

## 第一題

### Euler Method ( $h = 0.1$ )

t	Euler	Exact	Error (Euler)
1.000000	0.000000	0.000000	0.000000
1.100000	0.100000	0.105160	0.005160
1.200000	0.209917	0.221243	0.011325
1.300000	0.330471	0.349121	0.018651
1.400000	0.462354	0.489682	0.027328
1.500000	0.606285	0.643875	0.037590
1.600000	0.763041	0.812753	0.049711
1.700000	0.933475	0.997494	0.064019
1.800000	1.118537	1.199439	0.080902
1.900000	1.319293	1.420116	0.100823
2.000000	1.536943	1.661282	0.124338

### Taylor 2nd Order Method ( $h = 0.1$ )

t	Taylor 2nd	Exact	Error (Taylor 2nd)
1.000000	0.000000	0.000000	0.000000
1.100000	0.105000	0.105160	0.000160
1.200000	0.220919	0.221243	0.000324
1.300000	0.348612	0.349121	0.000509
1.400000	0.488954	0.489682	0.000728
1.500000	0.642883	0.643875	0.000993
1.600000	0.811438	0.812753	0.001315
1.700000	0.995787	0.997494	0.001707
1.800000	1.197252	1.199439	0.002187

1.900000	1.417344	1.420116	0.002772
2.000000	1.657795	1.661282	0.003487

## 第二題

### RK4 Results (h = 0.1)

t	u1_RK4	u1_exact	err_u1	u2_RK4	u2_exact	err_u2
0.0000 0000	1.33333333	1.3333 3333	0.00000000	0.66666667	0.6666 6667	0.00000000
0.1000 0000	-3.05243707	1.7930 6259	4.84549965	8.98930534	- 1.0320 0245	10.02130780
0.2000 0000	- 23.84779486	1.4239 0240	25.27169730	51.19270400	- 0.8746 8103	52.06738500
0.3000 0000	- 130.1652017 1	1.1315 7652	131.2967780 0	269.2691931 7	- 0.7249 9857	269.9941920 0
0.4000 0000	- 680.2314850 9	0.9094 0859	681.1408940 0	1399.368583 50	- 0.6082 1421	1399.976800 00
0.5000 0000	- 3531.299585 37	0.7387 8784	3532.038370 00	7258.241838 84	- 0.5156 5767	7258.757500 00
0.6000 0000	- 18312.79505 221	0.6057 0965	18313.40080 000	37634.95548 298	- 0.4404 1076	37635.39590 000
0.7000 0000	- 94951.33190 728	0.4998 6025	94951.83180 000	195131.8717 3536	- 0.3774 0382	195132.2490 0000
0.8000 0000	- 492306.4656	0.4136 7148	492306.8790 0000	1011721.872 07795	- 0.3229	1011722.200 00000

	3948				5352	
0.9000 0000	- 2552513.623 86741	0.3416 1435	2552513.970 00000	5245578.826 58988	- 0.2744 0884	5245579.100 00000
1.0000 0000	- 13234278.78 916787	0.2796 7491	13234279.10 000000	27197287.20 658695	- 0.2298 8784	27197287.40 000000

#### RK4 Results (h = 0.05)

t	u1_RK4	u1_exact	err_u1	u2_RK4	u2_exact	err_u2
0.0000000 0	1.3333333 3	1.3333333 3	0.0000000 0	0.6666666 7	0.6666666 7	0.0000000 0
0.0500000 0	1.7218802 6	1.9120586 3	0.1901783 8	- 0.4995993 4	- 0.9090765 9	0.4094772 4
0.1000000 0	1.7269150 5	1.7930625 9	0.0661475 4	- 0.8325977 1	- 1.0320024 5	0.1994047 5
0.1500000 0	1.6171606 3	1.6019667 6	0.0151938 7	- 0.8903729 9	- 0.9614587 1	0.0710857 2
0.2000000 0	1.4816872 9	1.4239024 0	0.0577848 9	- 0.8610420 9	- 0.8746810 3	0.0136389 4
0.2500000 0	1.3489450 3	1.2676456 2	0.0812994 1	- 0.8075045 3	- 0.7952207 7	0.0122837 6
0.3000000 0	1.2270633 0	1.1315765 2	0.0954867 8	- 0.7503406 3	- 0.7249985 7	0.0253420 6
0.3500000 0	1.1174781 2	1.0129985 6	0.1044795 7	- 0.6958859 1	- 0.6630596 3	0.0328262 9
0.4000000	1.0195254	0.9094085	0.1101168	- 0.6457317	- 0.6082142	0.0375175

0	6	9	7	6	1	5
0.4500000 0	0.9319766 7	0.8186295 3	0.1133471 3	- 0.5999342 4	- 0.5593892 5	0.0405449 9
0.5000000 0	0.8535405 1	0.7387878 4	0.1147526 7	- 0.5580924 9	- 0.5156576 7	0.0424348 2
0.5500000 0	0.7830172 7	0.6682746 6	0.1147426 1	- 0.5197062 7	- 0.4762247 5	0.0434815 2
0.6000000 0	0.7193370 2	0.6057096 5	0.1136273 7	- 0.4842903 0	- 0.4404107 6	0.0438795 5
0.6500000 0	0.6615602 9	0.5499094 1	0.1116508 8	- 0.4514070 6	- 0.4076353 4	0.0437717 2
0.7000000 0	0.6088676 6	0.4998602 5	0.1090074 1	- 0.4206726 2	- 0.3774038 2	0.0432688 0
0.7500000 0	0.5605468 4	0.4546947 4	0.1058521 1	- 0.3917540 8	- 0.3492955 1	0.0424585 7
0.8000000 0	0.5159800 5	0.4136714 8	0.1023085 7	- 0.3643646 8	- 0.3229535 2	0.0414111 6
0.8500000 0	0.4746325 7	0.3761577 1	0.0984748 6	- 0.3382585 9	- 0.2980760 5	0.0401825 4
0.9000000 0	0.4360426 2	0.3416143 5	0.0944282 7	- 0.3132261 0	- 0.2744088 4	0.0388172 7
0.9500000 0	0.3998123 1	0.3095830 0	0.0902293 0	- 0.2890892 6	- 0.2517386 8	0.0373505 7
1.0000000	0.3655998	0.2796749	0.0859249	-	-	0.0358101

0	3	1	2	0.2656979 9	0.2298878 4	5
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