myHDL Combinational Logic Elements: Multiplexers (MUXs))

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1 Refrances

@misc{xu_2018, title={Introduction to Digital Systems Supplementary Reading Shannon's Expansion Formulas and Compressed Truth Table}, author={Xu, Xuping}, year={Fall 2017} site=http://ecse.bd.psu.edu/cse271/comprttb.pdf (http://ecse.bd.psu.edu/cse271/comprttb.pdf) }

2 Libraries and Helper functions

```
In [1]: ▼ #This notebook also uses the `(some) LaTeX environments for Jupyter`
          #https://github.com/ProfFan/latex envs wich is part of the
          #jupyter_contrib_nbextensions package
          from myhdl import *
          from myhdlpeek import Peeker
          import numpy as np
          import pandas as pd
          import matplotlib.pyplot as plt
          %matplotlib inline
          from sympy import *
          init_printing()
          import itertools
          #https://github.com/jrjohansson/version_information
          %load_ext version_information
          %version information myhdl, myhdlpeek, numpy, pandas, matplotlib, sympy
Out[1]:
```

	,
Version	Software
3.6.2 64bit [GCC 4.4.7 20120313 (Red Hat 4.4.7-1)]	Python
6.2.1	IPython
Linux 4.15.0 30 generic x86_64 with debian stretch sid	os
0.10	myhdl
0.0.6	myhdlpeek
1.13.3	numpy
0.23.4	pandas
2.1.0	matplotlib
1.3	sympy
The 'itertools' distribution was not found and is required by the application	itertools
0.3.0	SchemDraw

Sun Sep 23 18:19:19 2018 MDT

```
def VerilogTextReader(loc, printresult=True):
              with open(f'{loc}.v', 'r') as vText:
                  VerilogText=vText.read()
              if printresult:
                  print(f'***Verilog modual from {loc}.v***\n\n', VerilogText)
              return VerilogText
          def VHDLTextReader(loc, printresult=True):
              with open(f'{loc}.vhd', 'r') as vText:
                  VerilogText=vText.read()
              if printresult:
                  print(f'***VHDL modual from {loc}.vhd***\n\n', VerilogText)
              return VerilogText
          def ConstraintXDCTextReader(loc, printresult=True):
              with open(f'{loc}.xdc', 'r') as xdcText:
                  ConstraintText=xdcText.read()
              if printresult:
                  print(f'***Constraint file from {loc}.xdc***\n\n', ConstraintTe
              return ConstraintText
In [3]: | def TruthTabelGenrator(BoolSymFunc):
              Function to generate a truth table from a sympy boolian expression
              BoolSymFunc: sympy boolian expression
              return TT: a Truth table stored in a pandas dataframe
              colsL=sorted([i for i in list(BoolSymFunc.rhs.atoms())], key=lambda
              colsR=sorted([i for i in list(BoolSymFunc.lhs.atoms())], key=lambda
              bitwidth=len(colsL)
              cols=colsL+colsR; cols
              TT=pd.DataFrame(columns=cols, index=range(2**bitwidth))
              for i in range(2**bitwidth):
                  inputs=[int(j) for j in list(np.binary_repr(i, bitwidth))]
                  outputs=BoolSymFunc.rhs.subs({j:v for j, v in zip(colsL, inputs
                  inputs.append(int(bool(outputs)))
                  TT.iloc[i]=inputs
              return TT
```

In [2]: ▼ #helper functions to read in the .v and .vhd generated files into pyth

3 Multiplexers

Definition 1 A Multiplexer, typically referred to as a MUX, is a Digital(or analog) switching unit that picks one input channel to be streamed to an output via a control input. For single output MUXs with 2^n inputs, there are then n input selection signals that make up the control word to select the input channel for output.

From a behavioral standpoint, a MUX can be thought of as an element that performs the same functionality as the if-elif-else (case) control statements found in almost every software language.

4 2 Channel Input:1 Channel Output multiplexer in Gate Level Logic

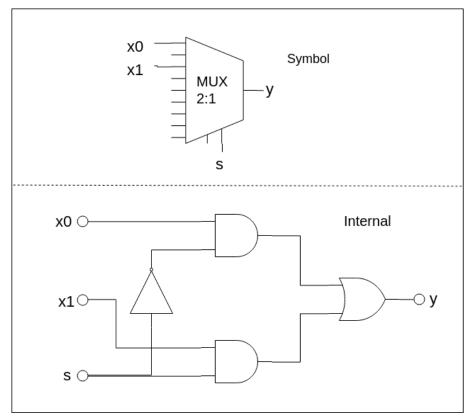


Figure 1: 2:1 MUX Symbol and Gate internals

4.1 Sympy Expression

```
x0, x1, s, y=symbols('x0, x1, s, y')
In [4]:
          y21Eq=Eq(y, (~s\&x0) | (s\&x1) ); y21Eq
```

Out[4]: $y = (s \wedge x_1) \vee (x_0 \wedge \neg s)$

```
In [5]:
          TruthTabelGenrator(y21Eq)[[x1, x0, s, y]]
Out[5]:
            x1 x0 s y
                0 0 0
         1
            1
                0 0 0
         2
            0
                1 0 1
            1
               1 0 1
            0
                0 1 0
         5
            1
               0 1 1
         6
            0 1 1 0
            1 1 1 1
In [6]:
          y21EqN=lambdify([x0, x1, s], y21Eq.rhs, dummify=False)
          SystmaticVals=np.array(list(itertools.product([0,1], repeat=3)))
          print(SystmaticVals)
          y21EqN(SystmaticVals[:, 1], SystmaticVals[:, 2], SystmaticVals[:, 0]).a
         [0 0 0]
          [0 \ 0 \ 1]
          [0 \ 1 \ 0]
          [0\ 1\ 1]
          [1 \ 0 \ 0]
          [1 0 1]
          [1 \ 1 \ 0]
          [1 \ 1 \ 1]
Out[6]: array([0, 0, 1, 1, 0, 1, 0, 1])
```

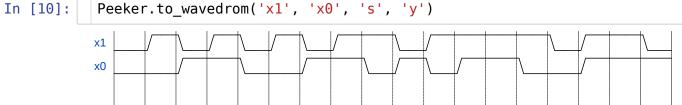
▼ 4.2 myHDL Module

4.3 myHDL Testing

18)

```
In [8]: ▼ #generate systmatic and random test values
          #stimules inputs X1 and X2
          TestLen=10
          SystmaticVals=list(itertools.product([0,1], repeat=3))
          xOTVs=np.array([i[1] for i in SystmaticVals]).astype(int)
          np.random.seed(15)
          x0TVs=np.append(x0TVs, np.random.randint(0,2, TestLen)).astype(int)
          x1TVs=np.array([i[2] for i in SystmaticVals]).astype(int)
          #the random genrator must have a differint seed beween each generation
          #call in order to produce differint values for each call
          np.random.seed(16)
          x1TVs=np.append(x1TVs, np.random.randint(0,2, TestLen)).astype(int)
          sTVs=np.array([i[0] for i in SystmaticVals]).astype(int)
          #the random genrator must have a differint seed beween each generation
          #call in order to produce differint values for each call
          np.random.seed(17)
          sTVs=np.append(sTVs, np.random.randint(0,2, TestLen)).astype(int)
          TestLen=len(x0TVs)
          x0TVs, x1TVs, sTVs, TestLen
Out[8]: (array([0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1]),
         array([0, 1, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0]),
         array([0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 1]),
```

```
In [9]:
          Peeker.clear()
          x0=Signal(bool(0)); Peeker(x0, 'x0')
          x1=Signal(bool(0)); Peeker(x1, 'x1')
          s=Signal(bool(0)); Peeker(s, 's')
          y=Signal(bool(0)); Peeker(y, 'y')
          DUT=MUX2_1\_Combo(x0, x1, s, y)
          def MUX2_1_Combo_TB():
              myHDL only testbench for module `MUX2_1_Combo`
              @instance
              def stimules():
                  for i in range(TestLen):
                      x0.next=int(x0TVs[i])
                      x1.next=int(x1TVs[i])
                      s.next=int(sTVs[i])
                      yield delay(1)
                  raise StopSimulation()
              return instances()
          sim=Simulation(DUT, MUX2_1_Combo_TB(), *Peeker.instances()).run()
          Peeker.to_wavedrom('x1', 'x0', 's', 'y')
```



```
MUX2_1_ComboData=Peeker.to_dataframe()
In [11]:
           MUX2_1_ComboData=MUX2_1_ComboData[['x1', 'x0', 's', 'y']]
           MUX2_1_ComboData
Out[11]:
              x1 x0 s y
           0
              0
                  0 0 0
           1
                  0 0 0
              1
           2
              0
                  1 0 1
           3
              1
                  1 0 1
              0
                  0 1 0
           5
                  0 1 1
              1
                  1 1 0
           7
              1
                  1 1 1
           8
                  0 1 1
              1
           9
                  1 1 0
          10
              1
                  0 1 1
In [12]:
           MUX2_1_ComboData['yRef']=MUX2_1_ComboData.apply(lambda row:y21EqN(row['
           MUX2_1_ComboData
Out[12]:
              x1 x0 s y yRef
              0
                  0 0 0
                            0
           1
              1
                  0 0 0
                           0
           2
              0
                  1 0 1
                           1
           3
                  1 0 1
              1
                           1
                  0 1 0
                            0
           4
              0
                  0 1 1
                           1
           6
                 1 1 0
                            0
              0
           7
               1
                  1 1 1
                           1
           8
              1
                  0 1 1
                           1
                  1 1 0
                            0
           9
              0
          10
                  0 1 1
                           1
          11
                  1 0 1
              1
                           1
          13
              1
                  0 1 1
                           1
          14
                  0 0 0
                            0
          15
              1
                  1 1 1
                           1
          16
                  1 0 1
                           1
              1
```

1 1 0

```
In [13]: Test=(MUX2_1_ComboData['y']==MUX2_1_ComboData['yRef']).all()
    print(f'Module `MUX2_1_Combo` works as exspected: {Test}')

Module `MUX2 1 Combo` works as exspected: True
```

4.4 Verilog Conversion

```
In [14]:
                                                  DUT.convert()
                                                  VerilogTextReader('MUX2 1 Combo');
                                          ***Verilog modual from MUX2 1 Combo.v***
                                              // File: MUX2_1_Combo.v
                                           // Generated by MyHDL 0.10
                                          // Date: Sun Sep 23 18:19:36 2018
                                           `timescale 1ns/10ps
                                          module MUX2 1 Combo (
                                                            χ0,
                                                             x1,
                                                             S,
                                                             У
                                           );
                                          // 2:1 Multiplexer written in full combo
                                          // Input:
                                          //
                                                                          x0(bool): input channel 0
                                                                          x1(bool): input channel 1
                                           //
                                                                                   ullet 
                                                                                                                                                                                                                                                                               RTL OR
```

Figure 2: MUX2 1 Combo RTL schematic; Xilinx Vivado 2017.4

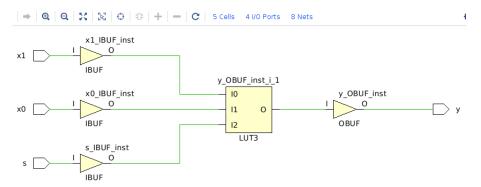


Figure 3: MUX2_1 Combo Synthesized Schematic; Xilinx Vivado 2017.4

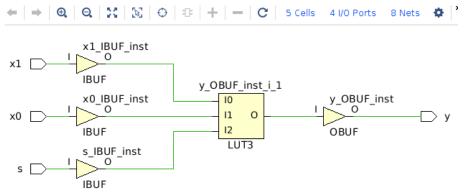


Figure 4: MUX2_1_Combo Implementated Schematic; Xilinx Vivado 2017.4

4.5 myHDL to Verilog Testbench

```
In [16]:
           @block
           def MUX2_1_Combo_TBV():
                myHDL -> Verilog testbench for module `MUX2 1 Combo`
                x0=Signal(bool(0))
                x1=Signal(bool(0))
                s=Signal(bool(0))
                y=Signal(bool(0))
                @always comb
                def print_data():
                    print(x0, x1, s, y)
                #Test Signal Bit Vectors
                x0TV=Signal(x0TVs)
                x1TV=Signal(x1TVs)
                sTV=Signal(sTVs)
                DUT=MUX2 1 Combo(x0, x1, s, y)
                @instance
                def stimules():
                    for i in range(TestLen):
                        x0.next=int(x0TV[i])
                        x1.next=int(x1TV[i])
                        s.next=int(sTV[i])
                        yield delay(1)
                    raise StopSimulation()
                return instances()
           TB=MUX2 1 Combo TBV()
           TB.convert(hdl="Verilog", initial_values=True)
            VerilogTextReader('MUX2_1_Combo_TBV');
          <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
          <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
<class 'myhdl._Signal._Signal'> <class '_ast.Name'>
          <class 'myhdl. Signal. Signal'> <class 'ast.Name'>
          ***Verilog modual from MUX2_1_Combo_TBV.v***
          // File: MUX2_1_Combo_TBV.v
          // Generated by MyHDL 0.10
          // Date: Sun Sep 23 18:19:44 2018
          `timescale 1ns/10ps
         module MUX2 1 Combo TBV (
          );
          // myHDL -> Verilog testbench for module `MUX2 1 Combo`
```

reg x0 = 0;

```
reg x1 = 0;
reg s = 0;
wire y;
wire [17:0] x0TV;
wire [17:0] \times 1TV;
wire [17:0] sTV;
assign x0TV = 18'd52583;
assign x1TV = 18'd87798;
assign sTV = 18'd16277;
always @(s, y, x0, x1) begin: MUX2_1_COMBO_TBV_PRINT DATA
    $write("%h", x0);
    $write(" ");
    $write("%h", x1);
    $write(" ");
    $write("%h", s);
    $write(" ");
    $write("%h", y);
    $write("\n");
end
assign y = (((!s) \&\& x0) | (s \&\& x1));
initial begin: MUX2 1 COMBO TBV STIMULES
    integer i;
    for (i=0; i<18; i=i+1) begin
        x0 \le x0TV[i];
        x1 <= x1TV[i];
        s <= sTV[i];
        # 1;
    end
    $finish;
end
endmodule
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x0TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x1TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: sTV
  category=ToVerilogWarning
```

4.6 PYNQ-Z1 Deployment

▼ 4.6.1 Board Circuit

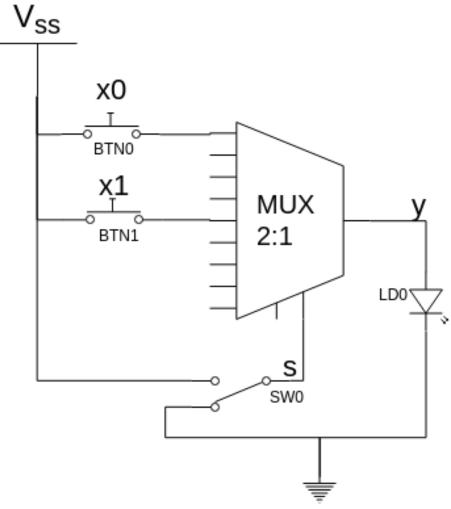


Figure 5: 2:1 MUX PYNQ-Z1 (Non SoC) conceptualized circuit

▼ 4.6.2 Board Constraint

```
In [17]:
           ConstraintXDCTextReader('MUX2 1');
         ***Constraint file from MUX2 1.xdc***
          ## PYNQ-Z1 Constraint File for MUX2 1 Combo
         ## Based on https://github.com/Xilinx/PYNQ/blob/master/boards/Pyng-Z1/b
         ase/vivado/constraints/base.xdc (https://github.com/Xilinx/PYNQ/blob/ma
         ster/boards/Pyng-Z1/base/vivado/constraints/base.xdc)
         ## Switches
         set property -dict {PACKAGE PIN M20 IOSTANDARD LVCMOS33} [get ports
          {s}]; ##SW0
         ## Buttons
         set property -dict {PACKAGE PIN D19 IOSTANDARD LVCMOS33} [get ports {x
         0}]; ## BT0
         set property -dict {PACKAGE PIN D20 IOSTANDARD LVCMOS33} [get ports {x
         1}]; ##BT1
         ## LEDs
         set_property -dict {PACKAGE_PIN R14 IOSTANDARD LVCMOS33} [get_ports
          {y}]; ## Led 0
```

4.6.3 Video of Deployment

MUX2_1_Combo myHDL PYNQ-Z1 (<u>YouTube (https://www.youtube.com/watch?v=UkXbnFdF010)</u>)

5 4 Channel Input : 1 Channel Output multiplexer in Gate Level Logic

5.1 Sympy Expression

```
In [18]: x_0, x_1, x_2, x_3, s_0, s_1, y=symbols('x_0, x_1, x_2, x_3, s_0, s_1, y')

y_41Eq=Eq(y, (\sim s_0 \sim s_1 \sim x_0) | (s_0 \sim s_1 \sim x_1) | (\sim s_0 \sim s_1 \sim x_0) | (s_0 \sim s_1 \sim x_0)

Out[18]: y = (s_0 \wedge s_1 \wedge x_3) \vee (s_0 \wedge x_1 \wedge \neg s_1) \vee (s_1 \wedge x_2 \wedge \neg s_0) \vee (x_0 \wedge \neg s_0 \wedge \neg s_1)
```

```
In [19]:
           TruthTabelGenrator(y41Eq)[[x3, x2, x1, x0, s1, s0, y]]
Out[19]:
              x3 x2 x1 x0 s1 s0
                                  У
           1
              1
                  0
                     0
                        0
                            0
                               0
                                 0
              0
                  1
                     0
                        0
                            0
                               0
              1
                  1
                     0
                        0
              0
                  0
                        0
                           0
                     1
                                 0
           5
                  0
                     1
                        0
                            0
           6
              0
                  1
                     1
                        0
                           0
           7
              1
                  1
                     1
                        0
                            0
                  0
                            0
           9
                     0
                        1
                               0
                                 1
              1
          10
                  1
                     0
                        1
                            0
           y41EqN=lambdify([x0, x1, x2, x3, s0, s1], y41Eq.rhs, dummify=False)
In [20]:
           SystmaticVals=np.array(list(itertools.product([0,1], repeat=6)))
           SystmaticVals
           y41EqN(*[SystmaticVals[:, i] for i in range(6)] ).astype(int)
Out[20]: array([0, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0, 0, 1, 0, 1, 0, 0, 1, 0, 0,
         0, 1,
                 1, 0, 1, 1, 0, 0, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 1, 1, 1, 0, 0,
          1, 1,
                 0, 1, 1, 0, 1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 1, 1, 1])
```

▼ 5.2 myHDL Module

```
In [21]:
           @block
          def MUX4_1_Combo(x0, x1, x2, x3, s0, s1, y):
               4:1 Multiplexer written in full combo
               Input:
                   x0(bool): input channel 0
                   x1(bool): input channel 1
                   x2(bool): input channel 2
                   x3(bool): input channel 3
                   s1(bool): channel selection input bit 1
                   s0(bool): channel selection input bit 0
               Output:
               y(bool): ouput
               @always_comb
               def logic():
                   y.next= (not s0 and not s1 and x0) or (s0 and not s1 and x1)
               return instances()
```

▼ 5.3 myHDL Testing

```
In [22]: ▼ #generate systmatic and random test values
           TestLen=5
           SystmaticVals=list(itertools.product([0,1], repeat=6))
           s0TVs=np.array([i[0] for i in SystmaticVals]).astype(int)
           np.random.seed(15)
           s0TVs=np.append(s0TVs, np.random.randint(0,2, TestLen)).astype(int)
           slTVs=np.array([i[1] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(16)
           s1TVs=np.append(s1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x0TVs=np.array([i[2] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(17)
           x0TVs=np.append(x0TVs, np.random.randint(0,2, TestLen)).astype(int)
           x1TVs=np.array([i[3] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(18)
           x1TVs=np.append(x1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x2TVs=np.array([i[4] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(19)
           x2TVs=np.append(x2TVs, np.random.randint(0,2, TestLen)).astype(int)
           x3TVs=np.array([i[5] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(20)
           x3TVs=np.append(x3TVs, np.random.randint(0,2, TestLen)).astype(int)
           TestLen=len(x0TVs)
           SystmaticVals, s0TVs, s1TVs, x3TVs, x2TVs, x1TVs, x0TVs, TestLen
Out[22]: ([(0, 0, 0, 0, 0, 0),
           (0, 0, 0, 0, 0, 1),
           (0, 0, 0, 0, 1, 0),
           (0, 0, 0, 0, 1, 1),
           (0, 0, 0, 1, 0, 0),
           (0, 0, 0, 1, 0, 1),
           (0, 0, 0, 1, 1, 0),
           (0, 0, 0, 1, 1, 1),
           (0, 0, 1, 0, 0, 0),
           (0, 0, 1, 0, 0, 1),
           (0, 0, 1, 0, 1, 0),
```

```
(0, 0, 1, 1, 0, 0),
           (0, 0, 1, 1, 0, 1),
           (0, 0, 1, 1, 1, 0),
           (0, 0, 1, 1, 1, 1),
           (0, 1, 0, 0, 0, 0),
           (0, 1, 0, 0, 0, 1),
           (0, 1, 0, 0, 1, 0),
In [23]:
           Peeker.clear()
           x0=Signal(bool(0)); Peeker(x0,
           x1=Signal(bool(0)); Peeker(x1,
                                           'x1')
           x2=Signal(bool(0)); Peeker(x2, 'x2')
           x3=Signal(bool(0)); Peeker(x3, 'x3')
           s0=Signal(bool(0)); Peeker(s0, 's0')
           s1=Signal(bool(0)); Peeker(s1, 's1')
           y=Signal(bool(0)); Peeker(y, 'y')
           DUT=MUX4_1_Combo(x0, x1, x2, x3, s0, s1, y)
           def MUX4_1_Combo_TB():
               myHDL only testbench for module `MUX4 1 Combo`
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TVs[i])
                       x1.next=int(x1TVs[i])
                       x2.next=int(x2TVs[i])
                       x3.next=int(x3TVs[i])
                       s0.next=int(s0TVs[i])
                       s1.next=int(s1TVs[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           sim=Simulation(DUT, MUX4_1_Combo_TB(), *Peeker.instances()).run()
In [24]:
           Peeker.to_wavedrom()
```

(0, 0, 1, 0, 1, 1),

```
In [25]:
            MUX4_1_ComboData=Peeker.to_dataframe()
            MUX4_1_ComboData=MUX4_1_ComboData[['x3', 'x2', 'x1', 'x0', 's1', 's0',
            MUX4_1_ComboData
Out[25]:
               x3 x2 x1 x0 s1 s0
                                    У
            0
                0
                   0
                       0
                          0
                              0
                                 0
                                    0
                1
                   0
            2
                0
                       0
                          0
                              0
                                 0
                                    0
                   1
            3
                       0
                          0
                              0
                                 0
                1
                   1
                                    0
                   0
                                 0
                       1
                   0
                          0
                              0
                                 0
                                    0
                1
                       1
                   1
                       1
                          0
                              0
            7
                1
                   1
                       1
                          0
                              0
                                 0
                                    0
            8
                   0
                       0
                              0
                          1
                                    1
                   0
           10
                              0
                0
                   1
                       0
                                 0
                          1
In [26]:
            MUX4_1_ComboData['yRef']=MUX4_1_ComboData.apply(lambda row:y41EqN(row[
            MUX4_1_ComboData
Out[26]:
               x3 x2 x1
                         x0 s1 s0
                                     y yRef
               0
                                 0
                                          0
                   0
                          0
                              0
                                 0
                                     0
                                          0
            1
                1
                       0
            2
                0
                   1
                       0
                          0
                              0
                                     0
                                          0
            3
                1
                   1
                       0
                          0
                              0
                                 0
                                     0
                                          0
                0
                   0
                       1
                          0
                              0
                                 0
                                     0
                                          0
                   0
                                          0
            6
                0
                   1
                          0
                              0
                                 0
                                     0
                                          0
                       1
            7
                1
                   1
                       1
                          0
                              0
                                 0
                                     0
                                          0
            8
                   0
                       0
                          1
                              0
                                 0
                                          1
            9
                   0
                1
                       0
                          1
                              0
                                          1
           10
                   1
                       0
                              0
                                          1
In [27]:
            Test=(MUX4 1 ComboData['y']==MUX4 1 ComboData['yRef']).all()
             print(f'Module `MUX4_1_Combo` works as exspected: {Test}')
          Module `MUX4_1_Combo` works as exspected: True
```

▼ 5.4 Verilog Conversion

```
In [28]:
                                               DUT.convert()
                                               VerilogTextReader('MUX4_1_Combo');
                                       ***Verilog modual from MUX4_1_Combo.v***
                                           // File: MUX4 1 Combo.v
                                        // Generated by MyHDL 0.10
                                        // Date: Sun Sep 23 18:20:10 2018
                                        `timescale 1ns/10ps
                                       module MUX4_1_Combo (
                                                        χ0,
                                                        x1,
                                                        x2,
                                                        х3,
                                                        s0,
                                                        s1,
                                                        У
                                        );
                                       // 4:1 Multiplexer written in full combo
                                       // Input:
                                       //
                                                                     x0(bool): input channel 0
                                                                     x1(bool): input channel 1
                                       //
                                       //
                                                                     x2(bool): input channel 2
                                                                     x3(bool): input channel 3
                                       //
                                                                     s1(bool): channel selection input bit 1
                                       //
                                                                     s0(bool): channel selection input bit 0
                                       // Output:
                                       //
                                                                     y(bool): ouput
                                       input x0;
                                       input x1;
                                       input x2;
                                       input x3;
                                       input s0;
                                       input s1;
                                       output y;
                                       wire y;
                                       assign y = (((!s0) \&\& (!s1) \&\& x0) || (s0 \&\& (!s1) \&\& x1) || ((!s0) \&\& x1) || ((!s0) \&\& x1) || ((!s0) \&\& x2) || ((!s0) \&\& x3) || ((!s0) \&\& x4) || ((!s0) \&\& x
                                       s1 && x2) || (s0 && s1 && x3));
```

endmodule

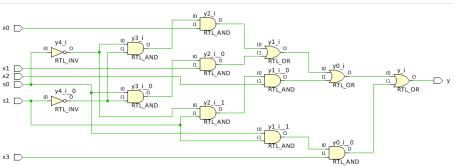


Figure 6: MUX4_1_Combo RTL schematic; Xilinx Vivado 2017.4

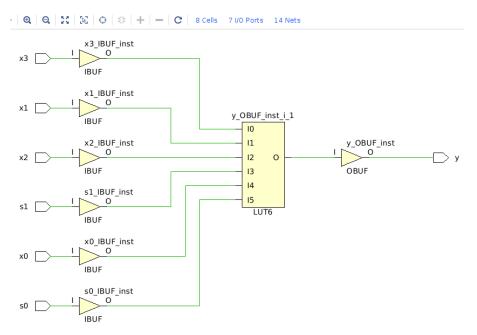


Figure 7: MUX4_1_Combo Synthesized Schematic; Xilinx Vivado 2017.4

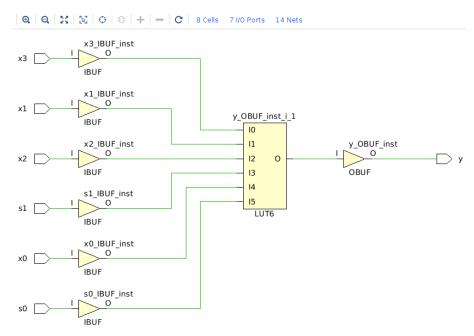


Figure 8: MUX4_1_Combo Implementated Schematic; Xilinx Vivado 2017.4

5.5 myHDL to Verilog Testbench

```
In [29]: ▼ #create BitVectors for MUX4 1 Combo TBV
       xOTVs=intbv(int(''.join(xOTVs.astype(str)), 2))[TestLen:]
       x1TVs=intbv(int(''.join(x1TVs.astype(str)), 2))[TestLen:]
x2TVs=intbv(int(''.join(x2TVs.astype(str)), 2))[TestLen:]
       x3TVs=intbv(int(''.join(x3TVs.astype(str)), 2))[TestLen:]
       sOTVs=intbv(int(''.join(sOTVs.astype(str)), 2))[TestLen:]
       s1TVs=intbv(int(''.join(s1TVs.astype(str)), 2))[TestLen:]
       x0TVs, bin(x0TVs), x1TVs, bin(x1TVs), x2TVs, bin(x2TVs), x3TVs, bin(x3TVs)
Out[29]: (intbv(2296870857426870268),
       intbv(34723282962276803050),
       intbv(118059162071741130356),
       intbv(196765270119568550582),
       0',
       intbv(137438953451),
       intbv(9007061817884663),
```

```
In [30]:
           @block
           def MUX4_1_Combo_TBV():
               myHDL -> Verilog testbench for module `MUX4 1 Combo`
               x0=Signal(bool(0))
               x1=Signal(bool(0))
               x2=Signal(bool(0))
               x3=Signal(bool(0))
               y=Signal(bool(0))
               s0=Signal(bool(0))
               s1=Signal(bool(0))
               @always_comb
               def print data():
                   print(x0, x1, x2, x3, s0, s1, y)
               #Test Signal Bit Vectors
               x0TV=Signal(x0TVs)
               x1TV=Signal(x1TVs)
               x2TV=Signal(x2TVs)
               x3TV=Signal(x3TVs)
               sOTV=Signal(sOTVs)
               s1TV=Signal(s1TVs)
               DUT=MUX4 1 Combo(x0, x1, x2, x3, s0, s1, y)
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TV[i])
                       x1.next=int(x1TV[i])
                       x2.next=int(x2TV[i])
                       x3.next=int(x3TV[i])
                       s0.next=int(s0TV[i])
                       s1.next=int(s1TV[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           TB=MUX4 1 Combo TBV()
           TB.convert(hdl="Verilog", initial_values=True)
           VerilogTextReader('MUX4_1_Combo_TBV');
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '</pre>
                                                   ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
```

Verilog modual from MUX4 1 Combo TBV.v

```
// File: MUX4 1 Combo TBV.v
// Generated by MyHDL 0.10
// Date: Sun Sep 23 18:20:16 2018
 `timescale 1ns/10ps
module MUX4_1_Combo_TBV (
// myHDL -> Verilog testbench for module `MUX4 1 Combo`
reg x0 = 0;
reg x1 = 0;
wire y;
reg x2 = 0;
reg x3 = 0;
reg s0 = 0;
reg s1 = 0;
wire [68:0] \times 0TV;
wire [68:0] x1TV;
wire [68:0] x2TV;
wire [68:0] x3TV;
wire [68:0] s0TV;
wire [68:0] s1TV;
assign x0TV = 69'd2296870857426870268;
assign x1TV = 69'd34723282962276803050;
assign x2TV = 69'd118059162071741130356;
assign x3TV = 69'd196765270119568550582;
assign sOTV = 69'd137438953451;
assign s1TV = 69'd9007061817884663;
always @(x0, x3, s0, x2, y, x1, s1) begin: MUX4_1_COMB0_TBV_PRINT_DATA
              $write("%h", x0);
              $write(" ");
              $write("%h", x1);
              $write(" ");
              $write("%h", x2);
              $write(" ");
              $write("%h", x3);
              $write(" ");
              $write("%h", s0);
              $write(" ");
             $write("%h", s1);
              $write(" ");
              $write("%h", y);
              $write("\n");
end
assign y = (((!s0) \&\& (!s1) \&\& x0) || (s0 \&\& (!s1) \&\& x1) || ((!s0) \&\& x
s1 && x2) || (s0 && s1 && x3));
```

```
initial begin: MUX4 1 COMBO TBV STIMULES
    integer i;
    for (i=0; i<69; i=i+1) begin
        x0 \le x0TV[i];
        x1 \ll x1TV[i];
        x2 <= x2TV[i];
        x3 <= x3TV[i];
        s0 <= s0TV[i];
        s1 <= s1TV[i];
        # 1;
    end
    $finish;
end
endmodule
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x0TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x1TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/_t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x2TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x3TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: s0TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/_t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: s1TV
  category=ToVerilogWarning
```

5.6 PYNQ-Z1 Deployment

▼ 5.6.1 Board Circuit

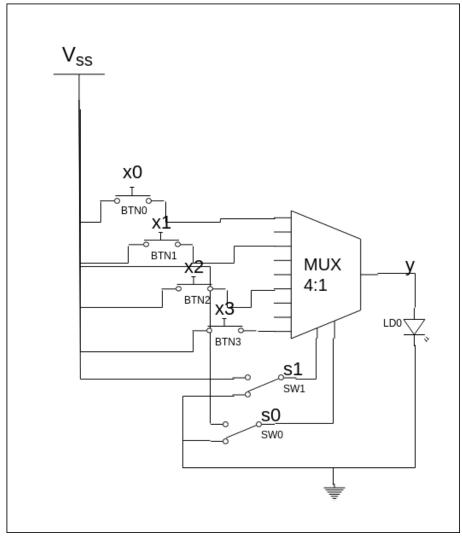


Figure 9: 4:1 MUX PYNQ-Z1 (Non SoC) conceptualized circuit

▼ 5.6.2 Board Constraint

```
In [31]:
           ConstraintXDCTextReader('MUX4 1');
         ***Constraint file from MUX4 1.xdc***
          ## PYNQ-Z1 Constraint File for MUX4 1 *
         ## Based on https://github.com/Xilinx/PYNQ/blob/master/boards/Pyng-Z1/b
         ase/vivado/constraints/base.xdc (https://github.com/Xilinx/PYNQ/blob/ma
         ster/boards/Pyng-Z1/base/vivado/constraints/base.xdc)
         ## Switches
         set property -dict {PACKAGE PIN M20 IOSTANDARD LVCMOS33} [get ports {s
         0}1; ## SW0
         set_property -dict {PACKAGE_PIN M19 IOSTANDARD LVCMOS33} [get_ports {s
         1}]; ## SW1
         ## Buttons
         set property -dict {PACKAGE PIN D19 IOSTANDARD LVCMOS33} [get ports {x
         0}1; ## BT0
         set_property -dict {PACKAGE_PIN D20 IOSTANDARD LVCMOS33} [get_ports {x
         1}]; ## BT1
         set property -dict {PACKAGE PIN L20 IOSTANDARD LVCMOS33} [get ports {x
         2}]; ## BT2
         set property -dict {PACKAGE PIN L19 IOSTANDARD LVCMOS33} [get ports {x
         3}1; ## BT3
```

LEDs set_property -dict {PACKAGE_PIN R14 IOSTANDARD LVCMOS33} [get_ports $\{y\}$]; ## Led 0

▼ 5.6.3 Video of Deployment

MUX4_1_MS myHDL PYNQ-Z1 (YouTube (https://www.youtube.com/watch?v=ZdwGjRM9WFk))

6 Shannon's Expansion Formula & Stacking of MUXs

<u>Claude Shannon (https://en.wikipedia.org/wiki/Claude_Shannon)</u>, of the famed Shannon-Nyquist theorem, discovered that any boolean expression $F(x_0, x_1, \ldots, x_n)$ can be decomposed in a manner akin to polynomials of perfect squares via

 $F(x_0,x_1,\ldots,x_n)=x_0\cdot F(x_0=1,x_1,\ldots,x_n)+\overline{x_0}\cdot F(x_0=0,x_1,\ldots,x_n)$ known as the Sum of Products (SOP) form since when the expansion is completed for all x_n the result is that

$$F(x_0, x_1, \dots, x_n) = \sum_{i=0}^{2^n - 1} (m_i \cdot F(m_i))$$

aka the Sum of all Minterms (m_i) belonging to the original boolean expression F factored down to the ith of n variables belonging to F and product (&) of F evaluated with the respective minterm as the argument

The Dual to the SOP form of Shannon's expansion formula is the Product of Sum (POS) form $F(x_0,x_1,\ldots,x_n)=(x_0+F(x_0=1,x_1,\ldots,x_n))\cdot (\overline{x_0}+F(x_0=0,x_1,\ldots,x_n))$ thus

$$F(x_0, x_1, \dots, x_n) = \prod_{i=0}^{2^n - 1} (M_i + F(M_i))$$

with M_i being the ith Maxterm

it is for this reason that Shannon's Expansion Formula is known is further liked to the fundamental theorem of algebra that it is called the "fundamental theorem of Boolean algebra"

So why then is Shannon's decomposition formula discussed in terms of Multiplexers. Because the general expression for a 2^n : 1 multiplexer is

$$y_{\text{MUX}} = \sum_{i=0}^{2^n - 1} m_i \cdot x_n$$

where then n is the required number of control inputs (referred to in this tutorial as s_i). Which is the same as the SOP form of Shannon's Formula for a boolean expression that has been fully decomposed (Factored). And further, if the boolean expression has not been fully factored we can replace n-1 parts of the partially factored expression with multiplexers. This then gives way to what is called "Multiplexer Stacking" in order to implement large boolean expressions and or large multiplexers

7 4 Channel Input: 1 Channel Output multiplexer via MUX Stacking

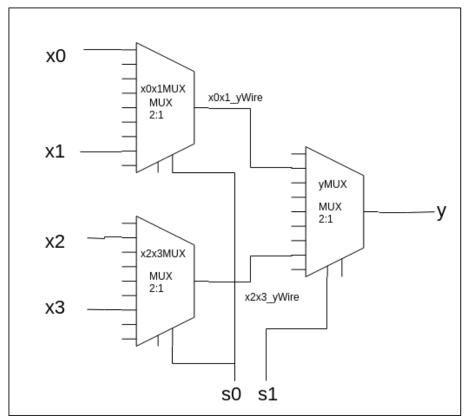


Figure 10: 4:1 MUX via MUX stacking 2:1MUXs

▼ 7.1 myHDL Module

```
In [32]:
           @block
           def MUX4_1_MS(x0, x1, x2, x3, s0, s1, y):
               4:1 Multiplexer via 2:1 MUX stacking
               Input:
                   x0(bool): input channel 0
                   x1(bool): input channel 1
                   x2(bool): input channel 2
                   x3(bool): input channel 3
                   s1(bool): channel selection input bit 1
                   s0(bool): channel selection input bit 0
               Output:
                   y(bool): ouput
               #create ouput from x0x1 input MUX to y ouput MUX
               x0x1_yWire=Signal(bool(0))
               #create instance of 2:1 mux and wire in inputs
               #a, b, s0 and wire to ouput mux
               x0x1MUX=MUX2\_1\_Combo(x0, x1, s0, x0x1\_yWire)
               #create ouput from x2x3 input MUX to y ouput MUX
               x2x3_yWire=Signal(bool(0))
               #create instance of 2:1 mux and wire in inputs
               #c, d, s0 and wire to ouput mux
               x2x3MUX=MUX2_1_Combo(x2, x3, s0, x2x3_yWire)
               #create ouput MUX and wire to internal wires,
               #s1 and ouput y
               yMUX=MUX2_1_Combo(x0x1_yWire, x2x3_yWire, s1, y)
               return instances()
```

7.2 myHDL Testing

```
In [33]: ▼
           #generate systmatic and random test values
           TestLen=5
           SystmaticVals=list(itertools.product([0,1], repeat=6))
           s0TVs=np.array([i[0] for i in SystmaticVals]).astype(int)
           np.random.seed(15)
           s0TVs=np.append(s0TVs, np.random.randint(0,2, TestLen)).astype(int)
           slTVs=np.array([i[1] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(16)
           s1TVs=np.append(s1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x0TVs=np.array([i[2] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(17)
           x0TVs=np.append(x0TVs, np.random.randint(0,2, TestLen)).astype(int)
           x1TVs=np.array([i[3] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(18)
           x1TVs=np.append(x1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x2TVs=np.array([i[4] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(19)
           x2TVs=np.append(x2TVs, np.random.randint(0,2, TestLen)).astype(int)
           x3TVs=np.array([i[5] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(20)
           x3TVs=np.append(x3TVs, np.random.randint(0,2, TestLen)).astype(int)
           TestLen=len(x0TVs)
           SystmaticVals, s0TVs, s1TVs, x3TVs, x2TVs, x1TVs, x0TVs, TestLen
Out[33]: ([(0, 0, 0, 0, 0, 0),
           (0, 0, 0, 0, 0, 1),
           (0, 0, 0, 0, 1, 0),
           (0, 0, 0, 0, 1, 1),
           (0, 0, 0, 1, 0, 0),
           (0, 0, 0, 1, 0, 1),
           (0, 0, 0, 1, 1, 0),
           (0, 0, 0, 1, 1, 1),
           (0, 0, 1, 0, 0, 0),
           (0, 0, 1, 0, 0, 1),
           (0, 0, 1, 0, 1, 0),
```

```
(0, 0, 1, 1, 0, 1),
           (0, 0, 1, 1, 1, 0),
           (0, 0, 1, 1, 1, 1),
           (0, 1, 0, 0, 0, 0),
           (0, 1, 0, 0, 0, 1),
           (0, 1, 0, 0, 1, 0),
In [34]:
           Peeker.clear()
           x0=Signal(bool(0)); Peeker(x0, 'x0')
           x1=Signal(bool(0)); Peeker(x1,
                                           'x1')
           x2=Signal(bool(0)); Peeker(x2, 'x2')
           x3=Signal(bool(0)); Peeker(x3, 'x3')
           s0=Signal(bool(0)); Peeker(s0, 's0')
           s1=Signal(bool(0)); Peeker(s1, 's1')
           y=Signal(bool(0)); Peeker(y, 'y')
           DUT=MUX4_1_MS(x0, x1, x2, x3, s0, s1, y)
           def MUX4_1_MS_TB():
               myHDL only testbench for module `MUX4 1 MS`
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TVs[i])
                       x1.next=int(x1TVs[i])
                       x2.next=int(x2TVs[i])
                       x3.next=int(x3TVs[i])
                       s0.next=int(s0TVs[i])
                       s1.next=int(s1TVs[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           sim=Simulation(DUT, MUX4_1_MS_TB(), *Peeker.instances()).run()
In [35]:
           Peeker.to_wavedrom()
```

(0, 0, 1, 0, 1, 1), (0, 0, 1, 1, 1, 0, 0),

```
In [36]:
           MUX4_1_MSData=Peeker.to_dataframe()
           MUX4_1_MSData=MUX4_1_MSData[['x3', 'x2', 'x1', 'x0', 's1', 's0', 'y']]
           MUX4_1_MSData
Out[36]:
             x3 x2 x1 x0 s1 s0 y
              0
                 0
                     0
                        0
                           0
                              0 0
                 0
              1
           2
              0
                 1
                     0
                        0
                           0
                              0 0
           3
              1
                 1
                     0
                        0
                           0
                 0
                     1
                 0
                        0
              1
                     1
                           0
                              0 0
                 1
                        0
                     1
           7
              1
                 1
                     1
                        0
                           0
                              0 0
           8
                 0
                     0
                        1
                           0
                 0
                           0
          10
              0
                 1
                     0
                          0
                              0 1
In [37]:
           Test=MUX4_1_ComboData[['x3', 'x2', 'x1', 'x0', 's1', 's0', 'y']]==MUX4_
           Test=Test.all().all()
           print(f'Module `MUX4_1_MS` works as exspected: {Test}')
```

Module `MUX4_1_MS` works as exspected: True

7.3 Verilog Conversion

```
In [38]:
         ***Verilog modual from MUX4 1 MS.v***
          // File: MUX4 1 MS.v
         // Generated by MyHDL 0.10
         // Date: Sun Sep 23 18:20:31 2018
          `timescale 1ns/10ps
         module MUX4_1_MS (
             χ0,
              x1,
              x2,
              х3,
              s0,
              s1,
              У
         );
         // 4:1 Multiplexer via 2:1 MUX stacking
         // Input:
         //
                 x0(bool): input channel 0
                 x1(bool): input channel 1
         //
                 x2(bool): input channel 2
         //
         //
                 x3(bool): input channel 3
         //
                 s1(bool): channel selection input bit 1
                 s0(bool): channel selection input bit 0
         //
         // Output:
                y(bool): ouput
         //
         input x0;
         input x1;
         input x2;
         input x3;
         input s0;
         input s1;
         output y;
         wire y;
         wire x0x1_yWire;
         wire MUX2_1_Combo1_0_y;
         assign x0x1_yWire = (((!s0) \&\& x0) | (s0 \&\& x1));
         assign MUX2_1_{combo1_0_y} = (((!s0) \&\& x2) | (s0 \&\& x3));
         assign y = (((!s1) \&\& x0x1_yWire) | (s1 \&\& MUX2_1_Combo1_0_y));
```

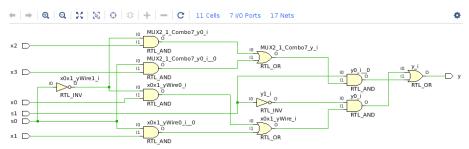


Figure 11: MUX4_1_MS RTL schematic; Xilinx Vivado 2017.4

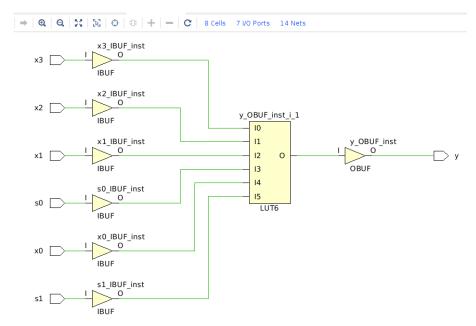


Figure 12: MUX4_1_MS Synthesized Schematic; Xilinx Vivado 2017.4

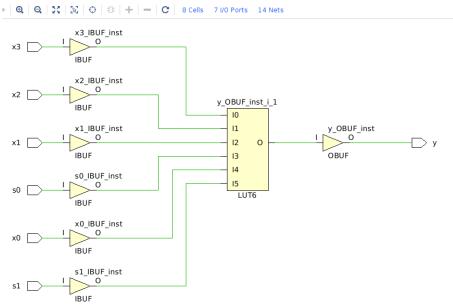


Figure 13: MUX4_1_MS Implementated Schematic; Xilinx Vivado 2017.4

▼ 7.4 myHDL to Verilog Testbench

```
In [39]: ▼ #create BitVectors
       x0TVs=intbv(int(''.join(x0TVs.astype(str)), 2))[TestLen:]
       x1TVs=intbv(int(''.join(x1TVs.astype(str)), 2))[TestLen:]
       x2TVs=intbv(int(''.join(x2TVs.astype(str)), 2))[TestLen:]
       x3TVs=intbv(int(''.join(x3TVs.astype(str)), 2))[TestLen:]
       s0TVs=intbv(int(''.join(s0TVs.astype(str)), 2))[TestLen:]
       slTVs=intbv(int(''.join(slTVs.astype(str)), 2))[TestLen:]
       x0TVs, bin(x0TVs), x1TVs, bin(x1TVs), x2TVs, bin(x2TVs), x3TVs, bin(x3TVs)
Out[39]: (intbv(2296870857426870268),
      intbv(34723282962276803050),
      intbv(118059162071741130356),
      intbv(196765270119568550582),
      Θ',
      intbv(137438953451),
      intbv(9007061817884663),
```

```
In [40]:
           @block
           def MUX4_1_MS_TBV():
               myHDL -> Verilog testbench for module `MUX4 1 MS`
               x0=Signal(bool(0))
               x1=Signal(bool(0))
               x2=Signal(bool(0))
               x3=Signal(bool(0))
               y=Signal(bool(0))
               s0=Signal(bool(0))
               s1=Signal(bool(0))
               @always_comb
               def print data():
                   print(x0, x1, x2, x3, s0, s1, y)
               #Test Signal Bit Vectors
               x0TV=Signal(x0TVs)
               x1TV=Signal(x1TVs)
               x2TV=Signal(x2TVs)
               x3TV=Signal(x3TVs)
               sOTV=Signal(sOTVs)
               s1TV=Signal(s1TVs)
               DUT=MUX4 1 MS(x0, x1, x2, x3, s0, s1, y)
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TV[i])
                       x1.next=int(x1TV[i])
                       x2.next=int(x2TV[i])
                       x3.next=int(x3TV[i])
                       s0.next=int(s0TV[i])
                       s1.next=int(s1TV[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           TB=MUX4 1 MS TBV()
           TB.convert(hdl="Verilog", initial_values=True)
           VerilogTextReader('MUX4_1_MS_TBV');
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl. Signal. Signal'> <class 'ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
```

```
<class 'myhdl._Signal._Signal'> <class '_ast.Name'>

***Verilog modual from MUX4_1_MS_TBV.v***
```

```
// File: MUX4_1_MS_TBV.v
// Generated by MyHDL 0.10
// Date: Sun Sep 23 18:20:41 2018

`timescale 1ns/10ps
module MUX4_1_MS_TBV (
);
// LIBITED No. 13 TO 15 TO 15
```

▼ 7.5 PYNQ-Z1 Deployment

7.5.1 Board Circuit

See Board Circuit for "4 Channel Input: 1 Channel Output multiplexer in Gate Level Logic"

7.5.2 Board Constraint

uses same 'MUX4_1.xdc' as "4 Channel Input : 1 Channel Output multiplexer in Gate Level Logic"

▼ 7.5.3 Video of Deployment

MUX4 1 MS myHDL PYNQ-Z1 (YouTube (https://www.youtube.com/watch?v=uO7VZ8ow Yg))

8 Introduction to HDL Behavioral Modeling

HDL behavioral modeling is a "High" level, though not at the HLS level, HDL syntax where the intended hardware element is modeled via its intended abstract algorithm behavior. Thus the common computer science (and mathematician)tool of abstraction is borrowed and incorporated into the HDL syntax. The abstraction that follows has, like all things, its pros and cons.

As a pro, this means that the Hard Ware Designer is no longer consumed by the manuchia of implementing boolean algebra for every device and can instead focus on implementing the intended algorithm in hardware. And it is thanks to this blending of Software and Hardware that the design of digital devices has grown as prolific as it has. However, there is quite a cache for using behavioral modeling. First off HDL now absolutely requires synthesis tools that can map the behavioral statements to hardware. And even when the behavioral logic is mapped at least to the RTL level there is no escaping two points. 1. At the end of the day, the RTL will be implemented via Gate level devices in some form or another. 2. the way the synthesis tool has mapped the abstract behavioral to RTL may not be physical implementable especially in ASIC implementations.

For these reasons it as Hardware Developers using Behavioral HDL we have to be able to still be able to implement the smallest indivisible units of our HDL at the gate level. Must know what physical limits our target architecture (FPGA, ASIC, etc) has and keep within these limits when writing our HDL code. And lastly, we can not grow lazy in writing behavioral HDL, but must always see at least down to the major RTL elements that our behavioral statements are embodying.

9 2:1 MUX via Behavioral IF

▼ 9.1 myHDL Module

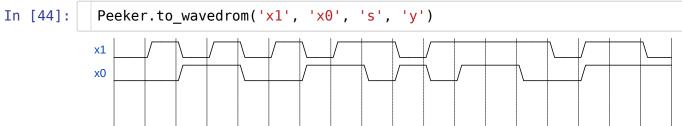
```
In [41]:
           @block
           def MUX2_1_B(x0, x1, s, y):
               2:1 Multiplexer written via behavioral if
                    x0(bool): input channel 0
                    x1(bool): input channel 1
                    s(bool): channel selection input
               Output:
                   y(bool): ouput
               @always comb
               def logic():
                   if s:
                        y.next=x1
                   else:
                        y.next=x0
               return instances()
```

9.2 myHDL Testing

```
In [42]: ▼
           #generate systmatic and random test values
           TestLen=10
           SystmaticVals=list(itertools.product([0,1], repeat=3))
           xOTVs=np.array([i[1] for i in SystmaticVals]).astype(int)
           np.random.seed(15)
           x0TVs=np.append(x0TVs, np.random.randint(0,2, TestLen)).astype(int)
           x1TVs=np.array([i[2] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(16)
           x1TVs=np.append(x1TVs, np.random.randint(0,2, TestLen)).astype(int)
           sTVs=np.array([i[0] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(17)
           sTVs=np.append(sTVs, np.random.randint(0,2, TestLen)).astype(int)
           TestLen=len(x0TVs)
           x0TVs, x1TVs, sTVs, TestLen
Out[42]: (array([0, 0, 1, 1, 0, 0, 1, 1, 0, 1, 1, 0, 0, 1, 1, 1]),
          array([0, 1, 0, 1, 0, 1, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 0]),
          array([0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 0, 0, 1, 0, 1, 0, 1]),
```

18)

```
In [43]:
           Peeker.clear()
           x0=Signal(bool(0)); Peeker(x0, 'x0')
           x1=Signal(bool(0)); Peeker(x1, 'x1')
           s=Signal(bool(0)); Peeker(s, 's')
           y=Signal(bool(0)); Peeker(y, 'y')
           DUT=MUX2\_1\_B(x0, x1, s, y)
           def MUX2_1_B_TB():
               myHDL only testbench for module `MUX2_1_B`
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TVs[i])
                       x1.next=int(x1TVs[i])
                       s.next=int(sTVs[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           sim=Simulation(DUT, MUX2_1_B_TB(), *Peeker.instances()).run()
           Peeker.to_wavedrom('x1', 'x0', 's', 'y')
```



```
In [45]:
          MUX2_1_BData=Peeker.to_dataframe()
          MUX2_1_BData=MUX2_1_BData[['x1', 'x0', 's', 'y']]
          MUX2_1_BData
Out[45]:
            x1 x0 s y
          0 0 0 0
                0 0 0
             1
          2
             0
               1 0 1
          3
             1
                1 0 1
                0 1 0
          5
               0 1 1
             1
                1 1 0
          7
            1
               1 1 1
          8
                0 1 1
             1
          9
             0 1 1 0
          10
             1 0 1 1
          11
             1 1 0 1
          13
            1 0 1 1
          14
            0 0 0 0
          15
            1 1 1 1
          16
                1 0 1
             1
          17
             0 1 1 0
          Test=MUX2\_1\_ComboData[['x1', 'x0', 's', 'y']]==MUX2\_1\_BData
In [46]:
          Test=Test.all().all()
           print(f'`MUX2_1_B` Behavioral is Eqivlint to `MUX2_1_Combo`: {Test}')
         `MUX2_1_B` Behavioral is Eqivlint to `MUX2_1_Combo`: True
```

9.3 Verilog Conversion

```
In [47]:
           DUT.convert()
           VerilogTextReader('MUX2_1_B');
         ***Verilog modual from MUX2_1_B.v***
          // File: MUX2_1_B.v
         // Generated by MyHDL 0.10
         // Date: Sun Sep 23 18:20:53 2018
         `timescale 1ns/10ps
         module MUX2_1_B (
             χ0,
             x1,
             S,
             У
         );
         // 2:1 Multiplexer written via behavioral if
         // Input:
                x0(bool): input channel 0
         //
         //
                x1(bool): input channel 1
                s(bool): channel selection input
         // Output:
                y(bool): ouput
         //
         input x0;
         input x1;
         input s;
         output y;
         reg y;
         always @(s, x0, x1) begin: MUX2_1_B_LOGIC
             if (s) begin
                 y = x1;
             end
             else begin
                 y = x0;
             end
         end
```

endmodule

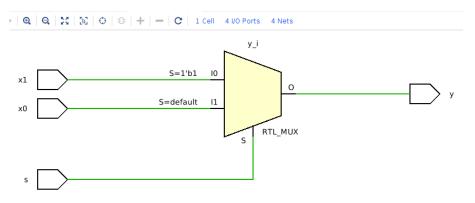


Figure 14: MUX2_1_B RTL schematic; Xilinx Vivado 2017.4

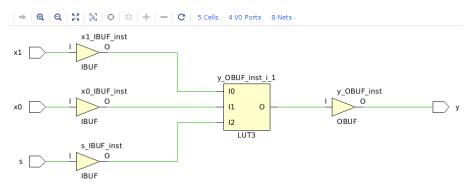


Figure 15: MUX2_1_B Synthesized Schematic; Xilinx Vivado 2017.4

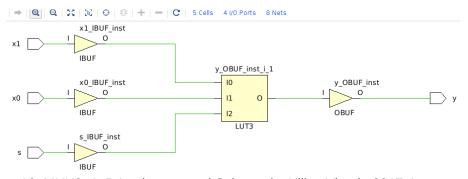


Figure 16: MUX2_1_B Implementated Schematic; Xilinx Vivado 2017.4

9.4 myHDL to Verilog Testbench

```
In [49]:
           @block
           def MUX2_1_B_TBV():
                myHDL -> Verilog testbench for module `MUX2 1 B`
                x0=Signal(bool(0))
                x1=Signal(bool(0))
                s=Signal(bool(0))
                y=Signal(bool(0))
                @always comb
                def print_data():
                    print(x0, x1, s, y)
                #Test Signal Bit Vectors
                x0TV=Signal(x0TVs)
                x1TV=Signal(x1TVs)
                sTV=Signal(sTVs)
                DUT=MUX2\_1\_B(x0, x1, s, y)
                @instance
                def stimules():
                    for i in range(TestLen):
                         x0.next=int(x0TV[i])
                         x1.next=int(x1TV[i])
                         s.next=int(sTV[i])
                         yield delay(1)
                    raise StopSimulation()
                return instances()
            TB=MUX2 1 B TBV()
            TB.convert(hdl="Verilog", initial_values=True)
            VerilogTextReader('MUX2 1 B TBV');
          <class 'myhdl. Signal. Signal'> <class 'ast.Name'>
          <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
<class 'myhdl._Signal._Signal'> <class '_ast.Name'>
          <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
          ***Verilog modual from MUX2_1_B TBV.v***
          // File: MUX2 1 B TBV.v
          // Generated by MyHDL 0.10
          // Date: Sun Sep 23 18:21:01 2018
          `timescale 1ns/10ps
         module MUX2 1 B TBV (
          );
          // myHDL -> Verilog testbench for module `MUX2 1 B`
```

reg x0 = 0;

```
reg x1 = 0;
reg s = 0;
reg y = 0;
wire [17:0] x0TV;
wire [17:0] x1TV;
wire [17:0] sTV;
assign x0TV = 18'd52583;
assign x1TV = 18'd87798;
assign sTV = 18'd16277;
always @(s, y, x0, x1) begin: MUX2_1_B_TBV_PRINT DATA
    $write("%h", x0);
    $write(" ");
    $write("%h", x1);
    $write(" ");
    $write("%h", s);
    $write(" ");
    $write("%h", y);
    $write("\n");
end
always @(s, x0, x1) begin: MUX2_1_B_TBV_MUX2_1_B0_0_LOGIC
    if (s) begin
        y = x1;
    end
    else begin
        y = x0;
    end
end
initial begin: MUX2 1 B TBV STIMULES
    integer i;
    for (i=0; i<18; i=i+1) begin
        x0 \le x0TV[i];
        x1 <= x1TV[i];
        s <= sTV[i];
        # 1;
    end
    $finish;
end
endmodule
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x0TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: x1TV
  category=ToVerilogWarning
/home/iridium/anaconda3/lib/python3.6/site-packages/myhdl/conversion/ t
oVerilog.py:349: ToVerilogWarning: Signal is not driven: sTV
  category=ToVerilogWarning
```

9.5 PYNQ-Z1 Deployment

9.5.1 Board Circuit

See Board Circuit for "2 Channel Input:1 Channel Output multiplexer in Gate Level Logic"

9.5.2 Board Constraint

uses the same MUX2_1.xdc as "2 Channel Input:1 Channel Output multiplexer in Gate Level Logic"

▼ 9.5.3 Video of Deployment

MUX2_1_B myHDL PYNQ-Z1 (YouTube (https://www.youtube.com/watch?v=QrHQfx_Sjnw))

10 4:1 MUX via Behavioral if-elif-else

▼ 10.1 myHDL Module

```
In [50]:
           @block
           def MUX4_1_B(x0, x1, x2, x3, s0, s1, y):
               4:1 Multiblexer written in if-elif-else Behavioral
               Input:
                   x0(bool): input channel 0
                   x1(bool): input channel 1
                   x2(bool): input channel 2
                   x3(bool): input channel 3
                   s1(bool): channel selection input bit 1
                   s0(bool): channel selection input bit 0
               Output:
                   y(bool): ouput
               @always comb
               def logic():
                   if s0==0 and s1==0:
                        y.next=x0
                   elif s0 == 1 and s1 == 0:
                        y.next=x1
                   elif s0==0 and s1==1:
                        y.next=x2
                   else:
                        y.next=x3
               return instances()
```

▼ 10.2 myHDL Testing

```
In [51]: ▼ #generate systmatic and random test values
           TestLen=5
           SystmaticVals=list(itertools.product([0,1], repeat=6))
           s0TVs=np.array([i[0] for i in SystmaticVals]).astype(int)
           np.random.seed(15)
           s0TVs=np.append(s0TVs, np.random.randint(0,2, TestLen)).astype(int)
           slTVs=np.array([i[1] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(16)
           s1TVs=np.append(s1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x0TVs=np.array([i[2] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(17)
           x0TVs=np.append(x0TVs, np.random.randint(0,2, TestLen)).astype(int)
           x1TVs=np.array([i[3] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(18)
           x1TVs=np.append(x1TVs, np.random.randint(0,2, TestLen)).astype(int)
           x2TVs=np.array([i[4] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(19)
           x2TVs=np.append(x2TVs, np.random.randint(0,2, TestLen)).astype(int)
           x3TVs=np.array([i[5] for i in SystmaticVals]).astype(int)
           #the random genrator must have a differint seed beween each generation
           #call in order to produce differint values for each call
           np.random.seed(20)
           x3TVs=np.append(x3TVs, np.random.randint(0,2, TestLen)).astype(int)
           TestLen=len(x0TVs)
           SystmaticVals, s0TVs, s1TVs, x3TVs, x2TVs, x1TVs, x0TVs, TestLen
Out[51]: ([(0, 0, 0, 0, 0, 0),
           (0, 0, 0, 0, 0, 1),
           (0, 0, 0, 0, 1, 0),
           (0, 0, 0, 0, 1, 1),
           (0, 0, 0, 1, 0, 0),
           (0, 0, 0, 1, 0, 1),
           (0, 0, 0, 1, 1, 0),
           (0, 0, 0, 1, 1, 1),
           (0, 0, 1, 0, 0, 0),
           (0, 0, 1, 0, 0, 1),
           (0, 0, 1, 0, 1, 0),
```

```
(0, 0, 1, 1, 0, 1),
           (0, 0, 1, 1, 1, 0),
           (0, 0, 1, 1, 1, 1),
           (0, 1, 0, 0, 0, 0),
           (0, 1, 0, 0, 0, 1),
           (0, 1, 0, 0, 1, 0),
In [52]:
           Peeker.clear()
           x0=Signal(bool(0)); Peeker(x0, 'x0')
           x1=Signal(bool(0)); Peeker(x1,
                                           'x1')
           x2=Signal(bool(0)); Peeker(x2, 'x2')
           x3=Signal(bool(0)); Peeker(x3, 'x3')
           s0=Signal(bool(0)); Peeker(s0, 's0')
           s1=Signal(bool(0)); Peeker(s1, 's1')
           y=Signal(bool(0)); Peeker(y, 'y')
           DUT=MUX4_1_B(x0, x1, x2, x3, s0, s1, y)
           def MUX4_1_B_TB():
               myHDL only testbench for module `MUX4 1 B`
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TVs[i])
                       x1.next=int(x1TVs[i])
                       x2.next=int(x2TVs[i])
                       x3.next=int(x3TVs[i])
                       s0.next=int(s0TVs[i])
                       s1.next=int(s1TVs[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           sim=Simulation(DUT, MUX4_1_B_TB(), *Peeker.instances()).run()
In [53]:
           Peeker.to_wavedrom()
```

(0, 0, 1, 0, 1, 1), (0, 0, 1, 1, 1, 0, 0),

```
In [54]:
           MUX4_1_BData=Peeker.to_dataframe()
           MUX4_1_BData=MUX4_1_BData[['x3', 'x2', 'x1', 'x0', 's1', 's0', 'y']]
           MUX4_1_BData
Out[54]:
             x3 x2 x1 x0 s1 s0 y
              0
                  0
                     0
                        0
                           0
                               0 0
              1
                  0
                     0
                           0
           2
              0
                  1
                     0
                        0
                           0
           3
                     0
                        0
                           0
                  1
               0
                  0
                     1
                        0
                           0
                               0
           5
                               0 0
                  0
                        0
                           0
              1
                     1
                  1
                     1
                        0
                           0
           7
              1
                  1
                     1
                        0
                           0
                               0
                                 0
           8
                  0
                     0
                        1
                           0
                  0
                     0
                           0
          10
                  1
                     0
                          0
                               0 1
                        1
In [55]:
           Test=MUX4_1_ComboData[['x3', 'x2', 'x1', 'x0', 's1', 's0', 'y']]==MUX4_
           Test=Test.all().all()
           print(f'Module `MUX4_1_B` works as exspected: {Test}')
```

Module `MUX4 $_1$ B` works as exspected: True

▼ 10.3 Verilog Conversion

```
In [56]:
         ***Verilog modual from MUX4_1_B.v***
          // File: MUX4 1 B.v
         // Generated by MyHDL 0.10
         // Date: Sun Sep 23 18:21:21 2018
         `timescale 1ns/10ps
         module MUX4_1_B (
             χ0,
             x1,
             x2,
             х3,
             s0,
             s1,
             У
         );
         // 4:1 Multiblexer written in if-elif-else Behavioral
         // Input:
         //
                 x0(bool): input channel 0
                x1(bool): input channel 1
         //
                x2(bool): input channel 2
         //
         //
                x3(bool): input channel 3
                s1(bool): channel selection input bit 1
         //
                s0(bool): channel selection input bit 0
         //
         // Output:
                y(bool): ouput
         //
         input x0;
         input x1;
         input x2;
         input x3;
         input s0;
         input s1;
         output y;
         reg y;
         always @(x0, s0, x3, x2, x1, s1) begin: MUX4_1_B_LOGIC
              if (((s0 == 0) \&\& (s1 == 0))) begin
                  y = x0;
             else if (((s0 == 1) \&\& (s1 == 0))) begin
                  y = x1;
             end
             else if (((s0 == 0) \&\& (s1 == 1))) begin
                  y = x2;
             end
             else begin
```

y = x3;

endmodule

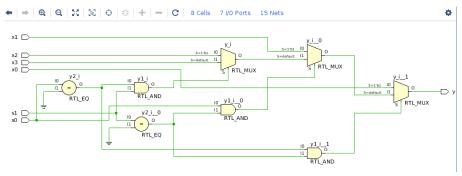


Figure 17: MUX4_1_B RTL schematic; Xilinx Vivado 2017.4

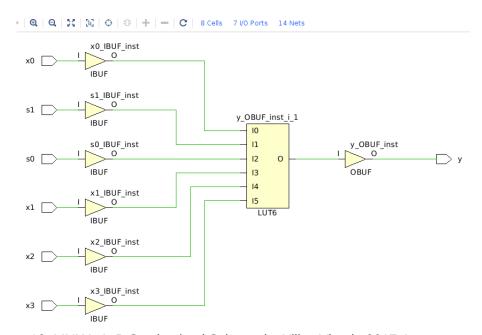


Figure 18: MUX4_1_B Synthesized Schematic; Xilinx Vivado 2017.4

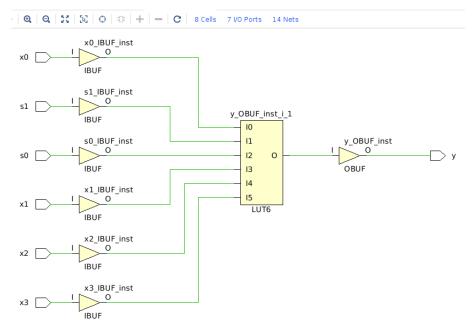


Figure 19: MUX4 1 B Implementated Schematic; Xilinx Vivado 2017.4

▼ 10.4 myHDL to Verilog Testbench

```
In [57]: ▼ #create BitVectors
       xOTVs=intbv(int(''.join(xOTVs.astype(str)), 2))[TestLen:]
       x1TVs=intbv(int(''.join(x1TVs.astype(str)), 2))[TestLen:]
x2TVs=intbv(int(''.join(x2TVs.astype(str)), 2))[TestLen:]
       x3TVs=intbv(int(''.join(x3TVs.astype(str)), 2))[TestLen:]
       sOTVs=intbv(int(''.join(sOTVs.astype(str)), 2))[TestLen:]
       s1TVs=intbv(int(''.join(s1TVs.astype(str)), 2))[TestLen:]
       x0TVs, bin(x0TVs), x1TVs, bin(x1TVs), x2TVs, bin(x2TVs), x3TVs, bin(x3TVs)
Out[57]: (intbv(2296870857426870268),
       intbv(34723282962276803050),
       intbv(118059162071741130356),
       intbv(196765270119568550582),
       0',
       intbv(137438953451),
       intbv(9007061817884663),
```

```
In [58]:
           @block
           def MUX4_1_B_TBV():
               myHDL -> Verilog testbench for module `MUX4 1 B`
               x0=Signal(bool(0))
               x1=Signal(bool(0))
               x2=Signal(bool(0))
               x3=Signal(bool(0))
               y=Signal(bool(0))
               s0=Signal(bool(0))
               s1=Signal(bool(0))
               @always_comb
               def print data():
                   print(x0, x1, x2, x3, s0, s1, y)
               #Test Signal Bit Vectors
               x0TV=Signal(x0TVs)
               x1TV=Signal(x1TVs)
               x2TV=Signal(x2TVs)
               x3TV=Signal(x3TVs)
               sOTV=Signal(sOTVs)
               s1TV=Signal(s1TVs)
               DUT=MUX4 1 B(x0, x1, x2, x3, s0, s1, y)
               @instance
               def stimules():
                   for i in range(TestLen):
                       x0.next=int(x0TV[i])
                       x1.next=int(x1TV[i])
                       x2.next=int(x2TV[i])
                       x3.next=int(x3TV[i])
                       s0.next=int(s0TV[i])
                       s1.next=int(s1TV[i])
                       yield delay(1)
                   raise StopSimulation()
               return instances()
           TB=MUX4 1 B TBV()
           TB.convert(hdl="Verilog", initial_values=True)
           VerilogTextReader('MUX4 1 B TBV');
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl. Signal. Signal'> <class 'ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '_ast.Name'>
         <class 'myhdl._Signal._Signal'> <class '</pre>
                                                   ast.Name'>
```

```
<class 'myhdl._Signal._Signal'> <class '_ast.Name'>

***Verilog modual from MUX4_1_B_TBV.v***
```

▼ 10.5 PYNQ-Z1 Deployment

▼ 10.5.1 Board Circuit

See Board Circuit for "4 Channel Input: 1 Channel Output multiplexer in Gate Level Logic"

▼ 10.5.2 Board Constraint

uses same 'MUX4_1.xdc' as "4 Channel Input : 1 Channel Output multiplexer in Gate Level Logic"

▼ 10.5.3 Video of Deployment

MUX4_1_B myHDL PYNQ-Z1 (YouTube (https://www.youtube.com/watch?v=UKXx4PYS1xI))

▼ 11 Multiplexer 4:1 Behavioral via Bitvectors

▼ 11.1 myHDL Module

```
In [59]:
           @block
           def MUX4_1_BV(X, S, y):
               4:1 Multiblexerwritten in behvioral "if-elif-else"(case)
               with BitVector inputs
               Input:
                   X(4bitBV):input bit vector; min=0, max=15
                   S(2bitBV):selection bit vector; min=0, max=3
               Output:
                   y(bool): ouput
               @always_comb
               def logic():
                   if S==0:
                       y.next=X[0]
                   elif S==1:
                       y.next=X[1]
                   elif S==2:
                       y.next=X[2]
                   else:
                       y.next=X[3]
               return instances()
```

▼ 11.2 myHDL Testing

```
In [60]: XTVs=np.array([1,2,4,8])
    XTVs=np.append(XTVs, np.random.choice([1,2,4,8], 6)).astype(int)
    TestLen=len(XTVs)

    np.random.seed(12)
    STVs=np.arange(0,4)
    STVs=np.append(STVs, np.random.randint(0,4, 5))
    TestLen, XTVs, STVs
```

```
In [61]:
           Peeker.clear()
           X=Signal(intbv(0)[4:]); Peeker(X, 'X')
           S=Signal(intbv(0)[2:]); Peeker(S, 'S')
           y=Signal(bool(0)); Peeker(y, 'y')
           DUT=MUX4_1_BV(X, S, y)
           def MUX4 1 BV TB():
               @instance
               def stimules():
                   for i in STVs:
                       for j in XTVs:
                           S.next=int(i)
                           X.next=int(j)
                           yield delay(1)
                   raise StopSimulation()
               return instances()
           sim=Simulation(DUT, MUX4_1_BV_TB(), *Peeker.instances()).run()
           Peeker.to_wavedrom('X', 'S', 'y', start_time=0, stop_time=2*TestLen+2)
In [62]:
               7 2 4 8 4 2 1 8 4 8 1 2 4 8 4 2 1 8 4 8 1 2 4
          S
                                                                           2
In [63]:
           MUX4 1 BVData=Peeker.to dataframe()
           MUX4_1_BVData=MUX4_1_BVData[['X', 'S', 'y']]
           MUX4 1 BVData
Out[63]:
             X S y
            1 0 1
          1
             2 0
                  0
             4 0
                  0
                0
                0
                  0
            2
                0
                  0
             1 0
                  1
             8
                0
                  0
                0
                  0
          9
             8 0
                  0
          10 1 1
```

```
MUX4 1 BVData['x0']=None; MUX4 1 BVData['x1']=None; MUX4 1 BVData['x2']
In [64]:
           MUX4\ 1\ BVData[['x3', 'x2', 'x1', 'x0']]=MUX4\ 1\ BVData[['X']].apply(lamk)
           MUX4 1 BVData['s0']=None; MUX4 1 BVData['s1']=None
           MUX4 1 BVData[['s1', 's0']]=MUX4 1 BVData[['S']].apply(lambda bv: [int(
           MUX4_1_BVData=MUX4_1_BVData[['X', 'x0', 'x1', 'x2', 'x3', 'S', 's0', 's
           MUX4 1 BVData
Out[64]:
              X x0 x1 x2 x3 S s0 s1 y
             1
                 1
                    0
                        0
                           0
                              0
                                 0
                                    0
                                      1
           1
              2
                 0
                    1
                        0
                           0
                              0
                                 0
             4
           2
                 0
                    0
                        1
                           0
                             0
                                 0
                                    0
                                      0
             8
                 0
                    0
                        0
                           1
                              0
                                 0
                 0
                    0
                        1
                           0
                              0
                                 0
                                    0
                                       0
              2
                 0
                                    0 0
                    1
                        0
                           0
                              0
                                 0
                    0
                           0
                              0
                                    0
           7
              8
                 0
                    0
                        0
                           1
                              0
                                 0
                                    0
                                      0
                 0
                    0
                        1
                           0
                              0
                                 0
                                      0
              8
                 0
                    0
                        0
                           1
                              0
                                 0
                                    0
                                       0
                    0
                                    0 0
          10 1
                 1
                        0
                           0 1
                                 1
In [65]:
           MUX4_1_BVData['yRef']=MUX4_1_BVData.apply(lambda row:y41EqN(row['x0'],
           MUX4 1 BVData
         /home/iridium/anaconda3/lib/python3.6/site-packages/ipykernel launche
          r.py:1: SettingWithCopyWarning:
         A value is trying to be set on a copy of a slice from a DataFrame.
         Try using .loc[row indexer,col indexer] = value instead
         See the caveats in the documentation: http://pandas.pydata.org/pandas
          -docs/stable/indexing.html#indexing-view-versus-copy (http://pandas.p
         vdata.org/pandas-docs/stable/indexing.html#indexing-view-versus-copy)
            """Entry point for launching an IPython kernel.
```

```
In [66]: Test=(MUX4_1_BVData['y']==MUX4_1_BVData['yRef']).all()
    print(f'Module `MUX4_1_BVData` works as exspected: {Test}')

Module `MUX4_1_BVData` works as exspected: True
```

▼ 11.3 Verilog Conversion

```
In [67]:
           DUT.convert()
           VerilogTextReader('MUX4_1_BV');
         ***Verilog modual from MUX4_1_BV.v***
          // File: MUX4 1 BV.v
         // Generated by MyHDL 0.10
         // Date: Sun Sep 23 18:21:56 2018
         `timescale 1ns/10ps
         module MUX4_1_BV (
             Χ,
             S,
             У
         );
         // 4:1 Multiblexerwritten in behvioral "if-elif-else"(case)
         // with BitVector inputs
         // Input:
                X(4bitBV):input bit vector; min=0, max=15
         //
                S(2bitBV):selection bit vector; min=0, max=3
         //
         // Output:
                y(bool): ouput
         //
         input [3:0] X;
         input [1:0] S;
         output y;
         reg y;
         always @(X, S) begin: MUX4 1 BV LOGIC
             case (S)
                  'h0: begin
                      y = X[0];
                 end
                  'h1: begin
                      y = X[1];
                 end
                  'h2: begin
                     y = X[2];
                 end
                 default: begin
                      y = X[3];
                 end
             endcase
         end
```

endmodule

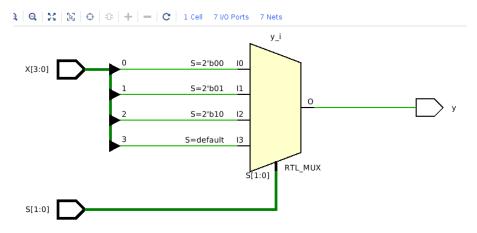


Figure 20: MUX4_1_BV RTL schematic; Xilinx Vivado 2017.4

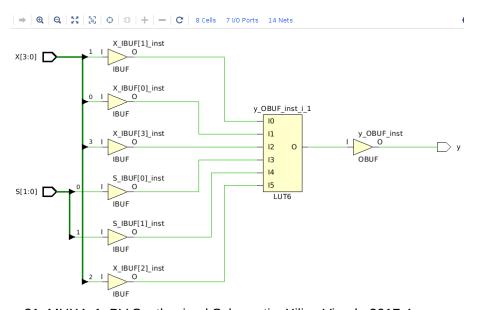


Figure 21: MUX4_1_BV Synthesized Schematic; Xilinx Vivado 2017.4

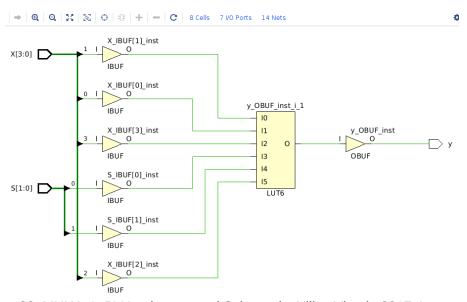


Figure 22: MUX4_1_BV Implementated Schematic; Xilinx Vivado 2017.4

11.4 myHDL to Verilog Testbench

Will Do later

11.5 PYNQ-Z1 Deployment

▼ 11.5.1 Board Circuit

See Board Circuit for "4 Channel Input: 1 Channel Output multiplexer in Gate Level Logic"

▼ 11.5.2 Board Constraint

notice that in <code>get_ports</code> the pin is set to the a single bit of the bitvector via bitvector indexing

```
In [68]:
           ConstraintXDCTextReader('MUX4 1 BV');
         ***Constraint file from MUX4 1 BV.xdc***
          ## PYNQ-Z1 Constraint File for MUX4 1 BV
         ## Based on https://github.com/Xilinx/PYNQ/blob/master/boards/Pyng-Z1/b
         ase/vivado/constraints/base.xdc (https://github.com/Xilinx/PYNO/blob/ma
         ster/boards/Pvng-Z1/base/vivado/constraints/base.xdc)
         ## Switches
         set_property -dict {PACKAGE_PIN M20 IOSTANDARD LVCMOS33} [get_ports {S
         [0]}]; ## SW0
         set property -dict {PACKAGE PIN M19 IOSTANDARD LVCMOS33} [get ports {S
         [1]}]; ## SW1
         ## Buttons
         set_property -dict {PACKAGE_PIN D19 IOSTANDARD LVCMOS33} [get_ports {X
         [0]}]; ## BT0
         set property -dict {PACKAGE PIN D20 IOSTANDARD LVCMOS33} [get ports {X
         [1]}]; ## BT1
         set_property -dict {PACKAGE_PIN L20 IOSTANDARD LVCMOS33} [get_ports {X
         [2]}]; ## BT2
         set_property -dict {PACKAGE_PIN L19 IOSTANDARD LVCMOS33} [get_ports {X
         [3]}]; ## BT3
         ## LEDs
         set property -dict {PACKAGE PIN R14 IOSTANDARD LVCMOS33} [get ports
          {y}]; ## Led 0
```

▼ 11.5.3 Video of Deployment

MUX4_1_BV myHDL PYNQ-Z1 (YouTube (https://www.youtube.com/watch?v=vFG9kgLXJek))