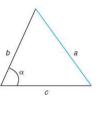
## Math Functions

## CS1010E Lecture 5

## Value-Returning Functions

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 $\hfill\Box$  Given the lengths of two sides of a triangle b and c, and the angle between them  $\alpha$  , compute a

$$a^2 = b^2 + c^2 - 2bc\cos\alpha$$

or

$$a = \sqrt{b^2 + c^2 - 2bc\cos\alpha}$$

### Lecture Outline

#### Math library functions

- Function expression and evaluation
- User defined functions
- Pass-by-value
- Lexical scoping
- Boolean function
- □ Function interface comments

## Math Library Functions

To use C math library functions, include the preprocessor directive

#include <math.h>

- Refer to http://www.acm.uiuc.edu/webmonkeys/book/c\_guide for a list of functions in <math.h>
  - Example: cos function declaration double cos(double x);
- cos function takes in double argument (say x) and produces another double value  $(\cos(x))$

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## Program: Side of a Triangle

## **Function Evaluation**

riangle Evaluate a function expression  $\Rightarrow$  "call" the function

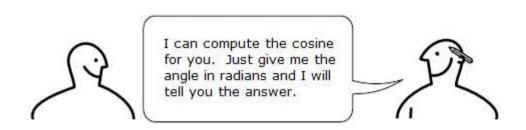
 $\text{argument value(s)} \rightarrow \boxed{\text{function}} \rightarrow \text{evaluated value}$ 

- Suppose  $\alpha=90$ , to evaluate cos(alpha\*PI/180)
  - 1. Arguments are evaluated: cos(1.570795)
  - 2. Argument values 1.570795 passed to function cos
  - 3. cos function performs desired computation
  - 4. cos returns the value 0.0 as the function evaluation
- □ Only one function executes at any one time

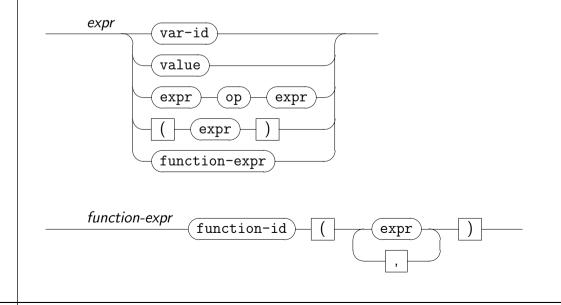
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## **Function Expression**

#### **Functions – Motivation from Life**



- □ Suppose you have a trustworthy friend whom you know can compute the cosine of an angle given in radians
- $\Box$  How to "call" him/her to find the cosine of say,  $\pi$ ?
  - What do you say (or "pass") to your friend?
  - What does he/she give (or "return") back to you?
  - Do you need to know how he/she computes the answer?



#### **User-Defined Function**

## **Function Definition**

□ Program template with user defined functions

```
/* preprocessor directives */
/* function prototypes */
int main(void) {
    /* declarations */
    /* statements */
    return 0;
}
```

- □ functionDefn
  - type: type of value returned from the function
  - function-id: meaningful function identifier
  - parameter-decl: parameter (variable) declaration
- □ parameter-decl
  - Variables declared to store the values passed from the "caller"
  - One variable per declaration separated by commas
- □ function-body
  - Defines the function implementation
  - return statement included as the last logical statement in the function body

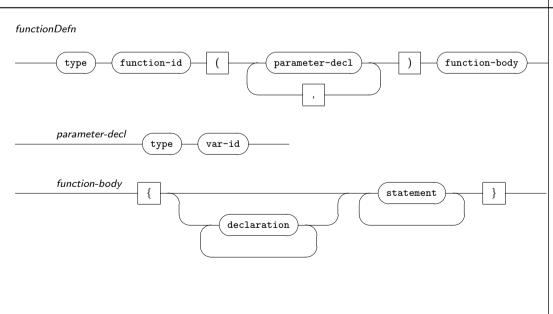
expression

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### return Statement

return-statement

#### **User-Defined Function**



- Upon executing the return statement,
  - 1. the expression is evaluated to a value
  - 2. the function returns the value to the "caller" and terminates

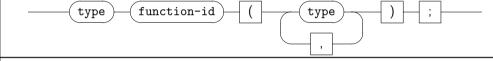
return

3. the "caller" function resumes execution with the value returned

### **Function Prototype**

- A function prototype declares the proper usage of the function in terms of function identifier, number/type of arguments and return values
- Hence, it is placed before the corresponding function calls and the definition of the function
- Almost the same as the corresponding function header, but need only specify the parameter type (parameter name is encouraged but not necessary)
- □ Keep in mind the semicolon at the end

functionPrototype



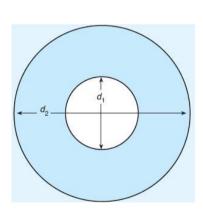
Program: Surface Area of a Flat Washer

```
#include <stdio.h>
#define PI 3.14159
double areaCircle(double);
int main(void) {
    double d2, d1, area;
    printf("Enter d2 and d1 diameters: ");
    scanf("%lf%lf", &d2, &d1);
    area = areaCircle(d2 / 2.0) - areaCircle(d1 / 2.0);
    printf("The surface area is %f\n", area);
    return 0;
}
double areaCircle(double radius) {
    double area;
    area = PI * radius * radius;
    return area;
}
```

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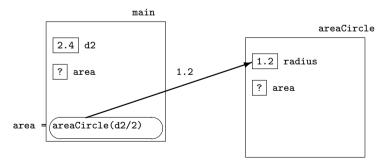
### **Example: Surface Area of a Flat Washer**



- Given the diameters  $d_1$  and  $d_2$ , find the surface area of the hollow disc
- $\Box$  E.g.  $d_1=1.2$  units and  $d_2=2.4$  units gives a surface area of 3.392917 square units
- $\Box$  Area of circle of radius r,  $f_{area}(r) = \pi r^2$ 
  - Surface area of the flat washer is  $f_{area}(\frac{d_2}{2}) f_{area}(\frac{d_1}{2})$
  - In general,  $f(x_1, x_2, \dots x_n)$  is analogous to passing arguments  $(x_1, x_2, \dots, x_n)$  to the function f

### Pass-by-Value

 During a function call, each argument expression is evaluated and the value passed to the function and stored in each input parameter



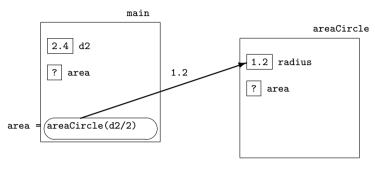
 In the example above, upon initiating the function call in main, areaCircle activates while execution in main suspends

## **Lexical Scoping**

- The scope of accessibility of a variable is within the function
- □ Variables within a function are **local** to that function

in which the variable is declared

□ Variables of the same name can co-exist across functions



## Program: Surface Area of a Flat Washer

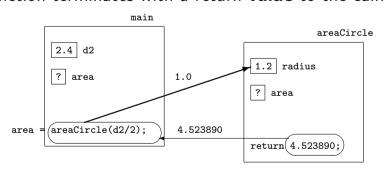
```
#include <stdio.h>
#define PI 3.14159
double areaCircle(double radius);
double surfaceArea(double dOut, double dIn):
int main(void) {
   double d2, d1, area;
   printf("Enter washer and hole diameters: ");
   scanf("%lf%lf", &d2, &d1);
   area = surfaceArea(d2,d1);
   printf("The surface area is %f\n". area):
   return 0;
double surfaceArea(double dOut, double dIn) {
   return areaCircle(dOut/2.0) - areaCircle(dIn/2.0);
double areaCircle(double radius) {
   return PI * radius * radius;
}
```

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**Boolean Functions** 

#### Return Value

☐ Function terminates with a return **value** to the caller



☐ In the example above, areaCircle returns the value to the caller function and **terminates**; main then **resumes** execution

- □ Boolean functions return true or false values
- Defined with bool return type with identifier names preferably starting with is..., e.g. isPrime
- Example: Primality testing
  - Given an integer n(>1), determine if n is prime
  - Loop through all divisors from 2 to p-1
  - If there is a divisor that divides p, p is **not prime**
  - p is prime only when **all** divisors from 2 to p-1 **do not** divide p

### **Program: Primality Testing**

```
#include <stdio.h>
#include <stdbool.h>
                                                             prime \leftarrow y
bool isPrime(int n):
int main(void) {
   int n:
                                                               i < n
   printf("Enter a number: ");
   scanf("%d", &n):
                                                              rem(n,i) =
   if (isPrime(n)) {
      printf("%d is prime\n", n);
      printf("%d is not prime\n", n);
                                                             prime \leftarrow n
   return 0:
                                                              \leftarrow i+1
bool isPrime(int n) {
   int i; bool prime=true;
                                                               i < n
   for (i = 2; i < n; i++) {</pre>
      if (n%i == 0) {
          prime = false;
                                                             return
                                                             prime
   return prime:
```

## **Function Interface Comments**

- A function should contain a comment on
  - Pre-condition condition that should hold true before the function is called
  - Post-condition condition that must hold true after the function completes (can be the purpose of the function)
- Example:

```
isPrime function returns true if n is prime,
   false otherwise.
   Precondition: n > 1
bool isPrime(int n) {
```

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## **Early Return**

```
The isPrime function can be defined to return early
```

```
bool isPrime(int n) {
   int i:
   for (i = 2; i < n; i++) {</pre>
      if (n\%i == 0) {
         return false;
   return true;
Preferred alternative that maintains single-entry-single-exit
bool isPrime(int n) {
   int i; bool prime=true;
```

if (n%i == 0) {

return prime;

prime = false;

for (i = 2; i < n && prime; i++) {</pre>

# **Lecture Summary**

- When working with functions, ensure type consistency
  - Between the argument values and the input parameters double areaCircle(double radius); /\* parameter type is double \*/ area = areaCircle(1.23); /\* argument type is double \*/
  - Between the type of return expression and the function return type

```
double areaCircle(double radius) { /* return type is double */
   return PI * radius * radius;
                                 /* expression type is double */
```

- Between the function return type and how it is used, e.g. printf("%f\n", areaCircle(radius));
- Appreciate the concepts of pass-by-value and lexical scoping

/\* %f prints double-type return value \*/