

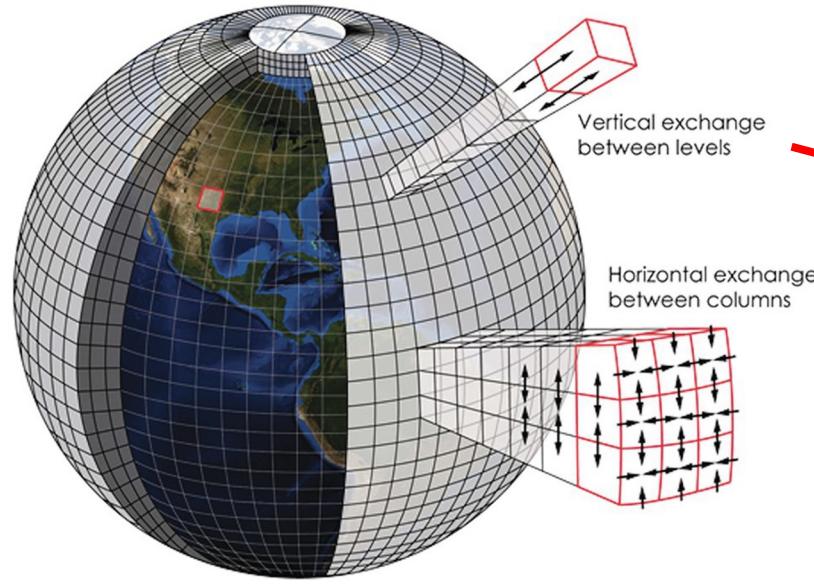
# Addressing the calibration bottleneck using machine learning: Application to the CNRM-CM6-1 model

**Romain Roehrig**

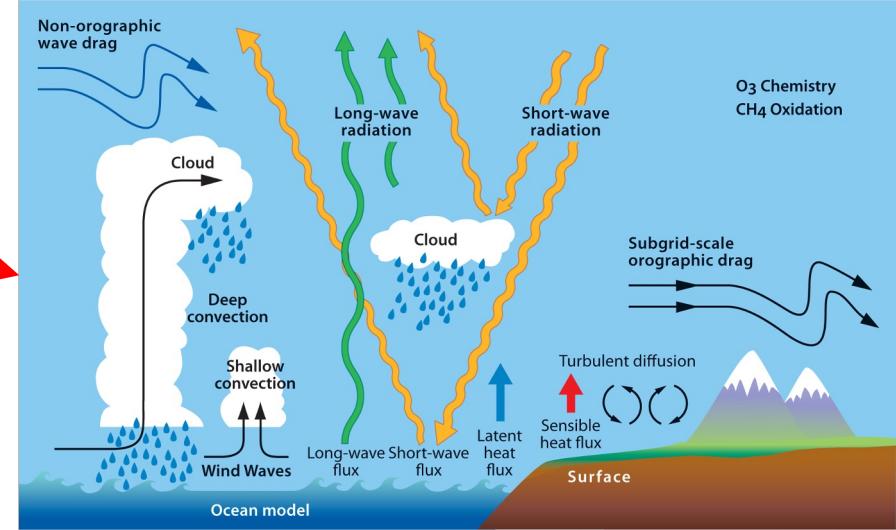
CNRM, Météo-France and CNRS, Toulouse, France

With contributions from D. Williamson, F. Couvreux, F. Hourdin, O. Audouin, J. Salter, N. Villefranque, V. Volodina, W. Xu...

# Climate models - basics



$$\frac{\partial \mathbf{x}}{\partial t} = \mathcal{D}(\mathbf{x}) + \sum_p \mathcal{P}_p(\mathbf{x})$$



## Developing a climate model:

- Choose a set of equations issued from fluid dynamics, thermodynamics, with some approximations.
- Discretise them on the sphere to solve them numerically
- Thereby introduce a model resolution:
  - some processes are explicitly resolved, some not >> parameterizations
  - note some processes need to be parameterized whatever the resolution (e.g., radiation, microphysics)
- Do it for each component of the climate system and couple individual models together

# Climate model calibration

**Climate model** = a software

- + external forcings
- + horizontal/vertical grids
- + a scientific content (i.e., fluid dynamics equations, parameterizations)
- + values for model internal/uncertain parameters >> **calibration**

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## **Calibration (or tuning)**

- Common to most modelling frameworks
- Can be seen as an optimisation procedure under constraints (or **metrics**), possibly with priorities/weights.
- Need for high-quality **references/observations**, with well-quantified uncertainties
- +1 W m<sup>-2</sup> at TOA ~ +0.5–1.5 K of global mean near-surface temperature (*Hourdin et al. 2017*).
  - *Given current uncertainties, present-day global-mean temperature in a climate model is mostly a result of tuning.*

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## A bottleneck for climate model development

- **High dimensionality** of the parameter space ~O(10)
- Climate model numerical simulations are **computationally expensive**
  - An exhaustive exploration of the parameter space is not directly possible.
- Large number and variety of metrics O(10-100++), sometimes subjective
- **Overfitting** issue, treatment of **uncertainties**

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## Calibration of CNRM-CM6-1 (*Voldoire et al. 2019, Roehrig et al. 2020*)

- Manual calibration, 1 or 2 parameters at the same time, mixing well-defined metrics and more subjective considerations
- Calibration of stand-alone components before coupling, priorities among metrics
- Often questioning the model physical content. But difficult to disentangle true model structural limits from “just” a poor calibration?

# A rationale for addressing the calibration bottleneck

## History matching

- Determine the plausible sets of model parameter values rather than optimize
- Or equivalently rule out the **implausible** sets of model parameter values
- For a given set of **quantitative metrics**
- Considering **reference/observations uncertainties**
- And introducing priors for **model structural errors** (interpreted here as tolerances to error)

## Machine learning

- **Emulate** the model behaviour (i.e. the dependence of metrics to model parameters), to explore at very weak cost the parameter space.
- Consider also the **emulators' uncertainty**
- **Gaussian processes** nicely provide predictions with an uncertainty estimate

## Iterative refocussing

- Be as **parsimonious** as possible in terms of true simulations
- Start with a ‘few’ simulations and progressively add new ones to improve the emulator quality, but only where it is needed
- Possibly add new metrics along the way, based on more expansive simulations (pre-conditioning with cheaper configurations)
  - A **formalized calibration procedure**, transparent and reproducible.
  - A semi-automatic and efficient framework, that allows us to **quantify the true benefit of a new development** more rapidly
  - More **rigorous comparison** between parameterizations or model physics.
  - Possibly not a single acceptable configuration but several: being able to explore the **model parametric uncertainty** of its emergent properties.

# The technical framework

1. Define targeted (scalar) **metrics**  $f$ , their **reference values**  $r_f$  and associated **uncertainties**  $\sigma_{r,f}$
2. Identify the relevant model **parameters**  $\lambda$ , and their “acceptable” range >> **input parameter space**  $\Lambda$
3. Define a simulation strategy, build an experimental design, run simulations >> **learning dataset**
4. **Emulate**  $f(\lambda)$  for each metric (Gaussian Processes)
5. Identify the sub-space of  $\Lambda$  which is compatible with references for all metrics  
    >> **Not-Ruled-Out-Yet – NROY – space**

considering

- The reference uncertainty
- The emulator uncertainty
- The model structural error (tolerance to error)  $\sigma_{d,f}$

>> **Implausibility** measure  $I_f$ , **cutoff**  $T$

$$I_f(\lambda) = \frac{|r_f - \mathbb{E}[f(\lambda)]|}{\sqrt{\sigma_{r,f}^2 + \sigma_{d,f}^2 + \text{Var}[f(\lambda)]}}.$$

$$\text{NROY}_f^1 = \{\lambda \mid I_f(\lambda) < T\}$$

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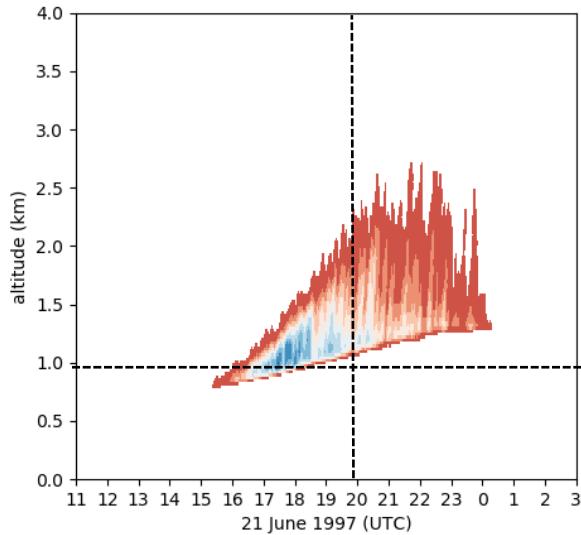
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6. Iterate over several waves to reduce the emulators’ uncertainty in  $\text{NROY}^{N-1}$ , until convergence

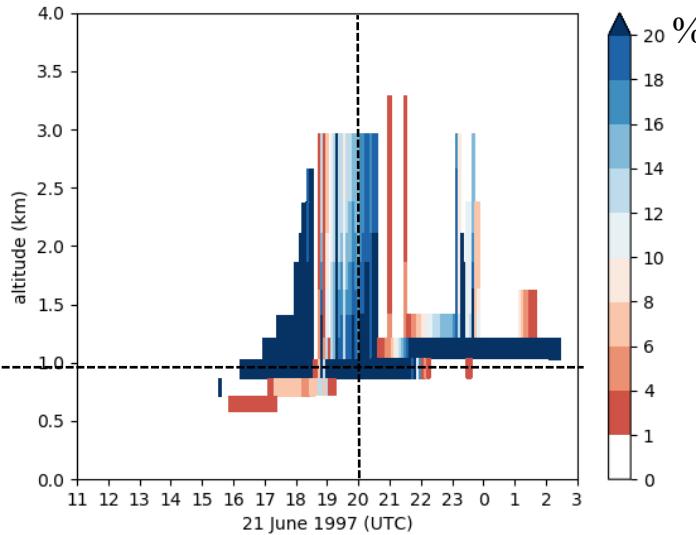
# First application: 1D configurations of CNRM-CM6-1

Cloud Fraction

LES (Meso-NH)



CNRM-CM6-1



**1D (Single-column model) vs Large-Eddy Simulation (LES):**

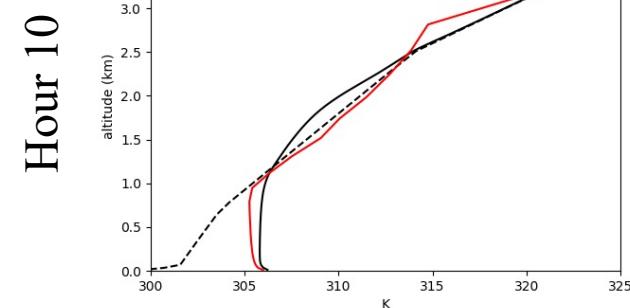
- *inspire the development of atmospheric parameterizations, validate and calibrate them*

ARM-Cumulus: diurnal cycle of continental cumulus

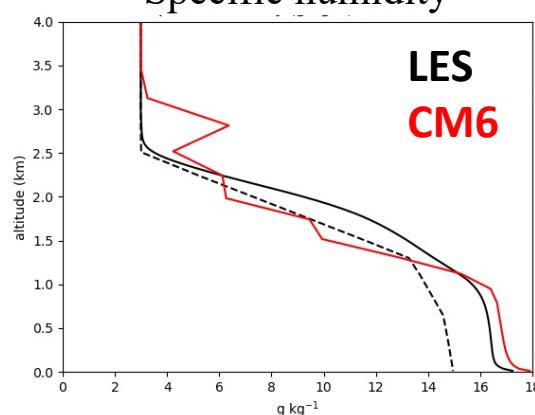
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- Overestimate of cloud fraction
- Cloud base too low
- Boundary layer not deep enough, mixing too weak
- Intermittency and numerical issues

Potential temperature



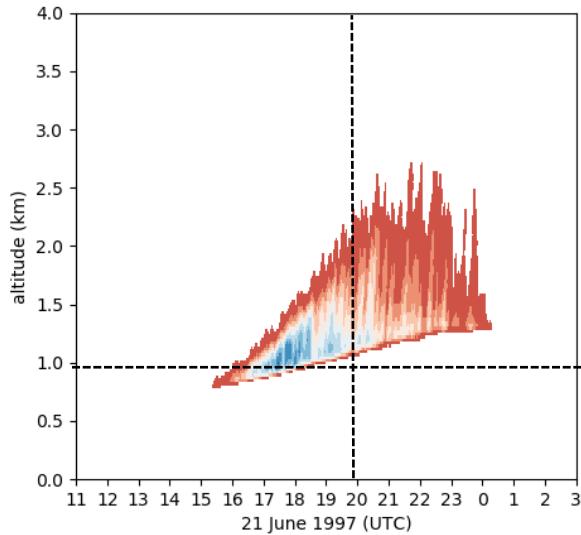
Specific humidity



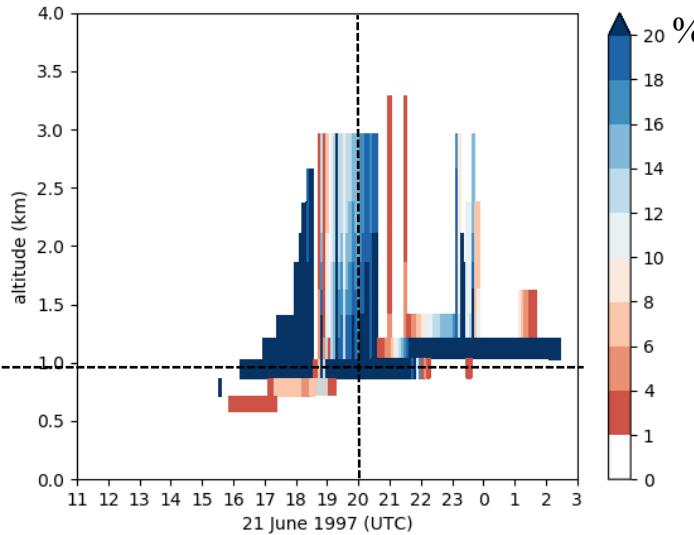
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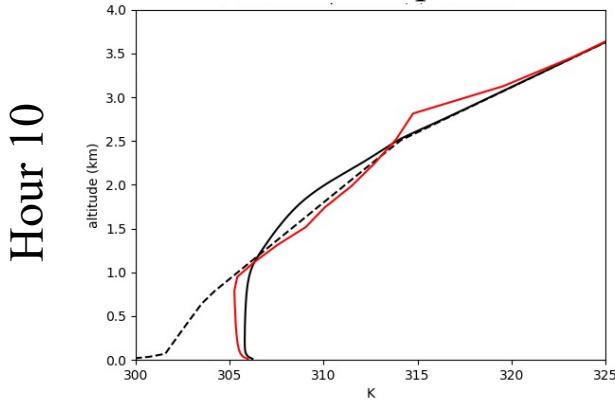
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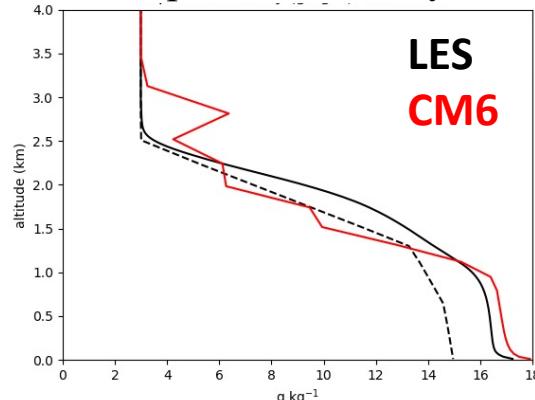
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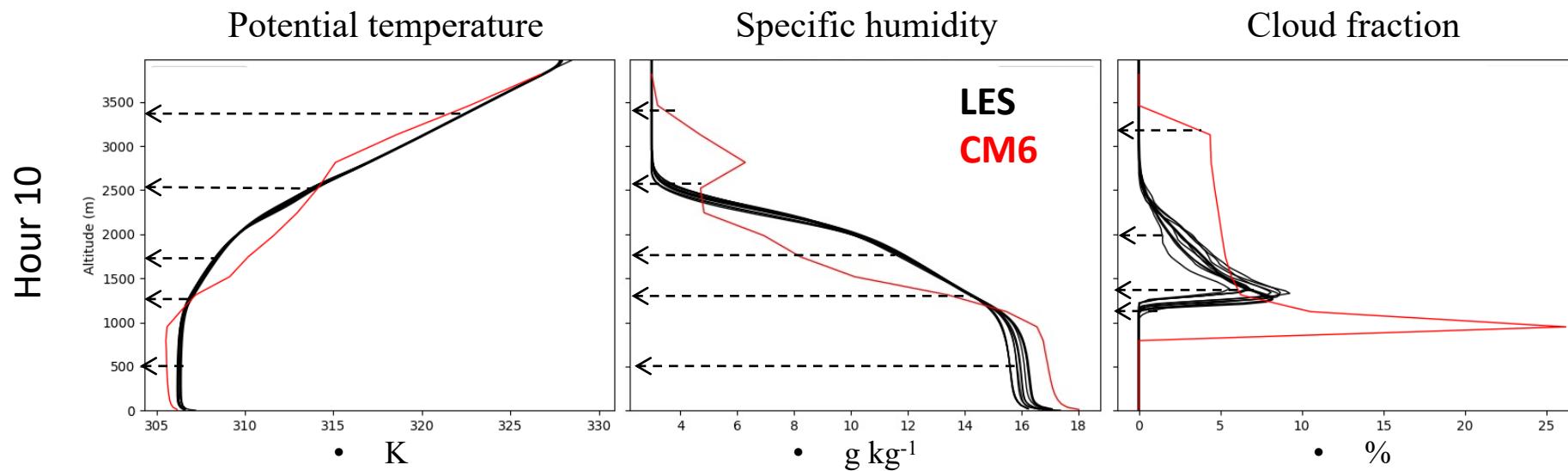
Specific humidity



- *Poor calibration, or intrinsic limits?*

# Calibration setup

- **14 metrics:** temperature, specific humidity and cloud fraction at a few levels (Hour 10)
- **Reference:** LES simulation with Meso-NH, uncertainty from an ensemble of LES simulations

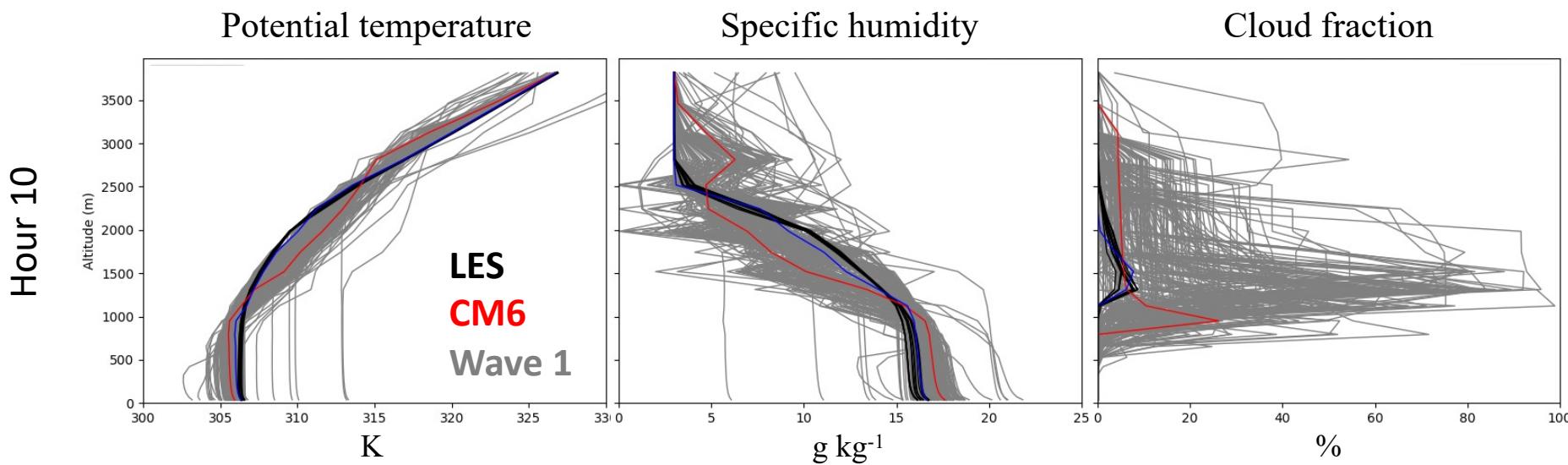


- **26 parameters:**
  - 13 related to convective transport (entrainment/detrainment, drag, buoyancy parameter)
  - 2 related with convective closure
  - 1 related to convective cloudiness
  - 6 related with liquid water microphysics
  - 4 related to turbulence
- Wave 1: 200 simulations, sampling based on a Latin hypercube
- Next waves: 200 simulations (within  $\text{NROY}^{N-1}$ )

# Wave 1

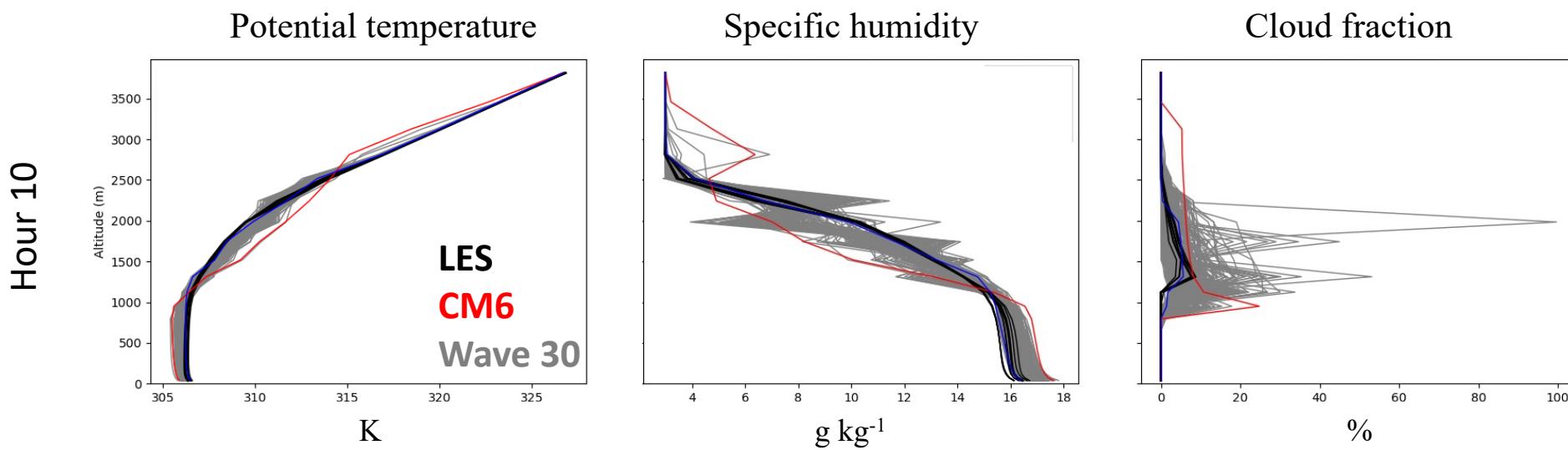
## Tolerance to error

- Potential temperature: 0.5 K except at 3400 m (0.1 K)
- Specific humidity: 0.5 g kg<sup>-1</sup>
- Cloud fraction: 5 %



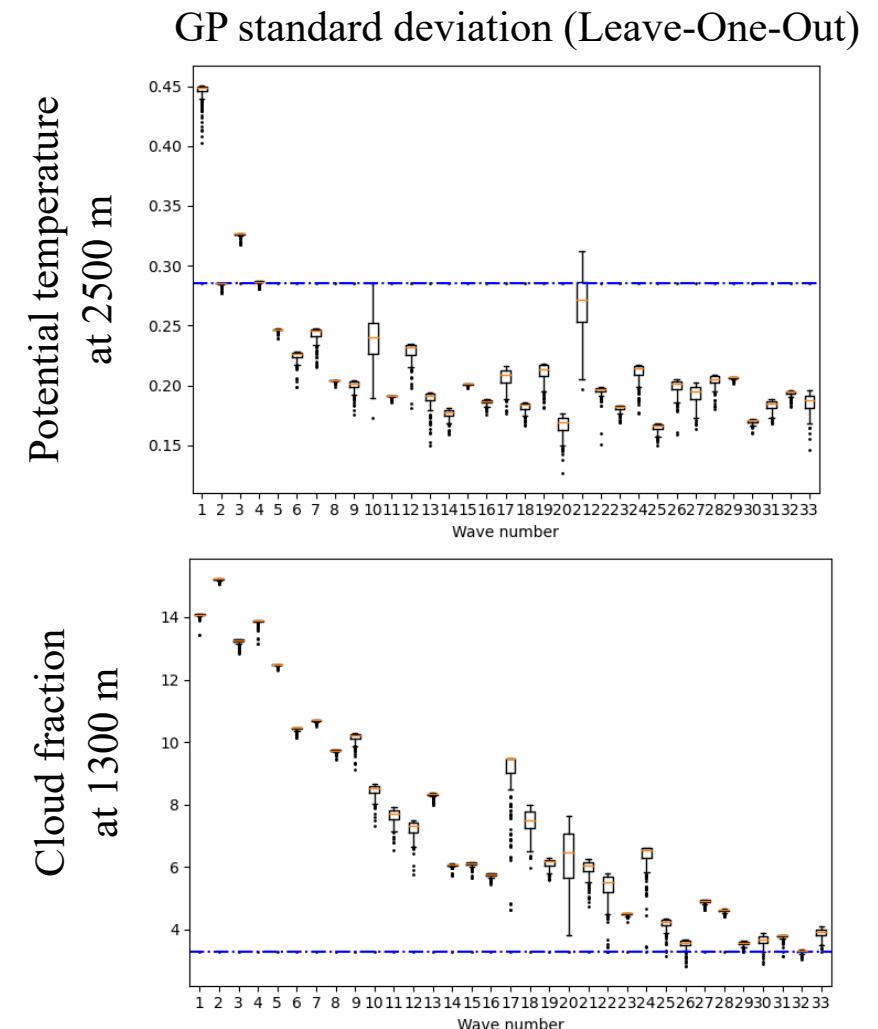
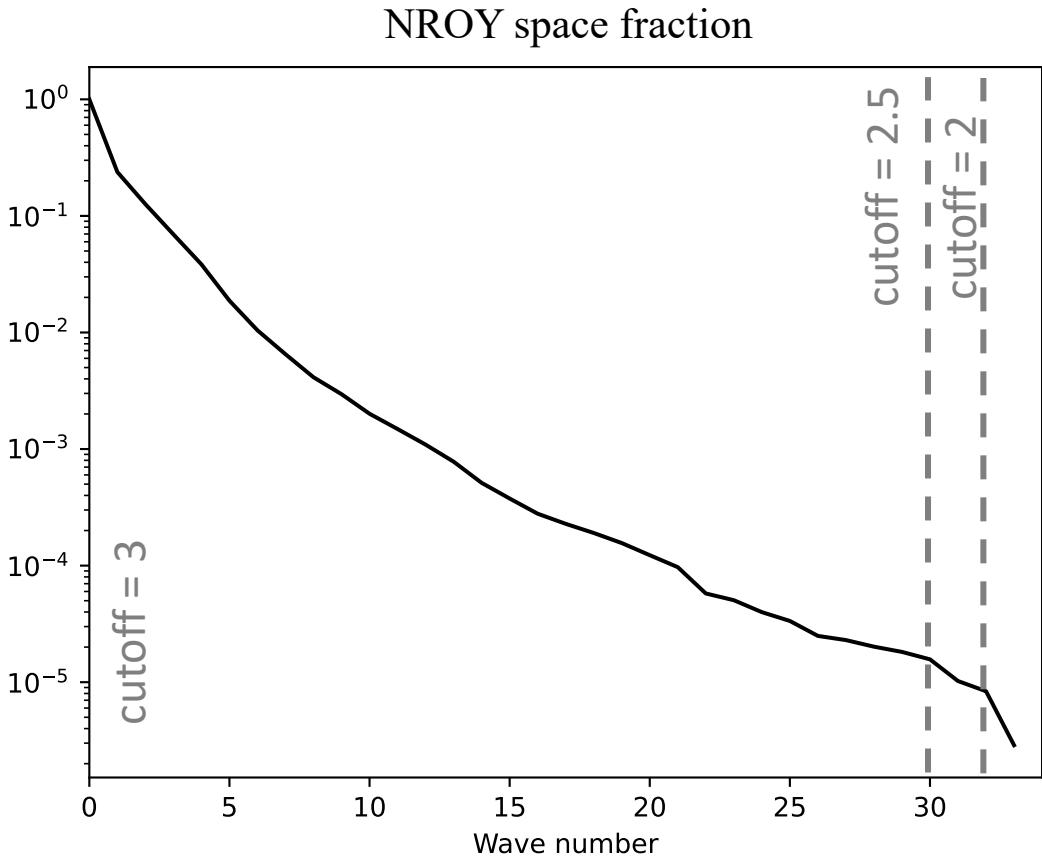
# Wave 33

- Several configurations much better than default.
- Convergence not fully achieved (esp. for cloud fraction).
- ***Intrinsic limits of the model physics:***
  - Some irregularities in the profiles seem intrinsic (esp.  $q_v$ )



# NROY space evolution and convergence

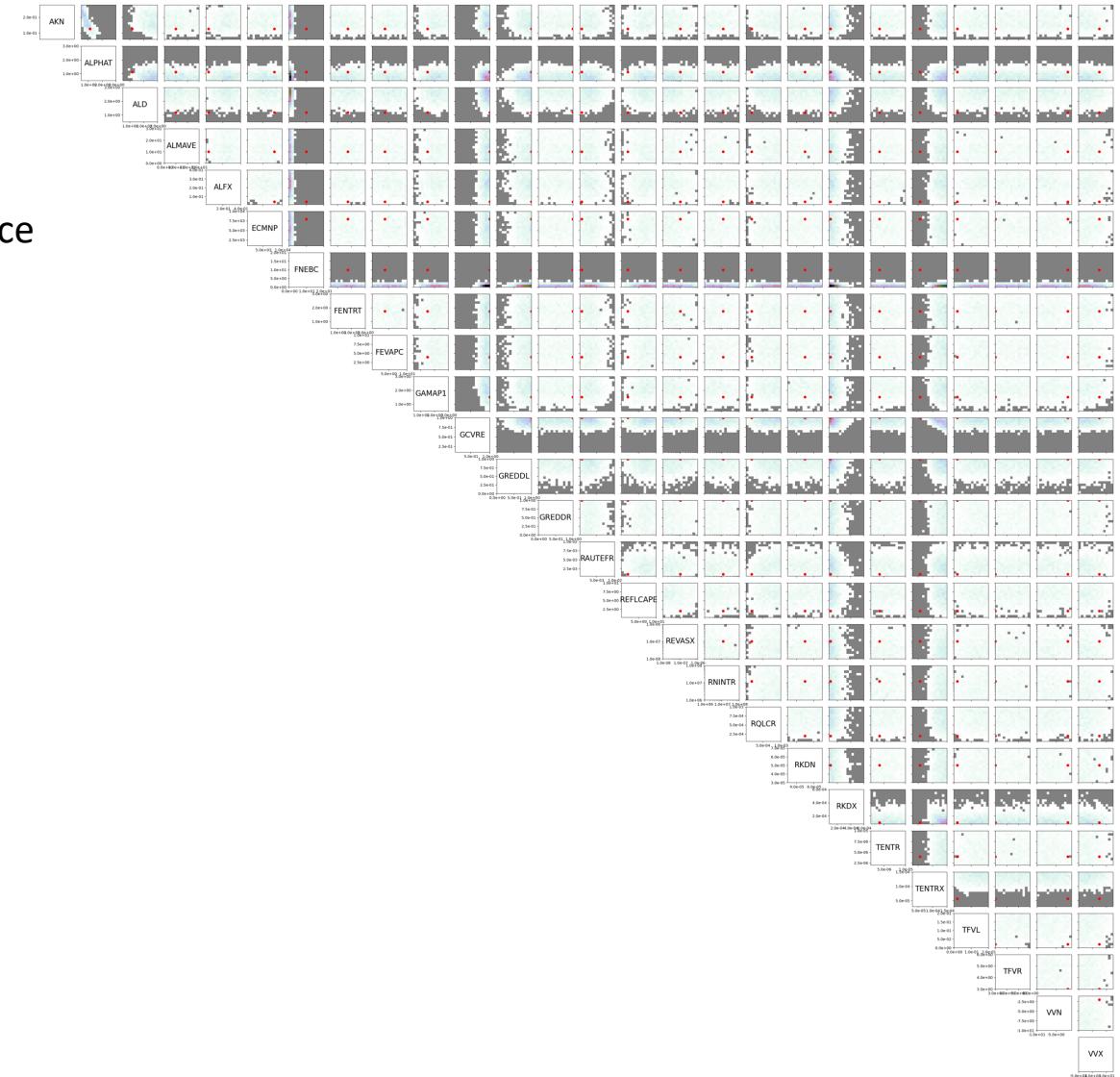
- Decrease of cutoff
  - when emulator uncertainty comparable/lower than reference uncertainty/tolerance-to-error
  - when NROY space size approximately stable
- After 33 waves, NROY  $\sim 2.9 \times 10^{-6}$  of the input parameter space  
 $\gg \sim 290$  over  $10^8$  configurations



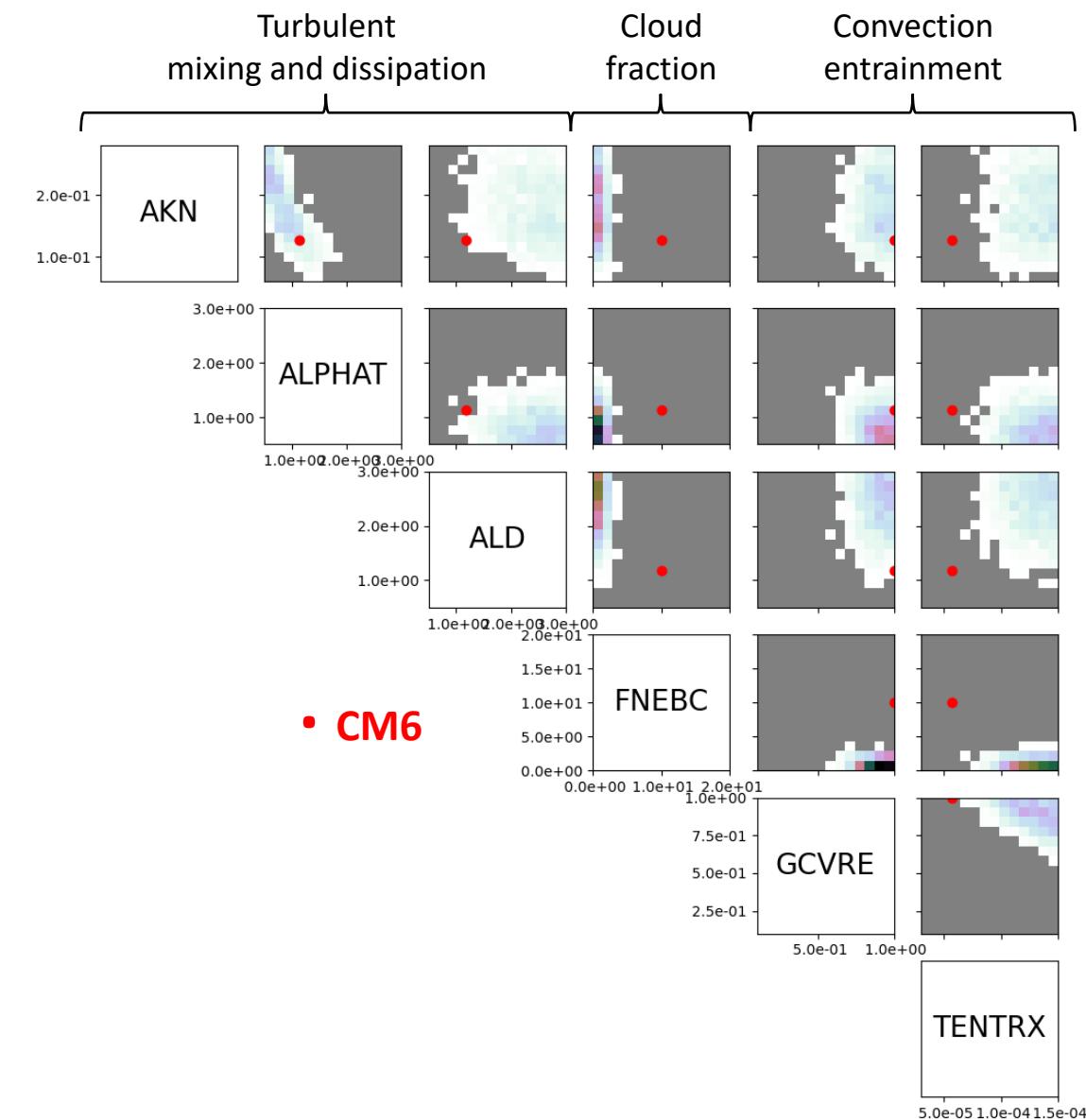
# Representing the NROY space

## Numerical characterization of the NROY space:

- (very) large sampling (LHS) of the input parameter space
- Use emulators to compute associated implausibilities
- Compute densities of points within NROY space as a function of parameters
- 1D or 2D representations



# Dominant parameters



## Dominant parameters

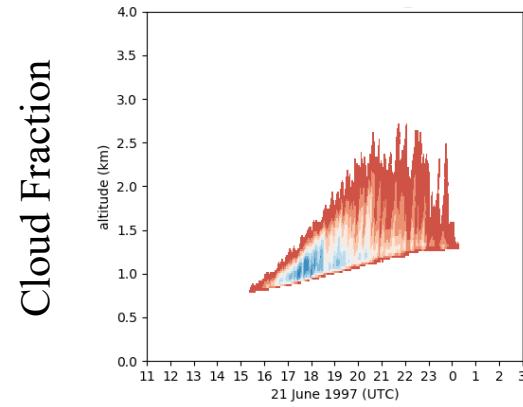
- Turbulent mixing (AKN and ALPHAT)
- TKE dissipation (ALD)
- Convective cloud fraction (FNEBC)
- Organized entrainment modulation factor (GCVRE)
- Maximum turbulent entrainment (TENTRX)

**Strong constraints on turbulent mixing  
and convective cloud fraction**

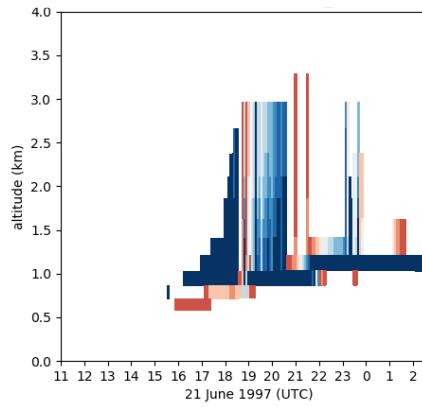
**High entrainment rates** required for convection

# One configuration within the NROY space

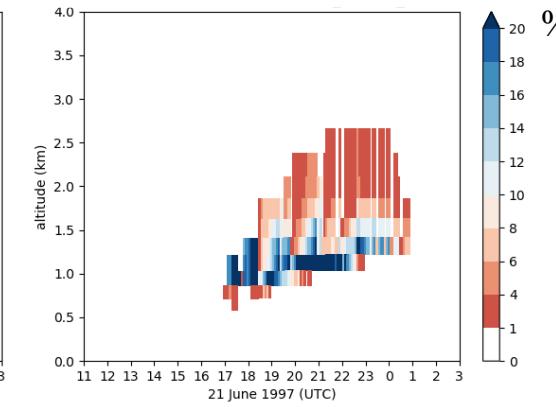
LES



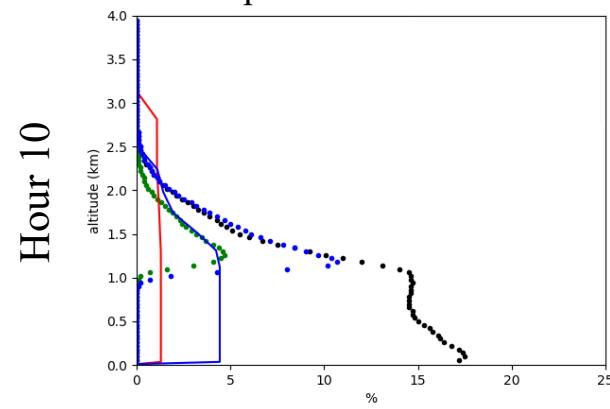
CM6



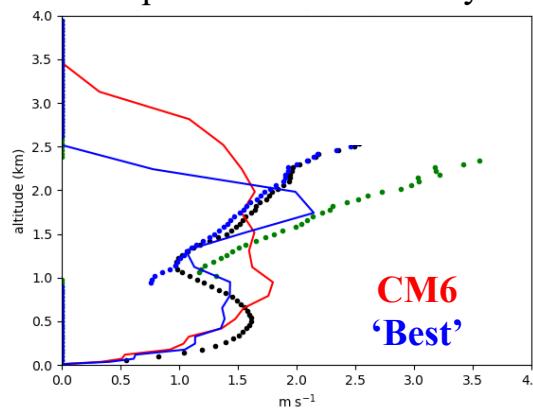
'one of the best'



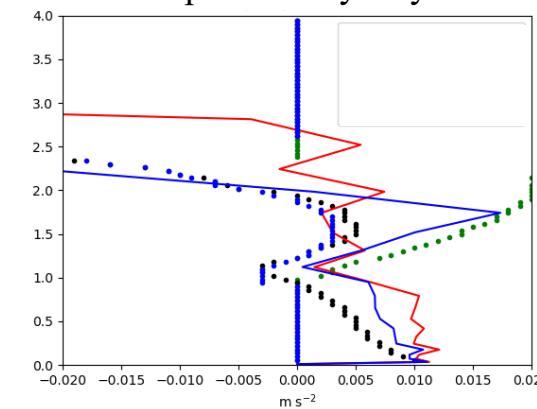
Updraft area fraction



Updraft vertical velocity



Updraft buoyancy



# Calibration vs. structural limits

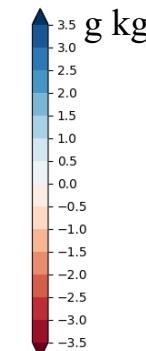
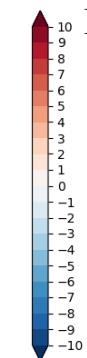
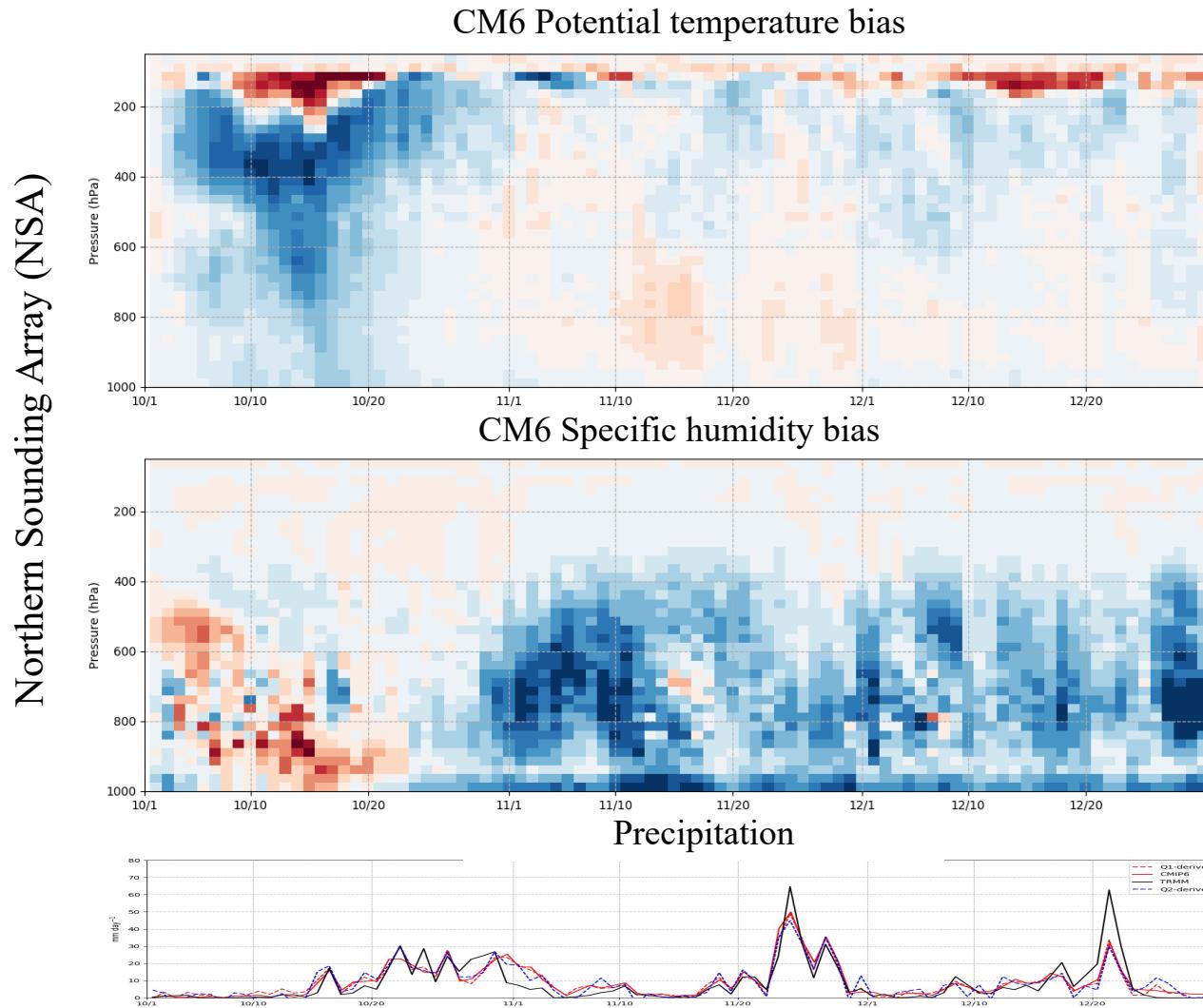
During the development and tuning of CNRM-CM6-1, hard to capture both shallow and deep convection (unified approach)

- *Is the CNRM-CM6-1 unified approach for convection parameterization appropriate?*

# Calibration vs. structural limits

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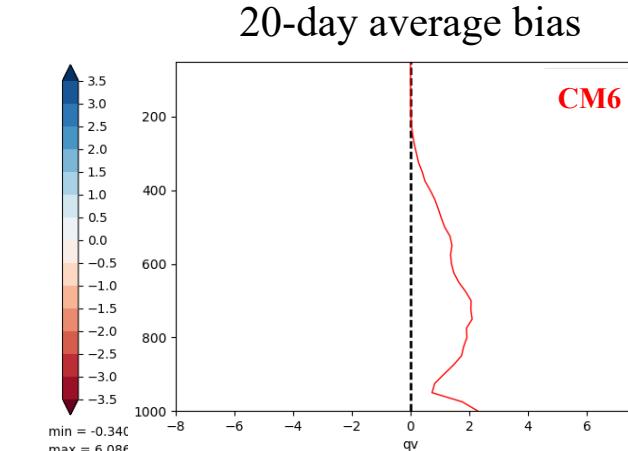
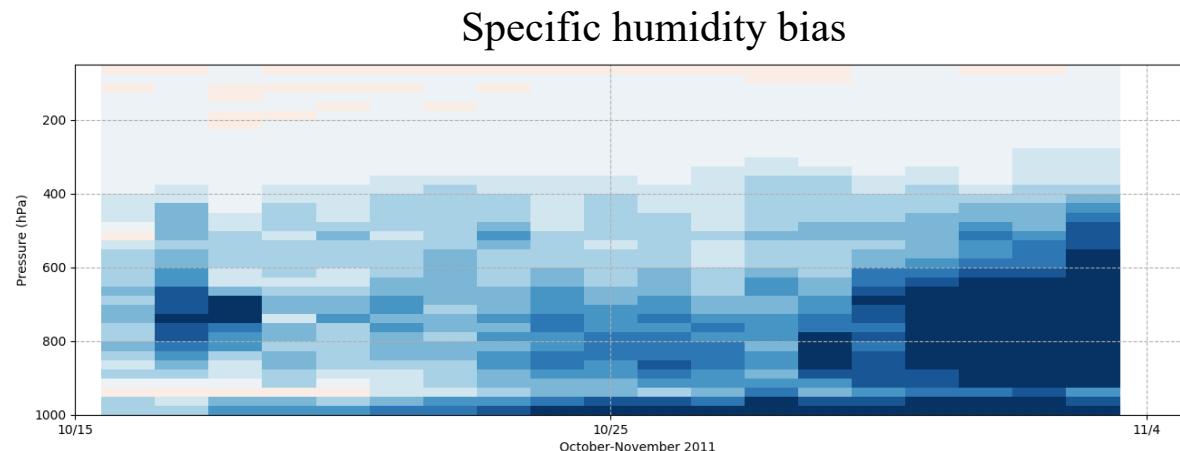
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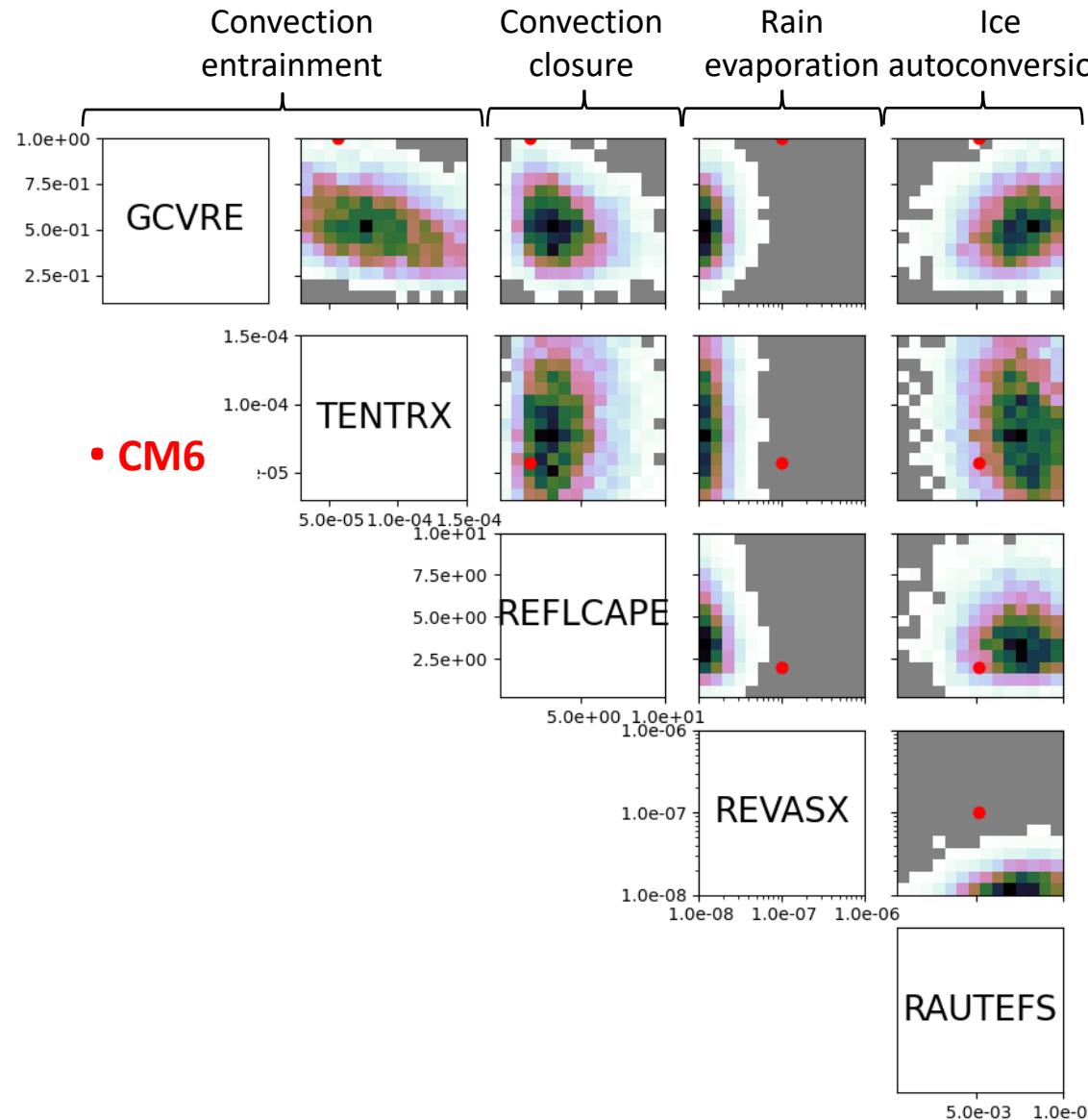
Consider the DYNAMO 1D case, based on a field campaign in OND 2011 in the Indian Ocean, and with alternating convectively-active and suppressed phases (Johnson and Ciesielski, 2013)

# Metrics, parameters and experimental design

- Focus on the first MJO event (15 October to 4 November 2011)
- **Metrics**: temperature/humidity average profiles
  - 3 levels for  $\theta$ : 925, 600 and 200 hPa
  - 2 for  $q_v$ : 925 and 700 hPa
  - 4 for RH: 850, 700, 500 and 300 hPa
- **Reference** (field campaign observations):
  - temperature uncertainty  $\sim 0.1$  K; tolerance 1 to 5 K
  - $q_v$  uncertainty  $\sim 0.1 \text{ g kg}^{-1}$ ; tolerance  $0.2/0.1 \text{ g kg}^{-1}$
  - RH uncertainty  $\sim 2\%$ ; tolerance 5 to 20%
- **Parameters**: same 26 parameters as for ARM-Cumulus
  - + 13 for ice microphysics
  - + 4 for cloud radiative properties
- Wave 1 and following: 200 simulations



## Wave 29



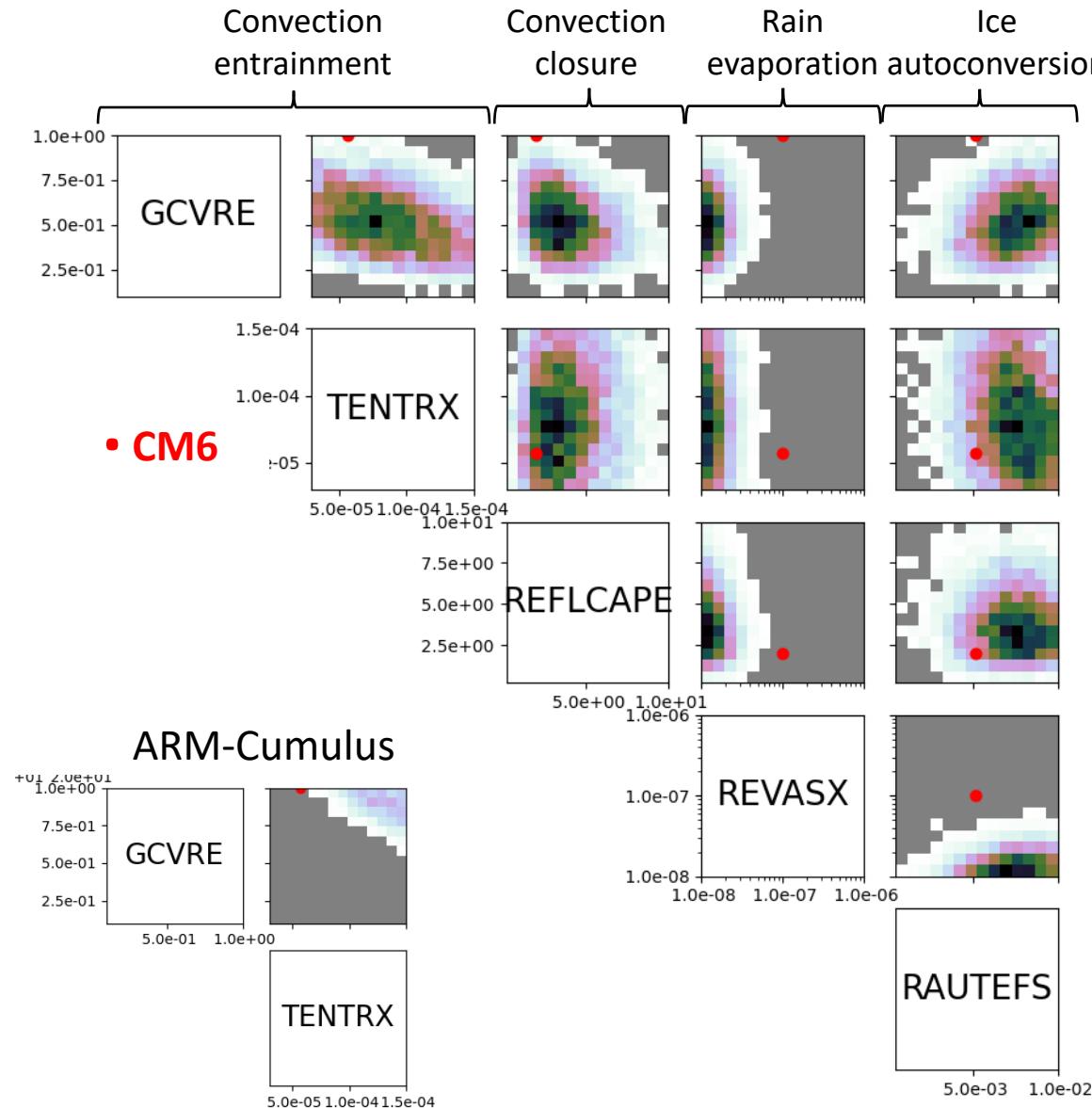
**Wave convergence not yet fully achieved.**

$\text{NROY}^{29} \sim 6.9 \times 10^{-5}$  of the input space

**Dominant parameters:**

- **Rain evaporation** rate key to get the moisture vertical profile right
- Reduced ice autoconversion required >> **longer life cycle of (high-level) ice clouds**. Feedback through LW heating?
- **Convection intensity** (closure) is important
- **Convective entrainment** still key, towards more moderate values compared to shallow convection.

# Deep vs. shallow convection



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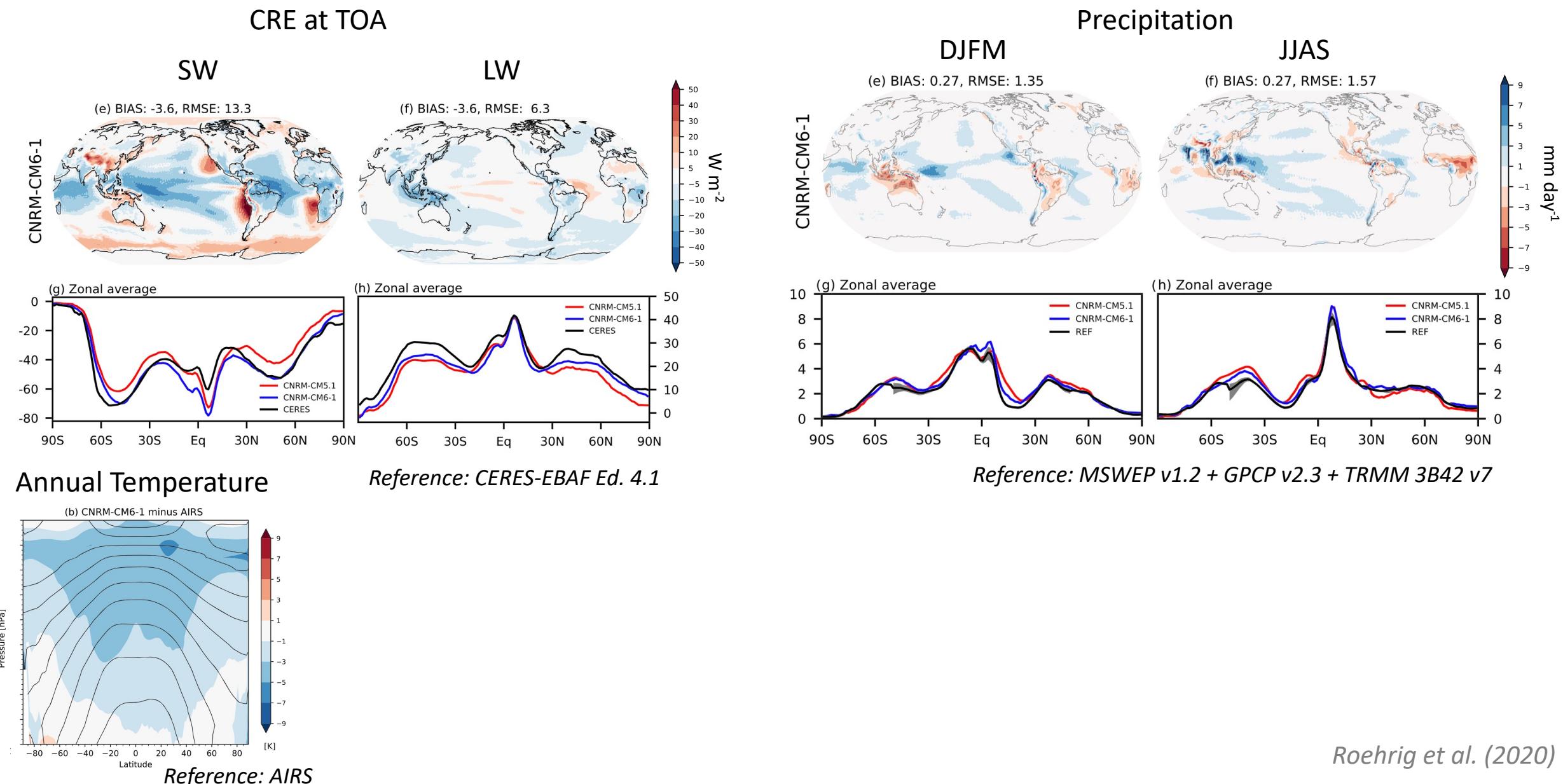
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- **Convective entrainment** still key, towards more moderate values compared to shallow convection.
- **Weak overlap between the entrainment parameter NROY spaces for shallow and deep cases**

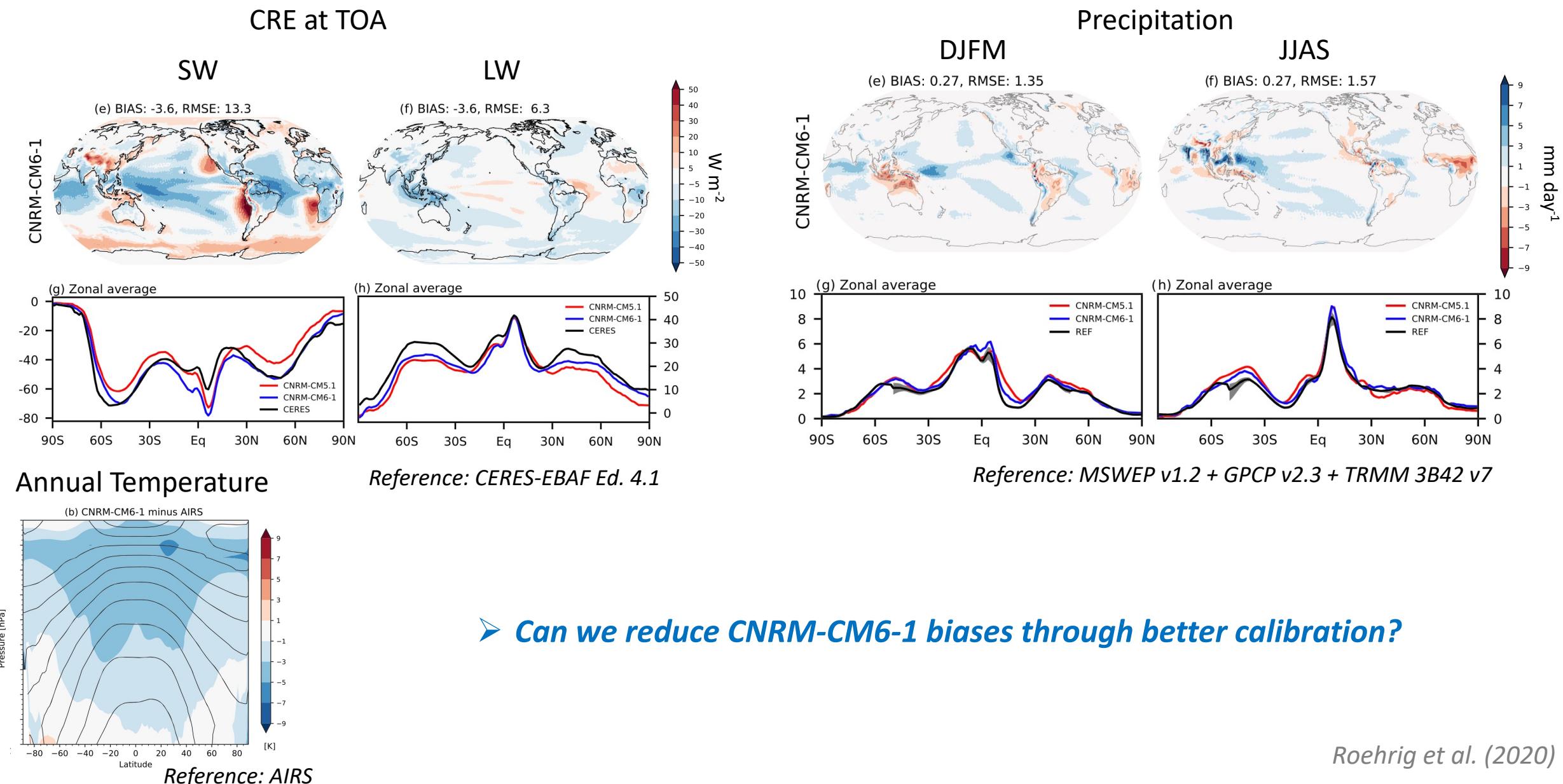
# What did we learn from 1D configurations?

- ***History Matching with Iterative refocusing***: framework to rigorously explore the ***parametric calibration*** of a parameterization/model physics, and identify its ***structural limits***
- Better tuning of the CNRM convective parameterization (in fact the CNRM physics) can be achieved for each of the two 1D cases addressed here.
- The combination of a shallow convection case and a deep convection case emphasizes the difficulty to make the CNRM “unified” convection parameterization work for both.
  - ***The CNRM-CM6-1 single-plume mass-flux approach is structurally limited.***
- Shallow and deep convection regimes require significantly different entrainment rates.
  - ***What about more ‘realistic’ (3D) configurations?***

# Calibrating the 3D (atmospheric) configuration of CNRM-CM6-1



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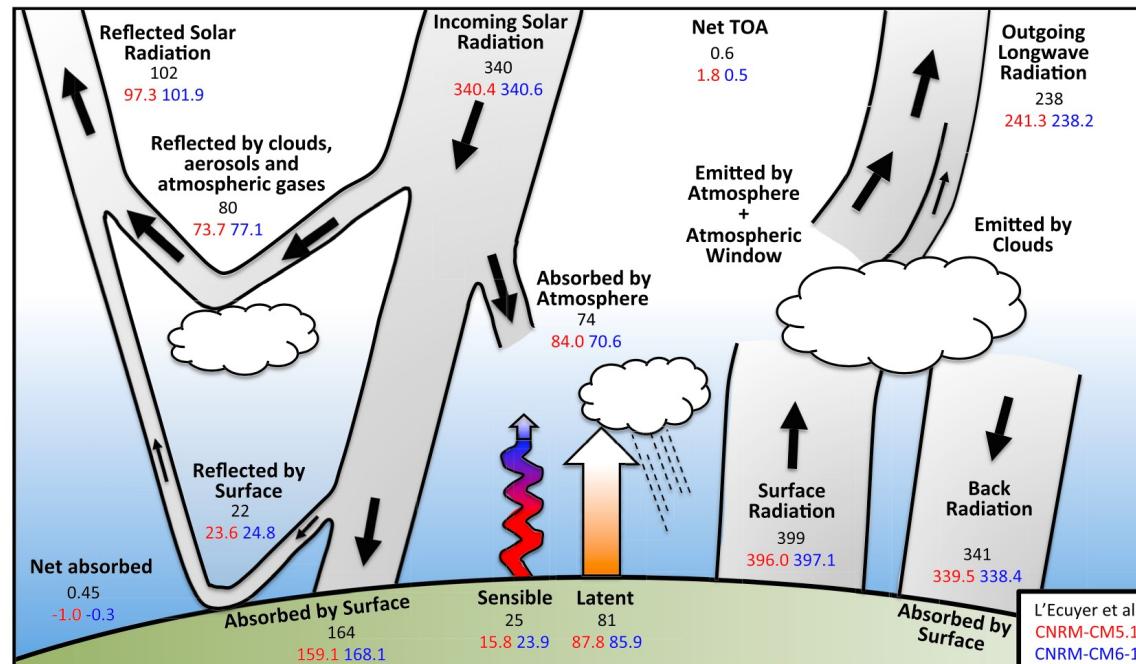


# Metrics, references and uncertainty estimates

Following the CNRM-CM6-1 tuning strategy, 3 classes of metrics:

## 1. *Global averages of the energy budget components*

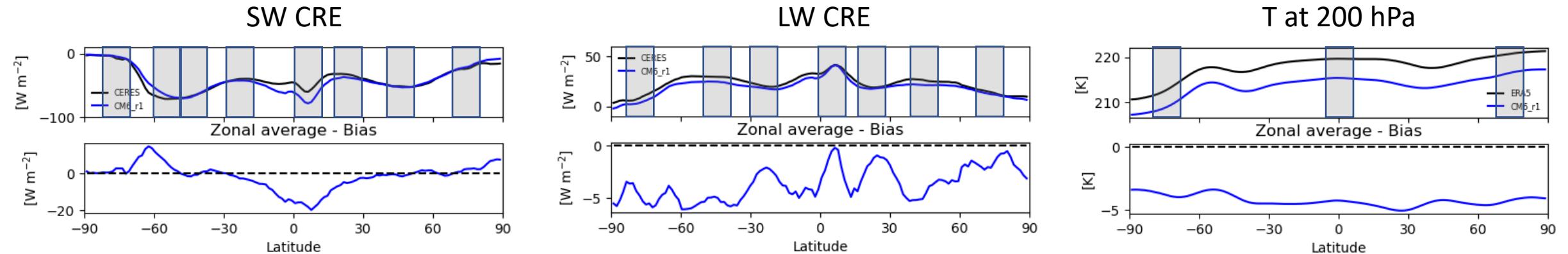
- at TOA: OLR, OSR, Net, SW/LW CRE
- at the surface ocean: Net, SWdn, LWdn
- Values from CERES-EBAF, uncertainties based on the literature
- Except Net at surface/TOA = 0 +/- 0.1 W m<sup>-2</sup>: the model has to be equilibrated.
- Tolerance to error: 0.5 W m<sup>-2</sup>



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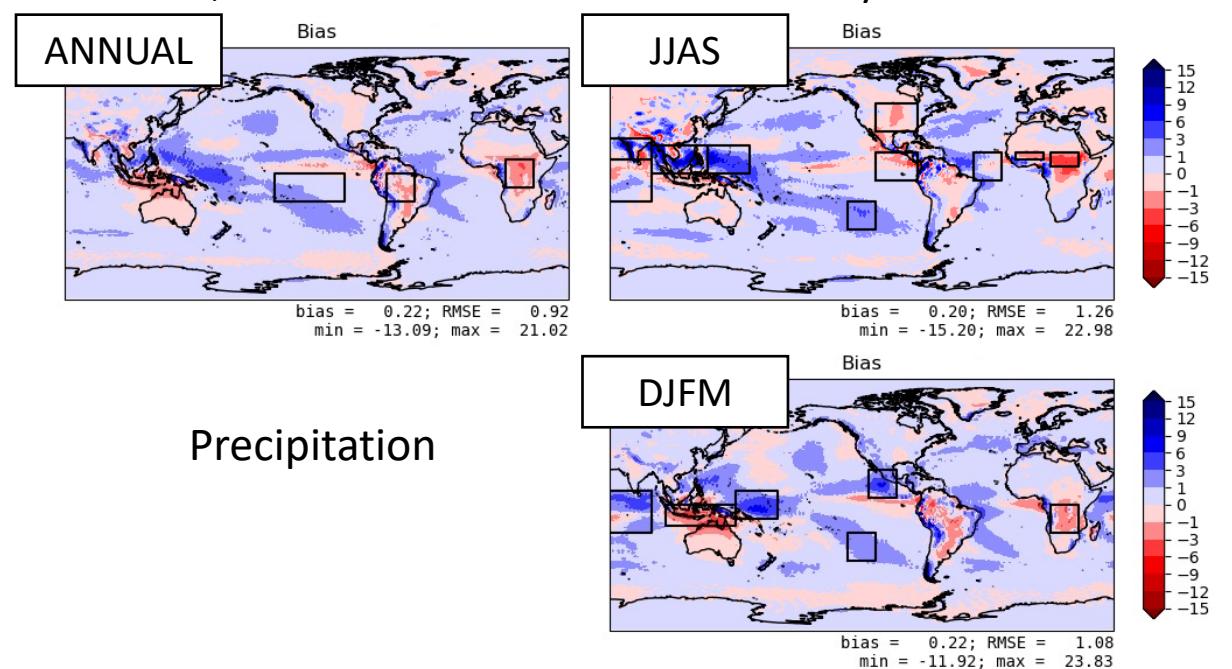
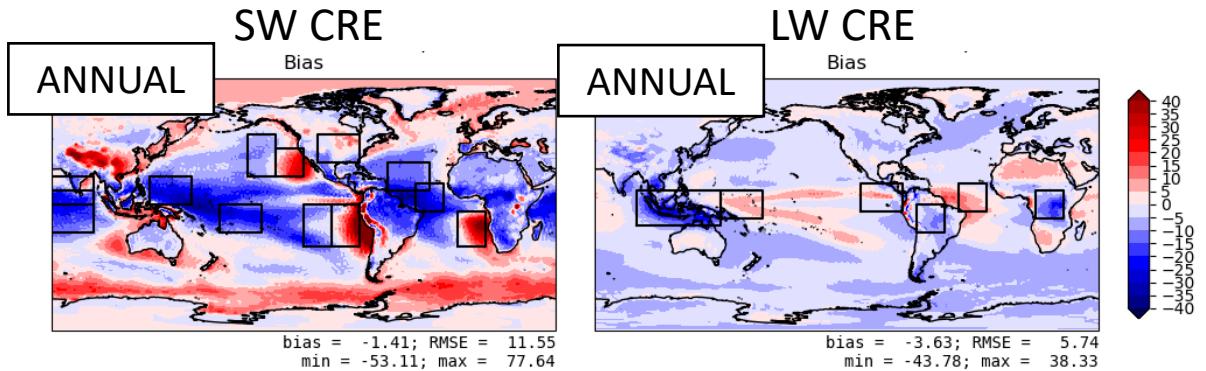
1. Global averages of the energy budget components
2. **Zonally average profiles** of SW/LW CRE + Temperature at 200 hPa
  - SW/LW CRE: CERES-EBAF with uncertainty of  $2 \text{ W m}^{-2}$  + tolerance of  $1 \text{ W m}^{-2}$
  - T200: based on ERA5/JRA55/MERRA/CFSR ensemble mean and std, tolerance 1.5 K



# Metrics, references and uncertainty estimates

Following the CNRM-CM6-1 tuning strategy, 3 classes of metrics:

1. Global averages of the energy budget components
2. Zonally average profiles of SW/LW CRE + Temperature at 200 hPa
3. ***Regional and seasonal averages*** of SW/LW CRE and precipitation
  - SW/LW CRE: CERES-EBAF, uncertainty of  $2 \text{ W m}^{-2}$ , tolerance of  $5 \text{ W m}^{-2}$
  - Precipitation: MSWEP/GPCP/TRMM 3B42 ensemble mean and std, tolerance between 0.5 and 1  $\text{mm day}^{-1}$



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Following the CNRM-CM6-1 tuning strategy, 3 classes of metrics:

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3. Regional and seasonal averages of SW/LW CRE and precipitation

➤ **63 (scalar) metrics**

# Model parameters and simulation strategy

## **46 model parameters**

- 7 from turbulence (TKE scheme + PBL-top entrainment)
- 16 from microphysics (1-moment, 5 hydrometeors)
- 19 from the unified dry, shallow and deep convection scheme
- 4 from cloud radiative properties (heterogeneity)

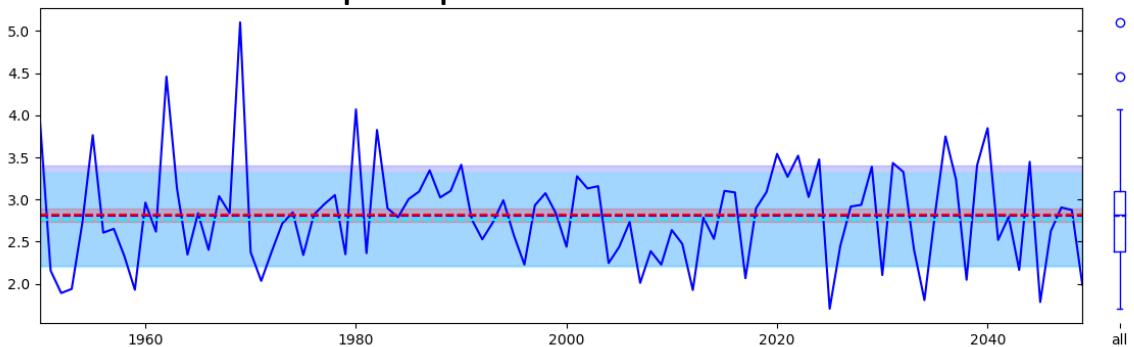
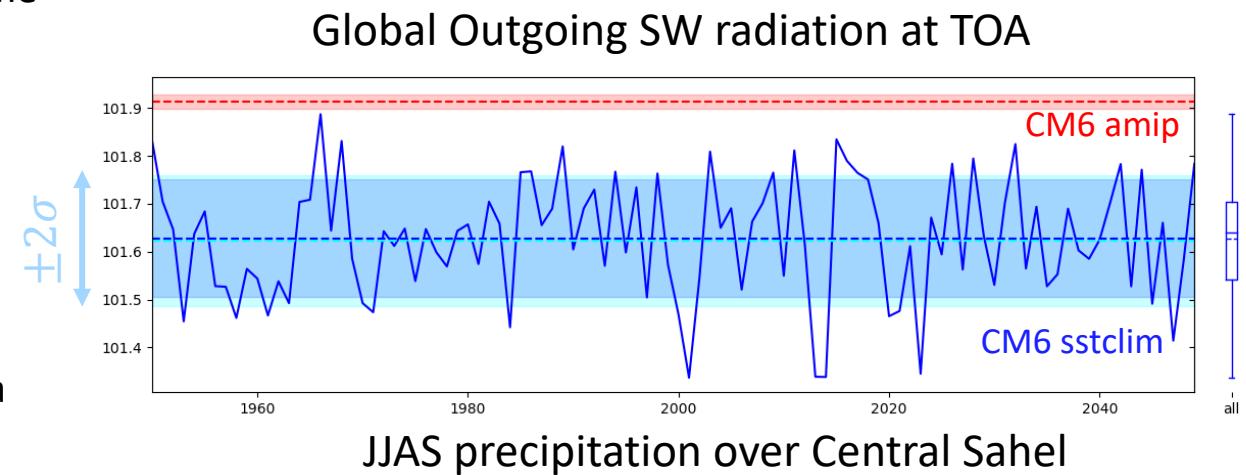
# Model parameters and simulation strategy

## 46 model parameters

- 7 from turbulence (TKE scheme + PBL-top entrainment)
- 16 from microphysics (1-moment, 5 hydrometeors)
- 19 from the unified dry, shallow and deep convection scheme
- 4 from cloud radiative properties (heterogeneity)

## Waves of 400 simulations

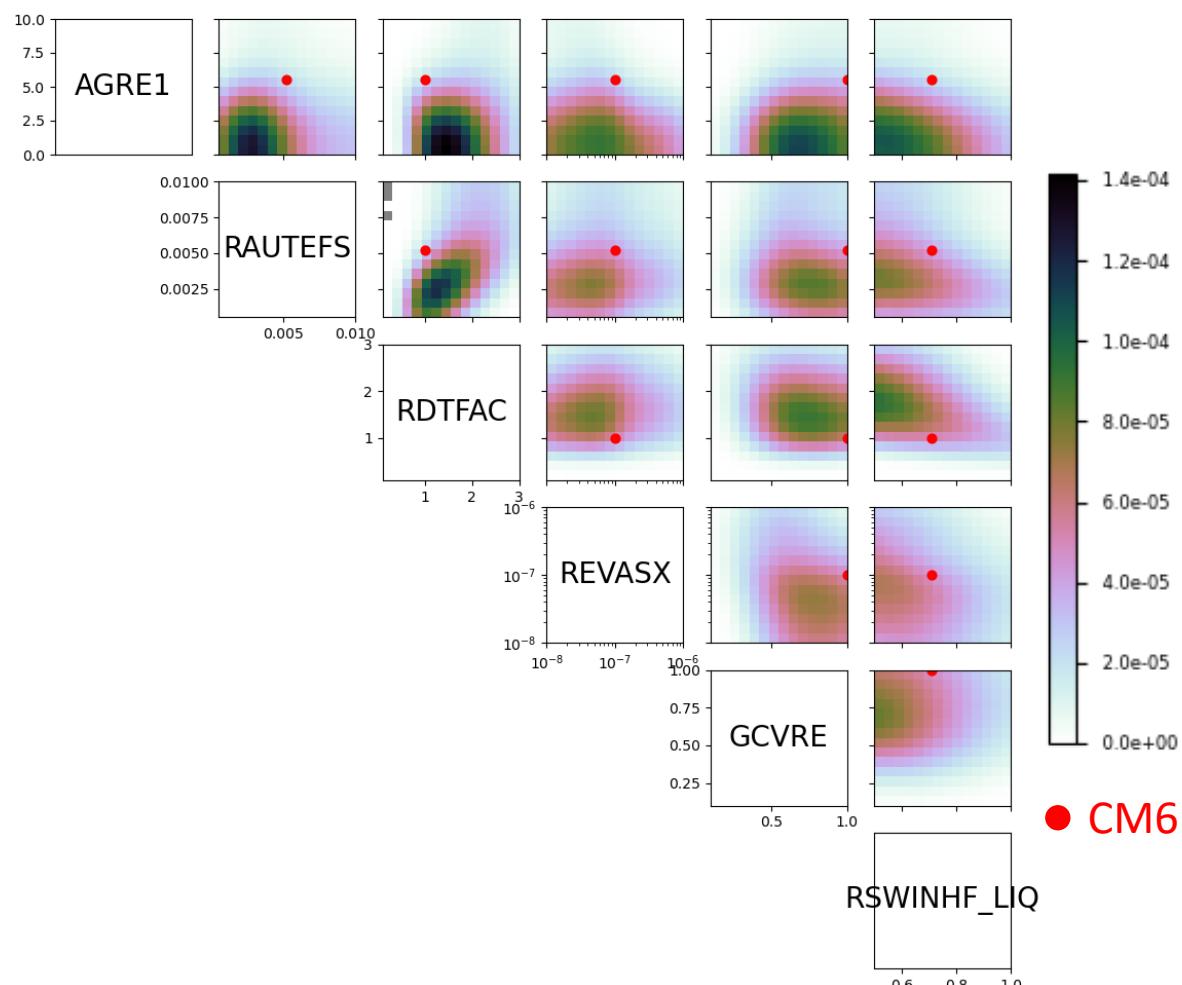
- 1-year **sstclim** simulations + 3-month spin-up
- sstclim vs amip correction of the reference target
- Consideration of **internal variability uncertainty** based on a 100-year sstclim simulation with CNRM-CM6-1.
- Latin Hypercube sampling for 1<sup>st</sup> wave



# Wave 1 results

- NROY<sup>1</sup> space: 0.66% of the input space
- Cloud (esp. ice) and convection parameters are critical

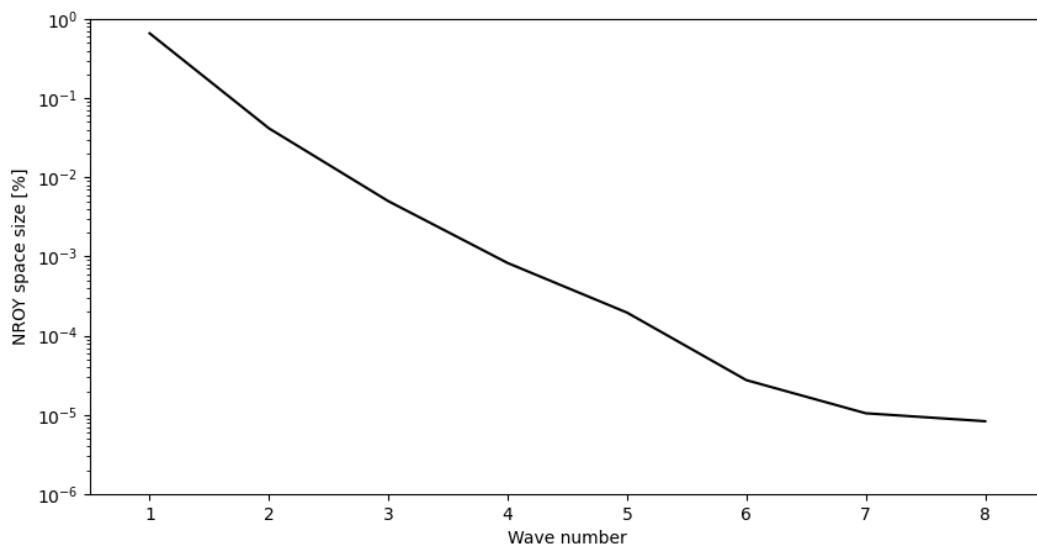
NROY<sup>1</sup> density within input parameter space  
For some of the dominant parameters



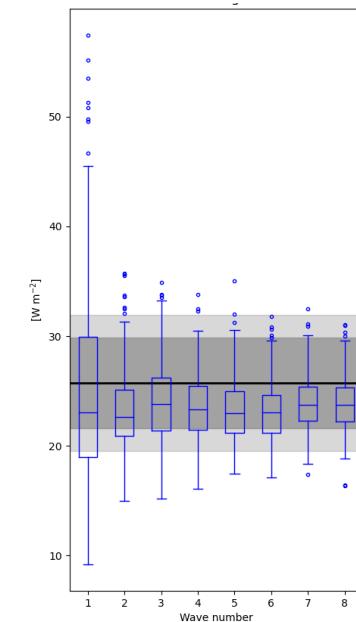
# From Wave 1 to Wave 8

- Large shrinking of the NROY space size (8 orders of magnitude)
- Some metrics have converged, some are more demanding

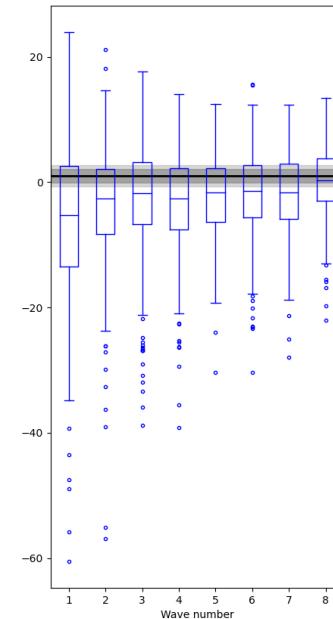
NROY space fraction of the input space



Global LW CRE at TOA

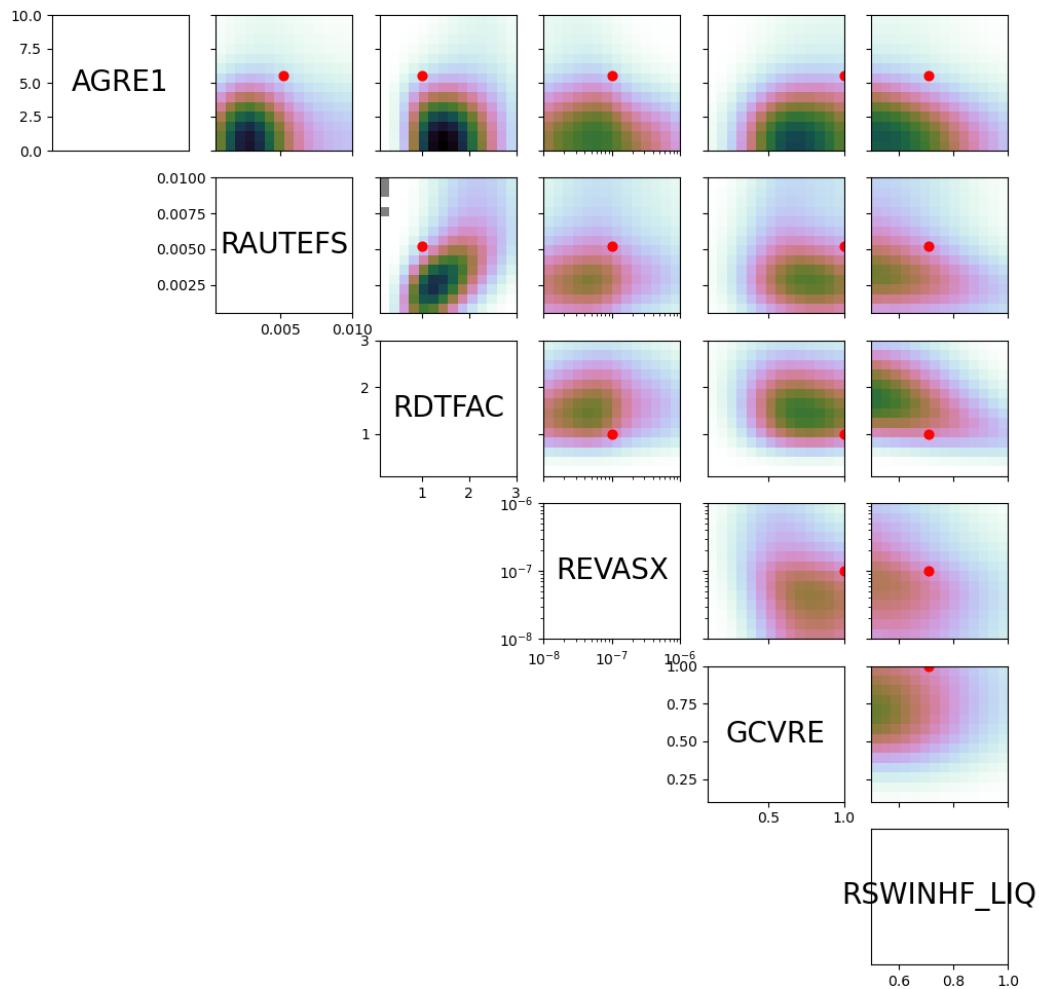


Ocean net energy flux

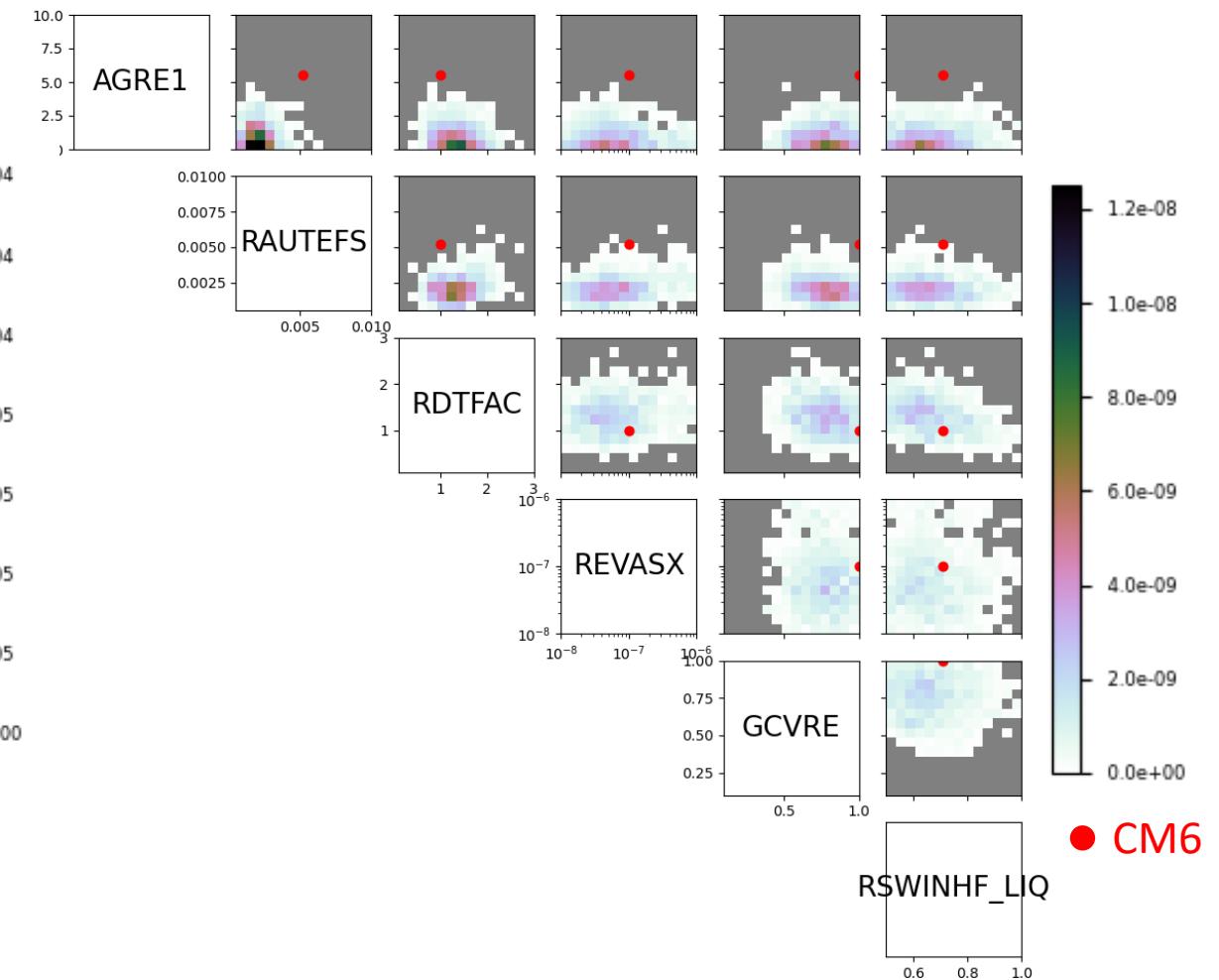


# From Wave 1 to Wave 8

NROY<sup>1</sup> density within input parameter space  
For some of the dominant parameters



NROY<sup>8</sup> density within input parameter space  
For some of the dominant parameters



+ some new dominant parameters have emerged

# Choosing configurations of interest

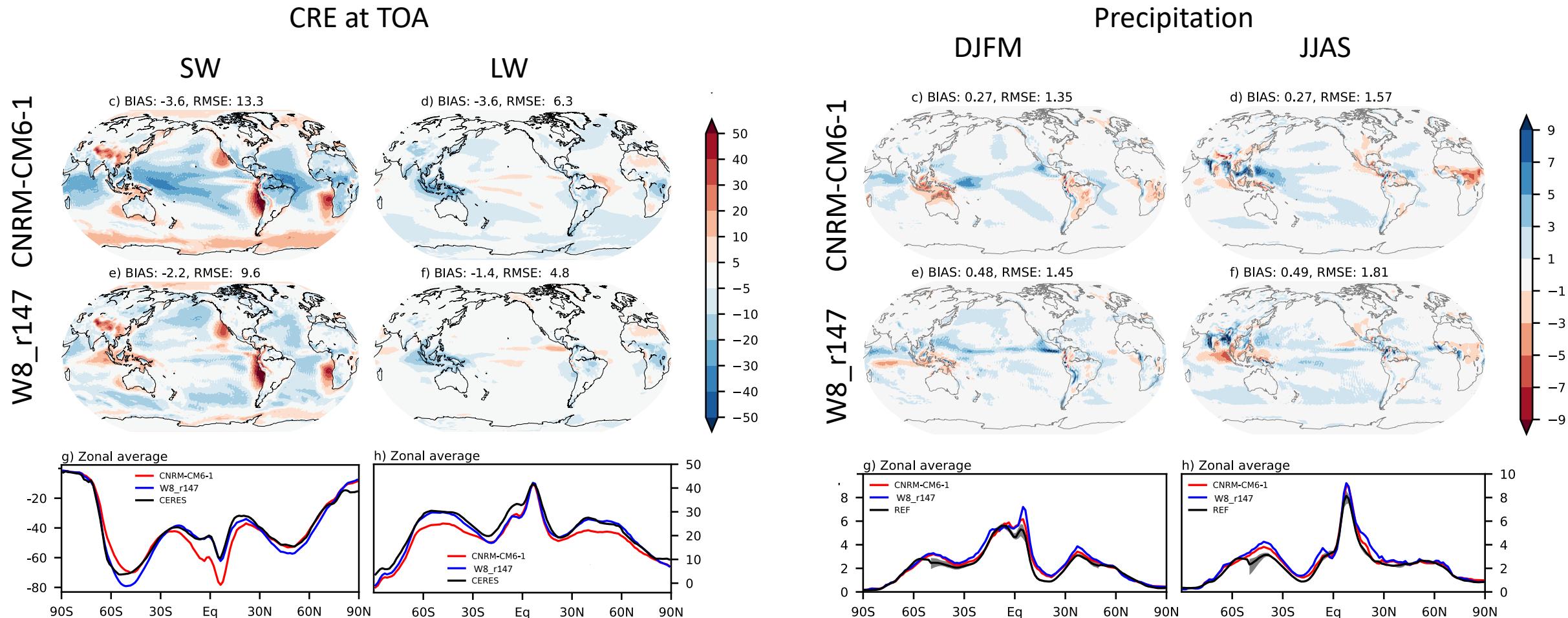
## ***Unfortunately, none of Wave 1-8 simulations fulfils all the metrics***

- Convergence is not yet achieved
- Appropriate sampling of small NROY spaces is difficult and requires further work
- Some tolerances to error are likely too weak and require to be revisited.

## ***Nevertheless***

- A few simulations fulfil all the metrics but one (for a cutoff of 3)
  - A few have interestingly low RMSEs for targeted variables
- A selection of these simulations is further analysed with 10-year amip-style simulations.

# Improved performance?



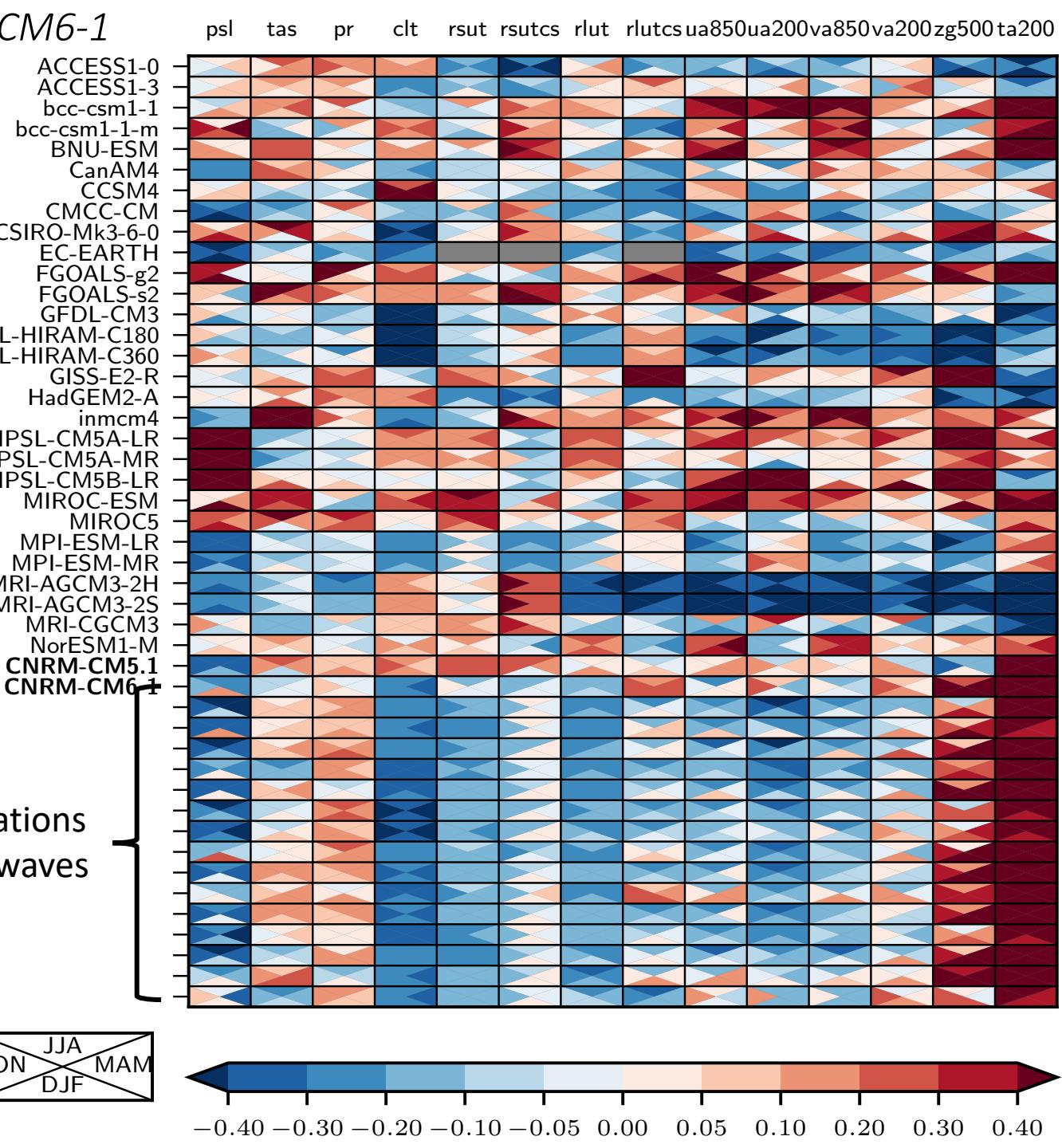
- **Improved or similar performance** on several mean state features
- Some errors seems truly structural: clouds/radiation over eastern part of ocean basins

# Improved performance?

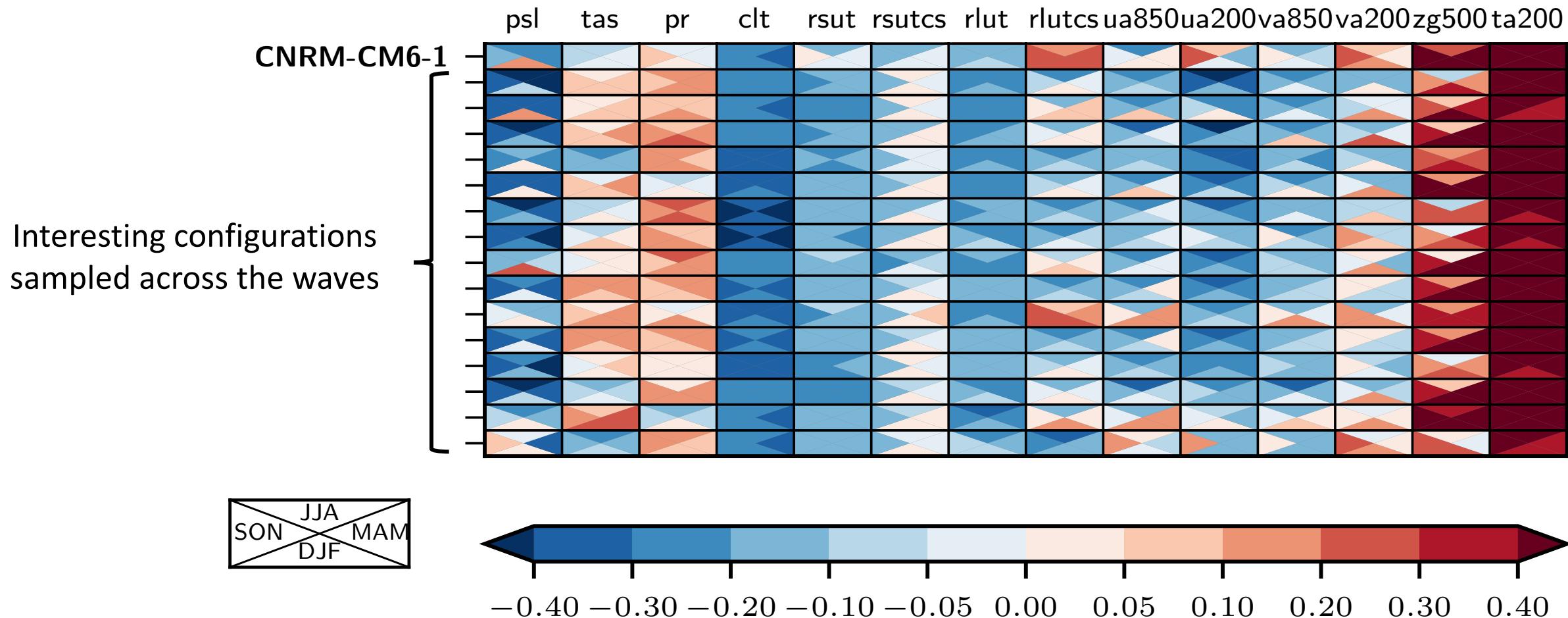
Relative score within the CMIP5 ensemble  
*(Gleckler et al. 2016)*

$$\text{score} = \frac{\text{RMSE} - \text{RMSE}_{\text{median}}}{\text{RMSE}_{\text{median}}}$$

Interesting configurations  
sampled across the waves

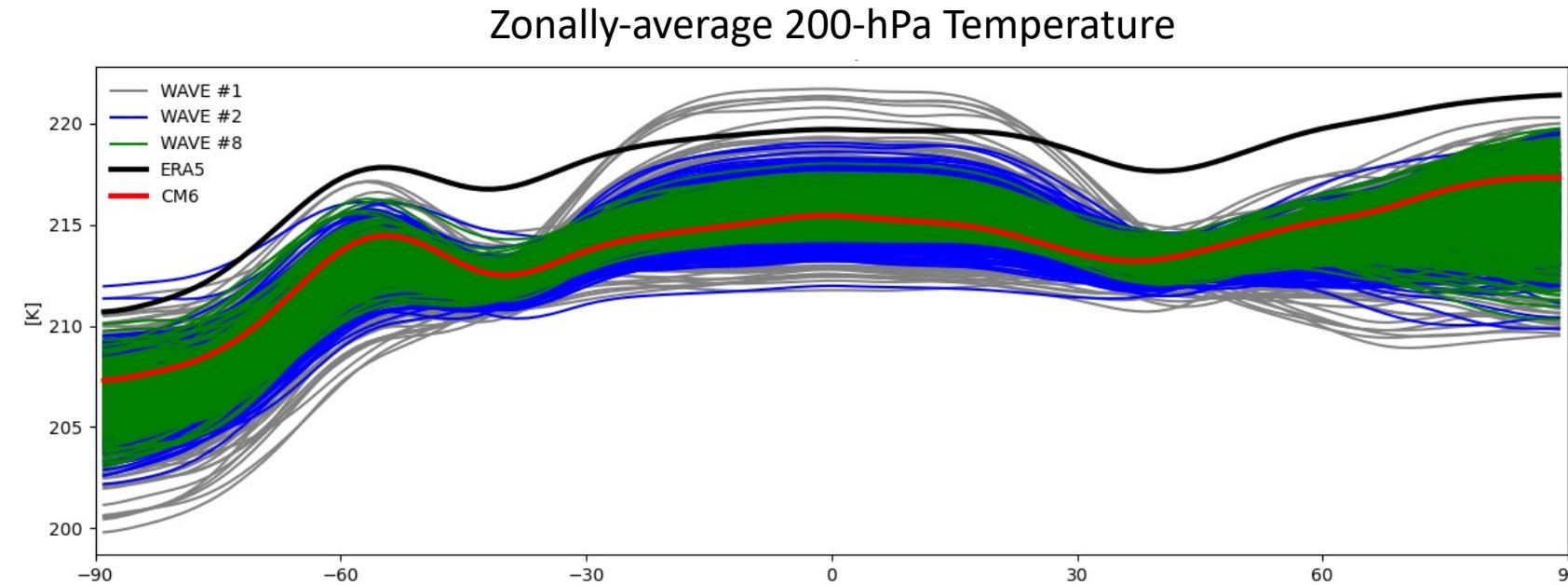


# Improved performance?



- **Improved or similar performance** on several mean state features
- Some errors seems truly structural: clouds/radiation over eastern part of ocean basins, upper-tropospheric temperature
- Some **trade-offs** are required

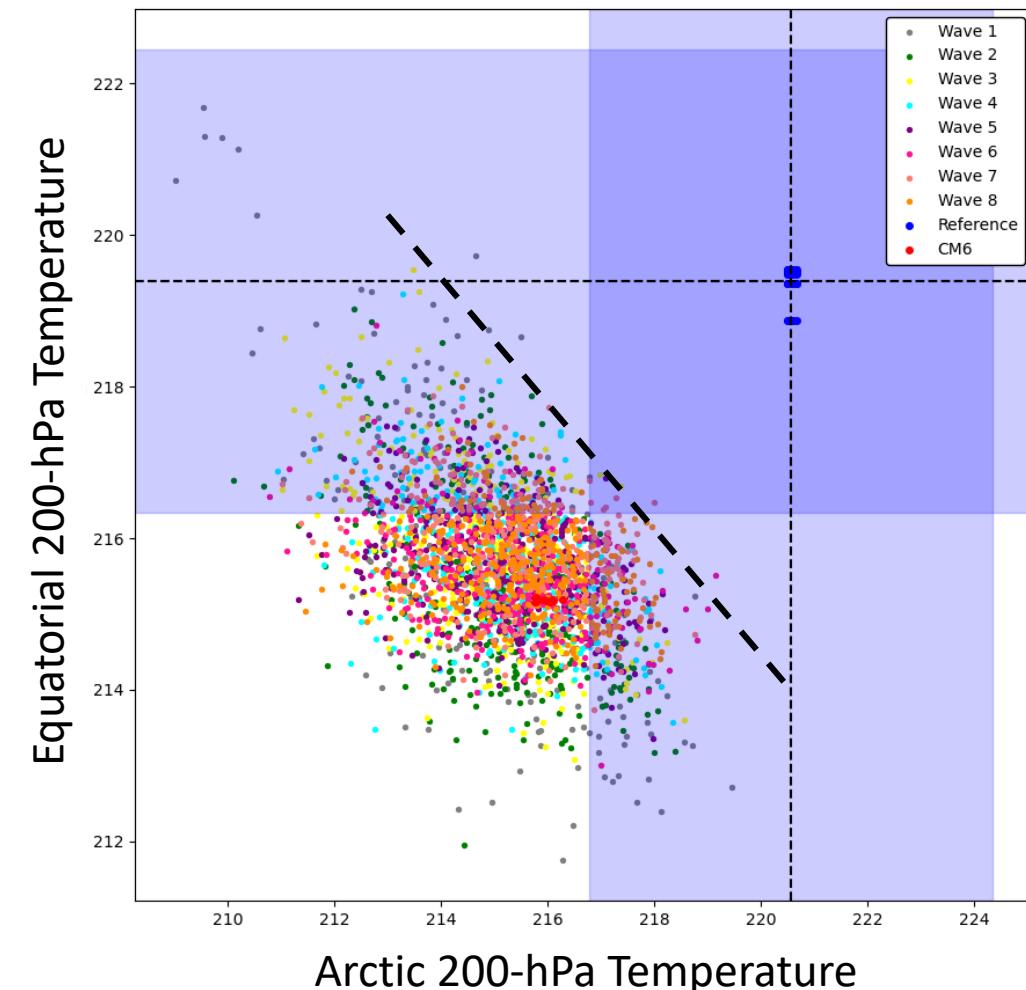
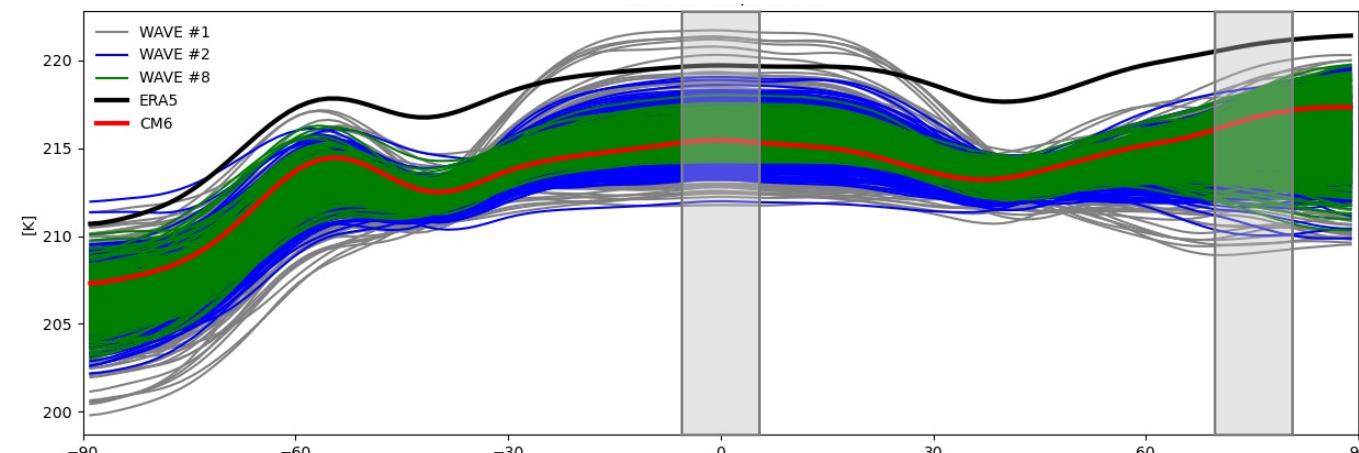
# Upper-tropospheric temperature bias: structural limit?



- Simulations performing well (beyond the chosen tolerance to error) in the equatorial regions disappear with successive waves
  - Incompatible with other metrics

# Upper-tropospheric temperature bias: structural limit?

Zonally-average 200-hPa Temperature



- Simulations performing well (beyond the chosen tolerance to error) in the equatorial regions disappear with successive waves
  - Incompatible with other metrics
- The model can most likely not capture both equatorial and arctic upper-tropospheric temperatures within uncertainty ranges, while remaining compatible with other metrics.

# From 1D and 3D: the High-Tune philosophy

- ***Start calibration at the process level*** (1D vs. LES) to ***pre-condition*** calibration of more realistic configurations
  - Keep the representation of processes right
- Requirement: have ***high-quality references*** (observations, LES or CPM) for the targeted processes.
  - Some are available (LES for boundary-layer convection/clouds, stable boundary layers)
  - Some are currently being developed (radiation for boundary-layer clouds)
  - Some are not fully appropriate or missing (e.g., microphysics)

# Proof of concept with LMDZ

## Multi 1D case approach (boundary-layer clouds) :

- Dry convective boundary layer (IHOP, Couvreux et al. 1996)
- Continental cumulus (ARMCU, Brown et al. 2002)
- Marine cumulus (RICO, van Zanten et al. 2011)
- Stratocumulus-cumulus transition (SANDU, Sandu et al. 2011)
- Reference LES: Meso-NH ou UCLA

Metrics Retained for the SCM/LES Tuning						
Case	IHOP	ARMCU	RICO	SANDU	SANDU	SANDU
Subcase	REF	REF	REF	REF	SLOW	FAST
Time	7–9	7–9	19–25	50–60	50–60	50–60
$\theta_{400\text{--}600\text{ m}}$	X	X	-	-	-	-
$q_v,400\text{--}600\text{ m}$	-	X	-	-	-	-
$\alpha_{cld,\text{max}}$	-	X	X	-	-	-
$z_{cld,\text{ave}}$	-	X	-	X	-	-
$z_{cld,\text{max}}$	-	X	-	X	X	X

## Metrics

- 11 1D metrics: potential temperature, humidity averaged in the boundary layer, cloud fraction
- 11 3D metrics: TOA radiative budget components, global/regional averages

## LMDZ model parameters

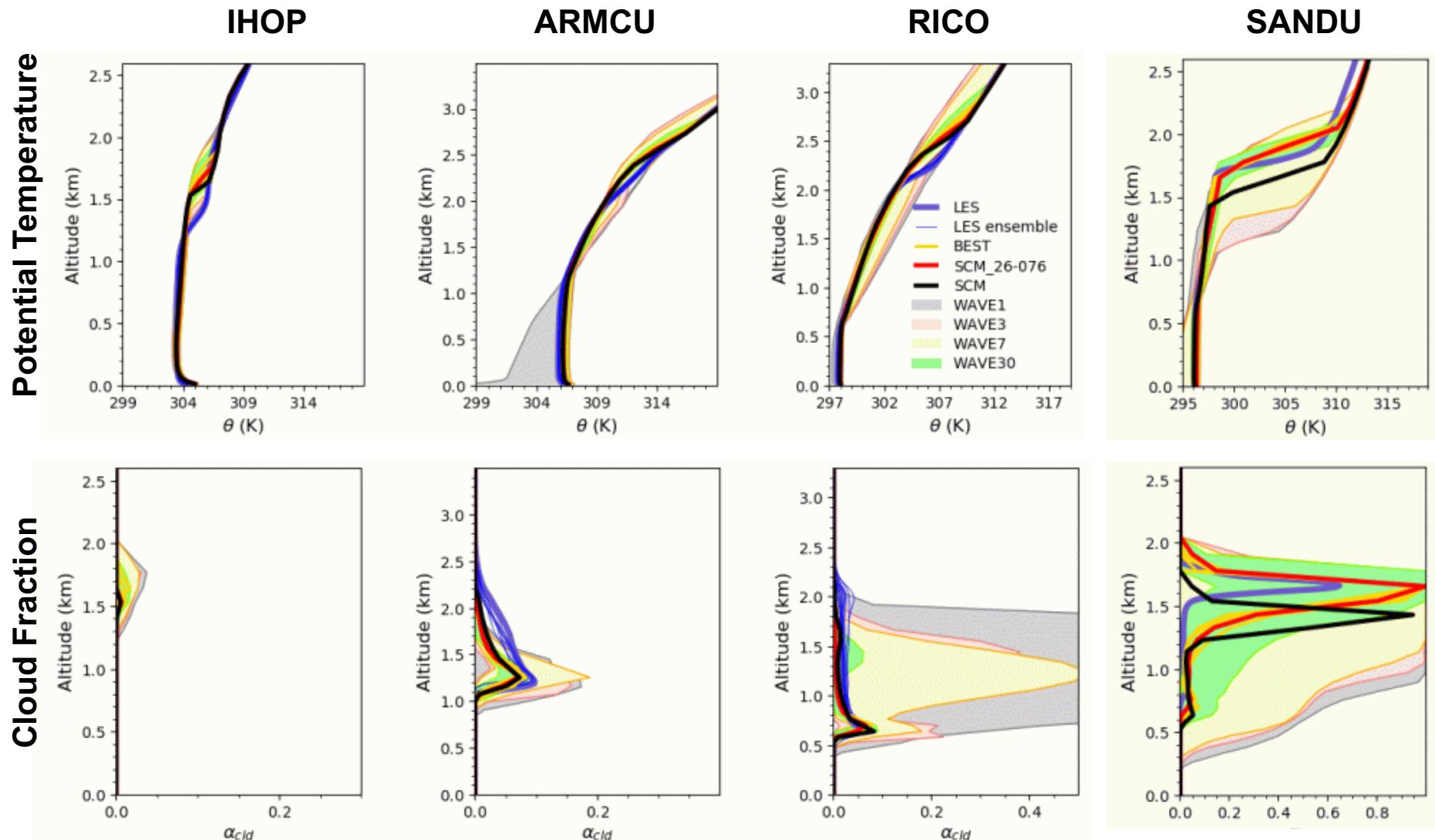
- 9 parameters from cloud, shallow convection and microphysics parameterizations

Mask	Variable	Metrics	target W m <sup>-2</sup>	error W m <sup>-2</sup>
	Total rad. TOA (rt) Swup TOA (rsut)	glob.rt	2.5	0.2
	glob.rsut	99.6	5	
	circAa.rsut	24.0	5	
	circAa.rlut	-48.6	5	
	subs.rsut	84.9	5	
	weak.rsut	81.8	5	
	conv.rsut	103.2	5	
	subs.rlut	274.6	5	
	weak.rlut	264.3	5	
	conv.rlut	235.8	5	
	etoa.rsut	11.0	5	
	SWup TOA (rsut) LWup TOA (rlut)			
	Eastern Tropical Ocean anomaly	SWup TOA (rsut)		

## Waves

- 30 waves with 1D configuration, progressive reduction of the implausibility cutoff (from 3 to 2)
- 2 waves with 3D configuration

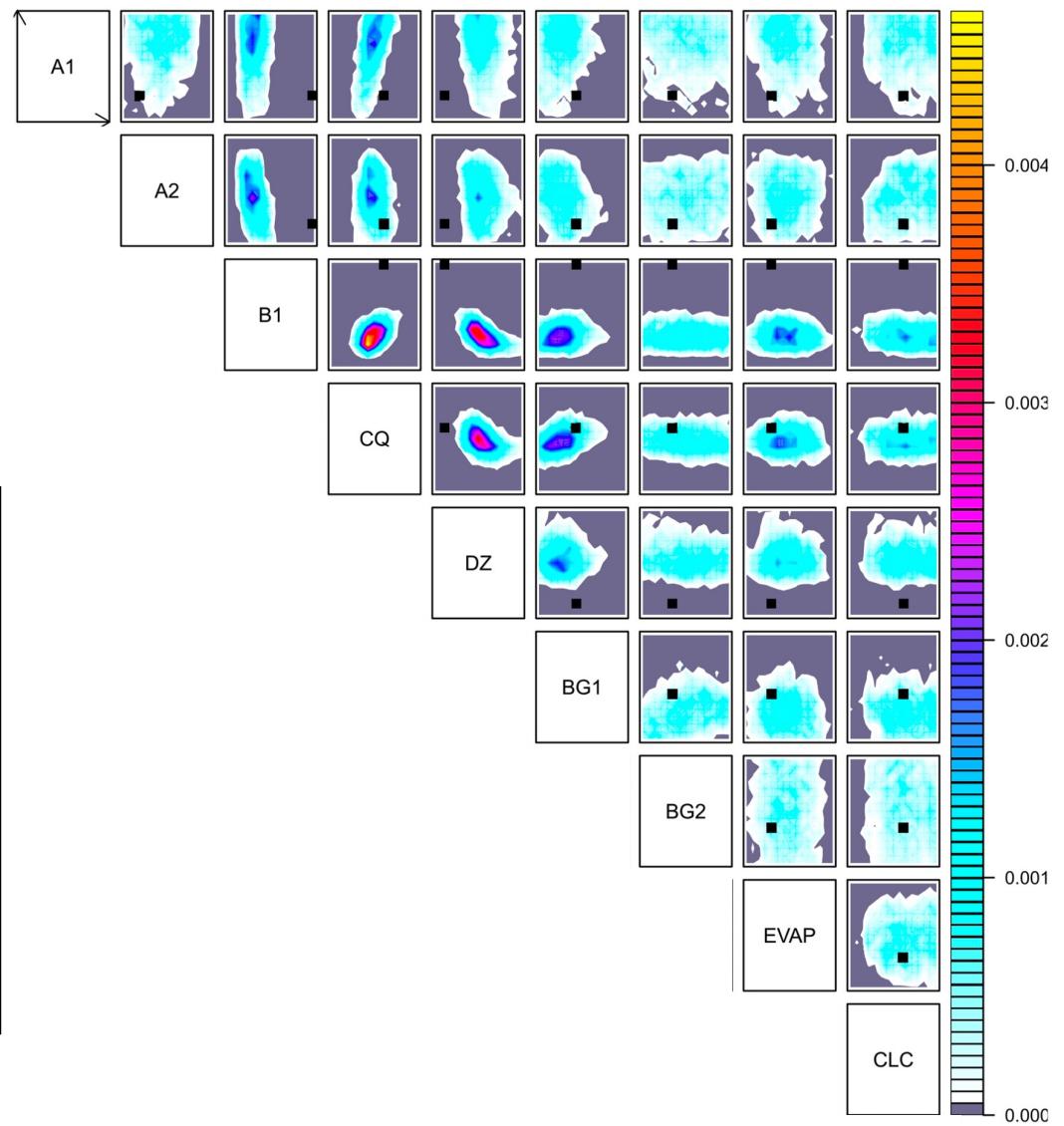
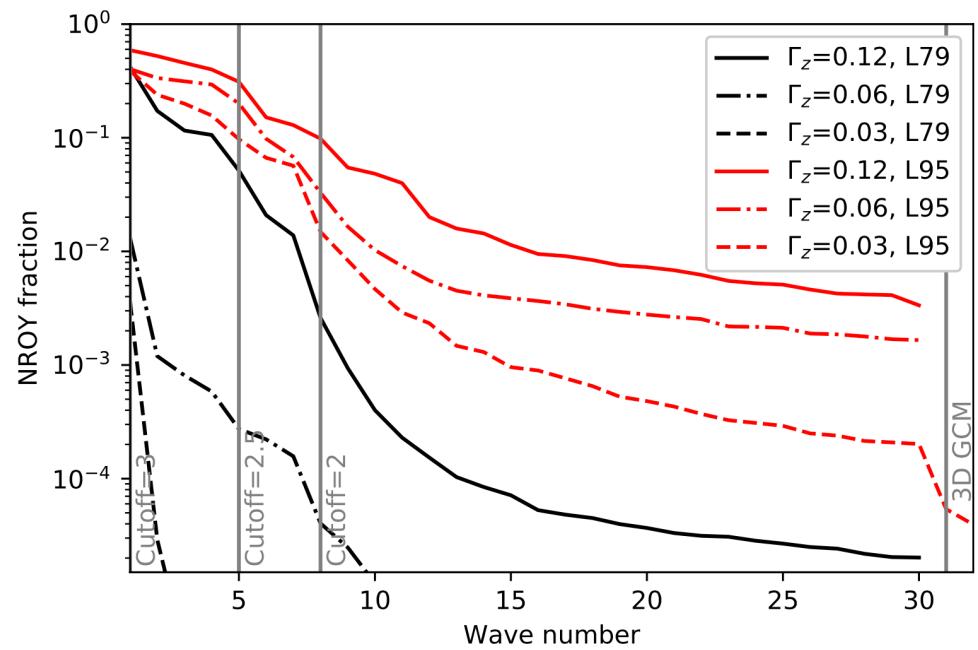
# 30 Waves in 1D



# 30 Waves in 1D

## NROY space

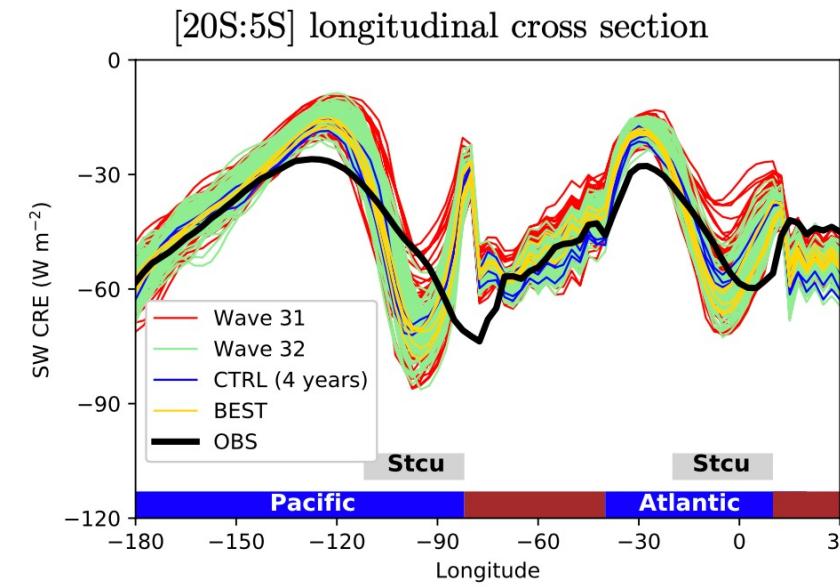
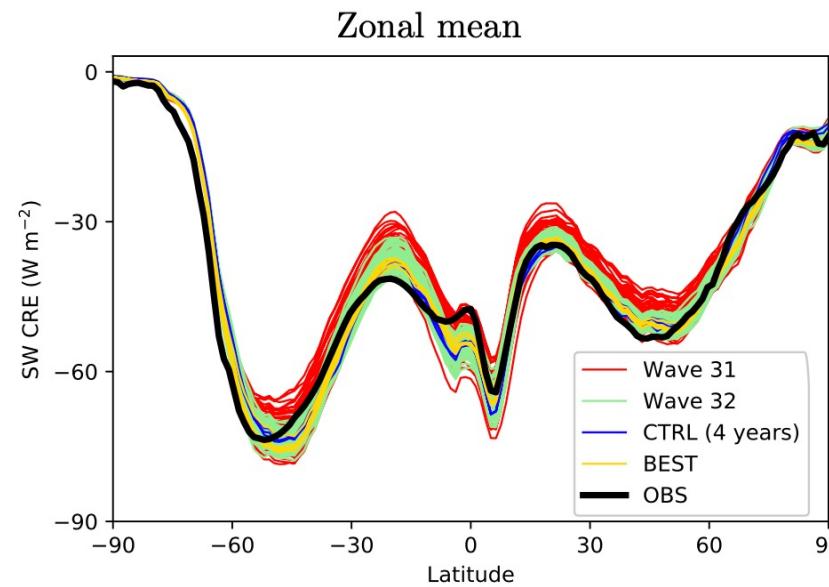
- Approximate convergence
- Non-empty space (0.02% of the *input space*)
- LMDZ6 calibration non optimal



# 2 waves in 3D

## Continuing calibration in 3D, starting from 1D NROY space

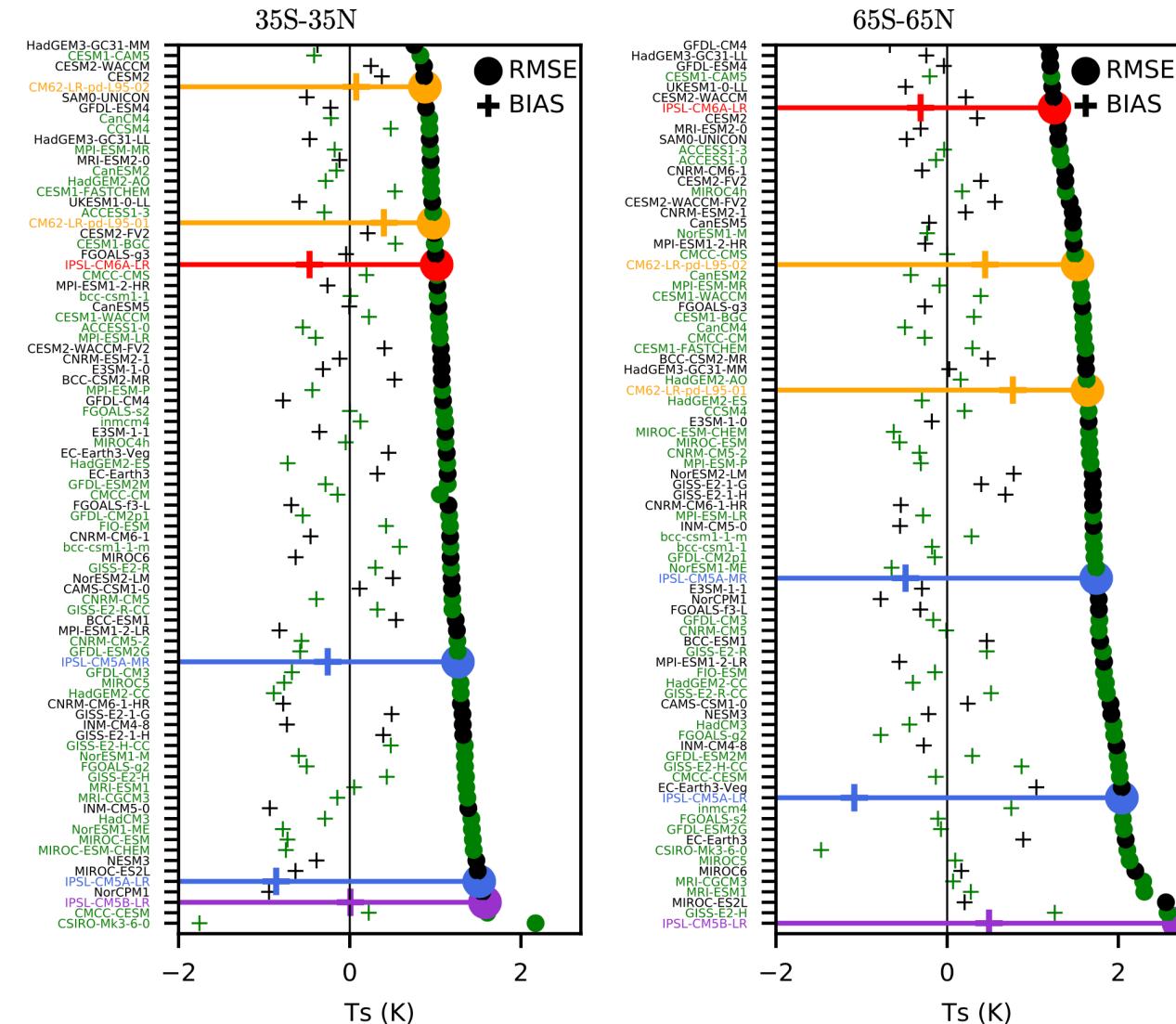
- Non-empty space (0.004% of the input space)
- 1D calibration resulted in an efficient pre-conditioning of the 3D model
- LMDZ6 calibrated ‘by hand’ relatively skilfull, though non optimal
- Probably necessary to add a few more waves (but dependent on computing resources)



# Testing in ocean-atmosphere coupled configurations

## From atmosphere-only to OA coupled configuration

- Calibration by hand of the TOA energy budget  
(1 parameter)
- Behaviour similar to the version calibrated  
by hand over 2-3 years.



# Conclusions, Perspectives

## *History matching with iterative refocussing*

- Provides a **relevant and efficient framework for model calibration in the presence of uncertainties**
- Can help accelerate model development by comparing calibrated model version
  - *Assessing the true added value of a new development*
- Helps better **identify and quantify model structural errors**, and thereby helps focus on bias understanding/model development
- **Overall questions the scientific content of a climate model**

## *Next steps*

- Play with tolerances to error to better identify/quantify model structural errors and trade-offs to be made
- Add new metrics, e.g., variability: can we get both mean state and variability right?
- Pre-conditioning with cheaper model configurations
  - e.g., 1D/LES for preserving process-level performance (*Couvreux et al. 2020, Hourdin et al. 2020*).
- Towards calibration of ocean-atmosphere coupled configurations:
  - accelerating spin-up, use of intermediate resolutions, fast/slow processes...
- Develop physical interpretations of what is happening in the calibration process.

## *More on the technical/statistical aspects*

- Develop strategies to better sample particularly small NROY spaces.
- Going beyond scalar metrics, emulate directly vectors/maps (e.g., using EOFs, *Salter et al. 2019*)
- Emulate the expert judgment ('subjective metrics', *Xu et al. 2023*)