

# CGnal

business innovation through algorithms

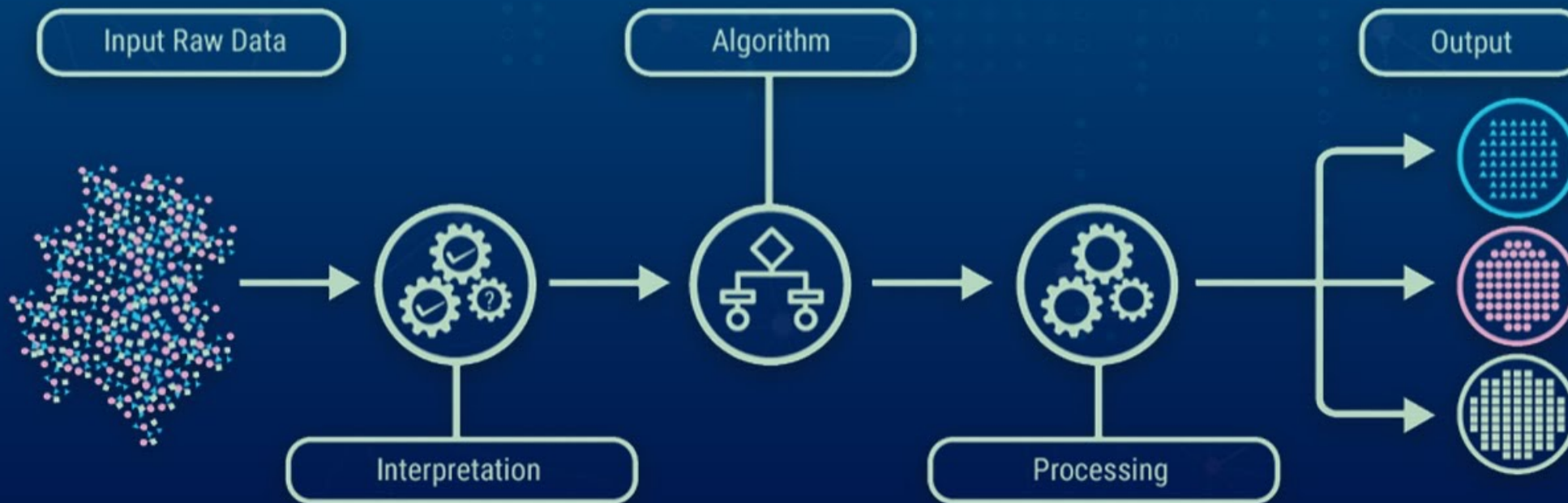
## Explainability & Interpretability

*Glass Box Model vs Black Box Model*

CGnal S.r.l – Corso Venezia 43 - Milano

Novembre 2022 | Milano

# SUPERVISED MACHINE LEARNING



# SUPERVISED MACHINE LEARNING

Input Raw Data



Interpr

**CAN YOU INTERPRET MACHINE LEARNING MODELS**

**JUST USE MORE MACHINE LEARNING**



# Machine Learning is everywhere



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[Google Apps Deciphered: Compute in the Cloud to Streamline Your Desktop](#)

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**New Releases**







# When Model Understanding is needed?

## Model Understanding is not needed when/because:

- Little to no consequences for incorrect predictions
- Problem is well studied and models are extensively validated in real world application
- ...

## Model Understanding is needed when/because:

- **The choice** can have **impacts** on the human lives, health or finances
- Problems are **not well studied** and it not possible to extensively validate in real world application
- **Accuracy (measures) of the model** is no longer enough: for example when the train and test data are not representative of new data encounter
- The model must to be fair (nondiscrimination)
- ...

# When Model Understanding is needed?

## A Typical Machine Learning Example

- I have data, and I want to solve a problem. So, just deploy a model!
- But in real life, things are much more complicated.
- You have various parties: ML Scientists, Product Managers, End Users.



### ***ML Scientist:***

Which model features should I use? Does my model perform well?



### ***Product Managers:***

Can I trust/deploy this model? Is it fair for all parties?



### ***End User:***

Why did it give me this prediction?

*If the users do not trust a model or a prediction, they will not use it*

# black box vs glass box

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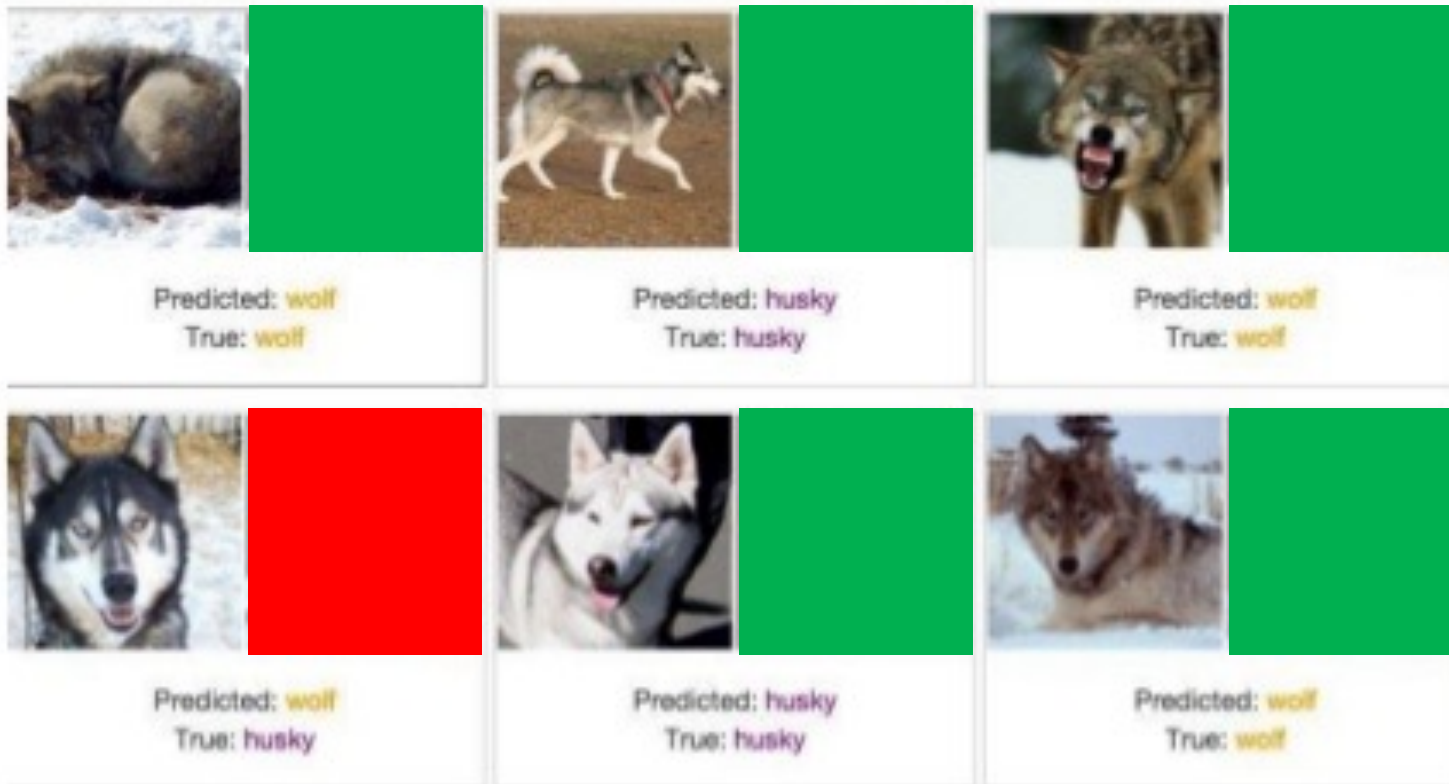
*If the users do not trust a model or a prediction, they will not use it*



For each actor it is  
necessary and usefull  
the model  
***intepretability***



# Understanding the model



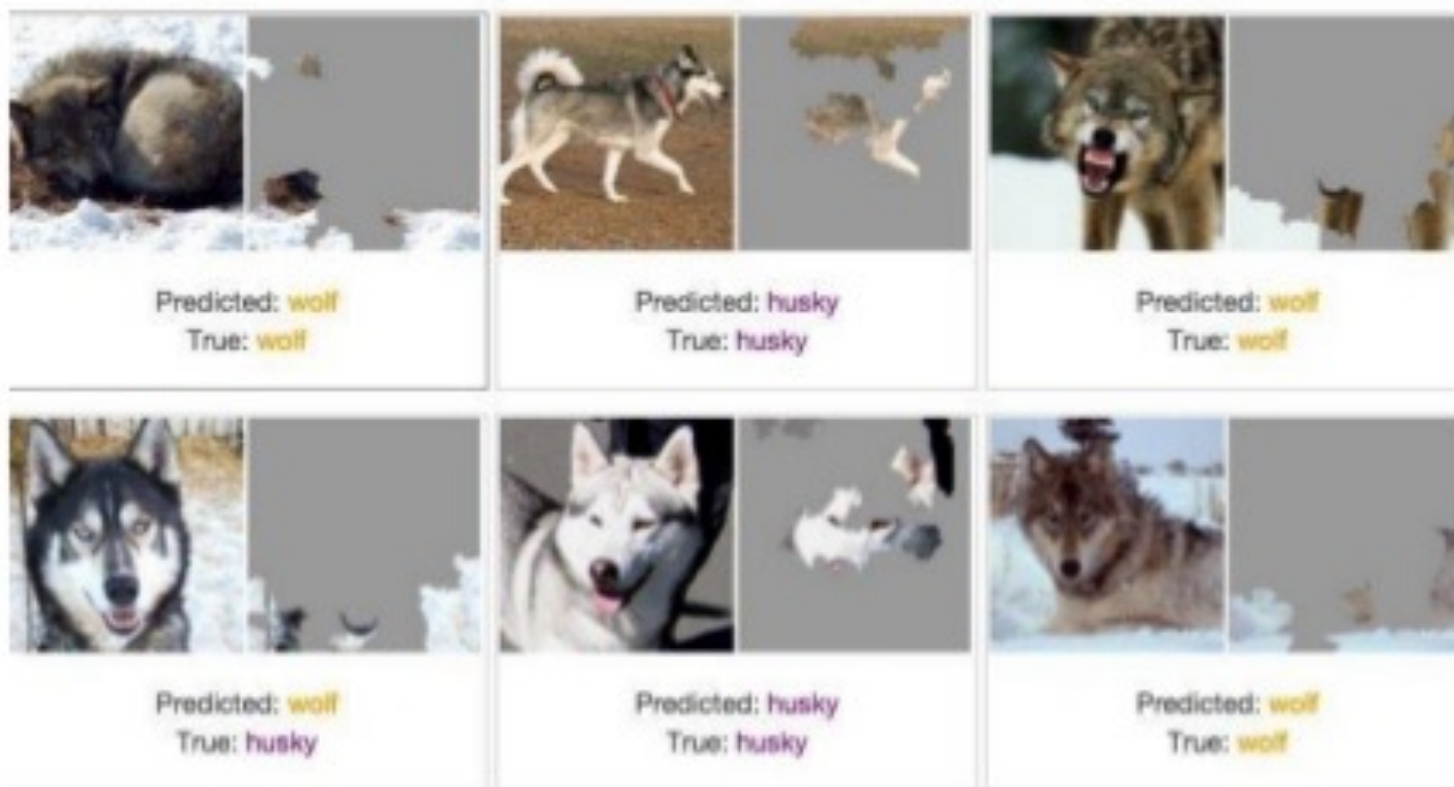
*The model perform very well !!!!*

*So just deploy it!*



# Understanding the model

**... YES, IF YOU WANT TO BUILD A GREAT SNOW  
DETECTOR!**



*No the model is biased by the snow*

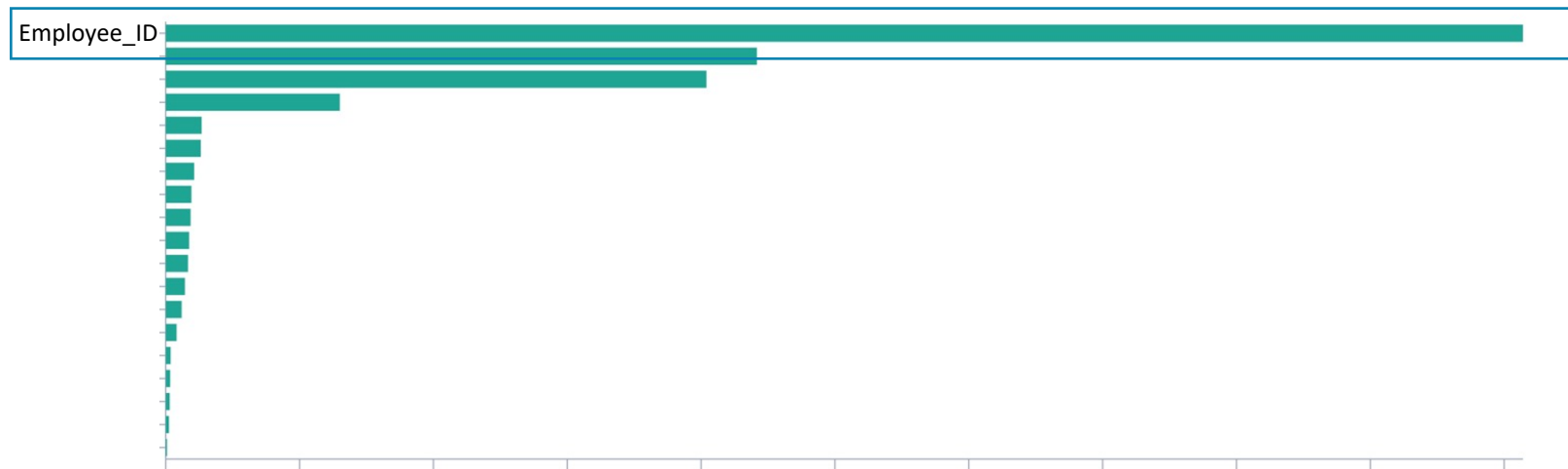


# Understanding the model

## LOAN APPROVAL:

Think if your colleague ROSSI usually works on the most critical contracts.

employee_ID	other features	target
ROSSI	....	DECLINED
ROSSI	....	DECLINED
BIANCHI	....	APPROVED
BIANCHI	....	APPROVED
ROSSI	....	DECLINED
ROSSI	....	DECLINED
...	....	....



The employee ID is one of the most important features



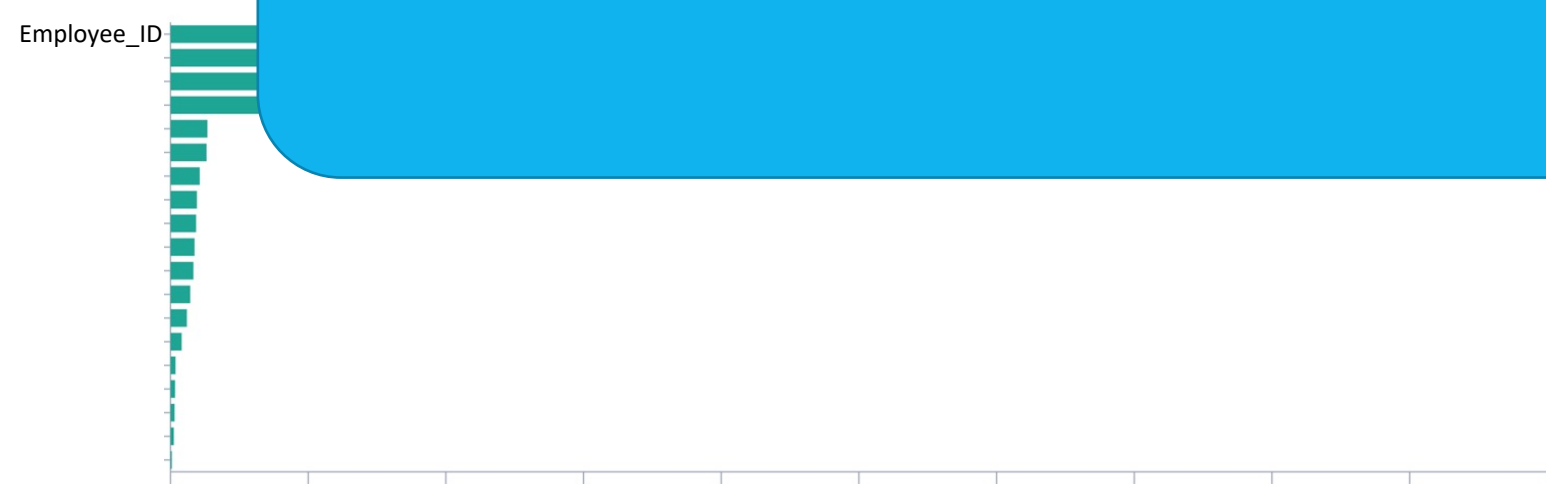
# Understanding the model

## LOAN APPROVAL:

Think if your colleague ROSSI usually works on the most critical contracts.

employee_ID	other features	target
-------------	----------------	--------

Model understanding facilitates the model debugging






# Understanding the model

## LOAN APPROVAL

Contract Request Form



START FILLING →




We have to decline this request



# Understanding the model

## LOAN APPROVAL

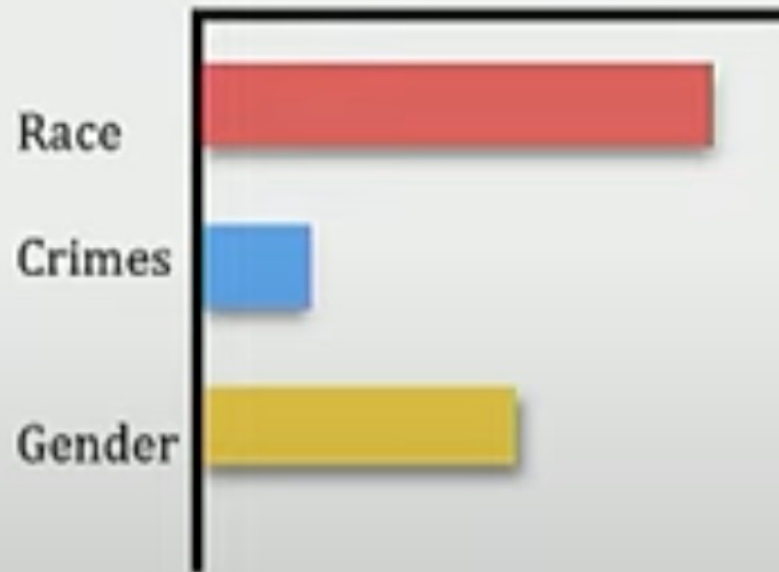
Contract Request Form



START FILLING ->



### Model Understanding



This prediction is biased!!!



# Understanding the model

## LOAN APPROVAL


Model understanding facilitates bias detection on a single prediction

This prediction is

# Understanding the model

## LOAN APPROVAL IN PRODUCTION

Contract Request Form



START FILLING →






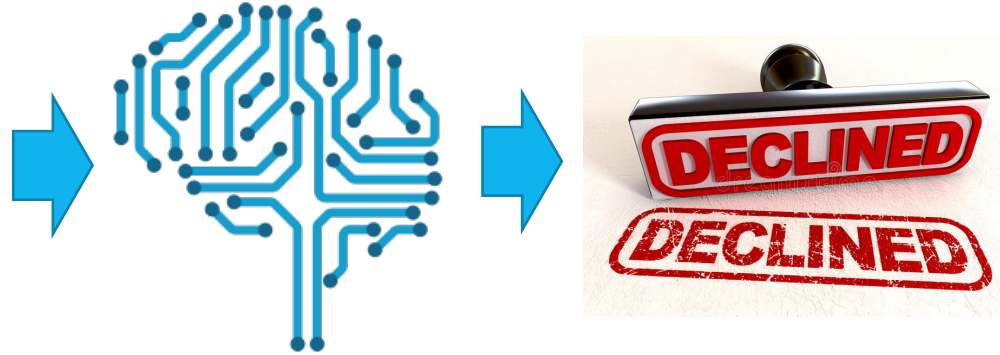
# Understanding the model

## LOAN APPROVAL IN PRODUCTION

Contract Request Form



START FILLING →



How can I get the loan in N months?



Loan applicant

### SUGGESTIONS:

- Pay credit card bills on time for the next 3 months
- Increment your salary by 50K
- ....

# Understanding the model

## LOAN APPROVAL IN PRODUCTION

Contract Request Form

How can I get the loan  
in N months?

Model understanding provide suggestions to individual  
affected by the model prediction

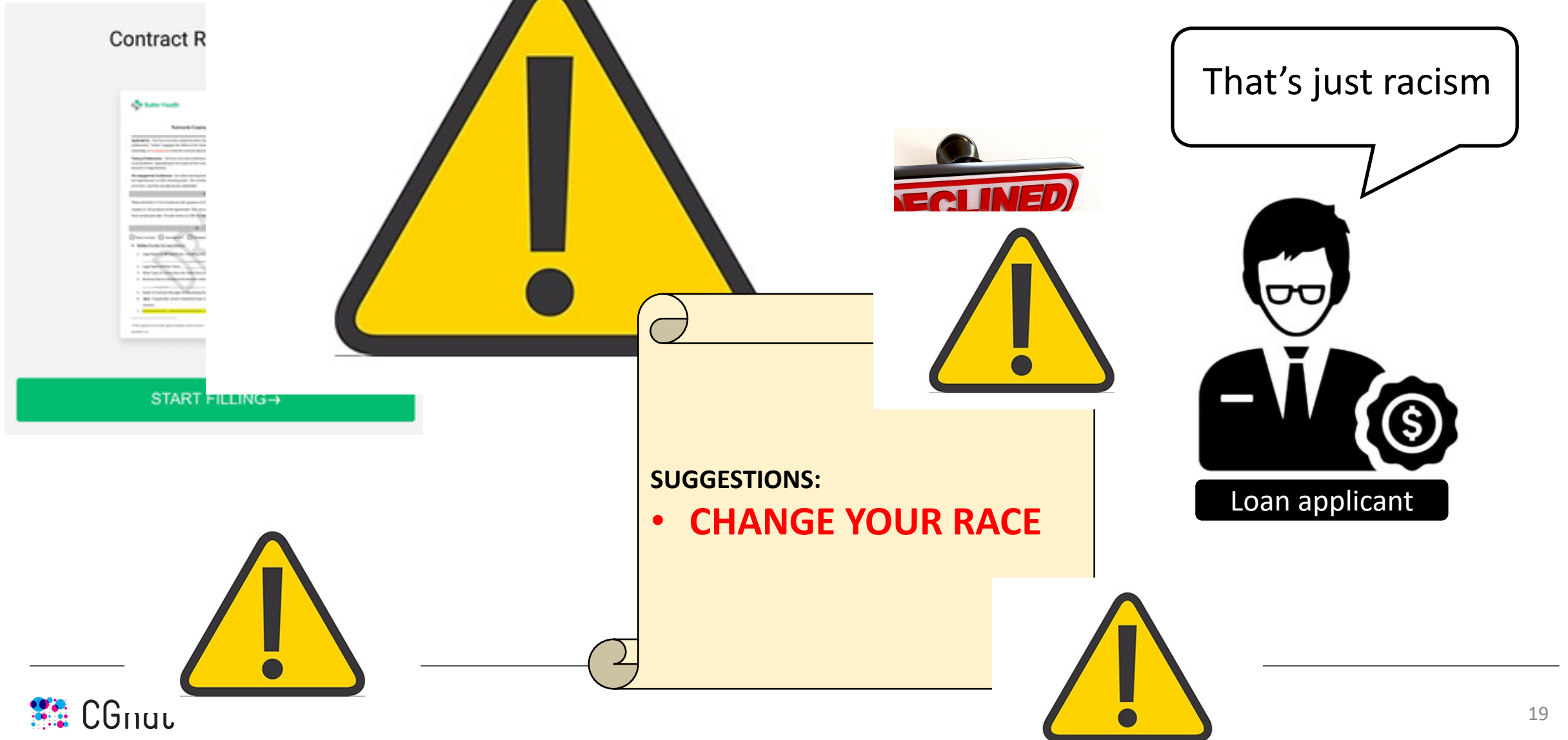
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- ....

Loan applicant

# Understanding the model

## LOAN APPRC



# Understanding the model

## LOAN APPRC

Contract R

SubHealth

Network Code

START FILLING→



We cannot deploy this model



Project Manager

### SUGGESTIONS:

- **CHANGE YOUR RACE**





# Summary: Why model understanding is usefull/needed?

## UTILITY

- Debugging
- Bias Detection
- Suggestions
- If and when to trust a prediction
- Asses suitability for the deployment

## STAKEHOLDERS

- End Users
- Decision making
- Regulatory systems
- Project manager
- ...

# Achiving Model Understanding

# Achiving Model Understanding

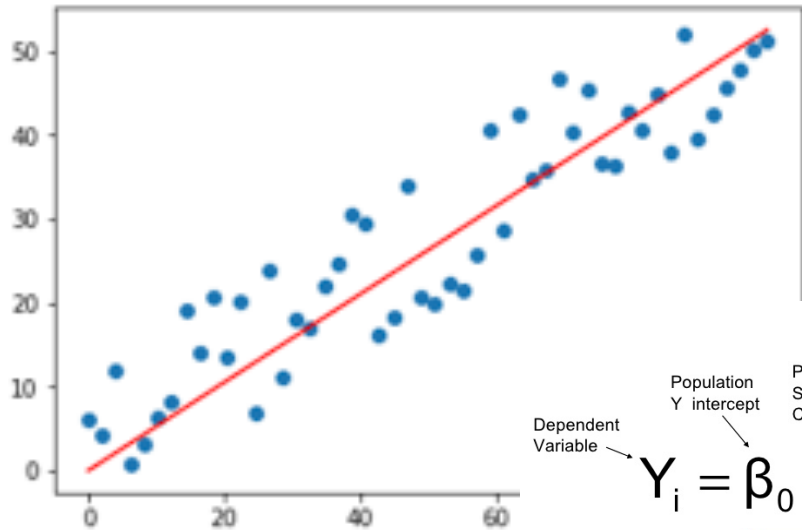
**Method 1:** Build *inherently interpretable* prediction models

---

# Achiving Model Understanding

## Method 1: Build *inherently interpretable* prediction models

### Linear regression



$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$$

Dependent Variable

Population Y intercept

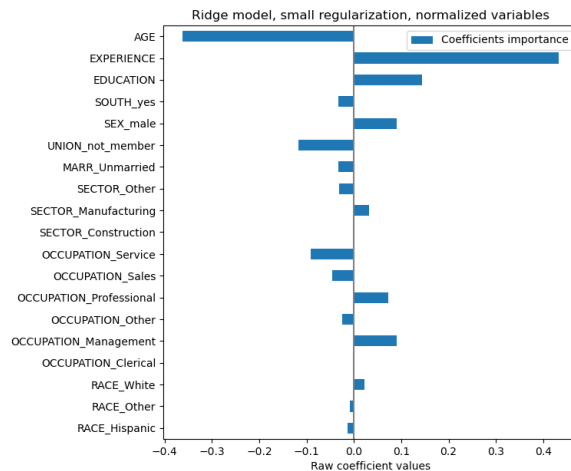
Population Slope Coefficient

Independent Variable

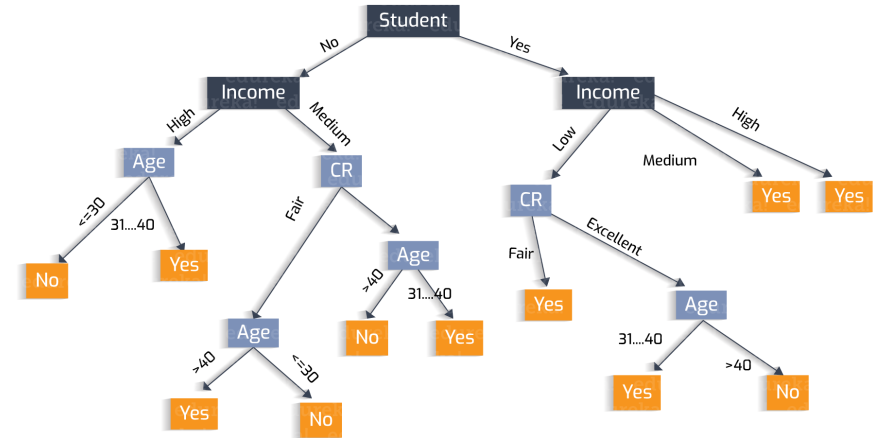
Random Error term

Linear component

Random Error component



### Tree model



If *Student==Yes*:  
if *Income==High*:  
then prediction Yes.  
else if *Income==Medium*:  
then prediction Yes.  
else:  
if *CR==Excellent*:

....



# Achiving Model Understanding

**Method 2: *Explain*** already-built model in a ***post-hoc*** manner

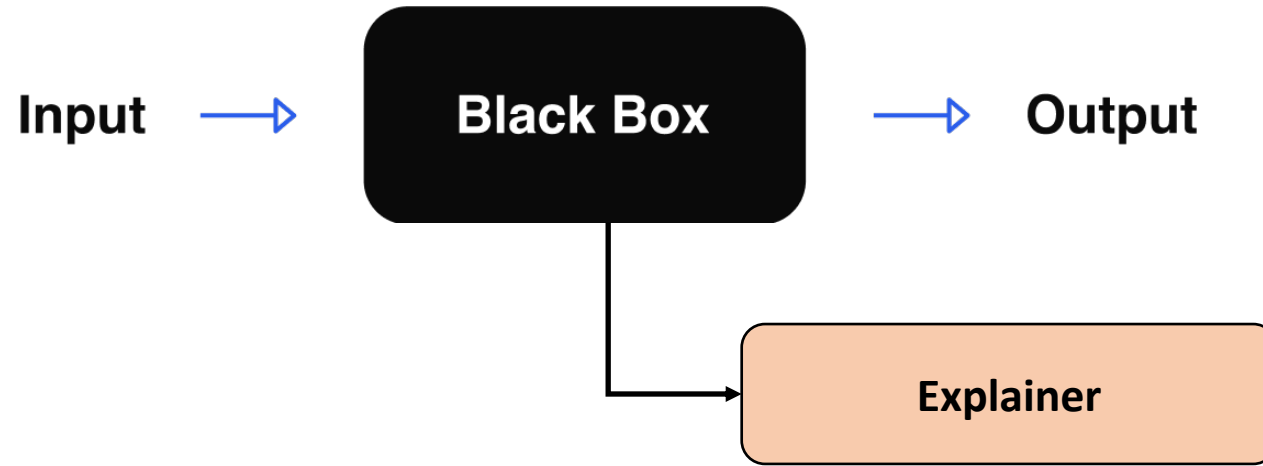
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# Achiving Model Understanding

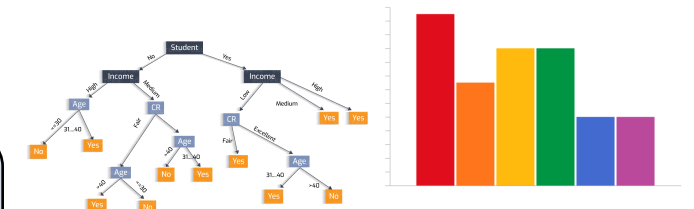
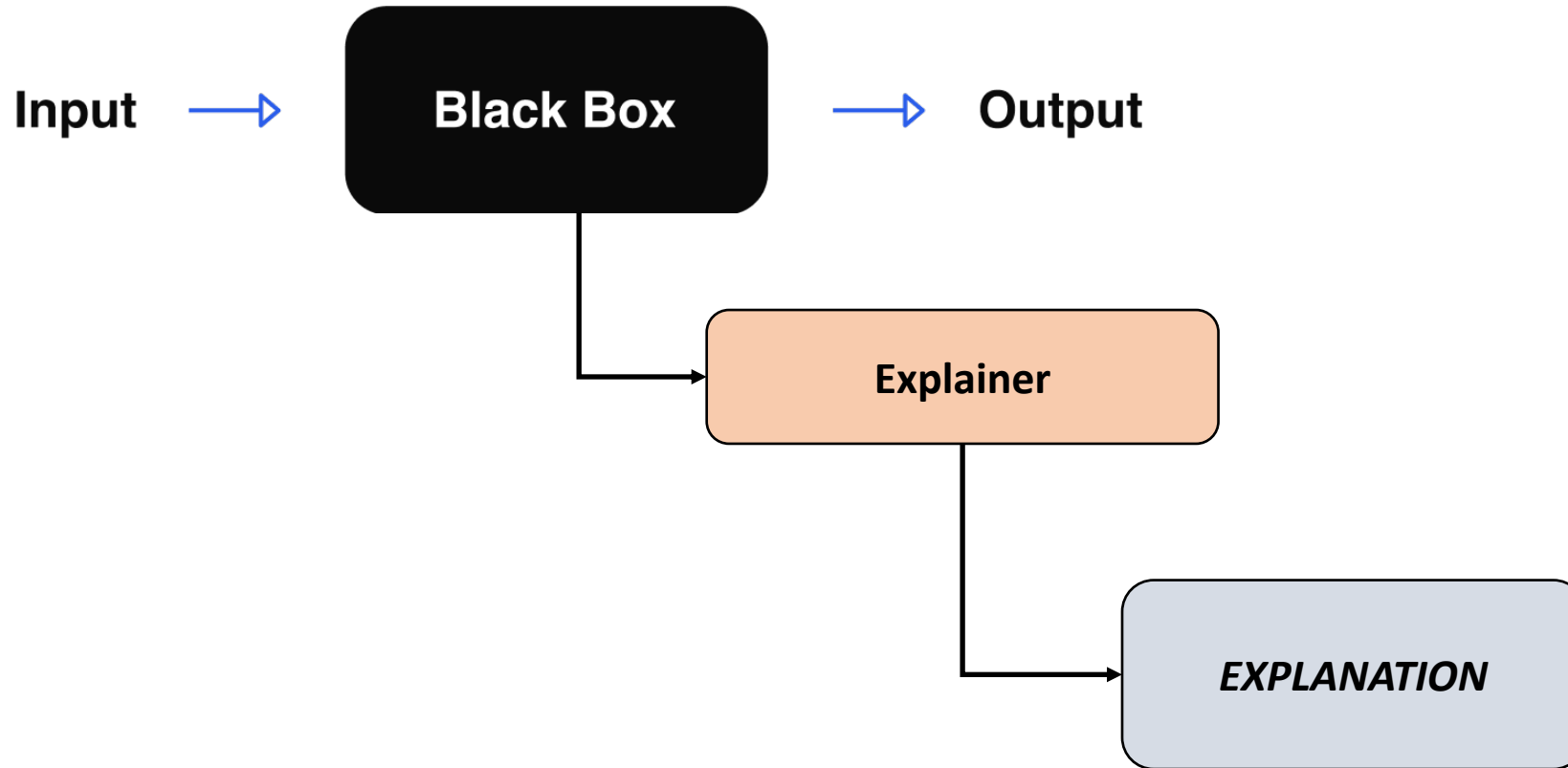
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---



# Achiving Model Understanding

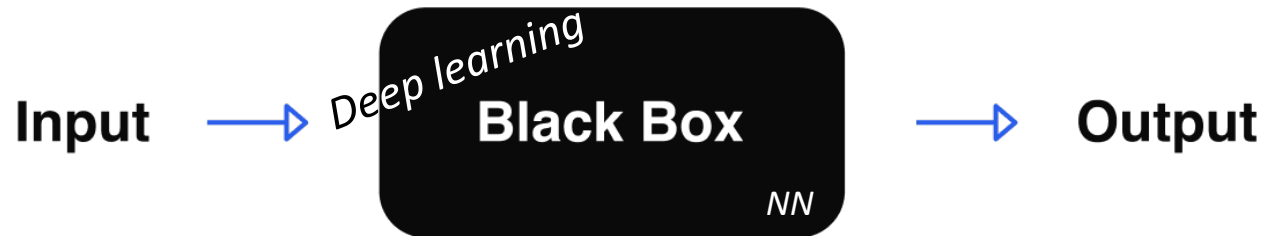
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```
If Student==Yes:
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  else:
    if CR==Excellent:
      ....
```

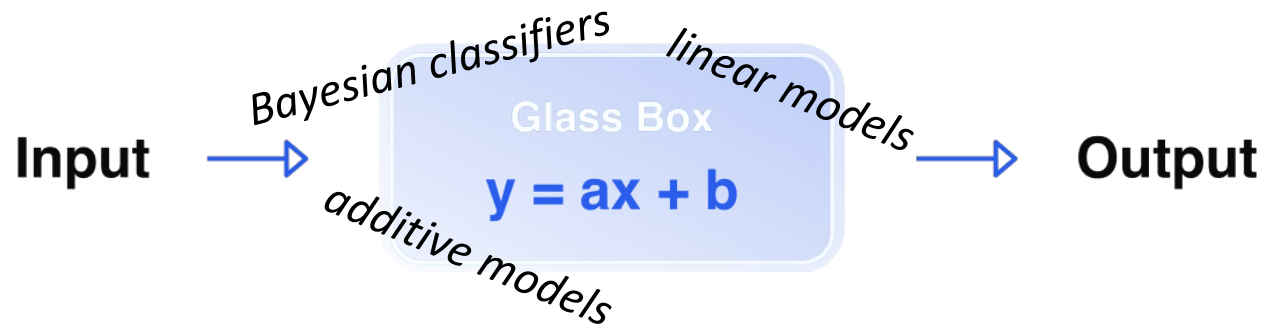
# black box vs glass box

Artificial Intelligence plays a big role in our daily lives. AI is being used everywhere, from our search queries on Google to self-driving vehicles such as Tesla. With the use of deep learning, the models used in these applications have become even more complex. In fact, they are so complex that in many cases we have no idea how these AI models reach their decisions.



Difficult to interpret.

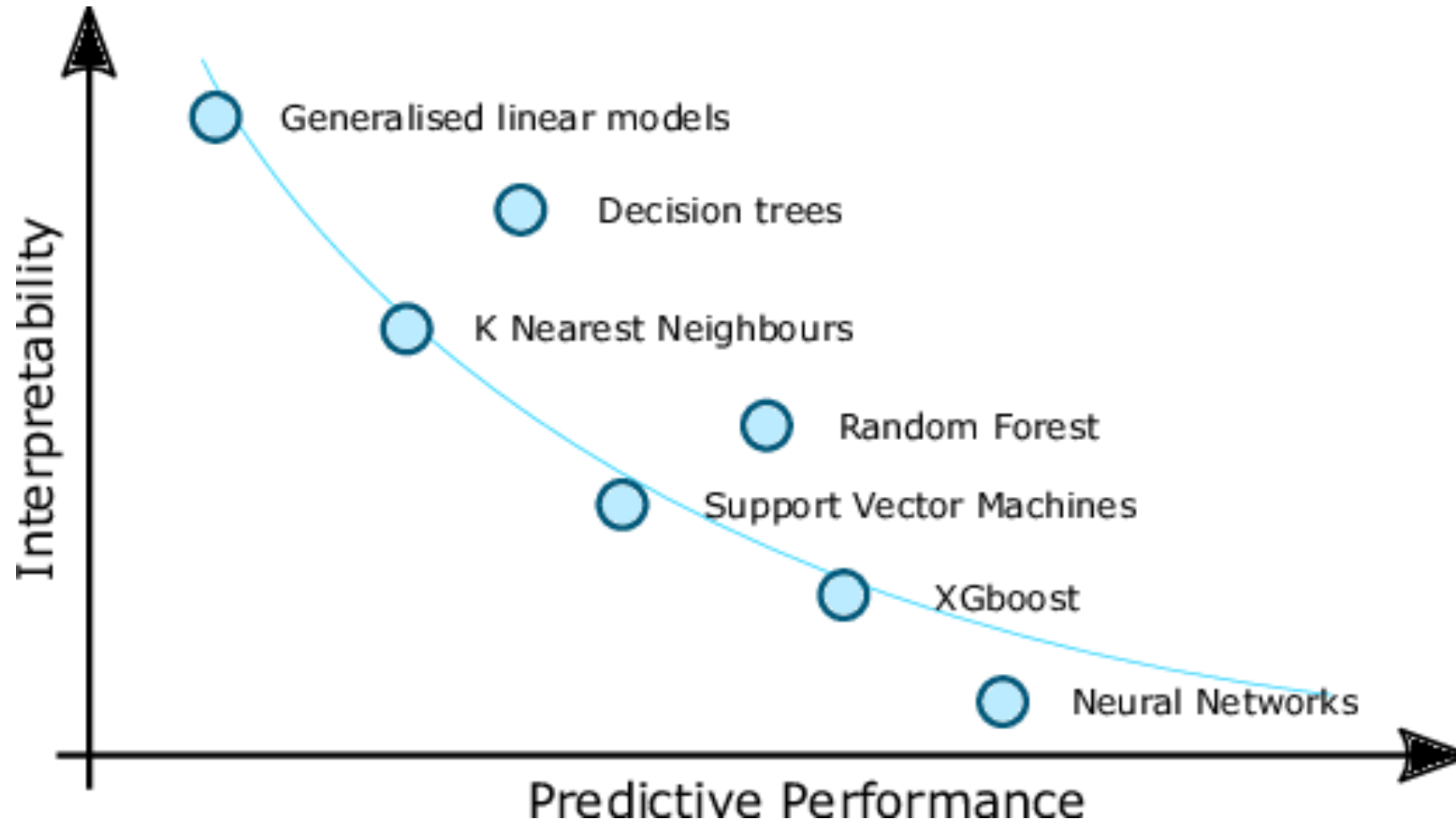
The model structure doesn't allow explainable reasons for the prediction



Easy to interpret.

The model structure gives explainable reasons for the prediction (ex: the coefficient of a linear regression)

## black box vs glass box



# Inherently Interpretable Model vs Post hoc Explanations

If you can build an easily interpretable model which is **adequately accurate** for your settings/problem.

**DO IT!!!!**

If you need a **more complex model** to achieve adequate accuracy, try to use **post hoc explanations**



# Interpretation Methods

The various interpretation methods can be roughly differentiated according to their results:

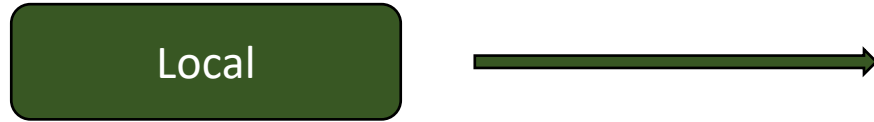
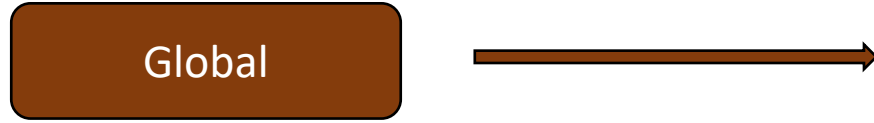
- **Features Importance:** techniques that calculate a score for all the input features for a given model. The scores simply represent the “importance” of each feature.
- **Model Internals:** interpretation of internal components (e.g. parameters, weights). Example are interpretation of intrinsically interpretable models or CNN.
- **Data points:** This category includes all methods that return data points (already existent or newly created) to make a model interpretable. Methods like *counterfactual explanations* (similar examples with differences in some features for which the predicted outcome changes in a relevant way) or *prototypes* of predicted classes.
- **Intrinsically interpretable model:** interpreting black box models is to approximate them (either globally or locally) with an interpretable model.

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# Feature Importance - Introduction



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Global



When the method try to explain which is the feature impact on the model predictions (entire model behaviour)

Local



When the method try to explain which is the feature impact on a specific prediction



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Model Based



Model Agnostic



# Feature Importance - Introduction

Global



When the method try to explain which is the feature impact on the model predictions (entire model behaviour)

Local



When the method try to explain which is the feature impact on a specific prediction

---

Model Based



Model-specific interpretation tools are limited to specific model classes. Example: linear regression coefficients or Gini Index

Model Agnostic



Model-agnostic tools can be used on any machine learning model and are applied after the model has been trained



# Feature Importance - methods

<i><b>Permutation Importance</b></i>	Model Agnostic	Global
<i><b>LIME</b></i>	Model Agnostic	Local
<i><b>SHAP</b></i>	Model Agnostic	Local

# Feature Importance - methods

<i><b>Permutation Importance</b></i>	Model Agnostic	Global	
<i><b>LIME</b></i>	Model Agnostic	Local	<i>SP-LIME</i> → Global
<i><b>SHAP</b></i>	Model Agnostic	Local	<i>aggregating</i> → Global

# Feature Importance – Permutation Feature Importance

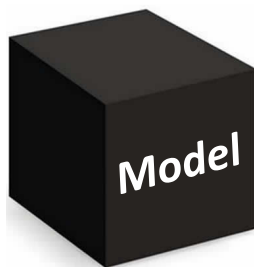
Measure the importance of a feature by calculating the increase in the **model's prediction error** after **permuting the feature**. A feature is “important” if shuffling its values increases the model error, because in this case the model relied on the feature for the prediction

	Feature_1	Feature_2	Feature_3	Label
Sample_1	1970	10.5	1	403.12
Sample_2	2020	14.9	2	412.15
Sample_3	1910	17.7	3	564.46



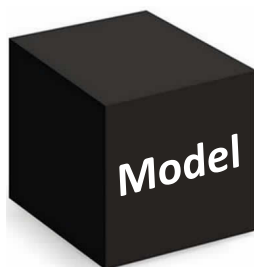
Permute "Feature\_2"

	Feature_1	Feature_2	Feature_3	Label
Sample_1	1970	17.7	1	403.12
Sample_2	2020	10.5	2	412.15
Sample_3	1910	14.9	3	564.46



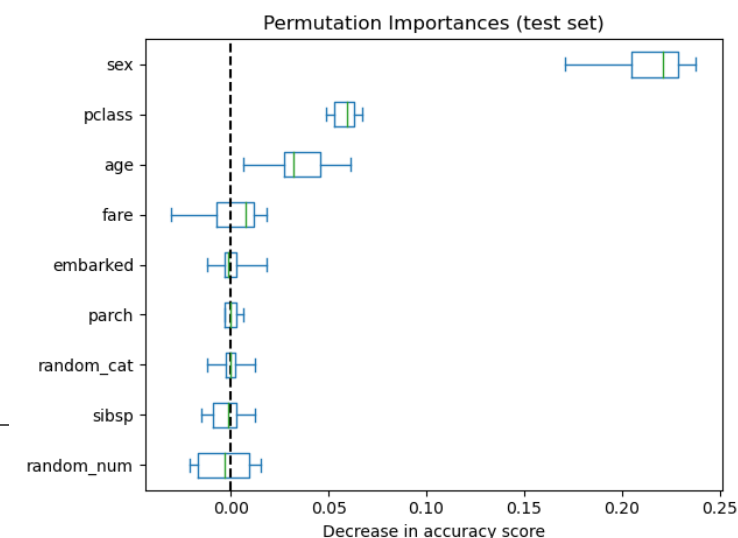
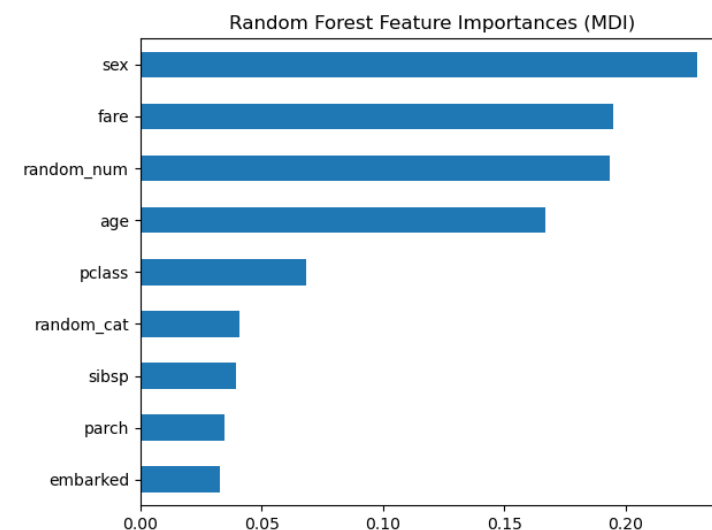
label (Predicted Original)
350.54
420.24
600.13

K times

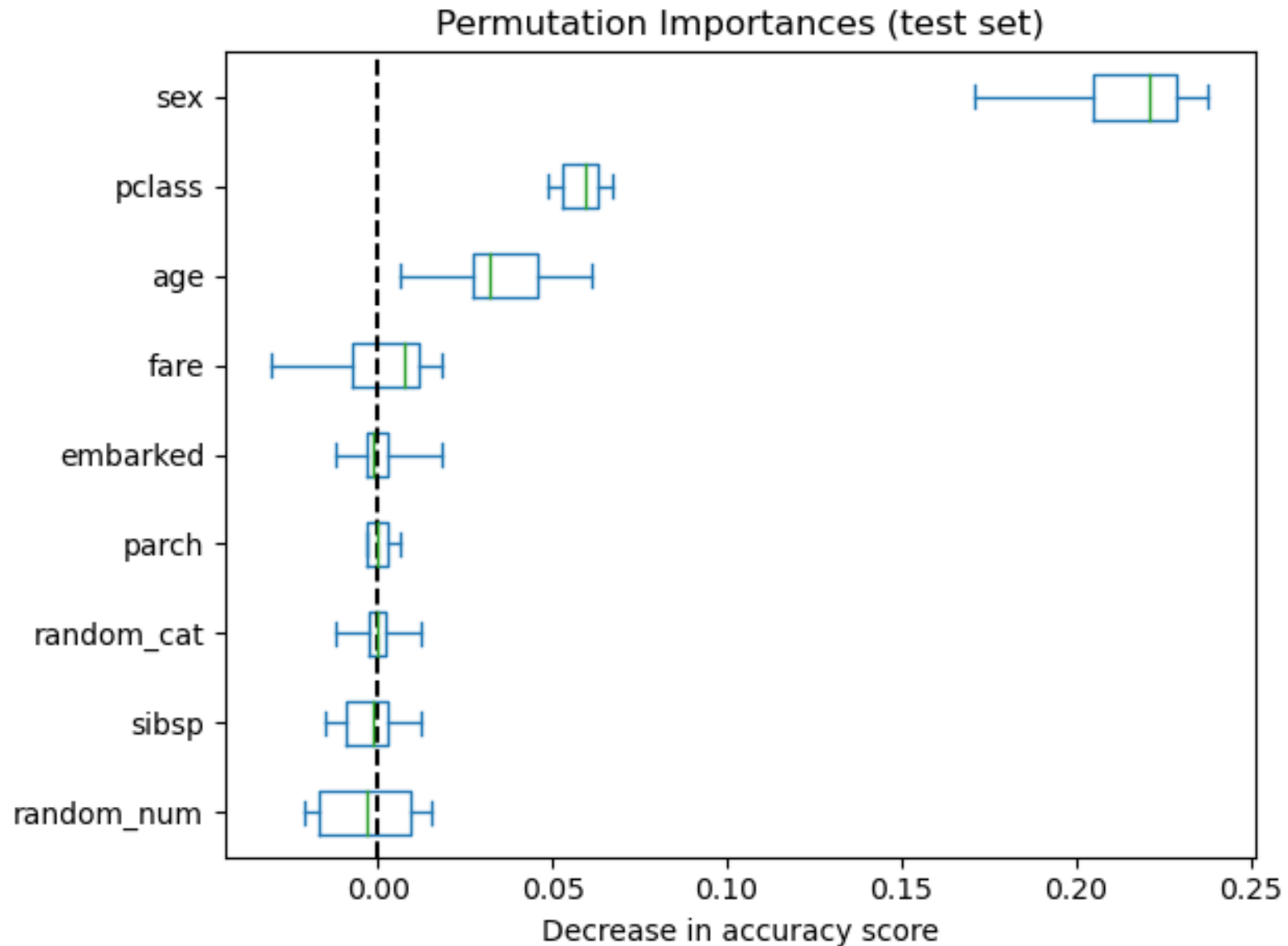


label (Predicted Permuted)
700.65
300.13
121.15

Average difference  
= Feature Importance



# Feature Importance – Permutation Feature Importance



# Feature Importance – Permutation Feature Importance

## Pseudo-code

- Inputs: fitted predictive model  $m$ , tabular dataset (training or validation)  $D$ .
- Compute the reference score  $s$  of the model  $m$  on data  $D$  (for instance the accuracy for a classifier or the  $R^2$  for a regressor).
- For each feature  $j$  (column of  $D$ ):
  - For each repetition  $k$  in  $1, \dots, K$ :
    - Randomly shuffle column  $j$  of dataset  $D$  to generate a corrupted version of the data named  $\tilde{D}_{k,j}$ .
    - Compute the score  $s_{k,j}$  of model  $m$  on corrupted data  $\tilde{D}_{k,j}$ .
  - Compute importance  $i_j$  for feature  $f_j$  defined as:

```
from sklearn.inspection import permutation_importance
```

$$i_j = s - \frac{1}{K} \sum_{k=1}^K s_{k,j}$$

## Criticism

When ***two features are correlated*** and one of the features is permuted, the model will still have access to the feature through its correlated feature. This will result in a lower importance value for both features, where they might *actually* be important.

# Feature Importance – LIME

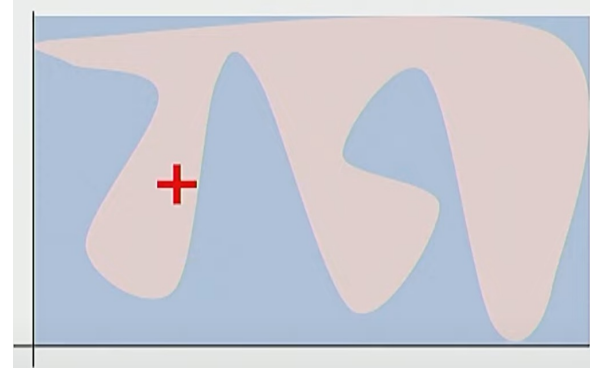
Model Agnostic

Local

**LIME = Local Interpretable Model-agnostic Explanations**

Try to fit a simple linear model locally

We would like to get features importance for a point  $x_i$ :





# Feature Importance – LIME

Model Agnostic

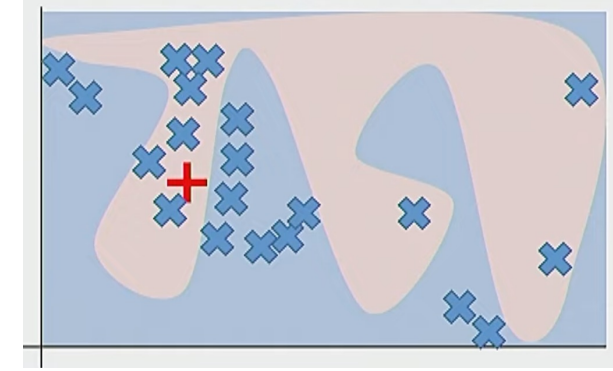
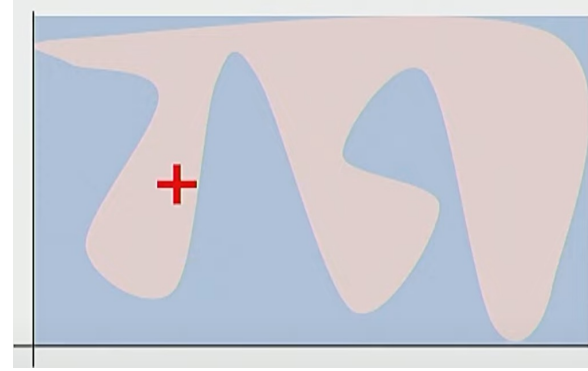
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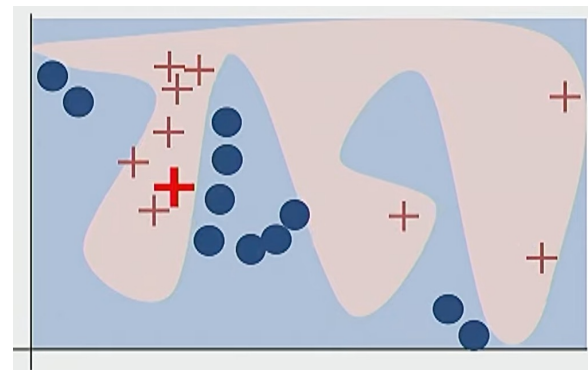
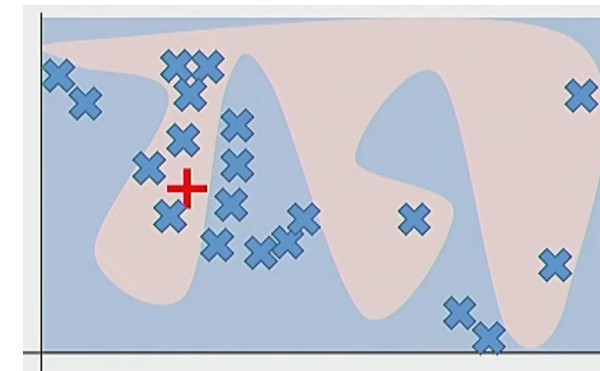
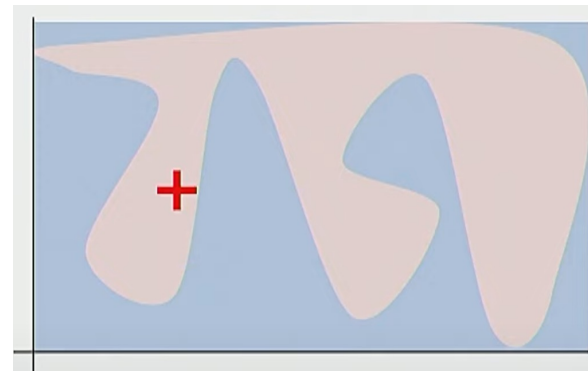
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We would like to get features importance for a point  $x_i$ :

1. Generate random sample points around  $x_i$
2. Use Model to predict each generated data point



# Feature Importance – LIME

Model Agnostic

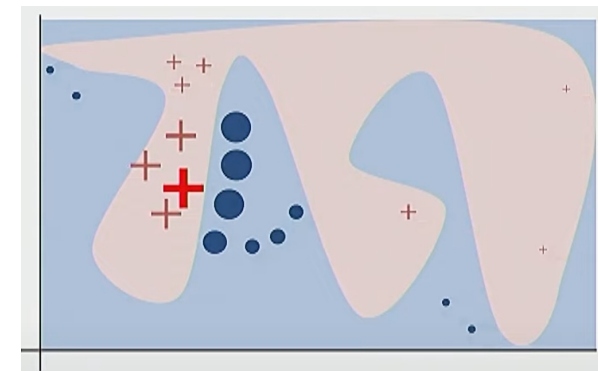
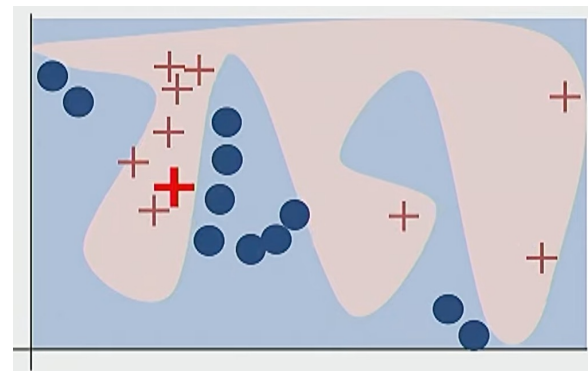
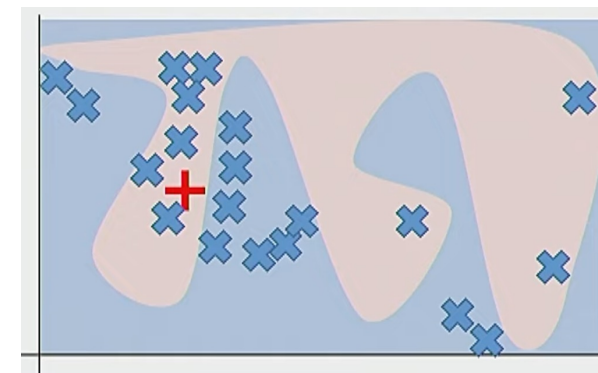
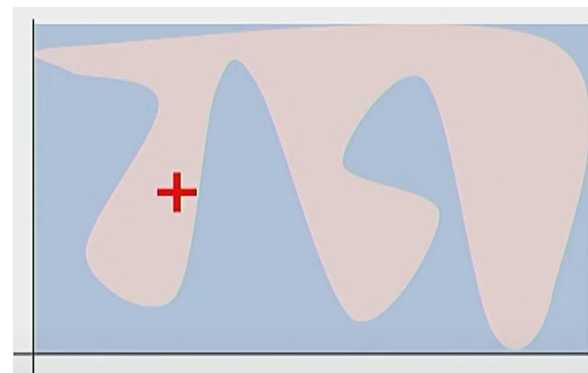
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We would like to get features importance for a point  $x_i$ :

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2. Use Model to predict each generated data point
3. Weight samples according to distance from  $x_i$



# Feature Importance – LIME

Model Agnostic

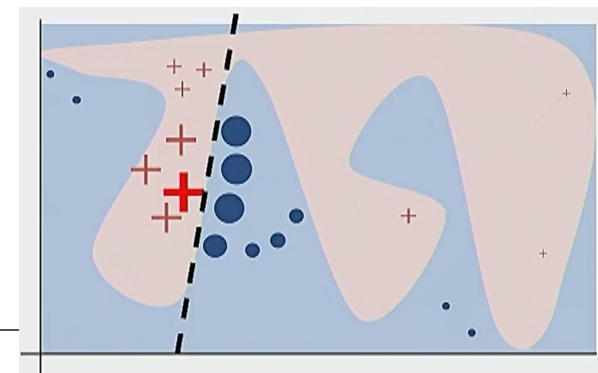
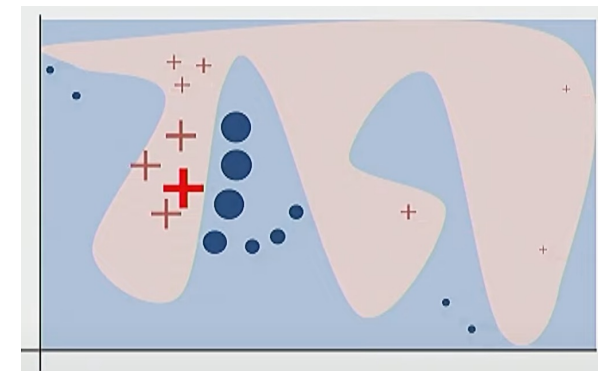
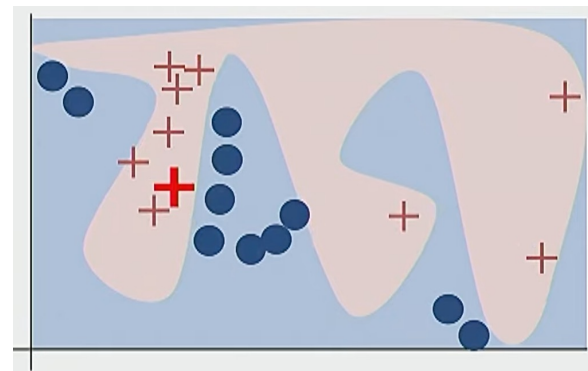
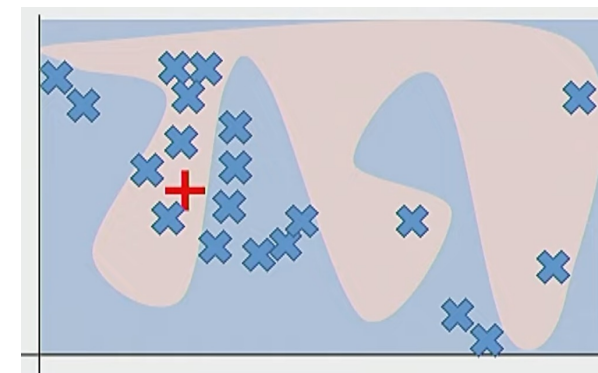
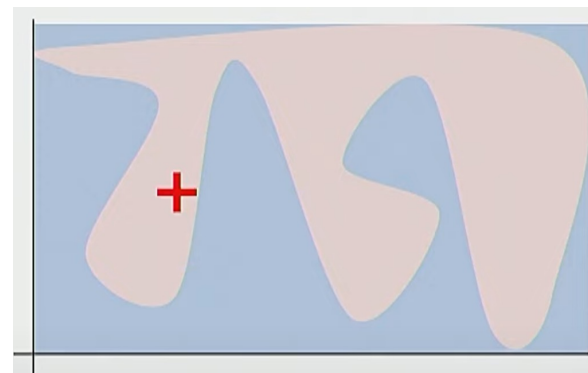
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4. Learn a simple weighted linear model on samples



# Feature Importance – LIME

Model Agnostic

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1. Generate random sample points around  $x_i$
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**LOCAL CONTRIBUTION OF THE FEATURES**

$$Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$$

Labels in the diagram:  
-  $Y_i$ : Dependent Variable  
-  $\beta_0$ : Population Y intercept  
-  $\beta_1$ : Population Slope Coefficient  
-  $X_i$ : Independent Variable  
-  $\varepsilon_i$ : Random Error term

$$\text{Ln}\left(\frac{P}{1-P}\right) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k$$

# Feature Importance – LIME

Model Agnostic

Local

## Advantages:

- When using Lasso or short trees, the resulting **explanations are short** (= selective) and possibly contrastive. Therefore, they make **human-friendly explanations**.
- The **fidelity measure** (how well the interpretable model approximates the black box predictions) gives us a good idea of how reliable the interpretable model is in explaining the black box predictions in the neighborhood of the data instance of interest.
- The explanations created with local surrogate models **can use other (interpretable) features than the original model was trained on..**

## Disadvantages:

- The correct **definition** of the **neighborhood** is a very big, **unsolved** problem when using LIME with tabular data.



# Feature Importance – SHAP

Model Agnostic

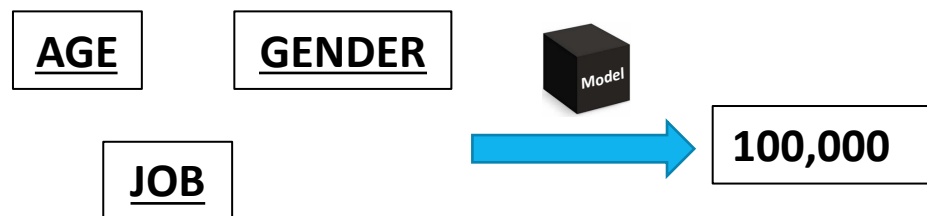
Local

## Shapley Values:

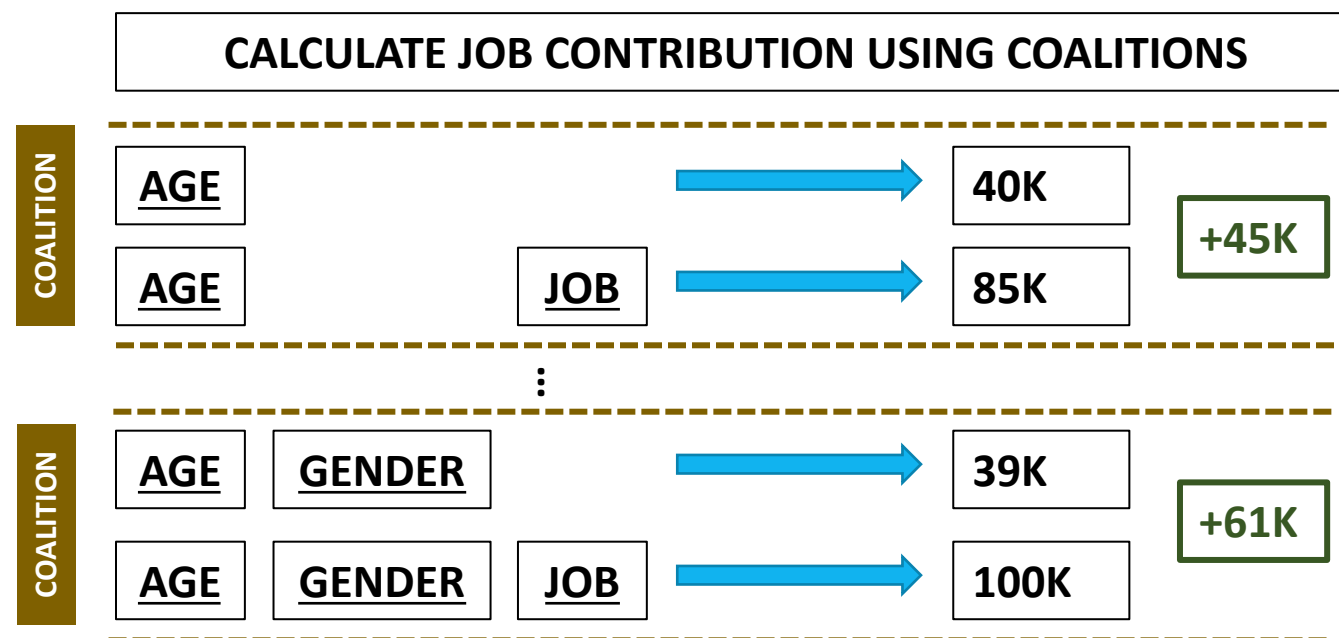
Shapley values – a method from coalitional game theory – tells us how to fairly distribute the “payout” among the features. Are based on the idea that the outcome of each possible combination (or coalition) of players should be considered to determine the importance of a single player.

Example:

You have trained a model that predicts the income of a person knowing **age**, **gender** and **job** of the person.



How much has **each feature value contributed** to the **prediction** compared to the average prediction?

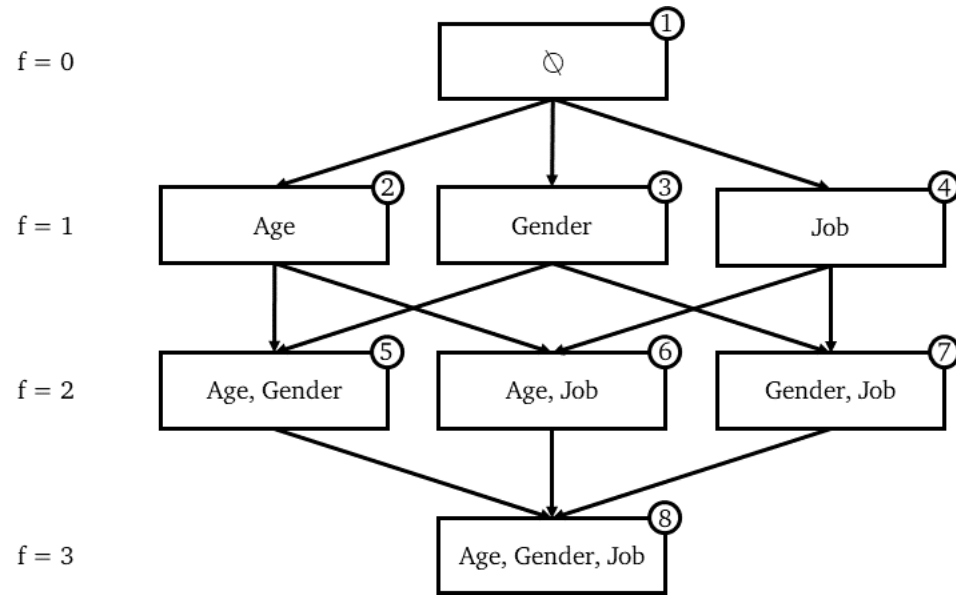


# Feature Importance – SHAP

Shaply values

Model Agnostic

Local

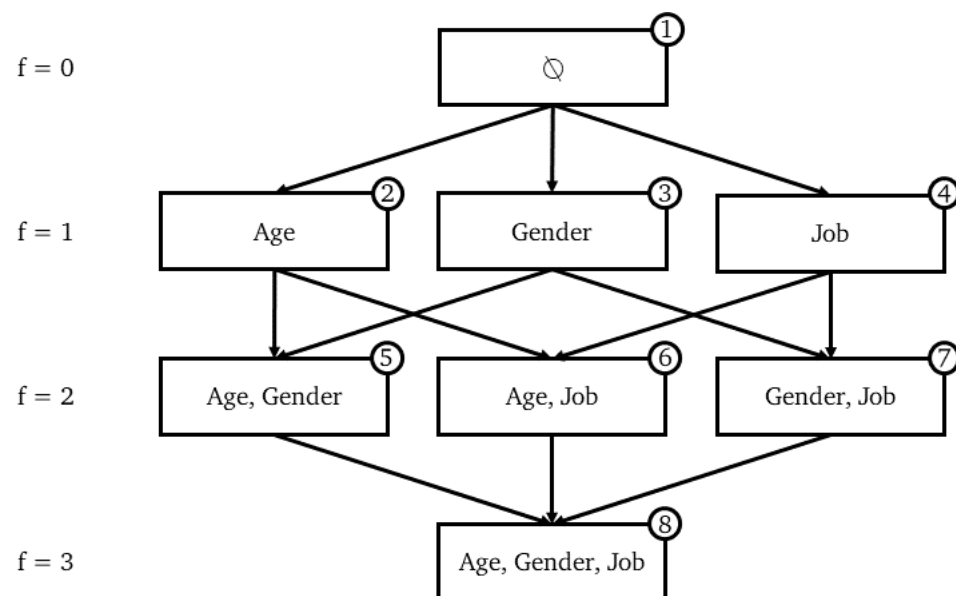


# Feature Importance – SHAP

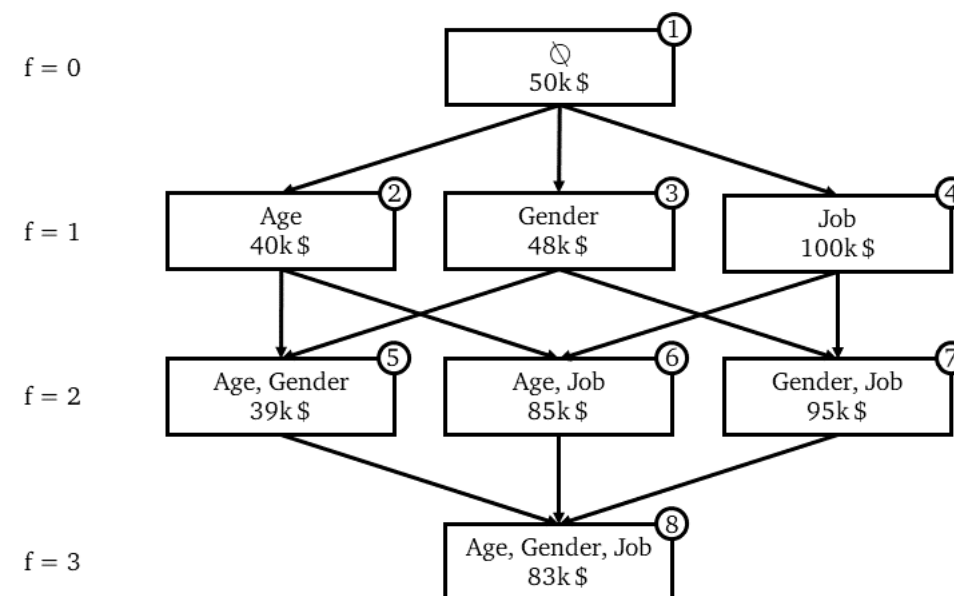
Shaply values

Model Agnostic

Local



Train 8 different models

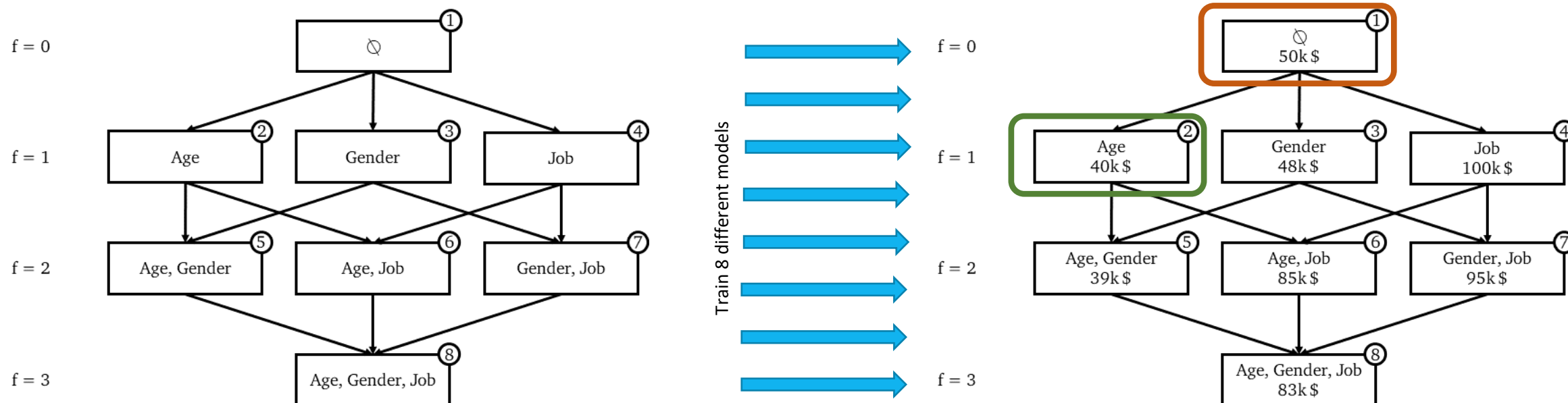


# Feature Importance – SHAP

Shaply values

Model Agnostic

Local



**Each edge represents the marginal contribution brought by a feature to a model.**

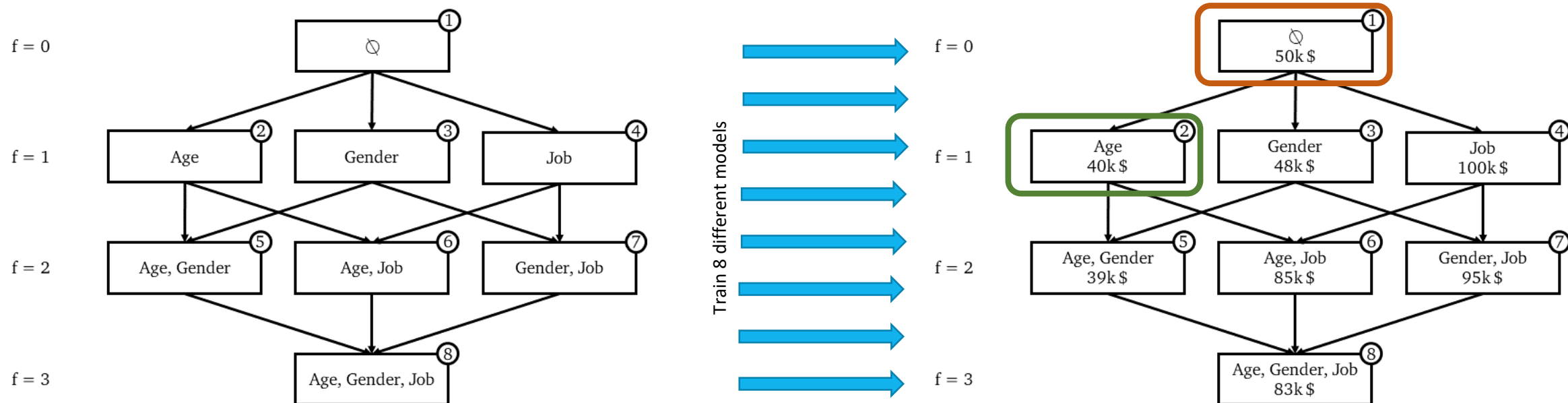
Which is the contribution of feature AGE from (1) to (2)

# Feature Importance – SHAP

Shaply values

Model Agnostic

Local



Each edge represents the marginal contribution brought by a feature to a model.

Which is the contribution of feature AGE from (1) to (2)

$$MC_{Age, \{Age\}}(x_0) = \text{Predict}_{\{Age\}}(x_0) - \text{Predict}_{\emptyset}(x_0) = 40k\$ - 50k\$ = -10k\$$$

$$MC_{Age, \{Age, Gender\}}(x_0)$$

$$MC_{Age, \{Age, Job\}}(x_0)$$

$$MC_{Age, \{Age, Gender, Job\}}(x_0)$$



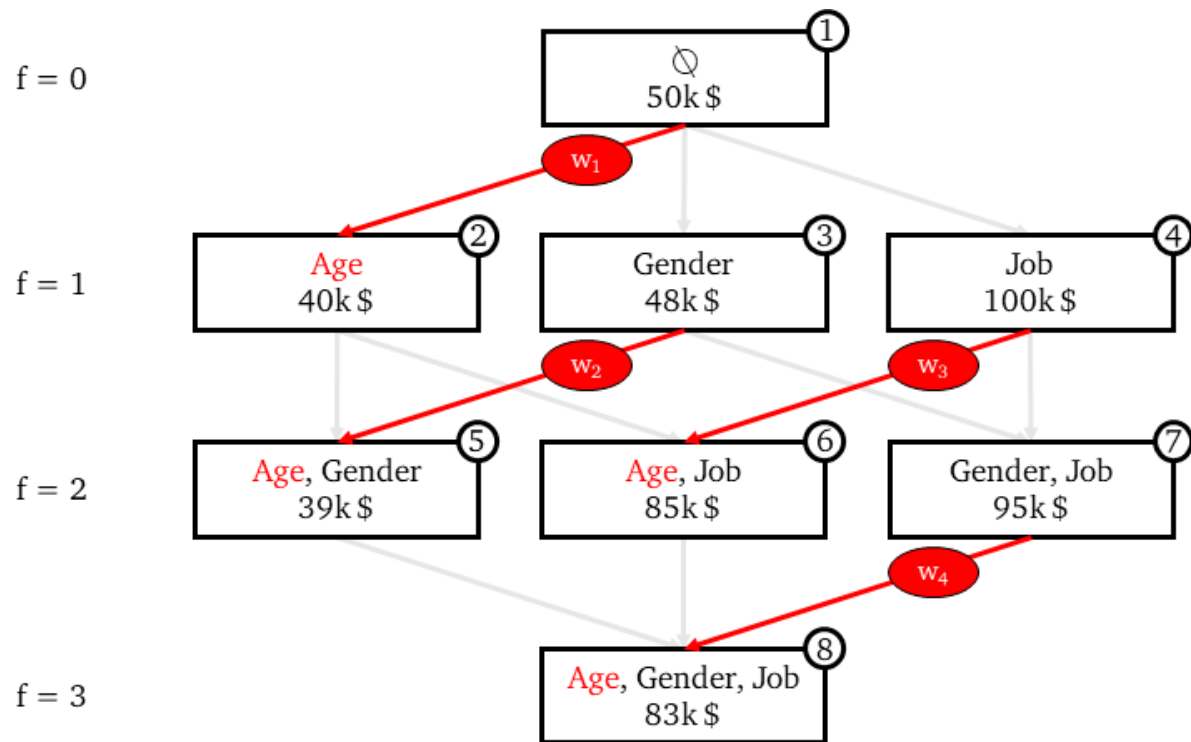
CGn

# Feature Importance – SHAP

Shaply values

Model Agnostic

Local



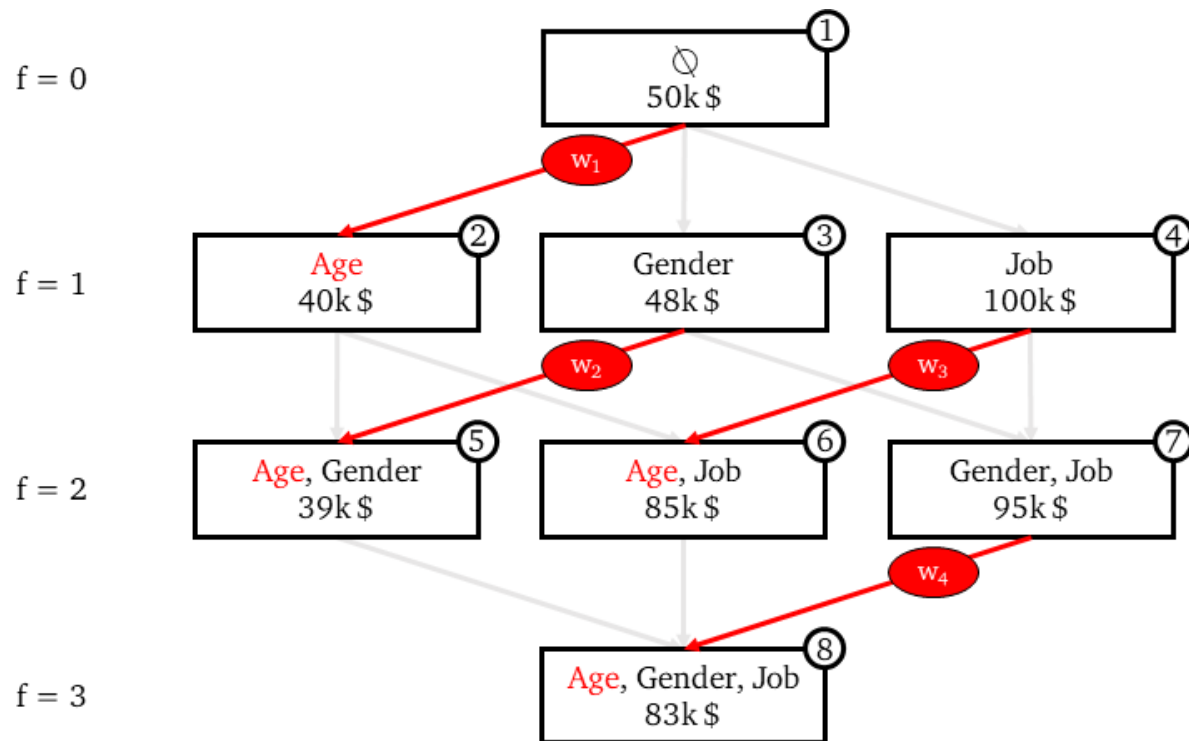
$$\begin{aligned} SHAP_{Age}(x_0) = & w_1 \times MC_{Age, \{Age\}}(x_0) + \\ & w_2 \times MC_{Age, \{Age, Gender\}}(x_0) + \\ & w_3 \times MC_{Age, \{Age, Job\}}(x_0) + \\ & w_4 \times MC_{Age, \{Age, Gender, Job\}}(x_0) \end{aligned}$$

# Feature Importance – SHAP

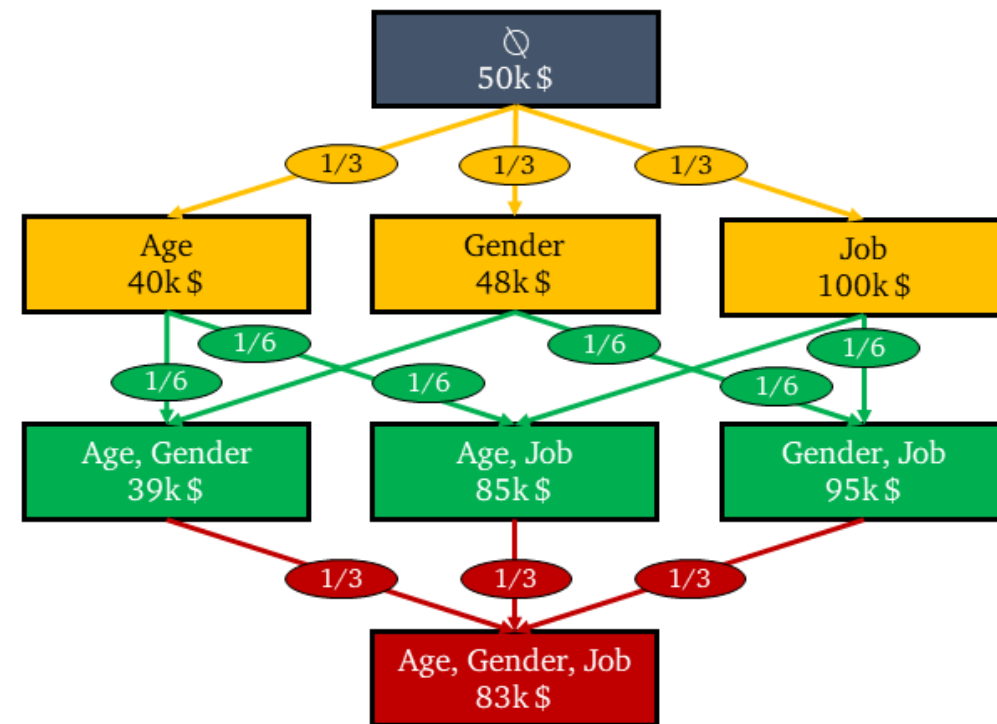
Shaply values

Model Agnostic

Local



$$SHAP_{Age}(x_0) = w_1 \times MC_{Age, \{Age\}}(x_0) + w_2 \times MC_{Age, \{Age, Gender\}}(x_0) + w_3 \times MC_{Age, \{Age, Job\}}(x_0) + w_4 \times MC_{Age, \{Age, Gender, Job\}}(x_0)$$



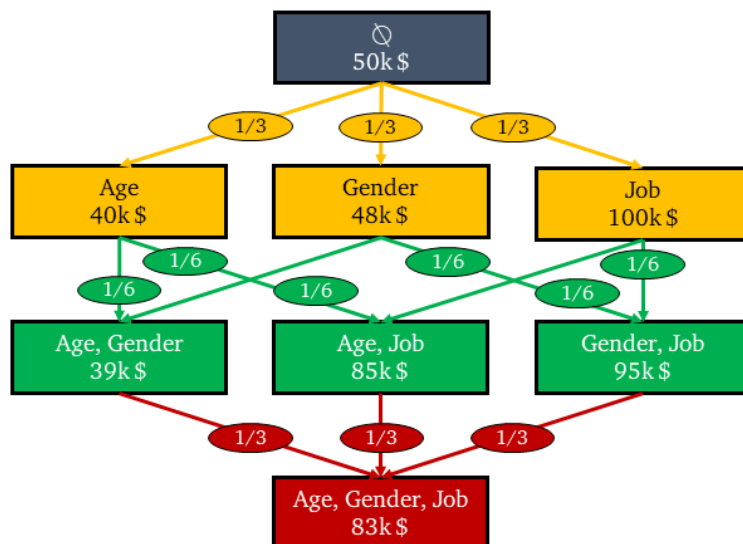
$$\begin{aligned} SHAP_{Age}(x_0) &= [(1 \times \binom{3}{1})^{-1} \times MC_{Age, \{Age\}}(x_0) + \\ &\quad [(2 \times \binom{3}{2})^{-1} \times MC_{Age, \{Age, Gender\}}(x_0) + \\ &\quad [(2 \times \binom{3}{2})^{-1} \times MC_{Age, \{Age, Job\}}(x_0) + \\ &\quad [(3 \times \binom{3}{3})^{-1} \times MC_{Age, \{Age, Gender, Job\}}(x_0) + \\ &= \frac{1}{3} \times (-10k\$) + \frac{1}{6} \times (-9k\$) + \frac{1}{6} \times (-15k\$) + \frac{1}{3} \times (-12k\$) \\ &= -11.33k\$ \end{aligned}$$

# Feature Importance – SHAP

Shaply values

Model Agnostic

Local



$$\begin{aligned}
 SHAP_{Age}(x_0) &= [(1 \times \binom{3}{1})^{-1} \times MC_{Age, \{Age\}}(x_0) + \\
 &\quad [(2 \times \binom{3}{2})^{-1} \times MC_{Age, \{Age, Gender\}}(x_0) + \\
 &\quad [(2 \times \binom{3}{2})^{-1} \times MC_{Age, \{Age, Job\}}(x_0) + \\
 &\quad [(3 \times \binom{3}{3})^{-1} \times MC_{Age, \{Age, Gender, Job\}}(x_0) + \\
 &= \frac{1}{3} \times (-10k\$) + \frac{1}{6} \times (-9k\$) + \frac{1}{6} \times (-15k\$) + \frac{1}{3} \times (-12k\$) \\
 &= -11.33k\$
 \end{aligned}$$

$$g(z') = \phi_0 + \sum_{j=1}^M \phi_j z'_j$$

where  $g$  is the explanation model,  $z' \in \{0, 1\}^M$  is the coalition vector,  $M$  is the maximum coalition size and  $\phi_j \in \mathbb{R}$  is the feature attribution for a feature  $j$ , the Shapley values. What I call “coalition — vector” is called “simplified features” in the SHAP paper.



# Feature Importance – SHAP

Model Agnostic

Local

```
pip install shap
```

**KernelSHAP**: an alternative, kernel-based estimation approach for Shapley values inspired by LIME.

```
from shap import KernelExplainer
```

**TreeSHAP**: an efficient estimation approach for tree-based models like *decision trees*, *random forest* and *gradient boosted trees*.

```
from shap import TreeExplainer
```

# Feature Importance – SHAP

Model Agnostic

Local

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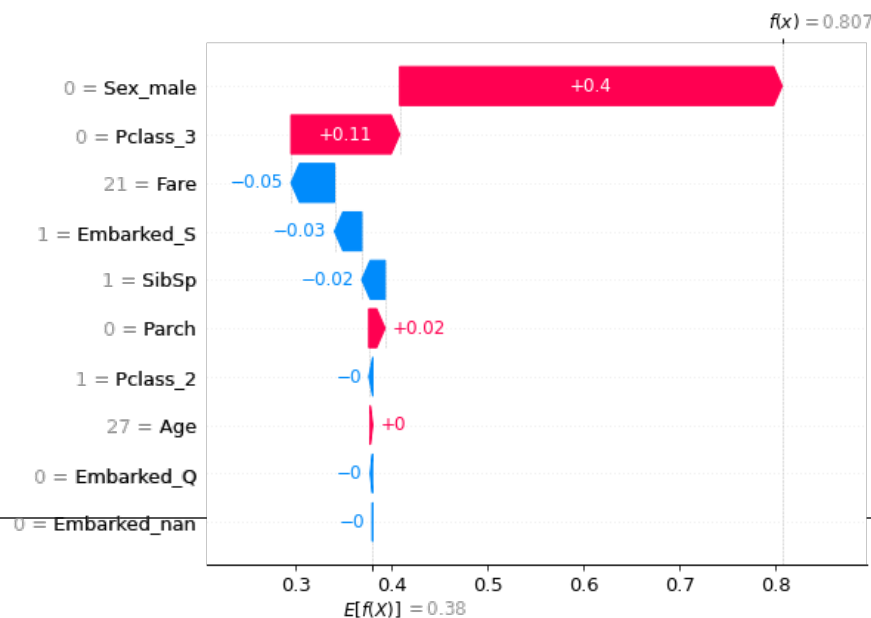
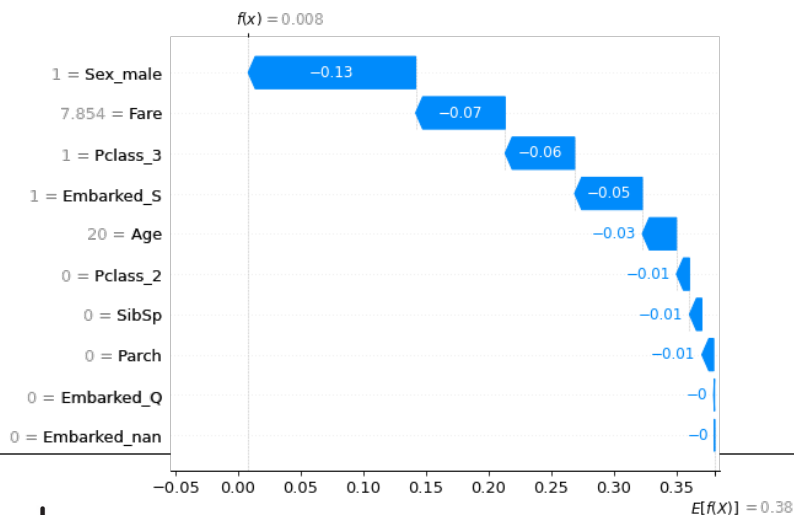
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from shap import TreeExplainer
```

## SHAP VALUES VISUALIZATION



$$\sum_{j=1}^M \phi_j z'_j$$

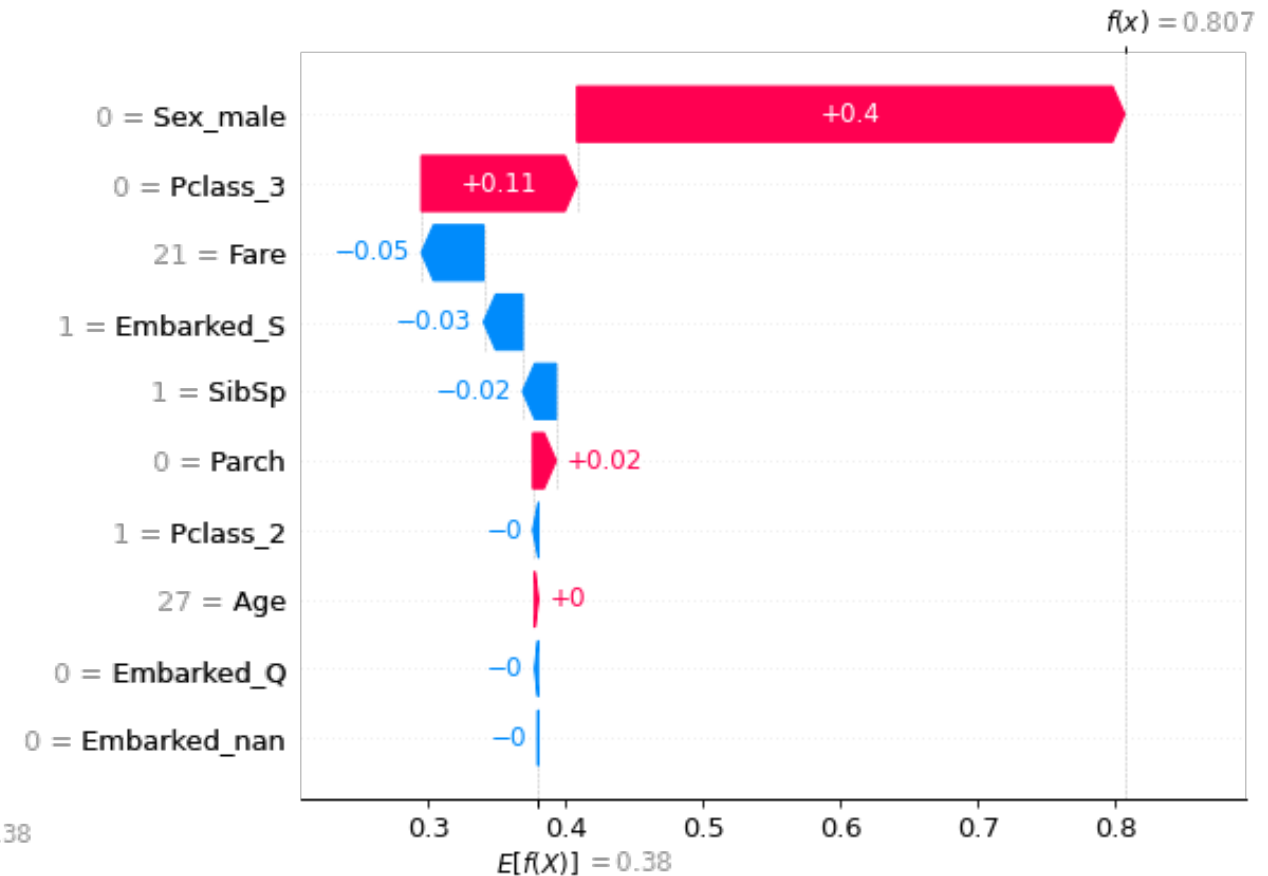
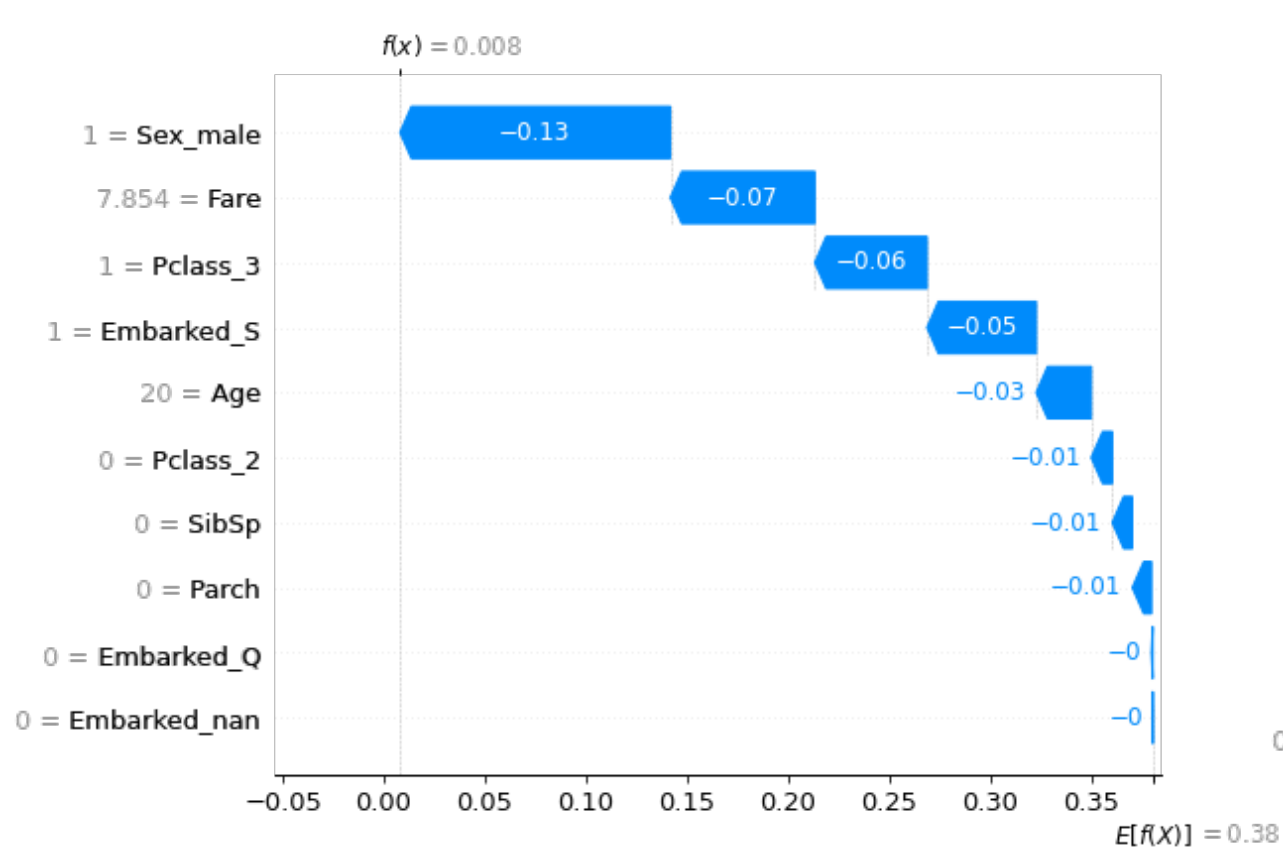
# Feature Importance – SHAP

Model Agnostic

Local

$$\sum_{j=1}^M \phi_j z'_j$$

SHAP explanation force plots for two different samples from the titanic dataset:



# Feature Importance – SHAP

Model Agnostic

Local

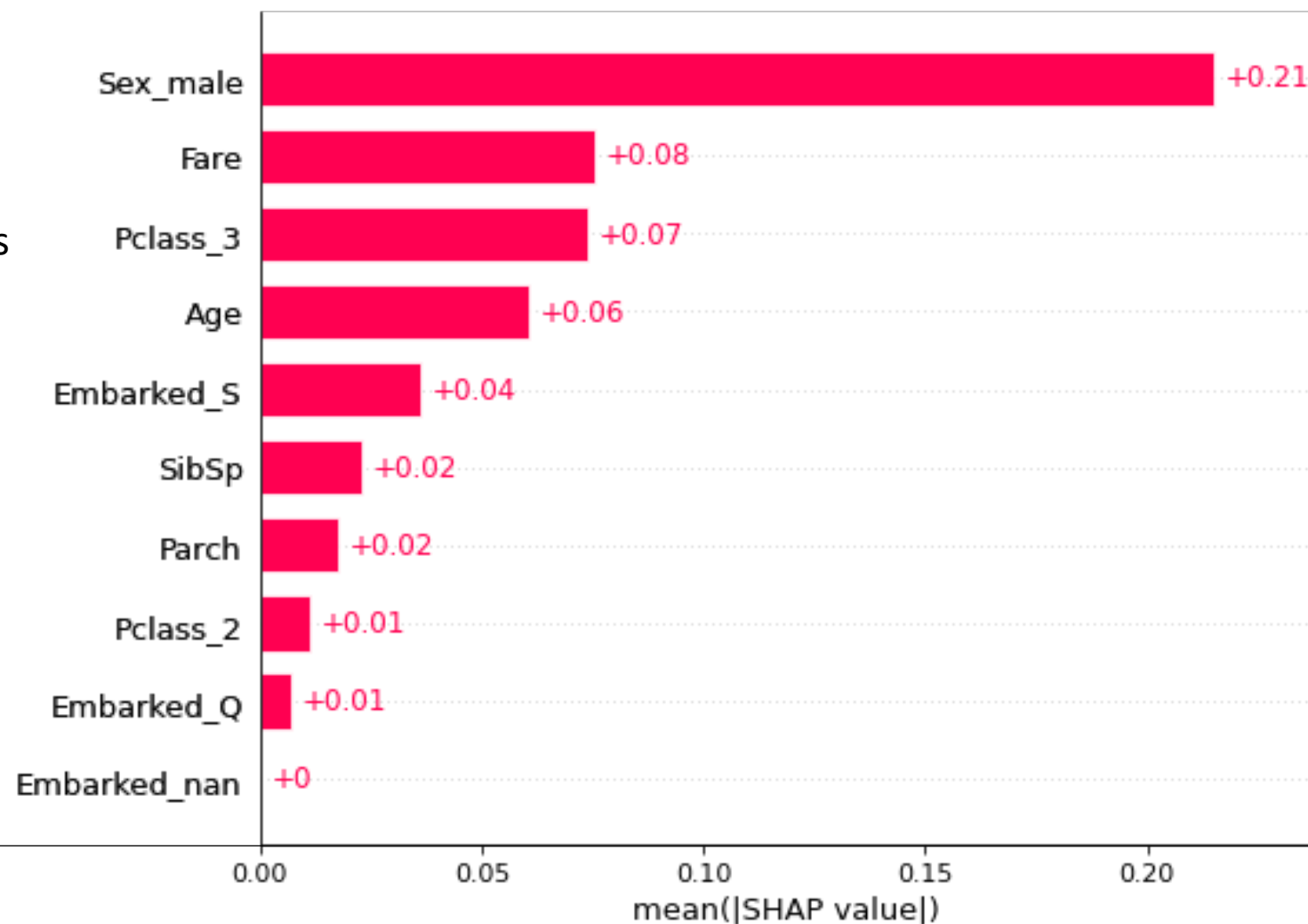
aggregating

Global

The idea behind SHAP feature importance is simple: Features with large absolute Shapley values are important. Since we want the global importance, we average the absolute Shapley values per feature  $j$  across the data:

$$I_j = \frac{1}{n} \sum_{i=1}^n |\phi_j^{(i)}|$$

Where  $n$  is the number of samples



# Feature Importance – SHAP

Model Agnostic

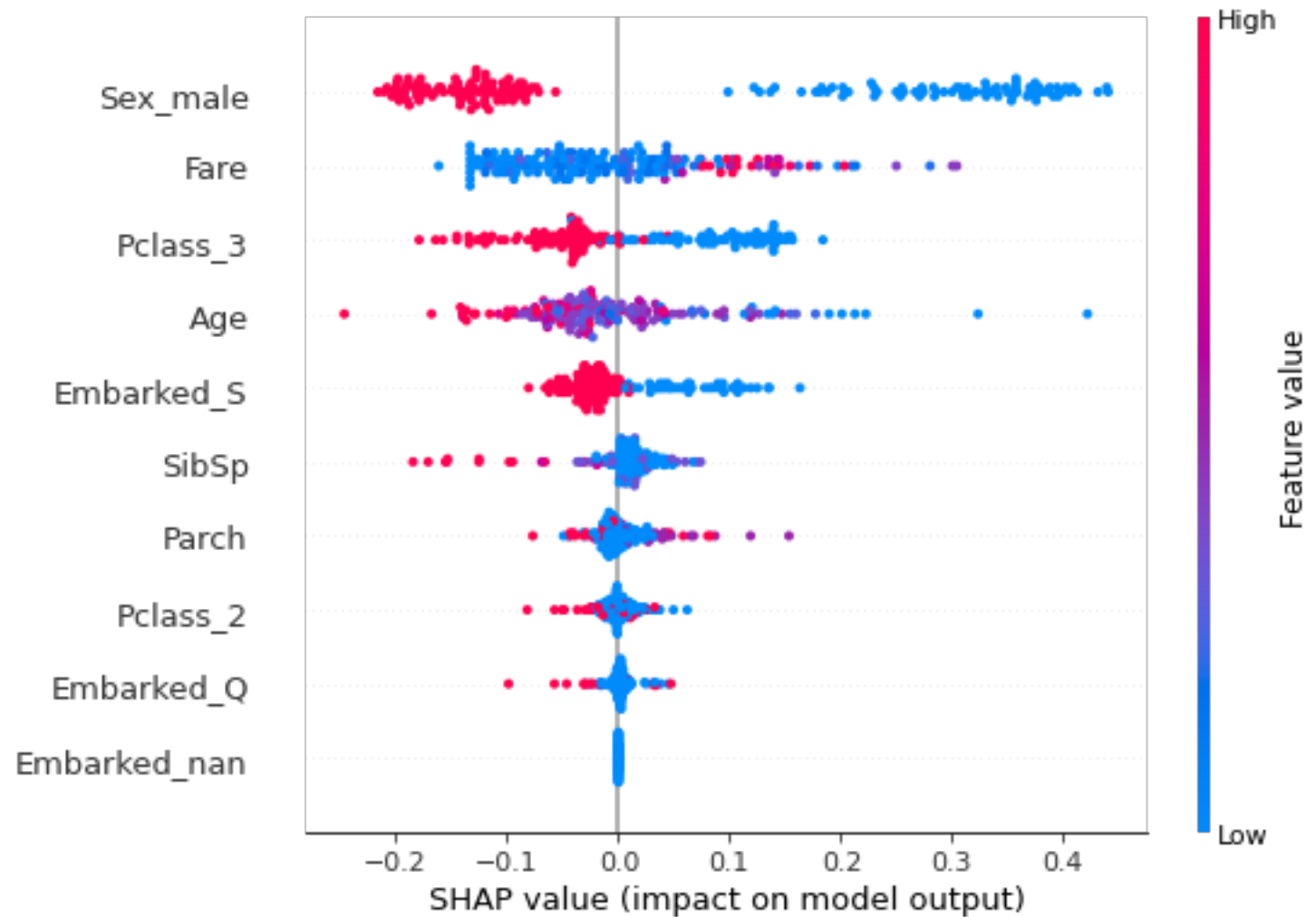
Local

aggregating

Global

## SHAP Summary Plot

The summary plot combines feature importance with feature effects.



# Feature Importance – SHAP

Model Agnostic

Local

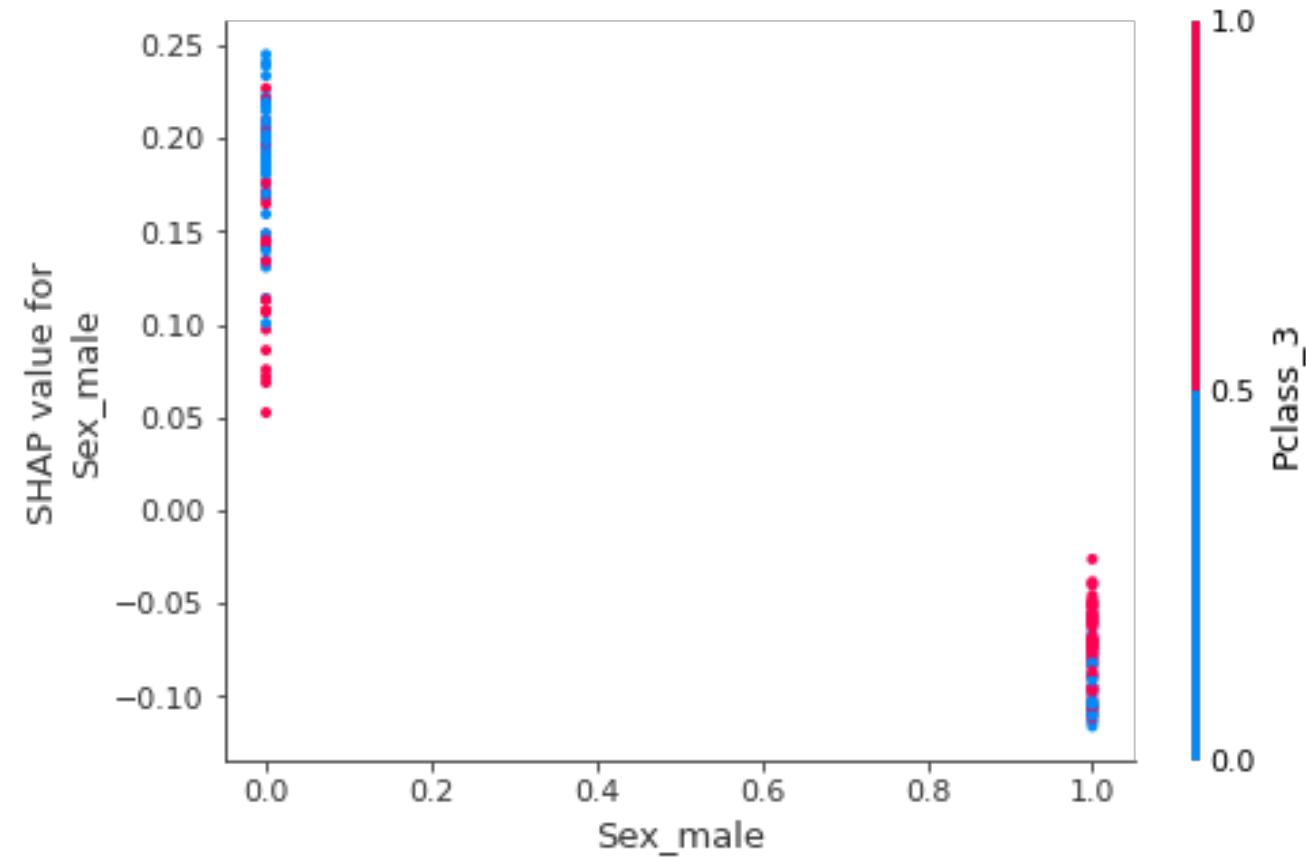
*aggregating*

Global

## SHAP – dependence plot

The dependency plot combines feature importance with feature value.

It is possible to visualize also interaction



# Feature Importance – SHAP

Model Agnostic

Local

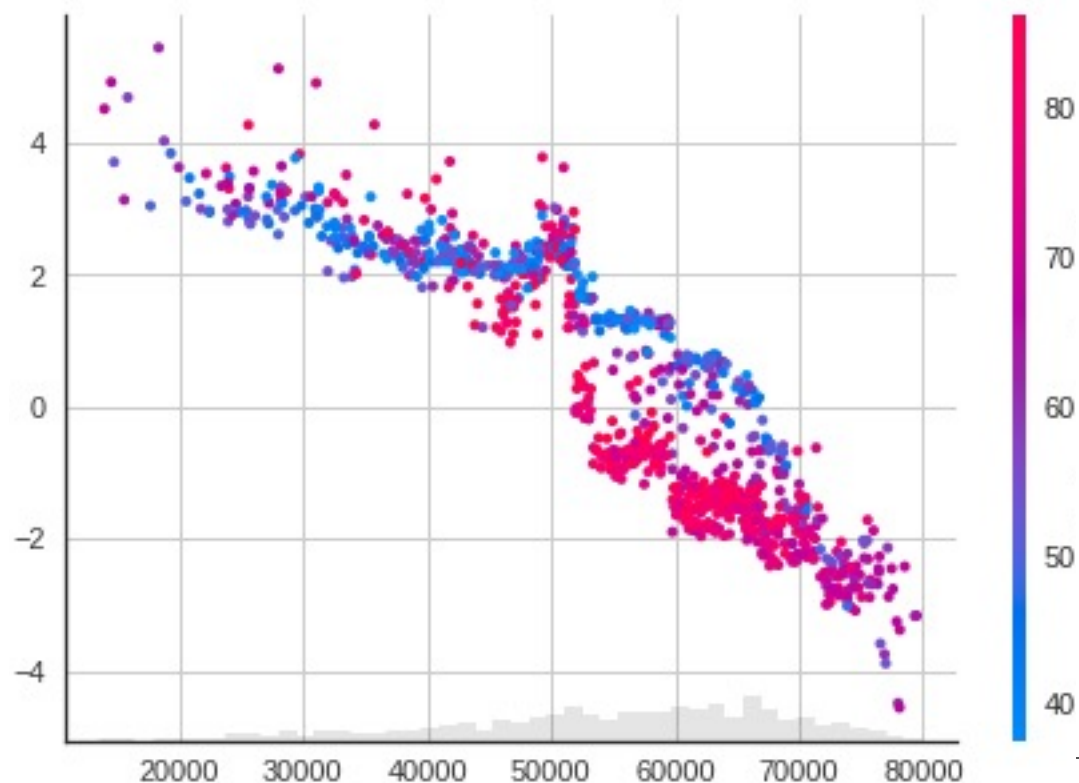
aggregating

Global

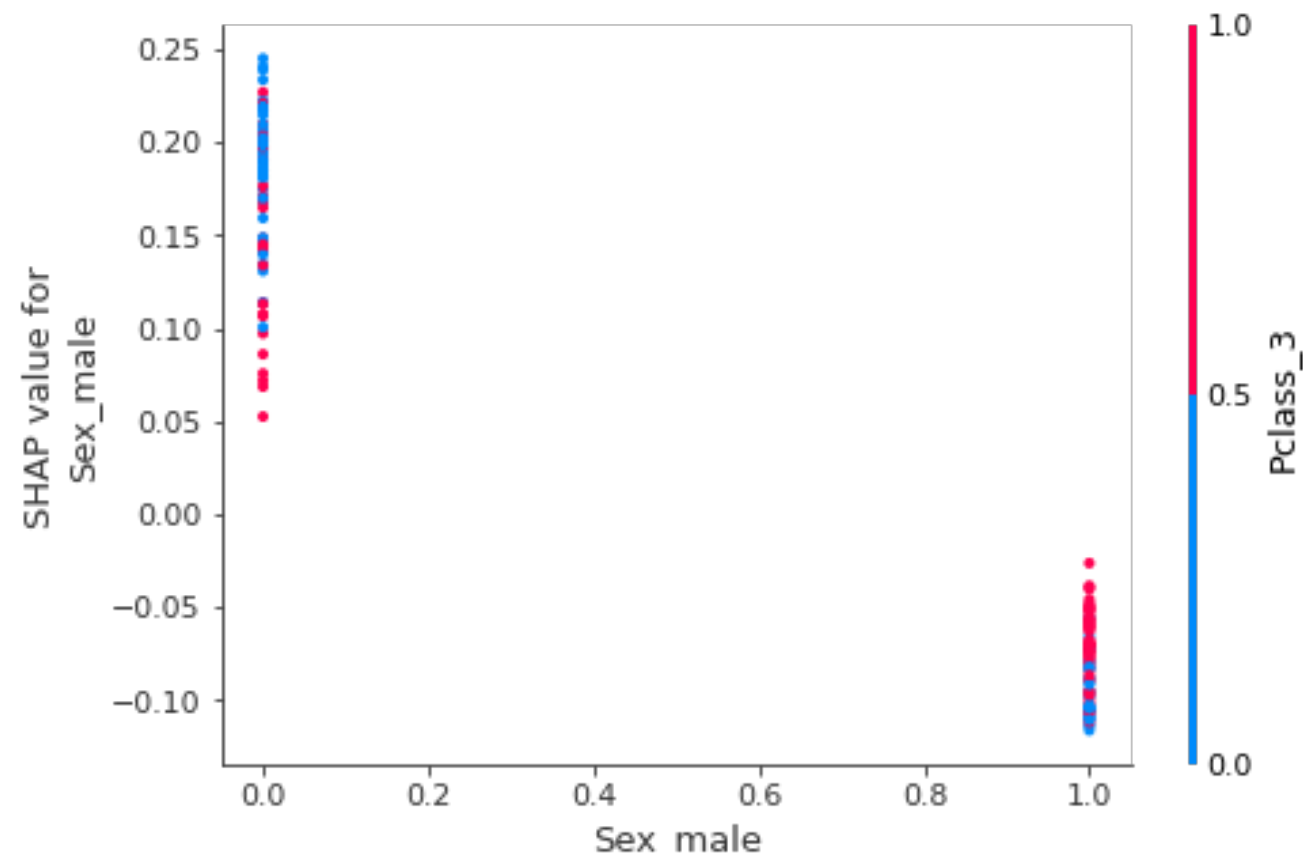
## SHAP – dependence plot

The dependency plot combines feature importance with feature value.

It is possible to visualize also interaction



CGnal



# Feature Importance – SHAP

Model Agnostic

Local

## Advantages:

- SHAP has a solid **theoretical foundation** in game theory
- SHAP **connects LIME and Shapley values**.
- SHAP has a **fast implementation for tree-based models**.

## Disadvantages:

- **KernelSHAP ignores feature dependence.**
- **TreeSHAP can produce unintuitive feature attributions.**



<https://christophm.github.io/interpretable-ml-book/>

<https://github.com/marcotcr/lime>

<https://towardsdatascience.com/shap-explained-the-way-i-wish-someone-explained-it-to-me-ab81cc69ef30>