Contribution: Yitong Li mainly finish the exercise 1 and Guoqing Liang mainly finish the exercise 2.

Code Link: CHU-2002/DD2360HT23 (github.com)

Exercise 1

- 1. Describe all optimizations you tried regardless of whether you committed to them or abandoned them and whether they improved or hurt performance
 - a) I tried use shard memory in kernel fuction, but there's no obvious effect.

As far as I'm concerned, the reason is the kernel cost only little time, even in the following example, 123154341, the kernel only cost 0.000013s. So Even the shared memory accelerate the computation, it is hard to detect.

I test 5 times for each method, here is the results(length = 123156789,time of kernal):

shared	0.000024s	0.000014	0.000013	0.000022	0.000018
golobal	0.000014	0.000016	0.000012	0.000015	0.000012

On average, 0.000004 seconds faster with shared memory.

```
The input length is 123154341

GPU cudaMemcpy Time elapsed 0.103810 sec

GPU histogram_kernel 1 Time elapsed 0.000013 sec

GPU histogram_kernel 4 Time elapsed 0.118223 sec

GPU convert_kernel Time elapsed 0.000071 sec

GPU cudaMemcpy Time elapsed 0.003455 sec

Correct!
```

b) I tried use streams, but because of the time cost in memory copy, it is hard to detect optimazation. As shown in FIG. The time kernel cost is ignorable.

2. Which optimizations you chose in the end and why?

Although the effect is not obvious, I still chose the above two optimizations. The reasons refer to the above description. In theory, these two optimizations are effective but little.

3. How many global memory reads are being performed by your kernel? Explain

For each data, read 1 time. To sum the results, each block read MUN_BINS times. So the number of reads of global memory is inputLength + MUM_BINS * MUM_Block = inputLength + 4,194,304.

4. How many atomic operations are being performed by your kernel? Explain

For each data, once. To sum the results, each block atinucAdd MUN_BINS times. So the number of reads of global memory is inputLength + MUM_BINS * MUM_Block = inputLength + 4,194,304.

5. How much shared memory is used in your code? Explain

For each Block, 4096 * 4bytes. So MUM_Block * 4096 * 4bytes = 16.78MB T4 provide 49152bytes per block, which is Sufficient for it.

6. How would the value distribution of the input array affect the contention among threads? For instance, what contentions would you expect if every element in the array has the same value?

The more concentrated the distribution, the more severe the contention. Because of the atomic operation, if two threads add to one bin, the contention occurred. So if every element in the array has the same value, contention will occur in each thread.

7. Plot a histogram generated by your code and specify your input length, thread block and grid.

Input length is 12949, gird is 1024 and block is 1024.

Here is a screen shot of the Top results. Please check the appendix A to check the full results.



8. For a input array of 1024 elements, profile with Nvidia Nsight and report Shared Memory Configuration Size and Achieved Occupancy. Did Nvsight report any potential performance issues?

Please check the appendix B to get the full results.

As the screen shot following. Shared Memory Configuration Size is 32.77 Kb. And static shared memory per block is 16.38 bytes. Here is no issues. Achieved Occupancy is 14.11%, here is no issues too.

histogram_kernel(unsigned int *, unsigned int *, unsigned int, unsigned int), 2023-Dec-10 20:48:23, Context 1, Stream 13 Section: GPU Speed Of Light Throughput

DRAM Frequency	cycle/nsecond	5.00
SM Frequency	cycle/usecond	584.93
Elapsed Cycles	cycle	1,989,984
Memory [%]	%	15.90
DRAM Throughput	%	0.01
Duration	msecond	3.40
L1/TEX Cache Throughput	%	16.19
L2 Cache Throughput	%	4.75
SM Active Cycles	cycle	1,954,370.30
Compute (SM) [%]	%	15.90

WRN This kernel exhibits low compute throughput and memory bandwidth utilization relative to the peak performance of this device. Achieved compute throughput and/or memory bandwidth below 60.0% of peak typically indicate latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons.

Section: Launch Statistics

Block Size		1,024
Function Cache Configuration		cudaFuncCachePreferNone
Grid Size		1,024
Registers Per Thread	register/thread	16
Shared Memory Configuration Size	Kbvte	32.77 0 0
Driver Shared Memory Per Block	byte/block	
Dynamic Shared Memory Per Block	byte/block	
Static Shared Memory Per Block	Kbyte/block	16.38
Threads	thread	1,048,576
Waves Per SM		25.60
Section: Occupancy		
Block Limit SM	block	16
Block Limit Registers	block	4
Block Limit Shared Mem	block	2
Block Limit Warps	block	1
Theoretical Active Warps per SM	warp	32
Theoretical Occupancy	%	100
Achieved Occupancy	%	14.11
Achieved Active Warps Per SM	warp	4.51

This kernel's theoretical occupancy is not impacted by any block limit. The difference between calculated theoretical (100.0%) and measured achieved occupancy (14.1%) can be the result of warp scheduling overheads or workload imbalances during the kernel execution. Load imbalances can occur between warps within a block as well as across blocks of the same kernel. See the CUDA Best Practices Guide (https://docs.nvidia.com/cuda/cuda-c-best-practices-guide/index.html#occupancy) for more details on optimizing occupancy.

Exercise 2

```
__global__ void MoverKernel(struct particles* part, struct EMfield* field, struct grid
   * grd, struct parameters* param){
2.
          int i = threadIdx.x + blockIdx.x * blockDim.x;
3.
4.
          if(i < part->nop){
5.
              // auxiliary variables
6.
              FPpart dt_sub_cycling = (FPpart) param->dt/((double) part->n_sub_cycles);
7.
              FPpart dto2 = .5*dt_sub_cycling, qomdt2 = part->qom*dto2/param->c;
8.
              FPpart omdtsq, denom, ut, vt, wt, udotb;
9.
10.
              // local (to the particle) electric and magnetic field
11.
              FPfield Exl=0.0, Eyl=0.0, Ezl=0.0, Bxl=0.0, Byl=0.0, Bzl=0.0;
```

```
12.
13.
              // interpolation densities
14.
             int ix,iy,iz;
15.
             FPfield weight[2][2][2];
16.
             FPfield xi[2], eta[2], zeta[2];
17.
18.
             // intermediate particle position and velocity
19.
             FPpart xptilde, yptilde, zptilde, uptilde, vptilde, wptilde;
20.
21.
22.
23.
24.
             xptilde = part->x[i];
25.
             yptilde = part->y[i];
26.
             zptilde = part->z[i];
27.
             // calculate the average velocity iteratively
28.
             for(int innter=0; innter < part->NiterMover; innter++){
29.
                 // interpolation G-->P
30.
                 ix = 2 + int((part->x[i] - grd->xStart)*grd->invdx);
31.
                 iy = 2 + int((part->y[i] - grd->yStart)*grd->invdy);
32.
                  iz = 2 + int((part->z[i] - grd->zStart)*grd->invdz);
33.
34.
                 // calculate weights
35.
                 xi[0] = part-x[i] - grd-xN[ix - 1][iy][iz];
36.
                  eta[0] = part->y[i] - grd->YN[ix][iy - 1][iz];
37.
                 zeta[0] = part->z[i] - grd->ZN[ix][iy][iz - 1];
38.
                        = grd->XN[ix][iy][iz] - part->x[i];
39.
                 eta[1] = grd->YN[ix][iy][iz] - part->y[i];
40.
                  zeta[1] = grd->ZN[ix][iy][iz] - part->z[i];
41.
                 for (int ii = 0; ii < 2; ii++)
42.
                     for (int jj = 0; jj < 2; jj++)
43.
                         for (int kk = 0; kk < 2; kk++)
44.
                             weight[ii][jj][kk] = xi[ii] * eta[jj] * zeta[kk] * grd->invVOL
45.
46.
                  // set to zero local electric and magnetic field
47.
                 Exl=0.0, Eyl=0.0, Ezl=0.0, Bxl=0.0, Byl=0.0, Bzl=0.0;
48.
49.
                 for (int ii=0; ii < 2; ii++)
50.
                      for (int jj=0; jj < 2; jj++)
51.
                         for(int kk=0; kk < 2; kk++){
52.
                             Exl += weight[ii][jj][kk]*field->Ex[ix- ii][iy -jj][iz- kk ];
53.
                             Eyl += weight[ii][jj][kk]*field->Ey[ix- ii][iy -jj][iz- kk ];
54.
                             Ezl += weight[ii][jj][kk]*field->Ez[ix- ii][iy -jj][iz -kk ];
```

```
55.
                              Bxl += weight[ii][jj][kk]*field->Bxn[ix- ii][iy -jj][iz -kk ];
56.
                              Byl += weight[ii][jj][kk]*field->Byn[ix- ii][iy -jj][iz -kk ];
57.
                              Bzl += weight[ii][jj][kk]*field->Bzn[ix- ii][iy -jj][iz -kk ];
58.
59.
60.
                  // end interpolation
61.
                  omdtsq = qomdt2*qomdt2*(Bxl*Bxl+Byl*Byl+Bzl*Bzl);
62.
                  denom = 1.0/(1.0 + \text{omdtsq});
63.
                  // solve the position equation
64.
                  ut= part->u[i] + qomdt2*Exl;
65.
                  vt= part->v[i] + qomdt2*Eyl;
66.
                  wt= part->w[i] + qomdt2*Ezl;
67.
                  udotb = ut*Bxl + vt*Byl + wt*Bzl;
68.
                  // solve the velocity equation
69.
                  uptilde = (ut+qomdt2*(vt*Bzl -wt*Byl + qomdt2*udotb*Bxl))*denom;
70.
                  vptilde = (vt+qomdt2*(wt*Bxl -ut*Bzl + qomdt2*udotb*Byl))*denom;
71.
                  wptilde = (wt+qomdt2*(ut*Byl -vt*Bxl + qomdt2*udotb*Bzl))*denom;
72.
                  // update position
73.
                  part->x[i] = xptilde + uptilde*dto2;
74.
                  part->y[i] = yptilde + vptilde*dto2;
75.
                  part->z[i] = zptilde + wptilde*dto2;
76.
77.
78.
              } // end of iteration
79.
              // update the final position and velocity
80.
              part->u[i]= 2.0*uptilde - part->u[i];
81.
              part->v[i]= 2.0*vptilde - part->v[i];
82.
              part->w[i]= 2.0*wptilde - part->w[i];
83.
              part->x[i] = xptilde + uptilde*dt_sub_cycling;
84.
              part->y[i] = yptilde + vptilde*dt_sub_cycling;
85.
              part->z[i] = zptilde + wptilde*dt_sub_cycling;
86.
87.
88.
89.
90.
              //////// BC
91.
92.
              // X-DIRECTION: BC particles
93.
              if (part->x[i] > grd->Lx){
94.
                  if (param->PERIODICX==true){ // PERIODIC
95.
                      part->x[i] = part->x[i] - grd->Lx;
96.
                  } else { // REFLECTING BC
97.
                      part->u[i] = -part->u[i];
98.
                      part-x[i] = 2*grd-xx - part-x[i];
```

```
99.
100.
              }
101.
102.
              if (part->x[i] < 0){</pre>
103.
                  if (param->PERIODICX==true){ // PERIODIC
104.
                      part->x[i] = part->x[i] + grd->Lx;
105.
                  } else { // REFLECTING BC
106.
                      part \rightarrow u[i] = -part \rightarrow u[i];
107.
                      part->x[i] = -part->x[i];
108.
                  }
109.
110.
111.
112.
              // Y-DIRECTION: BC particles
113.
              if (part->y[i] > grd->Ly){
114.
                  if (param->PERIODICY==true){ // PERIODIC
115.
                      part-y[i] = part-y[i] - grd-y;
116.
                  } else { // REFLECTING BC
117.
                      part->v[i] = -part->v[i];
118.
                      part-y[i] = 2*grd-yy - part-yy[i];
119.
120.
              }
121.
122.
              if (part-y[i] < 0){
123.
                  if (param->PERIODICY==true){ // PERIODIC
124.
                      part-y[i] = part-y[i] + grd->Ly;
125.
                  } else { // REFLECTING BC
126.
                      part->v[i] = -part->v[i];
127.
                     part->y[i] = -part->y[i];
128.
                  }
129.
130.
131.
              // Z-DIRECTION: BC particles
132.
              if (part->z[i] > grd->Lz){
133.
                  if (param->PERIODICZ==true){ // PERIODIC
134.
                      part->z[i] = part->z[i] - grd->Lz;
135.
                  } else { // REFLECTING BC
136.
                      part->w[i] = -part->w[i];
137.
                     part->z[i] = 2*grd->Lz - part->z[i];
138.
                  }
139.
140.
141.
              if (part->z[i] < 0){</pre>
142.
                  if (param->PERIODICZ==true){ // PERIODIC
```

```
143.
                     part->z[i] = part->z[i] + grd->Lz;
144.
                 } else { // REFLECTING BC
145.
                     part->w[i] = -part->w[i];
146.
                     part->z[i] = -part->z[i];
147.
148.
             }
149.
150.
151.
152.
153.
154.
155.
156. }
157.
158.
159.
160.
161. /** particle mover */
162. int mover_PC(struct particles* h_part, struct EMfield* h_field, struct grid* h_grd, st
   ruct parameters* h_param)
163. {
164.
         // print species and subcycling
         std::cout << "*** MOVER with SUBCYCLYING "<< h_param->n_sub_cycles << " - species
    " << h_part->species_ID << " ***" << std::endl;
166.
167.
168.
         // start subcycling
169.
        for (int i_sub=0; i_sub < h_part->n_sub_cycles; i_sub++){
170.
171.
172.
173.
174.
             int ThreadsPerBlock = 256;
175.
             int BlocksPerGrid = (h_part->nop + ThreadsPerBlock - 1)/ThreadsPerBlock;
176.
177.
             particles *part;
178.
             EMfield *field;
179.
             grid *grd;
180.
             parameters *param;
181.
182.
183.
184.
             cudaMalloc( &part , sizeof(particles));
```

```
185.
              cudaMalloc( &field , sizeof(EMfield));
186.
              cudaMalloc( &grd
                               , sizeof(grid));
187.
              cudaMalloc( &param , sizeof(parameters));
188.
189.
              cudaMemcpy( part, h_part, sizeof(particles), cudaMemcpyHostToDevice);
190.
              cudaMemcpy( field, h field, sizeof(EMfield),
                                                             cudaMemcpyHostToDevice);
191.
              cudaMemcpy( grd, h_grd, sizeof(grid), cudaMemcpyHostToDevice);
192.
              cudaMemcpy( param, h_param, sizeof(parameters), cudaMemcpyHostToDevice);
193.
194.
195.
              // move each particle with new fields
196.
              MoverKernel<<<BlocksPerGrid, ThreadsPerBlock>>>(part, field, grd, param);
197.
198.
              cudaMemcpy( h_part, part, sizeof(particles), cudaMemcpyDeviceToHost);
199.
              cudaMemcpy( h_field, field, sizeof(EMfield), cudaMemcpyDeviceToHost);
200.
              cudaMemcpy( h_grd,
                                         sizeof(grid),
                                                             cudaMemcpyDeviceToHost);
                                  grd,
201.
              cudaMemcpy( h_param, param, sizeof(parameters), cudaMemcpyDeviceToHost);
202.
203.
              cudaFree(part);
204.
              cudaFree(field);
205.
              cudaFree(grd);
206.
              cudaFree(param);
207.
208.
          } // end of one particle
209.
210.
          return(0); // exit successfully
211. } // end of the mover
```

1. Describe the environment you used, what changes you made to the Makefile, and how you ran the simulation.

The code was run on Google Colab T4 GPU. To make Makefile work correctly, I changed ARCH from "sm_30" to "sm_75", which stands for the latest version of NVIDIA GPU. After executing Makefile, a new file 'sputniPIC.out' was created and it can be used to ran the simulation.

2. Describe your design of the GPU implementation of mover_PC() briefly.

To enhance the performance of mover_PC(), a new global kernel 'MoverKernel' was created to conduct the calculation the average velocity of particles. When we need to move particle, the kernel will called and the calculation will be carried out in parallel on GPU.

3. Compare the output of both CPU and GPU implementation to guarantee that your GPU implementations produce correct answers.

Calling the original implementation function and comparePart() at the end of mover_pc() to

compare the result of two versions. The result shows that two version conduct same operation on particle.

```
void comparePart(struct particles* part1, struct particles* part2){
2.
          bool result = true:
3.
        for (int i=0; i < part1->nop; i++){
4.
            if(part1->x[i] != part2->x[i] || part1->y[i] != part2->y[i] || part1->z[i] != part2->z[i]||
5.
              part1->u[i] != part2->u[i] || part1->v[i] != part2->v[i] || part1->w[i] != part2->w[i]){
6.
              result = false;
7.
8.
9.
         if(result){
10.
          std::cout <<"GPU version and GPU version have SAME result "<< std::endl:
11.
12.
         else{
13.
         std::cout <<"GPU version and GPU version have DIFFERENT result "<< std::endl;
14.
15. }
```

```
cvcle = 1
*******
*** MOVER with SUBCYCLYING 1 - species 0 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 1 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 2 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 3 ***
GPU version and GPU version have SAME result
********
  cycle = 2
********
*** MOVER with SUBCYCLYING 1 - species 0 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 1 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 2 ***
GPU version and GPU version have SAME result
*** MOVER with SUBCYCLYING 1 - species 3 ***
GPU version and GPU version have SAME result
```

4. Compare the execution time of your GPU implementation with its CPU version.

Comparing to CPU version, the running time of the GPU version has significantly decreased.

CPU version:

GPU version:

Appendix A:

Results of EX1, question 7:
The input length is 12949
GPU histogram_kernel 4 Time elapsed 0.000112 sec
GPU convert_kernel Time elapsed 0.000007 sec
GPU cudaMemcpy Time elapsed 0.013441 sec
Correct!

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Appendix B:

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==PROF== Connected to process 41400 (/content/drive/MyDrive/Assignment3/a.out)
The input length is 1024
==PROF== Profiling "histogram_kernel" - 0: 0%....50%....100% - 8 passes
==PROF== Profiling "histogram_kernel" - 1: 0%....50%....100% - 8 passes
==PROF== Profiling "histogram_kernel" - 2: 0%....50%....100% - 8 passes
==PROF== Profiling "histogram_kernel" - 3: 0%....50%....100% - 8 passes
GPU histogram_kernel 4 Time elapsed 0.955816 sec
==PROF== Profiling "convert_kernel" - 4: 0%....50%....100% - 8 passes
GPU convert_kernel Time elapsed 0.151852 sec
GPU cudaMemcpy Time elapsed 0.000062 sec
Correct!
==PROF== Disconnected from process 41400
```

DRAM Frequency			
cycle/nsecond	5.00		
SM Frequency			
cycle/usecond	584.93		
Elapsed Cycles			
cycle	1,989,984		
Memory			
[%]			%
15.90			
DRAM			
Throughput			
%	0.01		
Duration			
msecond	3.40		
L1/TEX Cache			
Throughput	%		
16.19			
L2 Cache			
Throughput		%	
4.75			
SM Active Cycles			
cycle	1,954,370.30		
Compute (SM)			
[%]	%		
15.90			
	l exhibits low compute throughput and memory bandwidth		
utilization relative to the			
	e. Achieved compute throughput and/or memory bandwidth		
below 60.0% of peak typ			
latency issue	s. Look at Scheduler Statistics and Warp State Statistics for		
,			

Block Size		
1,024		
Function Cache Configuration		
cudaFuncCachePreferNone		
Grid Size		
1,024		
Registers Per Thread		
register/thread	16	
Shared Memory Configuration Size	e	
Kbyte 32.		
Driver Shared Memory Per Block	•	
byte/block	0	
Dynamic Shared Memory Per Bloo	•	
byte/block	0	
Static Shared Memory Per Block	· ·	
Kbyte/block	16.38	
Threads	10.00	
thread 1,048,5	576	
Waves Per SM	,,,,	
25.60		
Section: Occupancy		
Block Limit SM		
	16	
Block Limit Registers		
block	4	
Block Limit Shared Mem		
block	2	
Block Limit Warps		
block	1	
Theoretical Active Warps per SM		
warp	32	
Theoretical		
Occupancy		%
100		
Achieved		
Occupancy		%
14.11		
Achieved Active Warps Per SM		
warp 4.5	51	

WRN This kernel's theoretical occupancy is not impacted by any block limit. The difference between calculated

theoretical (100.0%) and measured achieved occupancy (14.1%) can be the result of warp scheduling overheads

or workload imbalances during the kernel execution. Load imbalances can occur between warps within a block

as well as across blocks of the same kernel. See the CUDA Best Practices $\mbox{\sc Guide}$

(https://docs.nvidia.com/cuda/cuda-c-best-practices-guide/index.html#occupancy) for more details on

optimizing occupancy.

histogram_kernel(unsigned int *, unsigned int *, unsigned int, unsigned int), 2023-Dec-10 20:48:23, Context 1, Stream 14

Section: GPU Speed Of Light Throughput

DRAM Frequency

cycle/nsecond 5.00

SM Frequency

cycle/usecond 584.93

Elapsed Cycles

cycle 1,989,995

Memory

[%]

15.90

DRAM

Throughput

% 0.01

Duration

msecond 3.40

L1/TEX Cache

Throughput %

16.19

L2 Cache

Throughput %

4.73

SM Active Cycles

cycle 1,954,355.10

WRN This kernel exhibits low compute throughput and memory bandwidth utilization relative to the peak performance of this device. Achieved compute throughput and/or memory bandwidth below 60.0% of peak typically indicate latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons. Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block byte/block 0 Static Shared Memory Per Block byte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	Compute (SM) [%]	%
utilization relative to the peak performance of this device. Achieved compute throughput and/or memory bandwidth below 60.0% of peak typically indicate latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons. Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	15.90	
utilization relative to the peak performance of this device. Achieved compute throughput and/or memory bandwidth below 60.0% of peak typically indicate latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons. Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons. Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	utilization relative to the peak performance	ce
potential reasons. Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	below 60.0% of peak typically indicate	
Section: Launch Statistics Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block byte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		ler Statistics and Warp State Statistics for
Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	potential reasons.	
Block Size 1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
1,024 Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
Function Cache Configuration cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
cudaFuncCachePreferNone Grid Size 1,024 Registers Per Thread register/thread Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
Grid Size 1,024 Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	_	
1,024 Registers Per Thread register/thread Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
Registers Per Thread register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60		
register/thread 16 Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy		
Shared Memory Configuration Size Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	_	16
Kbyte 32.77 Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60		
Driver Shared Memory Per Block byte/block 0 Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60	·	
Dynamic Shared Memory Per Block byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60		
byte/block 0 Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	byte/block	0
Static Shared Memory Per Block Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60 Section: Occupancy	Dynamic Shared Memory Per Block	
Kbyte/block 16.38 Threads thread 1,048,576 Waves Per SM 25.60	byte/block	0
Threads thread 1,048,576 Waves Per SM 25.60	Static Shared Memory Per Block	
thread 1,048,576 Waves Per SM 25.60	Kbyte/block	16.38
Waves Per SM 25.60	Threads	
25.60	thread 1,048,576	,)
Section: Occupancy	Waves Per SM	
	25.60	
	Section: Occupancy	
Dlock Limit CM	Block Limit SM	

16 block

Block Limit Registers		
block	4	
Block Limit Shared Mem	·	
block	2	
Block Limit Warps		
block	1	
Theoretical Active Warps	s per SM	
warp	32	
Theoretical		
Occupancy		%
100		
Achieved		
Occupancy		%
14.11		
Achieved Active Warps F		
warp	4.51	
difference between calculated theoretical (100.0 result of warp scheduling ove or workload imbal occur between warps within a as well as across b	0%) and measured achieved occupancy (14.1%) can be erheads lances during the kernel execution. Load imbalances cablock blocks of the same kernel. See the CUDA Best Practice la/cuda-c-best-practices-guide/index.html#occupancy	the an es
histogram_kernel(unsigned 2023-Dec-10 20:48:23, Cont Section: GPU Speed Of L	d int *, unsigned int *, unsigned int, unsigned int), text 1, Stream 15	
DRAM Frequency		
cycle/nsecond	5.00	
SM Frequency		
cycle/usecond	584.92	
Elapsed Cycles		
cycle	1,989,975	

Memory				
[%]				%
15.90				
DRAM				
Throughput				
%	0.00			
Duration				
msecond	3.4	10		
L1/TEX Cache				
Throughput			%	
16.19				
L2 Cache				
Throughput				%
4.74				
SM Active Cycles				
cycle	1,954,390.07			
Compute (SM)				
[%]			%	
15.90				
below 60.0% of peak typ	. Achieved compu ically indicate	te throughput and/c	r memory bandwidth	
Section: Launch Stat	istics 			
Block Size				
1,024				
Function Cache Con				
cudaFuncCachePreferNo	ne			
Grid Size				
1,024	_			
Registers Per Thread	l			
register/thread		16		
Shared Memory Con				
Kbyte	32.77			
Driver Shared Memo	ry Per Block			
byte/block		0		

Dynamic Shared Memo byte/block	ory Per Block 0	
Static Shared Memory		
Kbyte/block	16.38	
Threads		
thread	1,048,576	
Waves Per SM		
25.60		
Section: Occupancy		
Block Limit SM		
block	16	
Block Limit Registers		
block	4	
Block Limit Shared Mer	m	
block	2	
Block Limit Warps		
block	1	
Theoretical Active War	ps per SM	
warp	32	
Theoretical		
Occupancy		%
100		
Achieved		
Occupancy		%
14.11		
Achieved Active Warps	Per SM	
warp	4.51	
 WRN This kernel's t	hooratical accuracy	is not imported by any block limit. The
difference between calculat		is not impacted by any block limit. The
		chieved occupancy (14.1%) can be the
tileoretical (100)	. O / O/ aria measured at	Therea occupancy (17.1/0) can be the

theoretical (100.0%) and measured achieved occupancy (14.1%) can be the result of warp scheduling overheads

or workload imbalances during the kernel execution. Load imbalances can occur between warps within a block

as well as across blocks of the same kernel. See the CUDA Best Practices $\mbox{\sc Guide}$

(https://docs.nvidia.com/cuda/cuda-c-best-practices-guide/index.html#occupancy) for more details on

optimizing occupancy.

histogram_kernel(unsigned int *, unsigned int *, unsigned int, unsigned int), 2023-Dec-10 20:48:23, Context 1, Stream 16 Section: GPU Speed Of Light Throughput ______ **DRAM Frequency** cycle/nsecond 5.00 SM Frequency cycle/usecond 584.93 **Elapsed Cycles** 1,990,017 cycle Memory [%] % 15.90 **DRAM** Throughput % 0.00 Duration msecond 3.40 L1/TEX Cache Throughput % 16.19 L2 Cache Throughput % 4.71 **SM Active Cycles** cycle 1,954,368.23 Compute (SM) [%] % 15.90

WRN This kernel exhibits low compute throughput and memory bandwidth utilization relative to the peak performance

of this device. Achieved compute throughput and/or memory bandwidth below 60.0% of peak typically indicate

latency issues. Look at Scheduler Statistics and Warp State Statistics for potential reasons.

Section: Launch Statistics	
Block Size	
1,024	
Function Cache Configuration	
cudaFuncCachePreferNone	
Grid Size	
1,024	
Registers Per Thread	
register/thread	16
Shared Memory Configuration Size	
Kbyte 32.77	
Driver Shared Memory Per Block	
byte/block	0
Dynamic Shared Memory Per Block	
byte/block	0
Static Shared Memory Per Block	
, ,	16.38
Threads	
thread 1,048,576	
Waves Per SM	
25.60	
C 11 O	
Section: Occupancy	
Block Limit SM	
block 16	
Block Limit Registers	
block 4	
Block Limit Shared Mem	
block 2	
Block Limit Warps	
block 1	
Theoretical Active Warps per SM	
warp 32	
Theoretical	
Occupancy	

Occupancy %
100

Achieved Occupancy % 14.11 Achieved Active Warps Per SM 4.51 warp WRN This kernel's theoretical occupancy is not impacted by any block limit. The difference between calculated theoretical (100.0%) and measured achieved occupancy (14.1%) can be the result of warp scheduling overheads or workload imbalances during the kernel execution. Load imbalances can occur between warps within a block as well as across blocks of the same kernel. See the CUDA Best Practices Guide (https://docs.nvidia.com/cuda/cuda-c-best-practices-guide/index.html#occupancy) for more details on optimizing occupancy. convert_kernel(unsigned int *, unsigned int), 2023-Dec-10 20:48:24, Context 1, Stream 7 Section: GPU Speed Of Light Throughput _____ **DRAM Frequency** cycle/nsecond 4.80 **SM** Frequency cycle/usecond 561.84 **Elapsed Cycles** 3,598 cycle Memory [%] %

1.13

6.40

%

4.27

usecond

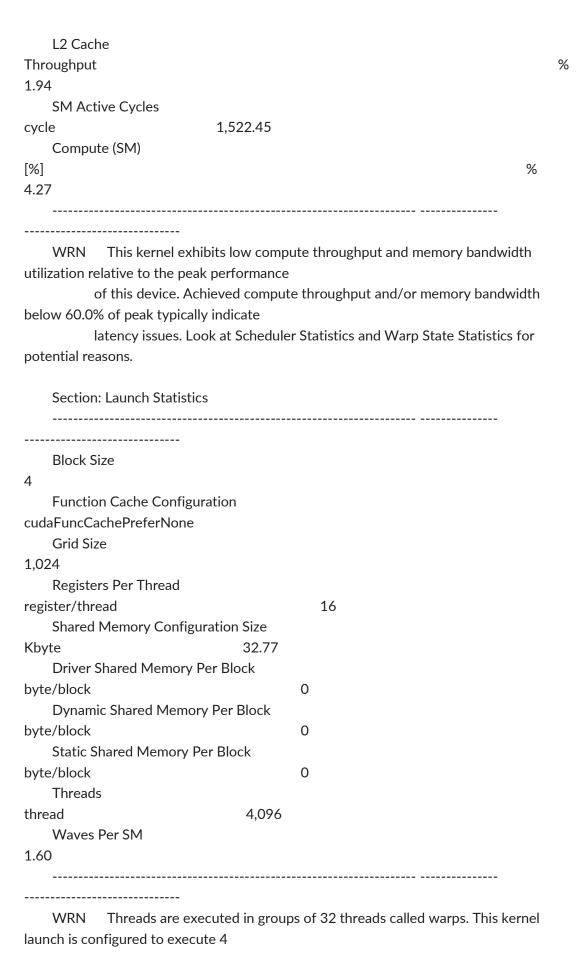
10.09

Throughput

DRAM
Throughput
%

Duration

L1/TEX Cache



threads per block. Consequently, some threads in a warp are masked off and those hardware resources are

unused. Try changing the number of threads per block to be a multiple of 32 threads. Between 128 and 256

threads per block is a good initial range for experimentation. Use smaller thread blocks rather than one

large thread block per multiprocessor if latency affects performance. This is particularly beneficial to

kernels that frequently call __syncthreads(). See the Hardware Model

 $(\underline{https://docs.nvidia.com/nsight-compute/ProfilingGuide/index.html\#metrics-hw-model}) \\ description for more$

details on launch configurations.

WRN A wave of thread blocks is defined as the maximum number of blocks that can be executed in parallel on the

target GPU. The number of blocks in a wave depends on the number of multiprocessors and the theoretical

occupancy of the kernel. This kernel launch results in 1 full waves and a partial wave of 384 thread blocks.

Under the assumption of a uniform execution duration of all thread blocks, the partial wave may account for

up to 50.0% of the total kernel runtime with a lower occupancy of 42.6%. Try launching a grid with no

partial wave. The overall impact of this tail effect also lessens with the number of full waves executed for

a grid. See the Hardware Model

(https://docs.nvidia.com/nsight-compute/ProfilingGuide/index.html#metrics-hw-model) description for more

details on launch configurations.

Section: Occupancy			
Block Limit SM			
block	16		
Block Limit Registers			
block	128		
Block Limit Shared Mem			
block	16		

Block Limit Warps		
block	32	
Theoretical Active Warps per	SM	
warp	16	
Theoretical		
Occupancy		%
50		
Achieved		
Occupancy		%
28.68		
Achieved Active Warps Per SI	М	
warp	9.18	

WRN This kernel's theoretical occupancy (50.0%) is limited by the required amount of shared memory This kernel's

theoretical occupancy (50.0%) is limited by the number of blocks that can fit on the SM The difference

between calculated theoretical (50.0%) and measured achieved occupancy (28.7%) can be the result of warp

scheduling overheads or workload imbalances during the kernel execution. Load imbalances can occur between

warps within a block as well as across blocks of the same kernel. See the CUDA Best Practices Guide

 $(\underline{\mathsf{https://docs.nvidia.com/cuda/cuda-c-best-practices-guide/index.\mathsf{html\#occupancy}}) \ for more \ details \ on$

optimizing occupancy.