

# Deep Learning as a model of the brain

@kordinglab, CIS 522, 2020

# CIS 522: Lecture 14T

Neuroscience & Deep Learning

4/28/20

# Today

- Why the brain must approximate BP
- Proposals of how the brain may approximate BP

# So far in this course

- Look at neuroscience
- and cognitive science
- Be (weakly) inspired to try new cost functions, architectures, and optimizers

Could the brain do something like backpropagation of error?



# What is a learning algorithm?

$$\Delta W$$

# What is a learning algorithm?

$$\Delta \mathcal{L} = \Delta W \frac{\partial \mathcal{L}}{\partial W}$$

# Why backpropagation works

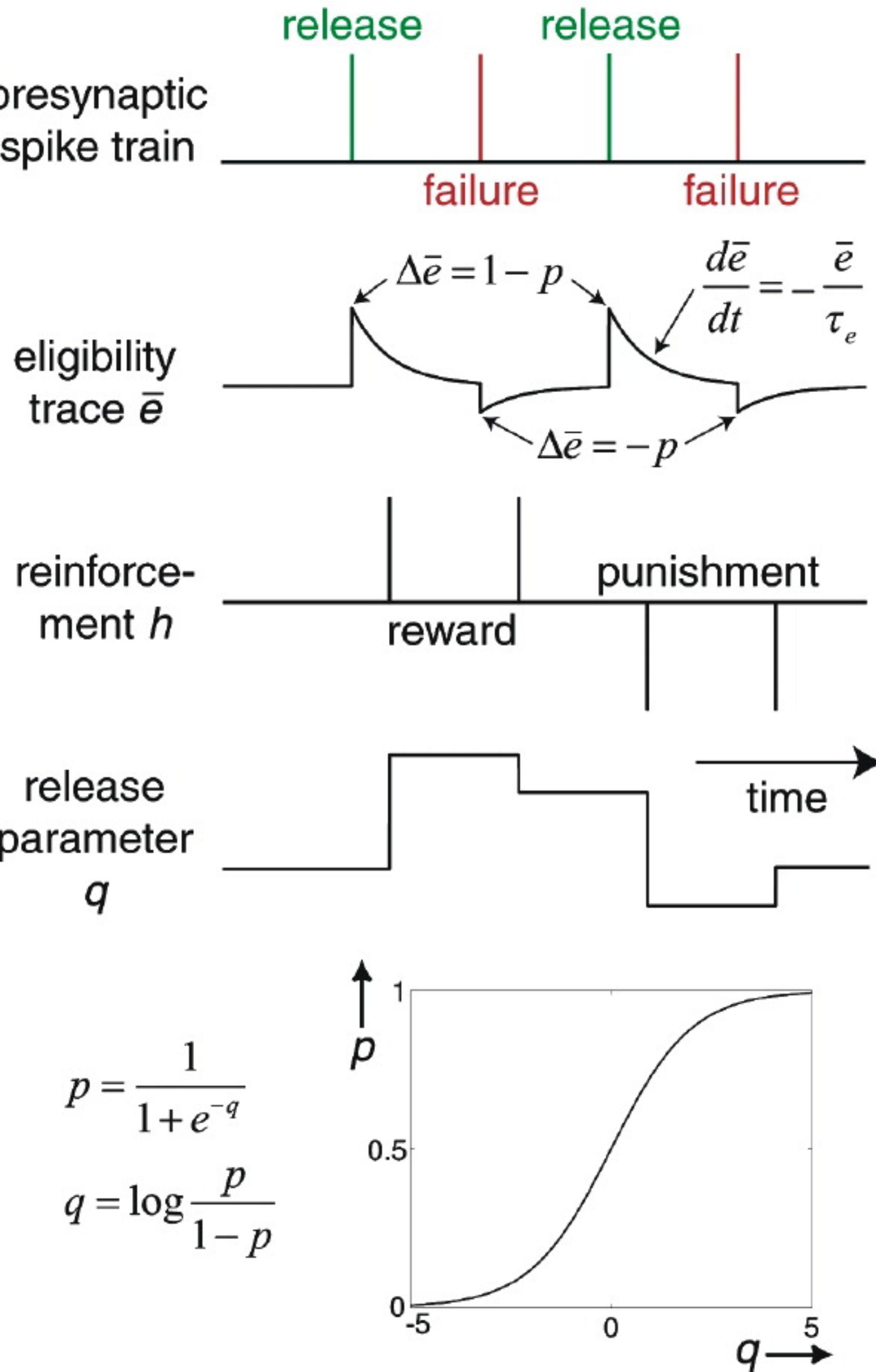
$$\Delta \mathcal{L} = \Delta W \frac{\partial \mathcal{L}}{\partial W}$$

$$\Delta W = -\eta \frac{\partial L}{\partial W}$$

$$\Rightarrow \Delta L = -\eta \left| \frac{\partial L}{\partial W} \right|^2$$

# **Simple solutions can not work**

# Weight perturbation



# Variance of the estimator?

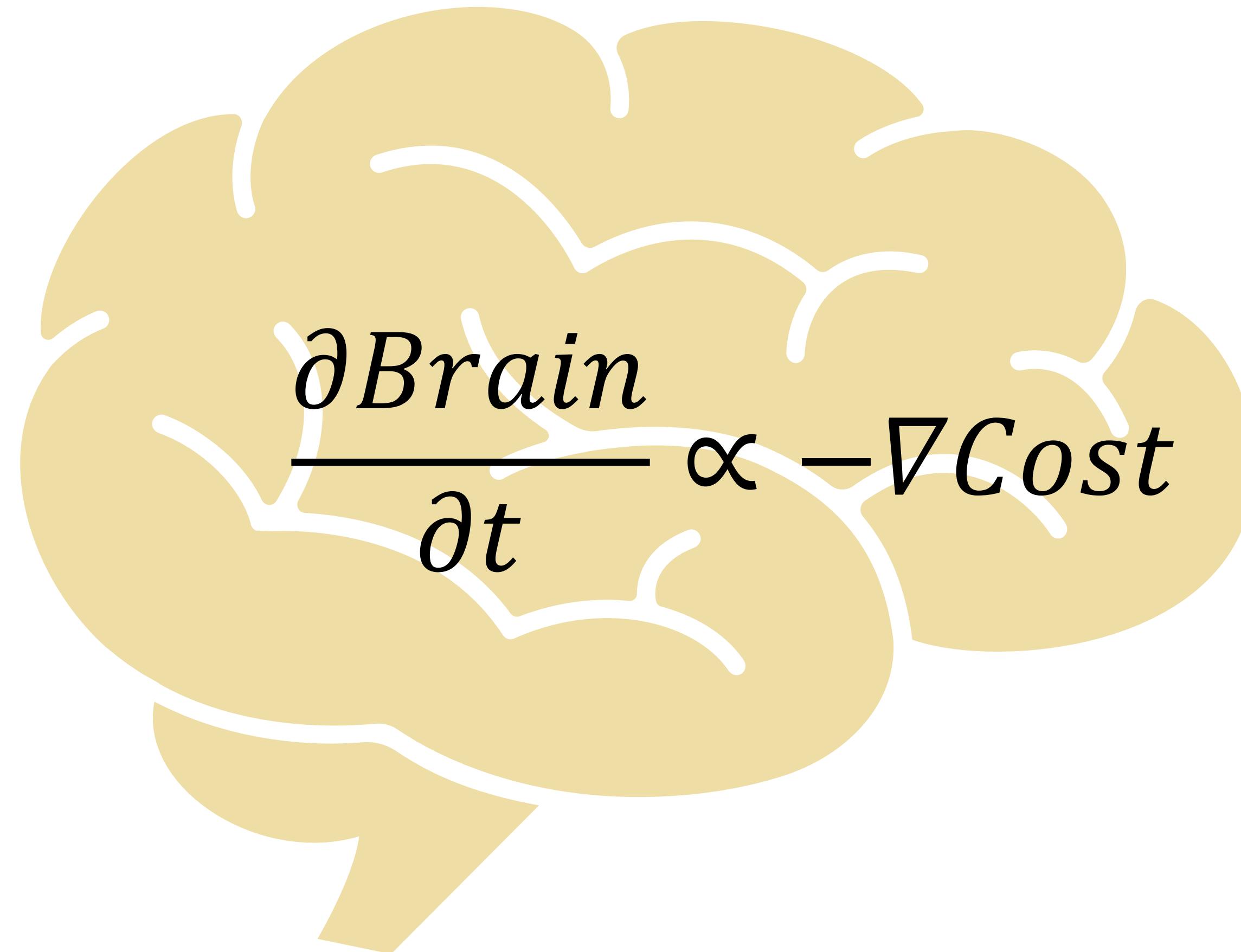
$$\Delta W \sim N(0, \epsilon)$$

$$f(W + \Delta W) = f(W) + \sum_i \frac{\partial f}{\partial W_i} \Delta W_i$$

$$var f(W + \Delta W) = N\epsilon$$

$$var \frac{\Delta f}{\Delta W_i} \approx N$$

# An increasingly popular hypothesis



# Why now?

- Hydraulic Brains
- Electric Brains
- Computer Brains
- Deep learning Brains

**Cynical answer:**  
Whatever works is  
our best hypothesis

# Could the brain implement backdrop?

- Problem 1: Weight transport
- Problem 2: Multiplexing

# Realistic BP is about as old as BP

COGNITIVE SCIENCE 9, 147–169 (1985)

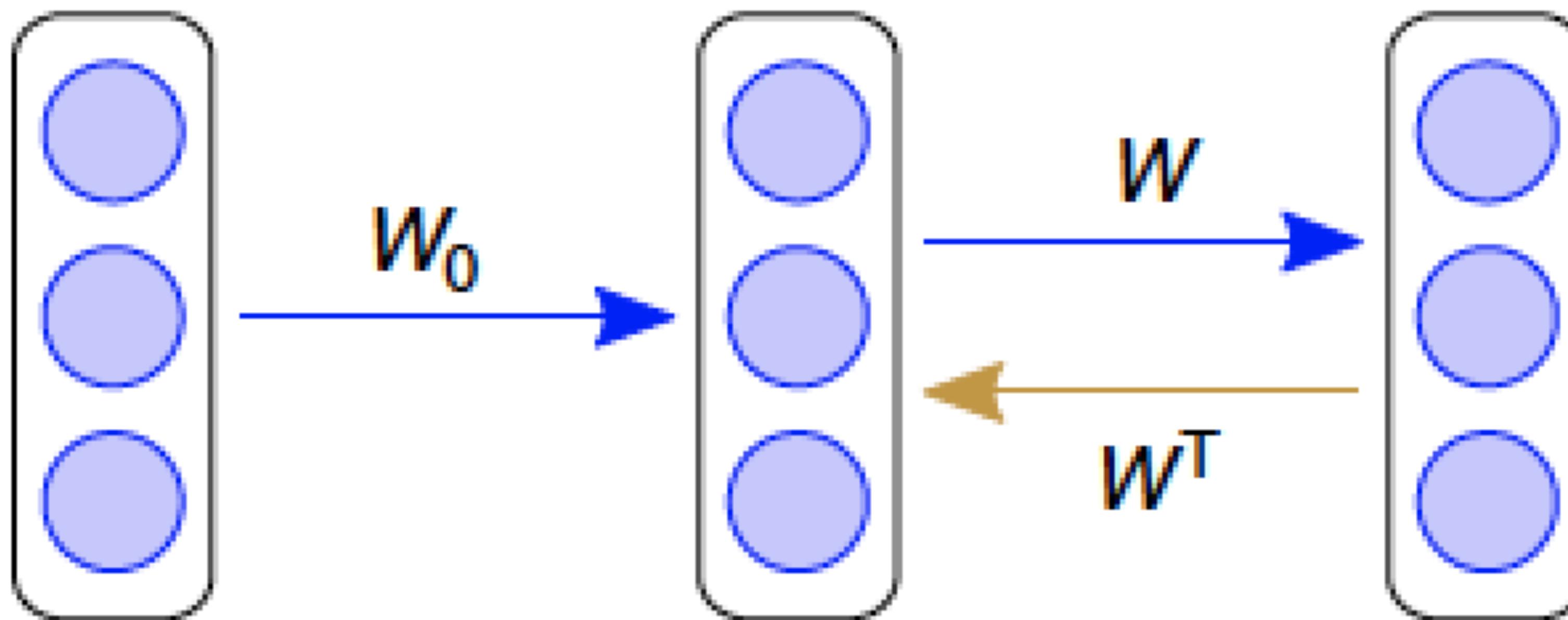
## A Learning Algorithm for Boltzmann Machines\*

DAVID H. ACKLEY  
GEOFFREY E. HINTON

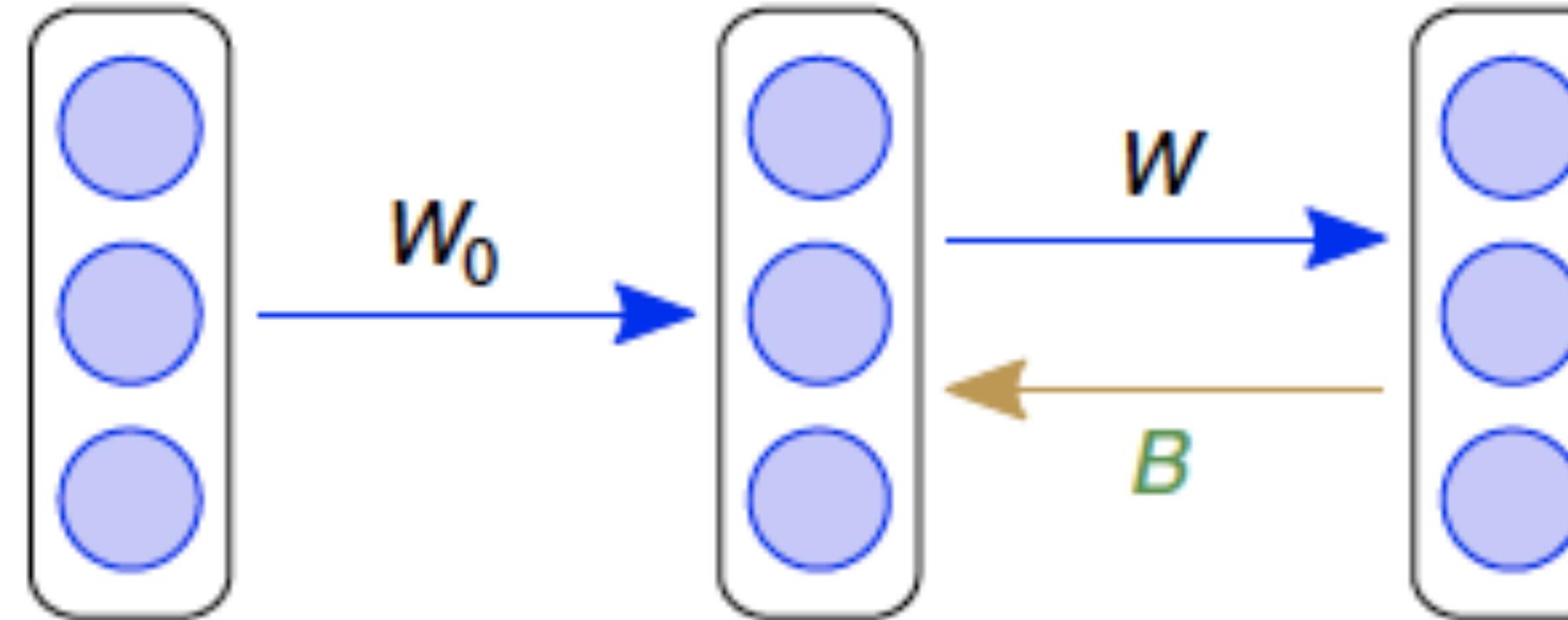
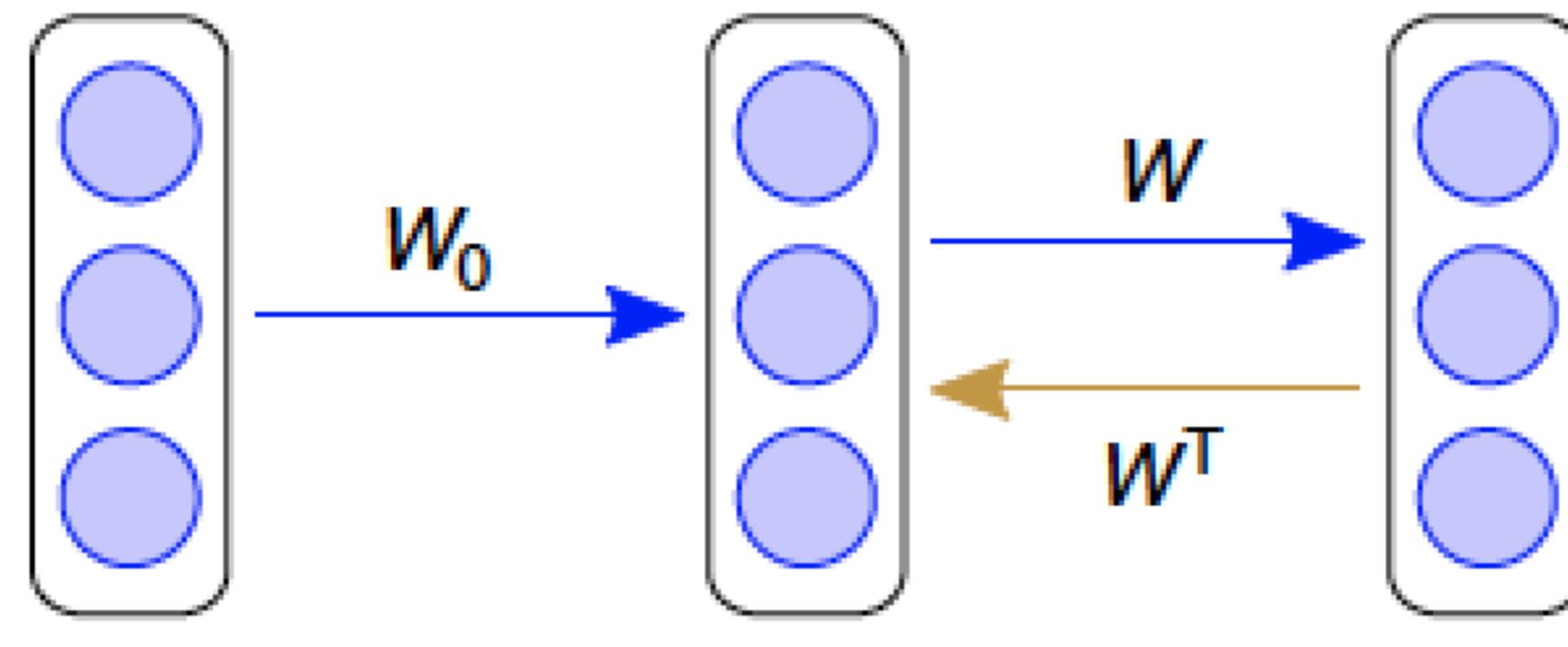
*Computer Science Department  
Carnegie-Mellon University*

TERRENCE J. SEJNOWSKI  
*Biophysics Department  
The Johns Hopkins University*

# Problem 1: weight transport



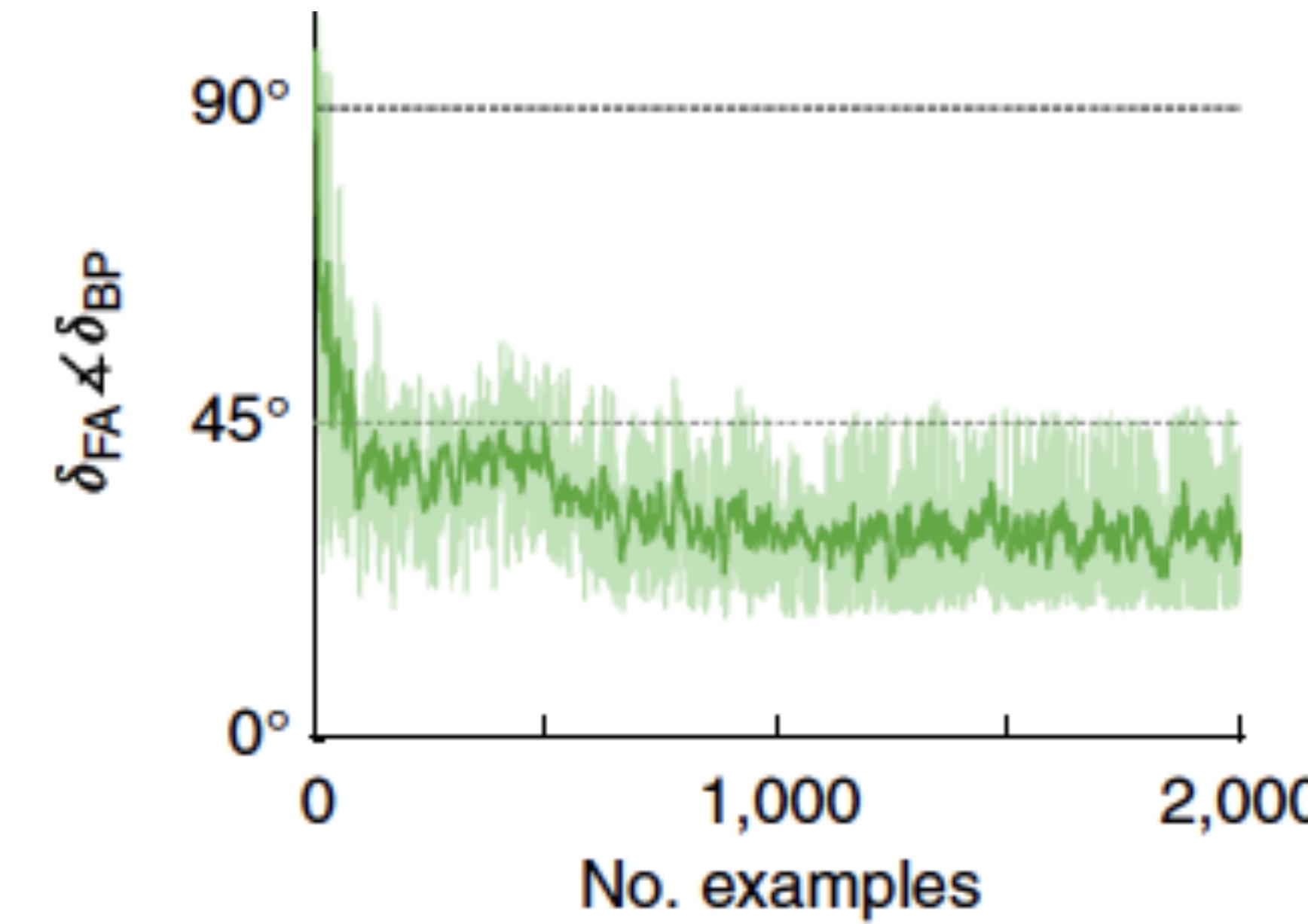
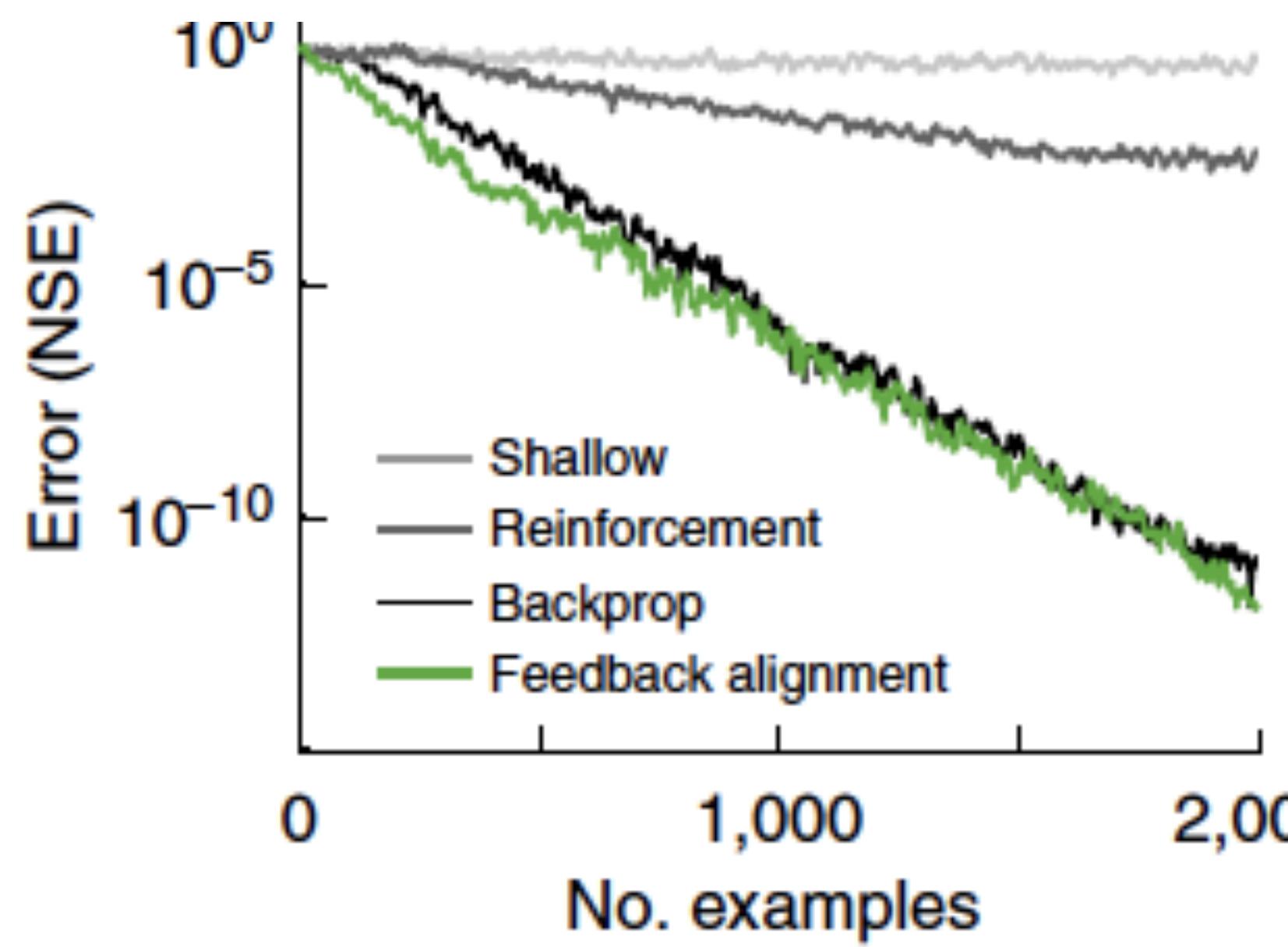
# Feedback alignment



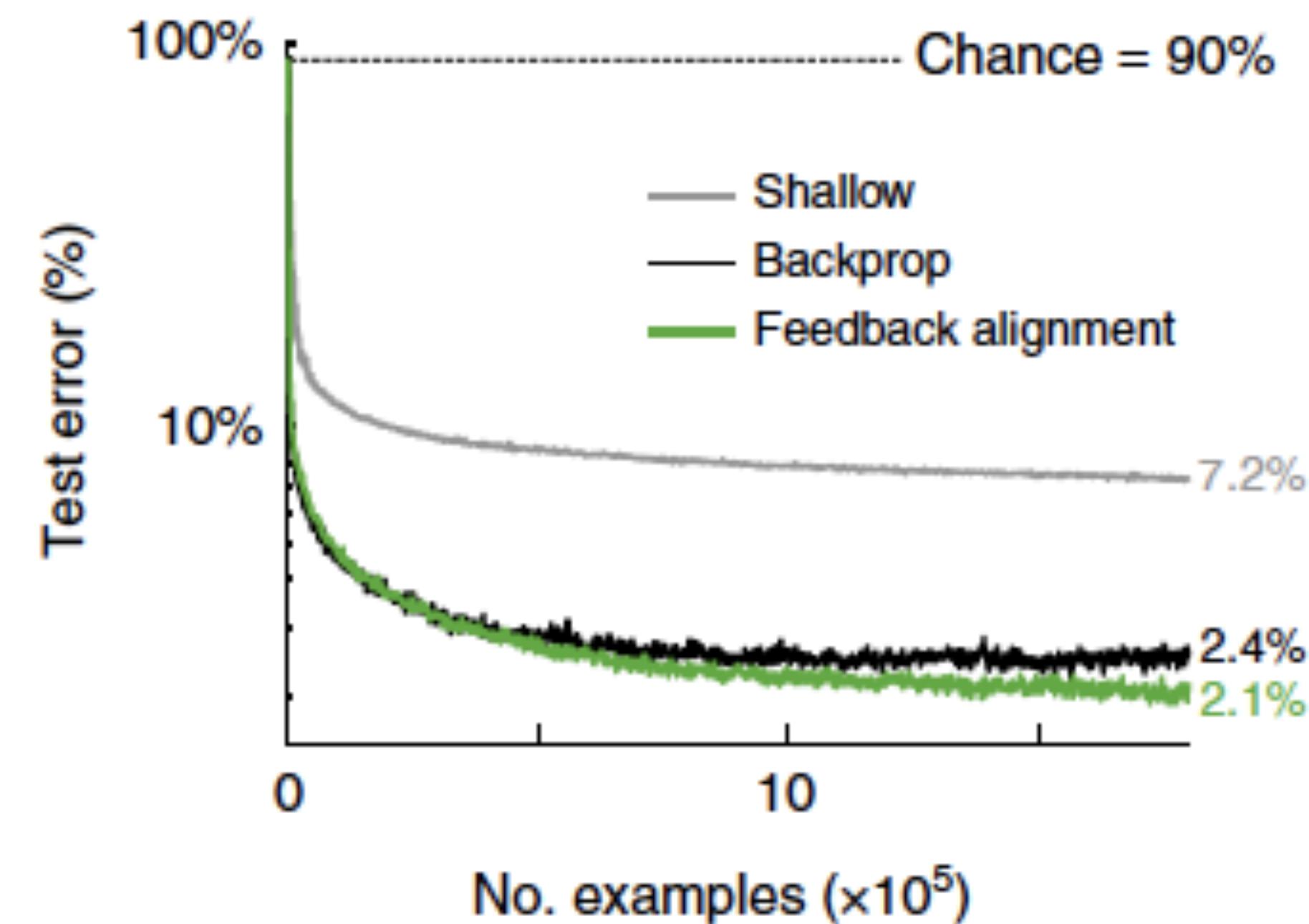
Lillicrap Tweed ...

$$\Delta W_0 \propto B e x^T$$

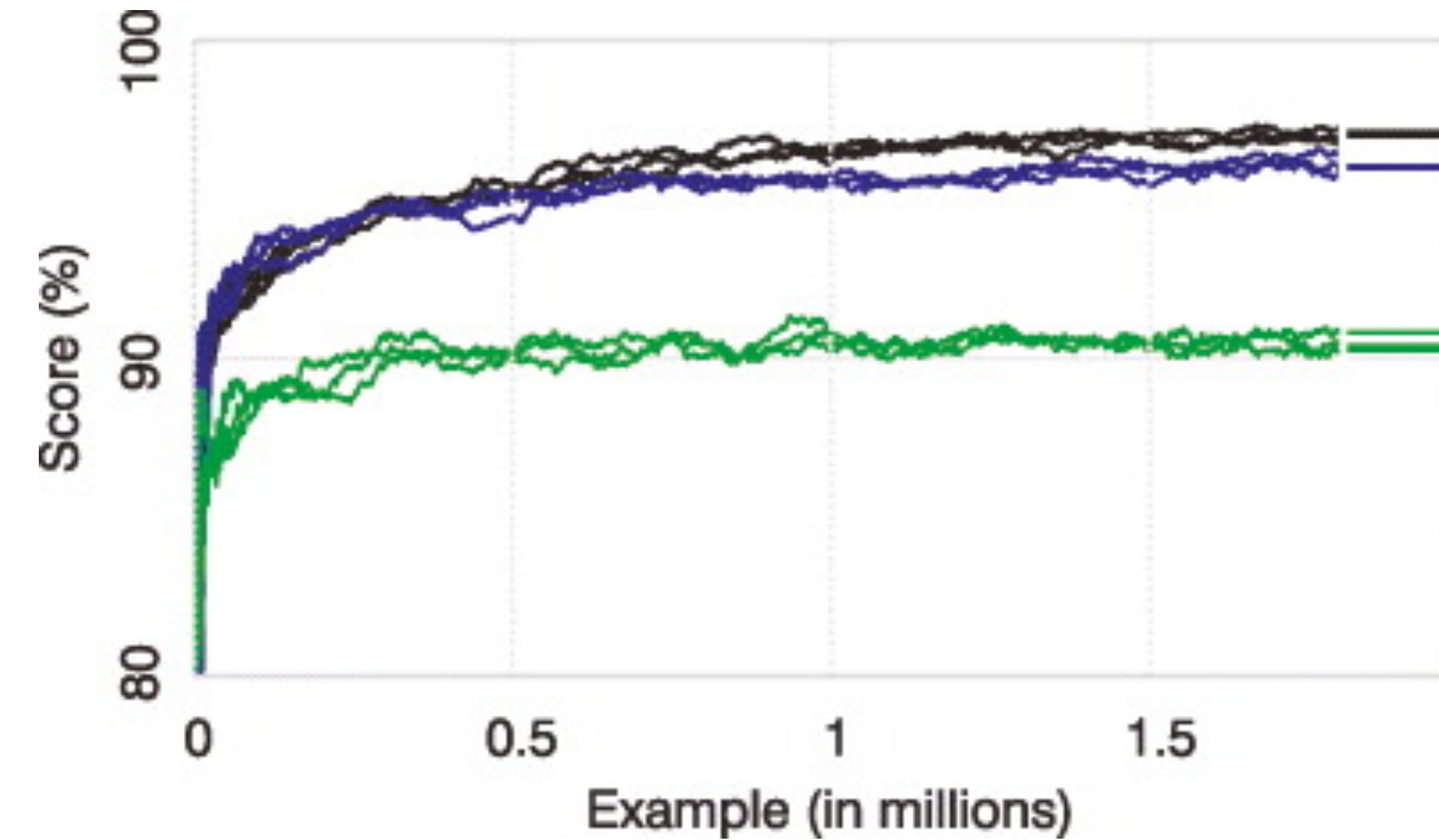
# Works on linear problems



# MNIST

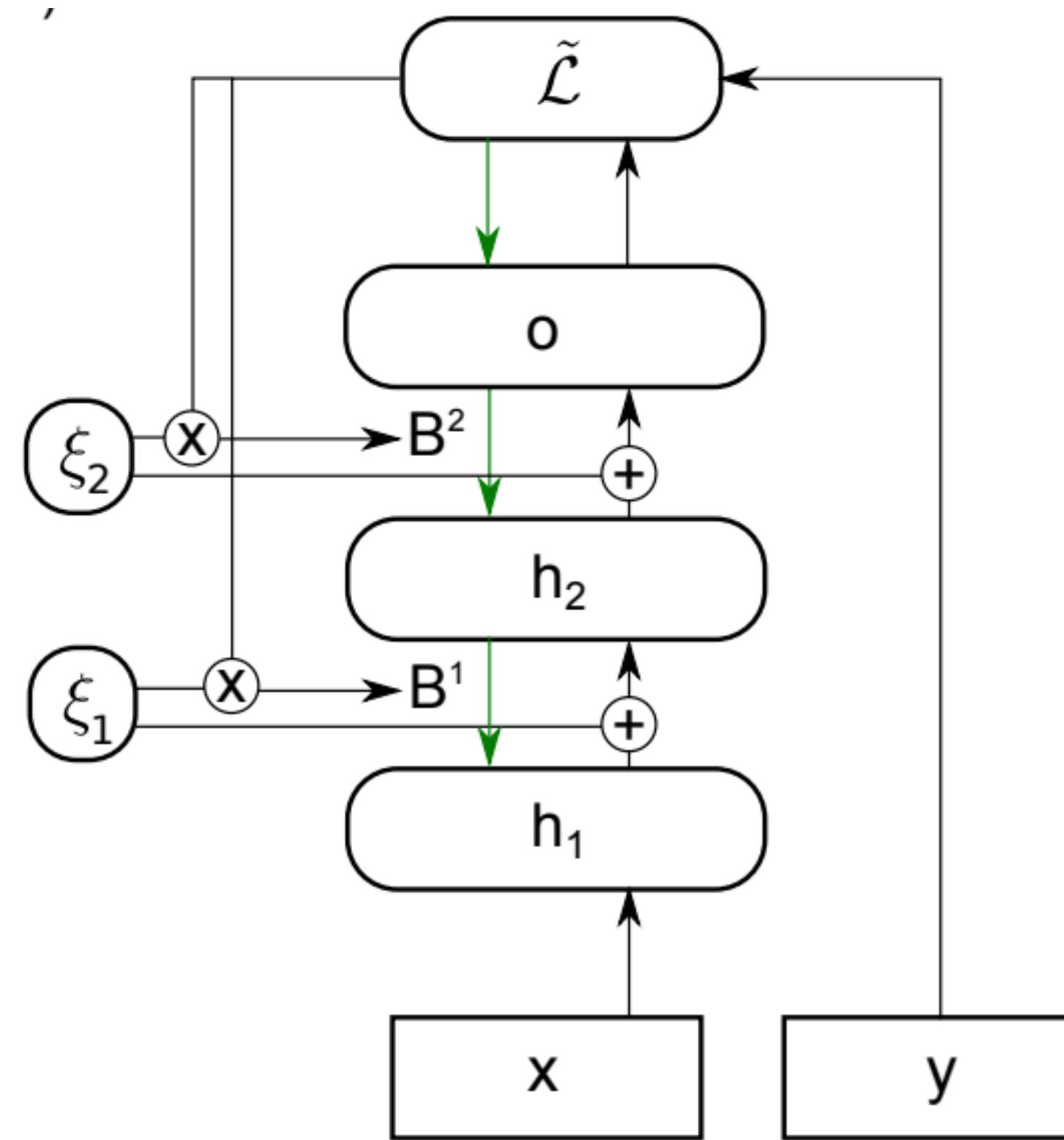


# Spiking MNIST



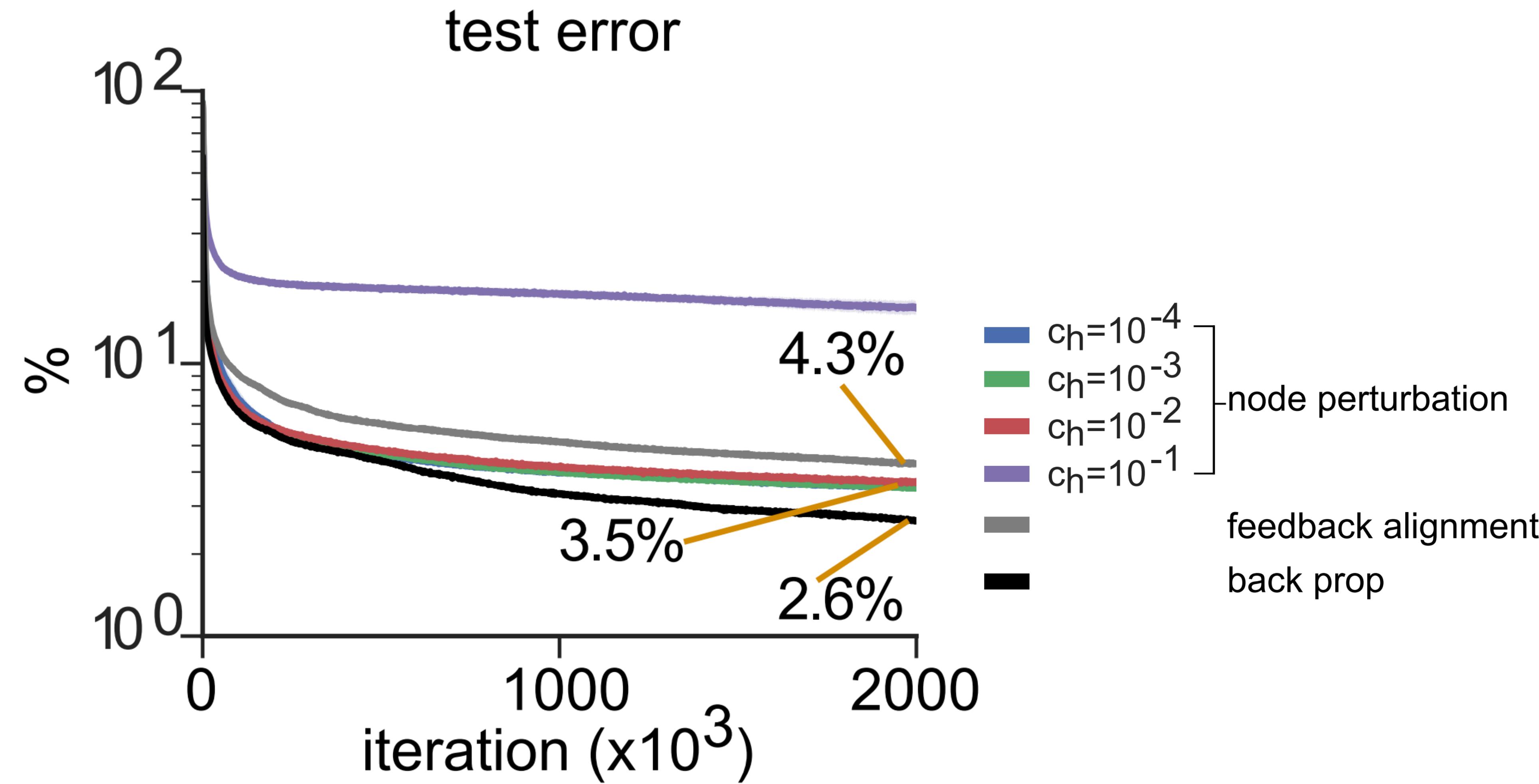
Samadi, Lillicrap, Tweed

# But then, why not improve the weights?



With Lansdell

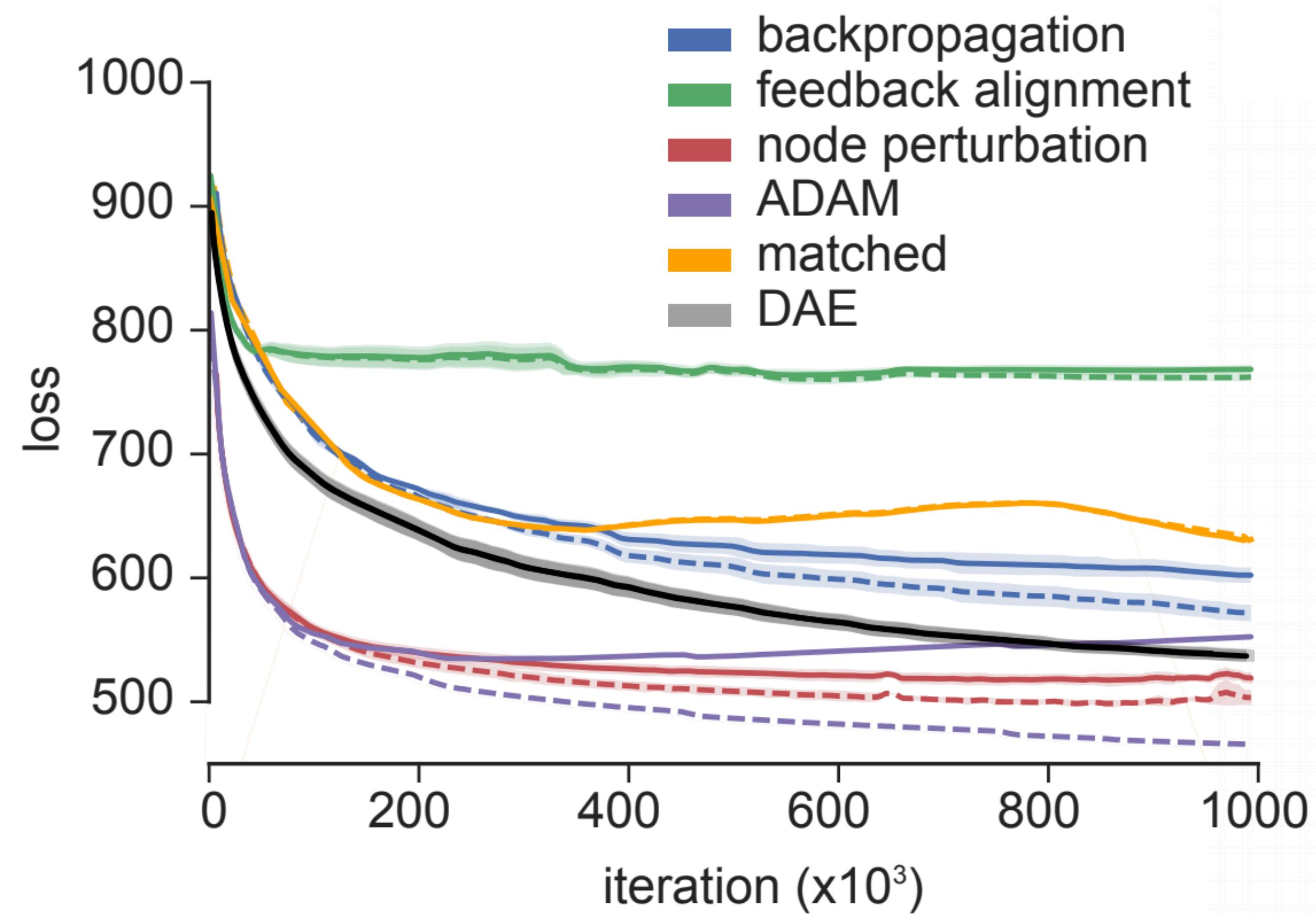
# Helps on MNIST



# MNIST autoencoder

	ADAM	backpropagation
output	2 9 6 9 9 1 9 9	2 8 3 6 9 7 0 5
input	2 4 3 4 9 1 4 5	2 2 3 6 4 7 0 2
	feedback alignment	node perturbation
output	7 3 5 1 9 0 8 2	8 2 7 5 1 2 4 7
input	3 8 8 4 9 6 1 6	5 2 7 8 1 2 0 9

# Helps a lot



# Also helps for nontrivial problems

dataset	backpropagation	node perturbation	DFA
CIFAR10	77	75	72
CIFAR100	51	48	47

# Proofs

- See paper for proofs
- for some cases we will converge to correct weights

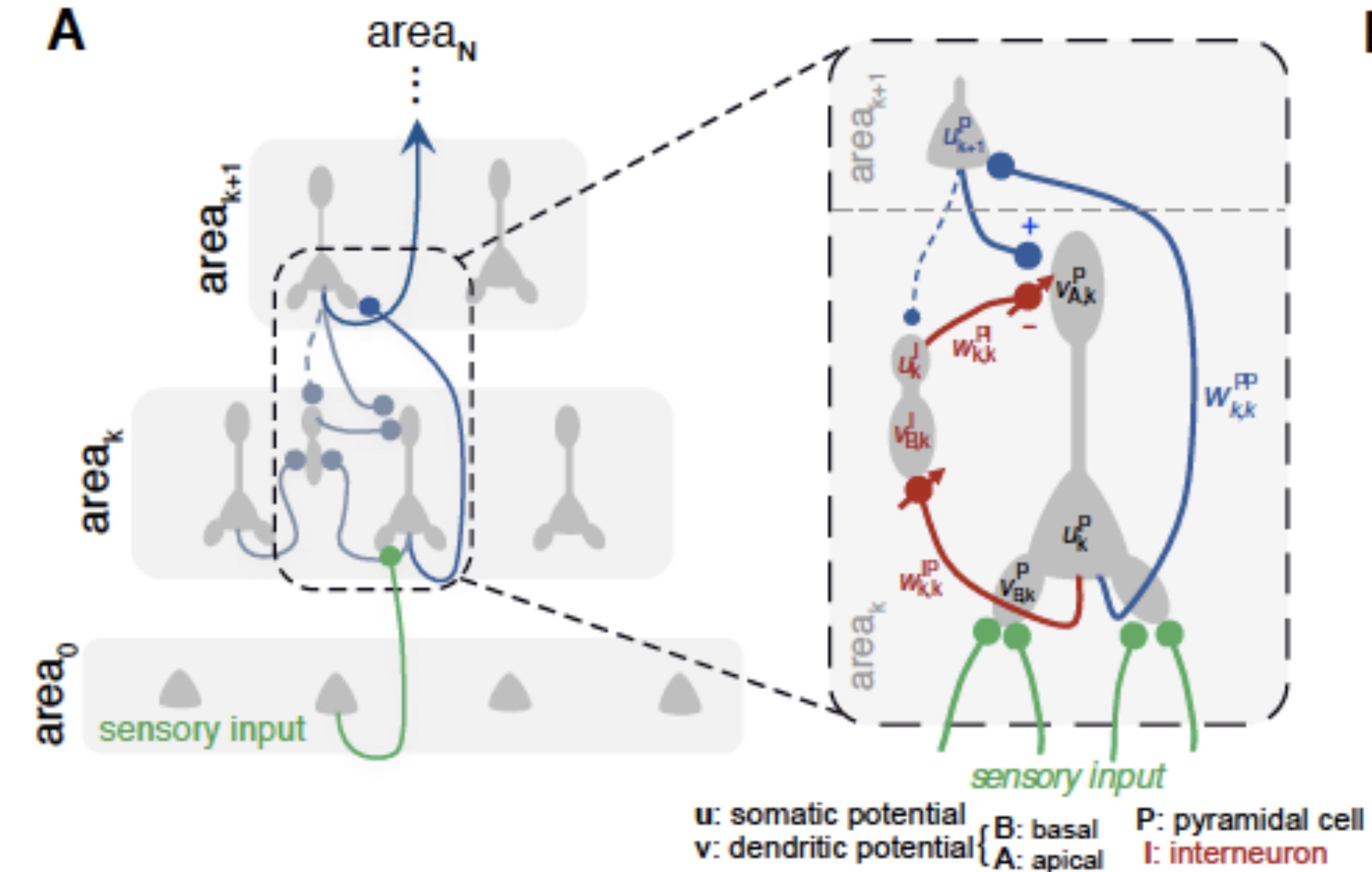
# Problem 2: Multiplexing

- Spikes are supposed to transmit the signals
- But then, how could they *\*also\** transmit the gradients
- “No-one has observed gradients being transmitted”

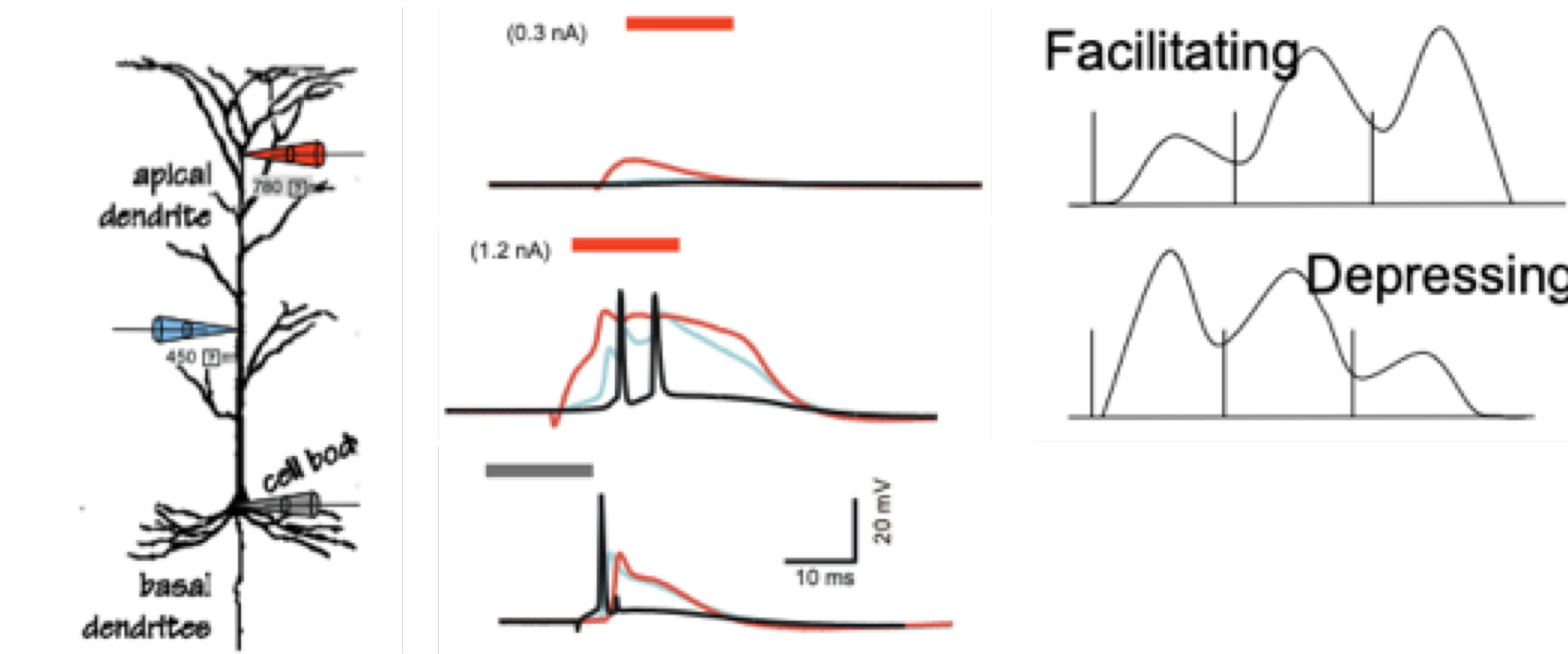
# Ideas

- Spikes vs Bursts
- Early vs Late
- Excitatory vs Inhibitory
- Metalearning

# e.g. Inhibition

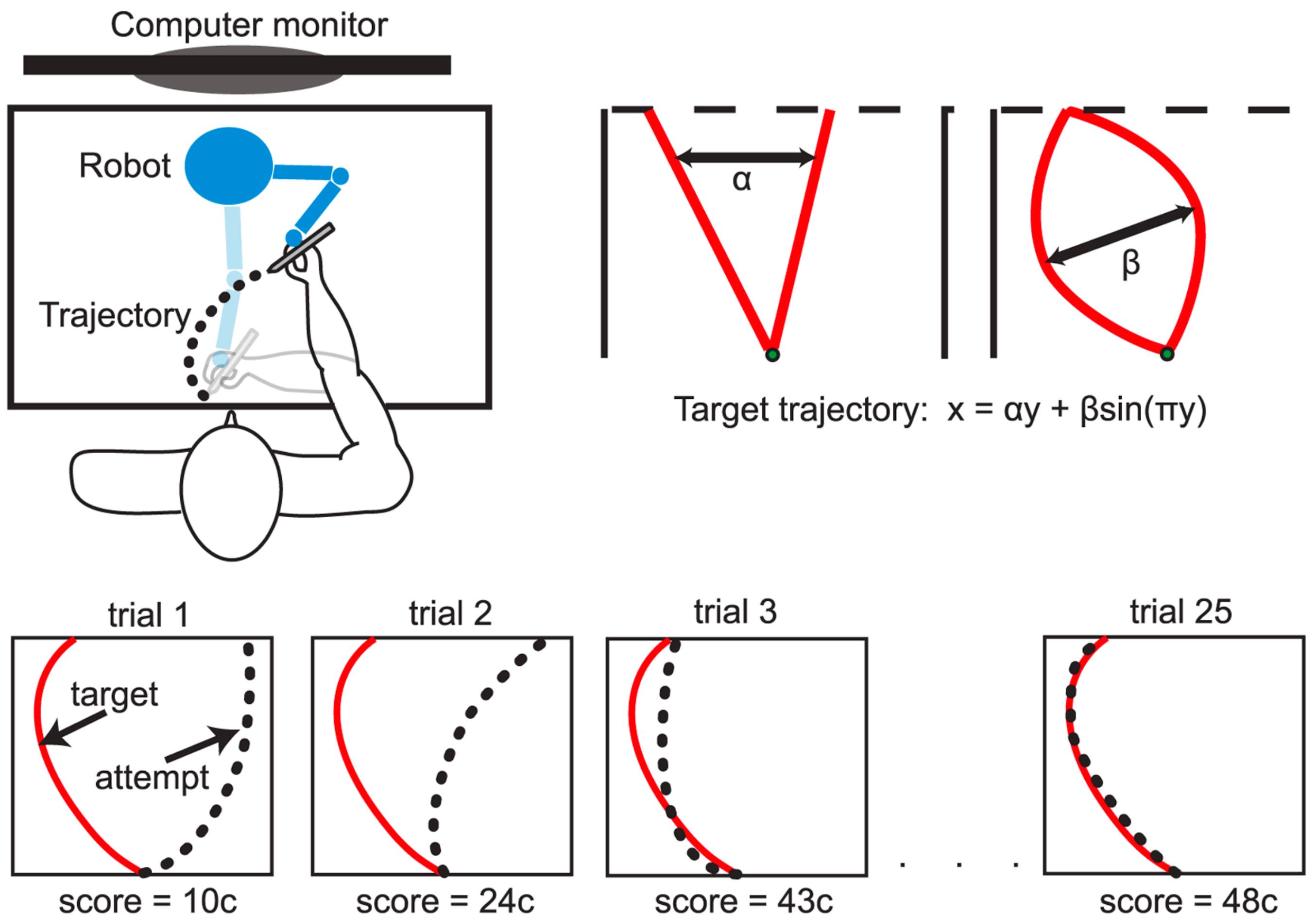


# e.g. Spikes vs Bursts

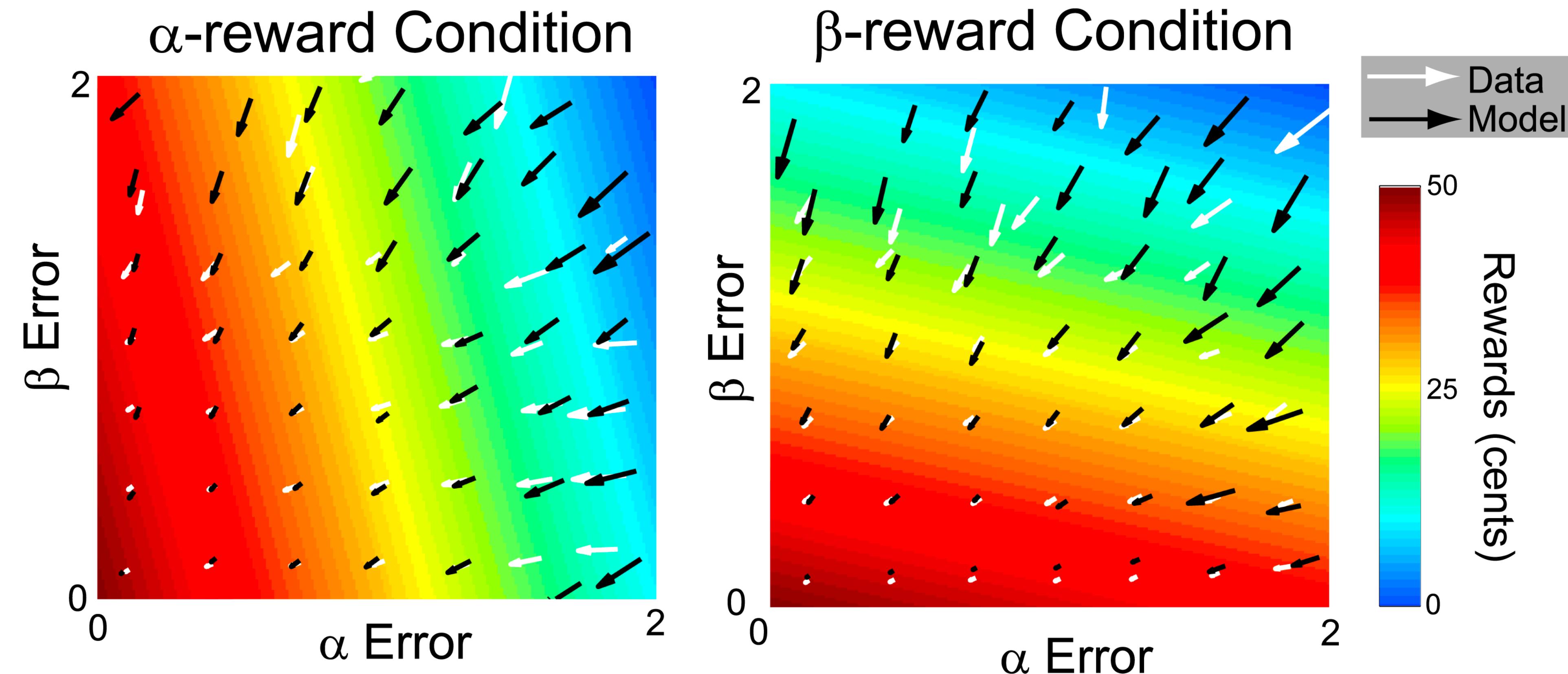


**e.g. Learning to learn**

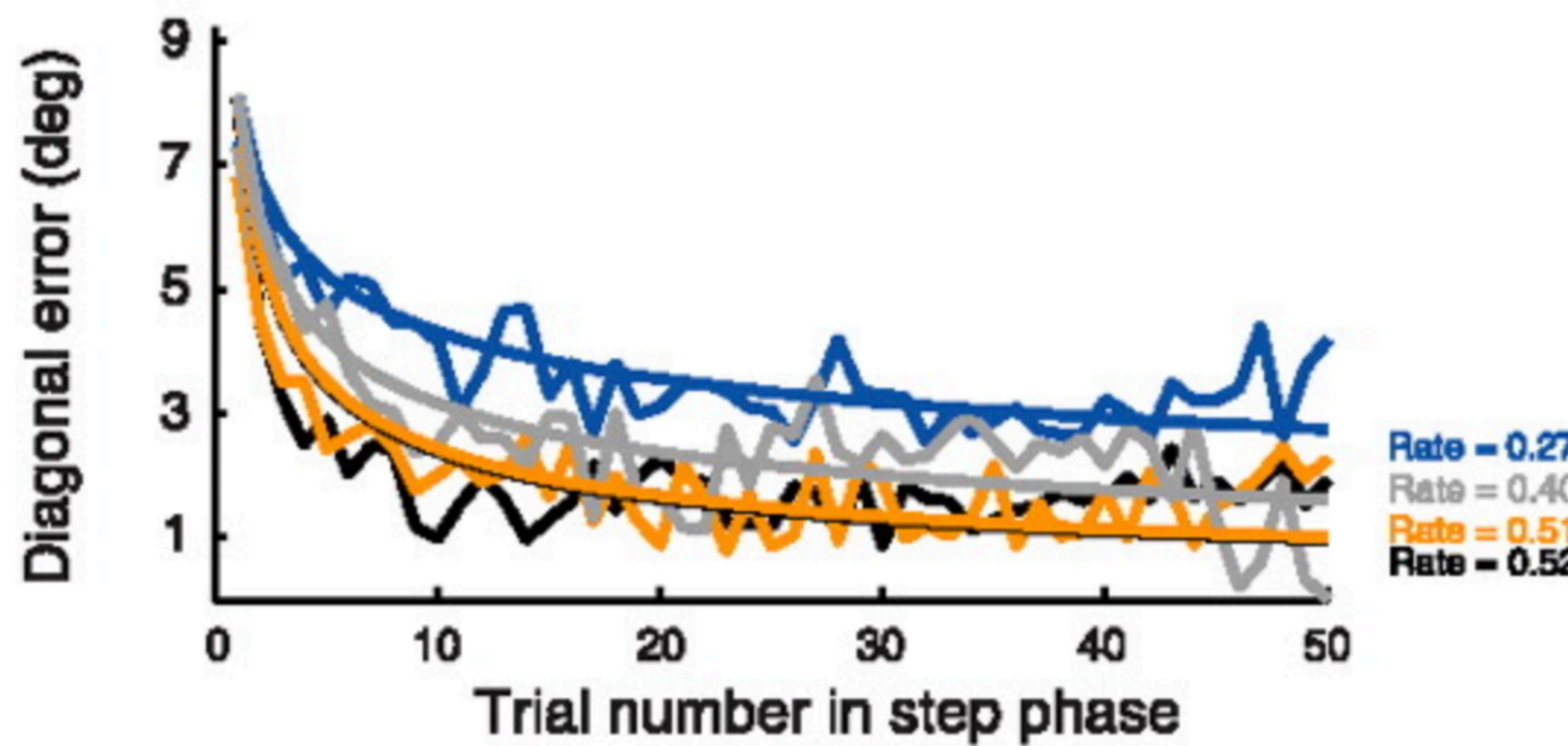
# People do it



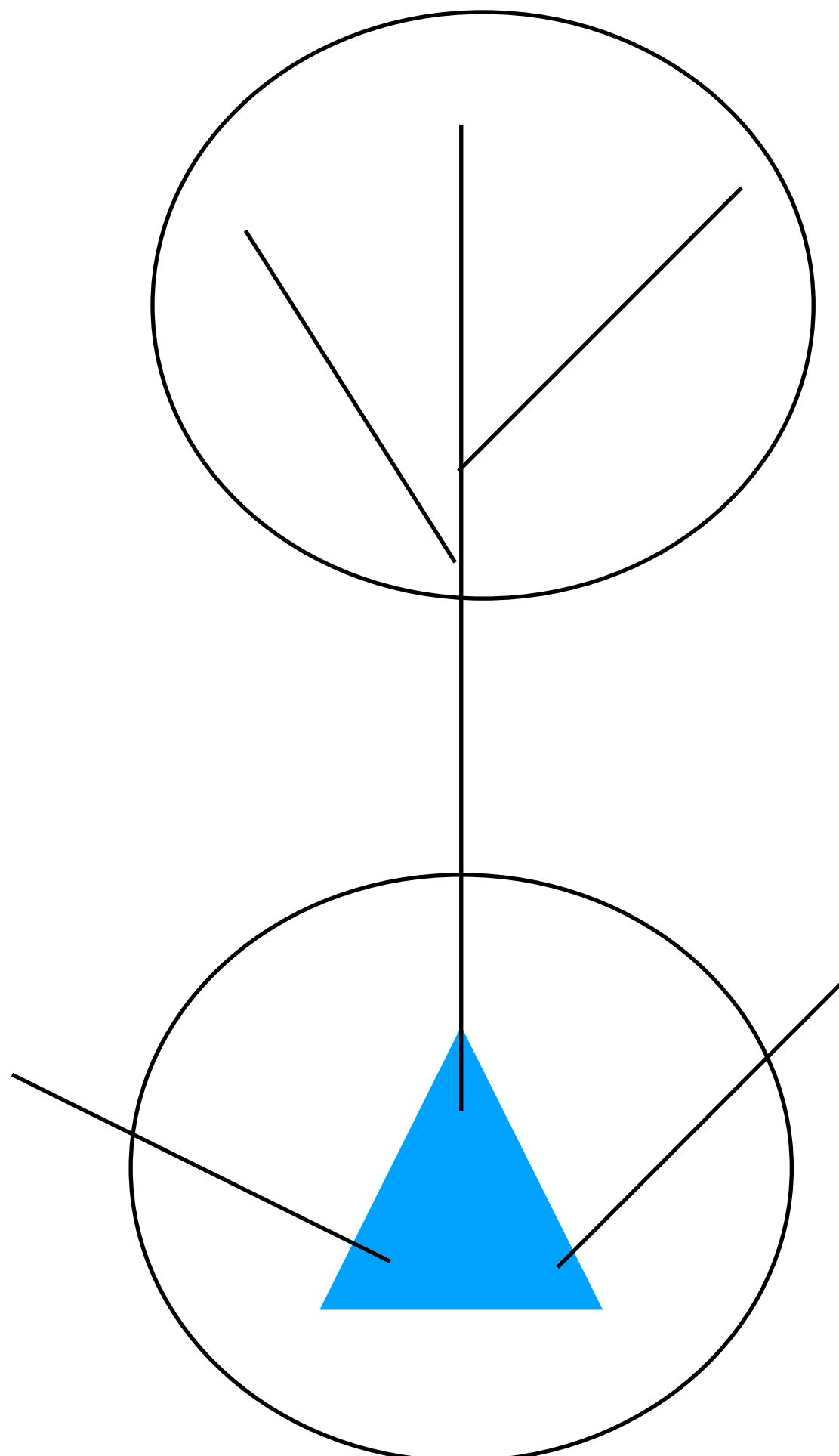
# Fast learning on axis that matters



# People do it: Learning to optimize



# Unspecific signals



**Teacher  
(needs access  
to truth)**

**Student**



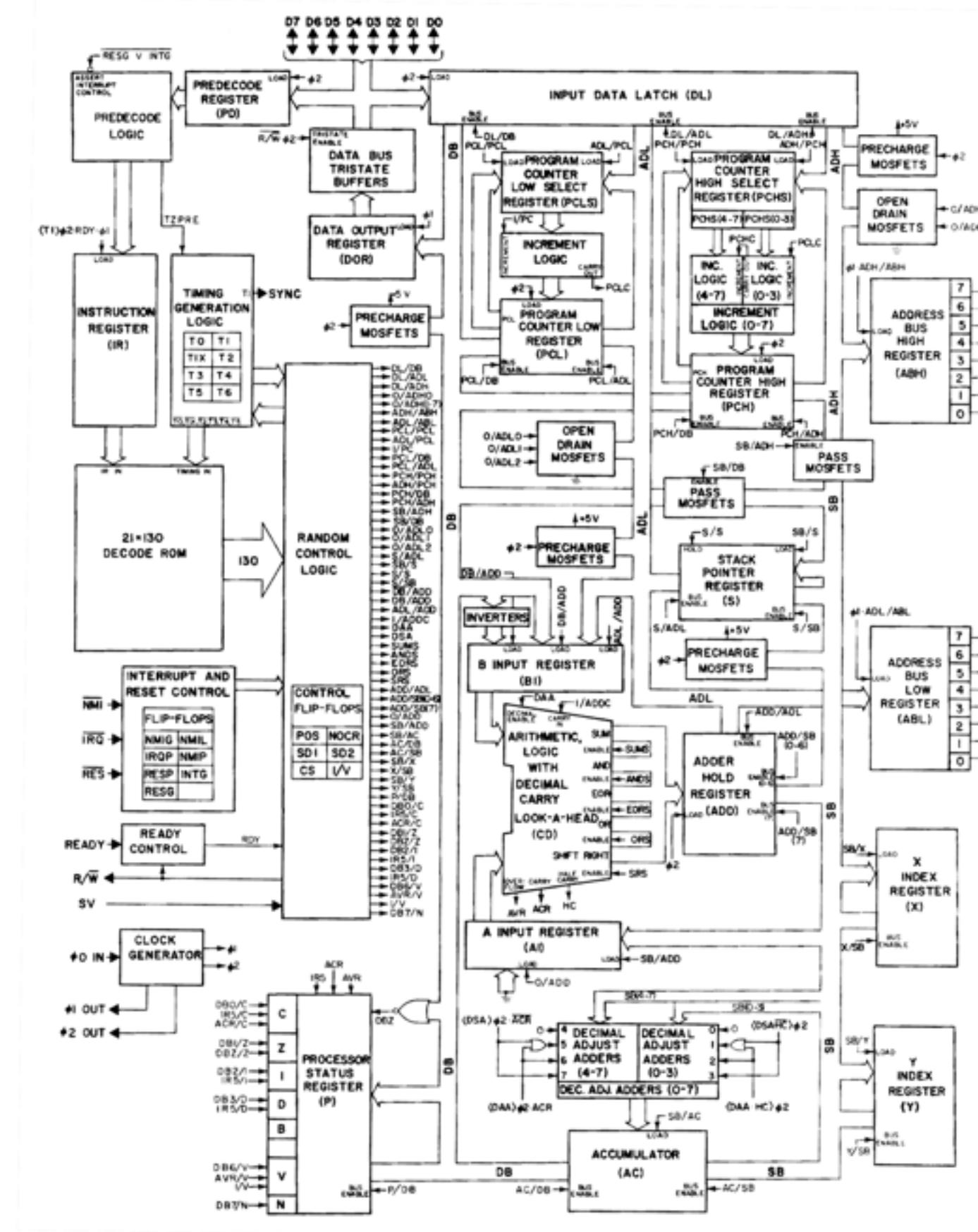
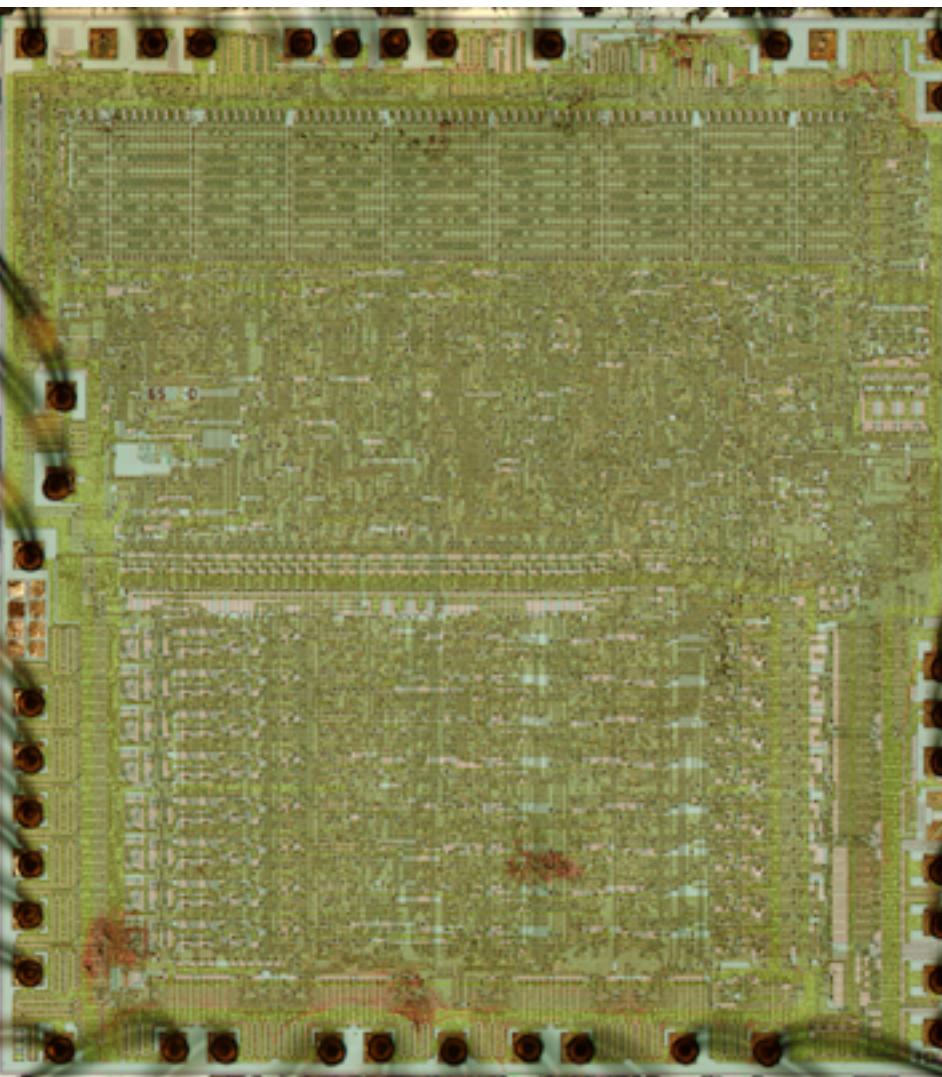
**Compare synthetic gradients**

# **III: Neuroscience is in a conceptual crisis**

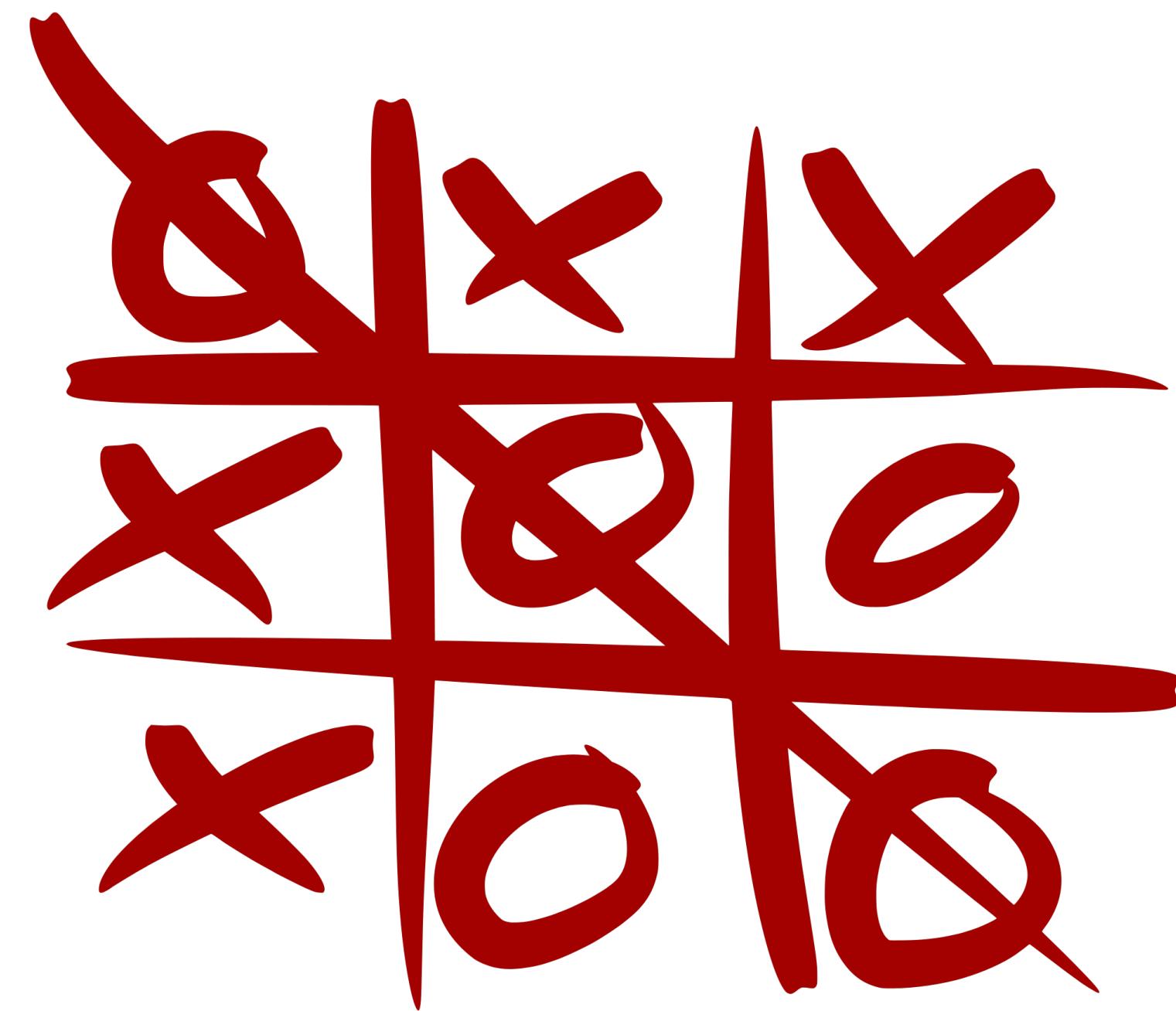
# Flavors of understanding

- Know some truths about it
- Fix it
- Simulate it
- Understand how it works

# Microprocessor as a model

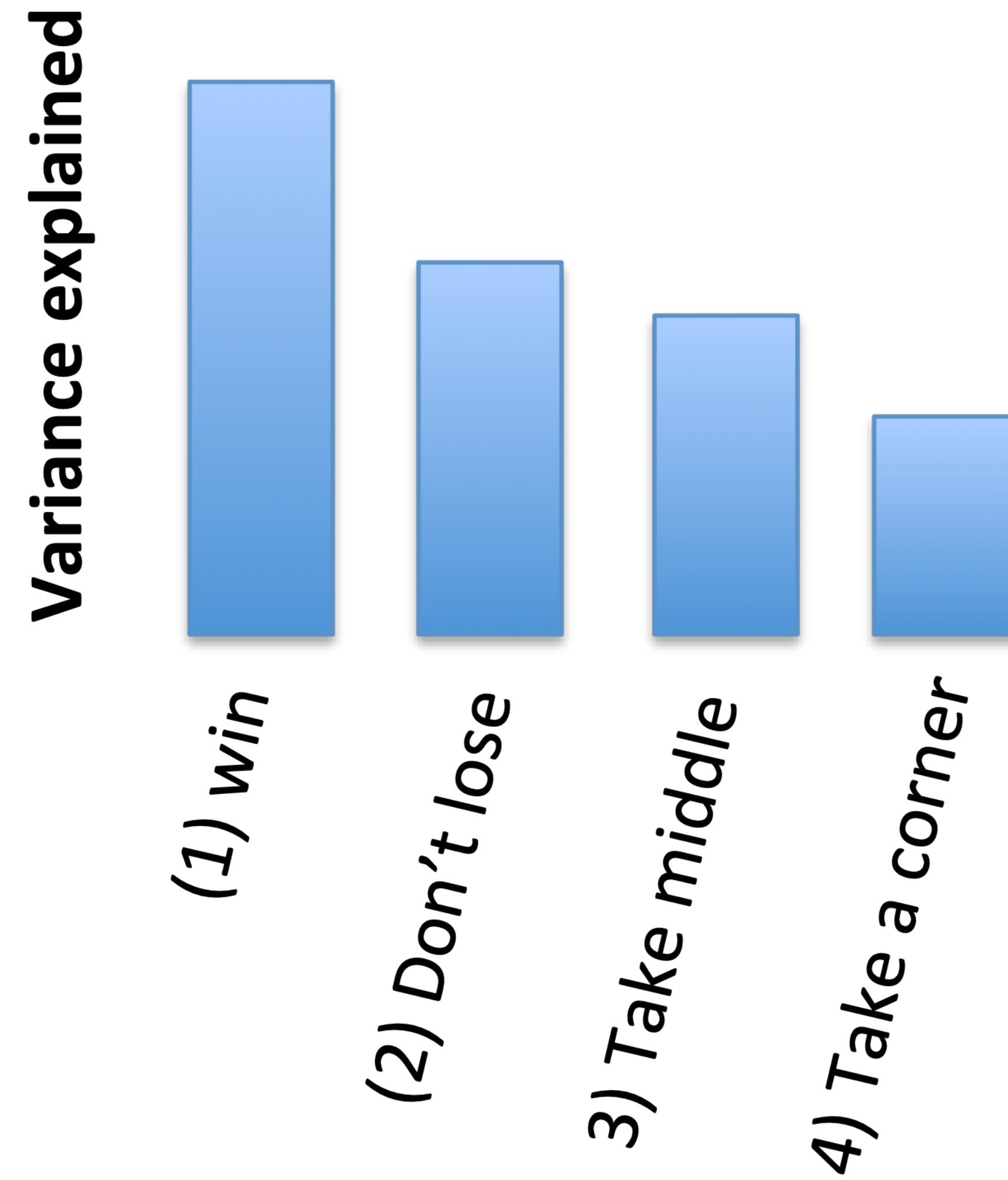


# Tic Tac Toe



255,168 distinct games!

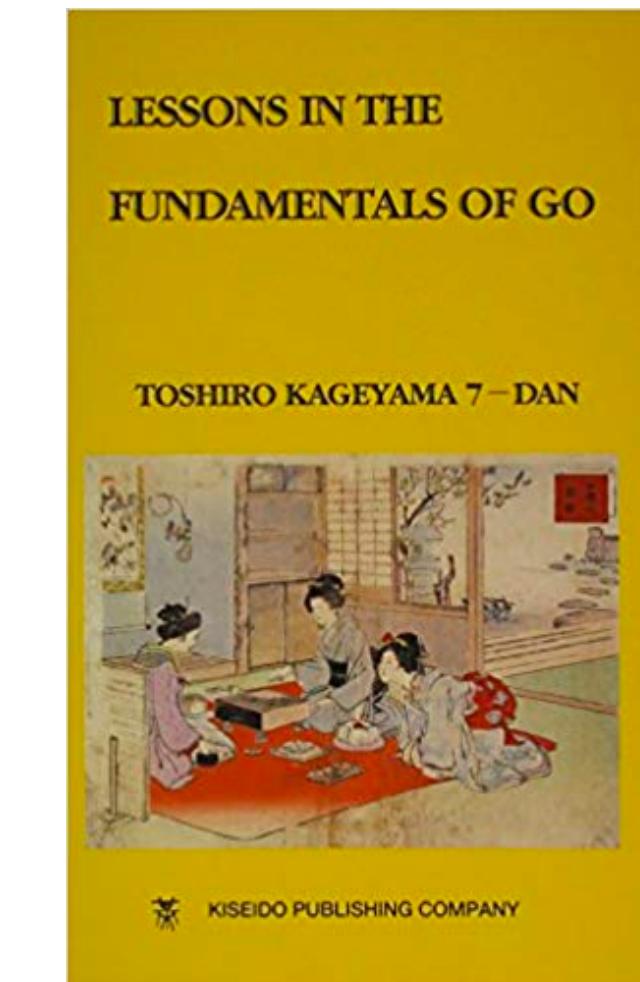
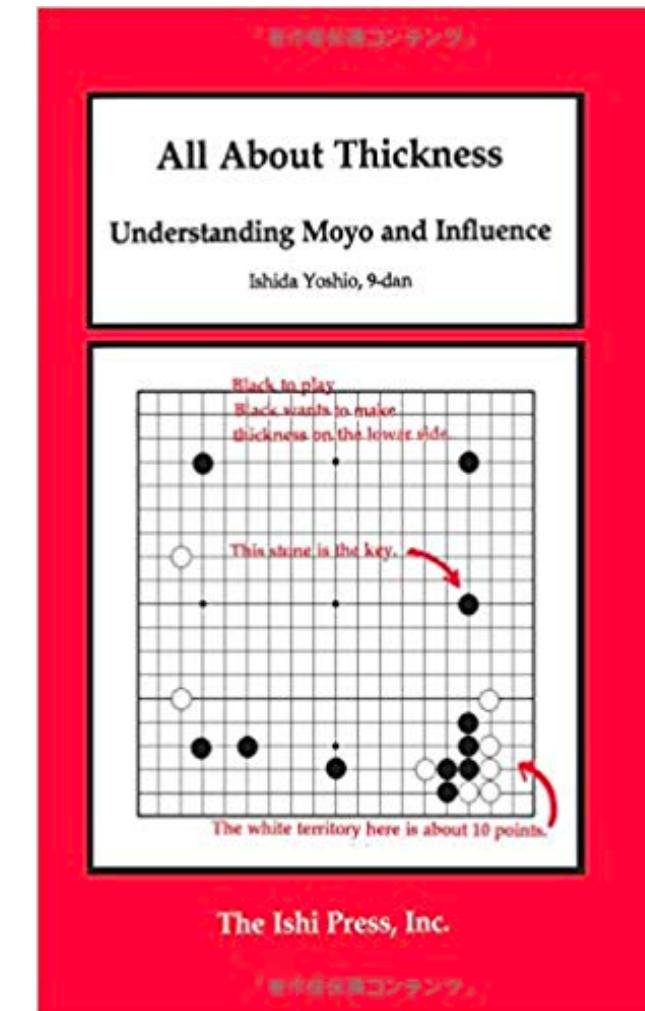
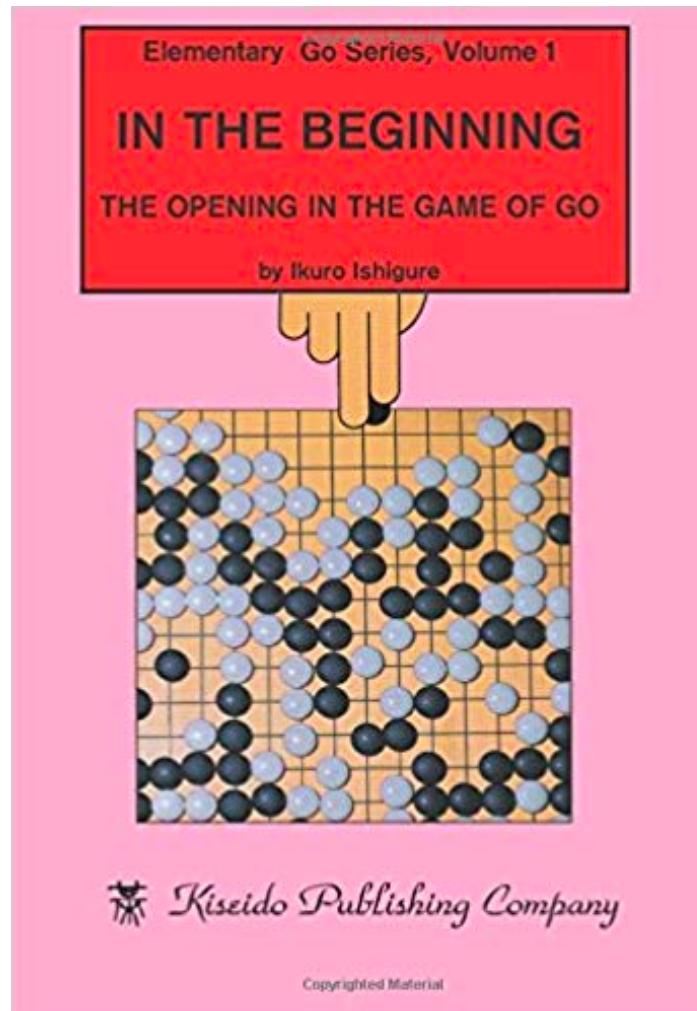
# Compressable



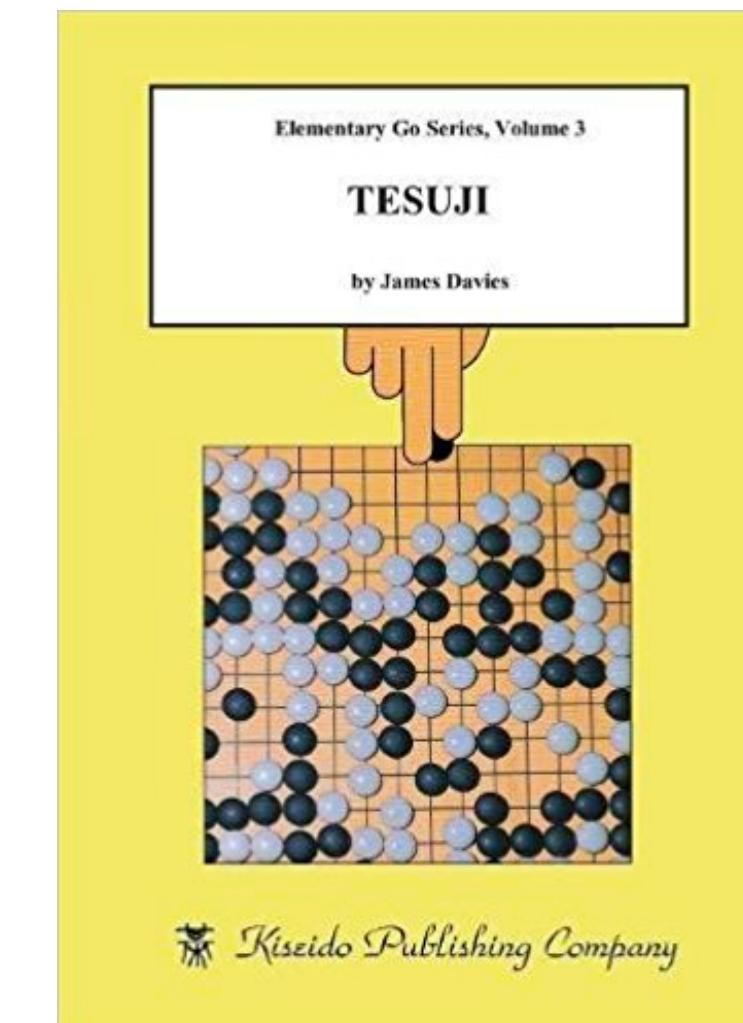
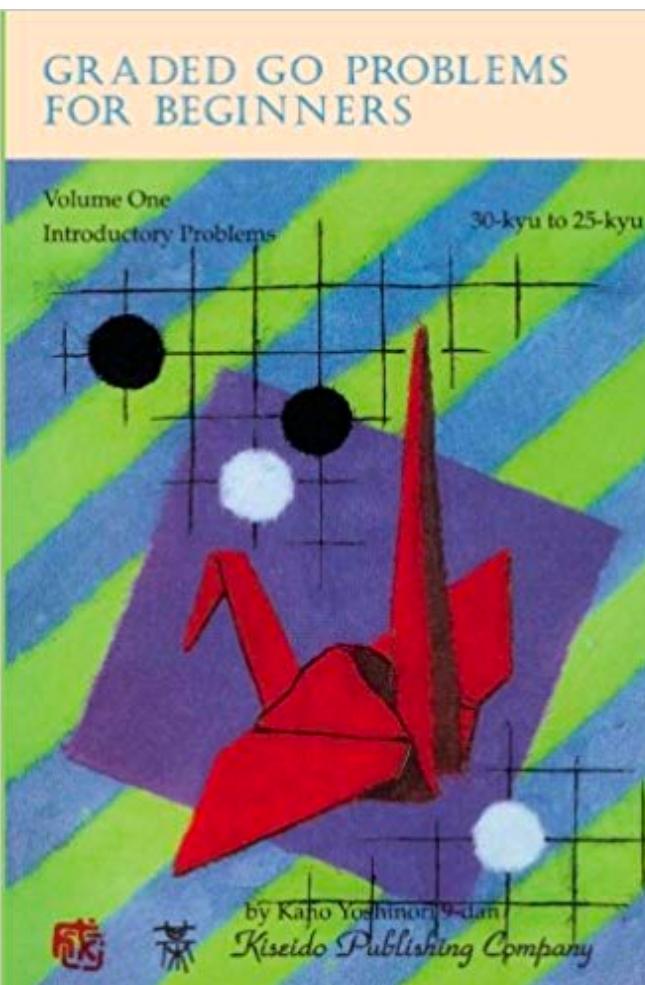
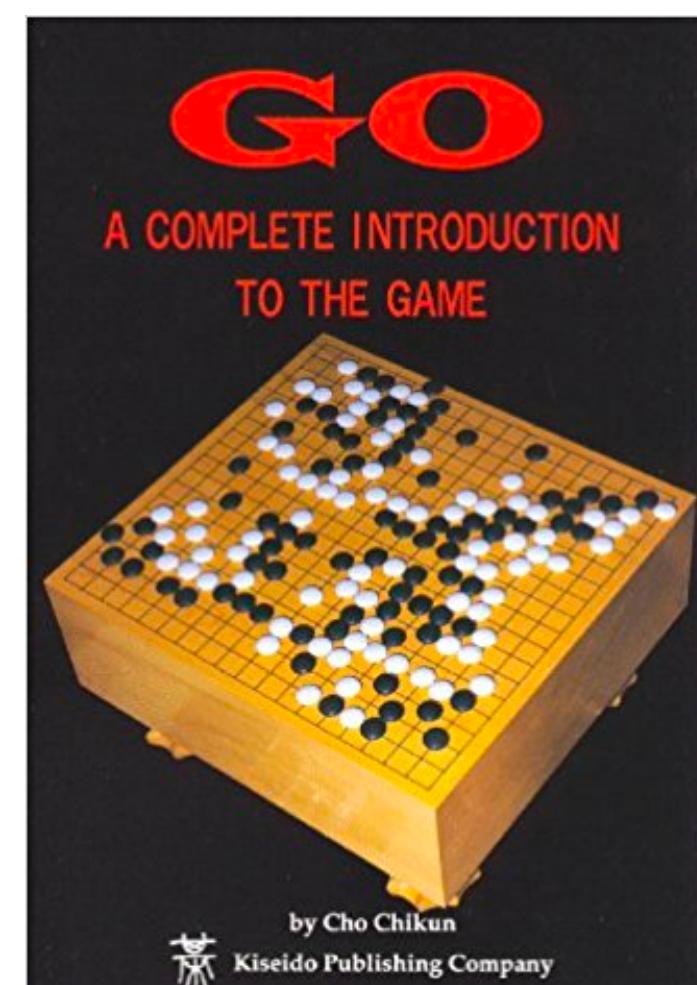
# Go

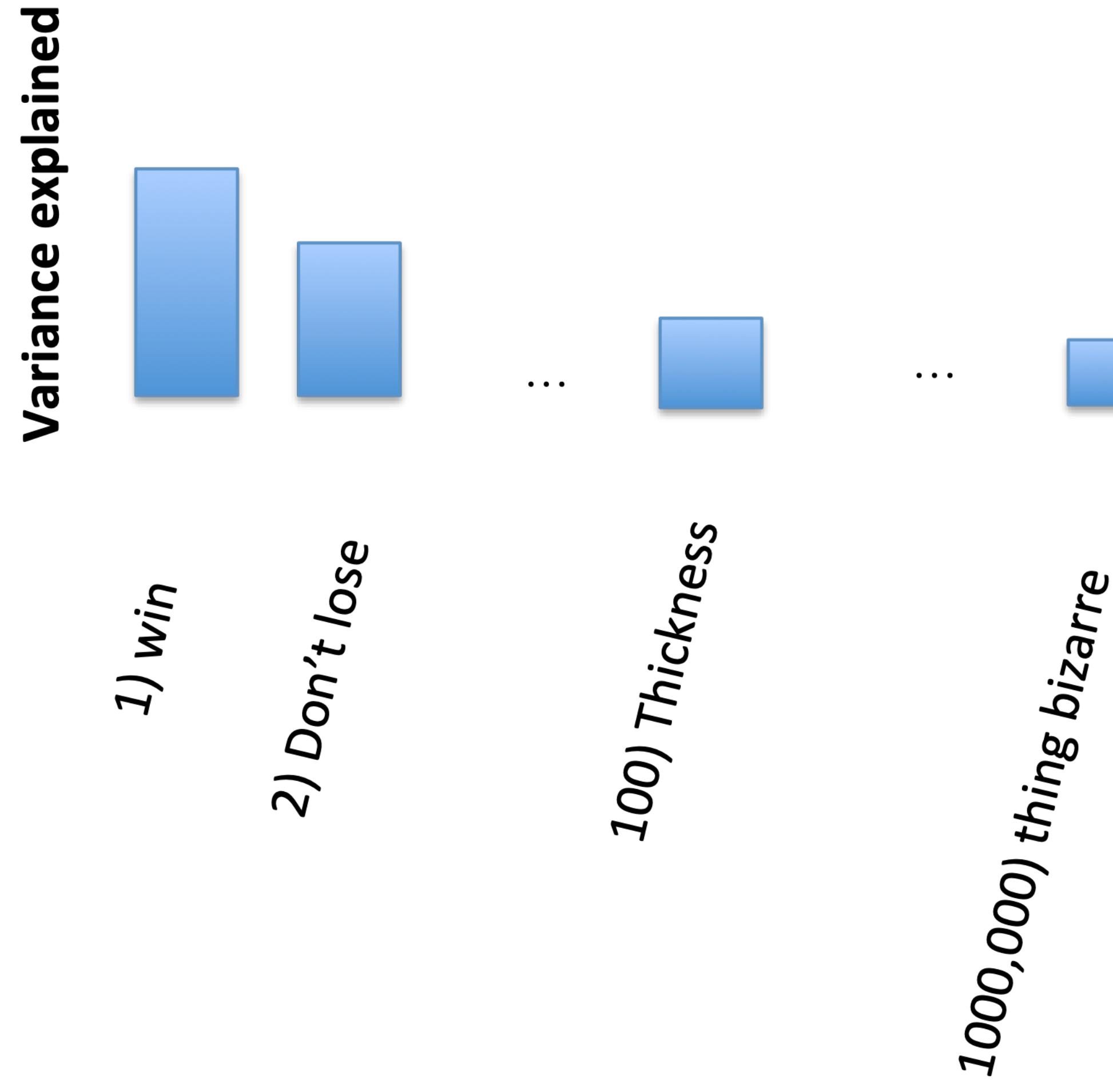


# Probably no way to compactly describe it



■ ■ ■





**They are all real. Replicable from Go grand master to Go grandmaster.**

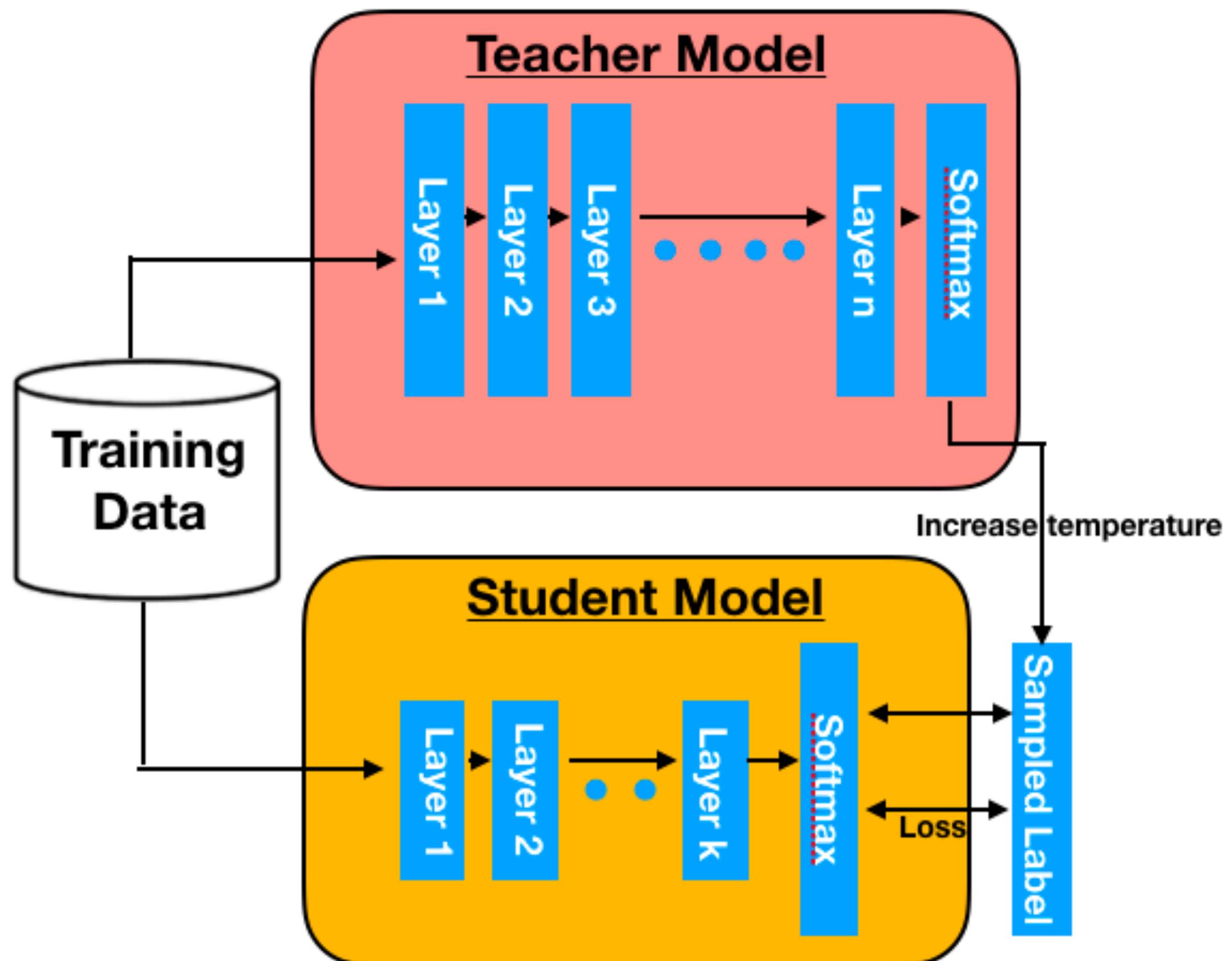
# Understand a neural network

- Pytorch code
- Vs the Weight dump

# Kolmogorov complexity of brain like computations

- Distillation
- Complexity calculations
- Back of the envelope calculations

# Distillation



from  
mc.ai

Factor 10-100 on MNIST, imagenet

e.g. Ba and Caruana, Zhu et al 2018

# Can we compress NNs?

- MNIST -> soft decision trees
  - BAD
- imagenet

# Back of the envelope

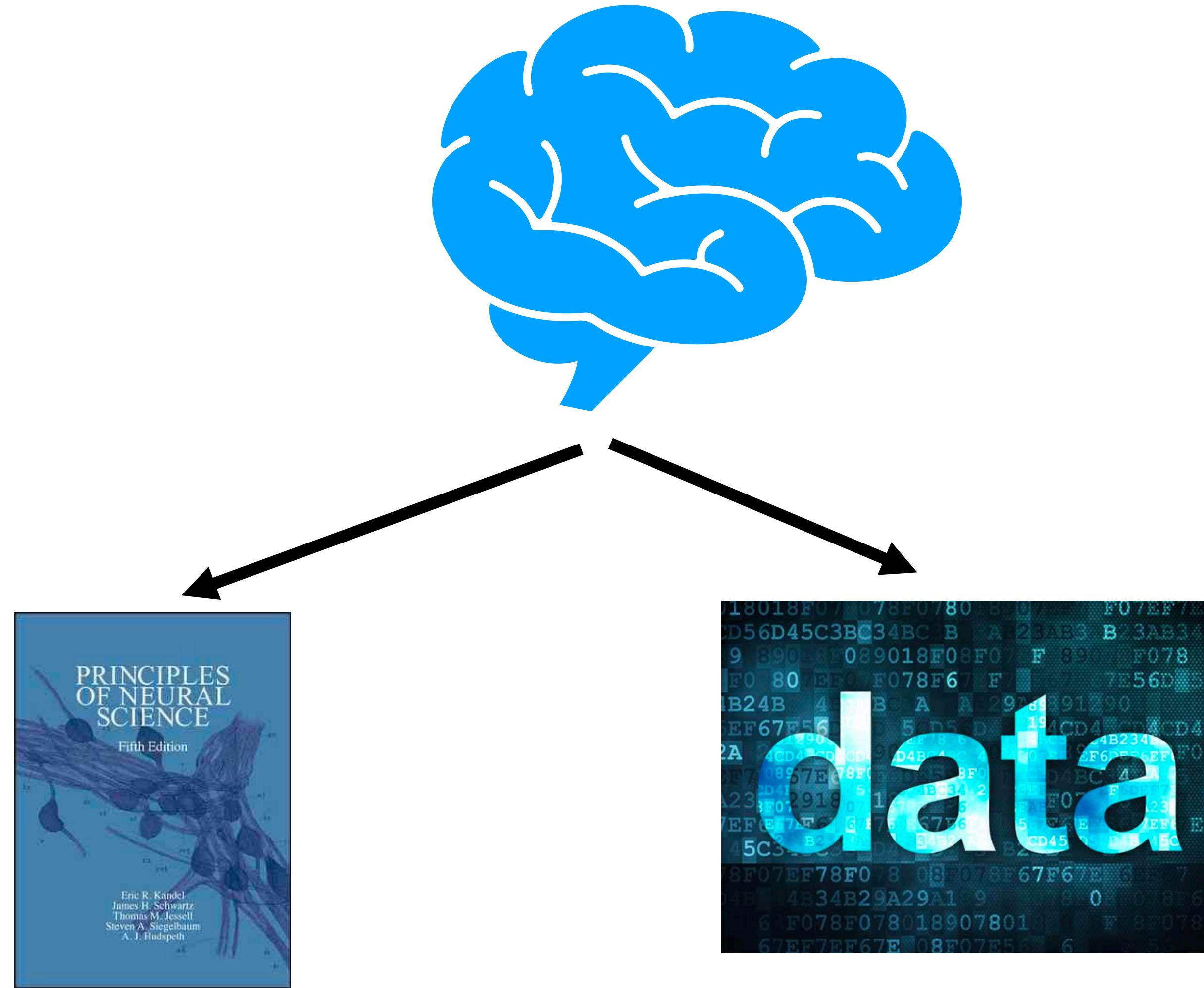
## human

- 10 bits/s
  - $\pi \times 10^7$  seconds/a
  - 30 years
- 
- $10^{10}$  bits
  - $10^6$  bits/book ->  $10^4$  books

# $H(DNA) \ll H(World)$

- DNA:  $2^*3^*10^9$  nucleotides
  - mostly non-nervous system
  - of nervous system possibly much non-computational
  - very non-compressed
- Nurture >> Nature

# Ok. So what if the brain is not compressible?

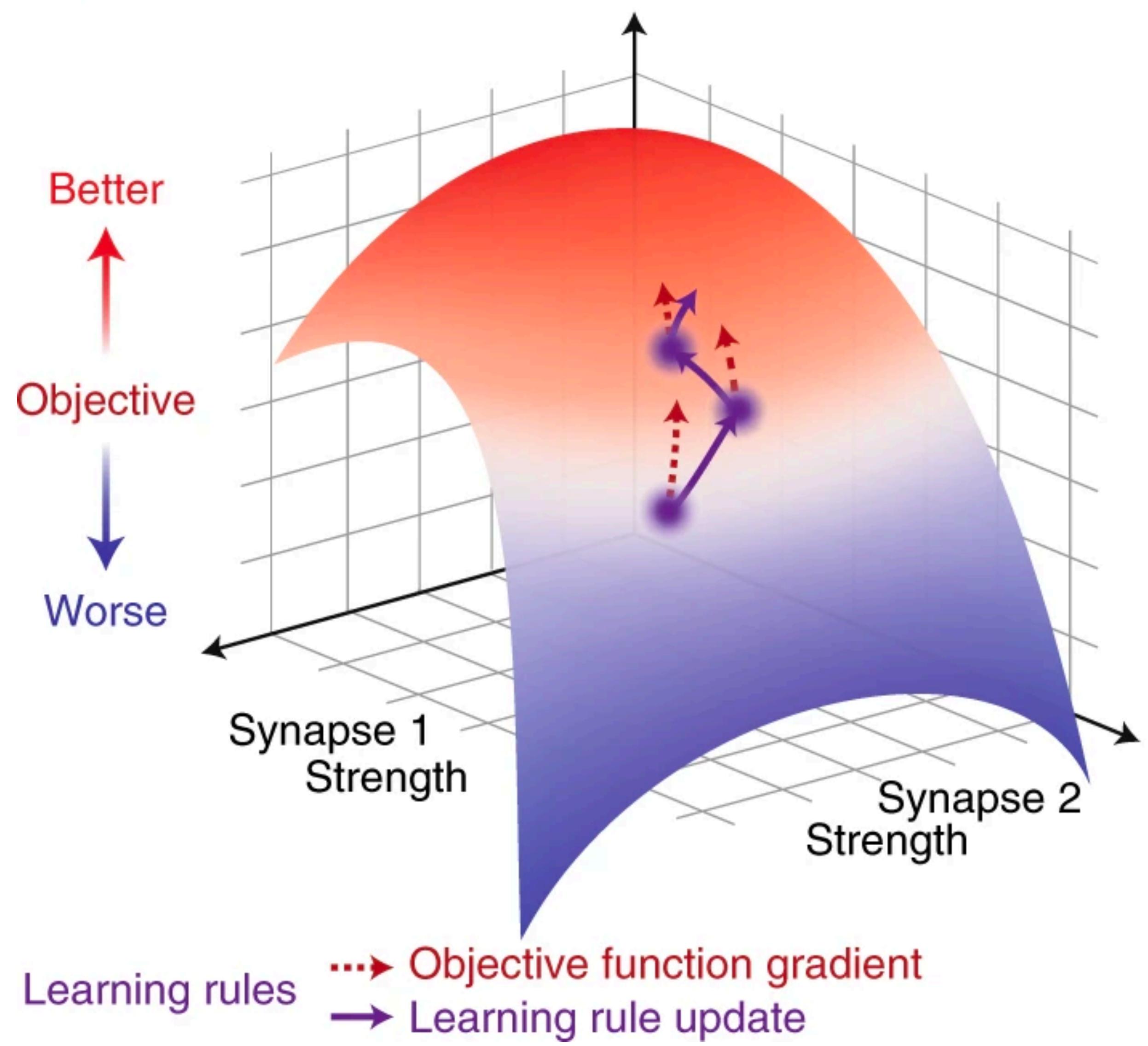


# Argument in a nutshell

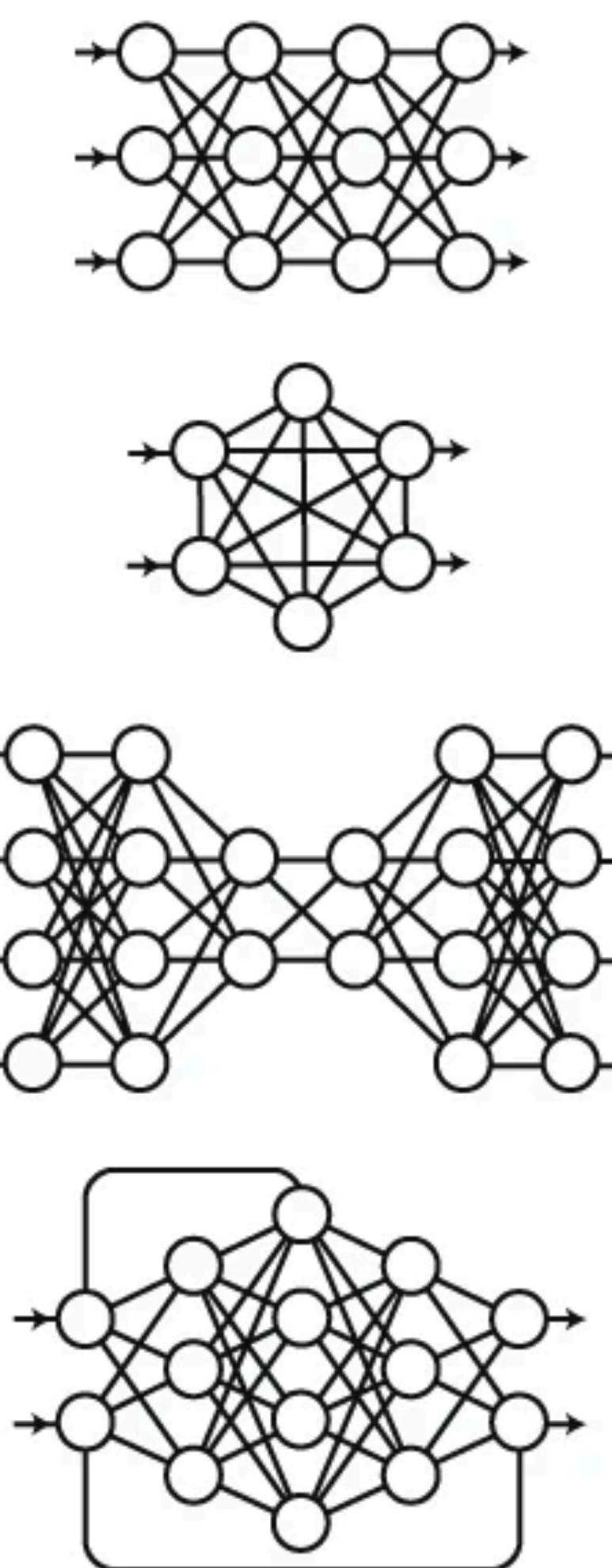
- Pytorch code to make an ANN is easy for us to understand
- Resulting network is (probably) impossible to understand
- So lets do the analogue of the first in neuroscience

**So how may neuroscience  
have to look like?**

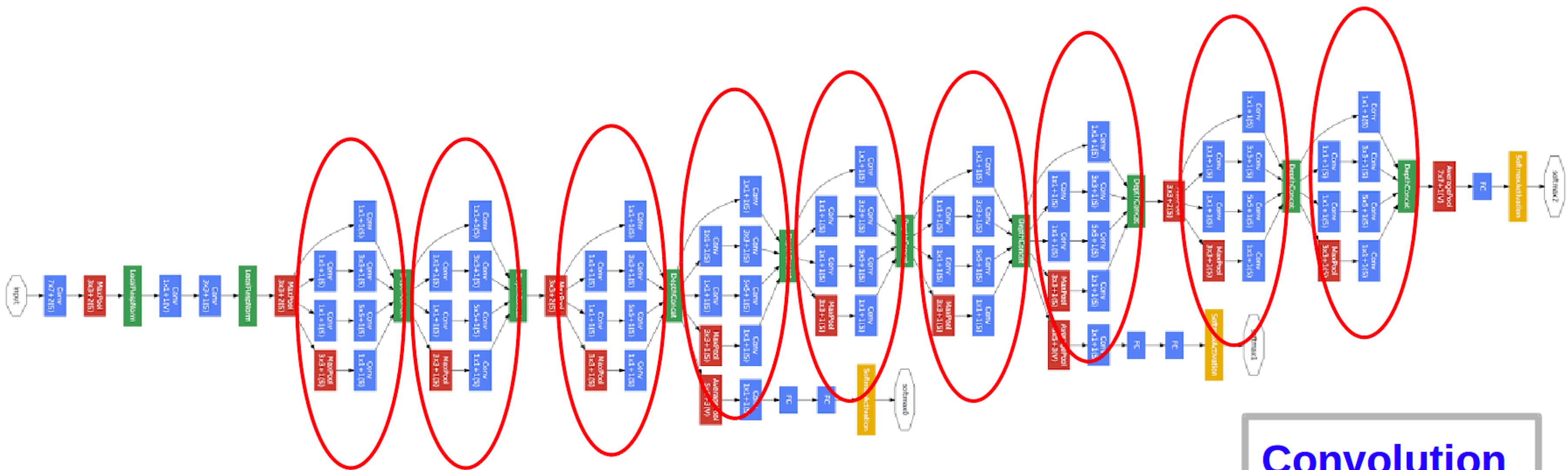
## Objective functions



## Architectures



# Anatomy (Googlenet)

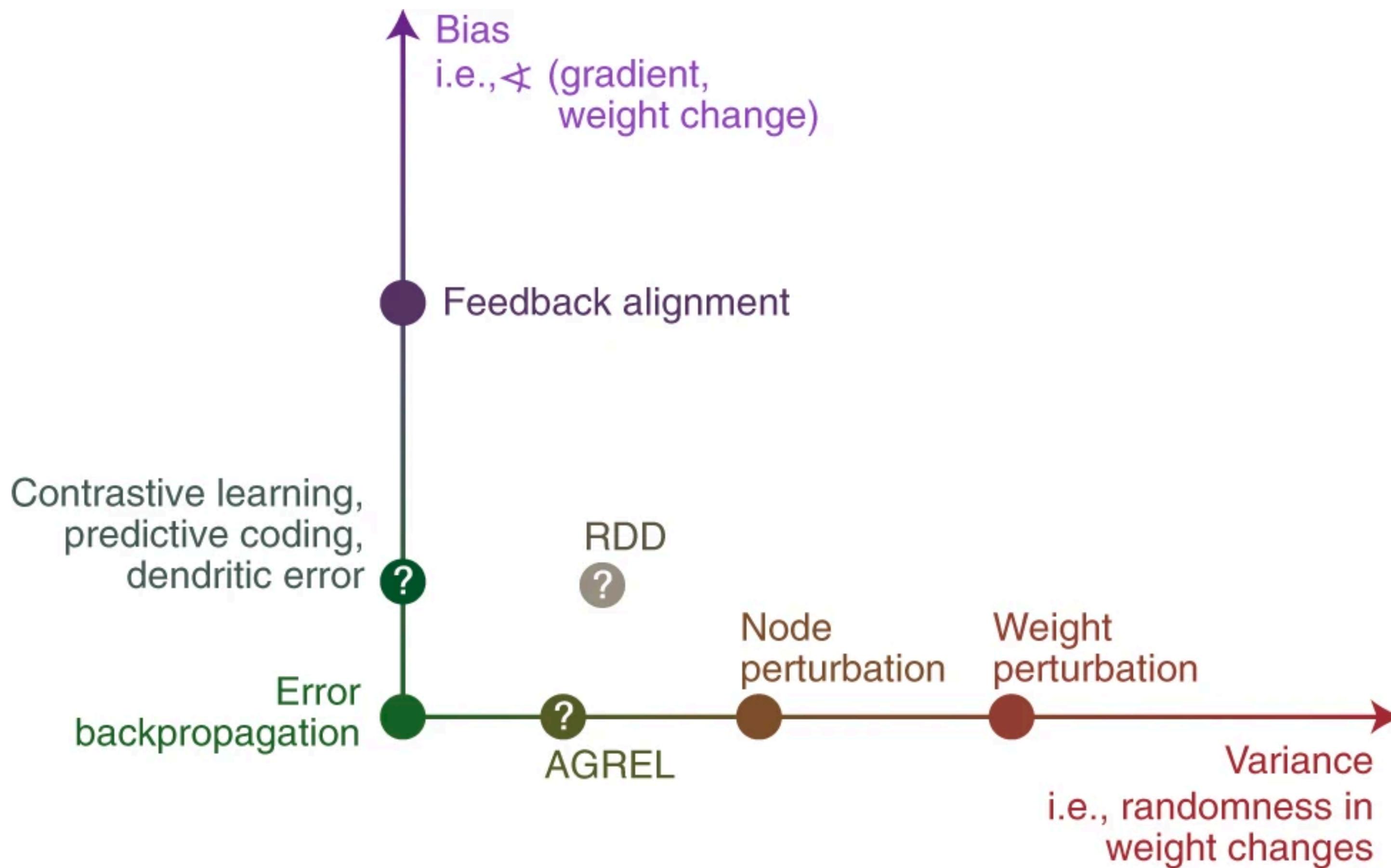


**Convolution**  
**Pooling**  
**Softmax**  
**Concat/Normalize**

# Objective function (softmax)

$$P(y = j \mid \mathbf{x}) = \frac{e^{\mathbf{x}^\top \mathbf{w}_j}}{\sum_{k=1}^K e^{\mathbf{x}^\top \mathbf{w}_k}}$$

# We need computational ideas!



# Summary

- Timely to think about DL as a model of the brain
- Weight transport is one problem
- Another problem is multiplexing
- And variance is always an issue
- DL may bring a new hope to neuroscience

# Last lecture, let us look back!

- This was a great experience for me
- I learned a great deal
- We have outstanding TAs
- Sadat was an amazing lead TA
- I hope you are and stay well