

$$n = 5$$

$$5! = \overline{5} \times \overline{4} \times \overline{3} \times \overline{2} \times \overline{1} = 1 \times 2 \times 3 \times 4 \times 5$$

$\text{fact} = 1$

$$\text{fact} = 0$$

loop $\{ 1 \text{ to } 5$

$$\text{fact} = 1 \times 1$$

for ($i=1$; $i \leq n$; $i++$)

$i \leq 5$

$\text{fact} = \text{fact} * i$; $\text{fact} = 1$

$$i = 1$$

$$\text{fact} = 0$$

$$0 \times 1$$

2nd time {

$$i = 2$$

$$\text{fact} = \text{fact} * i$$

$$\text{fact} = 0 \times 2 = 0$$

$$\text{fact} = 1 \times 2 = 2$$

$$\text{factorial}(5) = \underline{5 \times 4 \times 3 \times 2 \times 1}$$

$$\text{fact}(4) = \underline{4 \times 3 \times 2 \times 1}$$

$$\text{fact}(3) = \underline{3 \times 2 \times 1}$$

$$\text{fact}(2) = \underline{2 \times 1}$$

$$\text{fact}(1) = 1$$

$$\text{fact}(0) = 1$$

$$\text{fact}(6) = 6 \times \text{fact}(5)$$

$$= \underline{6 \times 5 \times 4 \times 3 \times 2 \times 1}$$

$$6 \times \underline{\text{fact}(5)}$$

$$n = 6$$

$$\underline{\underline{\text{fact}(n) = n \times \text{fact}(n-1);}}$$

$$\underline{\text{fact}(6)} = \underline{6 \times \underline{\text{fact}(5)}};$$

$$\text{fact}(5) = \underline{5 \times \text{fact}(4)}$$

fact(6) {

return 6 * fact(5)

fact(6)

└ 6 * fact(5)

└ 5 * fact(4)

└ 4 * (fact(3))

└ 3 * fact(2)

└ 2 * fact(1)

└ 1 * fact(0)

fact(0) = 1

f(5) 5 * 24 = 120

└ f(4) 4 * 6 = 24

└ f(3) 3 * 2 = 6

└ f(2) 2 * 1 = 2

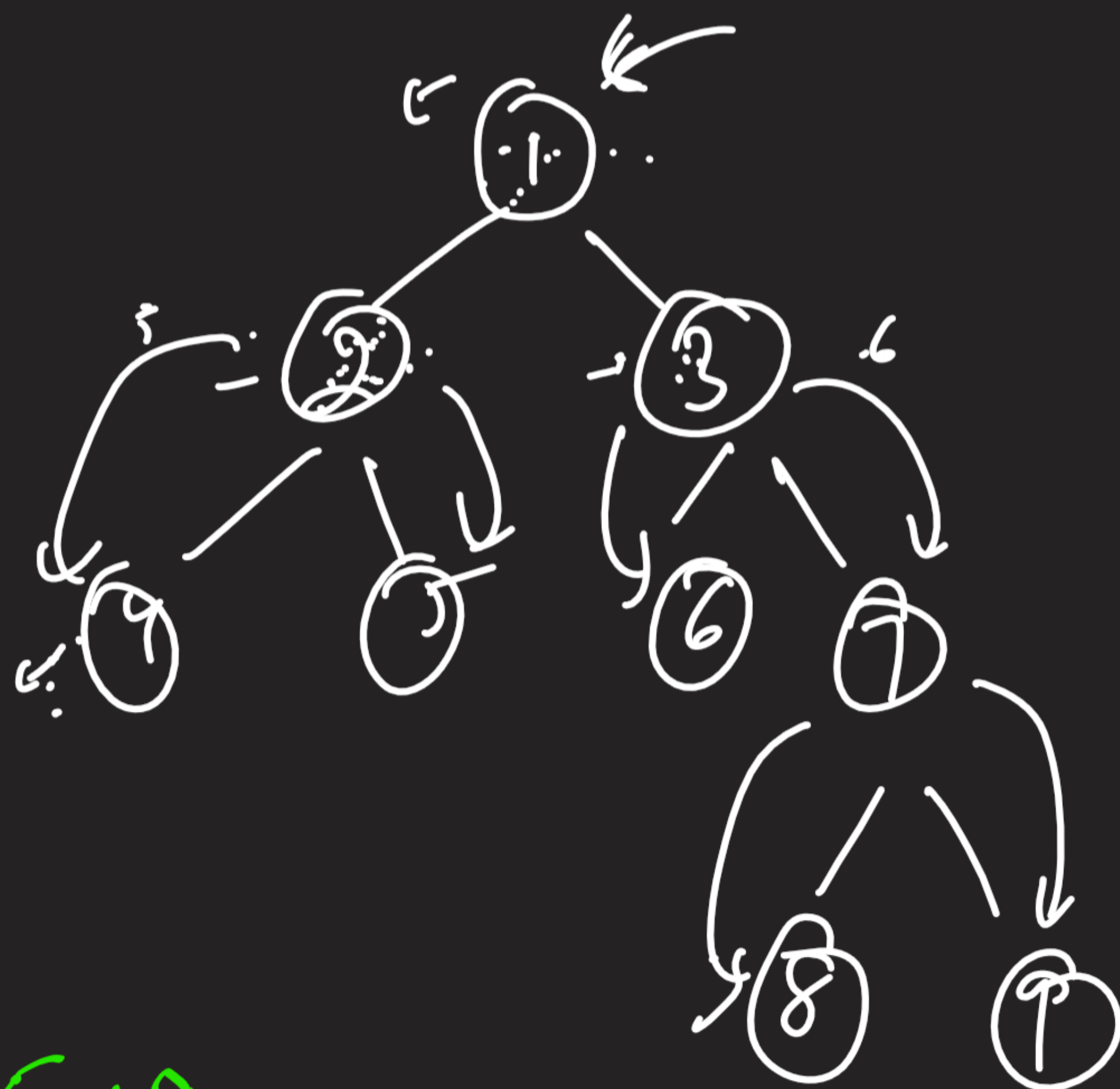
└ f(1) 1 * 1 = 1

└ f(0) 1 * fact(0)

1 * fact(0)

└ 0 * fact(-1)

└ -1 * fact(-2)



fib(0) = 0

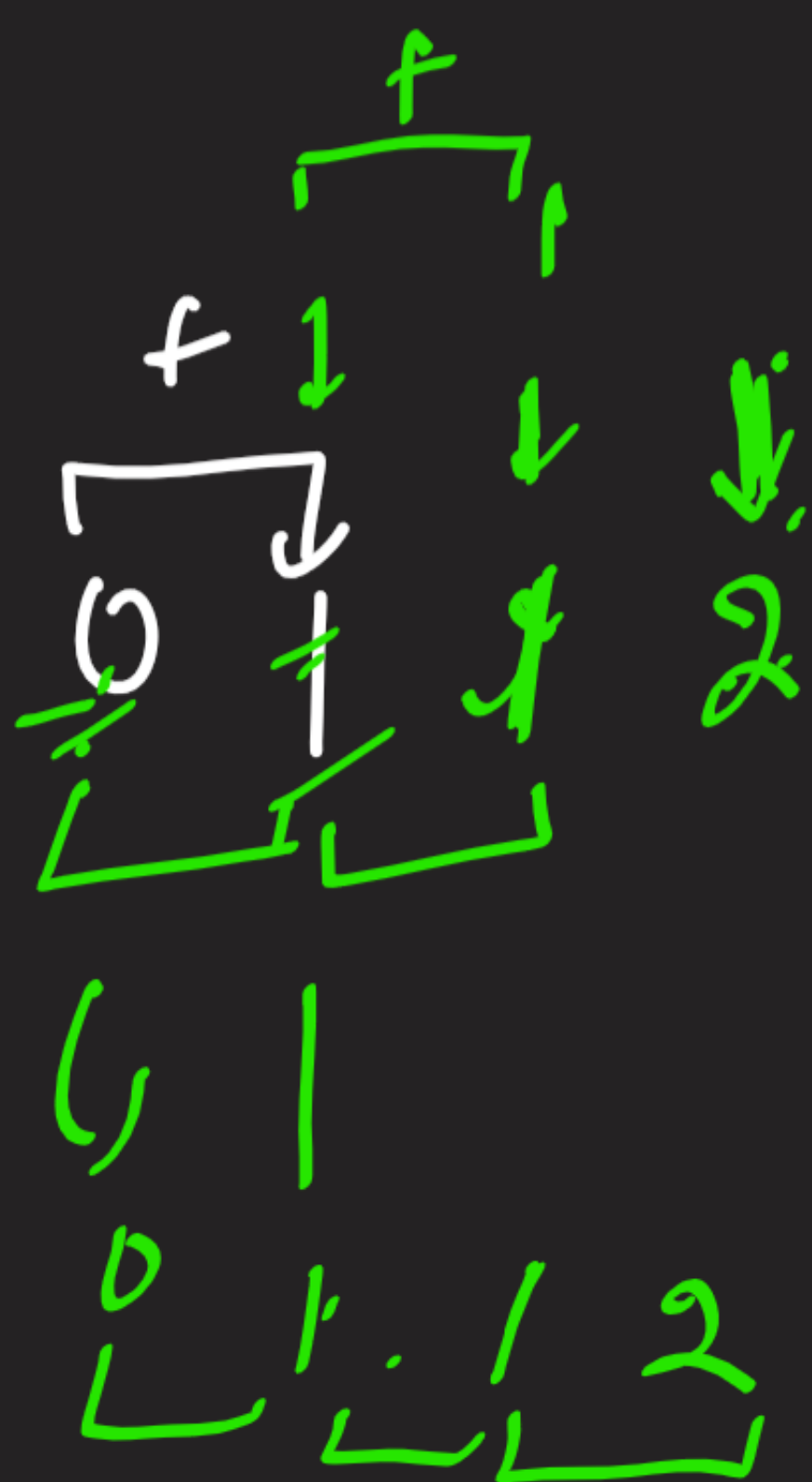
fib(1) = 1

fib(2) =

fib(1) +
fib(0)

fib(3) = fib(2) + fib(1)

fib(n) = fib(n-1) + fib(n-2)



5 + 8 = 13 21

$$\begin{aligned}
 \underline{\underline{\text{fib}(5)}} &= \underline{\underline{\text{fib}(4)}} + \underline{\underline{\text{fib}(3)}} \quad \text{--- } i_2 \quad = \quad 5 \\
 &\quad \swarrow \quad \searrow \\
 &\quad \underline{\underline{\text{fib}(3)}} + \underline{\underline{\text{fib}(2)}} \quad \quad \quad \underline{\underline{\text{fib}(2)}} + \underline{\underline{\text{fib}(1)}} \\
 &\quad \swarrow \quad \searrow \quad \quad \quad \swarrow \quad \searrow \\
 &\quad \underline{\underline{\text{fib}(2)}} + \underline{\underline{\text{fib}(1)}} \quad \quad \quad \underline{\underline{\text{fib}(1)}} + \underline{\underline{\text{fib}(0)}} \\
 &\quad \swarrow \quad \searrow \quad \quad \quad \swarrow \quad \searrow \\
 &\quad \underline{\underline{\text{fib}(1)}} + \underline{\underline{\text{fib}(0)}} \quad \quad \quad \underline{\underline{1}} + \underline{\underline{0}}
 \end{aligned}$$

Time complexity / space complexity
 Big O

$$1 + 2 + 3 + 4 + \dots + 100000000$$

$$T(n) \propto n$$

$$f(n) \propto \underline{n}$$

$$\underline{T(n)} = a\underline{n^2} + b$$

$$\boxed{O(n)}$$

Linear time complexity

$$y = \underline{mx} + c$$




```

for(int i=0; i<n; i++){
    for(int j=0; j<n; j++){
        cout << "hi";
    }
}

```

n time.

$i=0 \rightarrow n \text{ times}$
 $i=1 \rightarrow n \text{ times}$
 $i=2 \rightarrow n \text{ times}$
 \vdots
 $i=n-1 \rightarrow n \text{ times}$

$n \text{ times} + n \text{ times} + n \text{ times}$
 $\dots n \text{ times}$
 $n(n \text{ times})$

$T(n) \propto (n \times n)$ operation

$O(n^2) \rightarrow$ quadratic time comp.

$O(\log n) \rightarrow$
 $O(n \times \log n)$
 $\leftarrow \underline{O(1)} \rightarrow \text{constant time}$

$a = 10000$
 $b = 1 \rightarrow$
 $c = \frac{1+1}{2} \rightarrow$
 $= 2$

$1000000 + 1000000$ 3 step

$O(n!)$ very slow
 $O(n^3)$

$O(2^n)$ very slow.