

Compte rendu de TP3 – Full subtractor

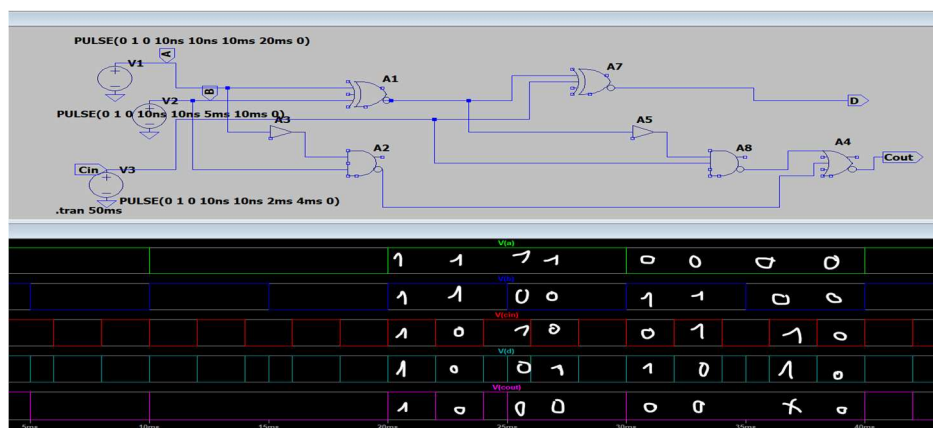
1.1 Objectif de ce TP

Le but de ce TP est de nous familiariser avec les logiciels LT-Spice et VIVADO, et de faire un exercice similaire à Full additionneur précédent avec sa simulation sous LT-Spice et ensuite sur VIVADO.

1.1.1 Exercice part 1 (logiciels LT-Spice)

Construire un full-subtractor 4bits

- Construire la table de vérité
- Réaliser le schéma électronique
- Réaliser l'analyse de chemin critique
- Simuler le circuit sous LT-spice, prouver son fonctionnement



INPUT			OUTPUT	
A	B	Bin	D	Bout
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

0 - 0 = 0
0 - 1 = 1 avec retenue 1
1 - 1 - 1 = -2 = 10 => D=0 et retenue 1

Handwritten derivation of the full subtractor logic:

$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$C_{out} = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}C_{in} + ABC_{in}$$

For simplification:

$$S = A(\bar{B}C_{in} + B\bar{C}_{in}) + \bar{A}(B\bar{C}_{in} + \bar{B}C_{in})$$

$$S = A(B \oplus C_{in}) + \bar{A}(B \oplus C_{in})$$

$$S = (A \oplus \bar{A})(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

Wait, this is incorrect. Let's re-derive correctly from the image:

$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$S = \bar{A}(\bar{B}C_{in} + BC_{in}) + A(\bar{B}\bar{C}_{in} + B\bar{C}_{in})$$

$$S = \bar{A}(B \oplus C_{in}) + A(B \oplus C_{in})$$

$$S = (\bar{A} + A)(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

Actually, the image shows a different derivation for S:

$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$S = \bar{A}(\bar{B}C_{in} + BC_{in}) + A(\bar{B}\bar{C}_{in} + B\bar{C}_{in})$$

$$S = \bar{A}(B \oplus C_{in}) + A(B \oplus C_{in})$$

$$S = (\bar{A} + A)(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

Wait, the image shows a different result for S:

$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$S = \bar{A}(\bar{B}C_{in} + BC_{in}) + A(\bar{B}\bar{C}_{in} + B\bar{C}_{in})$$

$$S = \bar{A}(B \oplus C_{in}) + A(B \oplus C_{in})$$

$$S = (\bar{A} + A)(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

The image shows a different derivation for S:

$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$S = \bar{A}(\bar{B}C_{in} + BC_{in}) + A(\bar{B}\bar{C}_{in} + B\bar{C}_{in})$$

$$S = \bar{A}(B \oplus C_{in}) + A(B \oplus C_{in})$$

$$S = (\bar{A} + A)(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

The image shows a different derivation for S:

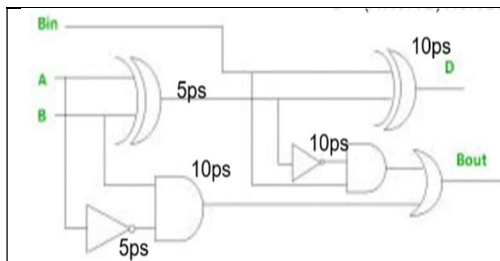
$$S = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

$$S = \bar{A}(\bar{B}C_{in} + BC_{in}) + A(\bar{B}\bar{C}_{in} + B\bar{C}_{in})$$

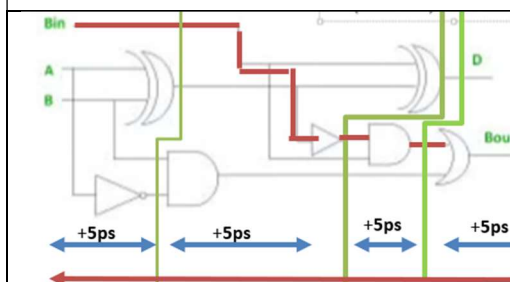
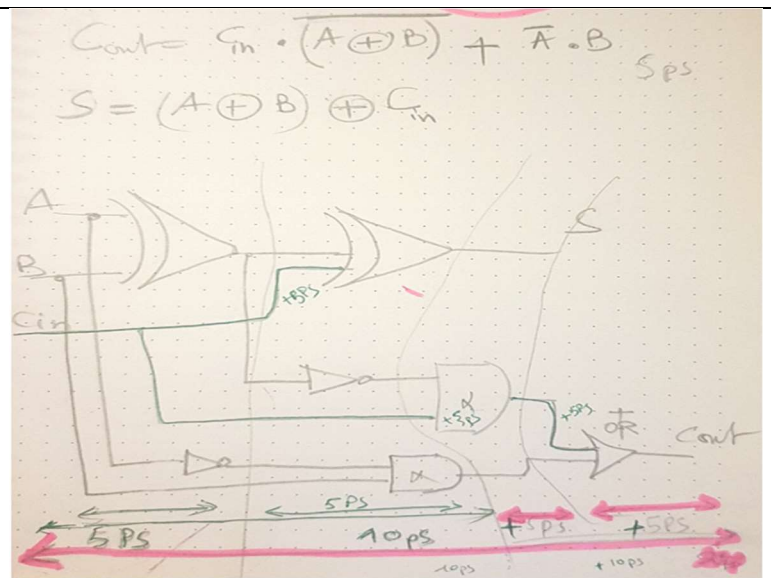
$$S = \bar{A}(B \oplus C_{in}) + A(B \oplus C_{in})$$

$$S = (\bar{A} + A)(B \oplus C_{in}) = 1 \cdot (B \oplus C_{in}) = B \oplus C_{in}$$

→ l'analyse de chemin critique

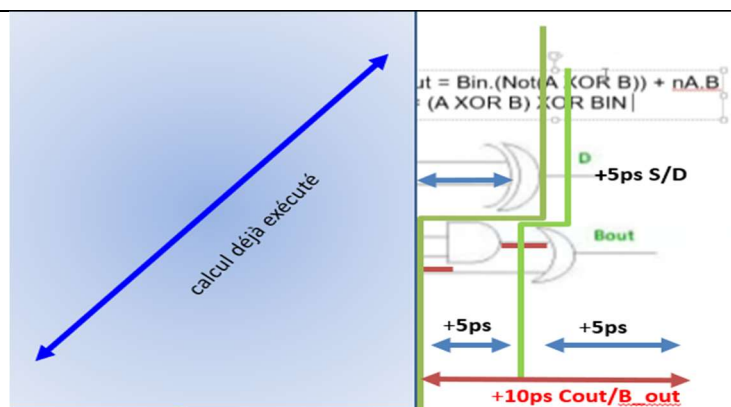


$D = S = (A \oplus B) \oplus C_{in}$
 $C_{out} = Bout = C_{in} \cdot [\text{not}(A \oplus B)] + B \cdot \text{not} A$



Latence 1^{er} LSB (bit0A-bit0B)

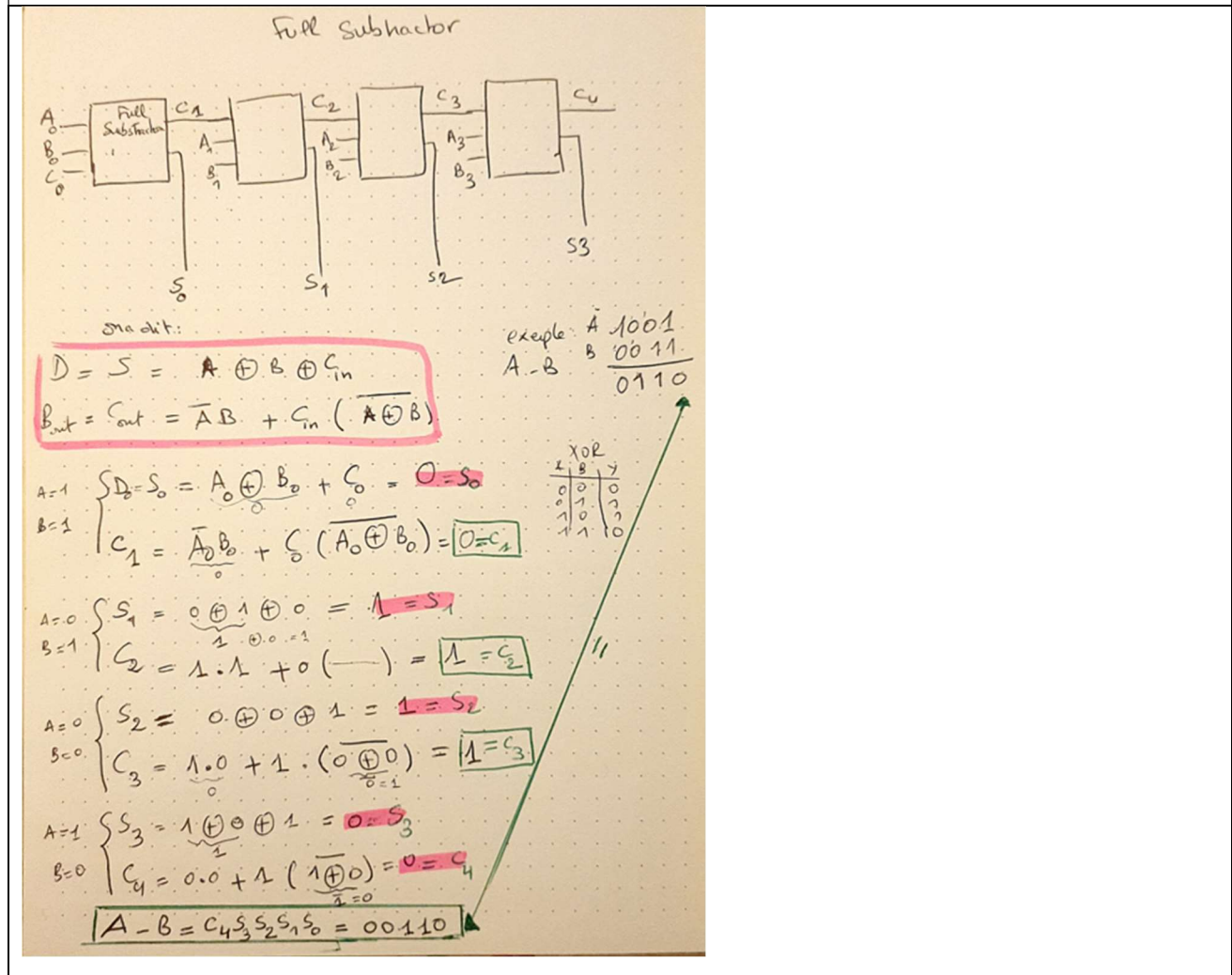
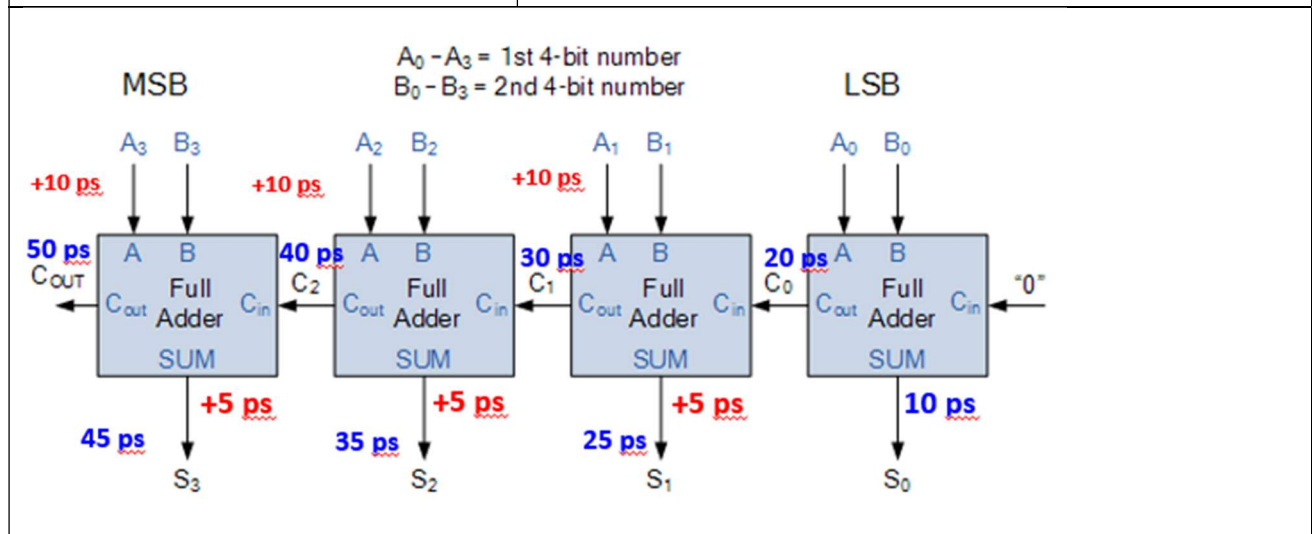
- = 20ps pour la retenue (Cout ou Bin)
- = 10ps pour la sortie D ou S



Latence pour chaque passage d'un block full soustracteur on a :

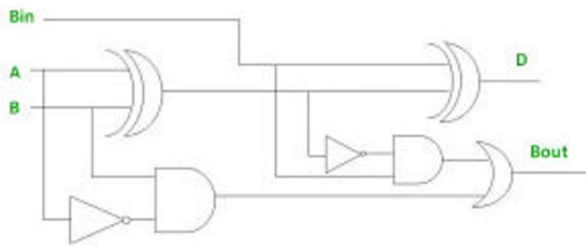
Latence (bit1A-bit1B)=Cout = 20ps + 10ps & S=20ps+5ps

	Latence (bit2A-bit2B)=Cout = 30ps +10ps & S=30ps+5ps Latence (bit3A-bit3B)=Cout = 40ps +10ps & S=40ps+5ps
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1.1.2 Exercice part 2 (logiciels Vivado)

- l'architecture RTL d'un full subtractor est la suivante :



INPUT			OUTPUT	
A	B	Bin	D	Bout
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

Le code subtractor :

```

1
2  -- Déclaration des paquets utiles pour le module
3  library ieee;
4  use ieee.std_logic_1164.all;
5  -- use ieee.std_logic_arith.all;
6  --use ieee.std_logic_unsigned.all;
7
8  --Description externe
9  entity subtractor is
10     Port ( A : in STD_LOGIC;
11           B : in STD_LOGIC;
12           Cin : in STD_LOGIC;
13           S : out STD_LOGIC;
14           Cout : out STD_LOGIC);
15 end subtractor;
16
17 architecture Behavioral of subtractor is
18 begin
19     S <= A XOR B XOR Cin ;
20     Cout <= ((not A)and B) or (Cin AND (not(A XOR B)));
21
22 end Behavioral;
23

```

Le code test bench - subtractor :

```

1  library ieee;
2  use ieee.std_logic_1164.all;
3
4  entity testbench_full_subtractor is
5  end testbench_full_subtractor;
6
7  architecture behavior of testbench_full_subtractor is
8
9      -- component declaration for the unit under test (ut)
10
11      component full_subtractor
12      port(
13          A : in std_logic;
14          B : in std_logic;
15          Cin : in std_logic;
16          S : out std_logic;
17          Cout : out std_logic
18      );
19  end component;
20
21  --Inputs
22  signal A : std_logic := '0';
23  signal B : std_logic := '0';
24  signal Cin : std_logic := '0';
25
26  --Outputs
27  signal S : std_logic:= '0';
28  signal Cout : std_logic:= '0';
29
30  begin
31
32      -- Instantiate the Unit Under Test (UUT)
33      uut: full_subtractor
34      port map (
35          A => A,
36          B => B,

```

$S \leq A \text{ XOR } B \text{ XOR } \text{Cin}$;

$\text{Cout} \leq ((\text{not } A) \text{ and } B) \text{ or } (\text{Cin AND } (\text{not}(A \text{ XOR } B)))$;

```

11  component full_subtractor
12  port(
13      A : in std_logic;
14      B : in std_logic;
15      Cin : in std_logic;
16      S : out std_logic;
17      Cout: out std_logic
18  );
19  end component;
20
21  --Inputs
22  signal A : std_logic := '0';
23  signal B : std_logic := '0';
24  signal Cin : std_logic := '0';
25
26  --Outputs
27  signal S : std_logic:= '0';
28  signal Cout : std_logic:= '0';
29
30  begin
31
32      -- Instantiate the Unit Under Test (UUT)
33      uut: full_subtractor
34      port map (
35          A => A,
36          B => B,
37          Cin => Cin,
38          S => S,
39          Cout => Cout
40      );
41  process
42  begin
43      -- hold reset state for 100 ns.
44      wait for 100 ns;
45

```

- ajouter des tests automatiques :

assert S='x' and Cout= 'Y' report "erreur calcul :expected S='X' and Cout='Y'" severity failure;

INPUT			OUTPUT	
A	B	Bin	D	Bout
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

1) A <= '1'; B <= '0'; Cin <= '0'

assert S='1' and Cout= '0' report "erreur calcul : expected S='1' and Cout='0'" severity failure;

2) A <= '0'; B <= '1'; Cin <= '0'

assert S='1' and Cout= '0' report "erreur calcul : expected S='1' and Cout='0'" severity failure;

3) A <= '1'; B <= '1'; Cin <= '0'

assert S='0' and Cout= '1' report "erreur calcul : expected S='0' and Cout='1'" severity failure;

4) A <= '0'; B <= '0'; Cin <= '1'

assert S='1' and Cout= '0' report "erreur calcul : expected S='1' and Cout='0'" severity failure;

5) A <= '1'; B <= '0'; Cin <= '1'

assert S='0' and Cout= '1' report "erreur calcul : expected S='0' and Cout='1'" severity failure;

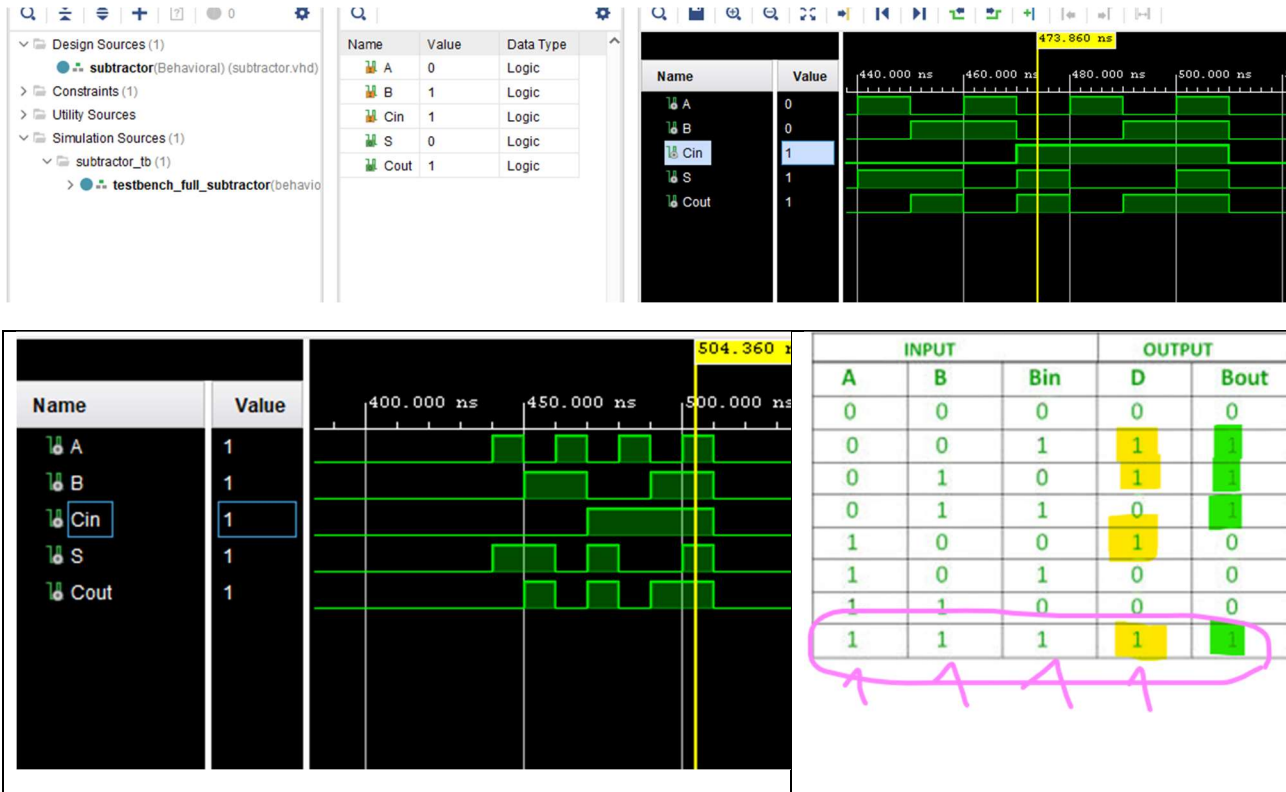
6) A <= '0'; B <= '1'; Cin <= '1'

assert S='0' and Cout= '1' report "erreur calcul : expected S='0' and Cout='1'" severity failure;

7) A <= '1'; B <= '1'; Cin <= '1'

assert S='1' and Cout= '1' report "erreur calcul : expected S='1' and Cout='1'" severity failure;

- La simulation schématique associée / Behavioral Simulation :



- Le schématique associé et La table de vérité associée

