BST Application

Range Query: 1D

你这个人太敏感了。这个社会什么都需要,唯独不需要敏感。

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1D Range Query

- \clubsuit Let $P = \{ p_1, p_2, p_3, \ldots, p_n \}$ be a set of n points on the x-axis
- **�** For any given interval $I = (x_1, x_2]$
 - COUNTING: how many points of P lies in the interval?
 - REPORTING: enumerate all points in $I \cap P$ (if not empty)
- ❖[Online] P is fixed while I is randomly and repeatedly given
- ❖ How to PREPROCESS P into a certain data structure s.t. the queries can be answered efficiently?



Brute-Force

- lacktriangle For each point p of P, test if $p \in (x_1, x_2]$
- ❖ Thus each query can be answered in LINEAR time
- ❖ Can we do it faster? It seems we can't, for ...
- ❖ In the worst case,

the interval contains up to O(n) points, which need O(n) time to enumerate

❖ However, how if we

ignore the time for enumerating and count only the searching time?



Binary Search

- ❖ Sort all points into a sorted vector and add an extra sentinel $p[0] = -\infty$
- \clubsuit For any interval $I = (x_1, x_2]$
 - Find $t = search(x_2) = max\{ i \mid p[i] \le x_2 \} //O(logn)$
 - Traverse the vector BACKWARD from p[t] and report each point //o(r)
 - until escaping from I at point p[s]
 - return r = t s //output size



Output-Sensitivity

- \diamondsuit An enumerating query can be answered in O(r + logn) time
- p[s] can also be found by binary search in o(logn) time
- ❖ Hence for COUNTING query, ⊘(logn) time is enough //independent to r
- ❖ Can this simple strategy be extended to PLANAR range query?

TTBOMK, unfortunately, no!

