



**UNIVERSIDAD POLITÉCNICA**  
DE LA ZONA METROPOLITANA DE GUADALAJARA

Materia: Cinemática de robots  
Profesor: Morán Garabito Carlos Enrique

## **PRACTICA # 2**



**T/M 8`B**  
**UPZMG**

Alumno: **CHRISTIAN SALVADOR GOMEZ CARRILLO,**



**(-7,-7), (2,-9), (-8,-3)**

**(-7,-7)**

$$q2 = \text{atan}\left(\frac{-7^2 + -7^2 - 30^2 - 20^2}{20(30)(20)}\right)$$

$$= -1.001 \quad q2 = \text{atan}(-1.001) \quad q2 = -45.04$$

$$q1 = \text{atan}\left(\frac{8}{2}\right) - \text{atan}\left(\frac{20 \sin(-45.04)}{30 + 20 \cos(-45.735)}\right) = \frac{-14.45}{44.13}$$

$$q1 = \text{atan}(4) - \text{atan}(-0.327) = 94.07$$

**(2,-9)**

$$q2 = \text{atan}\left(\frac{2^2 + (-9^2) - 30^2 - 20^2}{2(30)(20)}\right)$$

$$= -1.00125 \quad q2 = \text{atan}(-1.00125) \quad q2 = -45.35$$

$$q2 = \text{atan}\frac{8}{2} - \text{atan}\left(\frac{20 \sin(-45.35)}{30 + 20 \cos(-45.35)}\right) = \frac{-14.22}{44.05} = 0.3228$$

$$q1 = \text{atan}(4) - \text{atan}(0.3228) = 58.07$$

**(-8,-3)**

$$q2 = \text{atan}\left(\frac{-8^2 + (-3^2) - 30^2 - 20^2}{2(30)(20)}\right) = -1.144$$

$$= -1.00141 \quad q2 = \text{atan}(-1.00125) \quad q2 = -48.84$$

$$q2 = \text{atan}\frac{8}{2} - \text{atan}\left(\frac{20 \sin(-48.85)}{30 + 20 \cos(-48.85)}\right) = \frac{-15.05}{43.16} = 0.3489$$

$$q1 = \text{atan}(4) - \text{atan}(0.3428) = 56.76$$



SEGUNDA PARTE:

$$\begin{bmatrix} -L_1 \text{Sen}(q_1) & -L_2 \text{Sen}(q_1 + q_2) \\ -L_1 \text{Cos}(q_1) & -L_1 \text{Cos}(q_1 + q_2) \end{bmatrix} \begin{bmatrix} -L_2 \text{Sen}(q_1 + q_2) \\ -L_2 \text{Cos}(q_1 + q_2) \end{bmatrix}$$

(-7,-7)  $q_1 = 94.07$   $q_2 = -45.04$

$$\begin{bmatrix} -30 \text{Sen}(94.07) & -L_2 \text{Sen}(94.07 + (-45.04)) \\ -30 \text{Cos}(94.07) & -L_1 \text{Cos}(94.07 + (-45.04)) \end{bmatrix} \begin{bmatrix} -20 \text{Sen}(94.07 + (-45.04)) \\ -20 \text{Cos}(94.07 + (-45.04)) \end{bmatrix}$$

(2,-9)  $q_1 = 58.07$   $q_2 = -45.35$

$$\begin{bmatrix} -30 \text{Sen}(58.07) & -L_2 \text{Sen}(58.07 + (-45.35)) \\ -30 \text{Cos}(58.07) & -L_1 \text{Cos}(58.07 + (-45.35)) \end{bmatrix} \begin{bmatrix} -20 \text{Sen}(58.07 + (-45.35)) \\ -20 \text{Cos}(58.07 + (-45.35)) \end{bmatrix}$$

(-8,-3)  $q_1 = 56.72$   $q_2 = -48.84$

$$\begin{bmatrix} -30 \text{Sen}(56.72) & -L_2 \text{Sen}(56.72 + (-48.84)) \\ -30 \text{Cos}(56.72) & -L_1 \text{Cos}(56.72 + (-48.84)) \end{bmatrix} \begin{bmatrix} -20 \text{Sen}(56.72 + (-48.84)) \\ -20 \text{Cos}(56.72 + (-48.84)) \end{bmatrix}$$



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Dinámica 4

(1) (-1, 1), (2, 1), (-8, -3)

$q_2 = \arctan \left( \frac{(-1)^2 + (1)^2 - (30)^2 - (20)^2}{2(30)(20)} \right) = -1.001$

$q_2 = \arctan(-1.001) = -45.01$

$q_1 = \arctan \left( \frac{8}{2} \right) - \arctan \left( \frac{20 \sin(-45.01)}{30 + 20 \cos(-45.735)} \right) = \frac{-19.45}{44.13}$

$q_1 = \arctan(4) - \arctan(-0.327) = 99.07$

(2, -9)

$q_2 = \arctan \left( \frac{(2)^2 + (-9)^2 - (30)^2 - (20)^2}{2(30)(20)} \right) = -1.0125$

$q_2 = \arctan(-1.0125) = -45.35$

$q_1 = \arctan \left( \frac{8}{2} \right) - \arctan \left( \frac{20 \sin(-45.35)}{30 + 20 \cos(-45.35)} \right) = \frac{-14.22}{44.05} = 0$

$q_1 = \arctan(4) - \arctan(0.3228) = 58.07$

(-8, -3)

$q_2 = \arctan \left( \frac{(-8)^2 + (-3)^2 - (30)^2 - (20)^2}{2(30)(20)} \right) = -1.1441$

$q_2 = \arctan(-1.0125) = -48.84$

$q_1 = \arctan \left( \frac{8}{2} \right) - \arctan \left( \frac{20 \sin(-48.84)}{20 + 20 \cos(-48.84)} \right) = \frac{-15.05}{43.16} = 0$

$q_1 = \arctan(4) - \arctan(0.3484) = 56.22$