46	1.7e+03	2.1e+04

Samples were drawn using hmc with nuts.

For each parameter, N\_Eff is a crude measure of effective sample size, and R\_hat is the potential scale reduction factor on split chains (at convergence, R\_hat=1).

In this example, we conditioned the model on a dataset consisting of the outcomes of 10 bernoulli trials, where only 2 trials reported success. The 5%, 50%, and 95% percentile values for theta reflect the uncertainty in our estimate, due to the small amount of data, given the prior of beta(1, 1)

## 5. Optimization

The CmdStan executable can run Stan's optimization algorithms for penalized maximum likelihood estimation which provide a deterministic method to find the posterior mode. If the posterior is not convex, there is no guarantee Stan will be able to find the global mode as opposed to a local optimum of log probability.

The executable does not need to be recompiled in order to switch from sampling to optimization, and the data input format is the same. The following is a minimal call to Stan's optimizer using defaults for everything but the location of the data file.

```
> ./bernoulli optimize data file=bernoulli.data.json
```

Executing this command prints both output to the console and to a csv file.

The first part of the console output reports on the configuration used. The above command uses all default configurations, therefore the optimizer used is the L-BFGS optimizer and its default initial stepsize and tolerances for monitoring convergence:

```
./bernoulli optimize data file=bernoulli.data.json
method = optimize
  optimize
    algorithm = lbfgs (Default)
      lbfgs
        init_alpha = 0.001 (Default)
        tol_obj = 9.999999999999998e-13 (Default)
        tol_rel_obj = 10000 (Default)
        tol_grad = 1e-08 (Default)
        tol_rel_grad = 10000000 (Default)
        tol_param = 1e-08 (Default)
        history_size = 5 (Default)
      iter = 2000 (Default)
      save_iterations = 0 (Default)
    id = 0 (Default)
  data
    file = bernoulli.data.json
  init = 2 (Default)
  random
    seed = 3316231346 (Default)
```

```

output
  file = output.csv (Default)
  diagnostic_file = (Default)
  refresh = 100 (Default)

```

The second part of the output indicates how well the algorithm fared, here converging and terminating normally. The numbers reported indicate that it took 5 iterations and 8 gradient evaluations. This is, not surprisingly, far fewer iterations than required for sampling; even fewer iterations would be used with less stringent user-specified convergence tolerances. The alpha value is for step size used. In the final state the change in parameters was roughly 0.0002 and the length of the gradient roughly  $9e-8$ .

```
Initial log joint probability = -5.26908
```

Iter	log prob	dx	grad	alpha	alpha0
5	-5.00402	0.000172451	9.39034e-08	1	1

```
Optimization terminated normally:
```

```
Convergence detected: relative gradient magnitude is below tolerance
```

The output from optimization is written into the file `output.csv` by default. The output follows the same pattern as the output for sampling, first dumping the entire set of parameters used as comment lines:

```

# stan_version_major = 2
# stan_version_minor = 23
# stan_version_patch = 0
# model = bernoulli_model
# method = optimize
#   optimize
#     algorithm = lbfgs (Default)
...

```

Following the config information, are two lines of output: the CSV headers and the recorded values:

```

lp__,theta
-5.00402,0.2

```

Note that everything is a comment other than a line for the header, and a line for the values. Here, the header indicates the unnormalized log probability with `lp__` and the model parameter `theta`. The maximum log probability is -5.0 and the posterior mode for `theta` is 0.20. The mode exactly matches what we would expect from the data.<sup>1</sup>

---

<sup>1</sup>The Jacobian adjustment included for the sampler's log probability function is not applied during optimization, because it can change the shape of the posterior and hence the solution.



Because the prior was uniform, the result 0.20 represents the maximum likelihood estimate (MLE) for the very simple Bernoulli model. Note that no uncertainty is reported.

## 6. Variational Inference

CmdStan can approximate the posterior distribution using variational inference. The approximation is a Gaussian in the unconstrained variable space. Stan implements two variational algorithms. The `algorithm=meanfield` option uses a fully factorized Gaussian for the approximation. The `algorithm=fullrank` option uses a Gaussian with a full-rank covariance matrix for the approximation.

The executable does not need to be recompiled in order to switch to variational inference, and the data input format is the same. The following is a minimal call to Stan's variational inference algorithm using defaults for everything but the location of the data file.

```
> ./bernoulli variational data file=bernoulli.data.R
```

Executing this command prints both output to the console and to a csv file.

The first part of the console output reports on the configuration used. Here it indicates the default mean-field setting of the variational inference algorithm. It also indicates the default parameter sizes and tolerances for monitoring the algorithm's convergence.

```
method = variational
  variational
    algorithm = meanfield (Default)
      meanfield
    iter = 10000 (Default)
    grad_samples = 1 (Default)
    elbo_samples = 100 (Default)
    eta = 1 (Default)
    adapt
      engaged = 1 (Default)
      iter = 50 (Default)
    tol_rel_obj = 0.01 (Default)
    eval_elbo = 100 (Default)
    output_samples = 1000 (Default)
  id = 0 (Default)
data
  file = bernoulli.data.json
  init = 2 (Default)
```

```

random
  seed = 3323783840 (Default)
output
  file = output.csv (Default)
  diagnostic_file = (Default)
  refresh = 100 (Default)

```

After the configuration has been displayed, informational and timing messages are output:

-----  
 EXPERIMENTAL ALGORITHM:

This procedure has not been thoroughly tested and may be unstable or buggy. The interface is subject to change.

-----

Gradient evaluation took 2.1e-05 seconds  
 1000 transitions using 10 leapfrog steps per transition would take 0.21 seconds  
 Adjust your expectations accordingly!

The rest of the output describes the progression of the algorithm. An adaptation phase finds a good value for the step size scaling parameter  $\eta$ . The evidence lower bound (ELBO) is the variational objective function and is evaluated based on a Monte Carlo estimate. The variational inference algorithm in Stan is stochastic, which makes it challenging to assess convergence. That is, while the algorithm appears to have converged in  $\sim 250$  iterations, the algorithm runs for another few thousand iterations until mean change in ELBO drops below the default tolerance of 0.01.

Begin  $\eta$  adaptation.

```

Iteration: 1 / 250 [ 0%] (Adaptation)
Iteration: 50 / 250 [ 20%] (Adaptation)
Iteration: 100 / 250 [ 40%] (Adaptation)
Iteration: 150 / 250 [ 60%] (Adaptation)
Iteration: 200 / 250 [ 80%] (Adaptation)
Success! Found best value [eta = 1] earlier than expected.

```

Begin stochastic gradient ascent.

iter	ELBO	delta_ELBO_mean	delta_ELBO_med	notes
100	-6.131	1.000	1.000	
200	-6.458	0.525	1.000	
300	-6.300	0.359	0.051	
400	-6.137	0.276	0.051	

500	-6.243	0.224	0.027	
600	-6.305	0.188	0.027	
700	-6.289	0.162	0.025	
800	-6.402	0.144	0.025	
900	-6.103	0.133	0.025	
1000	-6.314	0.123	0.027	
1100	-6.348	0.024	0.025	
1200	-6.244	0.020	0.018	
1300	-6.293	0.019	0.017	
1400	-6.250	0.017	0.017	
1500	-6.241	0.015	0.010	MEDIAN ELBO COM

Drawing a sample of size 1000 from the approximate posterior...  
COMPLETED.

The output from variational is written into the file `output.csv` by default. The output follows the same pattern as the output for sampling, first dumping the entire set of parameters used as CSV comments:

```
# stan_version_major = 2
# stan_version_minor = 23
# stan_version_patch = 0
# model = bernoulli_model
# method = variational
#   variational
#     algorithm = meanfield (Default)
#       meanfield
#         iter = 10000 (Default)
#         grad_samples = 1 (Default)
#         elbo_samples = 100 (Default)
#         eta = 1 (Default)
#       adapt
#         engaged = 1 (Default)
#         iter = 50 (Default)
#         tol_rel_obj = 0.01 (Default)
#         eval_elbo = 100 (Default)
#         output_samples = 1000 (Default)
...
```

Next is the column header line, followed more CSV comments reporting the adapted value for the stepsize, followed by the values. The first line is special: it is the mean

of the variational approximation. The rest of the output contains `output_samples` number of samples drawn from the variational approximation.

```
lp__,log_p__,log_g__,theta
# Stepsize adaptation complete.
# eta = 1
0,0,0,0.236261
0,-6.82318,-0.0929121,0.300415
0,-6.89701,-0.158687,0.321982
0,-6.99391,-0.23916,0.343643
0,-7.35801,-0.51787,0.401554
0,-7.4668,-0.539473,0.123081
...
```

The header indicates the unnormalized log probability with `lp__`. This is a legacy feature that we do not use for variational inference. The ELBO is not stored unless a diagnostic option is given.

For further details, see Kucukelbir, Alp, Rajesh Ranganath, Andrew Gelman, and David M. Blei. 2015. *Automatic Variational Inference in Stan*. arXiv 1506.03431. <http://arxiv.org/abs/1506.03431>.

## 7. Generating Quantities of Interest from a Fitted Model

The generated quantities block computes *quantities of interest* (QOIs) based on the data, transformed data, parameters, and transformed parameters. It can be used to:

- generate simulated data for model testing by forward sampling
- generate predictions for new data
- calculate posterior event probabilities, including multiple comparisons, sign tests, etc.
- calculating posterior expectations
- transform parameters for reporting
- apply full Bayesian decision theory
- calculate log likelihoods, deviances, etc. for model comparison

The `generate_quantities` method allows you to generate additional quantities of interest from a fitted model without re-running the sampler. Instead, you write a modified version of the original Stan program and add a generated quantities block or modify the existing one which specifies how to compute the new quantities of interest. Running the `generate_quantities` method on the new program together with sampler outputs from the fitted model runs the generated quantities block of the new program using the estimated parameter values from the existing sample.

To illustrate how this works, we add posterior predictive checks to the example model `bernoulli.stan`. We create a new model, `bernoulli_yrep.stan` which contains the following generated quantities block:

```
generated quantities {  
  int y_sim[N];  
  real<lower=0,upper=1> theta_rep;  
  for (n in 1:N)  
    y_sim[n] = bernoulli_rng(theta);  
  theta_rep = sum(y) / N;  
}
```

We compile this model, and then run it with the fit from a previous run of the original model and the same input data file:

```
> ./bernoulli_yrep generate_quantities ....
```

# CmdStan Reference

This section provides a complete reference for all CmdStan methods:

- `sample`
- `optimize`
- `variational`
- `generate_quantities`
- `diagnose`
- `help`

## 8. Command-Line Interface Overview

A CmdStan executable is built from the Stan model concept and the CmdStan command line parser. The command line argument syntax consists of sets of keywords and keyword-value pairs. Arguments are grouped by the following keywords:

- **method** - specifies the kind of inference done on the model. Each kind of inference requires further configuration via sub-arguments. The **method** argument is required. It can be specified overtly as the a keyword-value pair **method=<inference>** or implicitly as one of the following:
  - **sample** - obtain a sample from the posterior using HMC
  - **optimize** - penalized maximum likelihood estimation
  - **variational** - automatic variational inference
  - **generate\_quantities** - run model's **generated quantities** block on existing sample to obtain new quantities of interest.
- **diagnose** - compute and compare sampler gradient calculations to finite differences.
- **data** - specifies the input data file, if any.
- **output** - specifies program outputs, both disk files and terminal window outputs.
- **init** - specifies initial values for the model parameters, if any.
- **random** - specifies the seed for the psuedo-random number.

The remainder of this chapter covers the general configuration options used for all processing. The following chapters cover the per-inference configuration options.

### 8.1. Input Data Argument

The values for all variables declared in the data block of the model are read in from an input data file in either JSON or Rdump format. The syntax for the input data argument is:

```
data file=<filepath>
```

The keyword **data** must be followed directly by the keyword-value pair **file=<filepath>**. If the model doesn't declare any data variables, this argument is ignored.



The input data file must contain definitions for all data variables declared in the data block. If one or more data block variables are missing from the input data file, the program will print an error message to the terminal. For example, the model `bernoulli.stan` defines two data variables `N` and `y`. If the input data file doesn't include both variables, or if the data variable doesn't match the declared type and dimensions, the program will exit with an error message at the point where it first encounters missing data.

For example if the input data file doesn't include the definition for variable `y`, the executable exits with the following message:

Exception: variable does not exist; processing stage=data initialization; va

## 8.2. Output Control Arguments

The `output` keyword is used to specify non-default options for output files and messages written to the terminal window. The `output` keyword takes several keyword-value pair sub-arguments.

The keyword value pair `file=<filepath>` specifies the location of the Stan csv output file. If unspecified, the output file is written to a file named `output.csv` in the current working directory.

The keyword value pair `diagnostic_file=<filepath>` specifies the location of the auxiliary output file. By default, no auxiliary output file is produced.

The keyword value pair `refresh=<int>` specifies the number of iterations between progress messages written to the terminal window. The default value is 100 iterations.

## 8.3. Initialize Model Parameters Argument

Initialization is only applied to parameters defined in the parameters block. By default, all parameters are initialized to random draws from a uniform distribution over the range  $[-2, 2]$ . These values are on the unconstrained scale, so must be inverse transformed back to satisfy the constraints declared for parameters. Because zero is chosen to be a reasonable default initial value for most parameters, the interval around zero provides a fairly diffuse starting point. For instance, unconstrained variables are initialized randomly in  $(-2, 2)$ , variables constrained to be positive are initialized roughly in  $(0.14, 7.4)$ , variables constrained to fall between 0 and 1 are initialized with values roughly in  $(0.12, 0.88)$ .

The initialization argument is specified as keyword-value pair with keyword `init`. The value can be one of the following:

- positive real number  $x$ . All parameters will be initialized to random draws from a uniform distribution over the range  $[-x, x]$ .

- 0 - All parameters will be initialized to zero values on the unconstrained scale. The transforms are arranged in such a way that zero initialization provides reasonable variable initializations: 0 for unconstrained parameters; 1 for parameters constrained to be positive; 0.5 for variables constrained to lie between 0 and 1; a symmetric (uniform) vector for simplexes; unit matrices for both correlation and covariance matrices; and so on.
- `filepath` - A data file in JSON or Rdump format containing initial parameters values for some or all of the model parameters. User specified initial values must satisfy the constraints declared in the model (i.e., they are on the constrained scale). Parameters which aren't explicitly initialized will be initialized randomly over the range  $[-2, 2]$ .

## 8.4. Random Number Generator Arguments

The random-number generator's behavior is determined by the unsigned seed (positive integer) it is started with. If a seed is not specified, or a seed of 0 or less is specified, the system time is used to generate a seed. The seed is recorded and included with Stan's output regardless of whether it was specified or generated randomly from the system time.

The syntax for the random seed argument is:

```
random seed=<int>
```

The keyword `random` must be followed directly by the keyword-value pair `seed=<int>`.

## 8.5. Chain Identifier Argument: `id`

The chain identifier argument is used in conjunction with the `random seed` argument when running multiple Markov chains for sampling. The chain identifier is used to advance the random number generator a very large number of random variates so that two chains with the same seed and different identifiers draw from non-overlapping subsequences of the random-number sequence determined by the seed. Together, the seed and chain identifier determine the behavior of the random number generator.

The syntax for the random seed argument is:

```
id=<int>
```

The default value is 0.

When running a set of chains from the command line with a specified seed, this argument should be set to the chain index. E.g., when running 4 chains, the value should be 1,...,4, successively. When running multiple chains from a single command, Stan's interfaces manage the chain identifier arguments automatically.

For complete reproducibility, every aspect of the environment needs to be locked down from the OS and version to the C++ compiler and version to the version of Stan and all dependent libraries. See the Stan Reference Manual Reproducibility chapter for further details.

## 8.6. Command Line Help

CmdStan provides a `help` and `help-all` mechanism that displays either the available top-level or keyword-specific key-value argument pairs. To display top-level help, call the CmdStan executable with keyword `help`:

```
> ./bernoulli help
```

```
Usage: ./bernoulli <arg1> <subarg1_1> ... <subarg1_m> ... <arg_n> <subarg_n_1> ...
```

Begin by selecting amongst the following inference methods and diagnostics,

<code>sample</code>	Bayesian inference with Markov Chain Monte Carlo
<code>optimize</code>	Point estimation
<code>variational</code>	Variational inference
<code>diagnose</code>	Model diagnostics
<code>generate_quantities</code>	Generate quantities of interest

Or see help information with

<code>help</code>	Prints help
<code>help-all</code>	Prints entire argument tree

Additional configuration available by specifying

<code>id</code>	Unique process identifier
<code>data</code>	Input data options
<code>init</code>	Initialization method: "x" initializes randomly between [-x, x]
<code>random</code>	Random number configuration
<code>output</code>	File output options

See `./bernoulli <arg1> [ help | help-all ]` for details on individual arguments.

## 9. MCMC Sampling using Hamiltonian Monte Carlo

The `sample` method provides Bayesian inference over the model conditioned on data using Hamiltonian Monte Carlo (HMC) sampling. By default, the inference engine used is the No-U-Turn sampler (NUTS), an adaptive form of Hamiltonian Monte Carlo sampling. For details on HMC and NUTS, see the Stan Reference Manual chapter on MCMC Sampling.

The full set of configuration options available for the `sample` method is reported at the beginning of the sampler output file as csv comments. When the example model `bernoulli.stan` is run via the command line with all default arguments, the resulting Stan csv file header comments show the complete set of default configuration options:

```
# model = bernoulli_model
# method = sample (Default)
#   sample
#     num_samples = 1000 (Default)
#     num_warmup = 1000 (Default)
#     save_warmup = 0 (Default)
#     thin = 1 (Default)
#     adapt
#       engaged = 1 (Default)
#       gamma = 0.05 (Default)
#       delta = 0.8 (Default)
#       kappa = 0.75 (Default)
#       t0 = 10 (Default)
#       init_buffer = 75 (Default)
#       term_buffer = 50 (Default)
#       window = 25 (Default)
#     algorithm = hmc (Default)
#       hmc
#         engine = nuts (Default)
#           nuts
#             max_depth = 10 (Default)
#             metric = diag_e (Default)
#             metric_file = (Default)
```

```
#         stepsize = 1 (Default)
#         stepsize_jitter = 0 (Default)
```

## 9.1. Iterations

At every sampler iteration, the sampler returns a set of estimates for all parameters and quantities of interest in the model. During warmup, the NUTS algorithm adjusts the HMC algorithm parameters `metric` and `stepsize` in order to efficiently sample from *typical set*, the neighborhood substantial posterior probability mass through which the Markov chain will travel in equilibrium. After warmup, the fixed metric and stepsize are used to produce a set of draws.

The following keyword-value arguments control the total number of iterations:

- `num_samples`
- `num_warmup`
- `save_warmup`
- `thin`

The values for arguments `num_samples` and `num_warmup` must be a non-negative integer. The default value for both is 1000.

For well-specified models and data, the sampler may converge faster and this many warmup iterations may be overkill. Conversely, complex models which have difficult posterior geometries may require more warmup iterations in order to arrive at good values for the step size and metric.

The number of sampling iterations to runs depends on the effective sample size (EFF) reported for each parameter and the desired precision of your estimates. An EFF of at least 100 is required to make a viable estimate. The precision of your estimate is  $\sqrt{N}$ ; therefore every additional decimal place of accuracy increases this by a factor of 10.

Argument `save_warmup` takes the value of either 0 or 1, which correspond to `False` and `True` respectively. The default value is 0, i.e., warmup draws are not saved to the output file. When the value is 1, the warmup draws are written to the csv output file directly after the csv header line.

Argument `thin` controls the number of draws from the posterior written to the output file. The value of argument `thin` must be a positive integer. When `thin` is set to value  $N$ , every  $N^{th}$  iteration is written to the output file.

Should the value of `thin` exceed the specified number of iterations, the first iteration is saved to the output. This is because the iteration counter starts from zero and whenever the counter modulo the value of `thin` equals zero, the iteration is saved to the output file. Since zero modulo any positive integer is zero, the first iteration is

always saved. When `num_sampling=M` and `thin=N`, the number of iterations written to the output csv file will be `ceiling(M/N)`. If `save_warmup=1`, thinning is applied to the warmup iterations as well.

## 9.2. Adaptation

The `adapt` keyword is used to specify non-default options for the sampler adaptation schedule and settings.

Adaptation can be turned off by setting sub-argument `engaged` to value 0. If `engaged=0`, no adaptation will be done, and all other adaptation sub-arguments will be ignored. Since the default argument is `engaged=1`, this keyword-value pair can be omitted from the command.

There are two sets of adaptation sub-arguments: step size optimization parameters and the warmup schedule. These are described in detail in the Reference Manual section Automatic Parameter Tuning.

### Step size optimization configuration

The following keyword-value arguments control the settings used to optimize the step size:

- `delta` - The target Metropolis acceptance rate. The default value is 0.8. Its value must be strictly between 0 and 1. Increasing the default value forces the algorithm to use smaller step sizes. This can improve sampling efficiency (effective sample size per iteration) at the cost of increased iteration times. Raising the value of `delta` will also allow some models that would otherwise get stuck to overcome their blockages.
- `gamma` - Adaptation regularization scale. Must be a positive real number, default value is 0.05. This is a parameter of the Nesterov dual-averaging algorithm. We recommend always using the default value.
- `gamma` - Adaptation relaxation exponent. Must be a positive real number, default value is 0.75. This is a parameter of the Nesterov dual-averaging algorithm. We recommend always using the default value.
- `t_0` - Adaptation iteration offset. Must be a positive real number, default value is 10. This is a parameter of the Nesterov dual-averaging algorithm. We recommend always using the default value.

### Warmup schedule configuration

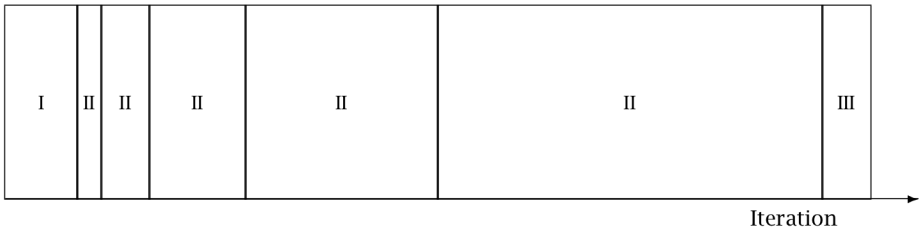
When adaptation is engaged, the warmup schedule is specified by sub-arguments, all of which take positive integers as values:

- `init_buffer` - The number of iterations spent tuning the step size at the outset of adaptation.
- `window` - The initial number of iterations devoted to tune the metric, will be doubled successively.
- `term_buffer` - The number of iterations used to re-tune the step size once the metric has been tuned.

The specified values may be modified slightly in order to ensure alignment between the warmup schedule and total number of warmup iterations.

The following figure is taken from the Stan Reference Manual, where label “I” correspond to `init_buffer`, the initial “II” corresponds to `window`, and the final “III” corresponds to `term_buffer`:

**Warmup Epochs Figure.** *Adaptation during warmup occurs in three stages: an initial fast adaptation interval (I), a series of expanding slow adaptation intervals (II), and a final fast adaptation interval (III). For HMC, both the fast and slow intervals are used for adapting the step size, while the slow intervals are used for learning the (co)variance necessitated by the metric. Iteration numbering starts at 1 on the left side of the figure and increases to the right.*



### 9.3. Algorithm

The `algorithm` keyword-value pair specifies the algorithm used to generate the sample. There are two possible values: `hmc`, which generates from an HMC-driven Markov chain; and `fixed_param` which generates a new sample without changing the state of the Markov chain. The default argument is `algorithm=hmc`.

#### Samples from a set of fixed parameters

If a model doesn't specify any parameters, then argument `algorithm=fixed_param` is mandatory.

The fixed parameter sampler generates a new sample without changing the current state of the Markov chain. This can be used to write models which generate pseudo-data via calls to RNG functions in the transformed data and generated quantities

blocks.

### HMC samplers

All HMC algorithms have three parameters:

- step size
- metric
- integration time - the number of steps taken along the Hamiltonian trajectory

See the Stan Reference Manual section on HMC algorithm parameters for further details.

#### *Step size*

The HMC algorithm simulates the evolution of a Hamiltonian system. The step size parameter controls the resolution of the sampler. Low step sizes can get HMC samplers unstuck that would otherwise get stuck with higher step sizes.

The following keyword-value arguments control the step size:

- **stepsize** - How far to move each time the Hamiltonian system evolves forward. Must be a positive real number, default value is 1.
- **stepsize\_jitter** - Allows step size to be “jittered” randomly during sampling to avoid any poor interactions with a fixed step size and regions of high curvature. Must be a real value between 0 and 1. The default value is 0. Setting **stepsize\_jitter** to 1 causes step sizes to be selected in the range of 0 to twice the adapted step size. Jittering below the adapted value will increase the number of steps required and will slow down sampling, while jittering above the adapted value can cause premature rejection due to simulation error in the Hamiltonian dynamics calculation. We strongly recommend always using the default value.

#### *Metric*

All HMC implementations in Stan utilize quadratic kinetic energy functions which are specified up to the choice of a symmetric, positive-definite matrix known as a *mass matrix* or, more formally, a *metric* Betancourt (2017).

The **metric** argument specifies the choice of Euclidean HMC implementations:

- **metric=unit** specifies unit metric (diagonal matrix of ones).
- **metric=diag\_e** specifies a diagonal metric (diagonal matrix with positive diagonal entries). This is the default value.



- `metric=dense_e` specifies a dense metric (a dense, symmetric positive definite matrix).

By default, the metric is estimated during warmup. However, when `metric=diag_e` or `metric=dense_e`, an initial guess for the metric can be specified with the `metric_file` argument whose value is the filepath to a JSON or Rdump file which contains a single variable `inv_metric`. For a `diag_e` metric the `inv_metric` value must be a vector of positive values, one for each parameter in the system. For a `dense_e` metric, `inv_metric` value must be a positive-definite square matrix with number of rows and columns equal to the number of parameters in the model.

The `metric_file` option can be used with and without adaptation enabled. If adaptation is enabled, the provided metric will be used as the initial guess in the adaptation process. If the initial guess is good, then adaptation should not change it much. If the metric is no good, then the adaptation will override the initial guess.

If adaptation is disabled, both the `metric_file` and `stepsize` arguments should be specified.

### *Integration Time*

The total integration time is determined by the argument `engine` which take possible values:

- `nuts` - the No-U-Turn Sampler which dynamically determines the optimal integration time.
- `static` - an HMC sampler which uses a user-specified integration time.

The default argument is `engine=nuts`.

The NUTS sampler generates a proposal by starting at an initial position determined by the parameters drawn in the last iteration. It then evolves the initial system both forwards and backwards in time to form a balanced binary tree. The algorithm is iterative; at each iteration the tree depth is increased by one, doubling the number of leapfrog steps thus effectively doubling the computation time. The algorithm terminates in one of two ways: either the NUTS criterion (i.e., a U-turn in Euclidean space on a subtree) is satisfied for a new subtree or the completed tree; or the depth of the completed tree hits the maximum depth allowed.

When `engine=nuts`, the subargument `max_depth` can be used to control the depth of the tree. The default argument is `max_depth=10`. In the case where a model has a difficult posterior from which to sample, `max_depth` should be increased to ensure that that the NUTS tree can grow as large as necessary.

When the argument `engine=static` is specified, the user must specify the integration time via keyword `int_time` which takes as a value a positive number. The default value is  $2\pi$ .

## 9.4. Sampler Diagnostic File

The output keyword sub-argument `diagnostic_file=<filepath>` specifies the location of the auxiliary output file which contains sampler information for each draw, including the gradients on the unconstrained scale and log probabilities. By default, no auxiliary output file is produced.

## 9.5. Examples

The Quickstart Guide MCMC Sampling chapter section on multiple chains showed how to run multiple chains given a model and data, using the minimal required command line options: the method, the name of the data file, and a chain-specific name for the output file.

To run 4 chains in parallel on Mac OS and Linux, the syntax in both bash and zsh is the same:

```
> for i in {1..4}
do
    ./bernoulli sample data file=my_model.data.json \
        output file=output_${i}.csv &
done
```

The backslash (\) indicates a line continuation in Unix. The expression `${i}` substitutes in the value of loop index variable `i`. The ampersand (&) pushes each process into the background which allows the loop to continue without waiting for the current chain to finish.

On Windows the corresponding loop is:

```
>for /! %i in (1, 1, 4) do start /b bernoulli.exe sample ^
    data file=my_model.data.json my_data ^
    output file=output_%i.csv
```

The caret (^) indicates a line continuation in DOS. The expression `%i` is the loop index.

In the following examples, we focus on just the nested sampler command for Unix.

### Running multiple chains with a specified RNG seed

For reproducibility, we specify the same RNG seed across all chains and use the chain id argument to specify the RNG offset.

The RNG seed is specified by `random seed=<int>` and the offset is specified by

`id=<loop index>`, so the call to the sampler is:

```
./my_model sample data file=my_model.data.json \
  output file=output_${i}.csv \
  random seed=12345 id=${i}
```

### Changing the default warmup and sampling iterations

The warmup and sampling iteration keyword-value arguments must follow the `sample` keyword. The call to the sampler which overrides the default warmup and sampling iterations is:

```
./my_model sample num_warmup=500 num_sampling=500 \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

### Saving warmup draws

To save warmup draws as part of the Stan csv output file, use the keyword-value argument `save_warmup=1`. This must be grouped with the other `sample` keyword sub-arguments.

```
./my_model sample num_warmup=500 num_sampling=500 save_warmup=1 \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

### Initializing parameters

By default, all parameters are initialized on an unconstrained scale to random draws from a uniform distribution over the range  $[-2, 2]$ . To initialize some or all parameters to good starting points on the constrained scale from a data file in JSON or Rdump format, use the keyword-value argument `init=<filepath>`:

```
./my_model sample init=my_param_inits.json data file=my_model.data.json \
  output file=output_${i}.csv
```

### Specifying the metric and stepsize

An initial guess for the metric can be specified with the `metric_file` argument whose value is the filepath to a JSON or Rdump file which contains a single variable `inv_metric`. The `metric_file` option can be used with and without adaptation enabled.

By default, the metric is estimated during warmup adaptation. If the initial guess is good, then adaptation should not change it much. If the metric is no good, then the adaptation will override the initial guess. For example, the JSON file `bernoulli.diag_e.json`, contents

```
{ "inv_metric" : [0.296291] }
```

can be used as the initial metric as follows:

```
../my_model sample algorithm=hmc metric_file=bernoulli.diag_e.json \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

If adaptation is disabled, both the `metric_file` and `stepsize` arguments should be specified.

```
../my_model sample adapt engaged=0 \
  algorithm=hmc stepsize=0.9 \
  metric_file=bernoulli.diag_e.json \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

The resulting output csv file will contain the following set of comment lines:

```
# Adaptation terminated
# Step size = 0.9
# Diagonal elements of inverse mass matrix:
# 0.296291
```

### Changing the NUTS-HMC adaptation parameters

The Stan User's Guide section on model conditioning and curvature provides a discussion of adaptation and stepsize issues. The Stan Reference Manual section on HMC algorithm parameters explains the NUTS-HMC adaptation schedule and the tuning parameters for setting the step size. The keyword-value arguments for these settings are grouped together under the `adapt` keyword which itself is a sub-argument of the `sample` keyword.

Models with difficult posterior geometries may require increasing the `delta` argument closer to 1.

```
../my_model sample adapt delta=0.95 \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

To skip adaptation altogether, use the keyword-value argument `engaged=0`. Disabling adaptation disables both metric and stepsize adaptation, so a stepsize should be provided along with a metric to enable efficient sampling.

```
../my_model sample adapt engaged=0 \
  algorithm=hmc stepsize=0.9 \
  metric_file=bernoulli.diag_e.json \
  data file=my_model.data.json \
```

```
output file=output_${i}.csv
```

Even with adaptation disabled, it is still advisable to run warmup iterations in order to allow the initial parameter values to be adjusted to estimates which fall within the typical set.

To skip warmup altogether requires specifying both `num_warmup=0` and `adapt_engaged=0`.

```
./my_model sample num_warmup=0 adapt engaged=0 \
  algorithm=hmc stepsize=0.9 \
  metric_file=bernoulli.diag_e.json \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

### Increasing the tree-depth

Models with difficult posterior geometries may require increasing the `max_depth` argument from its default value 10. This requires specifying a series of keyword-argument pairs:

```
./my_model sample adapt delta=0.95 \
  algorithm=hmc engine=nuts max_depth=15 \
  data file=my_model.data.json \
  output file=output_${i}.csv
```

### Capturing Hamiltonian diagnostics and gradients

The output keyword sub-argument `diagnostic_file=<filepath>` writes the sampler parameters and gradients of all model parameters for each draw to a csv file:

```
./my_model sample data file=my_model.data.json \
  output file=output_${i}.csv \
  diagnostic_file=diagnostics_${i}.csv
```

### Suppressing progress updates to the console

The output keyword sub-argument `refresh=<int>` specifies the number of iterations between progress messages written to the terminal window. The default value is 100 iterations. The progress updates look like:

```
Iteration:   1 / 2000 [  0%] (Warmup)
Iteration: 100 / 2000 [  5%] (Warmup)
Iteration: 200 / 2000 [ 10%] (Warmup)
Iteration: 300 / 2000 [ 15%] (Warmup)
```

For simple models which fit quickly, such updates can be annoying; to suppress them altogether, set `refresh=0`. This only turns off the `Iteration:` messages; the

configuration and timing information are still written to the terminal.

```
./my_model sample data file=my_model.data.json \
    output file=output_${i}.csv \
    refresh=0
```

For complicated models which take a long time to fit, setting the refresh rate to a low number, e.g. 10 or even 1, provides a way to more closely monitor the sampler.

### Everything Example

The CmdStan argument parser requires keeping sampler config sub-arguments together; interleaving sampler config with the inputs, outputs, inits, RNG seed and chain id config results in an error message such as the following:

```
./bernoulli sample data file=bernoulli.data.json adapt delta=0.95
adapt is either mistyped or misplaced.
```

Perhaps you meant one of the following valid configurations?

```
method=sample sample adapt
method=variational variational adapt
```

Failed to parse arguments, terminating Stan

The following example provides a template for a call to the sampler which specifies input data, initial parameters, initial step-size and metric, adaptation, output, and RNG initialization.

```
./my_model sample num_warmup=2000 \
    init=my_param_inits.json \
    adapt delta=0.95 init_buffer=100 \
    window=50 term_buffer=100 \
    algorithm=hmc engine=nuts max_depth=15 \
    metric=dense_e metric_file=my_metric.json \
    stepsize=0.6555 \
    data file=my_model.data.json \
    output file=output_${i}.csv refresh=10 \
    random seed=12345 id=${i}
```

The keywords `sample`, `data`, `output`, and `random` are the top-level argument groups. Within the `sample` config arguments, the keyword `adapt` groups the adaptation algorithm parameters and the keyword-value `algorithm=hmc` groups the NUTS-HMC parameters.

The top-level groups can be freely ordered with respect to one another. The following is also a valid command:

```
./my_model random seed=12345 id=${i} \  
  data file=my_model.data.json \  
  output file=output_${i}.csv refresh=10 \  
  sample num_warmup=2000 \  
  init=my_param_inits.json \  
  algorithm=hmc engine=nuts max_depth=15 \  
  metric=dense_e metric_file=my_metric.json \  
  stepsize=0.6555 \  
  adapt delta=0.95 init_buffer=100 \  
  window=50 term_buffer=100
```

## 10. Maximum Likelihood Estimation

The `optimize` method finds the mode of the posterior distribution, assuming that there is one. If the posterior is not convex, there is no guarantee Stan will be able to find the global mode as opposed to a local optimum of log probability. For optimization, the mode is calculated without the Jacobian adjustment for constrained variables, which shifts the mode due to the change of variables. Thus modes correspond to modes of the model as written.

The full set of configuration options available for the `optimize` method is reported at the beginning of the sampler output file as csv comments. When the example model `bernoulli.stan` is run with `method=optimize` via the command line with all default arguments, the resulting Stan csv file header comments show the complete set of default configuration options:

```
# model = bernoulli_model
# method = optimize
#   optimize
#     algorithm = lbfgs (Default)
#       lbfgs
#         init_alpha = 0.001 (Default)
#         tol_obj = 9.999999999999998e-13 (Default)
#         tol_rel_obj = 10000 (Default)
#         tol_grad = 1e-08 (Default)
#         tol_rel_grad = 10000000 (Default)
#         tol_param = 1e-08 (Default)
#         history_size = 5 (Default)
#     iter = 2000 (Default)
#     save_iterations = 0 (Default)
```

### 10.1. Optimization Algorithms

The `algorithm` argument specifies the optimization algorithm. This argument takes one of the following three values:

- `lbfgs` A quasi-Newton optimizer. This is the default optimizer and also much faster than the other optimizers.
- `bfgs` A quasi-Newton optimizer.



- **newton** A Newton optimizer. This is the least efficient optimization algorithm, but has the advantage of setting its own stepsize.

See the Stan Reference Manual's Optimization chapter for a description of these algorithms.

## 10.2. The quasi-Newton optimizers

For both BFGS and L-BFGS optimizers, convergence monitoring is controlled by a number of tolerance values, any one of which being satisfied causes the algorithm to terminate with a solution. See the BFGS and L-BFGS configuration chapter for details on the convergence tests.

Both BFGS and L-BFGS have the following configuration arguments:

- **init\_alpha** - The initial step size parameter. Must be a positive real number. Default value is 0.001
- **tol\_obj** - Convergence tolerance on changes in objective function value. Must be a positive real number. Default value is  $1^{-12}$ .
- **tol\_rel\_obj** - Convergence tolerance on relative changes in objective function value. Must be a positive real number. Default value is  $1^4$ .
- **tol\_grad** - Convergence tolerance on the norm of the gradient. Must be a positive real number. Default value is  $1^{-8}$ .
- **tol\_rel\_grad** - Convergence tolerance on the relative norm of the gradient. Must be a positive real number. Default value is  $1^7$ .
- **tol\_param** - Convergence tolerance on changes in parameter value. Must be a positive real number. Default value is  $1^{-8}$ .

The **init\_alpha** argument specifies the first step size to try on the initial iteration. If the first iteration takes a long time (and requires a lot of function evaluations), set **init\_alpha** to be the roughly equal to the alpha used in that first iteration. The default value is very small, which is reasonable for many problems but might be too large or too small depending on the objective function and initialization. Being too big or too small just means that the first iteration will take longer (i.e., require more gradient evaluations) before the line search finds a good step length.

In addition to the above, the L-BFGS algorithm has argument **history** which controls the size of the history it uses to approximate the Hessian. The value should be less than the dimensionality of the parameter space and, in general, relatively small values (5-10) are sufficient; the default value is 5.

If L-BFGS performs poorly but BFGS performs well, consider increasing the history size. Increasing history size will increase the memory usage, although this is unlikely to be an issue for typical Stan models.

### **10.3. The Newton optimizer**

There are no configuration parameters for the Newton optimizer. It is not recommended because of the slow Hessian calculation involving finite differences.

## 11. Variational Inference Algorithm: ADVI

CmdStan can approximate the posterior distribution using variational inference. The approximation is a Gaussian in the unconstrained variable space.

Stan implements an automatic variational inference algorithm, called Automatic Differentiation Variational Inference (ADVI) Kucukelbir et al. (2015). ADVI uses Monte Carlo integration to approximate the variational objective function, the ELBO (evidence lower bound). ADVI optimizes the ELBO in the real-coordinate space using stochastic gradient ascent. The measures of convergence are similar to the relative tolerance scheme of Stan's optimization algorithms.

The algorithm progression consists of an adaptation phase followed by a sampling phase. The adaptation phase finds a good value for the step size scaling parameter `eta`. The evidence lower bound (ELBO) is the variational objective function and is evaluated based on a Monte Carlo estimate. The variational inference algorithm in Stan is stochastic, which makes it challenging to assess convergence. The algorithm runs until the mean change in ELBO drops below the specified tolerance.

The full set of configuration options available for the `variational` method is reported at the beginning of the sampler output file as csv comments. When the example model `bernoulli.stan` is run with `method=variational` via the command line with all default arguments, the resulting Stan csv file header comments show the complete set of default configuration options:

```
# method = variational
#   variational
#     algorithm = meanfield (Default)
#       meanfield
#         iter = 10000 (Default)
#         grad_samples = 1 (Default)
#         elbo_samples = 100 (Default)
#         eta = 1 (Default)
#       adapt
#         engaged = 1 (Default)
#         iter = 50 (Default)
#         tol_rel_obj = 0.01 (Default)
#         eval_elbo = 100 (Default)
#         output_samples = 1000 (Default)
```

The console output includes a notice that this algorithm is considered to be experimental:

#### EXPERIMENTAL ALGORITHM:

This procedure has not been thoroughly tested and may be unstable or buggy. The interface is subject to change.

### 11.1. Variational Algorithms

Stan implements two variational algorithms. The `algorithm` argument specifies the variational algorithm.

- `algorithm=meanfield` - Use a fully factorized Gaussian for the approximation. This is the default algorithm.
- `algorithm=fullrank` Use a Gaussian with a full-rank covariance matrix for the approximation.

### 11.2. Configuration

- `iter=<int>` Maximum number of iterations. Must be  $< 0$ . Default is 10000.
- `grad_samples=<int>` Number of samples for Monte Carlo estimate of gradients. Must be  $< 0$ . Default is 1.
- `elbo_samples=<int>` Number of samples for Monte Carlo estimate of ELBO (objective function). Must be  $< 0$ . Default is 100.
- `eta=<double>` Stepsize weighting parameter for adaptive stepsize sequence. Must be  $< 0$ . Default is 1.0.
- `adapt` Warmup Adaptation keyword, takes sub-arguments:
  - `engaged=<boolean>` Adaptation engaged? Valid values: (0,1). Default is 1.
  - `iter=<int>` Maximum number of adaptation iterations. Must be  $< 0$ . Default is 50.
- `tol_rel_obj=<double>` Convergence tolerance on the relative norm of the objective. Must be  $< 0$ . Default is 0.01.
- `eval_elbo=<int>` Evaluate ELBO every Nth iteration. Must be  $< 0$ . Default is 100.
- `output_samples=<int>` Number of posterior samples to draw and save. Must be  $< 0$ . Default is 1000.

### 11.3. CSV Output

The output file consists of the following pieces of information:

- The full set of configuration options available for the `variational` method is reported at the beginning of the sampler output file as CSV comments.
- The first three output columns are labelled `lp__`, `log_p__`, `log_g__`, the rest are the model parameters.
- The stepsize adaptation information is output as csv comments following column header row.
- The following line contains the mean of the variational approximation.
- The rest of the output contains `output_samples` number of samples drawn from the variational approximation.

To illustrate, we call Stan's variational inference on the example model and data:

```
> ./bernoulli variational data file=bernoulli.data.R
```

By default, the output file is `output.csv`. Lines 1 - 28 contain configuration information:

```
# stan_version_major = 2
# stan_version_minor = 23
# stan_version_patch = 0
# model = bernoulli_model
# method = variational
#   variational
#     algorithm = meanfield (Default)
#       meanfield
#     iter = 10000 (Default)
#     grad_samples = 1 (Default)
#     elbo_samples = 100 (Default)
#     eta = 1 (Default)
#     adapt
#       engaged = 1 (Default)
#       iter = 50 (Default)
#     tol_rel_obj = 0.01 (Default)
#     eval_elbo = 100 (Default)
#     output_samples = 1000 (Default)
...

```

The column header row is:

```
lp__,log_p__,log_g__,theta
```

The stepsize adaptation information is:

```
# Stepsize adaptation complete.  
# eta = 1
```

The reported mean variational approximations information is:

```
0,0,0,0.214911
```

That is, the estimate for `theta` given the data is 0.2.

The following is a sample based on this approximation:

```
0,-14.0252,-5.21718,0.770397  
0,-7.05063,-0.10025,0.162061  
0,-6.75031,-0.0191099,0.241606  
...
```

## 12. Standalone Generate Quantities

The `generate_quantities` method allows you to generate additional quantities of interest from a fitted model without re-running the sampler.

This method requires sub-argument `fitted_params` which takes as its value an existing Stan csv file that contains a sample from an equivalent model, i.e., a model with the same parameters, transformed parameters, and model blocks, conditioned on the same data.

## 13. Diagnosing HMC by Comparison of Gradients

CmdStan has a basic diagnostic feature that will calculate gradients of the initial state and compare them with those calculated with finite differences. If there are discrepancies, there is a problem with the model or initial states (or a bug in Stan). To run on the different platforms, use one of the following.

Mac OS and Linux

```
> ./my_model diagnose data file=my_data
```

Windows

```
> my_model diagnose data file=my_data
```



# CmdStan Tools

This section provides a reference for the CmdStan tools:

- `stanc`
- `stansummary`
- `diagnose`
- `print` (deprecated)

## 14. **stanc**: Translating Stan to C++

CmdStan translates Stan programs to C++ using the Stan compiler program which is included in the CmdStan release `bin` directory as program `stanc`.

As of release 2.22, the CmdStan Stan to C++ compiler is written in OCaml. This compiler is called “`stanc3`” and has its own repository <https://github.com/stan-dev/stanc3>, from which pre-built binaries for Linux, Mac, and Windows can be downloaded.

Prior to release 2.22, the Stan compiler program was compiled from C++ source code that was part of the core Stan library. This C++ compiler is still available as program `bin/stanc2`. This compiler is no longer being maintained, i.e., existing bugs will not be fixed and new functions and features are only available in the `stanc3` compiler. Its intended use is as a diagnostic tool and backup for the new `stanc3` compiler. For some future version, it will be dropped from the release altogether.

### 14.1. Instantiating the **stanc** Binary

Before the Stan compiler can be used, the binary `stanc` must be created. This can be done using the makefile as follows. For Mac and Linux:

```
make bin/stanc
```

For Windows:

```
make bin/stanc.exe
```

To build the `bin/stanc2` program, specify:

```
make bin/stanc2
```

### 14.2. The Stan Compiler Program

The Stan compiler program `stanc` converts Stan programs to C++ concepts. If the compiler encounters syntax errors in the program, it will provide an error message indicating the location in the input where the failure occurred and reason for the failure. The following example illustrates a fully qualified call to `stanc` to generate the C++ translation of the example model `bernoulli.stan`. For Linux and Mac:

```
> cd <cmdstan-home>
> bin/stanc --o=bernoulli.hpp examples/bernoulli/bernoulli.stan
```

For Windows:

```
> cd <cmdstan-home>
> bin/stanc.exe --o=bernoulli.hpp examples/bernoulli/bernoulli.stan
```

The base name of the Stan program file determines the name of the C++ model class. Because this name is the name of a C++ class, it must start with an alphabetic character (a--z or A--Z) and contain only alphanumeric characters (a--z, A--Z, and 0--9) and underscores (\_) and should not conflict with any C++ reserved keyword.

The C++ code implementing the class is written to the file `bernoulli.hpp` in the current directory. The final argument, `bernoulli.stan`, is the file from which to read the Stan program.

In practice, `stanc` is invoked indirectly, via the GNU Make utility, which contains rules that compile a Stan program to its corresponding executable. To build the simple Bernoulli model via `make`, we specify the name of the target executable file. On Mac and Linux, this is the name of the Stan program with the `.stan` omitted. On Windows, replace `.stan` with `.exe`, and make sure that the path is given with slashes and not backslashes. For Linux and Mac:

```
> make examples/bernoulli/bernoulli
```

For Windows:

```
> make examples/bernoulli/bernoulli.exe
```

The makefile rules first invoke the `stanc` compiler to translate the Stan model to C++ , then compiles and links the C++ code to a binary executable. The makefile variable `STANCFLAGS` can be used to to override the default arguments to `stanc`, e.g.,

```
> make STANCFLAGS="--include-paths=~/.foo" examples/bernoulli/bernoulli
```

To use the `stanc2` compiler instead of the `stanc3` compiler, set the make option `STANC2`:

```
> make STANC2=TRUE examples/bernoulli/bernoulli
```

### 14.3. Command-Line Options for `stanc3`

The `stanc3` compiler has the following command-line syntax:

```
> stanc (options) <model_file>
```

where `<model_file>` is a path to a Stan model file ending in suffix `.stan`.

The `stanc3` options are:

- `--help` - Displays the complete list of `stanc3` options, then exits.
- `--version` - Display `stanc` version number

- `--name=<model_name>` - Specify the name of the class used for the implementation of the Stan model in the generated C++ code.
- `--o=<file_name>` - Specify the name of the file into which the generated C++ is written.
- `--allow-undefined` - Do not throw a parser error if there is a function in the Stan program that is declared but not defined in the functions block.
- `--include_paths=<dir1,...dirN>` - Takes a comma-separated list of directories that may contain a file in an `#include` directive.
- `--use-openssl` - If set, will use additional Stan OpenCL features enabled in the Stan-to-C++ compiler.
- `--auto-format` - Pretty prints the program to the console.
- `--print-canonical` - Prints the canonicalized program to the console.
- `--print-cpp` - If set, output the generated C++ Stan model class to stdout.
- `--O` - Allow the compiler to apply all optimizations to the Stan code. **WARNING:** *This is currently an experimental feature!*
- `--warn-uninitialized` - Emit warnings about uninitialized variables to stderr. Currently an experimental feature.

The compiler also provides a number of debug options which are primarily of interest to stanc3 developers; use the `--help` option to see the full set.

#### 14.4. Command-Line Options for stanc2

The stanc2 compiler has the same command-line syntax as the stanc3 compiler, but has fewer options:

- `--help` - Displays the complete list of stanc3 options, then exits.
- `--version` - Display stanc version number
- `--name=<model_name>` - Specify the name of the class used for the implementation of the Stan model in the generated C++ code.
- `--o=<file_name>` - Specify the name of the file into which the generated C++ is written.
- `--allow_undefined` - Do not throw a parser error if there is a function in the Stan program that is declared but not defined in the functions block.

- `--include_paths=<dir1,...dirN>` - Takes a comma-separated list of directories that may contain a file in an `#include` directive.

## 14.5. Using External C++ Code

The `--allow_undefined` flag can be passed to the call to `stanc`, which will allow undefined functions in the Stan language to be parsed without an error. We can then include a definition of the function in a C++ header file. This requires specifying two makefile variables: `- STANCFLAGS=--allow_undefined - USER_HEADER=<header_file.hpp>`, where `<header_file.hpp>` is the name of a header file that defines a function with the same name and signature in a namespace that is formed by concatenating the `class_name` argument to `stanc` documented above to the string `_namespace`

As an example, consider the following variant of the Bernoulli example

```
functions {
  real make_odds(real theta);
}
data {
  int<lower=0> N;
  int<lower=0,upper=1> y[N];
}
parameters {
  real<lower=0,upper=1> theta;
}
model {
  theta ~ beta(1,1); // uniform prior on interval 0,1
  y ~ bernoulli(theta);
}
generated quantities {
  real odds;
  odds = make_odds(theta);
}
```

Here the `make_odds` function is declared but not defined, which would ordinarily result in a parser error. However, if you put `STANCFLAGS = --allow_undefined` into the `make/local` file or into the `stanc` call, then the `stanc` compiler will translate this program to C++, but the generated C++ code will not compile unless you write a file such as `examples/bernoulli/make_odds.hpp` with the following lines

```
namespace bernoulli_model_namespace {
  template <typename T0__> inline typename
```

```

        boost::math::tools::promote_args<T0__>::type  make_odds(const T0__
theta, std::ostream* pstream__) {
    return theta / (1 - theta); }
}

```

Given the above, the following make invocation should work

```
> make STANCFLAGS=--allow_undefined USER_HEADER=examples/bernoulli/make_odds
```

Alternatively, you could put STANCFLAGS and USER\_HEADER into the make/local file instead of specifying them on the command-line.

If the function were more complicated and involved functions in the Stan Math Library, then you would need to prefix the function calls with `stan::math::`. The `pstream__` argument is mandatory in the signature but need not be used if your function does not print any output. To see the necessary boilerplate look at the corresponding lines in the generated C++ file.

For more details about how to write C++ code using the Stan Math Library, see <https://arxiv.org/abs/1509.07164>.

## 15. **stansummary: MCMC Output Analysis**

CmdStan's `stansummary` utility processes one or more output files from a run or set of runs of Stan's HMC sampler. For all parameters and quantities of interest in the Stan program, `stansummary` reports a set of statistics including mean, standard deviation, percentiles, effective number of samples, and  $\hat{R}$  values.

### 15.1. **Building the stansummary Command**

The CmdStan makefile task `build` compiles the `stansummary` utility into the `bin` directory. It can be compiled directly using the makefile as follows:

```
> cd <cmdstan-home>
> make bin/stansummary
```

### 15.2. **Running the stansummary Command**

The `stansummary` utility processes one or more output files from a run or set of runs of Stan's HMC sampler given a model and data. For all columns in the Stan csv output file `stansummary` reports a set of statistics including mean, standard deviation, percentiles, effective number of samples, and  $\hat{R}$  values.

To run `stansummary` on the output file or files generated by a run of the sampler, on Mac or Linux:

```
<cmdstan-home>/bin/stansummary <file_1.csv> ... <file_N.csv>
```

On Windows, use backslashes to call the `stansummary.exe`.

```
<cmdstan-home>\bin\stansummary.exe <file_1.csv> ... <file_N.csv>
```

The values for each quantity are the posterior means, standard deviations, and quantiles, along with Monte-Carlo standard error, effective sample size estimates (per second), and convergence diagnostic statistic.

For Windows, the forward slash in paths need to be converted to backslashes.

### 15.3. **Command-line Options**

The `stansummary` command syntax provides a set of flags to customize the output which must precede the list of filenames:

- `--sig_figs` - The number of significant figures displayed in the output. Must be an integer value  $> 0$ . The default value is 2.

- `--csv_file` - Writes output to the specified filename in csv format using # for comment lines. Appends output to the file if it exists.
- `--percentiles` - An string containing an ordered list of integers in the range (0,100) specifying the percentiles to use in the set of output columns. Defaults to "5, 50, 95".
- `--autocorr` - 0-based index into the list of filenames used to display the autocorrelation between all draws in that chain. For example, for a set of 4 csv files `--autocorr 0` will output the autocorrelation for chain 1 and `--autocorr 3` will examine the autocorrelation for chain 4. No autocorrelation output by default.



## 16. **diagnose: Diagnosing Biased Hamiltonian Monte Carlo Inferences**

CmdStan is distributed with a utility that is able to read in and analyze the output of one or more Markov chains to check for the following potential problems:

- Divergent transitions
- Transitions that hit the maximum treedepth
- Low E-BFMI values
- Low effective sample sizes
- High  $\hat{R}$  values

The meanings of several of these problems are discussed in <https://arxiv.org/abs/1701.02434>.

### 16.1. **Building the diagnose Command**

The CmdStan makefile task `build` compiles the `diagnose` utility into the `bin` directory. It can be compiled directly using the makefile as follows:

```
> cd <cmdstan-home>
> make bin/diagnose
```

### 16.2. **Running the diagnose Command**

The `diagnose` command is executed on one or more output files, which are provided as command-line arguments separated by spaces. If there are no apparent problems with the output files passed to `diagnose`, it outputs a message that all transitions are within treedepth limit and that no divergent transitions were found. If problems are detected, it outputs a summary of the problem along with possible ways to mitigate it.

To fully exercise the `diagnose` command, we run 4 chains to sample from the Neal's funnel distribution, discussed in the Stan User's Guide reparameterization section <https://mc-stan.org/docs/stan-users-guide/reparameterization-section.html>. This program defines a distribution which exemplifies the difficulties of sampling from some hierarchical models:

```
parameters {
  real y;
  vector[9] x;
}
```

```
model {
  y ~ normal(0, 3);
  x ~ normal(0, exp(y/2));
}
```

This program is available on GitHub: <https://github.com/stan-dev/example-models/blob/master/misc/funnel/funnel.stan>

Stan has trouble sampling from the region where  $y$  is small and thus  $x$  is constrained to be near 0. This is due to the fact that the density's scale changes with  $y$ , so that a step size that works well when  $y$  is large is inefficient when  $y$  is small and vice-versa.

Running 4 chains produces output files `output_1.csv`, ..., `output_4.csv`. We run `diagnose` command on this fileset:

```
> bin/diagnose output_*.csv
```

The output is printed to the terminal window:

```
Processing csv files: output_1.csv, output_2.csv, output_3.csv, output_4.csv
```

```
Checking sampler transitions treedepth.
```

```
9 of 4000 (0.23%) transitions hit the maximum treedepth limit of 10, or 2^10
```

```
Trajectories that are prematurely terminated due to this limit will result in
```

```
For optimal performance, increase this limit.
```

```
Checking sampler transitions for divergences.
```

```
9 of 4000 (0.23%) transitions ended with a divergence.
```

```
These divergent transitions indicate that HMC is not fully able to explore t
```

```
Try increasing adapt delta closer to 1.
```

```
If this doesn't remove all divergences, try to reparameterize the model.
```

```
Checking E-BFMI - sampler transitions HMC potential energy.
```

```
The E-BFMI, 0.078, is below the nominal threshold of 0.3 which suggests that
```

```
If possible, try to reparameterize the model.
```

```
Effective sample size satisfactory.
```

```
The following parameters had split R-hat greater than 1.1:
```

```
y
```

```
Such high values indicate incomplete mixing and biased estimation.
```

```
You should consider regularizing your model with additional prior informatio
```

Processing complete.

In this example, changing the model to use a non-centered parameterization is the only way to correct these problems. In this second model, the parameters `x_raw` and `y_raw` are sampled as independent standard normals, which is easy for Stan.

```
parameters {
  real y_raw;
  vector[9] x_raw;
}
transformed parameters {
  real y;
  vector[9] x;

  y = 3.0 * y_raw;
  x = exp(y/2) * x_raw;
}
model {
  y_raw ~ std_normal(); // implies y ~ normal(0, 3)
  x_raw ~ std_normal(); // implies x ~ normal(0, exp(y/2))
}
```

This program is available on GitHub: [https://github.com/stan-dev/example-models/blob/master/misc/funnel/funnel\\_reparam.stan](https://github.com/stan-dev/example-models/blob/master/misc/funnel/funnel_reparam.stan)

We compile the program and run 4 chains, as before. Now the `diagnose` command doesn't detect any problems:

Processing csv files: output\_1.csv, output\_2.csv, output\_3.csv, output\_4.csv

Checking sampler transitions treedepth.

Treedepth satisfactory for all transitions.

Checking sampler transitions for divergences.

No divergent transitions found.

Checking E-BFMI - sampler transitions HMC potential energy.

E-BFMI satisfactory for all transitions.

Effective sample size satisfactory.

Split R-hat values satisfactory all parameters.

Processing complete, no problems detected.

### 16.3. diagnose Warnings and Recommendations

#### Divergent transitions after warmup

Stan uses Hamiltonian Monte Carlo (HMC) to explore the target distribution — the posterior defined by a Stan program + data — by simulating the evolution of a Hamiltonian system. In order to approximate the exact solution of the Hamiltonian dynamics we need to choose a step size governing how far we move each time we evolve the system forward. That is, the *step size controls the resolution of the sampler*.

Unfortunately, for particularly hard problems there are features of the target distribution that are too small for this resolution. Consequently the sampler misses those features and returns biased estimates. Fortunately, this mismatch of scales manifests as *divergences* which provide a practical diagnostic. If there are any divergences after warmup, then the samples may be biased.

If the divergent transitions cannot be eliminated by increasing the `adapt_delta` parameter, we have to find a different way to write the model that is logically equivalent but simplifies the geometry of the posterior distribution. This problem occurs frequently with hierarchical models and one of the simplest examples is Neal's Funnel, which is discussed in the reparameterization section of the Stan User's Guide.

#### Maximum treedepth exceeded

Warnings about hitting the maximum treedepth are not as serious as warnings about divergent transitions. While divergent transitions are a *validity* concern, hitting the maximum treedepth is an *efficiency* concern. Configuring the No-U-Turn-Sampler (the variant of HMC used by Stan) requires putting a cap on the depth of the trees that it evaluates during each iteration (for details on this see the *Hamiltonian Monte Carlo Sampling* chapter in the Stan Reference Manual. When the maximum allowed tree depth is reached it indicates that NUTS is terminating prematurely to avoid excessively long execution time.

This is controlled through the `max_depth` argument. If the number of transitions which exceed maximum treedepth is low, increasing `max_depth` may correct this problem.

#### Low E-BFMI values - sampler transitions HMC potential energy.

The sampler csv output column `energy__` is used to diagnose the accuracy of any Hamiltonian Monte Carlo sampler. If the standard deviation of `energy` is much larger than  $\sqrt{D/2}$ , where  $D$  is the number of *unconstrained* parameters, then the sampler is unlikely to be able to explore the posterior adequately. This is usually due to

heavy-tailed posteriors and can sometime be remedied by reparameterizing the model.

The warning that some number of chains had an estimated Bayesian Fraction of Missing Information (BFMI) that was too low implies that the adaptation phase of the Markov Chains did not turn out well and those chains likely did not explore the posterior distribution efficiently. For more details on this diagnostic, see <https://arxiv.org/abs/1604.00695>. Should this occur, you can either run the sampler for more iterations, or consider reparameterizing your model.

### Low effective sample sizes

Roughly speaking, the effective sample size (ESS) of a quantity of interest captures how many independent draws contain the same amount of information as the dependent sample obtained by the MCMC algorithm. Clearly, the higher the ESS the better. Stan uses  $\hat{R}$  adjustment to use the between-chain information in computing the ESS. For example, in case of multimodal distributions with well-separated modes, this leads to an ESS estimate that is close to the number of distinct modes that are found.

Bulk-ESS refers to the effective sample size based on the rank normalized draws. This does not directly compute the ESS relevant for computing the mean of the parameter, but instead computes a quantity that is well defined even if the chains do not have finite mean or variance. Overall bulk-ESS estimates the sampling efficiency for the location of the distribution (e.g. mean and median).

Often quite smaller ESS would be sufficient for the desired estimation accuracy, but the estimation of ESS and convergence diagnostics themselves require higher ESS. We recommend requiring that the bulk-ESS is greater than 100 times the number of chains. For example, when running four chains, this corresponds to having a rank-normalized effective sample size of at least 400.

### High $\hat{R}$

$\hat{R}$  (R-hat) convergence diagnostic compares the between- and within-chain estimates for model parameters and other univariate quantities of interest. If chains have not mixed well (ie, the between- and within-chain estimates don't agree),  $\hat{R}$  is larger than 1. We recommend running at least four chains by default and only using the sample if  $\hat{R}$  is less than 1.01. Stan reports  $\hat{R}$  which is the maximum of rank normalized split-R-hat and rank normalized folded-split-R-hat, which works for thick tailed distributions and is sensitive also to differences in scale. For more details on this diagnostic, see <https://arxiv.org/abs/1903.08008>.

There is further discussion in <https://arxiv.org/abs/1701.02434>; however the correct resolution is necessarily model specific, hence all suggestions general guidelines only.

## 17. **print (deprecated): MCMC Output Analysis**

The `print` utility is deprecated, but is still available until CmdStan v3.0. Use the `stansummary` utility instead.

# Appendices

This section contains the following appendices:

- Stan CSV File Format
- JSON format
- RDump data format

## 18. Stan CSV File Format

The output from all CmdStan methods is in CSV format. Fundamentally, it is a data table consisting of zero or more method-specific columns followed by columns corresponding to the model parameters and/or quantities of interest.

Different methods also make (extensive) use of comment lines, i.e., lines which begin with the # character as a way of outputting additional information about the inference engine and the resulting estimate.

- Header row: column names
  - method specific variables
  - Stan program variables in block declaration order
- Data rows: numerical values (including NaN, inf, +inf, -inf)

### 18.1. MCMC Sampler CSV Output

#### **Sampler output**

- Config as comments
- Header row
- Warmup draws, if `save_warmup=1`
- Adaptation as comments, unless `algorithm=fixed_param`
- Sampling draws
- Timing information as comments

#### **Diagnostic file - latent Hamiltonian plus gradients**

- Header row
- Warmup draws, if `save_warmup=1`
- Sampling draws

### 18.2. Optimization Output

- Config as comments
- Header row
- Penalized maximum likelihood estimate

### 18.3. Variational Inference Output

- Config as comments
- Header row
- Adaptation as comments
- Variational estimate



- Sample draws from estimate of the posterior

#### **18.4. Generate Quantities Outputs**

- Header row
- Quantities of interest

#### **18.5. Diagnose Method Outputs**

- Header row
- Gradients

## 19. JSON Format for CmdStan

CmdStan can use JSON format for input data for both model data and parameters. Model data is read in by the model constructor. Model parameters are used to initialize the sampler and optimizer.

### 19.1. JSON Syntax Summary

JSON is a data interchange notation, defined by an ECMA standard. JSON data files must in Unicode. JSON data is a series of structural tokens, literal tokens, and values:

- Structural tokens are the left and right curly bracket `{}`, left and right square bracket `[]`, the semicolon `;`, and the comma `,`.
- Literal tokens must always be in lowercase. There are three literal tokens: `true`, `false`, `null`.
- A primitive value is a single token which is either a literal, a string, or a number.
- A string consists of zero or more Unicode characters enclosed in double quotes, e.g. `"foo"`. A backslash is used to escape the double quote character as well as the backslash itself. JSON allows the use of Unicode character escapes, e.g. `"\\uHHHH"` where HHHH is the Unicode code point in hex.
- All numbers are decimal numbers. Scientific notation is allowed. The following are examples of numbers: `17`, `17.2`, `-17.2`, `-17.2e8`, `17.2e-8`. *Note:* The concepts of positive and negative infinity as well as “not a number” cannot be expressed as numbers in JSON, but they can be encoded as strings `"+inf"`, `"-inf"`, and `"NaN"`, respectively, which can be mixed with numbers.
- A JSON array is an ordered, comma-separated list of zero or more JSON values enclosed in square brackets. The elements of an array can be of any type. The following are examples of arrays: `[]`, `[1]`, `[0.2, "-inf", true]`.
- A name-value pair consists of a string followed by a colon followed by a value, either primitive or compound.
- A JSON object is a comma-separated series of zero or more name-value pairs enclosed in curly brackets. Each name-value pair is a member of the object. Membership is unordered. Member names are not required to be unique. The following are examples of objects: `{ }`, `{"foo": null}`, `{"bar" : 17, "baz" : [14,15,16.6] }`.

## 19.2. Stan Data Types in JSON Notation

Stan follows the JSON standard. A Stan input file in JSON notation consists of single JSON object which contains zero or more name-value pairs. This structure corresponds to a Python data dictionary object. The following is an example of JSON data for the simple Bernoulli example model:

```
{ "N" : 10, "y" : [0,1,0,0,0,0,0,0,0,1] }
```

Matrix data and multi-dimensional arrays are indexed in row-major order. For a Stan program which has data block:

```
data {
  int d1;
  int d2;
  int d3;
  int ar[d1, d2, d3];
}
```

the following JSON input would be valid:

```
{ "d1" : 2,
  "d2" : 3,
  "d3" : 4,
  "ar" : [[[0,1,2,3], [4,5,6,7], [8,9,10,11]],
           [[12,13,14,15], [16,17,18,19], [20,21,22,23]]]
}
```

JSON ignores whitespace. In the above examples, the spaces and newlines are only used to improve readability and can be omitted.

All data inputs are encoded as name-value pairs. The following table provides more examples of JSON data. The left column contains a Stan data variable declaration and the right column contains valid JSON data inputs.

Stan variable	JSON data
<code>int i</code>	<code>"i": 17</code>
<code>real a</code>	<code>"a" : 17</code>
	<code>"a" : 17.2</code>
	<code>"a" : "NaN"</code>
	<code>"a" : "+inf"</code>
	<code>"a" : "-inf"</code>
<code>int a[5]</code>	<code>"a" : [1, 2, 3, 4, 5]</code>

Stan variable	JSON data
real a[5]	"a" : [ 1, 2, 3.3, "NaN", 5 ]
vector[5] a	"a" : [ 1, 2, 3.3, "NaN", 5 ]
row_vector[5] a	"a" : [ 1, 2, 3.3, "NaN", 5 ]
real a[5]	"a" : [ 1, 2, 3.3, "NaN", 5 ]
matrix[2,3] a	"a" : [ [ 1, 2, 3 ], [ 4, 5, 6 ] ]

### Empty arrays in JSON

JSON notation is not able to distinguish between multi-dimensional arrays where any dimension is 0, e.g., a 2-D array with dimensions (1,0), i.e., an array which contains a single array which is empty, has JSON representation [ ]. To see how this works, consider the following Stan program data block:

```
data {
  int d;
  int ar_1d[d];
  int ar_2d[d,d];
  int ar_3d[d,d,d];
}
```

In the case where variable `d` is 1, all arrays will contain a single value. If array variable `ar_d1` contains value 7, 2-D array variable `ar_d2` contains (an array which contains) value 8, and 3-D array variable `ar_d3` contains (an array which contains an array which contains) value 9, the JSON representation is:

```
{ "ar_d1" : [7],
  "ar_d2" : [[8]],
  "ar_d3" : [[[9]]]
}
```

However, in the case where variable `d` is 0, `ar_d1` is empty, i.e., it contains no values, as is `ar_d2`, `ar_d3`, and the JSON representation is

```
{ "d" : 0,
  "ar_d1" : [ ],
  "ar_d2" : [ ],
  "ar_d3" : [ ]
}
```

## 20. RDump Format for CmdStan

RDump format can be used to represent values for Stan variables. This format was introduced in SPLUS and is used in R, JAGS, and in BUGS (but with a different ordering).

A dump file is structured as a sequence of variable definitions. Each variable is defined in terms of its dimensionality and its values. There are three kinds of variable declarations: - scalars - sequences - general arrays

### 20.1. Creating Dump Files

Dump files can be created from R using RStan, via the `rstan` package function `stan_rdump`. Stan RDump files must be created via `stan_rdump` and not by R's native `dump` function because R's `dump` function uses a richer syntax than is supported by the underlying Stan i/o libraries.

### 20.2. Scalar Variables

A simple scalar value can be thought of as having an empty list of dimensions. Its declaration in the dump format follows the SPLUS assignment syntax. For example, the following would constitute a valid dump file defining a single scalar variable `y` with value 17.2:

```
y <- 17.2
```

### 20.3. Sequence Variables

One-dimensional arrays may be specified directly using the SPLUS sequence notation. The following example defines an integer-value and a real-valued sequence.

```
n <- c(1,2,3) y <- c(2.0,3.0,9.7)
```

Arrays are provided without a declaration of dimensionality because the reader just counts the number of entries to determine the size of the array.

Sequence variables may alternatively be represented with R's colon-based notation. For instance, the first example above could equivalently be written as

```
n <- 1:3
```

The sequence denoted by `1:3` is of length 3, running from 1 to 3 inclusive. The colon notation allows sequences going from high to low. The following are equivalent:

```
n <- 2:-2  
n <- c(2,1,0,-1,-2)
```

As a special case, a sequence of zeros can also be represented in the dump format by `integer(x)` and `double(x)`, for type `int` and `double`, respectively. Here `x` is a non-negative integer to specify the length. If `x` is 0, it can be omitted. The following are some examples.

```
x1 <- integer()
x2 <- integer(0)
x3 <- integer(2)
y1 <- double()
y2 <- double(0)
y3 <- double(2)
```

## 20.4. Array Variables

For more than one dimension, the dump format uses a dimensionality specification. For example, the following defines a  $2 \times 3$  array:

```
y <- structure(c(1,2,3,4,5,6), .Dim = c(2,3))
```

Data is stored column-major, thus the values for `y` will be:

```
y[1,1] = 1
y[1,2] = 3
y[1,3] = 5
y[2,1] = 2
y[2,2] = 4
y[2,3] = 6
```

The `structure` keyword just wraps a sequence of values and a dimensionality declaration, which is itself just a sequence of non-negative integer values. The product of the dimensions must equal the length of the array.

If the values happen to form a contiguous sequence of integers, they may be written with colon notation. Thus the example above is equivalent to the following.

```
y <- structure(1:6, .Dim = c(2,3))
```

Sequence notation can be used within any call to the generic `c()` function in R. In the above example, `c(2,3)` could be written as `c(2:3)`.

The generalization of column-major indexing is last-index major indexing. Arrays of more than two dimensions are written in a last-index major form. For example,

```
z <- structure(1:24, .Dim = c(2,3,4))
```

produces a three-dimensional `int` (assignable to `real`) array `z` with values:

```

z[1,1,1] = 1
z[2,1,1] = 2
z[1,2,1] = 3
z[2,2,1] = 4
z[1,3,1] = 5
z[2,3,1] = 6
z[1,1,2] = 7
z[2,1,2] = 8
z[1,2,2] = 9
z[2,2,2] = 10
z[1,3,2] = 11
z[2,3,2] = 12
z[1,1,3] = 13
z[2,1,3] = 14
z[1,2,3] = 15
z[2,2,3] = 16
z[1,3,3] = 17
z[2,3,3] = 18
z[1,1,4] = 19
z[2,1,4] = 20
z[1,2,4] = 21
z[2,2,4] = 22
z[1,3,4] = 23
z[2,3,4] = 24

```

If the underlying 3-D array is stored as a 1-D array in last-index major format, the innermost array elements will be contiguous.

The sequence of values inside `structure` can also be `integer(x)` or `double(x)`. In particular, if one or more dimensions is zero, `integer()` can be put inside `structure`. For instance, the following example is supported by the dump format.

```
y <- structure(integer(), .Dim = c(2,0))
```

## 20.5. Matrix- and Vector-Valued Variables

The dump format for matrices and vectors, including arrays of matrices and vectors, is the same as that for arrays of the same shape.

### Vector Dump Format

The following three declarations have the same dump format for their data.

```
real a[K];
```

```
vector[K] b;
row_vector[K] c;
```

### Matrix Dump Format

The following declarations have the same dump format.

```
real a[M,N];
matrix[M,N] b;
```

### Arrays of Vectors and Matrices

The key to understanding arrays is that the array indexing comes before any of the container indexing. That is, an array of vectors is just that: each array element is a vector. See the chapter on array and matrix types in the user's guide section of the language manual for more information.

For the dump data format, the following declarations have the same arrangement.

```
real a[M,N];
matrix[M,N] b;
vector[N] c[M];
row_vector[N] d[M];
```

Similarly, the following also have the same dump format.

```
real a[P,M,N];
matrix[M,N] b[P];
vector[N] c[P,M];
row_vector[N] d[P,M];
```

## 20.6. Integer- and Real-Valued Variables

There is no declaration in a dump file that distinguishes integer versus continuous values. If a value in a dump file's definition of a variable contains a decimal point (e.g., 132.3) or uses scientific notation (e.g., 1.323e2), Stan assumes that the values are real.

For a single value, if there is no decimal point, it may be assigned to an `int` or `real` variable in Stan. An array value may only be assigned to an `int` array if there is no decimal point or scientific notation in any of the values. This convention is compatible with the way R writes data.

The following dump file declares an integer value for `y`.

```
y <- 2
```

This definition can be used for a Stan variable `y` declared as `real` or as `int`. Assigning an integer value to a real variable automatically promotes the integer value to a real



value.

Integer values may optionally be followed by L or l, denoting long integer values. The following example, where the type is explicit, is equivalent to the above.

```
y <- 2L
```

The following dump file provides a real value for y.

```
y <- 2.0
```

Even though this is a round value, the occurrence of the decimal point in the value, 2.0, causes Stan to infer that y is real valued. This dump file may only be used for variables y declared as real in Stan.

### Scientific Notation

Numbers written in scientific notation may only be used for real values in Stan. R will write out the integer one million as  $1e + 06$ .

### Infinite and Not-a-Number Values

Stan's reader supports infinite and not-a-number values for scalar quantities (see the section of the reference manual section of the language manual for more information on Stan's numerical data types). Both infinite and not-a-number values are supported by Stan's dump-format readers.

	Value	Preferred Form	Alternative Forms
positive infinity	Inf		Infinity, infinity
negative infinity	-Inf		-Infinity, -infinity
not a number	NaN		

These strings are not case sensitive, so `inf` may also be used for positive infinity, or `NAN` for not-a-number.

## 20.7. Quoted Variable Names

In order to support JAGS data files, variables may be double quoted. For instance, the following definition is legal in a dump file.

```
"y" <- c(1,2,3) \end{Verbatim}
```

## 20.8. Line Breaks

The line breaks in a dump file are required to be consistent with the way R reads in data. Both of the following declarations are legal.

```
y <- 2
```

```
y <-
3
```

Also following R, breaking before the assignment arrow are not allowed, so the following is invalid.

```
y
<- 2 # Syntax Error
```

Lines may also be broken in the middle of sequences declared using the `c(...)` notation, as well as between the comma following a sequence definition and the dimensionality declaration. For example, the following declaration of a  $2 \times 2 \times 3$  array is valid.

```
y <-
structure(c(1,2,3,
4,5,6,7,8,9,10,11,
12), .Dim = c(2,2,
3))
```

Because there are no decimal points in the values, the resulting dump file may be used for three-dimensional array variables declared as `int` or `real`.

## 20.9. BNF Grammar for Dump Data

A more precise definition of the dump data format is provided by the following (mildly templated) Backus-Naur form grammar.

```
definition ::= name <- value optional_semicolon
```

```
name ::= char*          | ''' char* '''      | ''' char* '''
```

```
value ::= value<int> | value<double>
```

```
value<T> ::= T          | seq<T>              | zero_array<T>          |
'structure' '(' seq<T> ',' ".Dim" '=' seq<int> ')' | 'structure'
 '(' zero_array<T> ',' ".Dim" '=' seq<int> ')'
```

```
seq<int> ::= int ':' int          | cseq<int>
```

```
zero_array<int> ::= "integer" '(' <non-negative int>? ')'
```

```
zero_array<real> ::= "double" '(' <non-negative int>? ')'
```

```
seq<real> ::= cseq<real>
```

```
cseq<T> ::= 'c' '(' vseq<T> ')'
```

```
vseq<T> ::= T | T ',' vseq<T>
```

The template parameters `T` will be set to either `int` or `real`. Because Stan allows promotion of integer values to real values, an integer sequence specification in the dump data format may be assigned to either an integer- or real-based variable in Stan.

# Bibliography

- Betancourt, Michael. 2017. “A Conceptual Introduction to Hamiltonian Monte Carlo.” *arXiv* 1701.02434. <https://arxiv.org/abs/1701.02434>.
- Kucukelbir, Alp, Rajesh Ranganath, Andrew Gelman, and David M. Blei. 2015. “Automatic Variational Inference in Stan.” *arXiv* 1506.03431. <http://arxiv.org/abs/1506.03431>.