冬

概述

黄药师道:"你拿了这图,到临安府找一家客店或是寺观住下,三月之后,我派人前来取回。图中一切,只许心记,不得另行抄录印摹。"

邓 後 辉 deng@tsinghua.edu.cn

基本术语



edge|arc: e = |E|



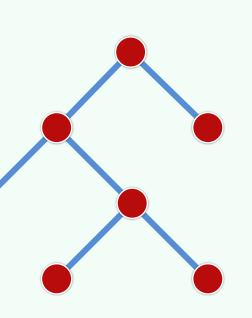
同一顶点自我邻接,构成自环(self-loop)

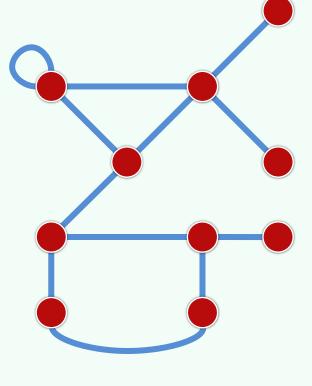
不含自环及重边,即为简单图(simple graph)

非简单(non-simple)图,暂不讨论

❖ 顶点与其所属的边,彼此关联(incidence)

度 (degree/valency): 与同一顶点关联的边数



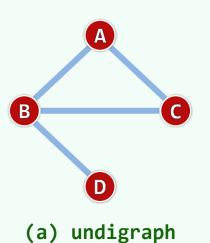


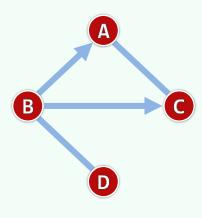
无向图 + 有向图

❖ 若邻接顶点u和v的次序无所谓

则(u, v)**为无向边 (undirected edge)**

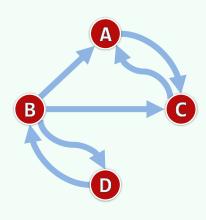
❖ 所有边均无方向的图,即无向图(undigraph)





(b) mixed graph

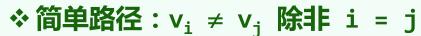
- ❖ 反之,有向图(digraph)中均为有向边(directed edge)
 - u、v分别称作边(u, v)的尾(tail)、头(head)
- ❖ 无向边、有向边并存的图 , 称作混合图 (mixed graph)
- ❖ 有向图通用性更强,故本章主要针对有向图介绍相关结构及算法



(c) digraph

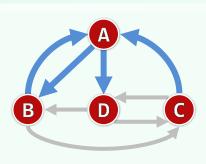
路径 + 环路

*路径
$$\pi = \langle V_0, V_1, \ldots, V_k \rangle$$
长度 $|\pi| = k$

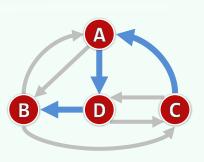


- ❖环/环路:v₀ = vk
- ❖有向无环图(DAG)
- ❖ 哈密尔顿环路: |π| = |V|

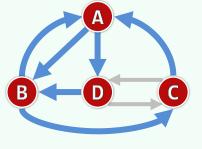
各顶点恰好出现一次



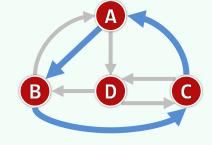




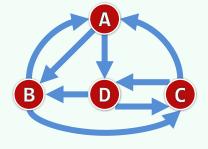
(ii) simple path



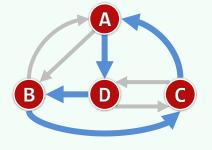
(i) cycle



(ii) simple cycle



(i) Eulerian tour

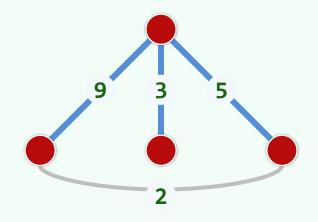


(ii) Hamiltonian tour

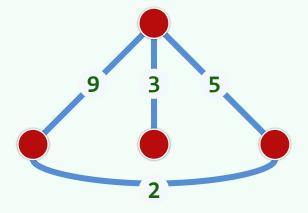
支撑树 + 带权网络 + 最小支撑树

❖图G = (V; E)的子图T = (V; F)若是树,即为其支撑树(spanning tree)

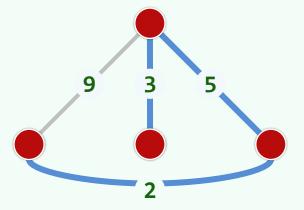
同一图的支撑树,通常并不唯一



spanning tree



weighted network
(triangle inequality?)



minimum spanning tree

- ❖ 各边e均有对应的权值wt(e),则为带权网络(weighted network)
- ❖ 同一网络的支撑树中,总权重最小者为最小支撑树(MST)