# Introduction to Counting APAM E4990 Modeling Social Data

Jake Hofman

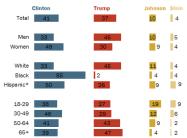
Columbia University

January 27, 2017

#### http://bit.ly/august2016poll

#### Demographic divides in candidate support

% of registered voters who support/lean toward ...



<sup>\*</sup> Small sample size: N=116.

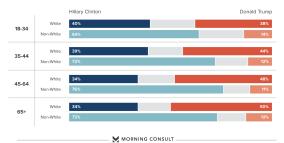
Notes: Based on registered voters. Whites and blacks include only those who are not Hispanic; Hispanics are of any race. Other/Don't know responses not shown. Q13/13a. Source: Survey conducted August 9-16, 2016.

#### PEW RESEARCH CENTER

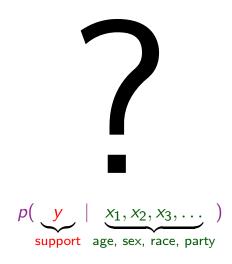


#### http://bit.ly/ageracepoll2016

If the Election Were Today, For Whom Would You Vote? (By Age & Race)



 $p(\underbrace{y}_{\text{support}} | \underbrace{x_1, x_2}_{\text{age, race}})$ 



#### Problem:

Traditionally difficult to obtain reliable estimates due to small sample sizes or sparsity

(e.g.,  $\sim$  100 age  $\times$  2 sex  $\times$  5 race  $\times$  3 party = 3,000 groups, but typical surveys collect  $\sim$  1,000s of responses)

#### Potential solution:

Sacrifice granularity for precision, by binning observations into larger, but fewer, groups

(e.g., bin age into a few groups: 18-29, 30-49, 50-64, 65+)

#### Potential solution:

Develop more sophisticated methods that generalize well from small samples

(e.g., fit a model: support  $\sim \beta_0 + \beta_1 age + \beta_2 age^2 + ...$ )

## (Partial) solution:

Obtain larger samples through other means, so we can just count and divide to make estimates via relative frequencies

(e.g., with  $\sim$  1M responses, we have 100s per group and can estimate support within a few percentage points)





Forecasting elections with non-representative polls
Wei Wang a.\*, David Rothschild b. Sharad Goel b. Andrew Gelman a.c.

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Compartment of Political Science, Columbia University, New York, NY, USA



Our analysis is based on an opt-in poll which was available continuously on the Xbox gaming platform during the 45 days preceding the 2012 US presidential election. Each day, three to five questions were posted, one of which gauged voter intention via the standard query, "If the election were held today, who would you vote for?". Full details of the questionnaire are given in the Appendix. The respondents were allowed to answer at most once per day. The first time they participated in an Xbox poll, respondents were also asked to provide basic demographic information about themselves, including their sex, race, age, education, state, party ID, political ideology, and who they voted for in the 2008 presidential election. In total 750, 148 interviews were conducted, witk 345,858 unique respondents - over 30,000 of whom completed five or more polls - making this one of the largest election panel studies ever.

http://bit.ly/nonreppoll

#### The good:

Shift away from sophisticated statistical methods on small samples to simpler methods on large samples

#### The bad:

Even simple methods (e.g., counting) are computationally challenging at large scales

(1M is easy, 1B a bit less so, 1T gets interesting)

#### Claim:

Solving the counting problem at scale enables you to investigate many interesting questions in the social sciences

# Learning to count

#### This week:

Counting at small/medium scales on a single machine

# Learning to count

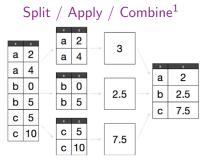
#### This week:

Counting at small/medium scales on a single machine

Following weeks:

Counting at large scales in parallel

# Counting, the easy way



- · Load dataset into memory
- Split: Arrange observations into groups of interest
- Apply: Compute distributions and statistics within each group
- Combine: Collect results across groups

# The generic group-by operation

Split / Apply / Combine

for each observation as (group, value):
 place value in bucket for corresponding group

for each group:
 apply a function over values in bucket
 output group and result

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for each observation as (group, value):
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Useful for computing arbitrary within-group statistics when we have required memory

(e.g., conditional distribution, median, etc.)

#### Anatomy of the Long Tail: Ordinary People with Extraordinary Tastes

Sharad Goel<sup>‡</sup>, Andrei Broder<sup>‡</sup>, Evgeniy Gabrilovich<sup>‡</sup>, Bo Pang<sup>‡</sup> ‡ Yahoo! Research, 111 West 40th Street, New York, NY 10018, USA † Yahoo! Research, 4301 Great America Parkway, Santa Clara, CA 95054, USA {goel, broder, gabr, bopang}@yahoo-inc.com

#### ABSTRACT

The success of "infinite-inventory" retailers such as Amazon.com and Netflix has been ascribed to a "long tail" phenomenon. To wit, while the majority of their inventory is not in high demand, in aggregate these "worst sellers," unavailable at limited-inventory competitors, generate a significant fraction of total revenue. The long tail phenomenon, however, is in principle consistent with two fundamentally different theories. The first, and more popular hypothesis, is that a majority of consumers consistently follow the crowds and only a minority have any interest in niche content; the sec-

#### Categories and Subject Descriptors

J.4 [Computer Applications]: Social and Behavioral Sciences

#### General Terms

Economics, Measurement

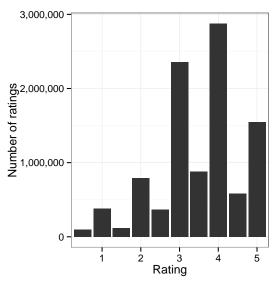
#### Keywords

Long tail, infinite inventory

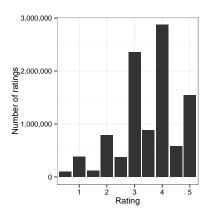
Dataset	Users	Items	Rating levels	Observations
Movielens	100K	10K	10	10M
Netflix	500K	20K	5	100M

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How many ratings are there at each star level?



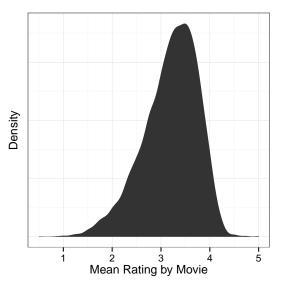
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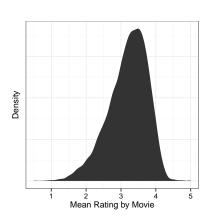
group by rating value
for each group:
 count # ratings

13 / 27

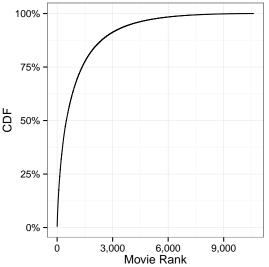
What is the distribution of average ratings by movie?



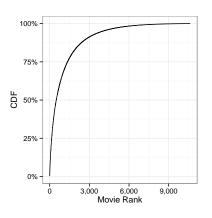
group by movie id for each group: compute average rating



What fraction of ratings are given to the most popular movies?



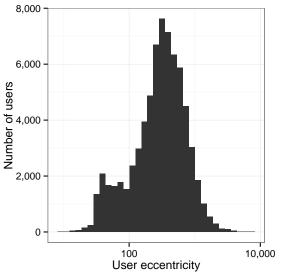
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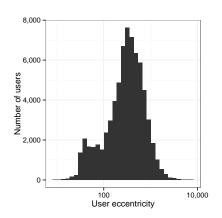
group by movie id for each group: count # ratings

sort by group size cumulatively sum group sizes

What is the median rank of each user's rated movies?



join movie ranks to ratings
group by user id
for each group:
compute median movie rank



Dataset	Users	Items	Rating levels	Observations
Movielens	100K	10K	10	10M
Netflix	500K	20K	5	100M

What do we do when the full dataset exceeds available memory?

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What do we do when the full dataset exceeds available memory?

Sampling?
Unreliable estimates for rare groups

Dataset	Users	Items	Rating levels	Observations
Movielens	100K	10K	10	10M
Netflix	500K	20K	5	100M

What do we do when the full dataset exceeds available memory?

Random access from disk? 1000x more storage, but 1000x slower<sup>2</sup>

Dataset	Users	Items	Rating levels	Observations
Movielens	100K	10K	10	10M
Netflix	500K	20K	5	100M

What do we do when the full dataset exceeds available memory?

## Streaming

Read data one observation at a time, storing only needed state

# The combinable group-by operation

## Streaming

```
for each observation as (group, value):
   if new group:
     initialize result
```

update result for corresponding group as function of existing result and current value

```
for each group:
  output group and result
```

# The combinable group-by operation

#### Streaming

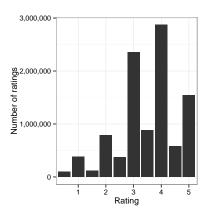
```
for each observation as (group, value):
   if new group:
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update result for corresponding group as function of existing result and current value

```
for each group:
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```

Useful for computing a subset of within-group statistics with a limited memory footprint

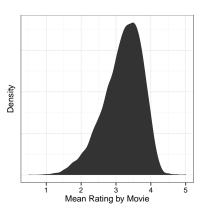
(e.g., min, mean, max, variance, etc.)



for each rating:
 counts[movie id]++

```
for each rating:
  totals[movie id] += rating
  counts[movie id]++
```

for each group:
 totals[movie id] /
 counts[movie id]



23 / 27

# Yet another group-by operation

# Per-group histograms

```
for each observation as (group, value):
   histogram[group][value]++
```

for each group:
 compute result as a function of histogram
 output group and result

# Yet another group-by operation

## Per-group histograms

for each observation as (group, value):
 histogram[group][value]++

for each group:
 compute result as a function of histogram
 output group and result

We can recover arbitrary statistics if we can afford to store counts of all distinct values within in each group

# The group-by operation

## For arbitrary input data:

Memory	Scenario	Distributions	Statistics
N	Small dataset	Yes	General
V*G	Small distributions	Yes	General
G	Small # groups	No	Combinable
V	Small # outcomes	No	No
1	Large # both	No	No

N =total number of observations

G = number of distinct groups

V =largest number of distinct values within group

# Examples (w/8GB RAM)

Median rating by movie for Netflix

 $N \sim 100 \mathrm{M}$  ratings  $G \sim 20 \text{K}$  movies  $V\sim 10$  half-star values

 $V^*G \sim 200$ K, store per-group histograms for arbitrary statistics

(scales to arbitrary N, if you're patient)

# Examples (w/8GB RAM)

#### Median rating by video for YouTube

 $N \sim 10 \text{B}$  ratings  $G \sim 1$ B videos  $V \sim 10$  half-star values

 $V^*G \sim 10$ B, fails because per-group histograms are too large to store in memory

 $G \sim 1$ B, but no (exact) calculation for streaming median

# Examples (w/ 8GB RAM)

Mean rating by video for YouTube

 $N\sim 10$ B ratings  $G\sim 1$ B videos  $V\sim 10$  half-star values

 $G \sim 1$ B, use streaming to compute combinable statistics

# The group-by operation

## For pre-grouped input data:

Memory	Scenario	Distributions	Statistics
N	Small dataset	Yes	General
V*G	Small distributions	Yes	General
G	Small $\#$ groups	No	Combinable
V	Small # outcomes	Yes	General
1	Large $\#$ both	No	Combinable

N =total number of observations

G = number of distinct groups

V =largest number of distinct values within group