

NAME -CHIRAG GARG

REG NO- 21BCE2769

DA 3



**VIT<sup>®</sup>**  
**Vellore Institute of Technology**  
(Deemed to be University under section 3 of UGC Act, 1956)

## **Digital assignment - III**

Class ID: VL2022230507148

Slots: Y11+Y12+Y21

- 1) Construct and explain the working principle of LED and PIN photo detector.

Digital Assignment-3

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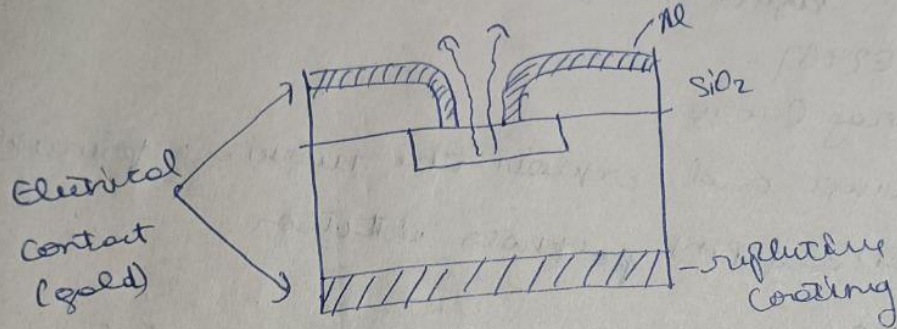
(b) LED

Light emitting diodes are semiconductor p-n junction diode which emits light when it is forward biased.

Construction

An n-type layer is grown on a substrate and a p-type layer is deposited on it by diffusion. Since carrier recombination takes place in the p-layer, it is deposited at the most for maximum light emission.

A metal film is deposited at the outer edge of the p-layer. The bottom of the substrate is coated with metal (gold) film for reflecting most of the light surface of the device and also provide connection with n-type layer.



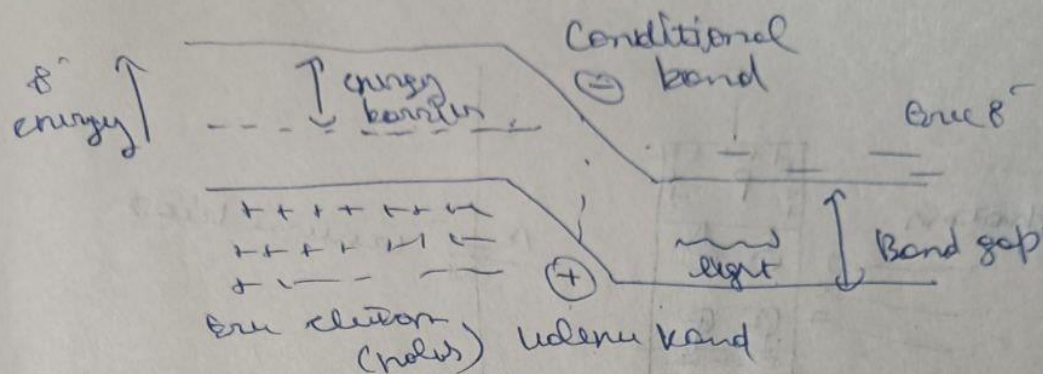
working

When p-n junction diode is forward biased the carrier width is reduced raising the potential energy on the n-side and lowering that on the p-side.

The free electrons and holes have sufficient energy to move into the junction region. If a free electron meets a hole, it recombines with each other resulting in the release of a photon.

The light radiation of the LED is caused by the recombination of holes and electrons that are injected into the junction by forward bias voltage.





### PIN photo detector

~~Construction~~

This is a device used to convert light energy into electrical energy.

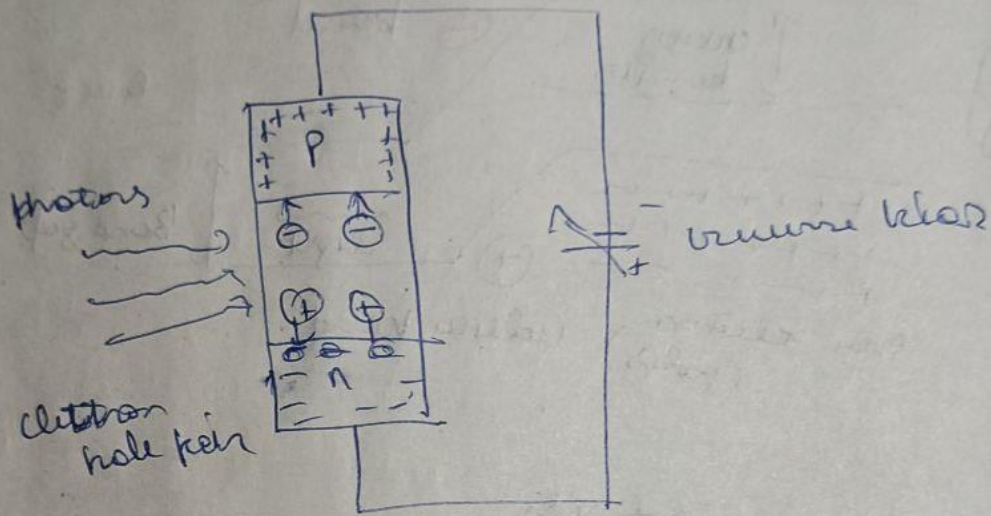
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It consists of three layers such as P, n and intrinsic region with proper

blocking

The P and n regions are heavily doped

The intrinsic layer is slightly larger than both P-type and n-type for creation of the light photons.



### Working

The PN diode is heavily reverse biased. When a photon of higher energy is incident over the larger width intrinsic semiconductor layer, the electron hole pairs are created.

The mobile charges are accelerated by applied voltage, which gives rise to the photo current in the external circuit.

It is linear device because of the photo current is directly proportional to the incident optical power on the PN-photo diode.



## Digital assignment - I

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1) Derive the wave equation of a string and write down the set of solutions of it.

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Engineering Physics  
DA-I

Consider y direction  
 $F_y = T \sin(\theta + d\theta) - T \sin \theta$

x direction force is always 0  $\approx T \cos(\theta + d\theta) - T \cos \theta$

As  $\sin \theta \approx \tan \theta$  when  $\theta$  is very small  
 $\tan \theta$  is also slope

$$F_y = T \frac{dy}{dx} \Big|_{x+\Delta x} - T \frac{dy}{dx} \Big|_x$$

We know that

$$\frac{dy}{dx} = \lim_{\Delta x \rightarrow 0} \frac{y(x+\Delta x, t) - y(x, t)}{\Delta x}$$

$$\frac{d^2 y}{dx^2} = \lim_{\Delta x \rightarrow 0} \frac{\frac{dy}{dx} \Big|_{x+\Delta x} - \frac{dy}{dx} \Big|_x}{\Delta x}$$

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From Newton's second law

$$F_y = m \frac{d^2 y}{dt^2} \quad a = \text{acceleration} = \frac{d^2 y}{dt^2}$$

$$m = \int ds \quad \rho = \text{mass density per unit length}$$

$$= \int \sqrt{(\Delta x)^2 + (\Delta y)^2} ds = \text{very small length}$$

$$= \rho \Delta x \sqrt{1 + \left(\frac{\Delta y}{\Delta x}\right)^2}$$

$$m \approx \rho \Delta x \quad v = \sqrt{\frac{T}{\rho}}$$

$$m \frac{d^2 y}{dt^2} = T \Delta x \frac{d^2 y}{dx^2}$$

$$\rho \Delta x \frac{d^2 y}{dt^2} = T \Delta x \frac{d^2 y}{dx^2}$$

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2) Consider a wave travelling along +x-axis through a string which has impedances  $z_1$  and  $z_2$  such that  $z_1 < z_2$ , write down the wave equations of incident, reflected and transmitted waves with diagrams.

Q-2

→ Incident wave can be described by the equation

$$y_1(x, t) = A_1 \cos(k_1 x - \omega t)$$

$A_1$  = Amplitude of incident wave

$k_1$  = wave number

$\omega$  = angular velocity

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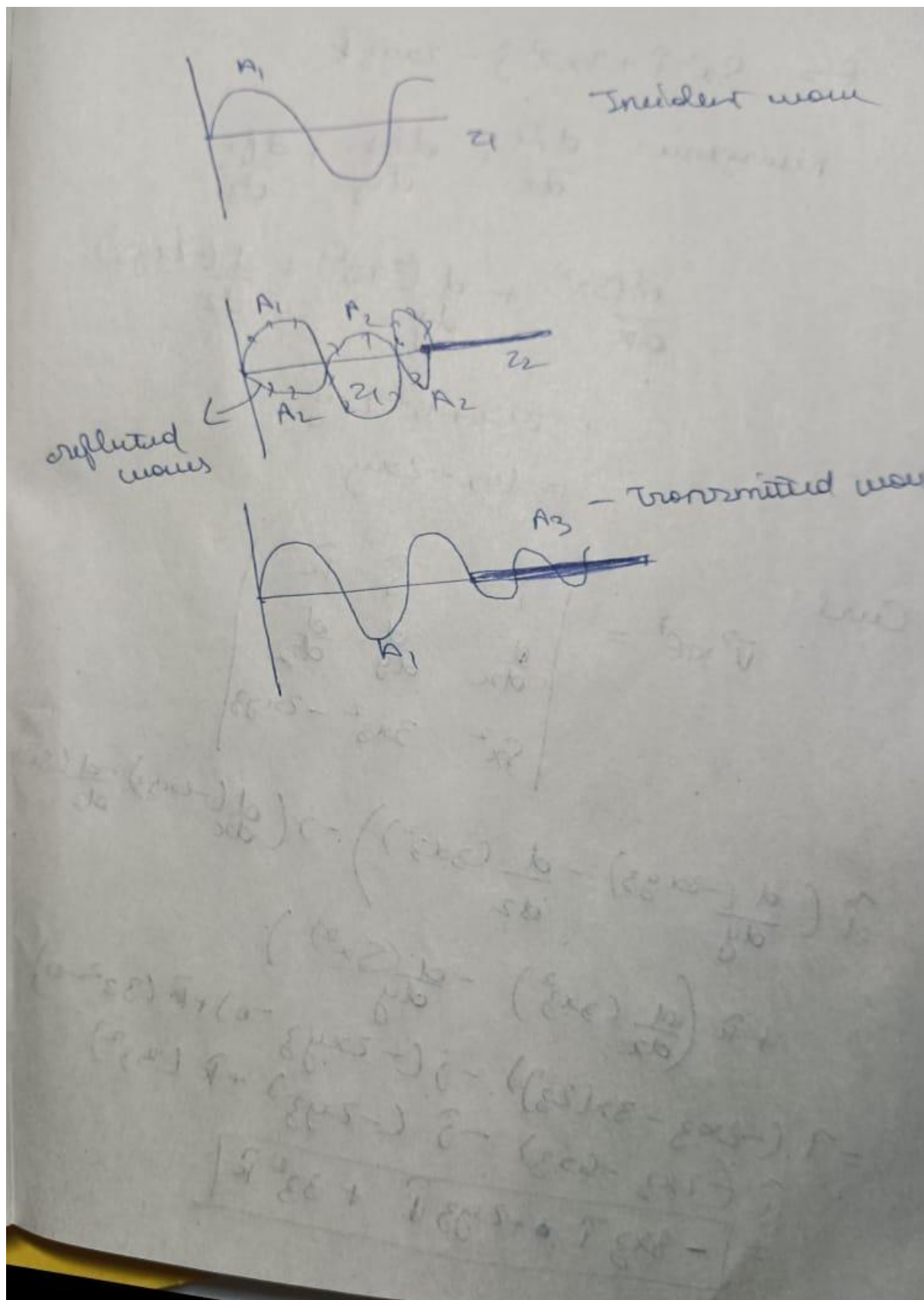
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3) Standing waves are formed by a string with length  $l$  whose ends are fixed by rigid walls. Derive the wavelength of a standing waves.

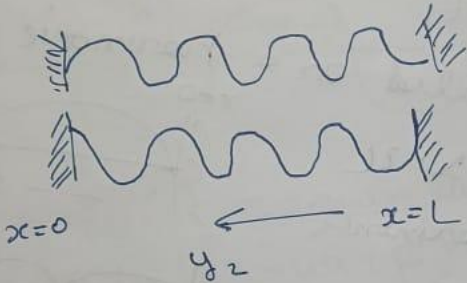
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$$y_k = y_1 + y_2$$

$$= A \sin(kx - \omega t) + A \sin(kx + \omega t)$$

$$y_k = 2A \sin kx \cos \omega t$$

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we need

$$2A \sin kL \cos \omega t = 0$$

$$\sin kL = 0$$

$$kL = n\pi$$

$$k_n = \frac{n\pi}{L}$$

$n = 1, 2, 3$

$$\lambda_n = \frac{2\pi}{k_n} = \frac{2\pi}{n\pi} L = \frac{2L}{n}$$

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4) Discuss the physical significance of gradient, divergence and curl. Calculate the divergence ( $\nabla \cdot \mathbf{f}$ ) and curl ( $\nabla \times \mathbf{f}$ ) of a given vector field

$$\mathbf{f} = 5x^2\hat{i} + 3xz^2\hat{j} - 2xyz\hat{k}$$

Q-4  
Ans

The gradient:

- Take height to be a function of  $x$  only. The gradient, then, would give you the direction (at a point) of greatest increase in height. In other words, it would point in the direction of steepest ~~or~~ elevation.
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The Divergence:

- This tells you, in some sense, how 'skiky' your vector field is at a point.
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- The curl tells you about the vector field's rotation (about a single point you're interested in)



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Divergence:  $\frac{d}{dx} + \frac{d}{dy} + \frac{d}{dz}$

$$\frac{d}{dx}(5x^2) + \frac{d}{dy}(3xz^2) + \frac{d}{dz}(-2xyz)$$

$$= 10x + 0 - 2xy$$

$$= 10x - 2xy$$

Curl:

$$\vec{\nabla} \times \vec{r} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{d}{dx} & \frac{d}{dy} & \frac{d}{dz} \\ 5x^2 & 3xz^2 & -2xyz \end{vmatrix}$$

$$\hat{i} \left( \frac{d}{dy}(-2xyz) - \frac{d}{dz}(3xz^2) \right) - \hat{j} \left( \frac{d}{dx}(-2xyz) - \frac{d}{dz}(5x^2) \right) + \hat{k} \left( \frac{d}{dx}(3xz^2) - \frac{d}{dy}(5x^2) \right)$$

$$= \hat{i}(-2xz - 3x(2z)) - \hat{j}(-2xy - 0) + \hat{k}(3z^2 - 0)$$

$$= \hat{i}(-2xz - 6xz) - \hat{j}(-2xy) + \hat{k}(3z^2)$$

$$= \boxed{-8xz \hat{i} + 2xy \hat{j} + 3z^2 \hat{k}}$$

5) Discuss the Maxwell's equations of electromagnetic wave. Derive the wave equation for electric and magnetic fields in vacuum.

The four Maxwell's eqn's are

1) Gauss's law

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constant

Gm make Biot's for free space in terms of  $\vec{B}$

$$\textcircled{1} \nabla \cdot \vec{B} = 0$$

$$\textcircled{2} \nabla \cdot \vec{B} = 0$$

$$\textcircled{3} \nabla \times \vec{E} = -\frac{d\vec{B}}{dt}$$

$$\textcircled{4} \nabla \times \vec{H} = \frac{d\vec{B}}{dt}$$



From Maxwell's 3rd Eqn

$$\vec{\nabla} \times \vec{E} = -\frac{d\vec{B}}{dt} \quad \text{--- (1)}$$

Taking curl of Eq (1)

$$\vec{\nabla} \times (\vec{\nabla} \times \vec{E}) = -\frac{d(\vec{\nabla} \times \vec{B})}{dt} \quad \text{--- (2)}$$

From vector identity we know

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$$\vec{\nabla} \cdot \vec{B} = 0 \text{ or } \vec{\nabla} \cdot \vec{E} = 0 \text{ for free space}$$

$$\& \vec{B} = \mu_0 \vec{H}$$

$$0 - \nabla^2 \vec{E} = \mu_0 \frac{d(\vec{\nabla} \times \vec{H})}{dt}$$

Maxwell's Eqn (4)  $\vec{\nabla} \times \vec{H} = \frac{d\vec{D}}{dt}$

$$\nabla^2 \vec{E} = \mu_0 \frac{d}{dt} \left( \frac{d\vec{D}}{dt} \right)$$

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$$\boxed{\vec{D} = \epsilon_0 \vec{E}}$$

Wave Equation

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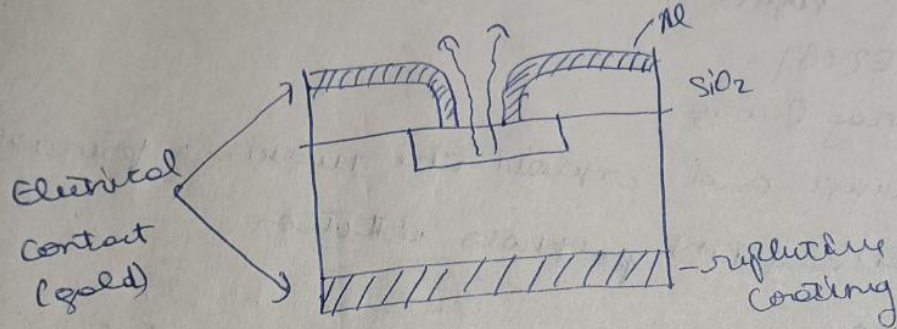
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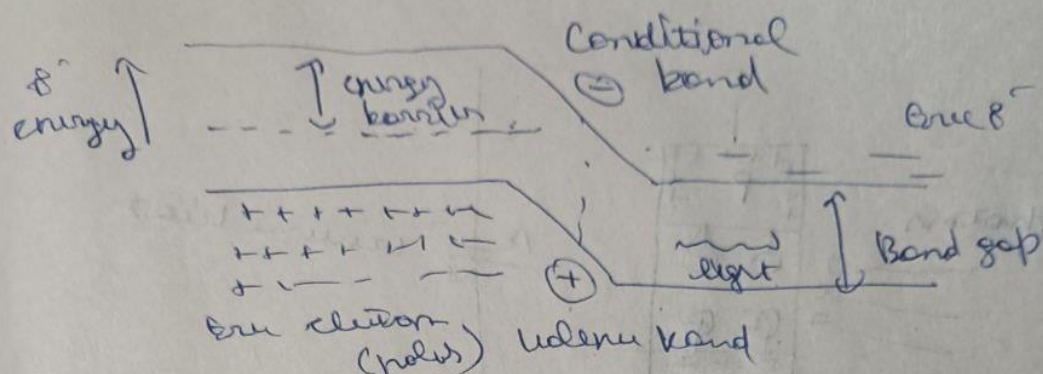


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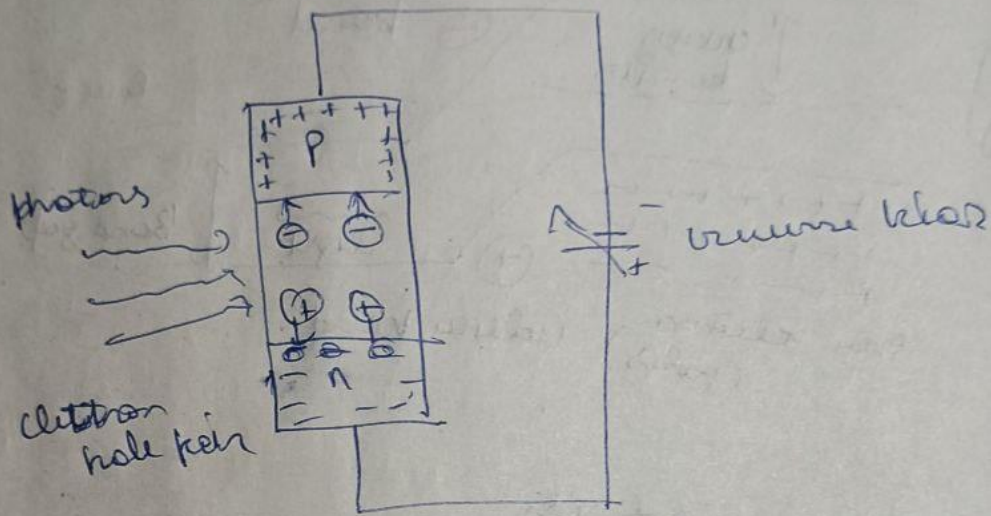
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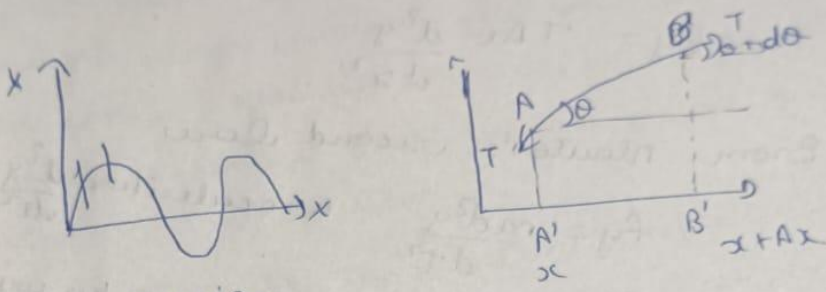
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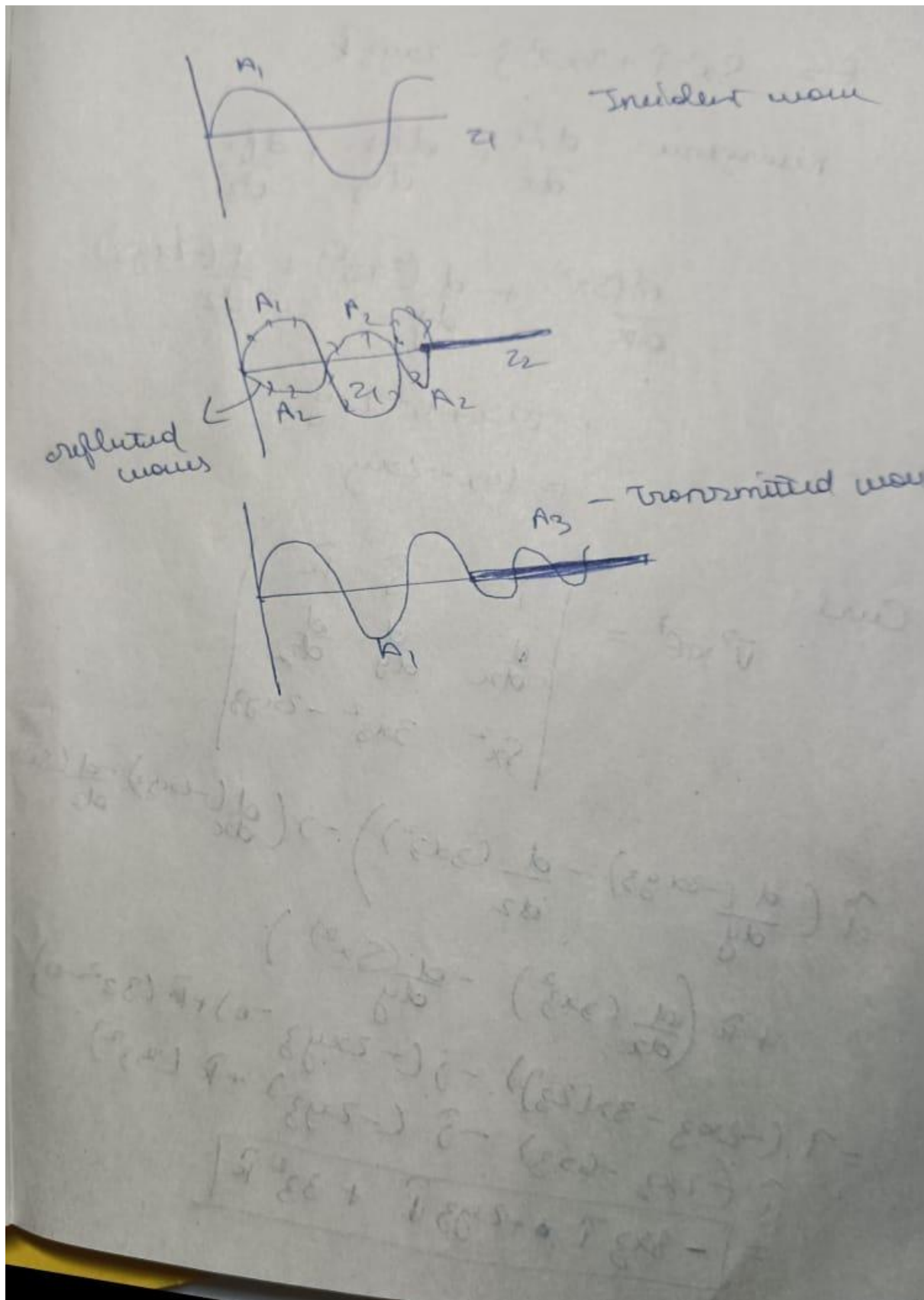
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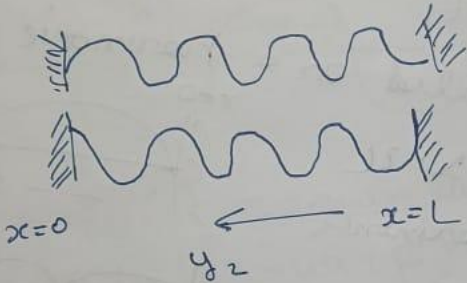
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From Maxwell's 3rd Eqn

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$$\nabla^2 \vec{E} = \mu_0 \epsilon_0 \frac{d^2 \vec{E}}{dt^2}$$

$$\boxed{\vec{D} = \epsilon_0 \vec{E}}$$

Wave Equation