

# 1 String Concatenation

You are given three strings  $a, b, c$  consisting of lowercase English letters. Calculate the length of the shortest string  $s$  such that all three strings  $a, b, c$  are continuous substrings of  $s$ .

## Input Format

- Three lines with strings  $a, b, c$  respectively.

## Output Format

- Output a single integer, the required length.

## Examples

### Input Example 1:

```
ab
cd
bc
```

### Output Example 1:

```
4
```

### Explanation:

One possible shortest string is "abcd", which contains "ab", "cd", and "bc" as substrings.

### Input Example 2:

```
aaa
bbb
ccc
```

### Output Example 2:

```
9
```

### Input Example 3:

```
abababab
ababab
ba
```

### Output Example 3:

```
8
```

## Data Scale

- For 30% of the test cases,  $1 \leq |a|, |b|, |c| \leq 100$
- For all test cases,  $1 \leq |a|, |b|, |c| \leq 10^5$

## 2 Robotics Signal Analysis

Imagine you are an engineer working on a next-generation robotics system. The robot uses a series of signals, represented as integers, to communicate its movements and operations. Your task is to decode these signals to identify the two signals that interact most strongly.

### Task

Your goal is to maximize the interaction strength between two signals. Interaction strength between two signals is defined as the **bitwise XOR** of their values. To achieve this, you need to:

1. Read a sequence of  $n$  signal values from the robot's system.
2. Identify the two signals that produce the highest interaction strength.

### Input Format

- The first line contains an integer  $n$ , the number of signals.
- The second line contains  $n$  integers, representing the signal values.

### Output Format

- Output the maximum interaction strength achieved between any two signals.

### Examples

#### Input Example 1:

```
4
1 2 3 4
```

#### Output Example 1:

```
7
```

#### Explanation:

The XOR of signal values 3 and 4 gives the maximum interaction strength of 7.

#### Input Example 2:

```
4
1 16 17 3
```

## Output Example 2:

19

## Explanation:

The XOR of signal values 3 and 16 gives the maximum interaction strength of 19.

## Data Scale

Let  $n$  represent the number of signal values. The constraints are as follows:

- For 40% of the data,  $1 \leq n \leq 50$ .
- For 70% of the data,  $1 \leq n \leq 1000$ .
- For 100% of the data,  $1 \leq n \leq 50000$ .

Each signal value is an integer in the range  $0 \leq \text{signal value} \leq 10^{18}$ .

## 3 Network Cable Management

Imagine you are an IT administrator tasked with managing a large-scale network. The network consists of  $n$  computers, each represented by a unique number from 1 to  $n$ . Initially, each computer is in its own isolated group.

## Task

Your job is to perform a series of operations to manage the network:

1. **Connect Operation**  $M \ i \ j$ : Connect the group containing computer  $i$  to the group containing computer  $j$ , forming a single network group. The order of computers in the group is preserved, with  $i$ 's group appearing before  $j$ 's group. It is guaranteed that  $i$  and  $j$  are in different groups.
2. **Query Operation**  $C \ i \ j$ : Check whether computer  $i$  and computer  $j$  are in the same group. If they are, output the number of computers between them in the group. If they are not, output  $-1$ .

## Input Format

- The first line contains an integer  $T$ , the total number of operations.
- Each of the next  $T$  lines contains one operation in one of the following formats:
  - $M \ i \ j$ : Connect the groups of computers  $i$  and  $j$ .
  - $C \ i \ j$ : Query whether computers  $i$  and  $j$  are in the same group.

## Output Format

- For a connect operation, output nothing.
- For a query operation, output the number of computers between  $i$  and  $j$  if they are in the same group, or  $-1$  otherwise.

## Examples

### Input Example 1:

```
4
M 2 3
C 1 2
M 2 4
C 4 2
```

### Output Example 1:

```
-1
1
```

### Explanation:

Step	Group 1	Group 2	Group 3	Group 4
Initial	1	2	3	4
M 2 3	1		3 2	4
C 1 2	Computers 1 and 2 are not in the same group. Output: -1			
M 2 4	1			4 3 2
C 4 2	Computers 4 and 2 have one computer (3) between them. Output: 1			

## Data Scale

Let  $T$  represent the total number of operations:

- For 20% of the data,  $1 \leq T \leq 100$ .
- For 30% of the data,  $1 \leq T \leq 1000$ .
- For 60% of the data,  $1 \leq T \leq 100000$ .

- For 100% of the data,  $1 \leq T \leq 500000$ .

## 4 Placing Tiles

You are given an  $n \times m$  chessboard whose rows are numbered from 0 to  $n - 1$  (top to bottom) and columns from 0 to  $m - 1$  (left to right). Each cell is either **empty** or contains an **obstacle**. A cell  $(i, j)$  is *black* if  $i + j$  is even, and *white* otherwise. You have an infinite supply of  $L$ -shaped tiles. The tile occupies exactly three cells: one “corner” cell and the two orthogonally adjacent cells. Note that the corner cell of each  $L$ -shaped tile must be placed on a black cell of the chessboard.

A placement of tiles is valid if:

- Tiles do not overlap.
- Tiles do not cover obstacle cells.
- The corner of every tile lies on a **black** cell; consequently, each tile covers one black cell and its two adjacent white cells.

Your task is to compute the **maximum number of tiles** that can be placed on the board.

### Input Format

- The first line contains two integers  $n$  and  $m$  ( $1 \leq n, m \leq 50$ ).
- The next  $n$  lines describe the board, each containing a string of length  $m$  consisting of ‘.’ (empty) and ‘X’ (obstacle).

### Output Format

Output a single integer: the maximum number of tiles that can be placed.

### Examples

#### Example 1

```
4 4
....
X..X
....
..X.
```

#### Output 1:

```
2
```

### Example 2

3 3

...  
...  
...

### Output 2:

2

### Example 3

5 6

X..X..

.....  
.....X  
...X..  
.....

### Output 3:

6

### Data Scale

- For 20% of the test cases,  $1 \leq n, m \leq 10$
- For 40% of the test cases,  $1 \leq n, m \leq 20$
- For all test cases,  $1 \leq n, m \leq 50$