Winter Domain Camp Day 2

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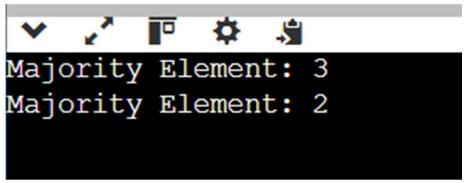
Semester: 5th Date of Performance: 20th December, 2024

Problem 1: Majority Elements

Given an array nums of size n, return the majority element. The majority element is the element that appears more than $\lfloor n/2 \rfloor$ times. You may assume that the majority element always exists in the array.

```
Solution:
    #include <iostream>
    #include <vector>
    int majorityElement(const std::vector<int>& nums)
      int candidate = 0, count = 0;
                                        // Phase 1: Find
                  for (int num : nums) {
the candidate
                                              if (count
== 0) {
               candidate = num;
                                        count = 1;
     } else if (num == candidate) {
              } else {
count++:
count--:
  // Phase 2: Verify the candidate (Optional since problem guarantees majority
                          for (int num : nums) {
                                                   if (num == candidate) {
            count = 0:
element)
count++;
  if (count > nums.size() / 2) {
return candidate;
  }
  throw std::runtime error("No majority element found.");
}
```

```
int main() {    std::vector<int> nums = {2, 2,
1, 1, 1, 2, 2};    try {
        std::cout << "Majority Element: " << majorityElement(nums) << std::endl;
        } catch (const std::exception& e) {
        std::cerr << e.what() << std::endl;
        }
        return 0;
    }
    Output:</pre>
```

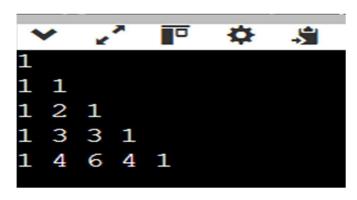


Problem 2: Pascal's Triangle

Given an integer numRows, return the first numRows of Pascal's triangle. In Pascal's triangle, each number is the sum of the two numbers directly above it

```
Solution:
```

```
#include <iostream>
#include <vector>
std::vector<std::vector<int>> generate(int numRows) {
std::vector<std::vector<int>> triangle(numRows);
(int i = 0; i < numRows; ++i) {
                                 triangle[i].resize(i +
         for (int j = 1; j < i; ++j) {
                                          triangle[i][j]
= triangle[i - 1][j - 1] + triangle[i - 1][j];
     }} return triangle;} int main() {
numRows = 5; // Example input
                                  auto result =
generate(numRows);
                      for (const auto& row:
             for (int num : row) std::cout <<
result) {
num << " ":
                 std::cout << "\n";} return
0;}
Output:
```



Problem 3: Single Number

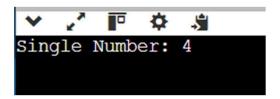
Given a non-empty array of integers nums, every element appears twice except for one. Find that single one. You must implement a solution with a linear runtime complexity and use only constant extra space.

```
Solution:
```

```
#include <iostream>
#include <vector>

int singleNumber(const std::vector<int>& nums)
{    int result = 0;    for (int num : nums) {
    result ^= num;
    }       return
    result; }

int main() {       std::vector<int> nums = {4, 1, 2, 1, 2}; // Example input
    std::cout << "Single Number: " << singleNumber(nums) << std::endl;
    return 0;
}
Output:</pre>
```



Problem 4: Merge Two Sorted Lists

You are given the heads of two sorted linked lists list1 and list2. Merge the two lists into one sorted list. The list should be made by splicing together the nodes of the first two lists. Return the head of the merged linked list.

```
Solution:
#include <iostream>
struct ListNode {
  int val;
  ListNode* next;
  ListNode(int x) : val(x), next(nullptr) {}
};
ListNode* mergeTwoLists(ListNode* list1, ListNode* list2) {
if (!list1) return list2; if (!list2) return list1; if (list1->val
                   list1->next = mergeTwoLists(list1->next,
< list2->val) {
           return list1;
list2);
  } else {
    list2->next = mergeTwoLists(list1, list2->next);
return list2;
  }
void printList(ListNode* head) {
while (head) {
                   std::cout <<
head->val << " ";
                      head =
head->next;
  }
}
int main() {
  ListNode* list1 = new ListNode(1);
>next = new ListNode(2);
                            list1->next->next=
new ListNode(4);
  ListNode* list2 = new ListNode(1);
                                         list2-
>next = new ListNode(3); list2->next->next =
new ListNode(4);
```

```
ListNode* mergedList = mergeTwoLists(list1, list2);
printList(mergedList);
return 0;
}
```



Problem 5: Linked List Cycle.

Given head, the head of a linked list, determine if the linked list has a cycle in it. There is a cycle in a linked list if there is some node in the list that can be reached again by continuously following the next pointer. Internally, pos is used to denote the index of the node that tail's next pointer is connected to. Note that pos is not passed as a parameter. Return true if there is a cycle in the linked list. Otherwise, return false.

```
Solution:
#include <iostream>

struct ListNode {
   int val;
   ListNode* next;
   ListNode(int x) : val(x), next(nullptr) {}
};

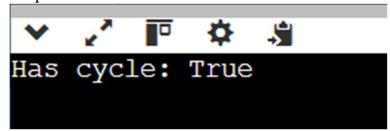
bool hasCycle(ListNode* head) {
   if (!head) return false;
   ListNode *slow = head, *fast = head;
```

```
while (fast && fast->next) {
    slow = slow -> next;
                               // Move slow pointer by 1 step
fast = fast->next->next;
                           // Move fast pointer by 2 steps
    if (slow == fast) 
                             // Cycle
                return true;}}
                                return false;
detected
// No cycle} int main() {
  // Example 1: Creating a cycle in the list ListNode* head = new
ListNode(3);
               head->next = new ListNode(2);
                                                 head->next->next = new
ListNode(0);
               head->next->next->next = new ListNode(-4);
>next->next->next->next = head->next; // Cycle starts at node with value
2
```

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```
std::cout << "Has cycle: " << (hasCycle(head) ? "True" : "False") << std::endl;
return 0;
}</pre>
```

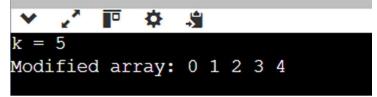
Output:



Problem 6: Remove Element

Given an integer array nums sorted in non-decreasing order, remove the duplicates in-place such that each unique element appears only once. The relative order of the elements should be kept the same. Then return the number of unique elements in nums. Consider the number of unique elements of nums to be k, to get accepted, you need to do the following things: Change the array nums such that the first k elements of nums contain the unique elements in the order they were present in nums initially. The remaining elements of nums are not important as well as the size of nums. Return k.

```
Solution:
#include <iostream>
#include <vector>
int removeDuplicates(std::vector<int>& nums) {
  if (nums.empty()) return 0;
  int k = 1; // Pointer for the next unique element
                                                     for (int i = 1; i <
nums.size(); ++i) {
                        if (nums[i] != nums[i - 1]) {
                                                             nums[k++]
= nums[i]; // Move the unique element to the front}}
                                                        return k; //
Number of unique elements} int main() {
                                            std::vector<int> nums =
\{0,0,1,1,1,2,2,3,3,4\}; int k = removeDuplicates(nums);
  std::cout << "k = " << k << std::endl;
std::cout << "Modified array: ";
(int i = 0; i < k; ++i) {
    std::cout << nums[i] << " ";
  std::cout << std::endl;
  return 0;}
Output:
```



Problem 7: Baseball Game:

You are keeping the scores for a baseball game with strange rules. At the beginning of the game, you start with an empty record. You are given a list of strings operations, where operations[i] is the ith operation you must apply to the record and is one of the following: An integer x. Record a new score of x. '+'. Record a new score that is the sum of the previous two scores. 'D'. Record a new score that is the double of the previous score. 'C'. Invalidate the previous score, removing it from the record. Return the sum of all the scores on the record after applying all the operations. The test cases are generated such that the answer and all intermediate calculations fit in a 32-bit integer and that all operations are valid.

```
Solution:
#include <iostream>
#include <vector>
#include <string>
int calPoints(std::vector<std::string>& ops) {
std::vector<int> record;
                           for (const auto&
op : ops) {
     if (op == "C") {
                             record.pop back(); //
Remove the last score
     \} else if (op == "D") {
       record.push back(2 * record.back()); // Double the last score
     } else if (op == "+") {
       record.push back(record[record.size() - 1] + record[record.size() - 2]); //
Sum of last two scores
     } else {
       record.push back(std::stoi(op)); // Add the integer score
  }
  int total = 0;
                  for (int
score : record) {
                      total
+= score;
  return total;
```

```
int main() {
   std::vector<std::string> ops = {"5","2","C","D","+"};
   std::cout << "Total score: " << calPoints(ops) << std::endl; // Output: 30
return 0; }Output:</pre>
```



Problem 8: Container With Most Water

You are given an integer array height of length n. There are n vertical lines drawn such that the two endpoints of the ith line are (i, 0) and (i, height[i]). Find two lines that together with the x-axis form a container, such that the container contains the most water. Return the maximum amount of water a container can store.

```
Solution:
#include <iostream>
#include <vector>

int maxArea(std::vector<int>& height) {
    int left = 0, right = height.size() - 1, maxArea = 0;
    while (left < right) {
    int width = right - left;
        int h = std::min(height[left], height[right]);
        maxArea = std::max(maxArea, width * h);

    if (height[left] < height[right]) {
        ++left;
    } else {
        --right;
    }
}</pre>
```



Problem 9: Jump Game II

You are given a 0-indexed array of integers nums of length n. You are initially positioned at nums[0]. Each element nums[i] represents the maximum length of a forward jump from index i. In other words, if you are at nums[i], you can jump to any nums[i+j] where: $0 \le j \le n$ nums[i] and $i+j \le n$ Return the minimum number of jumps to reach nums[n - 1]. The test cases are generated such that you can reach nums[n - 1].

```
Solution:
```

Problem 10: Design Circular Queue

Calculate the sum of the digits of a given number n. For example, for the number 12345, the sum of the digits is 1+2+3+4+5=15. To solve this, you will need to extract each digit from the number and calculate the total sum.

```
Solution:
#include <iostream>
#include <vector> class
MyCircularQueue {
private:
    std::vector<int> queue;
int front, rear, size, capacity;
public:
```

```
MyCircularQueue(int k): queue(k), front(-1), rear(-1), size(0), capacity(k) {}
bool enQueue(int value) {
                               if (size == capacity) return false;
== 0) front = 0;
                     rear = (rear + 1) % capacity;
                                                       queue[rear] = value;
     size++:
return true;}
bool deQueue() {
if (size == 0)
return false;
if (front == rear)
front = rear = -1;
     else front = (front + 1) % capacity;
                                             size--:
return true;}
               int Front() {
                                 return size == 0 ? -1 :
queue[front];}
                 int Rear() {
                                   return size == 0 ? -1 :
queue[rear];}
                bool isEmpty() {
                                       return size ==
0;} bool isFull() {
                          return size == capacity;}}; int
           MyCircularQueue q(3);
                                      std::cout <<
main() {
q.enQueue(1) << std::endl; // True
                                      std::cout <<
q.enQueue(2) << std::endl; // True
                                      std::cout <<
q.enQueue(3) << std::endl; // True
                                      std::cout <<
q.enQueue(4) << std::endl; // False (full)
                                            std::cout
<< q.Rear() << std::endl;
                            // 3
                                   std::cout <<
q.isFull() << std::endl; // True
                                   std::cout <<
q.deQueue() << std::endl; // True
                                     std::cout <<
q.enOueue(4) << std::endl; // True
                                      std::cout <<
q.Rear() << std::endl;
  return 0;}
Output:
```

Problem 11: Cherry Pickup II

You are given a rows x cols matrix grid representing a field of cherries where grid[i][j] represents the number of cherries that you can collect from the (i, j) cell. You have two robots that can collect cherries for you: Robot #1 is located at the top-left corner (0, 0), and Robot #2 is located at the top-right corner (0, cols - 1). Return the maximum number of cherries collection using both robots by following the rules below: From a cell (i, j), robots can move to cell (i + 1, j - 1), (i + 1, j), or (i + 1, j + 1). When any robot passes through a cell, It picks up all cherries, and the cell becomes an empty cell. When both robots stay in the same cell, only one takes the cherries. Both robots cannot move outside of the grid at any moment. Both robots should reach the bottom row in grid.

Solution:

```
#include <iostream> #include
<vector>
using namespace std;

class Solution { public:
    int cherryPickup(vector<vector<int>>& grid) {        int rows =
        grid.size(), cols = grid[0].size();        vector<vector<int>>>
        dp(rows, vector<vector<int>>(cols, vector<int>(cols, -1)));        return
    dfs(0, 0, cols - 1, grid, dp);
    }

private:
    int dfs(int row, int col1, int col2, vector<vector<int>>& grid,
    vector<vector<vector<int>>>& dp) {
        int rows = grid.size(), cols = grid[0].size();
        if (col1 < 0 || col2 < 0 || col1 >= cols || col2 >= cols) return 0;
    if (dp[row][col1][col2]!= -1) return dp[row][col1][col2];
```

```
int cherries = grid[row][col1];
                                         if (col1
!= col2) cherries += grid[row][col2];
                                           if (row
< rows - 1) {
                     int \maxCherries = 0;
       for (int d1 = -1; d1 \le 1; d1++) {
          for (int d2 = -1; d2 \le 1; d2++) {
                                                                   maxCherries =
max(maxCherries, dfs(row + 1, col1 + d1, col2 + d2, grid, dp));
       cherries += maxCherries;
    return dp[row][col1][col2] = cherries;
};
int main() {
Solution sol;
  vector<vector<int>> grid1 = {{3,1,1},{2,5,1},{1,5,5},{2,1,1}};
cout << sol.cherryPickup(grid1) << endl; // Output: 24
  vector<vector<int>> grid2 =
\{\{1,0,0,0,0,0,1\},\{2,0,0,0,0,3,0\},\{2,0,9,0,0,0,0\},\{0,3,0,5,4,0,0\},\{1,0,2,3,0,0,6\}\}\};
cout << sol.cherryPickup(grid2) << endl; // Output: 28 return 0;
```



Problem 12: Maximum Number of Darts Inside of a Circular Dartboard

Alice is throwing n darts on a very large wall. You are given an array darts where darts[i] = [xi, yi] is the position of the ith dart that Alice threw on the wall. Bob knows the positions of the n darts on the wall. He wants to place a dartboard of

radius r on the wall so that the maximum number of darts that Alice throws lie on the dartboard. Given the integer r, return the maximum number of darts that can lie on the dartboard.

```
Solution:
#include <iostream>
#include <vector> #include
<cmath>
using namespace std;
class Solution { public:
  int numPoints(vector<vector<int>>& darts, int r) {
    int maxCount = 1, n = darts.size();
                                             for (int i = 0; i < n; ++i) {
for (int j = i + 1; j < n; ++j) { double dx = darts[j][0] -
darts[i][0], dy = darts[i][1] - darts[i][1];
                                                  double dist = sqrt(dx *
dx + dy * dy;
         if (dist > 2 * r) continue;
                                             double midX = (darts[i][0] +
darts[i][0] / 2.0, midY = (darts[i][1] + darts[i][1]) / 2.0;
                                                                   double angle
=  sqrt(r * r - (dist / 2) * (dist / 2)), norm = dist ? r / dist :
0;
         maxCount = max(maxCount, count(darts, midX - norm * dy, midY +
norm * dx, r);
    return maxCount;
private:
  int count(const vector<vector<int>>& darts, double cx, double cy, int r) {
int c = 0;
    for (auto& dart : darts)
                                   if (pow(dart[0] - cx, 2) + pow(dart[1]
-cy, 2) \le r * r + 1e-7) ++c;
                                  return c;
};
int main() {
Solution sol;
```

vector<vector<int>> darts = {{-2, 0}, {2, 0}, {0, 2}, {0, -2}}; cout << sol.numPoints(darts, 2) << endl; // Output: 4 }



Problem 13: Design Skiplist

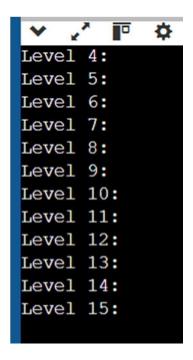
Design a Skiplist without using any built-in libraries. A skiplist is a data structure that takes O(log(n)) time to add, erase and search. Comparing with treap and redblack tree which has the same function and performance, the code length of Skiplist can be comparatively short and the idea behind Skiplists is just simple linked lists.

```
Solution:
#include <iostream>
#include <cstdlib>
#include <ctime>
#include <vector>
using namespace std;
// Node structure for Skiplist struct Node {
vector<Node*> forward; // Pointers to next nodes at each level
  Node(int value, int level) : value(value), forward(level, nullptr) {} };
// Skiplist class class
Skiplist { private:
  int maxLevel;
                      // Maximum level for the skiplist float probability;
// Probability of promoting a node to a higher level Node* header;
Header node
  // Random level generator function
                          int level =
int randomLevel() {
1;
```

```
while ((rand() \% 2) < probability \&\& level < maxLevel) {
       level++;
    return level;
public:
  Skiplist(int maxLevel = 16, float probability = 0.5)
: maxLevel(maxLevel), probability(probability) {
    header = new Node(-1, maxLevel); // Header node with a dummy value
  }
  // Search for a value in the Skiplist
bool search(int target) {
                             Node*
current = header;
     for (int i = \max Level - 1; i \ge 0; --i) { while (current->forward[i])
!= nullptr && current->forward[i]->value < target) {
                                                               current =
current->forward[i];
    current = current->forward[0];
                                        return (current !=
nullptr && current->value == target);
  }
  // Insert a value into the Skiplist
                                            void
insert(int value) {
                                vector<Node*>
update(maxLevel, nullptr);
    Node* current = header;
     for (int i = maxLevel - 1; i \ge 0; --i) { while (current->forward[i]
!= nullptr && current->forward[i]->value < value) {
                                                               current =
current->forward[i];
       update[i] = current;
     }
     current = current->forward[0];
                                         if (current
== nullptr || current->value != value) {
                                              int
level = randomLevel();
```

```
Node* newNode = new Node(value, level);
       for (int i = 0; i < level; ++i) {
                                              newNode-
>forward[i] = update[i]->forward[i];
                                              update[i]-
>forward[i] = newNode;
  }
  // Erase a value from the Skiplist
erase(int value) {
                                vector<Node*>
update(maxLevel, nullptr);
    Node* current = header;
     for (int i = maxLevel - 1; i \ge 0; --i) { while (current->forward[i]
!= nullptr && current->forward[i]->value < value) {
                                                              current =
current->forward[i];
       }
       update[i] = current;
     current = current->forward[0];
                                        if (current !=
nullptr && current->value == value) {
                                              for (int i =
0; i < maxLevel; ++i) {
                                 if (update[i]-
>forward[i] != current) break;
                                        update[i]-
>forward[i] = current->forward[i];
       delete current;
  }
  // Print the Skiplist
void print() {
     for (int i = 0; i < maxLevel; ++i) {
Node* current = header->forward[i];
cout << "Level " << i << ": ";
                                     while
(current != nullptr) {
                               cout <<
current->value << " ";
         current = current->forward[i];
```

```
cout << endl;
};
               srand(time(0)); // Seed for random
int main() {
level generation
  Skiplist skiplist;
  // Insert values into the Skiplist
                      skiplist.insert(40);
skiplist.insert(30);
skiplist.insert(50);
                      skiplist.insert(60);
skiplist.insert(70);
                      skiplist.insert(90);
  // Print the Skiplist
  cout << "Skiplist after insertions:" << endl;</pre>
skiplist.print();
  // Insert additional values
                      skiplist.insert(45);
skiplist.insert(80);
  cout << "Skiplist after adding 80 and 45:" << endl;
skiplist.print();
  // Search for some values
  cout << "Searching for 45: " << (skiplist.search(45)? "Found": "Not Found")
<< endl;
  cout << "Searching for 100: " << (skiplist.search(100)? "Found": "Not
Found") << endl;
                     skiplist.erase(50);
  // Erase a value
<< "Skiplist after removing 50:" << endl;</pre>
skiplist.print();
  return 0;
}Ouput:
```



Problem 14: All O'one Data Structure

Design a data structure to store the strings' count with the ability to return the strings with minimum and maximum counts. Implement the AllOne class: • AllOne() Initializes the object of the data structure. • inc(String key) Increments the count of the string key by 1. If key does not exist in the data structure, insert it with count 1. • dec(String key) Decrements the count of the string key by 1. If the count of key is 0 after the decrement, remove it from the data structure. It is guaranteed that key exists in the data structure before the decrement. • getMaxKey() Returns one of the keys with the maximal count. If no element exists, return an empty string "". • getMinKey() Returns one of the keys with the minimum count. If no element exists, return an empty string "".

Solution:

#include <iostream>
#include <unordered_map>
#include <string>
#include <list>
#include <map> using
namespace std; class
AllOne { private:

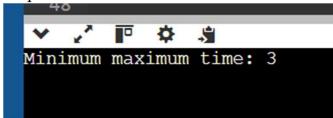
```
// Hash map to store the count of each key
unordered map<string, int> keyCount;
  // Map to store the strings by their counts, ordered by counts
map<int, list<string>> countKeys; public:
  AllOne() {}
  // Increment the count of a string by 1
void inc(string key) {
                          int count =
keyCount[key];
    // Remove the key from its old count list
    if (count > 0) {
       countKeys[count].remove(key);
if (countKeys[count].empty()) {
countKeys.erase(count);}}
    // Increment the count and add the key to the new count list
keyCount[key] = count + 1;
                                countKeys[count +
1].push back(key);} // Decrement the count of a string by 1
void dec(string key) {
                           int count = keyCount[key];
    // Remove the key from its current count list
countKeys[count].remove(key);
(countKeys[count].empty()) {
countKeys.erase(count); }
    // If count becomes 0, remove the key from keyCount
if (count == 1) {
                       keyCount.erase(key);
     } else {
       keyCount[key] = count - 1;
       countKeys[count - 1].push back(key);}}
// Get the key with the maximum count
                                         string
getMaxKey() {
    if (countKeys.empty()) return "";
                                          //
Get the last element (maximum count)
    return countKeys.rbegin()->second.front();
  }
  // Get the key with the minimum count
string getMinKey() {
    if (countKeys.empty()) return "";
                                          //
Get the first element (minimum count)
    return countKeys.begin()->second.front();
```

```
};
int main() {
  AllOne allOne;
  allOne.inc("hello");
                      allOne.inc("hello");
                                           cout << "Max
Key: " << allOne.getMaxKey() << endl; // "hello"
                                                cout << "Min
Key: " << allOne.getMinKey() << endl; // "hello"</pre>
  allOne.inc("leet");
  cout << "Max Key: " << allOne.getMaxKey() << endl; // "hello"</pre>
cout << "Min Key: " << allOne.getMinKey() << endl; // "leet"</pre>
  allOne.dec("hello"); cout << "Max Key: " <<
allOne.getMaxKey() << endl; // "hello"
                                       cout << "Min Key: " <<
allOne.getMinKey() << endl; // "leet"
  allOne.dec("leet");
                     cout << "Max Key: " <<
allOne.getMaxKey() << endl; // "hello"
                                       cout << "Min Key: " <<
allOne.getMinKey() << endl; // "hello"
  return 0;
Output:
    ∨ ,^ □
                   Ö
  Max Key: hello
  Min Key: hello
  Max Key: hello
  Min Key: leet
  Max Key: leet
  Min Key: leet
  Max Key: hello
  Min Key: hello
```

Problem 15: Find Minimum Time to Finish All Jobs

You are given an integer array jobs, where jobs[i] is the amount of time it takes to complete the ith job. There are k workers that you can assign jobs to. Each job should be assigned to exactly one worker. The working time of a worker is the sum of the time it takes to complete all jobs assigned to them. Your goal is to devise an optimal assignment such that the maximum working time of any worker is minimized. Return the minimum possible maximum working time of any assignment.

```
Solution:
#include <iostream>
#include <vector>
#include <numeric>
#include <algorithm>
using namespace std;
// Helper function to check if we can distribute jobs with max workload <= mid
bool canAssignJobs(const vector<int>& jobs, int k, int mid) {
currentSum = 0;
                   int workersUsed = 1; // Start with one worker
  for (int job : jobs) {
     if (currentSum + job > mid) {
       // Need a new worker since current worker cannot take this job
workersUsed++:
                                                  if (workersUsed >
                        currentSum = job;
k) return false; // More workers than allowed
     } else {
       currentSum += job;
  return true;
int minimumTimeRequired(vector<int>& jobs, int k) {
                                                         int left =
*max element(jobs.begin(), jobs.end()); // Max job time
                                                           int right =
accumulate(jobs.begin(), jobs.end(), 0); // Sum of all jobs
```



Problem 16: Minimum Number of People to Teach:

On a social network consisting of m users and some friendships between users, two users can communicate with each other if they know a common language. You are given an integer n, an array languages, and an array friendships where: There are n languages numbered 1 through n, languages[i] is the set of languages the ith user knows, and friendships[i] = [ui, vi] denotes a friendship between the users ui and vi. You can choose one language and teach it to some users so that all friends can communicate with each other. Return the minimum number of users you need to teach. Note that friendships are not transitive, meaning if x is a friend of y and y is a friend of z, this doesn't guarantee that x is a friend of z.

Solution:

```
#include <iostream>
#include <vector>
#include <unordered set>
#include <unordered map>
using namespace std;
class UnionFind { public:
  UnionFind(int n) {
parent.resize(n);
                     size.resize(n, 1);
for (int i = 0; i < n; ++i) parent[i] = i;
  }
  int find(int u) { if (parent[u] != u) {
parent[u] = find(parent[u]); // Path compression
    return parent[u];
  }
  void unionSets(int u, int v) {
                                    int rootU = find(u);
                    if (rootU != rootV) {
int rootV = find(v);
(size[rootU] < size[rootV]) swap(rootU, rootV);
parent[rootV] = rootU;
       size[rootU] += size[rootV];
  }
private:
  vector<int> parent;
vector<int> size;
};
```

```
int minimumTeachings(int n, vector<vector<int>>& languages,
vector<vector<int>>& friendships) {
                                        int m =
languages.size(); // Number of users
  // Step 1: Union-Find initialization for users
  UnionFind uf(m);
  // Step 2: Union users who share a common language
  unordered map<int, vector<int>> languageUsers;
  for (int i = 0; i < m; ++i) {
                                  for (int
lang : languages[i]) {
languageUsers[lang].push back(i);
  }
  // Union users based on shared languages
for (auto& [lang, users] : languageUsers) {
for (int i = 0; i < users.size(); ++i) {
for (int i = i + 1; i < users.size(); ++i) {
          uf.unionSets(users[i], users[j]);
     }
  }
  // Step 3: Union users based on friendships
for (auto& friendship: friendships) {
     int u = friendship[0] - 1;
int v = friendship[1] - 1;
                              if
(uf.find(u) != uf.find(v)) {
       uf.unionSets(u, v);
     }
  }
  // Step 4: Find the connected components and check if they can communicate
unordered map<int, unordered set<int>> components;
                                                           for (int i = 0; i < m;
                                     for (int lang : languages[i]) {
            int root = uf.find(i);
++i) {
       components[root].insert(lang);
     }
```

```
}
        // Step 5: Determine how many users need to be taught a new language
int result = 0;
         for (auto& [component, langs] : components) {
                 // If no language is shared among users in this component, we need to teach
at least one user
                                                                                if (langs.empty()) {
                                                                                                                                                                                      result++;
         return result;
int main()  { vector < vector < int >> languages 1 = {{1}, {2}, }
\{1, 2\}\}; vector<vector<int>> friendships1 = \{\{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2\}, \{1, 2
3}, {2, 3}};
                                                      int n1 = 2;
         cout << "Minimum number of users to teach: " << minimumTeachings(n1,
languages1, friendships1) << endl;
        vector<vector<int>> languages2 = \{\{2\}, \{1, 3\}, \{1, 2\}, \{3\}\};
vector<vector<int>> friendships2 = {{1, 4}, {1, 2}, {3, 4}, {2, 3}};
int n2 = 3;
         cout << "Minimum number of users to teach: " << minimumTeachings(n2,
languages2, friendships2) << endl;
         return 0;
Output:
            Output
   Minimum number of users to teach: 0
    Minimum number of users to teach: 0
```

Problem 17: Count Ways to Make Array With Product

You are given a 2D integer array, queries. For each queries[i], where queries[i] = [ni, ki], find the number of different ways you can place positive integers into an array of size ni such that the product of the integers is ki. As the number of ways may be too large, the answer to the ith query is the number of ways modulo 109 + 7. Return an integer array answer where answer.length == queries.length, and answer[i] is the answer to the ith query.

```
Solution:
#include <iostream>
#include <vector>
#include <cmath>
const int MOD = 1e9 + 7;
const int MAXN = 10000;
// Precompute factorials and modular inverses using Fermat's Little Theorem
std::vector<long long> factorial(MAXN + 1), inv factorial(MAXN + 1);
// Function to compute x^y % MOD
long long mod exp(long long x, long long y, long long mod) {
long long result = 1; while (y > 0) { if (y \% 2 == 1)
result = (result * x) % mod; x = (x * x) \% mod;
    y /= 2;
  return result;
}
// Function to precompute factorials and their inverses void
precompute() {
  factorial[0] = inv factorial[0] = 1;
for (int i = 1; i \le MAXN; ++i) {
```

```
factorial[i] = (factorial[i - 1] * i) % MOD;
  inv factorial[MAXN] = mod exp(factorial[MAXN], MOD - 2, MOD); //
Using Fermat's little theorem for (int i = MAXN - 1; i \ge 1; --i) {
inv factorial[i] = (inv factorial[i + 1] * (i + 1)) % MOD;
}
// Function to compute binomial coefficient C(n, k) % MOD
long long binomial(int n, int k) { if (k > n || k < 0) return 0;
(factorial[n] * inv factorial[k] % MOD) * inv factorial[n - k] % MOD; }
// Function to get the prime factorization of a number
std::vector<std::pair<int, int>> prime factors(int k) {
std::vector<std::pair<int, int>> factors;
                                          for (int i =
2; i * i \le k; ++i) {
                        if (k \% i == 0) {
                  while (k \% i == 0)  {
count = 0;
                                                 k =
i;
            count++;
       factors.push back({i, count});
                   if (k > 1) {
factors.push back({k, 1});
  return factors;
}
// Function to solve each query
long long solve(int n, int k) {
// Prime factorize k
  auto factors = prime factors(k);
  long long result = 1;
                          for (const
auto& factor : factors) {
                              int
prime = factor.first;
                         int
exponent = factor.second;
    // Calculate number of ways to split exponent of this prime into n parts
result = (result * binomial(exponent + n - 1, n - 1)) % MOD;
  }
```

```
return result;
}
std::vector<int> waysToPlaceIntegers(std::vector<std::vector<int>>& queries) {
precompute(); // Precompute factorials and inverses std::vector<int> result;
  for (auto& query : queries) {
     int n = query[0];
                           int k =
query[1];
result.push back(solve(n, k));
  return result;
}
int main() { //
Example usage
  std::vector<std::vector<int>> queries1 = {{2, 6}, {5, 1}, {73, 660}};
std::vector<int> result1 = waysToPlaceIntegers(queries1);
  for (int r : result1) {
std::cout << r << " ";
  }
  std::cout << std::endl;
  std::vector < std::vector < int >> queries 2 = {{1, 1}, {2, 2}, {3, 3}, {4, 4}, {5, 4}}
5}};
  std::vector<int> result2 = waysToPlaceIntegers(queries2);
  for (int r : result2) {
std::cout << r << " ";
  std::cout << std::endl;
  return 0;
```

Output 4 1 50734910 1 2 3 10 5

Problem 18: Maximum Twin Sum of a Linked List

In a linked list of size n, where n is even, the ith node (0-indexed) of the linked list is known as the twin of the (n-1-i)th node, if $0 \le i \le (n/2) - 1$. • For example, if n = 4, then node 0 is the twin of node 3, and node 1 is the twin of node 2. These are the only nodes with twins for n = 4. The twin sum is defined as the sum of a node and its twin. Given the head of a linked list with even length, return the maximum twin sum of the linked list.

```
Code:
#include <iostream>
#include <vector>
#include <algorithm>

using namespace std;

// Definition for singly-linked list.
struct ListNode {
int val;
   ListNode* next;
   ListNode(int x) : val(x), next(nullptr) {}
};

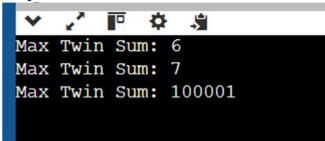
class Solution { public:
   int pairSum(ListNode* head) {
```

```
// Step 1: Store the values of the linked list in a vector
vector<int> values;
    ListNode* current = head:
    // Traverse the linked list and add each node's value to the vector
                                  values.push back(current->val);
while (current != nullptr) {
       current = current->next;
     }
    // Step 2: Calculate the maximum twin sum
    int n = values.size();
     int maxTwinSum = 0;
    // Iterate over the first half of the list and calculate twin sums
                              int twinSum = values[i] +
for (int i = 0; i < n / 2; ++i) {
values[n - 1 - i];
       maxTwinSum = max(maxTwinSum, twinSum);
     }
    return maxTwinSum;
  }
};
// Helper function to create a linked list from a vector
ListNode* createList(const vector<int>& nums) {
  ListNode* head = new ListNode(nums[0]);
  ListNode* current = head;
                               for (int i = 1;
i < nums.size(); ++i) {
                           current->next =
new ListNode(nums[i]);
     current = current->next;
  return head;
int main() {
                    // Example 1
vector<int> input1 = \{5, 4, 2, 1\};
  ListNode* head1 = createList(input1);
  Solution sol;
```

```
cout << "Max Twin Sum: " << sol.pairSum(head1) << endl; // Output: 6

// Example 2
vector<int> input2 = {4, 2, 2, 3};
ListNode* head2 = createList(input2);
cout << "Max Twin Sum: " << sol.pairSum(head2) << endl; // Output: 7

// Example 3
vector<int> input3 = {1, 100000};
ListNode* head3 = createList(input3); cout << "Max Twin Sum: "
<< sol.pairSum(head3) << endl; // Output:
100001
return 0;
}</pre>
```



Problem 19: Insert Greatest Common Divisors in Linked List Given the head of a linked list head, in which each node contains an integer value. Between every pair of adjacent nodes, insert a new node with a value equal to the greatest common divisor of them. Return the linked list after insertion. The greatest common divisor of two numbers is the largest positive integer that evenly divides both numbers. Solution:

```
#include <iostream>
#include <vector> // Include the vector header
#include <algorithm>
using namespace std;
```

// Definition for singly-linked list.

```
struct ListNode {
  int val;
  ListNode* next:
  ListNode(int x) : val(x), next(nullptr) {}
};
class Solution { public:
  // Function to compute GCD of two numbers
int gcd(int a, int b) {
                         while (b != 0) {
       int temp = b;
b = a \% b;
= temp;
return a;
  }
  // Function to insert GCD nodes between each pair of adjacent nodes
  ListNode* insertGreatestCommonDivisors(ListNode* head) {
    // Edge case: If the list is empty or has only one node, no insertion is needed
if (!head || !head->next) return head;
    ListNode* current = head;
    // Traverse the list
                                               int gcdValue = gcd(current-
     while (current && current->next) {
>val, current->next->val); // Calculate the
GCD
       ListNode* newNode = new ListNode(gcdValue); // Create a new node
with the GCD value
                           newNode->next = current->next; // Link the new
node to the next node
                             current->next = newNode; // Link the current
node to the new node
                             current = newNode->next; // Move to the next
pair of nodes
    return head;
};
```

```
// Helper function to create a linked list from a vector
ListNode* createList(const vector<int>& values) {
if (values.empty()) return nullptr;
  ListNode* head = new ListNode(values[0]);
                               for (int i = 1; i
  ListNode* current = head:
< values.size(); ++i) {
                            current->next =
new ListNode(values[i]);
     current = current->next;
  }
  return head;
// Helper function to print the linked list
void printList(ListNode* head) {
  while (head) {
                      cout <<
head->val;
              if (head->next)
cout << " -> "; head = head-
>next;
  }
  cout << endl;
int main() {
  Solution sol;
  // Test case 1
                  vector<int> values1
= \{18, 6, 10, 3\};
  ListNode* head1 = createList(values1);
  ListNode* result1 = sol.insertGreatestCommonDivisors(head1);
printList(result1); // Expected: 18 -> 6 -> 6 -> 2 -> 10 -> 1 -> 3
  // Test case 2
  vector\leqint\geq values2 = \{7\};
  ListNode* head2 = createList(values2);
  ListNode* result2 = sol.insertGreatestCommonDivisors(head2);
printList(result2); // Expected: 7
  return 0;
```

Output