

PRACTICAL NO. 1

Aim :- Basics of R Software

- 1) R is a software for statistical analysis and data computing
- 2) It is an effective data handling software and outcome storage is possible
- 3) It is capable of graphical display
- 4) It is a free software

Q.1 Solve the following

$$1) 4+6+8 \div 2-5 \\ > 4+6+8/2-5 \\ [1] 9$$



$$2) 2^2 + 1 - 31 + \sqrt{45} \\ > 2^2 + 1 - 31 + \sqrt{45} \\ [1] 13.7082$$

$$3) 5^3 + 7 \times 5 \times 8 + 46/5 \\ > 5^3 + 7 * 5 + 8 + 46/5 \\ [1] 414.2$$

3.2) $\rightarrow c(2,3,5,7) * 2$ $\rightarrow c(2,3,5,7) * c(2,3)$
 [1] 4 6 10 14 [1] 4 9 10 21
 $\rightarrow c(2,3,5,7) * c(2,3,6,2)$ $\rightarrow c(1,6,2,3) * c(-2,-3,-4,-1)$
 [1] 4 9 30 14 [1] -2 -18 -8 -3
 $\rightarrow c(2,3,5,7)^2$ $\rightarrow c(4,6,8,9,4,5)^2 c(1,2,3)$
 [1] 4 9 25 49 [1] 4 36 512 9 16
 $\rightarrow c(6,2,7,5) / c(4,5)$
 [1] 1.50 0.40 1.75 1.00

3.3) $\rightarrow x = 20 \rightarrow y = 30 \rightarrow z = 2$
 $\rightarrow x^2 + y^3 + z$
 [1] 97402
 $\rightarrow \text{sqrt}(x^2 + y)$
 [1] 20.73644
 $\rightarrow x^2 + y^2$
 [1] 1300

3.4) $\rightarrow x < -\text{matrix}(\text{nrow}=4, \text{ncol}=2, \text{data}=c(1,2,3,4,5,6,7,8))$

| | | |
|-----------------|------|------|
| $\rightarrow x$ | [,1] | [,2] |
| [1,] | 1 | 5 |
| [2,] | 2 | 6 |
| [3,] | 3 | 7 |
| [4,] | 4 | 8 |

Q.5 Find $x+y$ and $2x+3y$. where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$

$$y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

> $x <- \text{matrix}(\text{nrow}=3, \text{ncol}=3, \text{data} = c(10, 12, 15, -5, -4, -6, \dots)$

> y
[,1] [,2] [,3]
[1,] 10 -5 7
[2,] 12 -4 9
[3,] 15 -6 5

> $x+y$
[,1] [,2] [,3]
[1,] 10 -7 13
[2,] 12 -4 16
[3,] 24 -11 8

> $2 - x + 3 * y$
[,1] [,2] [,3]
[1,] 38 -19 33
[2,] 50 -12 41
[3,] 63 -28 21

Q.6 Masks of Statistics of CS Batch B

$x = c(58, 20, 35, 24, 46, 56, 55, 45, 21, 22, 47, 58, 54, 40, 50, 82, 36, 29, 33, 39)$

> $x = c(\text{data})$

breaks : $\text{seq}(20, 60, 5)$

a : $\text{Cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

> b = table(6)
 > c = transform(b)

| | a | freq |
|---|----------|------|
| 1 | [20, 25] | 3 |
| 2 | [25, 30] | 2 |
| 3 | [30, 35] | 1 |
| 4 | [35, 40] | 4 |
| 5 | [40, 45] | 1 |
| 6 | [45, 50] | 3 |
| 7 | [50, 55] | 2 |
| 8 | [55, 60] | 4 |

Q1
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PRACTICAL - 2

Topic :- Probability distribution

1) check whether the following are p.m.f or not

| x | $p(x)$ |
|-----|--------|
| 0 | 0.1 |
| 1 | 0.2 |
| 2 | -0.5 |
| 3 | 0.4 |
| 4 | 0.3 |
| 5 | 0.5 |

If the given data is p.m.f. then

$$\sum p(x) = 1$$

$$p(0) + p(1) + p(2) + p(3) + p(4) + p(5) = p(x)$$

$$\therefore 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ = 1.0$$

$\therefore p(x) = -0.5$, if ~~Can't~~ the probability mass function

$\therefore p(x) \geq 0, \forall x$

| 2) | x | $p(x)$ |
|----|-----|--------|
| | 1 | 0.2 |
| | 2 | 0.2 |
| | 3 | 0.3 |
| | 4 | 0.2 |
| | 5 | 0.2 |

The Condition for p.m.f is $\sum p(x) = 1$

So,

$$\begin{aligned}\sum p(x) &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1\end{aligned}$$

\therefore The given data is not a p.m.f because the $p(x) \neq 1$

| 3) | x | $p(x)$ |
|----|-----|--------|
| | 10 | 0.2 |
| | 20 | 0.2 |
| | 30 | 0.35 |
| | 40 | 0.15 |
| | 50 | 0.1 |

~~The Condition for p.m.f is~~

i) $p(x) \geq 0 \quad \forall x$ satisfy

ii) $p(x) = 1$

$$\begin{aligned}\sum p(x) &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1\end{aligned}$$

\therefore The given data is p.m.f

Code :

> prob = c(0.2, 0.2, 0.35, 0.15, 0.1)

> sum(prob)

[1] 1

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Q.2 Find the c.d.f for the following p.m.f and sketch its graph.

$x \quad 10 \quad 20 \quad 30 \quad 40 \quad 50$

$P(x) \quad 0.2 \quad 0.2 \quad 0.38 \quad 0.18 \quad 0.1$

$$P(x) = 0$$

$$x < 10$$

$$0.2$$

$$10 \leq x < 20$$

$$0.4$$

$$20 \leq x < 30$$

$$0.15$$

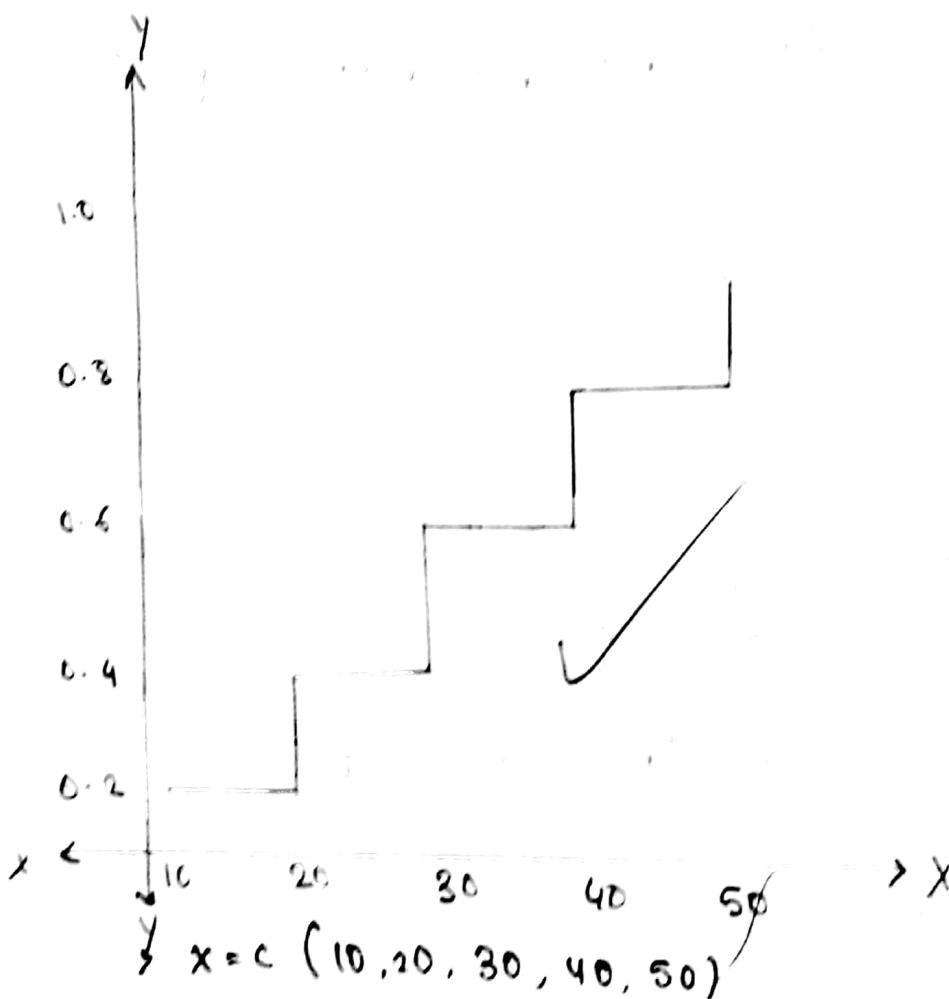
$$30 \leq x < 40$$

$$0.10$$

$$40 \leq x < 50$$

$$1.0$$

$$x \geq 50$$



$\rightarrow \text{plot}(x, \text{CumSum}(c), "s")$

12. Find

| | | | | | | |
|--------|------|------|-----|-----|-----|-----|
| x | 1 | 2 | 3 | 4 | 5 | 6 |
| $p(x)$ | 0.15 | 0.25 | 0.1 | 0.2 | 0.2 | 0.1 |

| | |
|------------|----------------|
| $F(x) = 0$ | $x < 1$ |
| $= 0.15$ | $1 \leq x < 2$ |
| $= 0.40$ | $2 \leq x < 3$ |
| $= 0.50$ | $3 \leq x < 4$ |
| $= 0.70$ | $4 \leq x < 5$ |
| $= 0.90$ | $5 \leq x < 6$ |
| $= 1.00$ | $x \geq 6$ |

> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)

> sum(prob)

[1] 1

> cumsum(prob)

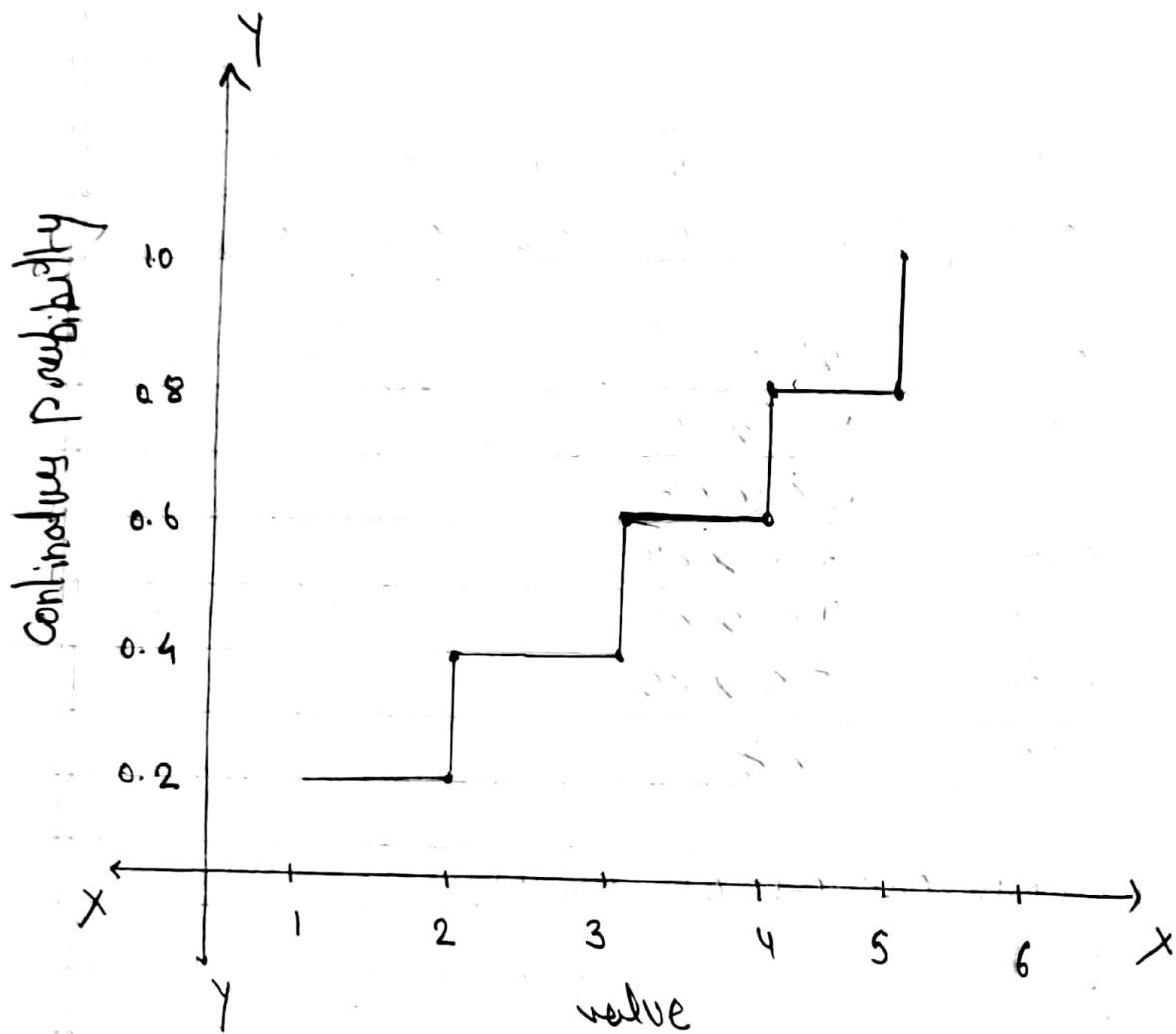
[1] 0.15, 0.40, 0.50, 0.70, 0.90, 1.00

> y = c(1, 2, 3, 4, 5, 6)

> plot(x, cumsum(prob), "s" x lab = "value",

y lab = "cumulative probability"

main = "CDF Graph", cex (= "brown")



3. Check that whether the following is p.d.f or not

$$\text{i) } f(x) = 3 - 2x ; 0 \leq x \leq 1$$

$$\text{ii) } f(x) = 3x^2 ; 0 < x < 1$$

$$\text{i) } f(x) = 3 - 2x$$

$$= \int_0^x f(x) dx$$

$$= \int_0^x (3 - 2x) dx$$

$$= \int_0^x 3 dx - \int_0^x 2x dx$$

$$= [3x - x^2]_0^1 = 2$$

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\therefore The $\int_0^1 f(x) = 1 \therefore$ It is not a pdf

2) $f(x) = 3x^2 ; 0 < x < 1$

$$\int_0^1 f(x)$$

$$= \int_0^1 3x^2$$

$$= 3 \int_0^1 x^2$$

$$= 3 \left[\frac{x^3}{3} \right]_0^1 \quad \because x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The $\int_0^1 f(x) = 1 \therefore$ It is a pdf

PRACTICAL: 3

1) $> x = dbinom(10, 100, 0.1)$

$> x$

[1] 0.1318653

2) i) $x = dbinom(4, 12, 0.2)$

[1] 0.1328756

ii) $pbinom(4, 12, 0.2)$

[1] 0.9274445

iii) $1 - pbinom(3, 12, 0.2)$

[1] 0.01940528

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3 dbinom (0:5, 5, 0.1)

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.00810

4 - 0.00045

5 - 0.00001

4 i) dbinom (5, 12, 0.25)

[1] 0.1032414

ii) pbisnom (5, 12, 0.25)

[1] 0.9455978

iii) 1-pbisnom (7, 12, 0.25)

[1] 0.0027815

iv) dbisnom (6, 12, 0.25)

[1] 0.04014945

v) dbisnom (8, 12, 0.25)

[1] 0.1032414

vi) dbisnom (5, 12, 0.25)

[1] 0.9455978

vii) 1 - pbisnom (7, 12, 0.25)

[1] 0.0027815

viii) dbisnom (6, 12, 0.25)

[1] 0.04014945

(8)

PRACTICAL NO. 3

Topic :- Binomial distribution

$p(x=x) = \text{dbinom}(x, n, p)$

$p(x \leq x) = \text{pbinom}(x, n, p)$

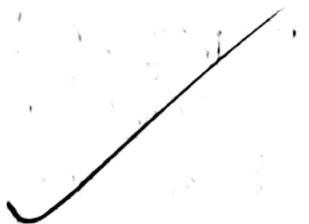
$p(x > x) = 1 - \text{pbinom}(x, n, p)$

if x is unknown

$$p_1 = p(x \leq x) = \text{qbinom}(p_1, n, p)$$

- i) Find the probability of exactly 10 success in hundred trials with $p=0.1$
- ii) Suppose there are 12 mcq, each question has 5 options out of which 1 is correct. Find the probability of having
 i) exactly 4 correct answers
 ii) almost 4 correct answers
 iii) more than 5 correctly answered
- iii) Find the complete distribution when $n=5$ and $p=0.1$
 probabilities
 i) $p(x=5)$ iii) $p(x>7)$ $n=12 \quad p=0.25$
 ii) $p(x \leq 5)$ iv) $p(5 < x < 7)$

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- 5) The probability of Sales making a Sale to customer is 0.15. Find probability
i) No Sales out of 10 customers
ii) More than 3 sales out of 20 customers.
- 6) A Salesman has 20% probability of making a Sale to Customers out of 30 customers. What is minimum no. of Sales he can make with 88% of probability.
- 7) X follows binomial distribution with $n=10, p=0.3$.
Plot the graph of p.m.f. & c.d.f.



5) $dbinom(0, 10, 0.15)$

[1] 0.196874

6) $pbinom(3, 20, 0.15)$

[1] 0.852274

6) $qbinom(0.88, 30, 0.2)$

[1] 9

7) $n = 10$

$\rightarrow p = 0.3$

$\rightarrow x = 0:n$

$\rightarrow prob = dbinom(x, n, p)$

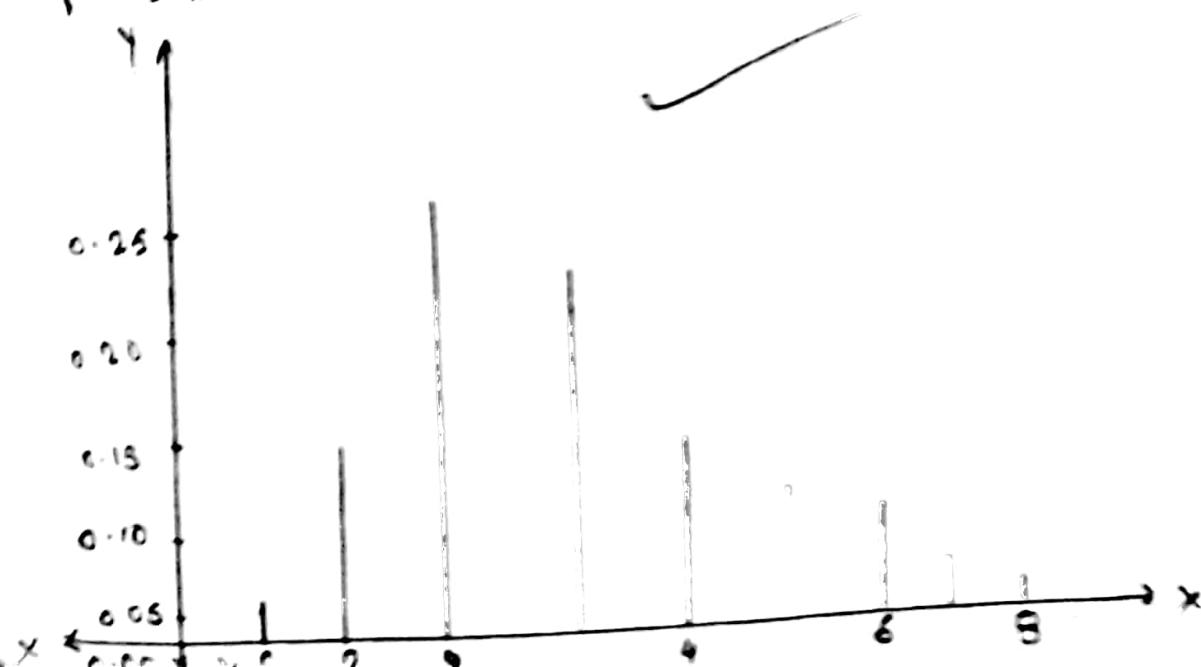
$\rightarrow Cumprob = pbinom(x, n, p)$

$\rightarrow d = data.frame("x value" = x, "probability" = prob)$

$\rightarrow print(d)$

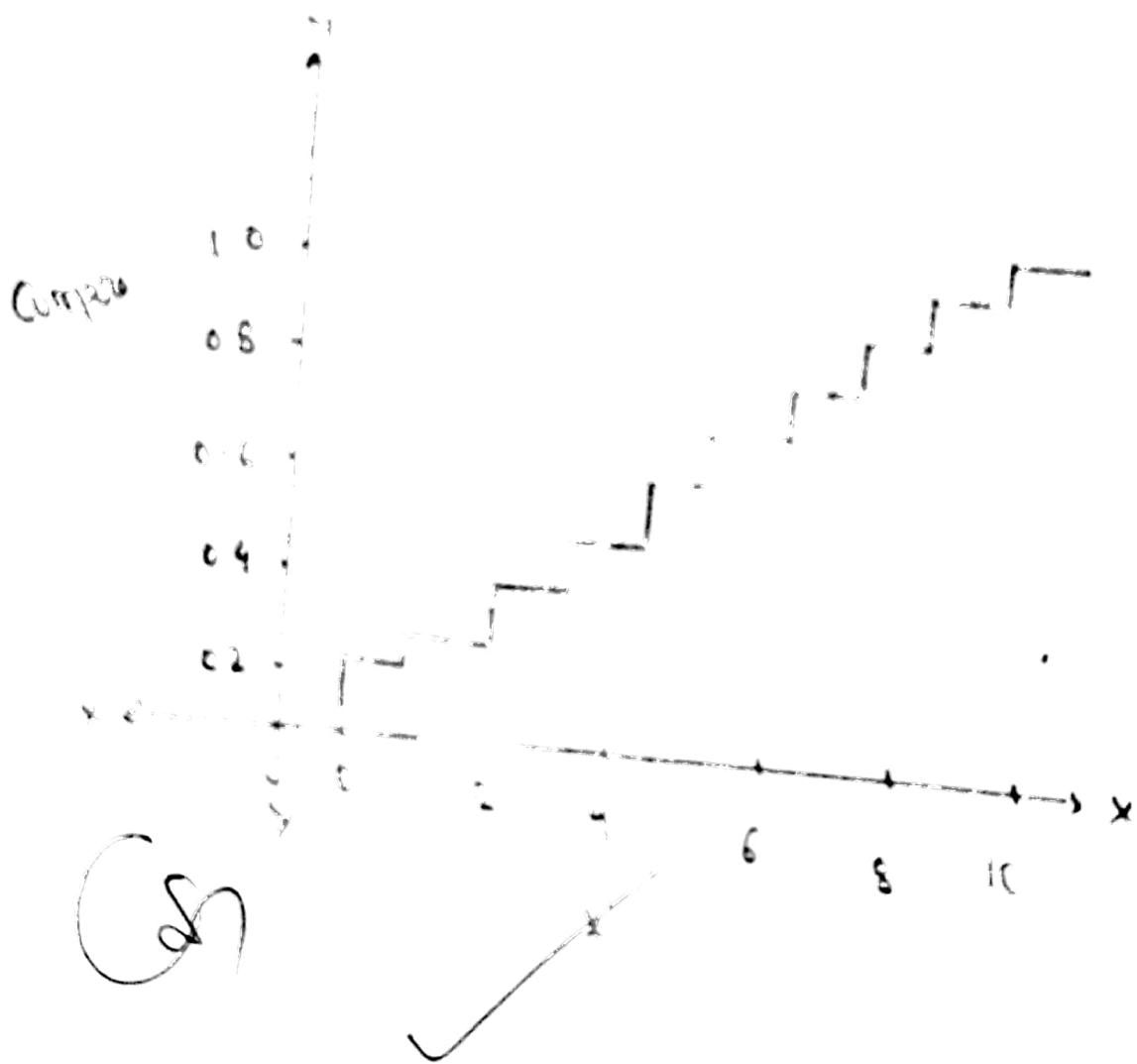
| x value | probability |
|---------|-------------|
| 0 | 0.0377 |
| 1 | 0.1210 |
| 2 | 0.2339 |
| 3 | 0.2668 |
| 4 | 0.2001 |
| 5 | 0.1024 |
| 6 | 0.0367 |
| 7 | 0.0090 |
| 8 | 0.0017 |
| 9 | 0.0001 |
| 10 | 0.0000 |
| 11 | |

$> plot(x, prob, "b")$



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> plot (> Compound, "s")



PRACTICA 4

Topic :- Normal Distribution

- i) $p(x=x) = \text{dnorm}(x, \mu, \sigma)$
- ii) $p(x \leq x) = \text{pnorm}(x, \mu, \sigma)$
- iii) $p(x > x) = 1 - \text{pnorm}(x, \mu, \sigma)$
- iv) To generate random numbers from a normal distribution (n random numbers) the R code is
 $\text{rnorm}(n, \mu, \sigma)$

Q.1. A random variable x follows normal distribution with mean = 12

CODE :-

```
> p1 = pnorm(15, 12, 3)
> p1
[1] 0.8413447
> p2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)
[1] 0.3780661
> p3 = 1 - pnorm(14, 12, 3)
[1] 0.2524925
> p4 = rnorm(5, 12, 3)
[1] 15.254723 16.548505 11.280615 6.419444
[4] 12.2460
```

i) x follows normal distribution with $\mu=10$, $\sigma=2$. Find
 p(i) $p(x \leq 7)$ ii) $p(5 < x < 10)$ iii) $p(x > 12)$ iv) 10 observations
 Also find k such that $p(x < k) = 0.4$

CODE :-

> $p_1 = \text{pnorm}(4, 10, 2)$

p_1

[1] 0.668072

> $p_2 = \text{pnorm}(5, 10, 2) - \text{pnorm}(12, 10, 2)$

p_2

[1] -0.885181

$p_3 = 1 - \text{pnorm}(12, 10, 2)$

p_3

[1] ~~0.1586~~ ~~pnorm(10, 10, 2)~~

$p_4 = \text{rnorm}(10, 10, 2)$

p_4

| | | | | |
|-----|-----------|----------|-----------|-----------|
| [1] | 17.608981 | 9.920414 | 12.637741 | 8.078354 |
| | 8.721380 | 9.143725 | 0.366824 | 11.707106 |
| | 9.537584 | 12.75006 | | |

$p_5 = qnorm(0.4, 10, 2)$

p_5

[1] 9.4998306

Q. Generate 5 random numbers from a normal distribution
 $\mu = 15$, $\sigma = 4$. Find Sample mean, median, S.D and
 print it.

Code :-

```

> rnorm(5, 15, 4)
[1] 10.7649 7.793249 9.963444 13.345904 17.50966
> am = mean(x)
am
[1] 11.87345
> cat("Sample mean is ", am)
Sample mean = 11.87345
> me = median(x)
> me
[1] 10.76499
> cat("Sample median = ", me)
Sample median = 10.76494
> n = 5
> v = (n-1) * var(x) / n
> v
[1] 11.09965
> SD = sqrt(v)
> SD
[1] 3.33163
> cat("SD = ", SD)
SD = 3.33163
  
```

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Q.4. $X \sim N(30, 100)$, $\sigma = 10$

- i) $P(X \leq 40)$; ii) $P(X > 85)$ iii) $P(25 < X < 35)$
- iv) find k such that $P(X < k) = 0.6$

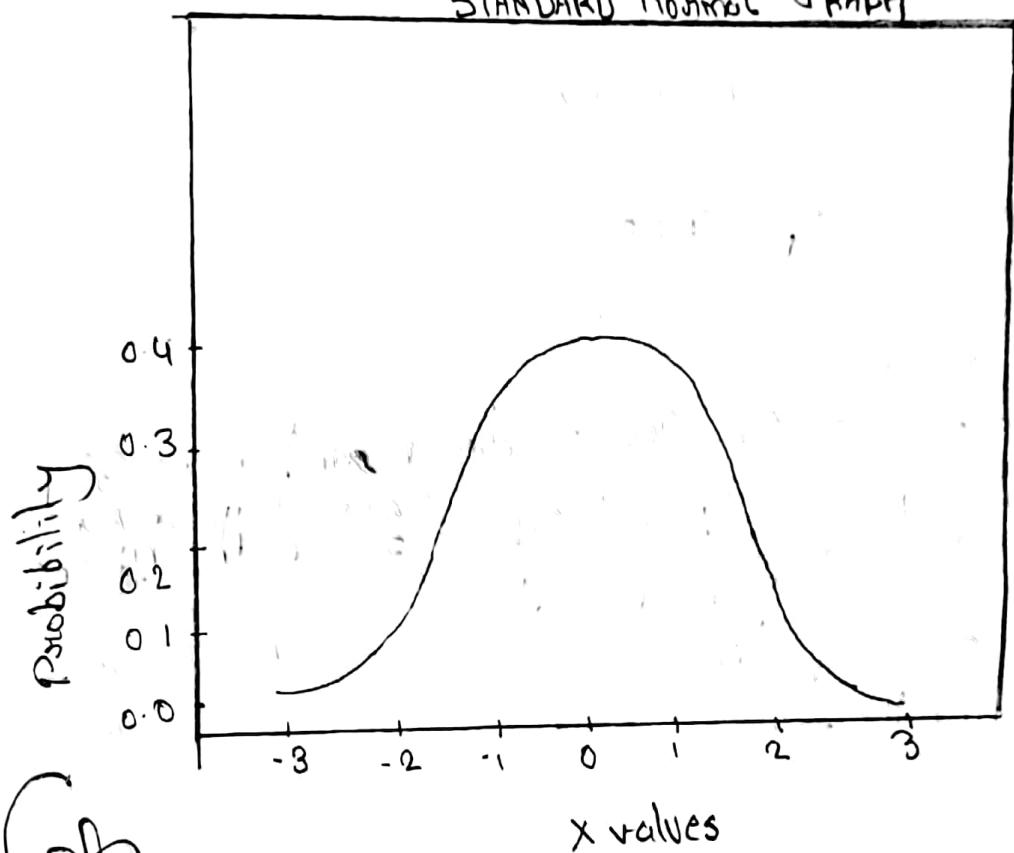
Code :-

```
> f1 =pnorm(40, 30, 10)
> f1
[1] 0.8418414
> f2 = 1 - pnorm(35, 30, 10)
> f2
[1] 0.3085375
> f3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)
f3
[1] 0.3829249
> f4 = qnorm(0.6, 30, 10)
> f4
[1] 32.53347
```

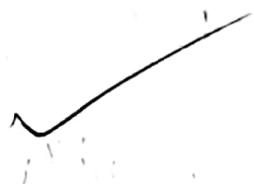
Q.5 plot standard normal graph

```
> x = seq(-3, 3, by = 0.1)
> y = dnorm(x)
> plot(x, y, xlab = "x values", ylab = "probability",
main = "standard normal graph")
```

STANDARD Normal GRAPH



(g)



PRACTICAL - 5

Topic : Normal and t-Test

i) $H_0 : \mu = 15$ $H_1 : \mu \neq 15$

Test the hypothesis

Random sample of size 400 is drawn and it is given.

The Sample mean is 14 and s.d is 3 test the hypothesis at 5% level of Significance at .5%

$0.05 >$ accept the value

$0.05 <$ less the value

> $m_0 = 15$

> $m_x = 14$

> $n = 400$

> $s_d = 3$

> $z_{cal} = (m_x - m_0) / [s_d / (\sqrt{n})]$

> z_{cal}

[.] - 6.6667

> Cal ("Calculated values of z is:" z_{cal})

Calculated values z is - 6.666

> pvalue = $2 * (1 - \text{pnorm}(z_{cal}))$

> pvalue

[.] 2.616796

∴ The value is less than 0.05 we will rejected the value of $H_0 : \mu = 15$

1) Test the hypothesis $H_0: \mu = 4-10$ against $H_1: \mu \neq 4-10$
 A random sample size of 400 is drawn with Sample
 mean = 10.2 and $s.d = 2.25$ Test the hypothesis at.

$$> m_0 = 10$$

$$> n = 400$$

$$> m_x = 10.2$$

$$> s_d = 2.25$$

$$> z_{cal} = (m_x - m_0) / [s_d / (\sqrt{n})]$$

$$> z_{cal}$$

$$[1] 1.7778$$

$$> pvalue = 2 * (1 - \text{pnorm}(z_{cal}))$$

$$> pvalue$$

$$> 0.01544036$$

\therefore The value pvalue is greater than 0.05. The value is accepted.

3) Test the hypothesis H_0 : proportion of smokers is College is 0.2. A sample is collected and Calculated the sample os 0.125 test the hypothesis at 5% level of significance [Sample size is 900]

$$> p = 0.2$$

$$> P = 0.125$$

$$> n = 400$$

$$> Q = 1 - P$$

$$> z_{cal} = (p - P) / \sqrt{P * Q / n}$$

\times cal ("Calculated value of z is", "z_{cal}

- [1] Calculated value of z is = -3.75
 > pvalue = $2 * (1 - \text{pnorm}(\text{abs}(z\text{cal})))$
 pvalue
 [1] 0.0001768346 (Reject)

4) Last Year Farmers lost 20% of their crops. A random sample of 60 fields are collected and it is test hypothesis at 1% levels of significance -

- > p = 0.2
 > p = 9/60
 > n = 60
 > $z\text{cal} = (p - P) / \sqrt{p * Q/n}$
 > $z\text{cal}$
 > [-1] = 0.96824
 > pvalue = $2 * (1 - \text{pnorm}(\text{abs}(z\text{cal})))$
 pvalue
 > [1] 0.332916

5) Test the hypothesis $H_0 : \mu = 12.5$ from the following sample at 5% level of significance.

- > $x = c(12.25, 11.97, 12.25, 12.08, 12.81, 12.28, 11.94, 11.84, 12.16, 12.04)$
 n = length(x)
 [1] 10
 $\text{mean} = \text{mean}[x]$

> \bar{x}

[1] 12.107

> variance = $(n-1) * \text{var}(x) / n$

Variance

[1] 0.019521

> $s_d = \sqrt{\text{variance}}$

> s_d

[1] 0.1343176

> $t = (\bar{x} - \mu_0) / (s_d / \sqrt{n})$

[1] -8.894909

> pvalue = $2 * (1 - \text{pnorm}(\text{obs}(t)))$

> pvalue

[1] 0

p: This value is less than 0.0 so the value is accepted.

Q



PRACTICA - 06

Topic : Large sample test

- 1) Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected the sample mean is 275 and S.P. 30. Test the hypothesis that the population mean is 250 or not on 5% level of significance.
- 2) In a random sample of 100 students it is found that 75 use value pen blue. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

→ Sol'n:

$$\rightarrow \mu_0 = 250$$

$$\rightarrow \mu_n = 275$$

$$\rightarrow S_d = 30$$

$$\rightarrow n = 100$$

$$Z_{cal} = (\mu_n - \mu_0) / [S_d / \sqrt{n}]$$

Calculated value of $Z = 8.333$, Z_{cal}

[1] calculated value is $Z = 8.333$

$$\rightarrow p-value = 2 * (1 - \text{pnorm}(\text{abs}(Z_{cal})))$$

p-value.

(i) 0

The value is less than 0.05 we will reject the null hypothesis.

Hence H₀: $\mu = 250$

$$p = 0.8$$

$$\text{or } 1-p$$

$$p = 750/1000$$

$$n = 1000$$

$$z_{\text{cal}} = (p - P) / \sqrt{p * (1/n)}$$

Cal "C" calculated value is $z = 1.201$

(ii) Calculated value of $z = -3.9558$

$$p\text{value} = 2 * (1 - \text{pnorm}(z_{\text{obs}}(201)))$$

pvalue

$$[4] 3.97628. \text{JR}$$

\therefore The value is less than 0.01 we reject H₀

3) A study sample of size 1000 & 2000 are drawn from two population with same sd 8.5 the sample mean are 67.5 and 6.8 test hypothesis $H_1: \mu_1 < \mu_2$ at 1% level of significance.

4) A study of noise level in 2 hospital given below test the claim that 2 hospital have same level of noise at 1% level of significance.

| Hos-A | Hos-B |
|-------|-------|
| 84 | 84 |
| 61.2 | 59.4 |
| 7.9 | 7.5 |

5) In a sample to 600 students is dg 400 used a blue ink. In another dg from a sample of 900 students use blue ink. Test the hypothesis test that the proportion of students using blue ink in two colleges course equal or not at 1% level of significance.

Solution:-

$$n_1 = 1000$$

$$n_2 = 2000$$

$$mx_1 = 67.5$$

$$mx_2 = 68$$

$$Sd_1 = 2.5$$

$$Sd_2 = 2.5$$

$$> z_{cal} = (mx_1 - mx_2) / \sqrt{((sd_1^2/n_1) + (sd_2^2/n_2))}$$

$$\cdot z_{cal}$$

$$[] = 5.163975$$

$$> pvalue <- 2 * (1 - pnorm(abs(z_{cal})))$$

$$pvalue$$

$$> [] 2.417564e-07 \sim \text{(rejected.)}$$

$$n_1 = 84$$

$$n_2 = 84$$

$$mx_1 = 69.4 \quad 61.2$$

$$mx_2 = 59.4$$

$$Sd_1 = 7.9$$

$$Sd_2 = 7.9$$

$$> z_{cal} = \frac{(m_1 - m_2)}{\sqrt{(\sigma_1^2/n_1 + \sigma_2^2/n_2)^{1/2}}}$$

[1] 1.162528

$$> pvalue = 2 * [1 - pnorm(z_{cal})]$$

[1] 0.245021

"The value is greater than 0.01 we accept the hypothesis.

5)

$$H_0: p_1 = p_2 \text{ against } H_1: p_1 \neq p_2$$

$$> n_1 = 600$$

$$> n_2 = 900$$

$$> p_1 = 400/600$$

$$> p_2 = 450/900$$

$$> p = \frac{(n_1 * p_1 + n_2 * p_2)}{(n_1 + n_2)}$$

> p

[1] 0.4333

$$> z_{cal} = \frac{(p_1 - p_2)}{\sqrt{p * q * (1/n_1 + 1/n_2)}}$$

[1] 6.381534

$$> pvalue = 2 * [1 - pnorm(z_{cal})]$$

[1] 1.7532e-16

(*)

\therefore value is less than 0.01 the value is rejected.

PRACTICAL - 7

Topic : Small Sample Test

The marks of 10 students are given by 63, 63, 66, 67, 68, 69, 70, 71, 72. Test the hypothesis that the sample from the population with average 66.

$$H_0 : \mu = 66$$

$$\bar{x} = c(66, 63, 66, 67, 68, 69, 70, 71, 72)$$

> t. test (\bar{x})

one Sample t-test

data : x

$$\bar{x} = 68.319, df = 9, pvalue = 1.558e^{-13}$$

alternative hypothesis

The mean is not equal to 0

95 percent Confidence interval

$$[65.63171, 70.14829]$$

sample estimates

mean of \bar{x}

$$67.9$$

The p value is less than 0.05 we reject the hypothesis at 5% level of significance.

2) Two groups of students Scanned the following marks Test the hypothesis that there is no significant difference between the 2 group.

GR1 :- 18, 22, 21, 17, 20, 17, 23, 20, 22, 21

GR2 :- 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H_0 : There is not difference b/w the 2 groups.

> $x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$

> $y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

> t.test(x, y)

welch Two Sample t-test
data : x and y

t = 2.2573 df = 16.376 p-value = 0.03798

alternative hypothesis

True difference in means is not equal

to 0 95 percent Confidence interval

0.1628205 5.0371745

sample estimates:

mean of x mean of y
20.1 17.5

> p-value = 0.03798

> if (pvalue > 0.05) {cat ("accept H₀")}

else {cat ("reject H₀")}

reject H₀.

Q) The sales data of 6 shops before & after a ⁶⁰ special campaign are given below

Before : - 53, 28, 31, 48, 50, 42

after : - 58, 29, 30, 55, 56, 45

Test the hypothesis different of Sales before

H_0 : There is no significant difference of sales before & after Campaign

> $x = c$ (Before)

> $y = c$ (After)

> t-test (x, y , paired = T, alternative = "greater")

paired t-test where

data : $x \& y$

$t = -2.7815$, $df = 5$, $pvalue = 0.9806$

alternative hypothesis :

True difference in means is greater than 0

95 percent Confidence interval:

-6.035547 inf.

Sample estimates

mean of the difference

-3.5

$\therefore pvalue$ is greater than 0.05, we accept the hypothesis at 5% Level of Significance.

Q) Is there any change in the weight before & after the diet program. Is the diet program effective?

Before : 120, 125, 115, 130, 123, 119

After : 100, 104, 95, 90, 115, 99

Null hypothesis :

H_0 : There is no significance difference

$\rightarrow x = c$ (Before)

$\rightarrow y = c$ (After)

t-test (x, y , paired = T, alternative = "less")
paired t-test

data : $x \& y$

t = 4.3438, df = 5, p-value = 0.9963

alternative hypothesis : true difference in means is
confidence interval

-inf 28.0295

Sample estimates:

mean of the difference

18.2333

i. p-value is greater than 0.05 we accept the
hypothesis at 5% level of significance.

2 medians are applied to two group of patient respectively.

gr1 : 10, 12, 13, 11, 14

gr2 : 8, 9, 12, 14, 15, 10, 9

Is there any significance difference b/w 2 medicines?

H_0 : There is no significance difference

$\gt x = c(\text{grp1})$

$\gt y = c(\text{grp2})$

$\gt t.test(x, y)$

data : $x \sim y$

$t = 0.80384$, $df = 9.7594$, $pvalue = 0.4406$

alternative hypothesis : true difference in mean is not equal to 0

95 percent confidence interval

-0.9698553 4.2981886

Sample estimates:

mean of x: mean of y

12.0000 10.333

$\therefore pvalue$ is greater than 0.05 is accept the hypothesis at 5% level of significance.

150

PRACTICA - 8

Topic: Large and Small test.

- Q.1) The arithmetic mean of a sample of 100 items from a large population is 52. If the standard deviation is 7. Test the hypothesis that the population mean is 55 against the alternative is more than 55 at 5% LOS.



- Q.2) In a big city 350 out of 700 males are found to be smokers. Does the information support that exactly half of the males in the city are smokers? Test at 1% LOS.



- Q.3) Thousand artifacts from the factory A are found of have 2% defective. 15000 artifacts from a 2nd factory B are found have 1% defective. Test at 5% LOS that the two factories are similar or not.



- Q.4) A sample of size 400 was drawn of a sample mean is 99. Test at 5% LOS that the sample comes from a population with the mean 100 and variance 64.

The flower stems are selected and the heights are
the height are found to be (cm) 63, 63, 68, 69, 71, 71, 72 test the
hypothesis that the mean is 66 and variance 64. not to 17.65.

Solution :

$$1) H_0 : \mu = 55, H_1 : \mu \neq 55$$

$$> n = 100$$

$$> \bar{m}_x = 52$$

$$> m_0 = 55$$

$$> s_d = 7$$

$$> z_{\text{cal}} = (\bar{m}_x - m_0) / (s_d / \sqrt{n})$$

$$> z_{\text{cal}}$$

$$[1] -4.285714$$

$$> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p\text{value}$$

$$[1] 1.82153e-05$$

$$2) H_0: p = 0.5 \text{ against } H_1: p \neq 0.5$$

$$> p = 0.5$$

$$> q = 1-p$$

$$> n = 700$$

$$> z_{\text{cal}} = (p - \bar{p}) / (\sqrt{p \cdot q / n})$$

$$> z_{\text{cal}}$$

$$[1] 0$$

$$> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> p\text{value}$$

Q8.

[1] 1

3) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

> $n_1 = 1000$

> $n_2 = 1500$

> $p_1 = 2/1000$

> $p_2 = 1/1500$

> $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> p

[1] 0.99880012

> $q = 1 - p$

[1] 0.9988

> $z_{\text{cal}} = (p_1 - p_2) / \sqrt{p_1 q * (1/n_1 + 1/n_2)}$

> z_{cal}

[1] 0.943375

> $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

> $p\text{value}$

[1] 0.345489

$\therefore p\text{value}$ is greater than 0.05 we accept H_0 and
5% level of significance.

4) $H_0: \mu = 100$ against $H_1: \mu \neq 100$

> $\text{var} = 64$

> $n = 400$

> $m_0 = 100$

> $m_2 = 99$

> $S_d = \sqrt{\text{var}}$

> S_d

[1] 8

```

> zcal = (m2 - m0) / (sd / (sqrt(n)))
> zcal
[1] -0.5
> pvalue = 2 * (1 - pnorm (abs(zcal)))
> pvalue
[1] 0.01241933

```

5) $H_0: \mu = 66$ against $H_1: \mu \neq 66$

```

> x = c(63, 65, 68, 69, 71, 71, 72)
> t.test(x)
One Sample t-test

data: x
t = 47.94, df = 6, p-value = 5.522e-09
64.66479 71.62092
sample estimates:
mean x
68.14286

```

Since p value is less than 0.05 we rejects H_0 at 1% level of significance.

Q

PRACTICAL . 9

Topic : - Non parametric tests

* Sign test :

Q.1.) The following data present earnings (in dollar) for a random sample of five Common stocks listed on the New York Exchange. Test whether median earnings are 4 dollars (1.68, 3.35, 2.50, 6.23, 3.24)

># Sign test.

```
> x <- c(1.68, 3.35, 2.50, 6.23, 3.24)
> n <- length(x); p0 <- 0.5;
> x > 4
[1] FALSE FALSE FALSE TRUE FALSE
```

```
> s <- sum(x > 4); s
x > 4
```

[1]

```
> binom.test(s, n, p = 0.5, alternative = "greater");
```

Exact binomial test

data: s and n

number of successes = 1, number of trials = 5, p-value
= 0.9688

alternative hypothesis: true probability of success is then
0.5 95 %. Confidence interval:

0.01020622 1.00000
Sample estimates
probability of success.

64

wilcoxon test:

a) The scores of 8 students in reading before and after lesson are as follows: Test whether there is effect of reading.

Student No:

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|--------------|----|----|----|----|----|----|----|----|
| Score before | 10 | 15 | 16 | 12 | 09 | 07 | 11 | 12 |
| Score After | 13 | 16 | 15 | 13 | 09 | 10 | 13 | 10 |

> b <- c(10, 15, 16, 12, 09, 07, 11, 12);

> a <- c(13, 16, 15, 13, 09, 10, 13, 10);

> D <- b-a;

> wilcox.test(D, alternative = "greater");

data: D

v = 10.5, p-values = 0.8722

alternative hypothesis: true location is greater than 0

warning message:

In wilcox.test.default(D, alternative = "greater"):

Cannot compute exact p-value with ties.

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Mann - Whitney - wilcoxon's test .

- Q.3) The diameter of a ball bearings was measured by 6 inspectors each using two different kinds of Calipers . Test whether average ball bearing fair .

| Inspector | 1 | 2 | 3 | 4 | 5 | 6 |
|-----------|-------|-------|-------|-------|-------|-------|
| Caliper 1 | 0.265 | 0.268 | 0.266 | 0.267 | 0.269 | 0.264 |
| Caliper 2 | 0.263 | 0.262 | 0.270 | 0.261 | 0.271 | 0.260 |

> # Given

> $x <- c(0.265, 0.268, 0.266, 0.267, 0.269, 0.264)$;

> $y <- c(0.263, 0.262, 0.270, 0.261, 0.271, 0.260)$;

> wilcox.test(x,y, alternative = "greater")

wilcoxon rank sum test

data : x and y

w = 24, p-value = 0.197

alternative hypothesis : true location shift is greater than 0 .

PRACTICAL NO - 10.

AIM : chi Square tests and ANOVA
 (Analysis of variance)

use the following data to test whether the condition of home & Condition of child are independent or not.

| Cond child | Cond Home | Home | Dirty |
|--------------|-----------|------|-------|
| clean | clean | 70 | 50 |
| Fairly clean | | 80 | 20 |
| Clean | | | 45 |
| Dirty | | 35 | |

H₀ : Condition of home & child are independent

> x = c(70, 80, 35, 50, 20, 45)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

| | | |
|------|------|----|
| [,1] | [,2] | |
| [1,] | 70 | 50 |
| [2,] | 80 | 20 |
| [3,] | 35 | 45 |

> pvalue = chisq.test(y)

> pvalue

pearson's chi-squared test

data: y

X-squared = 25.646

df = 2

p-value = 2.648e-06

They are independent

" pvalue is less than 0.05 we reject
the hypothesis at 5% level of significance.

Q.2. Test the hypothesis that vaccination and disease
are independent or not

vaccine

| Disease | Affected | Not Affected |
|--------------|----------|--------------|
| Affect | 70 | 46 |
| Non-affected | 35 | 37 |

H₀: Disease and vaccine are independent

> x = c(70, 35, 46, 37)

> m = 2

> n = 2

> Y = matrix(x, nrow = m, ncol = n)

> Y

[.1] [.2]

[1,] 70 46

[2,] 35 37

$\rightarrow p^v = \text{chisq} \cdot \text{test}(Y)$

$\rightarrow p^v$
pearson's chi squared test with
yates' continuity correction

data : Y

$$\chi^2 - \text{Square} = 2.0275$$

$$df = 1$$

$$p\text{-value} = 0.1545$$

\therefore p-value is more than 0.05 we accepted
the hypothesis at 5% level of significance.

\therefore They are INDEPENDENT.

