Given Data

```
file = unzip('/MATLAB Drive/yalefaces.zip');
df=file(1:90);
```

Image Vectors

```
all_img = zeros(243,320,90);
vectorized_img = zeros(77760,90);
for i = 1:90
    I =imread(df{i});
    all_img(:,:,i) = I;
    vectorized_img(:,i) = reshape(I,1,[]);
end
```

Normal Image Vectors

```
normal_img_vectors = zeros(77760,15);
for i = 1:15
    normal_img_vectors(:,i) = vectorized_img(:,6*i);
end
```

A

```
cnt=0;
for i = 1:90
    curr_img = vectorized_img(:,i);
    d = Inf;
    index =i;
    for j = 1 : 15
        v = curr_img - normal_img_vectors(:,j);
        if d \ge norm(v)
            index=j;
            d = norm(v);
        end
    end
    % index cross checking
    if 6*index - i <= 5 && 6*index - i >=0
        fprintf('%d Yes\n', i);
        cnt = cnt+1;
    else
        fprintf('%d No\n', i);
    end
end
```

```
1 Yes2 Yes3 Yes4 No5 No
```

- 6 Yes
- 7 Yes
- 8 Yes
- 9 Yes
- 10 Yes
- 11 Yes
- 12 Yes
- 13 No
- 14 Yes
- 15 Yes
- 16 No
- 17 Yes
- 18 Yes
- 19 Yes
- 20 Yes
- 21 Yes
- 22 No
- 23 Yes
- 24 Yes 25 Yes
- 26 Yes
- 27 Yes
- 28 No
- 29 Yes 30 Yes
- 31 No
- 32 Yes
- 33 Yes
- 34 No
- 35 Yes
- 36 Yes
- 37 No
- 38 Yes
- 39 Yes
- 40 No
- 41 Yes 42 Yes
- 43 Yes
- 44 Yes
- 45 Yes
- 46 No
- 47 No
- 48 Yes 49 No
- 50 No
- 51 Yes
- 52 No
- 53 Yes
- 54 Yes
- 55 No
- 56 No 57 Yes
- 58 No
- 59 Yes
- 60 Yes
- 61 Yes
- 62 Yes 63 Yes
- 64 Yes
- 65 Yes
- 66 Yes
- 67 No 68 No
- 69 No

```
70 Yes
 71 Yes
 72 Yes
 73 No
 74
    Yes
 75
    Yes
 76 No
 77
    Yes
 78 Yes
 79 Yes
 80 Yes
 81 Yes
 82 No
 83 Yes
 84 Yes
 85 Yes
 86 No
 87 Yes
 88 No
 89 No
 90 Yes
 disp(['The normal image classifier :'])
 The normal image classifier :
 cnt
 cnt = 63
B
 pcs = zeros(77760,15)
 pcs = 77760 \times 15
                                                                 0 . . .
     0
          0
               0
                    0
                         0
                              0
                                   0
                                        0
                                             0
                                                  0
                                                       0
                                                            0
     0
          0
               0
                    0
                         0
                              0
                                   0
                                        0
                                             0
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                                                            0
                                                                 0
     0
          0
              0
                    0
                         0
                              0
                                   0
     0
          0 0
                   0
                        0
                                        0
                                             0
                             0
                                   0
                                                  0
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                                                                 0
         0 0
     0
                 0
                        0
                             0
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                                                            0
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     0
         0 0
                 0
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     0
         0 0
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     0
         0
              0
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     0
         0
              0
                   0
                        0
                                   0
                                        0
                                             0
                                                  0
                                                       0
                                                            0
                                                                 0
                              0
     0
          0
               0
                    0
                         0
                              0
                                   0
                                        0
                                             0
                                                  0
                                                       0
                                                            0
                                                                 0
 for i = 1:15
     cd = vectorized_img(:,6*i-5:6*i);
     cd_sf = cd - mean(cd,1);
     c = cov(cd_sf);
     [e v] = eig(c);
     eval = diag(v);
     [~,ind] = sort(eval);
     new_data = cd*e(:,ind(6));
     new_data_rec= rescale(new_data,0,255);
     pcs(:,i) = new_data_rec;
```

end

```
pcs = 77760 \times 15
 115.0706 113.1425 127.5477 129.4189 110.2082 111.6888 127.3599 128.4888 ...
 255.0000 239.8999 255.0000 255.0000 253.3127 241.6530 255.0000 255.0000
 255.0000 252.7023 255.0000 255.0000 255.0000 255.0000
                                                          255.0000 255.0000
                                                255.0000
 255.0000 255.0000 255.0000 255.0000
                                       255.0000
                                                          255.0000 255.0000
 255.0000 255.0000 255.0000 255.0000
                                       255.0000
                                                255.0000
                                                          255.0000 255.0000
 255.0000 255.0000 255.0000
                             255.0000
                                                249.7864
                                       255.0000
                                                          255.0000 255.0000
 255.0000 255.0000
                    255.0000
                             255.0000
                                       255.0000
                                                212.5798
                                                          255.0000
                                                                   255.0000
 255.0000 255.0000
                    255.0000 255.0000
                                       255.0000
                                                222.1669
                                                          255.0000 255.0000
 255.0000 255.0000
                    255.0000 255.0000
                                       255.0000
                                                245.7935
                                                          255.0000 255.0000
 255.0000 255.0000 255.0000 255.0000 255.0000 254.1883 255.0000 255.0000
B = reshape(pcs(:,1),[243,320]);
B = uint8(B);
imshow(B)
```



```
cnt=0;
idx = zeros(90,1);
for i =1:90
    curr_img = vectorized_img(:,i);
    d = Inf;
    index =i;
    for j = 1 : 15
        v = curr_img - pcs(:,j);
        if d >= norm(v)
```

```
index=j;
    d = norm(v);
    end
end
% index cross checking
if 6*index - i <= 5 && 6*index - i >=0
    fprintf('%d Yes\n', i);
    cnt = cnt+1;
    idx(i)=1;
else
    fprintf('%d No\n', i);
end
end
```

```
1 Yes
2 Yes
3 Yes
4 Yes
5 No
6 Yes
7 Yes
8 Yes
9 Yes
10 Yes
11 Yes
12 Yes
13 Yes
14 Yes
15 Yes
16 No
17 Yes
18 Yes
19 Yes
20 Yes
21 Yes
22 No
23 Yes
24 Yes
25 Yes
26 Yes
27 Yes
28 No
29 Yes
30 Yes
31 No
32 Yes
33 Yes
34 No
35 Yes
36 Yes
37 Yes
38 Yes
39 Yes
40 No
41 Yes
42 Yes
43 Yes
44 Yes
45 Yes
```

46 No

```
47 Yes
48 Yes
49
   Yes
50 Yes
51
   Yes
52 No
53
   Yes
54 Yes
55 Yes
56 Yes
57 Yes
58 No
59 Yes
60 Yes
61 Yes
62 Yes
63 Yes
64 Yes
65 Yes
66 Yes
67 No
68 Yes
69 No
70 Yes
71 Yes
72 Yes
73 Yes
74 Yes
75 Yes
76 No
77 Yes
78 Yes
79 Yes
80 Yes
81 Yes
82 Yes
83 Yes
84 Yes
85 Yes
86 Yes
87 Yes
88 No
89 Yes
90 Yes
disp(['Classification with 1 rep. image :'])
Classification with 1 rep. image :
cnt
cnt = 76
```

C

```
pcs2 = zeros(77760,15);
for i = 1:15
    cd = vectorized_img(:,6*i-5:6*i);
    cd_sf = cd - mean(cd,1);
    c = cov(cd_sf);
    [e v] = eig(c);
```

```
eval = diag(v);
    [~,ind] = sort(eval);
    new data = cd*(e(:,ind(5))+e(:,ind(6)));
    new_data_rec= rescale(new_data,0,255);
    pcs2(:,i) = new_data_rec;
end
pcs2
pcs2 = 77760 \times 15
  96.3478 109.0976 122.3422 118.8471 93.6104 113.5731 112.8257 112.0121 • • •
 217.8103 206.1546 215.1518 211.0361 208.9911 173.9626 206.1240 202.1891
 217.8103 220.5893 215.1518 211.0361 211.0081 185.7797 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 185.7797 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 185.7797 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 181.1593 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 148.4990 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 157.0336 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 177.7378 206.1240 202.1891
  217.8103 223.1495 215.1518 211.0361 211.0081 184.9638 206.1240 202.1891
pcs2
pcs2 = 77760 \times 15
  96.3478 109.0976 122.3422 118.8471 93.6104 113.5731 112.8257 112.0121 • • •
 217.8103 206.1546 215.1518 211.0361 208.9911 173.9626 206.1240 202.1891
 217.8103 220.5893 215.1518 211.0361 211.0081 185.7797 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 185.7797 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 185.7797
                                                        206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 181.1593 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 148.4990 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 157.0336 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 177.7378 206.1240 202.1891
 217.8103 223.1495 215.1518 211.0361 211.0081 184.9638 206.1240 202.1891
B = reshape(pcs2(:,1),[243,320]);
B = uint8(B);
imshow(B)
```



```
cnt=0;
for i = 1:90
    curr_img = vectorized_img(:,i);
    d = Inf;
    index =i;
    for j = 1 : 15
        v = curr_img - pcs2(:,j);
        if d >= norm(v)
            index=j;
            d = norm(v);
        end
    end
    % index cross checking
    if 6*index - i <= 5 && 6*index - i >=0
        fprintf('%d Yes\n', i);
        cnt = cnt+1;
        idx(i)=1;
    else
        fprintf('%d No\n', i);
    end
end
```

```
2 Yes
3 Yes
```

1 Yes

- 4 No
- 5 No
- 6 Yes
- 7 Yes
- 8 Yes
- 9 Yes
- 10 No
- 11 Yes
- 12 Yes
- 13 No
- 14 Yes
- 15 Yes
- 16 No
- 17 Yes
- 18 Yes
- 19 Yes
- 20 Yes
- 21 Yes
- 22 No
- 23 Yes
- 24 Yes
- 25 Yes
- 26 Yes
- 27 Yes
- 28 No
- 29 Yes
- 30 Yes
- 31 No
- 32 Yes
- 33 Yes
- 34 No
- 35 Yes
- 36 Yes
- 37 No
- 38 Yes
- 39 Yes
- 40 No
- 41 Yes 42 Yes
- 43 Yes
- 44 Yes
- 45 Yes
- 46 No
- 47 No
- 48 Yes
- 49 No
- 50 No
- 51 Yes
- 52 No 53 Yes
- 54 Yes
- 55 No
- 56 No
- 57 Yes 58 No
- 59 Yes
- 60 Yes
- 61 Yes
- 62 Yes 63 Yes
- 64 Yes
- 65 Yes
- 66 Yes

```
67 No
68 No
69
   No
70
   Yes
71
   Yes
72
   Yes
73
   Yes
74 Yes
75
   Yes
76 No
77 Yes
78 Yes
79 Yes
80 Yes
81 Yes
82 No
83 Yes
84 Yes
85 Yes
86 Yes
87 Yes
88 No
89 Yes
90 No
disp(['Classification with 2 rep. images : '])
Classification with 2 rep. images :
cnt
cnt = 64
cnt_t=0;
for i=1:90
    if idx(i) == 1
         cnt_t = cnt_t+1;
    end
end
disp(['Unique classfications :'])
Unique classfications :
cnt_t
cnt_t = 76
```

Conclusion: In this question increasing the number of principal components does not necessarily mean that we will be able to classify more images correctly because effectively, we are obtaining a resultant image from 6 images belonging to a subject. This can improve the classification of one image as well and can reduce the classification accuracy of another image, as the number of principal components increases.